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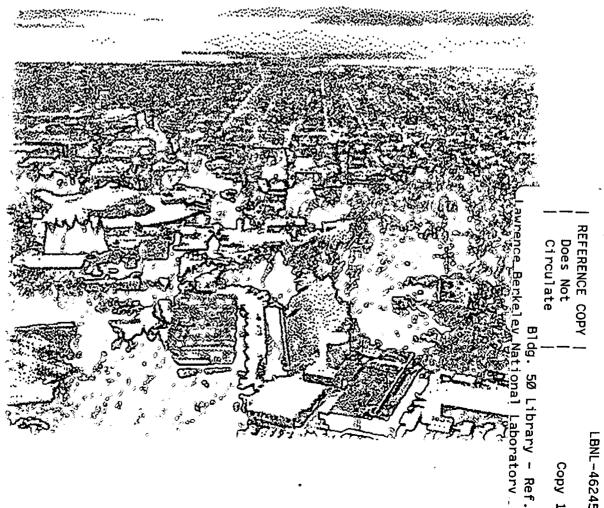
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Fission Transient Times from Fission Probabilities of Neighboring Isotopes

K.X. Jing, L. Phair, L.G. Moretto, Th. Rubehn, L. Beaulieu, T.S. Fan, and G.J. Wozniak

Nuclear Science Division

June 2000



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Fission Transient Times from Fission Probabilities of Neighboring Isotopes

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(June 27, 2000)

We present a new and straightforward method to estimate the fission transient time by utilizing the cumulative fission probabilities of neighboring isotopes. The fission probabilities were determined as the ratio of the measured fission cross sections to the Bass Model fusion cross sections. For five neighboring ¹⁸⁵⁻¹⁸⁹Os compound nuclei produced in ³He/⁴He-induced reactions on separated isotope W targets, the transient time τ_D is estimated to be smaller than 25×10^{-21} seconds, and the most likely value of τ_D is about 10×10^{-21} seconds.

The evolution of a fissioning nucleus from an assumed spherical shape towards the fission saddle, and eventually to the scission point, has been studied extensively [1-3]. If the transient time (τ_D) that a nucleus takes to evolve from a ground state shape to the saddle point is longer than the characteristic time for compound nucleus decay ($\tau_{\rm CN}$), then the fission probability is expected to be suppressed, and additional particles can be emitted as compared to those predicted by the standard theory. If on the other hand the transient time is short compared to $\tau_{\rm CN}$, then the stationary Kramers current [4] (i.e., the transition state fission rate) is expected.

This transient time effect has been advocated as an explanation for the large number of prescission neutrons [5-7], charged particles [8,9], and electric dipole γ rays [2,10] observed in relatively heavy fissioning systems. Fission time scales as long as $\sim 10^{-19}$ seconds have been inferred for fission from the observed prescission particles [1,11,12], although other recent works [13-16] indicate a shorter time scale.

Prescission particles can be emitted either before the system reaches the fission saddle, or during the descent from saddle to scission. Therefore, the fission time inferred from prescission particle emission is the sum of the transient time discussed above and of the time required for the nucleus to descend from saddle to scission. It is important to distinguish between presaddle and postsaddle times since postsaddle times do not affect the fission probability. Efforts have been made to separate the presaddle and postsaddle time components by examining the differences in the mean kinetic energy of charged particles emitted pre- and postsaddle [17]. The separation of presaddle and postsaddle particle emissions is, however, fraught with difficulties and ambiguities.

The transient time has a strong and direct effect on the fission probability. Consequently, its magnitude may be determined more reliably from fission probabilities [18] rather than from indirect methods such as particle/photon emission.

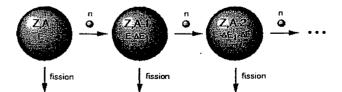
In the following, we illustrate a new method to estimate the transient time, based upon high precision fission probabilities of several neighboring isotopes. This approach is based on the fact that, except for a factor accounting for the transient time effects, the second chance fission probability of a nucleus (Z, A) appears as the first chance fission probability of the neighboring nucleus (Z, A - 1), whose second chance fission probability is in turn the first chance fission probability of its novel approach, which does not involve any consideration beyond the fission saddle, automatically bypasses the difficulties associated with the separation of the presaddle and postsaddle particle emissions.

