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Evidence for the production of two W bosons with the same electric charge and two jets in 20.3 fb<sup>-1</sup> of pp collisions at  $\sqrt{s} = 8$  TeV using the ATLAS detector

### By

### Alexander Sood

A dissertation submitted in partial satisfaction of the requirements for the degree of

Doctor of Philosophy

in

Physics

in the

Graduate Division

of the

University of California, Berkeley

Committee in charge:

Professor Beate Heinemann, Chair Professor Yury Kolomensky Professor Eric Norman

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#### Abstract

Evidence for the production of two W bosons with the same electric charge and two jets in 20.3 fb<sup>-1</sup> of pp collisions at  $\sqrt{s} = 8$  TeV using the ATLAS detector

by

Alexander Sood

Doctor of Philosophy in Physics

University of California, Berkeley

Professor Beate Heinemann, Chair

This dissertation presents a measurement of  $W^{\pm}W^{\pm}jj$  production in protonproton collisions with a center-of-mass energy of 8 TeV at the Large Hadron Collider using the ATLAS detector. The W bosons are required to decay leptonically, giving a signature of two leptons of the same electric charge, two jets, and missing transverse energy. The analysis is performed on the entire 8 TeV dataset, corresponding to an integrated luminosity of 20.3 fb<sup>-1</sup>. The cross section is measured in two fiducial regions, and an excess over the background-only prediction is observed with a significance of  $4.5\sigma$  for inclusive  $W^{\pm}W^{\pm}jj$  production and  $3.6\sigma$  for electroweak  $W^{\pm}W^{\pm}jj$  production. The measured cross sections are in agreement with Standard Model predictions, and limits are set on anomalous quartic gauge couplings.

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## Chapter 1

# Introduction

One of the major triumphs in the last half century of particle physics has 1 been the successful unified description of the electromagnetic and weak force 2 as a spontaneously broken gauge symmetry. For many years, results from 3 particle colliders provided confirmation of this theory, through the discovery 4 of the W and Z bosons predicted by the theory and by measuring their 5 couplings to matter, but the nature of the symmetry breaking remained a 6 mystery. The Large Hadron Collider (LHC) has begun to shed some light 7 on this subject with the discovery a new spin-0 particle consistent with the 8 HIggs boson of the Standard Model. It could be that the next 30 years of 9 particle physics will follow the previous 30 years with precise measurements 10 of Higgs properties continuing to confirm the Standard Model picture of 11 electroweak symmetry breaking, but it is also possible that there are other 12 new particles that play a role. 13

If these new particles are light enough, they may be observed directly 14 at the LHC, but their effects can also be seen in the scattering of W and Z15 bosons [1,2]  $(VV \to VV)$ , where V = W, Z. Without the Higgs boson, the 16 scattering of longitudinally-polarized bosons violates unitarity at center-of-17 mass energies around 1 TeV [3-5]. If the observed Higgs is not solely re-18 sponsible for electroweak symmetry breaking, there can still be some residual 19 growth of the scattering amplitude with energy that is prevented from vi-20 olating unitarity at higher energies by the presence of additional particles. 21 There are no previous measurements of processes that involve the quartic 22 interaction of W and Z bosons. The theoretical implications of vector bo-23 son scattering (VBS) cross sections combined with the lack of experimental 24 exploration make this an interesting process to study. 25

<sup>26</sup> Figure 1.1 depicts how vector boson scattering occurs at the LHC. This

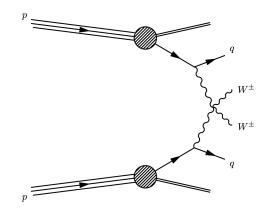


Figure 1.1: Example diagram of WW scattering at the LHC. Two quarks from the incoming protons radiate W bosons which then interact with each other.

leads to a final state that includes not only the two bosons but also two 27 jets due to the quarks. There are several other diagrams that produce the 28 same final state, examples of which are shown in Figure 1.2. The complete 29 set of diagrams can be separated two classes that are each gauge invariant. 30 The first involves only electroweak interactions at leading order and includes 31 vector boson scattering (as shown in Figure 1.1) as well as other diagrams 32 of order  $\alpha_{EW}^4$  like the one shown in Figure 1.2a. This will be referred to 33 as electroweak production. The second, termed strong production, consists 34 of diagrams, like the one shown in Figure 1.2b that contain both strong 35 and electroweak interactions. For most choices of the two vector bosons, 36 electroweak production is hard to measure because it is dwarfed by strong 37 production. However, for two W bosons with the same electric charge, the 38 cross sections for the two kinds of processes are comparable. 39

This dissertation presents a detailed description of the measurement in 40 Ref. [6], which reports the first evidence for the electroweak production of 41 two W bosons with the same electric charge in association with two jets. The 42 measurement is performed using  $20.3 \text{ fb}^{-1}$  of proton-proton collision data 43 with a center-of-mass energy of 8 TeV, provided by the LHC and collected 44 using the ATLAS detector. The W bosons are required to decay leptoni-45 cally  $(W^{\pm} \to \ell^{\pm} \nu)$ , where  $\ell = e, \mu$ ). Since neutrinos escape the interaction 46 point without being detected, this leads to an experimental signature of two 47 leptons with the same electric charge, two jets, and a transverse momentum 48 imbalance. 49

<sup>50</sup> The remaining chapters are organized as follows: Chapter 2 gives a the-

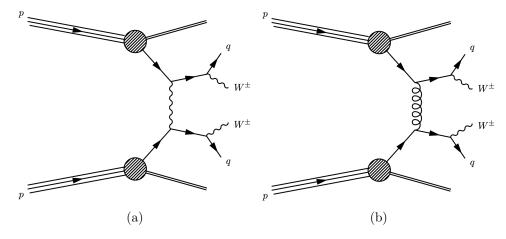


Figure 1.2: Examples of non-VBS diagrams that contribute to (a) electroweak production and (b) strong production of the VVjj final state.

