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Diagnosis and Communication in Distributed Systems

Raja Sengupta

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Diagnosis and Communication in Distributed Systems

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Abstract

This paper discusses diagnosis problems in distributed systems within the context of a language-theoretic discrete event formalism. A distributed system is seen as a system with multiple spatially separated sites with each site having a diagnoser that observes some of the events generated by the system and diagnoses the faults associated with the site. We allow the diagnosers to share information by sending messages to each other. Distributed systems are classified as being centrally, decentrally, and independently diagnosable. We characterise the class of distributed systems for which there exists a centralized diagnoser but there exists no inter-diagnoser messaging scheme that can replicate the information available to a centralized diagnoser. Plant properties that are necessary and sufficient for the three kinds of diagnosability are derived. The formulation and results are motivated by a discussion on the diagnosis of failures in a wireless LAN used to support the real-time operation of automated vehicles.

1 Introduction

We are interested in understanding the design of diagnostics for distributed systems. This theoretical work is motivated by our experience with the design of distributed diagnostics for coordinating vehicle systems [5, 10] and wireless local area networks [3, 6]. These systems are comprised of spatially separated sites (e.g., vehicles or radios) of semi-autonomous activity. Since these systems operate under distributed control, it is desirable that each site be able to diagnose (detect and isolate) its own failures. In general, we find that a site requires information from other sites to isolate some of its failures. This sharing of information is realized through protocols executed over a communication network. We seek insight into the role of communication in diagnostic design for distributed systems.

The relevant literature is as follows. Fault detection in distributed discrete event systems has been investigated in the context of Petri Net models with applications to telecommunication

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networks in [2] and [1]. Similar problems have been studied in the context of template languages for fault monitoring in [9]. Within the context of automata and language-theoretic models, centralized diagnostic design for discrete event systems was investigated in [12, 13]. The results presented in this paper are also in the context of a language-theoretic discrete event formalism and generalize some of the results in [12].

The system for which diagnostics is to be designed is called the *plant*. Diagnostic design for a distributed plant entails the design of several communicating diagnostic processes (hereafter *diagnosers*). Each diagnoser observes some of the events generated by the plant. Failure events are assumed to be unobservable to all the diagnosers. Each diagnoser tracks the plant by observing some subsequence of the event sequence executed by the plant, communicates with other diagnosers through the generation and reception of message events, infers the normal or failed status of the system using its observations and communications, isolates the particular failures, if any, that have occurred, and generates failure messages reporting the isolated failures to the controllers. Figure 1 shows this architecture. The diagnosers (e.g., D_1, D_2, D_3 in figure 1) are assumed to communicate over a communication system distinct from the plant. A distributed plant for which there exist diagnosers that are able to diagnose the failures at the respective sites, is said to be a *diagnosable* system. This paper formalizes the distinction between diagnosable and non-diagnosable systems.

We shall concern ourselves with three kinds of diagnosability, i.e., a distributed system may be *independently diagnosable*, *decentrally diagnosable*, and *centrally diagnosable*. We think of a distributed system as being independently diagnosable if for every site, the failures of interest to the site can be diagnosed using local information alone, i.e., without information from other sites. A distributed system is decentrally diagnosable if there exists an inter-diagnoser communication scheme providing remote information that together with local observation will provide each site with enough information to diagnose the failures of interest. Finally, we think of a distributed system as being centrally diagnosable if all the failures at all sites can be diagnosed by a central observer observing instantaneously any event observed at any site. Our intuition suggests that independently diagnosable systems should be decentrally diagnosable and decentrally diagnosable systems should be centrally diagnosable. However, the converse may not be true. We seek to understand when centrally diagnosable systems fail to be decentrally diagnosable, i.e., why no inter-diagnoser messaging scheme exists even when the global observation structure is rich enough to support diagnosis.

The plant is formalized as a discrete event system that in general *concurrently*, *spontaneously* and *asynchronously* executes multiple processes. However, the representation of concurrency is restricted to an interleaved semantics. The behavior of a single process is an event sequence. The behavior of a collection of processes is also an event sequence. Accordingly, the set of possible behaviors of the plant is a language L , $\subseteq \Sigma_p^*$, where Σ_p is a finite alphabet. We assume the diagnosers have no control capabilities with respect to the plant. For example, in the language of supervisory control ([11]), all plant events appear uncontrollable to the diagnosers. The diagnosers may not force, disable or delay the execution of plant events. Diagnosers communicate by synchronizing on message events. We think of these messages as being sent over a faultless communication system distinct from the plant. Therefore the generation of message and plant events is completely asynchronous. No assumptions are made to bound delays in the inter-diagnoser communication system. Therefore in the interleaved semantics, arbitrarily many plant events may precede or succeed a diagnoser message event.

The structure of the paper is as follows. Section 2 formulates the problem mathematically. Section 3 presents a motivating example. Section 4 presents results characterising diagnosable and non-diagnosable systems. Section 5 summarizes the results of the paper.

2 Problem Formulation

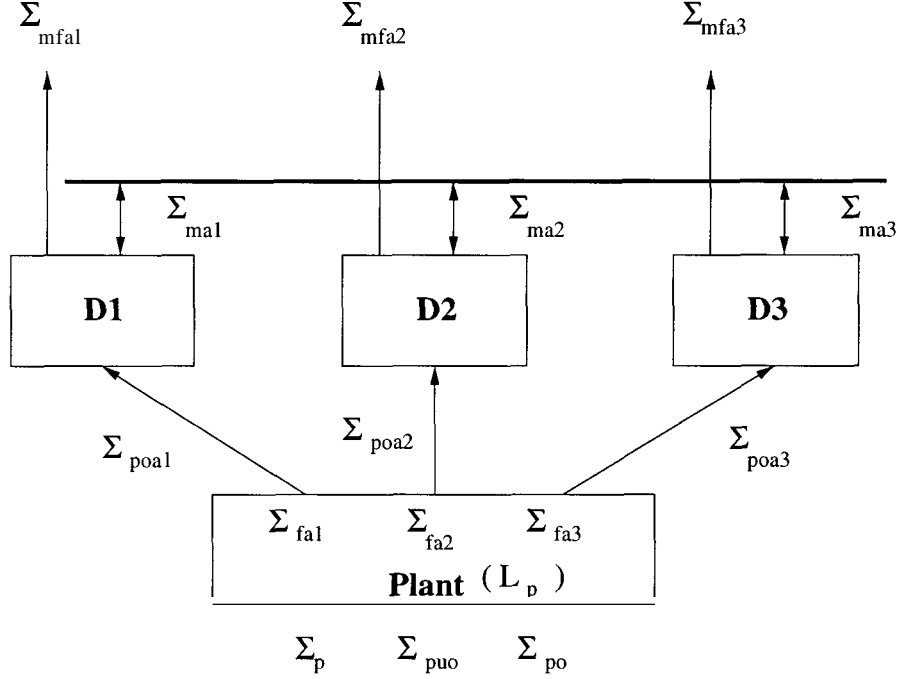


Figure 1: Decentralized Diagnostic System Architecture

In this section we define the entities in figure 1, and the three kinds of diagnosability.

