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**RESEARCH ARTICLE**



## **Towards assessing and improving the reliability of ultrashort echo time quantitative magnetization transfer (UTE‑qMT) MRI of cortical bone: In silico and ex vivo study**

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### **Abstract**

**Objective** To assess and improve the reliability of the ultrashort echo time quantitative magnetization transfer (UTE-qMT) modeling of the cortical bone.

**Materials and Methods** Simulation-based digital phantoms were created that mimic the UTE-qMT properties of cortical bones. A wide range of SNR from 25 to 200 was simulated by adding diferent levels of noise to the synthesized MT-weighted images to assess the efect of SNR on UTE-qMT ftting results. Tensor-based denoising algorithm was applied to improve the ftting results. These results from digital phantom studies were validated via ex vivo rat leg bone scans.

**Results** The selection of initial points for nonlinear ftting and the number of data points tested for qMT analysis have minimal efect on the ftting result. Magnetization exchange rate measurements are highly dependent on the SNR of raw images, which can be substantially improved with an appropriate denoising algorithm that gives similar fitting results from the raw images with an 8-fold higher SNR.

**Discussion** The digital phantom approach enables the assessment of the reliability of bone UTE-qMT ftting by providing the known ground truth. These fndings can be utilized for optimizing the data acquisition and analysis pipeline for UTEqMT imaging of cortical bones.

**Keywords** Ultrashort echo time (UTE) · Quantitative magnetization transfer (qMT) · MRI · Cortical bone · Digital phantom

### **Introduction**

Bone fractures are a growing public health issue posing a serious worldwide healthcare and economic burden [[1\]](#page-9-0). The risk of bone fractures is signifcantly increased in people with osteoporosis and diabetes, with the global prevalence of each disease estimated to be 19.7% [\[2](#page-9-1)] and 10.5% [[3](#page-9-2)],

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respectively. The most widely used fracture risk assessment is dual-energy X-ray absorptiometry (DXA)-based bone mineral density (BMD) measurement. However, clinical studies have reported that the BMD measurement only explains 30–50% of fractures [\[4](#page-9-3)[–6\]](#page-9-4). This limited sensitivity of BMD has motivated the need for more reliable fracture risk assessment tools that focus on not only the BMD but also other features and constituents of the bone, such as bone microstructure [\[7](#page-9-5)] and organic matrix [[8,](#page-9-6) [9\]](#page-9-7).

Magnetic resonance imaging (MRI) can not only provide anatomical images but also quantitative information on molecular components of tissues, leveraging its numerous contrast mechanisms. Quantitative magnetization transfer (qMT) imaging is one of the widely studied MRI methods for probing the macromolecular content and their properties in tissues  $[10-12]$  $[10-12]$  $[10-12]$ . While the usage of qMT imaging has been limited to soft tissues [\[13](#page-9-10)[–17](#page-9-11)] (e.g., brain, muscle, spinal cord and kidney) due to the very short  $T_2^*$  relaxation of hard tissues, combining qMT with an ultrashort echo time (UTE-qMT) readout sequence has enabled the application of qMT analysis to measure the macromolecular fraction (MMF) of cortical bones [\[18](#page-9-12)–[20\]](#page-9-13). Other qMT parameters such as magnetization exchange rates between the free water and macromolecular pools may also provide insights into the quality of the bone that accounts for fracture risk [[21,](#page-9-14) [22\]](#page-9-15).

Yet, even with the use of UTE readouts, it is unclear whether the signal-to-noise ratios (SNR) of bone MT-weighted images is sufficient for qMT modeling. From previous MT studies on other tissues, it is known that the measurements of exchange rates are highly affected by the SNR of the images, and to a much greater degree than the MMF measurements are [[23](#page-9-16), [24](#page-9-17)]. Such SNR-based reliability of qMT modeling has not been studied for UTEqMT imaging of bones. Towards the goal of developing qMT parameters as robust imaging markers that are correlated to bone fracture risk, a systematic assessment of the robustness and reliability of bone UTE-qMT must be performed (including the minimum SNR requirements) and strategies must be established for improving qMT parameter measurements.