Assuming a step function for the transient time effects, the fission decay width can be written as

$$\Gamma_f = \Gamma_f^{(\infty)} \int_0^\infty \zeta(t) \, \frac{N(t)}{N_0} \, \lambda_{\rm CN} \, dt = \Gamma_f^{(\infty)} \int_{\tau_D}^\infty \frac{N(t)}{N_0} \, \frac{dt}{\tau_{\rm CN}},$$
(1)

where $\zeta(t) = 0$ $(t < \tau_D)$ and $\zeta(t) = 1$ $(t \ge \tau_D)$; τ_D is the fission transient time; N(t) is the number of remaining compound nuclei at time t (starting with N_0 compound nuclei at t=0); $\lambda_{\rm CN}$ is the total decay constant of the compound nucleus, and $\tau_{\rm CN} = 1/\lambda_{\rm CN}$ is the compound nucleus lifetime; $\Gamma_f^{(\infty)}$ denotes the transition-state fission width, or the fission width expected when no transient time effects are present. In the following we will use λ 's $(\tau$'s) to refer implicitly to the corresponding decay (time) constants without transient time effects since the effects have been taken care of by the step function $\zeta(t)$.

Now consider a decay chain starting from the compound nucleus (Z, A) with excitation energy E:



where ΔE_i $(i=1,2,\cdots)$ denotes the average energy loss by evaporation of the *i*th neutron. ΔE_i can be estimated as $(B_n + 2T)_i$ where T_i is the temperature of the residual nucleus after *i*th neutron emission and B_n is the corresponding neutron separation energy. Let $\lambda_n^{(i)}$,

 $\lambda_f^{(i)}, \ \lambda_{CN}^{(i)}(=\lambda_n^{(i)}+\lambda_f^{(i)}) \ (i=0,1,2,\cdots)$ be the neutron, fission and total decay constants of the nucleus $(Z, A-i, E-\sum_{i=1}^{j=i} \Delta E_j)$, respectively. The inverse of these decay

constants defines the corresponding characteristic times: $\tau_n^{(i)}$, $\tau_f^{(i)}$, $\tau_{CN}^{(i)}$. Let $N_0(t)$, $N_1(t)$, $N_2(t)$, \cdots , $N_i(t)$, \cdots , be the numbers of nuclei (Z, A), (Z, A - 1), (Z, A - 2), \cdots , (Z, A - i), \cdots , respectively, at time t (starting with N_0 compound nuclei at t = 0: $N_0(0) = N_0$, $N_1(0) = 0$, $N_2(0) = 0$, \cdots). Given a transient time τ_D and assuming a step function for the transient time effects, the number of nuclei (Z, A - i) must satisfy the balance equations:

$$\frac{dN_i(t)}{dt} = \lambda_n^{(i-1)} N_{i-1}(t) - \lambda_n^{(i)} N_i(t), \qquad (t \le \tau_D) \quad (2)$$

$$\frac{dN_i(t)}{dt} = \lambda_n^{(i-1)} N_{i-1}(t) - \lambda_{CN}^{(i)} N_i(t), \quad (t \ge \tau_D) \quad (3)$$

where $\lambda_n^{(i-1)}$ and $\lambda_n^{(i)}$ are the neutron decay constants of the nuclei (Z, A - i + 1) and (Z, A - i), respectively; $\lambda_{CN}^{(i)}$ is the total decay constant of the nucleus (Z, A - i), and $\lambda_{CN}^{(i)} = \lambda_n^{(i)} + \lambda_f^{(i)}$ with $\lambda_f^{(i)}$ being the fission decay constant. The solution of the above equations is straightforward [19]:

$$\frac{N_{i}(t)}{N_{0}} = \sum_{j=0}^{j=i} a_{i,j} \exp(-\lambda_{n}^{(j)} t), \quad (t \leq \tau_{D}) \quad (4)$$