As stated in the introduction, the plant is modeled as a language L , that lies in the kleene closure Σ_p^* , of a finite alphabet Σ_p . $\mathbf{A} = \{1, \dots, |\mathcal{A}|\}$ is an index set of sites, $|\mathcal{A}|$ is the cardinality of the set \mathbf{A} and the number of sites, $\Sigma_{poi} \subseteq \Sigma_p$, is the set of plant events observed at site i , and $\Sigma_{fi} \subseteq \Sigma_p$, is the set of plant failure events that should be diagnosed by site i . Let $\bigcup_{i=1}^{|\mathcal{A}|} \Sigma_{poi} = \Sigma_{po}$ and $\bigcup_{i=1}^{|\mathcal{A}|} \Sigma_{fi} = \Sigma_f$ be respectively the set of all observable and failure events in the plant. It is assumed that

$$\Sigma_f \cup \Sigma_{po} = \mathbf{0},$$

i.e., all failures are unobservable to all sites. We assume that L_p is prefix-closed and live. $\Sigma_{puo} = \Sigma_p - \Sigma_{po}$, denotes the set of unobservable plant events.

The task of each diagnoser is to process observations and generate failure messages that isolate the failures that have occurred for the benefit of fault management control. Let Σ_{mfi} denote the set of failure messages generated by site i and $\Sigma_{mf} = \bigcup_{i=1}^{|\mathcal{A}|} \Sigma_{mfi}$ be the set of all failure messages. Without loss of generality we pick Σ_{mf} to be any set of symbols, disjoint from all the other alphabets, that can be put in one-to-one correspondence with Σ_f . Let $\theta : \Sigma_f \rightarrow \Sigma_{mf}$ be a bijection. Then $\theta[\Sigma_{fi}] = \Sigma_{mfi}$.

We let Σ_{mi} denote the set of inter-diagnoser communication messages generated by site i . It is assumed that the Σ_{mi} are pairwise disjoint and $\Sigma_m = \biguplus_{i=1}^{|\mathcal{A}|} \Sigma_{mi}$, is disjoint from Σ_p and Σ_{mf} . The alphabet $\Sigma = \Sigma_p \uplus \Sigma_m \uplus \Sigma_{mf}$, is the set of all events generated by the plant and the diagnosers.

The triple $(L_p, \{\Sigma_{poi}\}_{i \in \mathcal{A}}, \{\Sigma_{fi}\}_{i \in \mathcal{A}})$ specifies the plant, the decentralized observation structure, and the failures to be diagnosed by each diagnoser. Since the concurrent operation of

the plant and diagnosers is represented in an interleaved semantics, their combined behavior is an event trace in Σ^* . Let $L \subseteq \Sigma^*$ denote the set of all possible interleaved behaviors of the plant and diagnosers. Thus L specifies a design, i.e., the generation of inter-diagnoser communication messages, and the generation of failure messages by the diagnosers. We will refer to L as the designed language. Our objective is to design \mathbf{L} and the associated $\{\Sigma_{mi}\}_{i \in \mathcal{A}}$ so that the diagnosers will generate failure messages when failures have occurred and not generate such messages when failures have not occurred.

2.1 Admissible Designs

We require that diagnosers not force, disable, or delay the generation of plant events. We will also require that designs be causal, i.e., the messages generated by a diagnoser should be a function of its observations and communications. Designs having these properties are said to be admissible and formalized as follows. Let P_A denotes the projection of a trace in Σ^* onto A^* , for an alphabet $A \subseteq \Sigma$.

Definition 1 L is an admissible design iff

1. \mathbf{L} is prefix-closed.
2. L is plant consistent, i.e., $L \subseteq \Sigma^*$, $P_{\Sigma_p}(L) = L$, $(\forall w \in \mathbf{L}, P_{\Sigma_p}(w)\sigma \in L, \Rightarrow w\sigma \in L)$.
3. L is causal, i.e., $\forall i \in \mathbf{d}, \mathbf{a} \in \Sigma_{mf_i} \cup \Sigma_{mi}, u, v \in L$,

$$(u\sigma \in L) \wedge (P_{\Sigma_{oi}}(u) = P_{\Sigma_{oi}}(v)) \Rightarrow v\sigma \in L.$$

The plant consistency assumption says that the diagnosers cannot force, disable, or delay the behavior of the plant. The causality condition says that the messaging scheme designed for a diagnoser must be a function of the observations of the diagnoser. The following is an example of a noncausal design.

Example: There is only one agent. The first FSM in figure 2 is the plant model. There are two unobservable events, $\Sigma_{puo} = \{f_1, f_2\}$. Both are failure events. All other events are observable. We pick $\Sigma_{mf} = \{mf1, mf2\}$. The second FSM models a design L . L is correct but noncausal since for two different plant behaviors, generating the same observation, it generates two different message sequences.

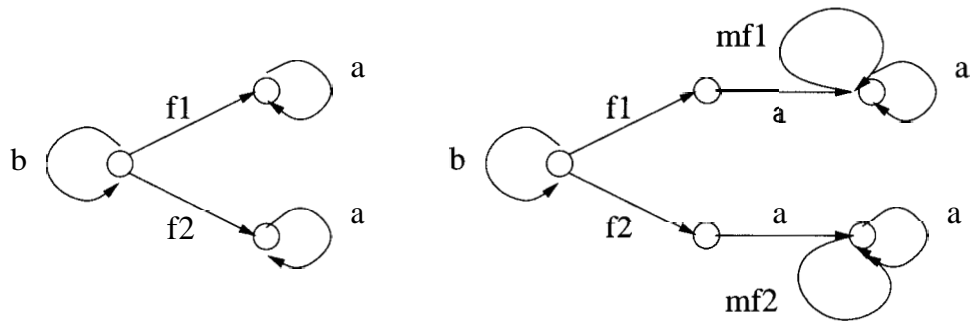


Figure 2: A plant and a non-causal diagnoser design

2.2 Correct Designs

It is desirable to design diagnosers that generate failure messages when there are failures in the plant and do not generate failure messages when there are no failures in the plant. These ideas are formalized as follows. It is assumed in the following that L is admissible.

Definition 2 L is *i-detecting* iff for all $\sigma_{f_i} \in \Sigma_{f_i}$, there exists n_i such that for all $u, v \in \Sigma^*$, $u\sigma_{f_i}v \in L$, $|P_{\Sigma_p}(v)| \geq n_i$, $\sigma_{m_{f_i}} \in u\sigma_{f_i}v$ or there exists $t \in (\Sigma_m \cup \Sigma_{m_f})^*$ such that $u\sigma_{f_i}vt\sigma_{m_{f_i}} \in L$.

The definition says that for all failures and for all ways in which that failures might occur, the design is such that it will generate a failure message within finitely many plant events following the failure, though it may wait to receive finitely many messages caused by the plant behavior before generating the failure message.

Definition 3 L is *i-false alarm free* iff for all $u\sigma_{m_{f_i}} \in L$, $\sigma_{f_i} \in u$.

The definition says that the design is such that every generation of a fault message by a diagnoser is preceded by the occurrence of the corresponding fault in the plant.

Definition 4 L is *ai-correct* iff L is *i-detecting* and *i-false alarm free*.

It is desirable that all diagnosers be correct. In our experience, a diagnostic design is generally correct under assumptions restricting the failures that can occur in the plant. Nevertheless it is important to understand the existence and computation of such solutions.