oretical overview of the Standard Model and anomalous gauge couplings. 51 Chapters 3 and 4 describe the LHC and the ATLAS detector. Chapter 5 52 discusses the reconstruction of physical objects from detector data and how 53 events are selected using these objects. Chapter 6 explains how contribu-54 tions to the selected events from various physical processes are estimated. 55 Chapter 7 covers sources of systematic uncertainty on the measurement and 56 how these uncertainties are estimated. Chapter 8 describes a study of jet en-57 ergy scale performance using Z+jet events. The results of the measurement 58 are shown in Chapter 9, and conclusions are presented in Chapter 10. 59

## Chapter 2

# **Theoretical Introduction**

The fundamental constituents of matter and their interactions are described 1 with remarkable accuracy by the Standard Model, which has remained ba-2 sically unchanged for 40 years. In that time, the Standard Model has been repeatedly validated by the discovery of new particles that play important 4 roles in the theory. These discoveries include the W and Z bosons (weak 5 force carriers), the third generation of fermions (needed to get CP violation 6 in the Standard Model), and the Higgs boson (explains particle masses ex-7 cept for neutrinos). The first part of this chapter is devoted to a brief review 8 of the Standard Model. A more complete description of the Standard Model 9 and of quantum field theory, in general, is given in Ref. [7]. 10

While the theory does an outstanding job of describing the phenomena 11 it seeks to explain, the Standard Model also leaves several puzzles unsolved. 12 For example, it contains no description of gravity or dark matter. Though it 13 contains a mechanism for CP violation, the amount is too small to explain 14 the matter/anti-matter asymmetry in the universe. There is no explanation 15 for non-zero neutrino masses and the arbitrary scattering of fermion masses 16 across several orders of magnitude or for why the universe has the symmetry 17 group  $SU(3)_C \otimes SU(2)_L \otimes U(1)_Y$ . Several extensions of the Standard Model 18 have been proposed to explain some of these puzzles. This measurement is 19 not interpreted in the context of a particular model for new physics. Instead, 20 the measured rate of  $W^{\pm}W^{\pm}jj$  production is compared to an effective theory 21 parameterizing the low-energy effects on vector boson scattering from new 22 physics at high energies. Effective theories are described toward the end of 23 the chapter. 24

Particle	Spin	Electric Charge	Color	Mass			
Leptons							
Electron/Muon/Tau	1/2	-1	singlet	$0.511 \ { m MeV}/0.106 \ { m GeV}/1.78 \ { m GeV}$			
Electron/Muon/Tau neutrino	1/2	0	singlet	$< 2~{\rm eV}/{<}$ 0.19 ${\rm MeV}/{<}$ 18 ${\rm MeV}$			
		Quarks					
Up/Charm/Top	1/2	+2/3	triplet	$2.3 { m MeV}/1.28 { m GeV}/173 { m GeV}$			
Down/Strange/Bottom	1/2	-1/3	triplet	$4.8 { m MeV}/95 { m MeV}/4.18 { m GeV}$			
	Gauge Bosons						
Gluon	1	0	octet	0			
Photon	1	0	singlet	0			
W	1	±1	singlet	$80.4 \mathrm{GeV}$			
Z	1	0	singlet	$91.2  {\rm GeV}$			
Higgs	0	0	singlet	$125.6 \mathrm{GeV}$			

Table 2.1: Fundamental particles of the Standard Model [8].

#### 25 2.1 Standard Model

The particles of the Standard Model are summarized in Table 2.1. Matter 26 in the Standard Model is made up of spin-1/2 fermions and comes in three 27 generations. Each generation consists of two quarks, which experience both 28 strong and electroweak interactions, and two leptons, which experience only 29 electroweak interactions. The two quarks contain one up-type quark with 30 an electric charge of Q = +2/3 and one down-type quark with Q = -1/3. 31 while the two leptons are one charged lepton with Q = -1 and one neutrino 32 with Q = 0. The three generations of matter differ only by the masses of the 33 particles. The lightest generation consists of the up (u) quark, the down (d) 34 quark, the electron (e), and the electron neutrino ( $\nu_e$ ). For the second and 35 third generation, the corresponding particles are the charm (c) and top (t) 36 quarks, the strange (s) and bottom (b) quarks, the muon ( $\mu$ ) and tau lepton 37  $(\tau)$ , and their associated neutrinos  $(\nu_{\mu}, \nu_{\tau})$ . 38

Forces in the Standard Model are described by gauge symmetries, which predict the existence of massless spin-1 bosons to mediate these interactions. The boson responsible for carrying the electromagnetic force is the photon  $(\gamma)$ . Eight gluons (g) are the force carriers for the strong nuclear force, and the weak nuclear force is mediated by the  $W^{\pm}$  and Z bosons. The weak bosons are not massless as would be predicted by a plain gauge theory. In fact, they have quite large masses, nearly 100 times the mass of the proton. In the Standard Model, this is explained by a spontaneous breaking of the
electroweak gauge symmetry due to the presence of a spin-0 field. This is
discussed in more detail in Section 2.1.2 and leads to the prediction of one
fundamental spin-0 boson, called the Higgs boson.

#### <sup>50</sup> 2.1.1 Gauge Structure of the Standard Model

The symmetry group of the Standard Model is  $SU(3)_C \otimes SU(2)_L \otimes U(1)_Y$ . 51  $SU(3)_C$  is the symmetry group of the strong interaction while  $SU(2)_L \otimes$ 52  $U(1)_Y$  describes electroweak interactions. Fermions that are charged un-53 der a particular force transform as  $\psi \to e^{i\alpha^a(x)\tau^a}\psi$  under the associated 54 symmetry, where  $\tau^a$  are the generators of that symmetry. Quarks come in 55 three colors that transform as a triplet under  $SU(3)_C$ , left-handed fermions 56 form  $SU(2)_L$  doublets  $\begin{pmatrix} u_L \\ d_L \end{pmatrix}, \begin{pmatrix} \nu_L \\ e_L \end{pmatrix}$ , and all Standard Model fermions carry hypercharge (are charged under  $U(1)_Y$ ). Hypercharge is related to 57 58 electric charge by  $Q = T^3 + Y$ , where  $T^3$  is the  $SU(2)_L$  quantum number of 59 the particle  $(\pm \frac{1}{2})$  for left-handed fermions and 0 for right-handed fermions). 60 These symmetries are required to symmetries of the Lagrangian, but this 61 will clearly not be the case in a theory that involves only fermions. Using 62 the transformation law given above, we get: 63