In this study, we built a digital phantom through UTEqMT simulation that mimics the MR properties of cortical bones. Unlike in vivo or ex vivo qMT studies, the simulationbased approach allows one to examine whether the qMT ftting is robust and reliable as the ground truths are known.

Multiple series of MT-weighted images were synthesized to generate a wide range of SNR levels to examine the efect of SNR on qMT ftting results. The number of data points and the initial points for the qMT ftting were controlled to simulate how acquisition and analysis pipelines can afect the qMT ftting result. An ex vivo rat leg bone was scanned to validate the digital phantom results. For both digital phantom and ex vivo data, a tensor-based multidimensional denoising algorithm [\[25](#page-9-18)] was tested as a potential solution for the inherently low SNR of bone MRI and compared its performance with conventional Gaussian fltering.

### **Materials and methods**

#### **Digital phantom preparation**

Digital phantom preparation was performed using customwritten MATLAB code (MathWorks, Natick, MA). The overall fow of phantom preparation and analysis is summarized in Fig. [1](#page-2-0).

The binary spin bath (BSB) model was assumed for the digital phantom generation, modeling the cortical bone as a combination of two compartments, the free water pool (pool *a*) and the macromolecular pool (pool *b*) [[26](#page-9-19)]. The BSB model with a pulsed saturation scheme can be well



<span id="page-2-0"></span>**Fig. 1** Schematic fow of digital phantom preparation and qMT ftting. Twenty digital cortical bone chip images acquired at two or three saturation powers and five offset frequencies are simulated based on the UTE-qMT parameters measured from previous cortical bone studies. The Rician noise is added to the simulated bone chip images to generate the range of SNR levels from 25 to 200. The

simulated bone chip images with added noise are ftted back to the UTE-qMT model to measure the macromolecular fraction (MMF) and exchange rates  $(k_{ab}$  and  $k_{ba}$ ) by testing a different number of data points, selection of initial points of nonlinear ftting and applying a denoising algorithm

described by the rectangular pulse (RP) model by Sled and Pike [[27](#page-9-20)], which was further modifed for multiple acquisitions after a single MT preparation pulse [\[21](#page-9-14)]. This modifed RP model was used for both generating digital phantoms and subsequent ftting for testing diferent SNR levels, the number of data points, and the efect of initial points for nonlinear ftting.

The modified RP model is described by a total of seven parameters: The size of the free water pool  $(M_{0a})$ , longitudinal relaxation rates of the free water and macromolecular pool  $(R_{1a}$  and  $R_{1b}$ ), exchange rate from free water to macromolecular pool  $(k_{ab})$ , MMF (defined as  $M_{0b}/(M_{0a} + M_{0b})$ , T<sub>2</sub> of free water and macromolecular pools  $(T_{2a}$  and  $T_{2b}$ ). As shown in previous studies,  $R_{1b}$  can be fixed to  $1 \text{ s}^{-1}$  [\[26](#page-9-19), [28–](#page-9-21)[30\]](#page-10-0).  $R_{1a}$  can be determined by other parameters and observed  $T_1$  (e.g.,  $T_{1obs}=1/R_{1obs}$ ):

$$
R_{1a} = R_{1obs} - \frac{k_{ab}(R_{1b} - R_{1obs})}{R_{1b} - R_{1obs} + \frac{k_{ab}(1 - MMF)}{MMF}}
$$

Thus, with the  $R_{1obs}$  measured, a total of five parameters can be determined through ftting. The exchange rate from the macromolecular pool to the free water pool  $(k_{ba})$  can be determined as  $k_{ab} \frac{1-\tilde{M}MF}{MMF}$ 