Note the similarities to the Neymann-Pearson problem [8]. This problem is deterministic. Therefore unlike the Neymann-Pearson problem languages with type one or type two errors cannot be compared in terms of false alarm and misdetection probabilities. Nevertheless in practise detecting languages with false alarms are a useful concept.

Like the Neyman-Pearson problem the following are true. A detecting language exists for every L , i.e., choose,

$$L = \{u : u \in L_p, \text{ or } u = v\sigma_1 \dots \sigma_k, v \in L_p\}, \Sigma_{m_{f_i}} = \{\sigma_1, \dots, \sigma_k\}.$$

Similarly, a false alarm free L always exists, i.e., choose $L = L$.

2.3 Diagnosability

We next formalize independent diagnosability, decentralized diagnosability and centralized diagnosability. We begin with the definition of decentralized diagnosability since it is the most complex.

Definition 5 The triple $(L_p, \{\Sigma_{p_{oi}}\}_{i \in \mathcal{A}}, \{\Sigma_{f_i}\}_{i \in \mathcal{A}})$ is *decentrally diagnosable* iff there exists $\{\Sigma_{m_i}\}_{i \in \mathcal{A}}$ and $L \subseteq \Sigma^*$ such that L is *i-correct* for all $i \in \mathcal{A}$.

Thus a plant is decentrally diagnosable iff there exists some message set and associated design in which each site can correctly generate the failure messages of interest after waiting for finitely many plant events and finitely many inter-diagnoser message events caused by the finitely many plant events.

Definition 6 The triple $(L_p, \{\Sigma_{poi}\}_{i \in \mathcal{A}}, \{\Sigma_{fi}\}_{i \in \mathcal{A}})$ is independently diagnosable iff for $\Sigma_{mi} = \emptyset$ for all $i \in \mathcal{A}$ there exists $L \subseteq \Sigma^*$ such that L is i -correct for all $i \in \mathcal{A}$.

Thus a plant is independently diagnosable if it is decentrally diagnosable with an empty inter-diagnoser communication message set, i.e., without inter-diagnoser communication.

Definition 7 The triple $(L_p, \{\Sigma_{poi}\}_{i \in \mathcal{A}}, \{\Sigma_{fi}\}_{i \in \mathcal{A}})$ is centrally diagnosable iff the corresponding single site triple $(L_p, \Sigma_{po}, \Sigma_f)$ is decentrally diagnosable, i.e., there exists L with $\Sigma_m = \emptyset$ such that L is 1-correct.

Thus a plant is centrally diagnosable iff a central diagnoser that observes every event observed by every site instantaneously, i.e., it observes the exact ordering of the observations of different sites, can diagnose all the failures of interest to all the sites.

It is immediate from definitions 6 and 5 that independent diagnosability implies decentralized diagnosability. The fact that decentralized diagnosability implies centralized diagnosability is also almost immediate from the definitions. It may be argued as follows. Let $(L_p, \{\Sigma_{poi}\}_{i \in \mathcal{A}}, \{\Sigma_{fi}\}_{i \in \mathcal{A}})$ be decentrally diagnosable and $L, \{\Sigma_{mi}\}_{i \in \mathcal{A}}$ be the corresponding design. Let $\Sigma' = \Sigma_p \cup \Sigma_{mf}$. Then $P_{\Sigma'}(L)$ is 1-correct for the triple $(L_p, \Sigma_{po}, \Sigma_f)$. In other words the centralized diagnostic design is obtained by simply deleting all the inter-diagnoser messaging events. The messaging is redundant because all the plant events causing the messages were centrally observed anyway.

3 Motivating Example

This section discusses an automated vehicle platoon wireless LAN diagnostic problem [3] that motivates our formulation of the diagnosis problem for distributed systems.

The concept of automated vehicle platoons on intelligent highways has been a subject of active research for several years. The following linear control law [14] has been extensively used for platoon follower control,

$$u_i = (1 - k_a)\ddot{x}_l + k_a\ddot{x}_{i-1} + k_v(\dot{x}_{i-1} - \dot{x}_i) + k_p(x_{i-1} - x_i - l) + c_v(\dot{x}_l - 5i) + c_p(x_l - x_i - iL),$$

where k_r, k, k_a, k_v, c_p are control gains, x_l is the position of the lead vehicle in an inertial reference frame, and x_i is the position of the i -th platoon follower in the same reference frame. Observe that the commanded acceleration of a platoon follower vehicle is a function of variables that cannot be sensed, such as the acceleration and velocity of the lead vehicle. Therefore platoon operation is supported by a wireless LAN [4],[7] that transmits information from one vehicle to the other at the sampling rate (typically 20ms) of the longitudinal control system. We are interested in the problem of designing diagnostics for the wireless LAN.

The physical structure of the platoon LAN corresponds closely with the distributed system diagnostic architecture in figure 1. Each vehicle in the platoon constitutes a site. It has radios that can transmit and receive. Each vehicle needs to have a diagnoser that can diagnose faults in its radios. The site diagnoser observes only the messages received by its radio. We shall see that the LAN radio network is centrally diagnosable but not independently diagnosable. A central diagnoser is difficult to realize and undesirable in a distributed system that is required to be highly fault tolerant. Therefore a decentralized diagnoser design is required and the vehicle diagnosers must exchange information for the purpose of diagnosis. We are motivated to understand if for a system

with a global observation structure rich enough to support centralized diagnosis there always exists an inter-diagnoser messaging scheme that can replicate some of the information utilized to obtain central diagnosability, i.e., are centrally diagnosable systems decentrally diagnosable? We explain the intuition behind our approach to this question in the context of the LAN example. Section 4 provides a more formal answer to this question.

We use a simplified model of the LAN operation that captures the features essential for diagnostic design. For the full model and design see [3]. Using this model, we show that the LAN diagnosis problem can be solved if the diagnosers can exchange information over a network distinct from the LAN itself. Fortunately the vehicles are also connected to a WAN that can be used for occasional messaging. It should be noted that there is no dedicated WAN bandwidth for a vehicle and therefore there are no deterministic bounds on the WAN communication delays.

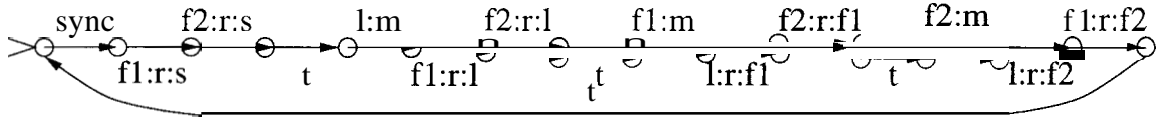


Figure 3: Normal Operation LAN Model for a Three Vehicle Platoon

sync	is the transmission of the synchronization pulse by the lead vehicle
f1:r:s	is the reception of the synchronization by the first follower vehicle
f2:r:s	is the reception of the synchronization by the second follower vehicle
t	is the expiration of the time slot
l:m	is the transmission of the lead vehicle control message
f1:r:l	is the reception of the lead vehicle control message by the first follower
f2:r:l	is the reception of the lead vehicle control message by the second follower
f1:m	is the transmission of the control message by the first follower
l:r:f1	is the reception of the first follower control message by the lead vehicle
f2:r:f1	is the reception of the first follower control message by the second follower
f2:m	is the transmission of the control message by the second follower
l:r:f2	is the reception of the second follower control message by the lead vehicle
f1:r:f2	is the reception of the second follower control message by the first follower

Table 1: LAN Model Events

The normal operation of the LAN network for a three vehicle platoon is shown by the finite state machine (FSM) in figure 3. The meanings of the event labels are explained by table 1. The vehicles share the LAN through a TDMA scheme [4,7]. The longitudinal control sampling interval is divided into slots of fixed duration with one slot being allocated to each vehicle in the platoon. At the beginning of the sampling interval the lead vehicle transmits a synchronizing pulse to which all the platoon vehicles set their clocks. The first slot is then used by the lead vehicle to transmit control information, the second is used by the first follower vehicle of the platoon, and so on until the last vehicle transmits, after which the lead vehicle synchronizes clocks again. Therefore under normal conditions the LAN has a time-driven operation with vehicles consecutively transmitting on the shared LAN channel. Since all transmissions occur on a shared channel we assume that in the absence of faults every transmission by a vehicle is received by every other vehicle. Note that a specific ordering of the reception events has been assumed for simplicity. In practise this is not the case.