$$\mathcal{L} = i\bar{\psi}_L\gamma^{\mu}\partial_{\mu}\psi_L + i\bar{\psi}_R\gamma^{\mu}\partial_{\mu}\psi_R - m(\bar{\psi}_L\psi_R + \bar{\psi}_R\psi_L)$$
  

$$\rightarrow i\bar{\psi}_LV^{\dagger}\gamma^{\mu}\partial_{\mu}(V\psi_L) + i\bar{\psi}_RU^{\dagger}\gamma^{\mu}\partial_{\mu}(U\psi_R) - m(\bar{\psi}_LV^{\dagger}U\psi_R + \bar{\psi}_RU^{\dagger}V\psi_L)$$
  

$$= i\bar{\psi}_L\gamma^{\mu}\partial_{\mu}\psi_L + i\bar{\psi}_R\gamma^{\mu}\partial_{\mu}\psi_R + i\bar{\psi}_LV^{\dagger}\gamma^{\mu}\partial_{\mu}(V)\psi_L + i\bar{\psi}_RU^{\dagger}\gamma^{\mu}\partial_{\mu}(U)\psi_R$$
  

$$- m(\bar{\psi}_LV^{\dagger}U\psi_R + \bar{\psi}_RU^{\dagger}V\psi_L)$$
(2.1)

where  $V(x) = e^{i\alpha_L^a(x)\tau_L^a}$  and  $U(x) = e^{i\alpha_R^a(x)\tau_R^a}$  are the transformations 64 for left-handed and right-handed fermions under the symmetry in ques-65 tion. As long as left-handed and right-handed fermions transform in the 66 same way (V = U), the mass term will be invariant, but an extra piece 67 remains from the transformation of the kinetic term. This can be remedied 68 by adding to the Lagrangian a term coupling fermions to new spin-1 parti-69 cles,  $g\bar{\psi}_L\gamma^{\mu}A^a_{\mu}\tau^a\psi_L$ , where g is a dimensionless constant and the symmetry 70 transformation of the new field is given by  $A^a_\mu \tau^a \to V(A^a_\mu \tau^a + \frac{i}{g} \partial_\mu) V^{\dagger}$  (and 71 similarly for the right-handed fermions). This term is also not invariant 72 under the symmetry: 73

$$\mathcal{L}_{int} = g\psi_L \gamma^{\mu} A^a_{\mu} \tau^a \psi_L$$

$$\rightarrow g\bar{\psi}_L V^{\dagger} \gamma^{\mu} V (A^a_{\mu} \tau^a + \frac{i}{g} \partial_{\mu}) V^{\dagger} (V\psi_L)$$

$$= g\bar{\psi}_L V^{\dagger} V \gamma^{\mu} A^a_{\mu} \tau^a V^{\dagger} V \psi_L + i\bar{\psi}_L V^{\dagger} V \gamma^{\mu} \partial_{\mu} (V^{\dagger}) V \psi_L \qquad (2.2)$$

$$= g\bar{\psi}_L \gamma^{\mu} A^a_{\mu} \tau^a \psi_L + i\bar{\psi}_L \gamma^{\mu} (\partial_{\mu} (V^{\dagger} V) - V^{\dagger} \partial_{\mu} (V)) \psi_L$$

$$= g\bar{\psi}_L \gamma^{\mu} A^a_{\mu} \tau^a \psi_L - i\bar{\psi}_L V^{\dagger} \gamma^{\mu} \partial_{\mu} (V) \psi_L$$

but the change in the interaction term is precisely opposite of the change
in the fermion kinetic term, so the sum of the two is invariant. In this way,
imposing gauge symmetries on the Lagrangian implies the existence of one
spin-1 boson for each generator of the symmetry.

So far, the parameter m appearing in the Lagrangian has been inter-78 preted as the physical mass of a fermion while q gives the coupling strength 79 for a particular force. Assuming the coupling is small, cross sections for 80 scattering processes can be calculated using a perturbation series in g. This 81 expansion can be visualized in terms of Feynman diagrams. As an example, 82 consider for the electromagnetic force the process  $e^+e^- \rightarrow \mu^+\mu^-$ . In this 83 case, g is equal the electron charge e. Figure 2.1 shows two diagrams for 84  $e^+e^- \rightarrow \mu^+\mu^-$ , one leading order diagram which has a contribution to the 85 cross section of order  $e^4$  and one diagram at the next order in the expansion, 86 which contributes at order  $e^8$ . 87

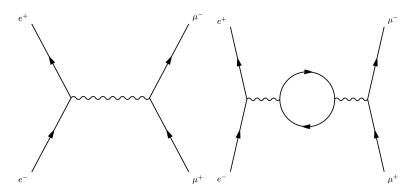


Figure 2.1: Leading-order diagram (left) and an example next-to-leading-order diagram (right) for  $e^+e^- \rightarrow \mu^+\mu^-$ .

When calculating the cross section for this process, we must sum over all possible intermediate states, which includes summing over all possible

momenta for the intermediate particles. For the leading-order diagram, 90 there is only one term in the sum as the momentum of the gauge boson 91 is fixed by momentum conservation. When including next-to-leading-order 92 diagrams, we run into a complication. As can be seen in the right-hand side 93 of Figure 2.1, when there is a closed loop, the number of constraints for 94 momentum conservation is fewer than the number of particles in the loop, 95 leaving the momentum of one of them unconstrained. Since we must sum 96 over all possible momenta, this causes the contribution from this diagram 97 to become divergent. 98

Figure 2.2: Full photon propagator as a perturbation series in the contribution from one-particle-irreducible insertions (top), which sums over all one-particle-insertion diagrams (bottom).

