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SURFACE DISTORTION IN FACE-CENTERED CUBIC SOLIDS

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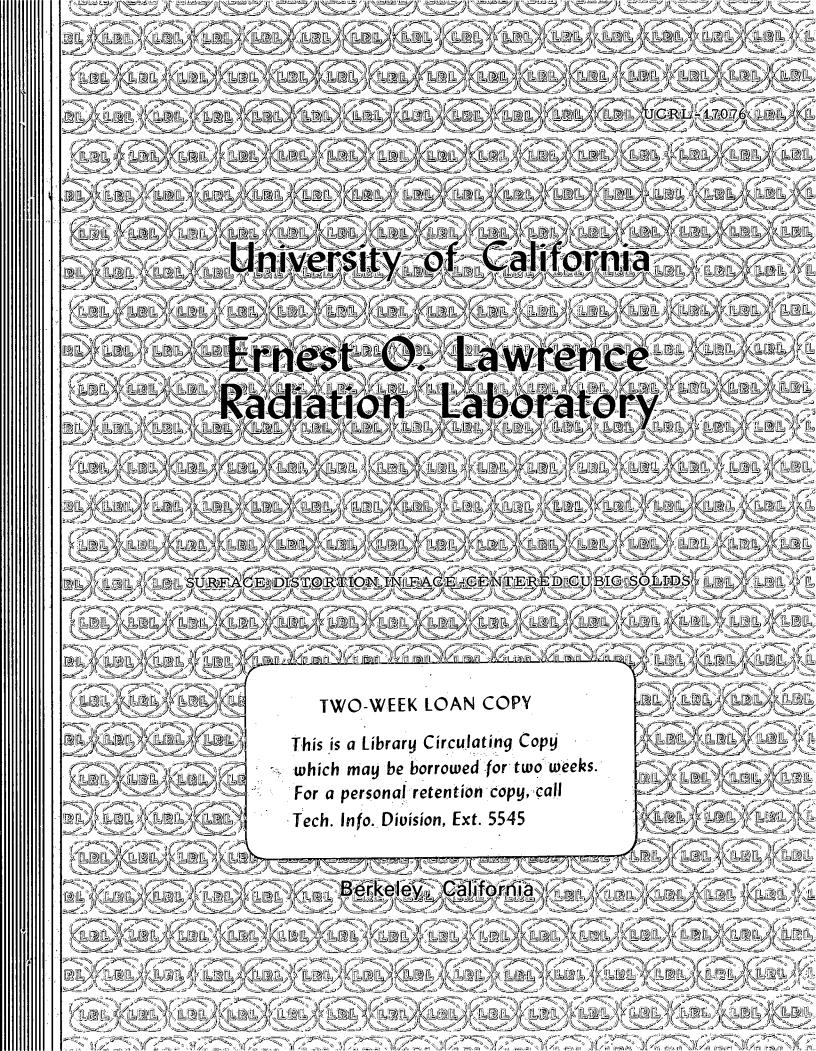
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August 1966



#### SURFACE DISTORTION IN FACE-CENTERED CUBIC SOLIDS

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Until now, experimental values have not been obtained for the displacement of the surface layers from the bulk of semi-infinite crystals; such information will probably soon be available from Low Energy Electron Diffraction (LEED) studies. It is desirable to have some theoretical estimation of the order of magnitude of the displacements.

Gazis and Wallis have shown that a one dimensional lattice with

D.G. Gazis and R. F. Wallis, Surf. Sci. 3, 19 (1964).

nearest and next-nearest neighbor interactions may exhibit a distortion of the lattice spacing at a free surface; the predicted distortion decreases exponentially with distance from the surface.

Shuttleworth has calculated the displacement of the first layer of

the (100) surface of argon and Alder, Vaisnys, and Jura have calculated

the displacements of the first five layers of the (100) surface of argon. Alder et al. found that the distortion decreased proportionally to the inverse cube of the distance from the surface.

The values of the coefficients in the Morse potential

$$\varphi(r) = D[e -2e(r-r_0) -2e(r-r_0)]$$

R. Shuttleworth, Proc. Roy. Soc. (London) A62, 167 (1949).

 $<sup>^3</sup>$  B.J. Alder, J.R. Vaisnys, and G. Jura, J. Phys. Chem. Solids, 11, 182 (1949).

were tabulated by Girifalco and Weizer 4 for six fcc metals, Ca, Ag, Al,

Pb, Cu, and Ni (Table 1). We have calculated the displacements,  $\delta_1$  (Fig. 1) of the first two surface layers of these metals for the (100), (110), and (111) surfaces. For comparison purposes we have also calculated the same displacements for argon using a Lennard-Jones 6-12 potential.  $\frac{5}{2}$ 

The surface energy, without allowing for distortion  $E_0$ , was calculated for each case considered by direct summation over a lattice of 2000 atoms. The surface energy was then minimized with respect to the displacements,  $\delta_i$ , by direct summation of the energy over a lattice of 360 atoms on a CDC 6600 computer.

The surface energies without relaxation,  $E_0$ , the displacements,  $\delta_i$ , and the changes in surface energy due to relaxation,  $\Delta E$ , are tabulated in Tables 2, 5, and 4 for the (100), (110), and (111) surfaces respectively. The displacements,  $\delta_i$ , are given in units of percentage of the normal bulk planar spacing. The values of Alder et al. are included in Table 2.