We will illustrate the diagnosis of faults in the lead and first follower vehicles. The diagnosis

problem for subsequent followers is similar to that of the first follower. It is assumed that each radio can have a transmitter or receiver fault. The former implies that it is unable to transmit and the latter that it is unable to receive. Therefore we are concerned with diagnosis of the four fault events in table 2.

ltf	is the lead vehicle transmitter fault
lrf	is the lead vehicle receiver fault
$f1tf$	is the first follower transmitter fault
$f1rf$	is the first follower receiver fault

Table 2: LAN Failure Events

The complete LAN model (G_{lan}) is shown in figure 4. A vehicle that does not receive the synchronising pulse does not transmit since it may collide with the others if it does so. The lead vehicle transmits even if it does not receive anything because it controls the synchronisation. Once again for simplicity, it is assumed here that the faults occur only at the beginning of the sampling interval and only single failures are considered. If multiple failures occur they will be diagnosed incorrectly. Fortunately multiple failures are rare. In our experience it is generally the case that most systems cannot be instrumented to isolate multiple simultaneous failures.

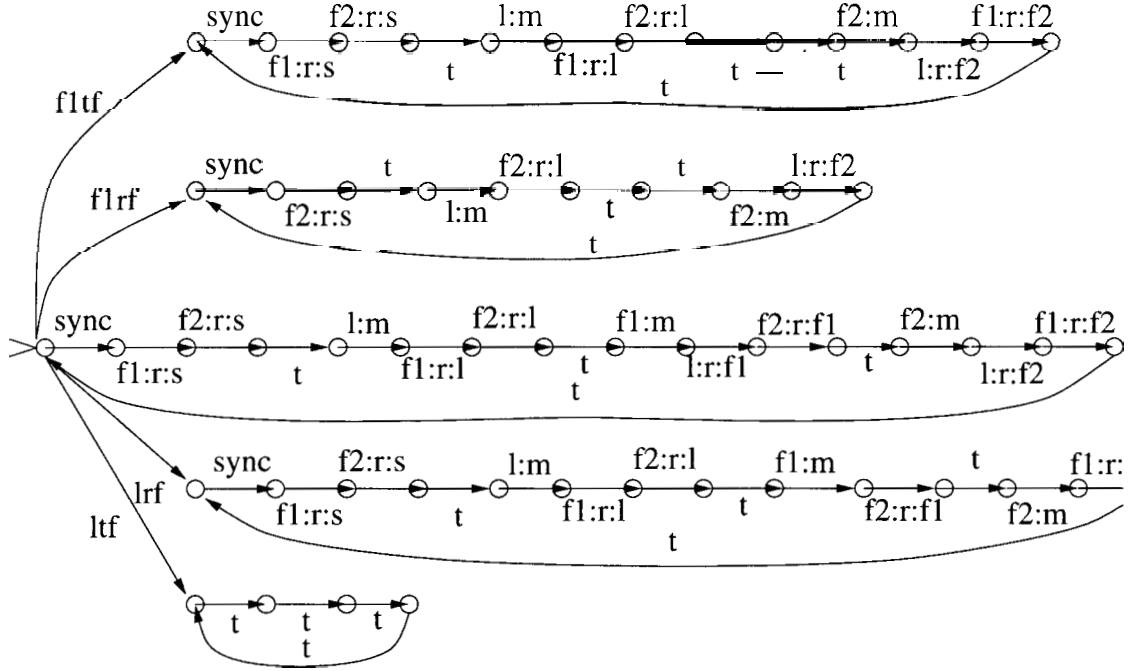


Figure 4: Complete LAN Model for a Three Vehicle Platoon

Since each vehicle has a receiver and a transmitter, it is assumed that each vehicle is desirous of diagnosing its own receiver and transmitter fault. Moreover there is a natural decomposition of observation, i.e., each vehicle diagnoser only observes the messages received by its receiver. Transmission events are unobservable. The clock ticks are observable. Formally the diagnostic problem is specified by the plant FSM of figure 4, and the following sets of failure and observable events for each vehicle

$$\Sigma_{ol} = \{tick, l:r:f1, l:r:f2\}, \Sigma_{of1} = \{tick, f1:r:l, f1:r:f2\}, \Sigma_{of2} = \{tick, f2:r:f1, f1:r:f2\},$$

$$\Sigma_{f1} = \{ltf, lrf\}, \Sigma_{f1} = \{f1tf, f1rf\}, \Sigma_{f2} = \{f2tf, f2rf\}.$$