This would seem to be a disaster for the strategy of calculating cross sec-99 tions using perturbative expansions, but these divergences can be reconciled 100 by absorbing them into the Lagrangian parameters. This process is referred 101 to as renormalization. To give an example of how renormalization works, 102 we consider the two example diagrams of  $e^+e^- \rightarrow \mu^+\mu^-$ . The second dia-103 gram can be thought of as a correction to the photon propagator. The full 104 propagator containing all corrections can be written as a geometric series 105 the correction from one-particle-irreducible insertions, diagrams that cannot 106 be split in two by breaking a single line. This is illustrated in Figure 2.2. 107 Summing the geometric series gives a correction factor of: 108

$$\frac{1}{1 - \Pi(q^2)} \tag{2.3}$$

where  $(q^2 q^{\mu\nu} - q^{\mu} q^{\nu}) \Pi(q^2)$  is the contribution of one-particle-irreducible 109 insertions. A photon propagator will always be accompanied by  $e^2$ , so the 110 factor in Equation 2.3 can be interpreted as an effective electromagnetic 111 coupling. Evaluating this contribution requires a method of regularizing 112 divergent integrals over loop momenta. The most common procedure is 113 dimensional regularization [11] in which the integral is evaluated in  $d = 4 - \epsilon$ 114 dimensions. At leading order using dimensional regularization,  $\Pi(q^2)$  is 115 given by: 116

$$\Pi(q^2) = \frac{e^2}{2\pi^2} \int_0^1 dx x (1-x) (\frac{2}{\epsilon} - \log(m_e^2 - x(1-x)q^2) - \gamma)$$
(2.4)

where  $\gamma \approx 0.5772$  is the Euler-Mascheroni constant. This contains a divergent piece that is independent of  $q^2$ . This can be eliminated by rescaling the coupling *e* that appears in the Lagrangian so that:

$$e^2 = \frac{e_0^2}{1 - \Pi(\mu^2)} \tag{2.5}$$

where  $e_0$  is now the parameter appearing in the Lagrangian, which is now distinct from the physical coupling e, and  $\mu^2$  is the renormalization scale, the particular value of  $q^2$  at which the coupling is rescaled. The effective coupling can now be written as:

$$e_{eff}^2 = \frac{e^2}{1 - (\Pi(q^2) - \Pi(\mu^2))}$$
(2.6)

The choice of renormalization scale is an arbitrary one on which physical observables should have no dependence. In practice, the truncation of the perturbation series causes some scale dependence to remain. The degree to which a prediction depends on the renormalization scale is frequently used to provide an estimate of the size of higher-order corrections [74].

Notice that the effective coupling depends on the energy scale of the 129 interaction. This running of the coupling has important consequences for 130 physics at the LHC. The effective coupling for the strong force increases with 131 decreasing energy so that that coupling becomes  $\mathcal{O}(1)$  at an energy scale of 132  $\sim 1$  GeV. This leads to a phenomenon known as "confinement" for quarks 133 and gluons. As two colored particles move apart, it becomes energetically 134 favorable to produce a new  $q\bar{q}$  pair from the vacuum. As a result, only 135 colorless combinations of these particles are able to propagate freely. Quarks 136 and gluons are therefore confined to these colorless combinations, called 137 hadrons. As the energy scale increases to hundreds of GeV, the effective 138 coupling decreases to  $\mathcal{O}(0.1)$ . This frees quarks and gluons at this energy 139 from their confinement to hadrons. This is known as "asymptotic freedom." 140 The running of the strong coupling has been confirmed experimentally as 141 shown in Figure 2.3, where  $\alpha_s = \frac{g_s^2}{4\pi}$ . 142

Both asymptotic freedom and confinement are important at the LHC. Protons are collided at very high energies, where the quarks and gluons are asymptotically free. A quark or gluon scattered away from the interaction

point will begin to radiate, creating more gluons and  $q\bar{q}$  pairs with lower 146 energy until they reach the scale of confinement and become grouped into 147 hadrons. This shower of hadrons, collimated in the direction of the original 148 quark/gluon, is what is reconstructed in the detector and is termed a "jet." 149 In order to make predictions, it is important to have a good understanding of 150 both the initial hard scatter and jet formation. The former can be treated 151 perturbatively while the latter is done with parton shower models, which 152 handle the radiation of particles from an outgoing quark/gluon one at time, 153 starting with the widest-angle or highest-transverse-momentum radiation. 154 The ability to treat the short-distance physics (the hard scatter) and long-155 distance physics (the parton shower) independently is called factorization. 156 The energy scale at which the switch is made from perturbative treatment 157 to parton showering is called the factorization scale. 158

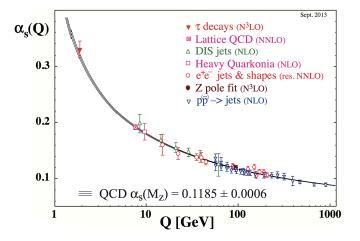


Figure 2.3: Measurements of the strong coupling  $\alpha_s$  at energies ranging from  $\sim 2$  GeV almost up to 1 TeV [8].