 $\sum_{i=1}^{N}$  The input qMT parameters for generating digital phantoms were chosen from previous studies on UTEqMT imaging of cortical bones  $[21, 31]$  $[21, 31]$  $[21, 31]$  (MMF=30–60%,  $k_{ab} = 10-60 \text{ s}^{-1}$ ,  $T_{1obs} = 220-280 \text{ ms}$ ,  $T_{2a} = 0.7-1.0 \text{ ms}$ ,  $T_{2b}$ =fixed to 15 µs [[32](#page-10-2)]). Twenty combinations of these parameters were used for simulating diferent conditions of cortical bones. For each condition, 324 qMT spectra were simulated to create a digital bone chip with the size of  $18 \times 18$  voxels. Three MT saturation powers (3SP, flip angle =  $400^\circ$ ,  $800^\circ$ ,  $1200^\circ$ ) and five offset frequencies (2, 5, 10, 20, 50 kHz) were used to generate qMT spectra. To simulate diferent levels of SNR, Rician noise with zero mean and diferent levels of standard deviation were added to the images so that the SNR of the image at the lowest saturation power  $(400^{\circ})$  and the largest offset frequency (50 kHz) ranges from 25 to 200. SNR was calculated as the mean signal intensity of digital phantoms divided by the standard deviation of the Rician noise used for noise generation. All the SNRs reported in this study are based on the image simulated or acquired at the lowest saturation power and the largest offset frequency unless indicated otherwise.

#### **Digital phantom analysis**

The prepared digital phantom images were ftted back into the UTE-qMT model to quantify the MMF and exchange rates  $(k_{ab}$  and  $k_{ba}$ ) and observe whether the results matched the input parameters used for generating

the phantoms. The non-linear ftting was performed using the 'lsqcurveft' function in MATLAB with the default Trust-region ftting algorithm.

To assess the effect of the number of saturation powers and offset frequencies, we tested the full set of MT spectra (3 saturation powers and 5 offset frequencies, 15 data points) and the MT spectra with only 2 saturation powers (2SP, 800˚ dataset excluded, 10 data points). For this assessment, the initial point of non-linear ftting was fxed to the ground truth of each phantom so that only the efect of the number of data points can be assessed. The effect of the initial point of the nonlinear fitting process was also tested by using the initial point of either the ground truth of each phantom or the fxed one  $(MMF=50\%, k_{ab}=25 \text{ s}^{-1}, T_{1obs}=240 \text{ ms}, T_{2a}=0.8 \text{ ms}),$ near the midpoint of the range of parameters tested. All these assessments were done at diferent SNR levels.

A denoising algorithm was tested on the digital phantoms to examine whether qMT parameter fitting results improved. Among numerous potential algorithms, we tested a recently developed tensor Marchenko-Pastur distribution Principal Component Analysis (tMPPCA) method [[25\]](#page-9-18). The digital phantom image with the SNR of 50 was denoised by tMPPCA with a window size of  $3 \times 3 \times 3$  [\[33](#page-10-3)]. The Gaussian filtering with the kernel standard deviation fxed to 1 was also tested for comparison.

#### **Ex vivo** *rat bone MR image acquisition and analysis*

An ex vivo rat leg bone was scanned on a 3 T scanner (Bruker, Billerica, MA) with a 1 cm loop coil to confrm the digital phantom results. The bone marrow of the bone was removed and placed in Fomblin (Ausimont, Thorofare, NJ) for susceptibility-matching purposes. MT-weighted UTE images were acquired at three saturation powers  $(500^{\circ}, 1000^{\circ}, 1500^{\circ})$  and five offset frequencies  $(2, 5, 1000^{\circ})$ 10, 20, 50, kHz). Readout parameters are as follows:  $TR/TE = 86/0.026$  ms, number of spokes per MT saturation = 13, inter-spoke  $TR = 5$  ms, flip angle = 10<sup>°</sup>, field-of-view  $(FOV) = 10$  mm  $\times 10$  mm  $\times 80$  mm, matrix =  $84 \times 84 \times 84$ , receiver bandwidth = 100 kHz. The MT-weighted image acquisition was repeated 64 times to manually control the number of averages (NA). NA of 1, 4, 8, 16, 32, and 64 were tested to match with the SNR of 25–200 used for digital phantom simulation. For the  $qMT$  fitting process, the  $T_{1obs}$  was assumed to be 250 ms [[31](#page-10-1), [34](#page-10-4)–[38](#page-10-5)]. The effect of denoising on MT parameter ftting was also tested using the same tMPPCA denoising algorithm. All the analysis was performed twice, once with the full dataset (3SP) and once with 2 saturation powers (2SP, 1000˚ dataset excluded).