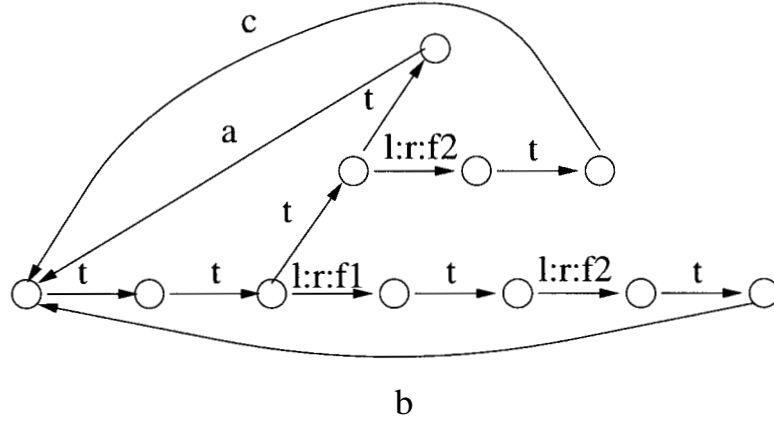


Figure 5: Simplified Lead Vehicle Observation Model

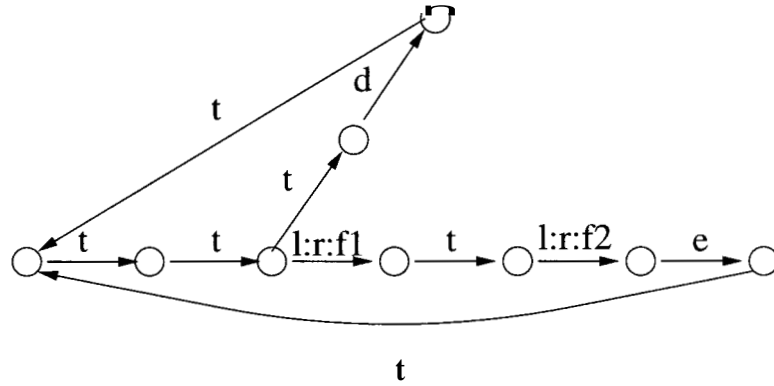


Figure 6: Simplified First Follower Vehicle Observation Model

The projection of G_{lan} onto Σ_{ol} indicates that over an entire sampling interval the lead vehicle observes the same behavior for the failures ltf and Zrf . Likewise it observes the same behavior for the failures $flrf$ and $fltf$. To reduce complexity we encode the observation process over the entire sampling interval into single events. Since there are three distinct kinds of observation over a sampling interval for the lead vehicle, the encoding is represented by three events a, b, c . In the case of the first follower the failures ltf and $flrf$ are indistinguishable, as are the normal mode and the failures $fltf, lrf$. Therefore for the first follower the encoding of the observation process can be represented by two events d, e . This encoding process is represented by the finite state machines in figures 5 and 6. This encoding allows us to ignore the more numerous set of original plant behaviors and study the diagnostic problem by projecting the composition of G_{lan} and the FSM's in figures 5 and 6 onto the reduced event set $\{ltf, lrf, fltf, flrf, a, b, c, d, e\}$. This projection can be represented as the composition of three FSM's. Figure 7 represents the failures and the corresponding encoded observation process of the lead vehicle (G_l^{red}), figure 8 that of the first follower vehicle (G_{f1}^{red}), and the FSM (G_{fair}) in figure 9 represents the plant property that in every sampling interval observations will be made by both lead and follower vehicles. This sort of "fairness" in observation is important since if the plant has arbitrarily long behaviors that only yield observations to a single diagnoser, then the other diagnosers are of little use in these situations. The local information of the single diagnoser must suffice. The composition of the three FSM's (G_{lan}^{red}) is shown in figure 10.

Figures 7 and 8 show that the LAN is not independently diagnosable. Figure 7 shows that

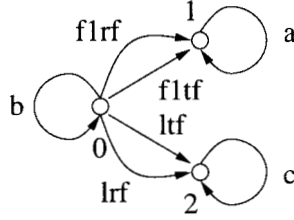


Figure 7: Projection of the Plant onto Reduced Lead Vehicle Observations

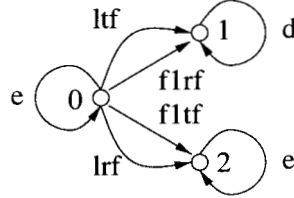


Figure 8: Projection of the Plant onto Reduced First Follower Observations

the lead vehicle observes the event c for both ltf and lrf , making them indistinguishable given local information. Similarly, figure 8 shows that the first follower observes e for the normal mode, $fltf$, and lrf making these two failures indistinguishable from each other and the normal mode given local information. On the other hand the LAN is centrally diagnosable since a diagnoser observing all the messages received by the lead and follower vehicles, i.e., with the observable event set $\Sigma_{ol} \cup \Sigma_{of1}$, could distinguish all four failure modes and the normal mode. Figure 10 shows that the future possible observable event sequences from the state sets

$$\{0, 9\}, \{1, 5\}, \{2, 6\}, \{3, 7\}, \{4, 8\},$$

are all pairwise different. For any of the four failures, the third event following the failure will provide a signature that will uniquely identify the state entered by the plant after the failure and therefore the failure event itself. In section 4 we prove the diagnosability of this system formally.

Finally, we are left with the question of whether the LAN is decentrally diagnosable, i.e., whether there exists an inter-diagnoser messaging scheme that can provide each vehicle with some of the information that enables central diagnosability. One straightforward communication scheme is for each vehicle to communicate all its observations to the others. Intuitively, this scheme represents the possibility of “maximizing” the replication of global information. We show in section 4 that if this communication scheme does not work then no communication scheme works. However, this communication scheme is not a practical solution to decentralized diagnosis problems for at least two reasons. Firstly, the bandwidth required to support diagnosis would likely be very nearly the same as that required for normal operation. The second reason arises explicitly from our modeling assumptions. Suppose the lead vehicle observes the sequence b^n , and is designed to communicate every observation of b to the first follower by generating the message event m_b . Since we make no assumptions on the delays in the inter-diagnoser communication network, there is clearly no bound on the number of b 's that may be generated by the plant before the first m_b is delivered to the other diagnoser. Since each b observation puts an m_b in the message queue, the lead vehicle diagnoser in general needs to schedule an unbounded queue (specifically of size n for b^n) of m_b messages to be delivered. Formally, we show in section 4 that for a regular plant language L , the correct L corresponding to the “communicate all observations” communication scheme is not generally regular.

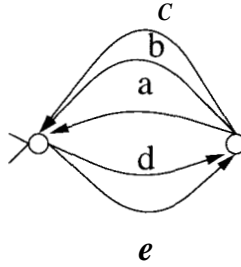


Figure 9: Projection of the Plant onto the Reduced Observable Event Set

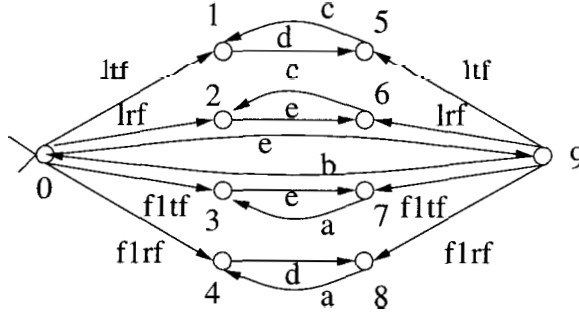


Figure 10: Reduced LAN Model

A more practical decentralized diagnosis scheme that works for this example is shown in figures 11 and 12. The two figures show diagnoser designs for the lead and follower vehicle respectively. Basically, if the lead observes c it sends a message to the first follower. The follower then reports the first observation after receipt of the message. The lead vehicle then generates the appropriate fault message. If the lead vehicle observes a then it reports the observation to the first follower. The first follower then waits for the first plant observation following the lead vehicles message and then generates the appropriate failure message.

The protocol is similar if the lead observes c .

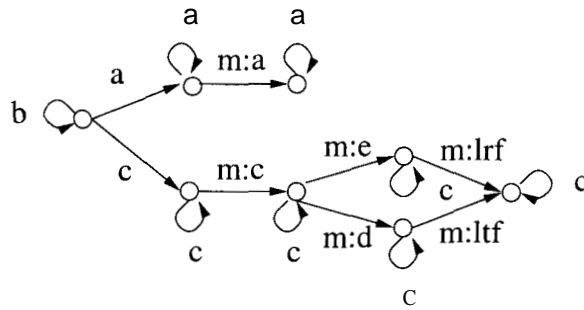


Figure 11: Lead Vehicle LAN Diagnoser Design

4 Existence of a Correct Design

The following theorem provides a necessary and sufficient condition for the existence of a messaging scheme for a given decentralized diagnostic problem. The condition is a qualitative property of the

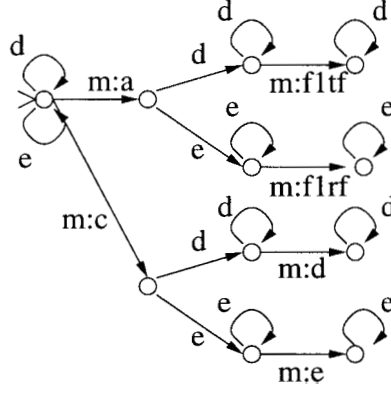


Figure 12: First Follower Vehicle LAN Diagnoser Design

DES plant. It generalizes a theorem presented in [12] on centralized diagnosis. We apply it to the example in section 3 and to other examples that help us understand the distinction between systems for which inter-diagnoser communication can replicate some of the global information adequately and systems for which it cannot. We also state a corollary of the theorem stating necessary and sufficient conditions for the three kinds of diagnosability.