The electroweak couplings are much weaker than the strong coupling, 159 so electroweak interaction does not pose the same calculational difficulties 160 at low energies, and unlike for strong interactions, the effective coupling 161 increases with energy. But the electroweak symmetry presents a new chal-162 lenge: it must be broken in order to explain why particles have mass. To 163 begin with, the bosons of unbroken gauge theories must be massless because 164 the addition of a mass term for the boson would violate gauge invariance. 165 This is easiest to see using the infinitesimal transformation law for the vector 166 fields,  $A^a_\mu \to A^a_\mu + \frac{1}{g} \partial_\mu \alpha^a + f^{abc} A^b_\mu \alpha^c$ , where the structure constant  $f^{abc}$  is 167

168 defined by  $[\tau^a, \tau^b] = i f^{abc} \tau^c$ .

$$\frac{1}{2}m^2 A^a_\mu A^{\mu a} \rightarrow \frac{1}{2}m^2 (A^a_\mu + \frac{1}{g}\partial_\mu\alpha^a + f^{abc}A^b_\mu\alpha^c)(A^{\mu a} + \frac{1}{g}\partial^\mu\alpha^a + f^{aij}A^{\mu i}\alpha^j)$$
$$= \frac{1}{2}m^2 (A^a_\mu A^{\mu a} + 2f^{abc}A^b_\mu\alpha^c A^{\mu a} + \frac{2}{g}A^a_\mu\partial^\mu\alpha^a) + \mathcal{O}(\alpha^2)$$
(2.7)

where we see that an  $\mathcal{O}\alpha$  rotation of the fields produces an  $\mathcal{O}\alpha$  change 169 to the Lagrangian. This requirement of massless bosons is inconsistent with 170 the observed masses of the W and Z bosons, and the electroweak interac-171 tion has a further complication that only left-handed fermions are charged 172 under  $SU(2)_L$ . Left-handed and right-handed fermions also have different 173 hypercharges. Recall that fermion mass terms are only gauge invariant if 174 the transformations for left-handed and right-handed fermions are the same. 175 So imposing electroweak gauge symmetry requires fermions to be massless 176 as well. In order for the Standard Model to be consistent with the observed 177 masses for fermions and W and Z bosons, a mechanism must be intro-178 duced to break  $SU(2)_L \otimes U(1)_Y$ . And since the photon remains massless, 179 this symmetry breaking mechanism must also leave intact a U(1) symmetry 180 corresponding to electromagnetism. 181

#### <sup>182</sup> 2.1.2 Electroweak Symmetry Breaking

In the Standard Model, electroweak symmetry is spontaneously broken using the Higgs mechanism. A complex scalar is introduced that has a hypercharge of 1/2 and transforms as a doublet under  $SU(2)_L$ . Then the following terms are added to the Lagrangian:

$$\Delta \mathcal{L}_{kinetic} = (D_{\mu}\phi)^{\dagger} D^{\mu}\phi \qquad (2.8)$$

187

$$\Delta \mathcal{L}_{potential} = -\mu^2 |\phi|^2 + \lambda |\phi|^4 \tag{2.9}$$

where  $D_{\mu} = \partial_{\mu} - ig \frac{\sigma^a}{2} W^a_{\mu} - i \frac{g'}{2} B_{\mu}$ . If  $\mu^2$  and  $\lambda$  are both positive, then the ground state will have a non-zero vacuum expectation value ("VEV"). Since the potential only depends on the magnitude of  $\phi$ , there are many degenerate vacua, but only one of them can be the vacuum of our universe. By gauge invariance, coordinates can be chosen so that VEV is  $\langle \phi \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v \end{pmatrix}$ , where  $v = \sqrt{\mu^2/\lambda}$ . The choice of orientation of the VEV breaks the electroweak symmetry, leaving behind the gauge symmetry of electromagnetism. Putting
the VEV back into the kinetic term gives mass terms for the gauge bosons.

$$\Delta \mathcal{L} = \langle \phi \rangle (ig \frac{\sigma^a}{2} W^a_\mu + i \frac{g'}{2} B_\mu) (-ig \frac{\sigma^b}{2} W^b_\mu - i \frac{g'}{2} B_\mu) \langle \phi \rangle$$
  
=  $\frac{v^2}{2} (\frac{g^2}{4} W^a_\mu W^{\mu a} + \frac{g'^2}{4} B_\mu B^\mu + \frac{gg'}{2} W^3_\mu B^\mu)$  (2.10)

The mass matrix the gauge bosons,  $(W^a_\mu, B_\mu)$ , is:

$$\frac{v^2}{4} \begin{pmatrix} g^2 & 0 & 0 & 0\\ 0 & g^2 & 0 & 0\\ 0 & 0 & g^2 & gg'\\ 0 & 0 & gg' & g'^2 \end{pmatrix}$$
(2.11)

which is invariant under rotations of the  $W^a_{\mu}$  fields. This remaining global SU(2) symmetry is referred to as "custodial symmetry" [91]. In the absence of hypercharge, this would imply equal masses for all of the weak gauge bosons, but mixing between the  $W^3_{\mu}$  and  $B_{\mu}$  fields shifts the mass of the neutral weak boson. Diagonalizing the matrix, the mass eigenstates of the gauge fields are

$$W^{\pm}_{\mu} = \frac{1}{\sqrt{2}} (W^{1}_{\mu} \mp i W^{2}_{\mu}), \ m_{W} = \frac{gv}{2}$$
(2.12)

203

$$Z_{\mu} = \frac{1}{\sqrt{g^2 + g'^2}} (gW_{\mu}^3 - g'B_{\mu}), \ m_Z = \frac{v}{2}\sqrt{g^2 + g'^2}$$
(2.13)

204

$$A_{\mu} = \frac{1}{\sqrt{g^2 + g'^2}} (g' W_{\mu}^3 + g B_{\mu}), \ m_A = 0$$
 (2.14)

giving three massive gauge bosons corresponding to the three broken generators of  $SU(2)_L \otimes U(1)_Y$  and one massless boson corresponding to the unbroken  $U(1)_{EM}$ . The W and Z bosons now have mass, but what about fermions? Masses for the fermions are generated in a similar manner, by introducing terms coupling the Higgs field to matter.

$$\Delta \mathcal{L} = -y_d (\bar{q}_L \dot{\phi}) d_R - y_u (\epsilon^{ab} \bar{q}_{La} \phi_b^{\dagger}) u_R + h.c.$$
(2.15)

where  $q_L = \begin{pmatrix} u_L \\ d_L \end{pmatrix}$ . The  $SU(2)_L$  indices of  $\phi$  and  $q_L$  are contracted and, the hypercharges sum to zero (e.g.  $-Y^{q_L} + Y^{\phi} + Y^{d_R} = -\frac{1}{6} + \frac{1}{2} - \frac{1}{3} = 0$ ), avoiding both problems that prevented the inclusion of  $\bar{q}_L d_R$  and similar terms. Once again, mass terms arise from the non-zero Higgs VEV.