$$a_{i,j} = \frac{\lambda_{n}^{(i-1)} a_{i-1,j}}{\lambda_{n}^{(i)} - \lambda_{n}^{(j)}}, \quad j = 0, 1, 2, \cdots, i-1,$$

$$a_{i,i} = -\sum_{j=0}^{j=i-1} a_{i,j},$$

$$a_{0,0} = 1.0;$$

$$\frac{N_{i}(t)}{N_{0}} = \sum_{j=0}^{j=i} b_{i,j} \exp(-\lambda_{CN}^{(j)} t), \quad (t \geq \tau_{D}) \quad (5)$$

$$b_{i,j} = \frac{\lambda_{CN}^{(i-1)} b_{i-1,j}}{\lambda_{CN}^{(i)} - \lambda_{CN}^{(j)}}, \quad j = 0, 1, 2, \cdots, i-1,$$

$$b_{i,i} = \exp(\lambda_{CN}^{(i)} \tau_{D}) \left[\frac{N_{i}(\tau_{D})}{N_{0}} - \sum_{j=0}^{j=i-1} b_{i,j} \exp(-\lambda_{CN}^{(j)} \tau_{D}) \right],$$

$$b_{0,0} = \exp\left(\left(\lambda_{CN}^{(0)} - \lambda_{n}^{(0)}\right) \tau_{D}\right).$$

This solution, as written above, also provides the algorithm to follow the decay chain until all the excitation energy is exhausted.

With the solution $N_i(t)$ $(i=0,1,2,\cdots)$ in hand, the total fission probabilities P_f^i can be simply calculated as

$$P_f^{t} = \sum_{i=0} P_f^{ith}, \tag{6}$$

$$P_{f}^{i\text{th}} = \int_{\tau_{D}}^{\infty} \lambda_{f}^{(i)} \frac{N_{i}(t)}{N_{0}} dt = P_{f}(Z, A - i, E - \sum_{j=1}^{j=i} \Delta E_{j})$$

$$\times \sum_{j=0}^{j=i} b_{i,j} \frac{\lambda_{\rm CN}^{(i)}}{\lambda_{\rm CN}^{(j)}} \exp(-\tau_D / \tau_{\rm CN}^{(j)}), \tag{7}$$

where
$$\tau_{CN}^{(i)} = 1/\lambda_{CN}^{(i)}$$
, and $P_f(Z, A - i, E - \sum_{j=1}^{j=i} \Delta E_j) =$

 $\lambda_f^{(i)}/\lambda_{CN}^{(i)}$ is the expected (theoretical) first chance fission probability for the compound nucleus (Z, A-i) with excitation energy $E - \sum_{j=1}^{j=i} \Delta E_j$ when no transient time effects are present.

The transition state fission width $\Gamma_f^{(\infty)} = \lambda_f \hbar$ and the neutron decay width $\Gamma_n = \lambda_n \hbar$ can be estimated as [18]

$$\Gamma_f^{(\infty)} \approx T_s \, \frac{\rho_s (E - B_f - E_r^s)}{2\pi \rho_n (E - E_r^{gs})},\tag{8}$$

$$\Gamma_n \approx K T_n^2 \, \frac{\rho_n (E - B_n - E_r^{\rm gs})}{2\pi \rho_n (E - E_r^{\rm gs})},\tag{9}$$

where T_s and T_n are the temperatures of the nucleus at the saddle point and of the residual nucleus after neutron emission, respectively; B_f is the fission barrier; E_r^s and E_r^{gs} are the rotational energies of the system at the saddle and at the ground state, respectively. The constant $K = 2mR^2g'/\hbar^2$ where *m* is the neutron mass, *R* the radius of the residual nucleus after neutron emission, and the spin degeneracy g' = 2. Taking the simplest form for the level density $\rho \propto \exp\left(2\sqrt{aE}\right)$, the level density at the saddle ρ_s and the level density at the ground state ρ_n can be expressed as [18,20]:

$$\rho_s(E - B_f - E_r^{\rm s}) \propto e^{\left(2\sqrt{a_f(E - B_f - E_r^{\rm s} - \Delta E_e)}\right)}, \quad (10)$$
$$\rho_n(E - B_n - E_r^{\rm gs}) \propto$$