### **Results**

Digital phantom simulation shows similar MMF fitting results from MT spectra with 2SP and 3SP datasets (Fig. [2A](#page-4-0)), whereas the exchange rate measurements are slightly improved on the 3SP dataset. The MMF measurement is relatively robust throughout the SNR levels tested ranging from  $58.8 \pm 27.4\%$  (2SP) and  $57.0 \pm 25.7\%$  (3SP) at SNR of 25 to  $51.8 \pm 6.3\%$  (2SP) and  $51.0 \pm 5.1\%$  (3SP) at SNR of 200 (Fig. [2B](#page-4-0)). The exchange rate measurements are unstable in the lower SNR levels and become comparable to the ground truth at the SNR of 150 or above. These trends are also shown in the parameter maps at diferent SNR levels shown in Fig. [2C](#page-4-0).

Similar trends are seen from the assessment of the initial point efect (Fig. [3](#page-5-0)). Overall, the choice of initial points did not signifcantly afect the ftting results, while the MMF measurement is more stable than the exchange rate measurements (Fig. [3A](#page-5-0)). Exchange rate measurements are reliable at the SNR of 150 or above, regardless of the choice of the initial point for nonlinear ftting (Fig. [3](#page-5-0)B). Still, the MMF measurement shows that the initial point set to the ground truth gives a more accurate result than the fxed initial point for certain phantoms at high SNR

levels. This better measurement of MMF is also translated to a marginally improved measurement of  $k_{ba}$  in certain phantoms (Fig. [3\)](#page-5-0).

The improvement of qMT ftting via denoising was also observed (Fig. [4\)](#page-6-0). Although following the patterns in the ground truth, the exchange rate maps are highly noisy due to the unstable ftting without denoising. Both tMPPCA and Gaussian denoising of the raw digital phantom images generate the parameter maps that are closer to the ground truths, albeit with some residual regional variations in the parameter maps. Interestingly, the tMPPCA algorithm showed a more accurate measurement of high MMF values than the Gaussian fltering.

To validate the digital phantom results, ex vivo rat bones were scanned, and the improvement of qMT ftting was observed along with increasing the number of averages (Fig. [5](#page-7-0)). The SNR of raw images (saturation power=500˚, offset frequency = 50 kHz) increased from 37.4 ( $NA = 1$ ) to  $306.4$  (NA = 64), matching with the SNR levels tested in the digital phantom simulations. Denoising via the tMPPCA method was tested on the  $NA = 1$  dataset, which showed substantial improvement of SNR (131.6) and the subsequent qMT ftting that generated a result comparable to the one from the  $NA = 64$  dataset with preserved spatial resolution (Fig. [5\)](#page-7-0). The Gaussian fltering also showed improvement





SNR

<span id="page-4-0"></span>Fig. 2 The effect of the number of data points and signal-to-noise ratio (SNR) on cortical bone UTE-qMT ftting. The UTE-qMT parameters acquired via ftting 2 saturation powers (400˚ and 1200˚, 2SP) and 3 saturation powers (400˚, 800˚ and 1200˚, 3SP) are compared. **A** UTE-qMT parameter maps generated from the dataset with SNR of 100 with the initial point chosen as the ground truth of each phantom. **B** The exchange rates  $(k_{ab}$  and  $k_{ab})$  show the fitting results are more stable and closer to the ground truth upon using the 3SP dataset. Macromolecular fraction (MMF) measurements are stable for

both 2SP and 3SP datasets. The 2SP dataset shows higher spatial variation of parameter ftting represented as larger standard deviations of the measurements. The measurements are from the phantom with the white box shown in A.  $k_{ab}$  and  $k_{ba}$  measurements are only shown at SNR of 75 or above due to abnormally large values from unstable ftting. **C** UTE-qMT parameters maps of the phantom analyzed (white box in A) at diferent SNR levels (25–200) and the maps of ground truth parameters





<span id="page-5-0"></span>**Fig. 3** The efect of the choice of initial point of nonlinear ftting of the UTE-qMT model. **A** UTE-qMT parameter maps from digital phantoms with three saturation powers and an SNR of 100. Parameter maps in the frst two columns (Fitting) are the ftting results from using the initial point of either the ground truth of each phantom (Ground Truth) or the fxed values (parameters used for the phantom

in parameter ftting, but substantial spatial blurring is also observed as expected.