The theorem states that a plant is decentrally diagnosable iff for every failure event, and every plant behavior that precedes and succeeds the failure event, where the succeeding behavior is sufficiently long, any other behavior that looks the same to all the sites must also have the same failure in it. Thus as long as every failed and non-failed plant behavior can be distinguished by at least one site the diagnosis problem can be correctly solved. In particular, we show the sufficiency of the plant property by proving that the “communicate all observations” messaging scheme results in a correct diagnostic design.

Theorem 1 *There exists L , i -correct for all $i \in \mathcal{A}$, iff there exists $n \in \mathbb{N}$ such that for all $\sigma_f \in \Sigma_f$ and $u\sigma_f v \in L$, with $|v| > n$, the following condition is satisfied,*

$$(w \in L_p) \wedge (\forall i, P_{\Sigma_{poi}}(u\sigma_f v) = P_{\Sigma_{poi}}(w)) \Rightarrow \sigma_f \in w.$$

Proof: We first prove the necessity of the condition. Let L be i -correct for all $i \in \mathcal{A}$ and the hypothesis be false. In other words there exists $\sigma_f \in \Sigma_{fi}$ and $u\sigma_f \in L$, such that for all $n \in \mathbb{N}$ there exists $v_n, w, \in X^n$ with $u\sigma_f v_n \in L$, $|v| > n, \forall j, P_{\Sigma_{poj}}(w_n) = P_{\Sigma_{poj}}(u\sigma_f v_n)$, and $\sigma_f \notin w$. Since $u\sigma_f v \in L$, $u\sigma_f v \in L$. Since L is i -correct it is i -detecting. Therefore there exist $N \in \mathbb{N}$ and $t \in (\Sigma_m \cup \Sigma_{mf})^*$ such that $u\sigma_f v_N t \sigma_{mf} \in L$, where $\sigma_{mf} \in \Sigma_{mf}$ is the failure message generated by diagnoser i corresponding to failure σ_f . Let $t = \sigma_1^t \dots \sigma_K^t$.

Claim 1 $w_N t \in L$ and $P_{\Sigma_{oi}}(w_N t) = P_{\Sigma_{oi}}(u\sigma_f v_N t)$.

Proof: We prove by induction. Let $w_N \sigma_1^t \dots \sigma_k^t \in L$ and for all j ,

$$P_{\Sigma_{oj}}(w_N \sigma_1^t \dots \sigma_k^t) = P_{\Sigma_{oj}}(u\sigma_f v_N \sigma_1^t \dots \sigma_k^t).$$

Let $\sigma_{k+1}^t \in \Sigma_{ml} \cup \Sigma_{mfl}$. Since $P_{\Sigma_{ol}}(w_N \sigma_1^t \dots \sigma_k^t) = P_{\Sigma_{ol}}(u\sigma_f v_N \sigma_1^t \dots \sigma_k^t)$, and $u\sigma_f v_N \sigma_1^t \dots \sigma_{k+1}^t \in L$, by causality of L , $w_N \sigma_1^t \dots \sigma_{k+1}^t \in L$. Also

$$P_{\Sigma_{ol}}(w_N \sigma_1^t \dots \sigma_{k+1}^t) = P_{\Sigma_{ol}}(w_N \sigma_1^t \dots \sigma_k^t) \sigma_{k+1}^t = P_{\Sigma_{ol}}(u\sigma_f v_N \sigma_1^t \dots \sigma_k^t) \sigma_{k+1}^t = P_{\Sigma_{ol}}(u\sigma_f v_N \sigma_1^t \dots \sigma_{k+1}^t).$$

For $j \neq l$, $\sigma_{k+1}^t \notin \Sigma_{oj}$, and hence,

$$P_{\Sigma_{oj}}(w_N \sigma_1^t \dots \sigma_{k+1}^t) = P_{\Sigma_{oj}}(w_N \sigma_1^t \dots \sigma_k^t) = P_{\Sigma_{oj}}(u \sigma_f v_N \sigma_1^t \dots \sigma_k^t) = P_{\Sigma_{oj}}(u \sigma_f v_N \sigma_1^t \dots \sigma_{k+1}^t).$$

This establishes the induction step. The base case is $w_N \in L$ and for all j , $P_{\Sigma_{oj}}(u \sigma_f v_N) = P_{\Sigma_{oj}}(w_N)$. By induction the claim is true. \bullet

The claim together with the causality of \mathbf{L} , and $u \sigma_f v_N t \sigma_{mf} \in \mathbf{L}$, implies that $w_N \sigma_{mf} \in \mathbf{L}$. But $\sigma_f \notin w_N$, which implies that \mathbf{L} has a false alarm and L is not i -correct. By contradiction the hypothesis is true.

We prove sufficiency by construction. Pick a collection of message sets $\{\Sigma_{mi}\}_{i \in \mathcal{A}}$ such that the message sets are disjoint from each other, Σ_p , and Σ_{mf} . Furthermore each Σ_{mi} should be such that there exists a bijection $\eta_i : \Sigma_{poi} \rightarrow \Sigma_{mi}$. Let

$$\mathbf{L} = \{w \in \Sigma^* : P_{\Sigma_p}(w) \in L_p, \forall i P_{\Sigma_{mi}}(w) \leq \eta_i \circ P_{\Sigma_{poi}}(w), \text{ and } (w = s \sigma_{mf}) \Rightarrow \exists u \sigma_f v \in \mathbf{L}, |\mathbf{v}| > n, \text{ such that } \forall j ((P_{\Sigma_{poj}}(s) \geq P_{\Sigma_{poj}}(u \sigma_f v)) \wedge (PC, (w) \geq \eta_j \circ P_{\Sigma_{poj}}(u \sigma_f v)))\}.$$

1. L is non-empty: From the definition of \mathbf{L} , $L_p \subseteq \mathbf{L}$.

2. L is plant consistent: By definition, $L \subseteq \mathbf{L}$, and for all $w \in L$, $P_{\Sigma_p}(w) \in L_p$. For $w \in \mathbf{L}$, let $P_{\Sigma_p}(w) \sigma \in L$. Then

$$P_{\Sigma_{mi}}(w \sigma) = P_{\Sigma_{mi}}(w) \leq \eta_i \circ P_{\Sigma_{poi}}(w) \mathbf{I} \eta_i \circ P_{\Sigma_{poi}}(w \sigma).$$

Thus $w \sigma \in \mathbf{L}$.

3. L is causal: Consider $u \sigma_m \in L$, $\sigma_m \in \Sigma_{mi} \cup \Sigma_{mfi}$, $\mathbf{v} \in \mathbf{L}$, $P_{\Sigma_{oi}}(u) \models P_{\Sigma_{oi}}(\mathbf{v})$. We show that $v \sigma_m \in L$.