$$e^{\left(2\sqrt{a_n(E-B_n-E_r^{g_3}-\Delta_{shell}-\Delta E_c)}\right)}, \quad (11)$$

where B_f is the fission barrier, ΔE_c is the pairing condensation energy, and Δ_{shell} is the ground state shell effect of the daughter nucleus after neutron emission. For an even-even nucleus, $\Delta E_c = (1/2)g\Delta_0^2$; and for an odd A nucleus, $\Delta E_c = (1/2)g\Delta_0^2 - \Delta_0$, where Δ_0 is the gap parameter and g is the doubly-degenerate single particle levels $(g = (3/\pi^2)a$ with a being the level density parameter either at the saddle (a_f) , or at the ground state (a_n)).

The total fission probabilities $P_f^t(Z, A, E)$ of different isotopes at different excitation energies can be determined as the ratio of the fission cross section σ_f to the fusion cross section σ_0 .

We have recently measured with high precision the fission excitation functions of the neighboring compound osmium nuclei 185,186,187,189 Os produced in ³He-induced reactions on isotopically enriched tungsten targets 182,183,184,186 W (see Fig. 1). The isotopic enrichments of the 182 W, 183 W, 184 W and 186 W targets were

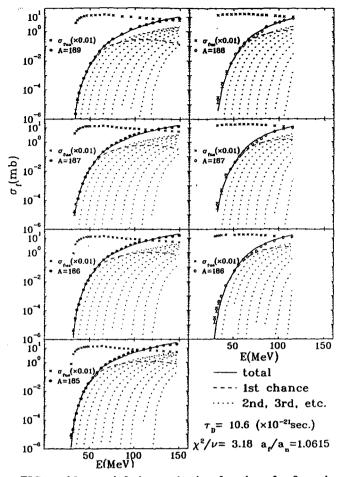


FIG. 1. Measured fission excitation functions for five adjacent Os compound nuclei produced in the ${}^{3}\text{He}(\bullet)/{}^{4}\text{He}(\bullet)$ -induced reactions on W targets. The fusion cross sections (x) are the Bass Model predictions [23]. For each excitation function, the contributions from first, second, third, \cdots chance fission to the total fit (solid line) are shown. The τ_{D} value obtained from this simultaneous fit to seven excitation functions is 10×10^{-21} sec, and a_f/a_n is 1.062.

94.0%, 82.5%, 93.8% and 97.3%, respectively. Fission events were identified by detecting both fission fragments in two large area parallel plate avalanche counters. The experimental details are described in ref. [21]. The statistical errors of the measured fission cross sections σ_{f} are smaller than 2% for the compound nucleus Os isotopes at excitation energies above 50 MeV. Since the fission cross sections for all four isotopes were measured with the same detector setup in a single experiment, the systematic errors are estimated to be small ($\sim 4\%$). The fission excitation functions for compound nuclei 186,187,188Os produced in ⁴He-induced reactions on ^{182,183,184}W targets are also available [22]. All these excitation functions cover an excursion in fission cross section from 10^{-5} mb to 10 mb. The fusion cross sections σ_0 of the above reactions can be estimated with theoretical models such as the Bass Model [23] (see Fig. 1).

We extracted a value for τ_D by fitting simultaneously

all the available fission excitation functions for the compound nuclei (189Os, 188Os, 187Os, 186Os and 185Os) with Eqs. 6 & 7. In order to reduce possible correlations between different parameters, we proceeded as follows. To extract the fission barriers B_{f} , we first fit the low energy (<70 MeV) portion of the fission excitation functions. In this fit, the fission barriers B_f for the nuclei 189,188,187,186,185Os were taken as free parameters. The value of τ_D was set to zero since first chance fission is expected to dominate at low energies. Setting $\tau_D = 0$ reduces the formalism to the form with which the first chance fission probability is usually obtained. The ratio a_f/a_n was assumed to be the same for all nuclei, but its value was let free in the fit. a_n was assumed to be A/8 (MeV^{-1}) , and the shell effects of all nuclei involved were taken to be the nominal values from Möller et al. [24]. The pairing gap parameter Δ_0 was chosen to be 0.85 MeV. The extracted fission barriers yield corresponding liquid-drop values $(B_{\text{macro}} = B_f - \Delta_{\text{shell}})$ which should vary smoothly with the mass number A of the Os isotopes. The barrier values for isotopes lighter than ¹⁸⁵Os can therefore be obtained by a linear extrapolation of the corresponding liquid-drop values of the extracted barriers for ¹⁸⁵⁻¹⁸⁹Os. The fission barriers extracted from this fit, the corresponding liquid-drop values, and their extrapolations for light Os isotopes are shown in Fig. 2.