The quantitative measurements of qMT parameters from ex vivo scans also show the robust measurement MMF across all NAs tested, whereas the exchange rate measurements are not reliable at NA of 1 (Fig. [6](#page-7-1)). Compared to digital phantoms, however, low SNR ex vivo scans ( $NA = 1$ , 4, 8) show much more comparable results to those from high SNR scans ( $NA = 32$  and 64). The tMPPCA denoising of the dataset with NA of 1 substantially improved the quality of ftting compared to the original image. Despite the overestimated MMF  $(43.4 \pm 7.2 \text{ vs. } 40.4 \pm 5.2\%; \text{ Fig. 6A})$  $(43.4 \pm 7.2 \text{ vs. } 40.4 \pm 5.2\%; \text{ Fig. 6A})$  $(43.4 \pm 7.2 \text{ vs. } 40.4 \pm 5.2\%; \text{ Fig. 6A})$ and underestimated exchange rates  $(k_{ab}: 20.7 \pm 12.8 \text{ s}^{-1} \text{ vs.})$  $22.6 \pm 9.1$ ;  $k_{ba}$ :  $28.2 \pm 21.2$  s<sup>-1</sup> vs  $34.2 \pm 18.6$  s<sup>-1</sup>; Fig. [6B](#page-7-1), [C\)](#page-7-1), the results from the denoised  $NA = 1$  dataset are comparable to those from the  $NA = 64$  dataset. The use of the 3SP dataset signifcantly reduced the variation of all the UTEqMT parameter measurements in the given ROI compared to the results from the 2SP dataset.

### **Discussion**

Here, we systematically assessed the SNR requirements and how the ftting process afects the UTE-qMT imaging of bone. Similar to qMT imaging of other tissues, the MMF

with the red box; Fixed). Ground truth maps are also included in the right-most column for comparison. **B** The macromolecular fraction (MMF) and exchange rate  $(k_{ab}$  and  $k_{ba}$ ) measurements from 4 phantoms indicated in the white boxes shown in A.  $k_{ab}$  and  $k_{ba}$  measurements are only shown at SNR of 75 or above due to abnormally large values from unstable ftting

measurement was robust across a range of SNR levels, whereas exchange rate measurements became accurate when the SNR reached around 150 or above. The UTEqMT ftting process also turned out to be robust against the selection of the initial point of the nonlinear ftting process, and the 2SP dataset generated comparable results as those from 3SP datasets. The denoising algorithm tested in this study substantially improved the ftting accuracy. These results were also reproduced in ex vivo rat leg bone scans, with relatively more robust MMF measurements and substantial improvement of qMT measurements after denoising.

The advantage of the digital phantom approach demonstrated in this study is the known ground truth. Although the quality of qMT ftting is usually measured by the goodness-of-ft, whether the ground truth value is obtained through the ftting cannot be known by actual scans, unless followed by validation studies such as histology or biochemical assays from tissue samples. By knowing the ground truth values, the digital phantom simulation approach allows examining whether the qMT ftting provides correct results and permits subsequent optimization of the data acquisition and analysis pipeline. Optimizing the qMT ftting pipeline using the known ground truth is also expected to facilitate the development of more advanced techniques for qMT ftting such as neural network-based approaches by



<span id="page-6-0"></span>**Fig. 4** tMPPCA denoising improves the UTE-qMT ftting of simulated digital phantoms. The simulated digital phantom with three saturation powers and an SNR of 50 was tested. The initial point of ftting was selected as the ground truth of each phantom. Both tMP-PCA and Gaussian denoising have significantly improved the UTE-

providing more accurate and refned training datasets [\[39,](#page-10-6) [40](#page-10-7)].

Comparing the fitting results with the ground truth showed that the exchange rate measurements are highly SNR dependent whereas MMF measurements are more robust even in the low SNR regime, regardless of the number of data points and initial points tested. The unstable ftting of exchange rates at low SNR has been previously shown from qMT studies on other soft tissues [[23](#page-9-16), [41](#page-10-8)]. The qMT study on human patellar cartilage reported that the percentage change of the exchange rate becomes lower than 1% only after the SNR of an image becomes 75 or higher [[23](#page-9-16)]. Our digital phantom-based analysis shows that at least an SNR of 100–150 is needed for reasonable voxel-based measurements of exchange rates, whereas MMF measurements are acceptable even with an SNR of around 50. The unstable ftting of exchange rates at SNR of 50 or lower generated unrealistically large values  $(k_{ab} > 10^3$  and  $k_{ba}$ >5 × 10<sup>3</sup> s<sup>-1</sup>) and variations that had to be excluded