$v \sigma_m \in \Sigma^*$ is immediate. Consider the case $\sigma_m \in \Sigma_{mi}$. For $j \neq i$,

$$\begin{aligned} P_{\Sigma_{mj}}(v \sigma_m) &= P_{\Sigma_{mj}}(v) && [\sigma_m \notin \Sigma_{mj}] \\ &\mathbf{I} \eta_j P_{\Sigma_{poj}}(v) && [v \in L] \\ &= \eta_j P_{\Sigma_{poj}}(v \sigma_m) && [\sigma_m \notin \Sigma_{mj}] \end{aligned}$$

For $j = i$,

$$\begin{aligned} PC,; (v \sigma_m) &= P_{\Sigma_{mi}}(v) \sigma_m && [\sigma_m \in \Sigma_{mi}] \\ &= P_{\Sigma_{mi}}(u) \sigma_m && [P_{\Sigma_{oi}}(u) = P_{\Sigma_{oi}}(v)] \\ &= P_{\Sigma_{mi}}(u \sigma_m) \\ &\mathbf{I} \eta_i P_{\Sigma_{poi}}(u \sigma_m) && [u \sigma_m \in \mathbf{L}] \\ &= \eta_i P_{\Sigma_{poi}}(u) && [\sigma_m \notin \Sigma_{poi}] \\ &= \eta_i P_{\Sigma_{poi}}(v) && [P_{\Sigma_{oi}}(u) = P_{\Sigma_{oi}}(v)] \\ &= \eta_i P_{\Sigma_{poi}}(v \sigma_m) && [\sigma_m \notin \Sigma_{poi}]. \end{aligned}$$

Thus $v \sigma_m \in L$.

Consider the case $\sigma_m \in \Sigma_{mfi}$. From $P_{\Sigma_{oi}}(u) = P_{\Sigma_{oi}}(v)$ we get for all j , $P_{\Sigma_{mj}}(u) \models P_{\Sigma_{mj}}(v)$. Also there exists $s \sigma_f t \in \mathbf{L}$, $|t| > n$, such that for all j , $P_{\Sigma_{poj}}(u) \geq P_{\Sigma_{poj}}(s \sigma_f t)$ and $P_{\Sigma_{mj}}(u) \geq \eta_j P_{\Sigma_{oj}}(s \sigma_f t)$. We show that v satisfies the same inequalities. The second one is immediate from $P_{\Sigma_{mj}}(u) \models P_{\Sigma_{mj}}(v)$. We prove the first by contradiction.

Let $P_{\Sigma_{poj}}(v) < P_{\Sigma_{poj}}(s \sigma_f t)$. Then

$$\eta_j P_{\Sigma_{poj}}(s \sigma_f t) > \eta_j P_{\Sigma_{poj}}(v) \geq P_{\Sigma_{mj}}(v) = P_{\Sigma_{mj}}(u).$$

By contradiction $P_{\Sigma_{poj}}(v) \geq P_{\Sigma_{poj}}(s \sigma_f t)$. Thus $v \sigma_m \in L$.

4. L is i -detecting for all i : Pick any $u\sigma_{fi}v \in L$, $|P_{\Sigma_p}(v)| > n$, where n is as in the hypothesis. Assume w.l.o.g. that $\sigma_{fmi} \notin u\sigma_{fi}v$. Note that for all j , $P_{\Sigma_{poj}}(u\sigma_{fi}v) = P_{\Sigma_{poj}}(PC,(u)\sigma_{fi}P_{\Sigma_p}(v))$, where $P_{\Sigma_p}(u)\sigma_{fi}P_{\Sigma_p}(v) \in L$. In the case where for all j , $P_{\Sigma_{mj}}(u\sigma_{fi}v) \geq \eta_j P_{\Sigma_{poj}}(P_{\Sigma_p}(u)\sigma_{fi}P_{\Sigma_p}(v))$, by definition of L , $u\sigma_{fi}v\sigma_{mfa_i} \in L$. Assume there exists j such that $P_{\Sigma_{mj}}(u\sigma_{fi}v) < \eta_j P_{\Sigma_{poj}}(P_{\Sigma_p}(u)\sigma_{fi}P_{\Sigma_p}(v))$. For all j , pick $t_j \in \Sigma_{mj}^*$ such that $P_{\Sigma_{mj}}(u\sigma_{fi}vt_1 \dots t_{|\mathcal{A}|}) = \eta_j P_{\Sigma_{poj}}(PC,(u)\sigma_{fi}P_{\Sigma_p}(v))$. Then by definition of L , $u\sigma_{fi}vt_1 \dots t_{|\mathcal{A}|}\sigma_{mfa_i} \in L$. Thus L is i -detecting.
5. L is false-alarm free: Let $s\sigma_{fm} \in L$. Then there exists $u\sigma_{fv} \in L$, $|v| > n$ such that for all j , $P_{\Sigma_{poj}}(u\sigma_{fv}) = P_{\Sigma_{poj}}(s)$. In particular, for all j , $P_{\Sigma_{poj}}(u\sigma_{fv}) = P_{\Sigma_{poj}}(P_{\Sigma_p}(s))$. Since $P_{\Sigma_p}(s) \in L$, by the hypothesis, $\sigma_f \in P_{\Sigma_p}(s)$. This implies $\sigma_f \in s$.

Observe that the diagnosing language constructed in the proof is not regular in general. Consider the plant FSM in figure 13. Let there be two sites with observation sets $\Sigma_{o1} = \{a\}$ and $\Sigma_{o2} = \{b\}$. $\Sigma_f = \Sigma_{f1} = \{f\}$ is the one unobservable fault event to be diagnosed by site 1. Let the corresponding message sets be $\Sigma_{m1} = \{m\}$ and $\Sigma_{m2} = \{m_b\}$. Let L be as in the proof. Then for any $n, m \in \mathbb{N}$, $n > m$, a^n is not Nerode equivalent in L to a^m , because $a^n m_a^n \in L$ but $a^m m_a^n \notin L$.

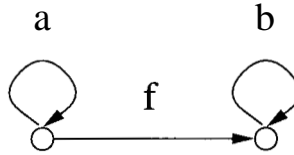


Figure 13: A Simple Plant

The following corollary of theorem 1 relates the the theorem to the definitions of decentralized, centralized, and independent diagnosability.