We now let τ_D free, and fit the complete excitation functions with τ_D and a_f/a_n as the only free parameters, using the fission barriers obtained above as the fixed parameters. In Fig. 1, we show the simultaneous fit for five neighboring osmium compound nuclei among which ¹⁸⁶Os and ¹⁸⁷Os were produced in both ³He- and ⁴Heinduced reactions. All seven fission excitation functions are well reproduced with only two free parameters, and the value obtained for τ_D from this fit is $10(\pm 1) \times 10^{-21}$ sec. This τ_D value is consistent with the conclusion reached from the universal scaling in fission probabilities [18,25], and also consistent with the recent τ_D values reported in [13–16].

The a_f/a_n value given by the fit is 1.062. It is found that fits of comparable quality can be achieved for other a_f/a_n values in a small range centered at 1.062 (see the χ^2 values in the upper panel of Fig. 3). Higher estimates for fission probabilities resulting from a larger a_f/a_n value seem to be (to a substantial extent) compensated by a larger value of τ_D (bottom panel of Fig. 3), and vice versa. This correlation between a_f/a_n and τ_D values makes it difficult to obtain a unique value for τ_D . A good fit can be obtained with a τ_D value as small as zero, but not with a τ_D value larger than 25×10^{-21} sec, above which the fit not only requires an even larger a_f/a_n value (>1.075), but also the χ^2 of the fit become greater than twice the minimum value.

The fusion cross sections σ_0 (see Fig. 1), which were calculated with the Bass Model [23] and used to determine the total fission probability P_f^t in the current analysis, are a source of uncertainty. Unfortunately, no significant experiments are available in the energy regime of

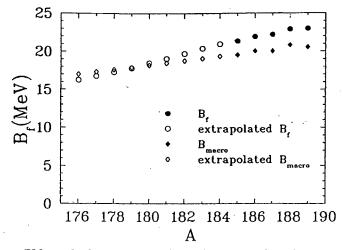


FIG. 2. Os fission barriers (o or •) are plotted vs the mass number A. The fission barriers for A=185-189 (•) were obtained by simultaneously fitting the low energy portion (<70 MeV) of the fission excitation functions shown in Fig. 1 (see text). For A < 185, the fission barriers (o) were obtained by a linear extrapolation (\circ) of the corresponding liquid-drop values $B_f - \Delta_{shell}$ (filled diamond) for the extracted barriers B_f for A=185-189.

interest to this work (>70 MeV), that could be used to judge the correctness of the Bass Model calculations. If the actual fusion cross sections are lower than the Bass predictions, which is likely [19,26], the resulting value for the transient time τ_D will be smaller.

In summary, we have found a new and straightforward way to estimate the transient time of fissioning systems, by utilizing the cumulative fission probabilities of neighboring isotopes. For five Os isotopes, the fission transient time τ_D is estimated to be smaller than 25×10^{-21} sec, and the most likely value of τ_D is about $10(\pm 1) \times 10^{-21}$ sec. The quality of the fit for $\tau_D=0$ is such that no modification of the standard theory is demanded.

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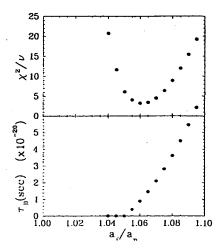


FIG. 3. Bottom panel: The τ_D value extracted from the simultaneous fit with the a_f/a_n value fixed is plotted versus a_f/a_n . Top panel: The χ^2 value per degree of freedom (ν) corresponding to the simultaneous fit with a fixed a_f/a_n value is plotted vs a_f/a_n value.

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