qMT parameter ftting with less noise in the parameter map, and the results are more comparable to the ground truth. The white arrows indicate the diference in MMF measurement between tMPPCA and Gaussian denoising

from the measurements (Figs. [2B](#page-4-0) and [3](#page-5-0)B). The instability of exchange rate measurements may be alleviated by setting up narrower but still realistic boundary conditions during the ftting process. Still, considering the inherently low SNR of actual bone MR images acquired in a clinically feasible scan time, only a region-of-interest (ROI)-based analysis seems applicable for the exchange rate measurements unless certain strategies to improve the SNR are employed, such as lowpass fltering and other denoising algorithms.

As a potential method of improving the SNR and corresponding qMT ftting results, we tested the tMPPCA algorithm on both digital phantoms and rat bone data and compared it with conventional Gaussian filtering. The tMPPCA is designed for denoising multidimensional MRI data by leveraging the redundancy in the extra dimensions [[25](#page-9-18)]. This algorithm has demonstrated substantial improvement of SNR of multi-echo images, diffusion-weighted images, and  $T_1$ -weighted images, as well as subsequent parameter ftting results [[25](#page-9-18), [33](#page-10-3)]. We



<span id="page-7-0"></span>**Fig. 5** Ex vivo rat leg bone scans with diferent degrees of averaging. The number of averages (NA) was controlled from 1 to 64 to cover the SNR range of 25–200 simulated for digital phantoms. The SNR levels are indicated in parentheses. Denoising via the tMPPCA algorithm and Gaussian flter were also tested on the NA1 dataset  $(NA1 + dn)$ . The macromolecular fraction  $(MMF)$  fitting is stable except for the one from the NA1 dataset, whereas the exchange rate

maps  $(k_{ab}$  and  $k_{ba}$ ) are steadily improving with the increasing NA. The tMPPCA-denoised NA1 dataset shows comparable results with the NA32 and NA64 datasets. The denoising with the Gaussian flter also shows improved exchange rate measurement along with a signifcant blurring in both raw image and parametric maps. The UTEqMT parameter maps shown here are generated using the full dataset acquired (three saturation powers)



are shown

<span id="page-7-1"></span>**Fig. 6** Ex vivo rat bone scan measurements. The UTE-qMT ftting results shown in Fig. [5](#page-7-0) were measured with a region of interest covering the entire rat bone. Macromolecular fraction (MMF) measurements show stable measurements across the range of number of averages (NA) used, regardless of using 2 saturation powers (2SP) and 3 saturation powers (3SP). The measurement of exchange rates  $(k_{ab}$  and

denoised low SNR dataset  $(NA=1)$ . Compared to Gaussian fltering, the tMPPCA denoising did not show any spatial blurring. These results indicate that even with the low SNR raw data, the exchange rates can also be reliably measured with a proper denoising strategy.

While MMF alone can be a great imaging marker of the content of organic matrix in the bone, exchange rates can also be valuable markers of macromolecule conditions in the bone. With the growing evidence that BMD is not sufficient to examine the bone fracture risk, bone quality is drawing

 $k_{\rm ba}$ ) is more NA-dependent than MMF measurements. The variation of exchange rate measurements is also signifcantly reduced when using the 3SP dataset. Due to signifcant spatial blurring upon Gaussian denoising, only the results from tMPPCA denoising  $(NA1 + dn)$ 

hypothesized that this algorithm would also bring high SNR gain to qMT datasets as qMT data are inherently multidimensional due to repeated acquisitions at diferent saturation powers and offset frequencies. The digital phantom simulation showed that tMPPCA denoising enables accurate voxel-wise measurement of exchange rates even with an SNR of 50, similar to the results from Gaussian fltering. This result was validated by applying the same algorithm to the rat bone dataset, shown by the similar ftting results between the raw high SNR dataset  $(NA=64)$  and the more attention as another determinant of bone fracture risk [[42](#page-10-9)[–44\]](#page-10-10). For instance, non-enzymatic crosslinking of collagen fbrils via advanced glycation end products in the cortical bone is considered to be a key contributor to the increased fracture risk in type 2 diabetes patients despite the preserved or even elevated BMD measurements [[45](#page-10-11)[–47](#page-10-12)]. Since the exchange rate measurements were demonstrated to be altered upon crosslinking collagens in cornea and cartilage, as well as other polymers [[48–](#page-10-13)[50\]](#page-10-14), robust measurements of exchange rates via UTE-qMT modeling can potentially be a valuable marker of assessing the bone quality and fracture risk.