$$\begin{aligned} \Delta \mathcal{L} &= -y_d (\bar{q}_L \cdot \langle \phi \rangle) d_R - y_u (\epsilon^{ab} \bar{q}_{La} \langle \phi \rangle_b^{\dagger}) u_R + h.c. \\ &= -\frac{1}{\sqrt{2}} y_d (\begin{pmatrix} \bar{u}_L \\ \bar{d}_L \end{pmatrix} \cdot \begin{pmatrix} 0 \\ v \end{pmatrix}) d_R - \frac{1}{\sqrt{2}} y_u (\epsilon^{ab} \begin{pmatrix} \bar{u}_L \\ \bar{d}_L \end{pmatrix}_a \begin{pmatrix} 0 \\ v \end{pmatrix}_b) u_R + h.c. \\ &= -y_d \frac{v}{\sqrt{2}} \bar{d}_L d_R - y_u \frac{v}{\sqrt{2}} \bar{u}_L u_R + h.c. \end{aligned}$$

$$(2.16)$$

So far we have recovered the particle masses we needed by inserting the VEV for the Higgs field. A natural question to ask is whether the addition of this new field leads to any new phenomena that we can observe. Expanding around the minimum of the Higgs potential, we have  $\phi = \begin{pmatrix} w^1(x) + iw^2(x) \\ v + h(x) + iw^3(x) \end{pmatrix}$ . Inserting this into the potential, we get:

$$\Delta \mathcal{L}_{potential} = \frac{-\mu^2}{2} [(v+h)^2 + w^a w^a] + \frac{\lambda}{4} [(v+h)^2 + w^a w^a]^2$$
  
=  $(\lambda v^3 - \mu^2 v)h + \frac{1}{2} (3\lambda v^2 - \mu^2)h^2 + \frac{1}{2} (\lambda v^2 - \mu^2) w^a w^a$   
+  $\lambda v (h^3 + h w^a w^a) + \frac{\lambda}{4} (h^4 + 2h^2 w^a w^a)$   
=  $\frac{1}{2} (2\lambda v^2)h^2 + \lambda v (h^3 + h w^a w^a) + \frac{\lambda}{4} (h^4 + 2h^2 w^a w^a)$  (2.17)

The mass terms for the  $w^a$  fields vanish while the remaining field acquires 219 a mass of  $m_h = \sqrt{2\lambda v^2}$ . The three massless fields are not independent 220 physical particles but are "eaten" to become the longitudinal polarizations 221 of the W and Z bosons. The massive scalar field that remains is referred 222 to as the Higgs boson. In another triumph for the Standard Model, a new 223 particle with a mass of 125 GeV and properties consistent with the Higgs 224 boson was discovered by the ATLAS and CMS collaborations at the LHC in 225 2012 [9,10]. Going back to Equations 2.10 and 2.16 and substituting v + h226 for v, we see that the couplings of the Higgs boson to vector bosons and 227 fermions are: 228

$$\begin{split} \Delta \mathcal{L}_{boson} &= \frac{(v+h)^2}{2} (\frac{g^2}{4} W^a_\mu W^{\mu a} + \frac{g'^2}{4} B_\mu B^\mu + \frac{gg'}{2} W^3_\mu B^\mu) \\ &= \frac{(v+h)^2}{2} (\frac{g^2}{2} W^+_\mu W^{-\mu} + \frac{g^2 + g'^2}{4} Z_\mu Z^\mu) \\ &\supset \frac{2m_W^2}{v} h W^+_\mu W^{-\mu} + \frac{m_Z^2}{v} h Z_\mu Z^\mu + \frac{m_W^2}{v^2} h^2 W^+_\mu W^{-\mu} + \frac{m_Z^2}{2v^2} h^2 Z_\mu Z^\mu \end{split}$$
(2.18)

$$\Delta \mathcal{L}_{fermion} = -y_f \frac{v+h}{\sqrt{2}} \bar{f}_L f_R + h.c.$$
  
$$\supset -\frac{m_f}{v} h \bar{f}_L f_R + h.c.$$
 (2.19)

where f runs over all fermions. The coupling of the Higgs boson to other Standard Model particles is proportional particle's mass. We therefore expect the inclusion of the Higgs boson to have the largest effects on processes involving heavy vector bosons or top quarks.

<sup>233</sup> A quick aside on Mandelstam variables, three quantities that are defined <sup>234</sup> for  $2\rightarrow 2$  scattering processes as follows:

$$s = (p_i + k_i)^2 = (p_f + k_f)^2$$
  

$$t = (p_f - p_i)^2 = (k_f - k_i)^2$$
  

$$u = (k_f - p_i)^2 = (p_f - k_i)^2$$
  
(2.20)

where  $p_i$  and  $k_i$  are the momenta of the initial state particles and  $p_i$  and 235  $k_i$  are the momenta of the final state particles. Amplitudes are often ex-236 pressed in terms of these variables in order to ease the use crossing symmetry, 237 the equivalence between having a particle with momentum p in the initial 238 state and having its antiparticle with momentum -p in the final state, in 239 determining the amplitudes for two similar processes without going through 240 both calculations. For diagrams in which a single virtual particle with mo-241 mentum q is exchanged,  $q^2$  will be equal to one of the Mandelstam variables. 242 It is common to refer to such diagrams as belonging to the s/t/u-channel, 243 a convention I will adopt in a moment. 244

The Higgs boson plays a very important role in vector boson scattering (VBS). The non-Abelian nature of the electroweak gauge symmetry gives rise to interactions among the corresponding gauge bosons, allowing them to scatter off each other. The three leading-order diagrams for  $W^{\pm}W^{\pm}$  scattering, not involving the Higgs boson, are shown in Figure 2.4. If these were the only contributions, the scattering of longitudinally-polarized vector bosons would present a problem at high energies. Expressions for the amplitude of these diagrams can be written using the Feynman rules for electroweak diagrams:

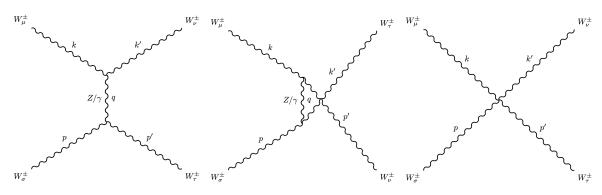


Figure 2.4: Leading order diagrams for  $W^{\pm}W^{\pm}$  scattering involving triple gauge couplings in the *t*-channel (left) and *u*-channel (middle) and quartic gauge couplings (right).

t-channel diagram:  $i\mathcal{M} = i\hat{\epsilon}_{\mu}(k)\hat{\epsilon}_{\nu}^{*}(k')[g^{\mu\nu}(k-k')^{\rho} - g^{\mu\rho}(q+k)^{\nu} + g^{\rho\nu}(q+k')^{\mu}] \times \left(\frac{g^{2}c_{W}^{2}}{q^{2} - m_{Z}^{2}} + \frac{g^{2}s_{W}^{2}}{q^{2}}\right)g_{\lambda\rho} \times \left[g^{\sigma\tau}(p-p')^{\lambda} - g^{\sigma\lambda}(q+p)^{\tau} + g^{\lambda\tau}(q+p')^{\sigma}]\hat{\epsilon}_{\sigma}(p)\hat{\epsilon}_{\tau}^{*}(p')\right]$  (2.21)

$$u-\text{channel diagram}:$$

$$i\mathcal{M} = i\hat{\epsilon}_{\mu}(k)\hat{\epsilon}_{\nu}^{*}(p')[g^{\mu\nu}(k-p')^{\rho} - g^{\mu\rho}(q+k)^{\nu} + g^{\rho\nu}(q+p')^{\mu}] \times \left(\frac{g^{2}c_{W}^{2}}{q^{2} - m_{Z}^{2}} + \frac{g^{2}s_{W}^{2}}{q^{2}}\right)g_{\lambda\rho} \times \left[g^{\sigma\tau}(p-k')^{\lambda} - g^{\sigma\lambda}(q+p)^{\tau} + g^{\lambda\tau}(q+k')^{\sigma}]\hat{\epsilon}_{\sigma}(p)\hat{\epsilon}_{\tau}^{*}(k')\right]$$

$$(2.22)$$

quartic coupling diagram:  

$$i\mathcal{M} = ig^2 \hat{\epsilon}_{\mu}(k) \hat{\epsilon}^*_{\nu}(k') \hat{\epsilon}_{\sigma}(p) \hat{\epsilon}^*_{\tau}(p') (2g^{\mu\nu}g^{\sigma\tau} - g^{\mu\sigma}g^{\nu\tau} - g^{\mu\tau}g^{\nu\sigma})$$
(2.23)

where  $\{\epsilon\}$  are the polarization vectors of the W bosons,  $\{p, k\}$  are their 254 momenta, and  $c_W$  and  $s_W$  are the cosine and sine of the weak mixing angle, 255 defined in terms of the weak and hypercharge couplings by  $s_W = \frac{g'}{\sqrt{g^2 + {g'}^2}}$ . 256 Now let us consider the case when the W bosons are longitudinally polarized. 257 For a boson with momentum  $k_{\mu} = (E_k, 0, 0, k)$  the longitudinal polarization 258 vector is given by  $\hat{\epsilon}_{\mu} = (\frac{k}{m}, 0, 0, \frac{E_k}{m})$ . In the limit that the momentum is 259 much larger than the mass of the particle, this polarization vector becomes 260 proportional to the momentum. 261

$$\hat{\epsilon}_{\mu} = \left(\frac{k}{m}, 0, 0, \frac{E_k}{m}\right)$$

$$= \frac{1}{m} \left(E_k \sqrt{1 - \frac{m^2}{E_k^2}}, 0, 0, k \sqrt{1 + \frac{m^2}{k^2}}\right)$$

$$= \frac{k^{\mu}}{m} + \mathcal{O}\left(\frac{m}{E_k}\right)$$
(2.24)

Substituting the large momentum limit for the longitudinal polarization vectors into the expressions for the scattering amplitudes, we can see that, to leading order in  $\frac{s}{m_W^2}$ , each diagram has a contribution of order  $\frac{s^2}{m_W^4}$ . When summing over the diagrams, these contributions cancel, but the terms of order  $\frac{s}{m_W^2}$  do not. For a 2  $\rightarrow$  2 scattering process with particles of equal masses, the cross section in the center-of-mass frame can be written as:

$$\sigma = \frac{1}{32\pi^2 s} \int d\Omega \sqrt{1 - \frac{4m^2}{s}} |\mathcal{M}|^2 \tag{2.25}$$

Here we see that if the amplitude is proportional to  $\frac{s}{m_W^2}$ , the cross section will also be proportional to  $\frac{s}{m_W^4}$ . The indefinite growth of the cross section with energy will eventually violate unitarity, meaning that the predicted probability for vector boson scattering in pp collisions will exceed unity. For vector boson scattering, this occurs at energies near 1 TeV [3–5].

In the Standard Model, VBS can also proceed through the exchange of a
Higgs boson, as shown in Figure 2.5. The contributions from Higgs exchange
are:

$$t-\text{channel diagram}:$$
  
$$i\mathcal{M} = -ig^2 m_W^2 \frac{\hat{\epsilon}_\mu(k)\hat{\epsilon}_\nu^*(k')g^{\mu\nu}g^{\sigma\tau}\hat{\epsilon}_\sigma(p)\hat{\epsilon}_\tau^*(p')}{q^2 - m_h^2}$$
(2.26)

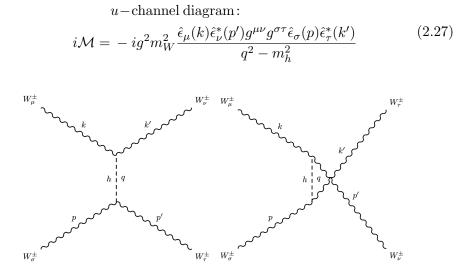


Figure 2.5: Vector boson scattering diagrams with Higgs exchange in the t-channel (left) and u-channel (right).