The results of Alder et al.  $^3$  are based on direct summation of the energy over a lattice of roughly forty thousand atoms and integration over the remainder of the lattice; our results are based on only 360 atoms. Comparison of Alder's results with ours shows that this small lattice yields good values of  $\delta_1$ ,  $\delta_2$  and  $\Delta E$ . Alder's work shows that consider that of the relaxation of only two surface layers gives good values of the surface energy.

L. A. Girifalco and V. G. Weizer, Phys. Rev. 114, 687 (1959).

<sup>&</sup>lt;sup>5</sup> T. Kihara, J. Phys. Soc. Japan, <u>3</u>, 265 (1948).

For all the materials considered, it was found that the (111) surface was the lowest energy surface and the (110) the highest; distortion
was largest for the (100) surface and smallest for the (111) surface.
Relaxations were found to alter the surface energy by at most 6% and
only slightly affected the ratios of the surface energies of the
various faces.

#### ACKNOWLEDGEMENTS

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Commission.

TABLE 1
Parameters of Morse Potential  $-2\alpha(\mathbf{r-r_0}) -\alpha(\mathbf{r-r_0})$   $\phi(\mathbf{r}) = \mathbf{D}[\mathbf{e} -2\mathbf{e}]$ 

Metal	$\alpha(\mathring{A}^{-1})$	r <sub>o</sub> (Å)	D(ev)
Pb	1.1836	3.733	.2348
Ag	1.3690	3.115	•3323
Ni	1.4199	2.780	.4205
Cu	1.3588	2.866	<b>.</b> 3429
Al	1,1646	3.253	.2703
Ca	80535	4.569	.1623

TABLE 2

The (100) Surface: Relaxations,  $\delta_i$ , are given as a percentage of the bul: (100) planar spacing; E is the unrelaxed (100) surface energy;

ΔE is the change in surface energy due to relaxation.

Solid	81(%)	***************************************	82(%)	E <sub>o</sub> (ev)	∆E(ev)
Ca	12.504		5 <b>.</b> 587	•99925	06556
Ag	6.456		1.259	1.30502	03755
Ale	10.972		2.963	1.49150	08410
Pb	5.542		•978	.85209	02011
Cu	9.669		2.433	1.72345	08319
Ni	9.121		2.232	2.02644	09119
Ar	2.604	,	.625	.039021	000355
Ar*	2.577		<b>.</b> 589	•03951	000349
					•

<sup>\*</sup> Obtained by Alder et al.3

TABLE 3

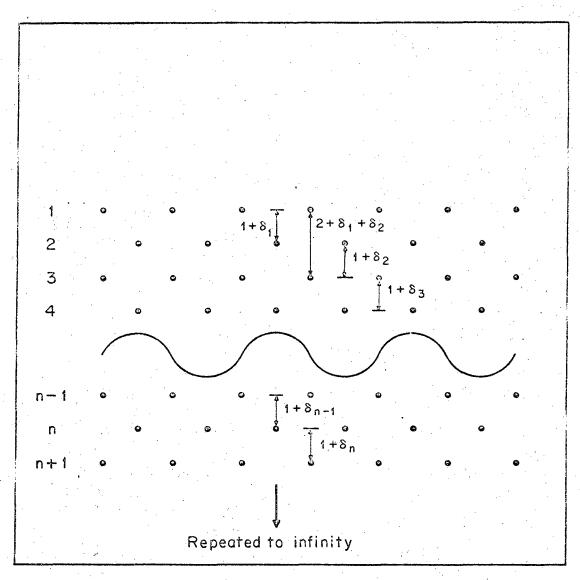
The (110) Surface: Relaxations,  $\delta_i$ , are given as a percentage of the bulk (110) planar spacing; E is the unrelaxed (110) surface energy;  $\Delta E$  is the change in surface energy due to relaxation.

Solid	δ <sub>1</sub> (%)	δ <sub>2</sub> (%)		E <sub>O</sub> (ev)	ΔE(ev)
Ca	9.621	2.628		1.45532	08664
Ag	4.783	.768	·	1.93619	04494
Al	8,362	2.099		2.18216	10898
Pb	4.075	•559		1.27073	02347
Cu	7.314	1.671		2.53181	10587
Ni	6.872	1.507		2.98250	11498
Ar	1.809	.366		.05779	000394

TABLE 4

The (lll) Surface: Relaxations,  $\delta_i$ , are given as a percentage of the bulk (lll) planar spacing; E is the unrelaxed (lll) surface energy;  $\Delta E$  is the change in surface energy due to relaxation.

Solid.	გ_(%)	8 <sub>2</sub> (%)	E <sub>o</sub> (ev)	ΔE(ev)
Ca	4.297	.899	.87518	<b></b> 02558
Ag	1.910	.225	1.11727	01087
Al	3 <b>.</b> 667	•709	1.30167	03111
Pb	1.580	•159	.72635	<b></b> 00539
Cu	3.142	•544	1.49844	02913
Ni	2.927	•490	1.75856	03114
Ar	.820	•190	.032520	000113



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Fig. 1 Schematic diagram of a semi-infinite crystal with displacements indicated

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