A typical limitation of qMT parameter measurements via the BSB model is parameter correlation. Previous studies have shown that MMF and  $k_{ab}$  measurements can be coupled, rather than independent [\[24,](#page-9-17) [51](#page-10-15)]. This parameter coupling was also observed in this study, as shown in the scatter plot of voxel-wise measurement of MMF and  $k_{ab}$  (Figure S1). An anisotropic distribution of MMF and  $k_{ab}$  measurements was observed throughout the SNR levels tested, indicating that these parameter measurements are not independent. The overall trend of MMF and  $k_{ab}$  measurement shows the tendency to compensate for the underestimation of MMF with the overestimation of  $k_{ab}$  and vice versa, which is a previously reported phenomenon [[27](#page-9-20)]. Other qMT parameter estimation approaches that do not depend on nonlinear ftting, such as the dictionary-matching method [[52](#page-10-16)], may alleviate the issue.

In this study, we only tested the effect of SNR, the number of data points, and the selection of initial points for the ftting, but other parameters involved in the image acquisition and analysis procedure can also be tested using the digital phantom approach in the future. The number and selection of offset frequencies and saturation powers can be further tested to identify the combination of these parameters that gives the best ftting accuracy with the minimum data acquisition to reduce the scan time. Testing for the effect of  $B_1$  inhomogeneity and  $T_1$  relaxation time is another validation test that may be performed through digital phantoms. In this study, we assumed a perfect  $B_1$  homogeneity and  $T_1$  relaxation time measurement. For in vivo UTE-qMT scans of cortical bone, however, the accurate measurements of  $B_1$  inhomogeneity and  $T_1$  relaxation are challenging due to the short  $T_2^*$  of the cortical bone [[34](#page-10-4)]. Examining the tolerance of  $B_1$  and  $T_1$ errors during the qMT ftting will give a better assessment of the reliability of the UTE-qMT imaging. In that regard, the ex vivo rat bone scan results can be improved with the actual measurement of  $B_1$  inhomogeneity and  $T_1$ . These studies should also be validated through in vivo scans in the future. Due to the higher body temperature and other tissues surrounding the cortical bone (e.g., bone marrow and muscle), the SNR of in vivo bone scan is expected to be lower than the ex vivo scans [[53](#page-10-17)]. The digital phantom approach taken in this study may also be biased due to the discrepancy between the in vivo conditions and the model chosen for generating digital phantoms and subsequent ftting. Whether the fndings through the digital phantom demonstrated in this study can be applied to in vivo scans should be further examined. Finally, we chose the tMPPCA algorithm with a fxed window size for denoising. Other denoising algorithms, as well as image fltering and ROIaveraging with diferent numbers of voxels within an ROI, can also be tested for establishing a robust UTE-qMT analysis pipeline.

### **Conclusion**

Here, we demonstrated the usage of digital phantom simulation to assess the reliability of qMT measurements. Similar to qMT imaging of other tissues, cortical bone digital phantoms showed robust MMF measurements whereas exchange rate measurements were unstable in low SNR levels. The number of data points and the selection of initial points tested in this study yielded negligible effects on the UTE-qMT ftting results. Denoising via the tMPPCA method showed substantial improvement in qMT ftting in both simulation and ex vivo scans, supporting the feasibility of reliable voxel-wise measurements of bone UTE-qMT parameters.

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**Data availability** The data supporting the reported fndings and the code used for analyzing the data are available from the corresponding authors upon reasonable request.

#### **Declarations**

**Conflict of interest** There are no conficts of interest to disclose.

**Ethical standard** All experimental procedures are in accordance with the ethical standards of the institutional research committee.

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