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Singular Spectrum Analysis for astronomical time series: constructing a parsimonious hypothesis test

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Abstract We present a data-adaptive spectral method - Monte Carlo Singular Spectrum Analysis (MC-SSA) - and its modification to tackle astrophysical problems. Through numerical simulations we show the ability of the MC-SSA in dealing with $1/f^\beta$ power-law noise affected by photon counting statistics. Such noise process is simulated by a first-order autoregressive, AR(1) process corrupted by intrinsic Poisson noise. In doing so, we statistically estimate a basic stochastic variation of the source and the corresponding fluctuations due to the quantum nature of light. In addition, MC-SSA test retains its effectiveness even when a significant percentage of the signal falls below a certain level of detection, *e.g.*, caused by the instrument sensitivity. The parsimonious approach presented here may be broadly applied, from the search for extrasolar planets to the extraction of low-intensity coherent phenomena probably hidden in high energy transients.

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1 Colored noise and MC-SSA

$1/f^\beta$ power-law noise is known to be highly relevant in several astrophysical systems [4, 5, 3]. It includes the well-known white noise ($\beta = 0$), pink noise ($\beta = 1$) and red or Brownian noise ($\beta = 2$). Such kind of noises are very often not tied to instrumental disturbance but rather they are property of the observed sources that emit radiation varying in a stochastic manner. In the context of our work, it is sufficient to qualitatively characterize $1/f^\beta$ to generate a parsimonious hypothesis test in MC-SSA (see below). Subsequently, the dynamical origin of noise fluctuation or the extra-noise variance – according to acceptance or rejection of our null hypothesis – has to be determined by theoretical analysis.

Singular Spectrum Analysis (SSA) is an effective, data-adaptive and non-parametric method for the decomposition of a time series into a well-defined set of independent and interpretable components that include a non-linear trend, anharmonic, amplitude-modulated oscillations, and noise [6]. In its later developments, the Monte Carlo approach to signal-to-noise separation introduced by [1] has become known as Monte Carlo SSA (MC-SSA) [2]. The distinction between what is *noise* and what is *signal* is made through the measure of the resemblance of a given noise surrogate to the original data via eigendecomposition of the time-lagged covariance matrix. For this study the noise surrogates set is generated by using an AR(1) process. In practice, the AR(1) coefficients are estimated from the time-series under consideration by using a maximum-likelihood criterion. Subsequently, these AR(1) noise surrogates are corrupted by Poisson noise to mimic the effect of a photon counting detector.

2 Simulated $1/f^\beta$ series test

The procedure has been tested on a large sample of artificial time series of arbitrary colored noises. As a test of validity, we show several discrete colored noise vectors of length $N = 5000$, with a power-law distribution of slope β ranging from 1 to 2 in steps of two. To obtain sequences of colored noises we use the Matlab library CNOISE¹. A threshold of signal identification is incorporated by subtracting a mean value $\sim 35\%$ of the maximum peak-flux, C_{max} . In this way, we take into account episodes of emission during which the emission count rate drops to the background level. Finally, the time series are corrupted by Poisson noise to simulate the effect of the shot noise based on Poisson photon statistics. The resulting test series, are shown in the supplementary video². The signal to noise ratio (SNR) of the artificial series test increases as the simulations run.

¹ http://people.sc.fsu.edu/~jburkardt/m_src/cnoise/cnoise.html

² <https://vimeo.com/120699083>

3 Conclusion and future work

We present a modified data-adaptive spectral method – Monte Carlo Singular Spectrum Analysis (MC-SSA) – in which a parsimonious (dynamic and instrumental) noise-model H_0 is adopted for astrophysical applications, i.e. $H_0 = \{\text{AR}(1) + \text{Poisson noise}\}$. AR(1) noise takes into account the long-term variability in the power-law slope $-\beta$ of a light-curve’s spectral density, and the Poisson noise considers the short-term variability imposed by the quantum nature of light. Our simulations show a remarkable effectiveness of the model for colored noises with β values between 1.5 and 2 and with $C_{max} > 1000$ counts; otherwise one should re-bin the light-curve to improve the signal-to-noise ratio of the source.

All analyses were performed by using SSA-MTM Toolkit freeware that has been developed by the Theoretical Climate Dynamics Group at UCLA³. To obtain presented results we relied on an advanced option in SSA-MTM Toolkit for MC-SSA that allows to read in ensemble of surrogates created off-line and corresponding to an arbitrary noise null-hypothesis H_0 . In this regard, MC-SSA allows to iteratively refine the working hypothesis and adapt the null-hypothesis H_0 for various theoretical scenarios. We plan to extend further SSA-MTM Toolkit for astrophysical applications by directly including the algorithm for parsimonious H_0 in the freeware. Current and future work will focus on SSA as a promising technique for analysing complex spatio-temporal structures to detect possible periodicities and other statistical regularities due to various astrophysical processes.

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³ <http://www.atmos.ucla.edu/tcd/ssa/>