Corollary 1 1. The triple $(L_p, \{\Sigma_{poi}\}_{i \in \mathcal{A}}, \{\Sigma_{fi}\}_{i \in \mathcal{A}})$ is decentrally diagnosable iff there exists $n \in \mathbb{N}$ such that for all $\sigma_f \in \Sigma_f$ and $u\sigma_f v \in L$, with $|v| > n$, the following condition is satisfied,

$$(w \in L_p) \wedge (\forall i, P_{\Sigma_{poi}}(u\sigma_f v) = P_{\Sigma_{poi}}(w)) \Rightarrow \sigma_f \in w.$$

2. The triple $(L_p, \{\Sigma_{poi}\}_{i \in \mathcal{A}}, \{\Sigma_{fi}\}_{i \in \mathcal{A}})$ is centrally diagnosable iff there exists $n \in \mathbb{N}$ such that for all $\sigma_f \in \Sigma_f$ and $u\sigma_f v \in L$, with $|v| > n$, the following condition is satisfied,

$$(w \in L_p) \wedge (P_{\Sigma_{po}}(u\sigma_f v) = P_{\Sigma_{po}}(w)) \Rightarrow \sigma_f \in w.$$

3. The triple $(L_p, \{\Sigma_{poi}\}_{i \in \mathcal{A}}, \{\Sigma_{fi}\}_{i \in \mathcal{A}})$ is independently diagnosable iff for all $i \in \mathcal{A}$ there exists $n_i \in \mathbb{N}$ such that for all $\sigma_f \in \Sigma_{fi}$ and $u\sigma_f v \in L$, with $|v| > n_i$, the following condition is satisfied,

$$(w \in L_p) \wedge (P_{\Sigma_{poi}}(u\sigma_f v) = P_{\Sigma_{poi}}(w)) \Rightarrow \sigma_f \in w.$$

Proof:

1. Immediate from definition 5 and theorem 1.
2. Immediate by applying theorem 1 with $|\mathcal{A}| = 1$ to $(L_p, \Sigma_{po}, \Sigma_f)$.

3. Let the triple be independently diagnosable. Then there exists L , i -correct for all $i \in \mathcal{A}$, and $\Sigma_{m_i} = \emptyset, i \in \mathcal{A}$. Pick any $\Sigma_f \in \Sigma_{f_i}$ and $u\sigma_f v \in L_p$ with $|v| > n_i$. Let $w \in L_p$ and $P_{\Sigma_{p_{oi}}}(u\sigma_f v) = P_{\Sigma_{p_{oi}}}(w)$. Since $\Sigma_{m_i} = \emptyset$, $u\sigma_f v\sigma_{mf} \in L$. By causality $w\sigma_{mf} \in L$. Since L is false-alarm-free $\sigma_f \in w$.

Let the condition be true. Pick $n = \max_i n_i$ and let

$$L = \{w \in (\Sigma_p \cup \Sigma_{mf})^* : P_{\Sigma_p}(w) \in L, \text{ and } w = s\sigma_{mf} \Rightarrow \exists u\sigma_f v \in L_p, |v| > n, \forall j P_{\Sigma_{p_{oj}}}(s) \geq P_{\Sigma_{p_{oj}}}(u\sigma_f v)\}$$

It can be shown in a manner similar to the sufficiency proof of theorem 1 that L is correct for all $i \in \mathcal{A}$.

The following is an example of a plant that can be diagnosed by a single diagnoser but cannot be diagnosed by two diagnosers who jointly observe the same events as the single agent but observe less severally.

Example: There are two diagnosers with observation and failure events events $\Sigma_{p_{o1}} = \{a, c\}, \Sigma_{f1} = \{f1\}, \Sigma_{p_{o2}} = \{b, c\}, \Sigma_{f2} = \{f2\}$. The plant is shown in figure 14. There is no correct messaging design as evident from $u\sigma_f v = f1abc^n$, and $w = f2bac^n$. Then for all n , $P_{\Sigma_{oi}}(u\sigma_f v) = P_{\Sigma_{oi}}(w)$, $i = 1, 2$ and $f1 \notin w$. However, if there is a single diagnoser with observation $\Sigma_{p_o} = \{a, b, c\}$, a correct design exists because $P_{\Sigma_{p_o}}(u\sigma_f v) \neq P_{\Sigma_{p_o}}(w)$ for any $n \in \mathbb{N}$.

This is an example of plant in which the isolation of $f1$ and $f2$ from each other depends upon the correct ordering of the observable events generated by the plant and with the decentralization of observation being as given no amount of messaging or memory can reconstruct the exact order in which a and b occurred. It seems that the only way to diagnose failures in this kind of plant would be to use time-stamps from a global clock.

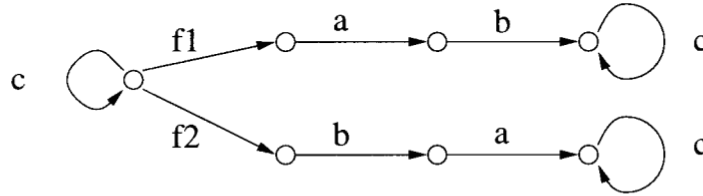


Figure 14: The difference between centralized and decentralized diagnostics

We can use theorem 1 to show that a correct diagnostic design exists for the LAN network example discussed in section 3. The argument refers to the finite state machines shown in figure 10. We pick the $n = 2$, where n is as in theorem 1. Consider $\sigma_f = fltf$. Then for all $ufltf \in L$, $v = ae$ or $v = ea$. Let w be such that

$$P_{\Sigma_{oi}}(u\sigma_f v) = P_{\Sigma_{oi}}(w), P_{\Sigma_{f1}}(u\sigma_f v) = P_{\Sigma_{f1}}(w), \sigma_f \notin w.$$

Since $a \in w$, the assumptions imply $f1rf \in w$. Since $d \in w$, this implies

$$w = (eb)^n f1rf, \text{ or } w = (eb)^n e f1rf.$$

This implies $a \notin w$ which is a contradiction. Therefore $f1tf \in w$. The arguments are similar for the three other failure events. They are not presented.

5 Summary

We have formulated a diagnostic problem for distributed systems within the context of a language-theoretic discrete event formalism. The diagnosis problem is non-trivial because the plant is partially observed. In particular the failure events are assumed to be unobservable. We say that the distributed system is diagnosable if there exists a failure message design that is a function of the observations that is detecting and false-alarm-free in the Neymann-Pearson sense. Three notions of diagnosability, namely centralized, decentralized, and independent, are investigated.

In a plant with decentralized observation the sites collectively observe more than they do individually. We have presented a wireless LAN diagnosis problem in which local site information is inadequate to diagnose the failures at the site, but the collective information is adequate. However, the collective information can only be realized by inter-diagnoser messaging. A suitable message design is presented for the wireless LAN example. We show that in general there exist finite state systems for which the full collective information cannot be realized by any inter-diagnoser communication scheme. In other words, there exist centrally diagnosable systems that are not decentrally diagnosable. This happens when diagnosis depends on the ordering of plant events and the order cannot be reconstructed due to the decentralization of information. This problem could not arise in a distributed system where the site clocks are synchronized. However, in systems with unsynchronized local clocks these problems are to be expected.

We have presented a theorem that qualitatively describes, in a necessary and sufficient manner, the class of partially observed discrete event plants for which there exists an inter-diagnoser messaging scheme that is adequate. This result generalizes the results presented in [12]. We are able to use the theorem to prove the diagnosability or non-diagnosability of some interesting examples that give us an understanding of the distinctions between the solvable and unsolvable problems. We investigate the properties of the “communicate all observations scheme” that intuitively seems to maximize the information of each site. The proof of theorem 1 shows that in a decentrally diagnosable plant this scheme always works though it may require unbounded memory to execute. For the LAN example we can see that better finite memory solutions exist.

The investigations described in this paper offer many interesting avenues of further research. Within the context of this model one could investigate decidability and the synthesis of efficient communication. We are also left with the feeling that an interleaved semantics is a rather poor way of representing concurrency. Richer models expressing bounds on communication delays or concurrent observation would allow more interesting formulations of partial observation problems in distributed systems.

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