Putting in the longitudinal polarization vectors, we get the amplitude of these diagrams to go as  $\frac{s}{m_W^2}$ , but with the opposite sign. The contribution from these diagrams exactly cancels the  $\frac{s}{m_W^2}$  contribution from the diagrams involving only the gauge bosons. The combined amplitude asymptotes to a constant as *s* increases, leading to a cross section that decreases with energy, thereby preserving unitarity.

### 282 2.2 $W^{\pm}W^{\pm}jj$ Production at the LHC

In this dissertation,  $W^{\pm}W^{\pm}jj$  production is the process chosen for studying electroweak symmetry breaking. The Standard Model description of  $W^{\pm}W^{\pm}jj$  production is tested by comparing the observed number of events passing some selection criteria to the theoretical prediction. The predicted number of events can be expressed as follows:

$$N = \int \mathcal{L}dt \cdot \sigma \cdot A \cdot \epsilon \tag{2.28}$$

where  $\mathcal{L}$  is the luminosity, a measure of the collision rate discussed further in Chapter 3,  $\sigma$  is the cross section for the  $W^{\pm}W^{\pm}jj$  process, the rate

at which  $W^{\pm}W^{\pm}jj$  production occurs in pp collisions, A is the acceptance, 290 the fraction of  $W^{\pm}W^{\pm}ii$  events that would pass all selections given a per-291 fectly efficient detector, and  $\epsilon$  is the efficiency to reconstruct events within 292 the acceptance. The portion of the phase space of the final state particles 293 that pass the selection criteria is referred to as the "fiducial phase space," 294 and the product  $\sigma \cdot A$ , which gives the rate to produce events in this phase 295 space, is referred to as the "fiducial cross section." Luminosity is indepen-296 dent of the physical process under consideration (see Chapter 3), and the 297 efficiency is determined by simulating the interaction of final state particles 298 with the detector. What must be provided by the theoretical calculation is 299 the fiducial cross section for  $W^{\pm}W^{\pm}jj$  production. 300

For a given two initial partons, the cross section for  $W^{\pm}W^{\pm}jj$  production can be computed as follows. Working in the center-of-mass frame and neglecting quark masses, the cross section can be written as:

$$\sigma = \frac{1}{2E_{CM}^2} \int \left(\prod_f \frac{d^3 p_f}{(2\pi)^3} \frac{1}{2E_f}\right) |\mathcal{M}(\{p_f\})|^2 (2\pi)^4 \delta^4(\sum p_f)$$
(2.29)

where  $\{p_f\}$  and  $\{E_f\}$  are the momenta and energy of the final state 304 particles,  $E_{CM}$  is the center-of-mass energy of the collision, and  $|\mathcal{M}|^2$  is the 305 scattering amplitude for producing final state particles with momenta  $\{p_f\}$ . 306 All of the information about the interactions in the theory is contained in 307  $\mathcal{M}$ , which sums over all diagrams with identical initial and final states as 308 shown in Figure 2.6. The number of diagrams in the sum is infinite, but since 309 both the electroweak and strong couplings are small at LHC energies, a good 310 approximation can be obtained by neglecting terms that have higher powers 311 of the couplings. The predictions used for this measurement truncate the 312 sum at leading order in the electroweak coupling and next-to-leading order 313 in the strong coupling. 314

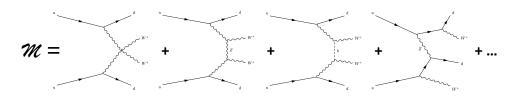


Figure 2.6: A few leading order diagrams for electroweak  $W^{\pm}W^{\pm}jj$  production.

The  $W^{\pm}W^{\pm}jj$  process can be split into electroweak production, which

contains diagrams of order  $\alpha_{EW}^4$  in the coupling strengths, and strong pro-316 duction, which contains diagrams of order  $\alpha_{EW}^2 \alpha_s^2$ . Representative diagrams 317 for both are shown in Figure 1.2. In both cases, the incoming quarks scatter 318 off of each other through the exchange of vector bosons. The color connec-319 tion forged between the quarks in the strong production mechanism pulls 320 them closer together, causing them to scatter at large angles with respect to 321 the beam direction. But for electroweak production, there is no color flow, 322 and the quarks scatter at smaller angles. This difference between the pro-323 duction mechanisms provides a powerful tool for separating the two using 324 kinematic selections. 325

The particles being collided at the LHC are not quarks but protons 326 containing a mixture of quarks and gluons. Translating cross sections for qq327 initial states into a cross section for a pp initial state is done using parton 328 distribution functions (PDFs). The PDF for a parton gives the probability 329 density to find that parton carrying a particular fraction of the proton's 330 momentum. PDFs also depend on the energy of the collision. Let  $f_i(x, Q^2)$ 331 and  $f_i(y, Q^2)$  be the proton PDFs for partons i and j, where x/y denote 332 the fraction of the proton's momentum the each parton is carrying and Q333 is the collision energy. In the case of two partons colliding at the LHC, 334  $Q = (x + y)E_{beam}$ , where  $E_{beam}$  is the energy of each proton beam. The 335 expression for the cross section in Equation 2.29 depends on the identities 336 and center-of-mass energy of the two partons:  $\sigma = \sigma_{ij}((x+y)E_{beam})$ . In 337 order to translate this into a cross section for the pp center-of-mass energy, 338 the cross section must be weighted by the probability of picking out in a 339 given collision partons i and j carrying fractions x and y of the momenta of 340 the two protons, and we must sum over all possible combinations of i, j, x, 341 and y. Then the cross section for pp collisions is given by: 342

$$\sigma_p p = \sum_{\langle ij \rangle} \int_0^1 \int_0^1 dx dy f_i(x, ((x+y)E_{beam})^2) f_j(y, ((x+y)E_{beam})^2) \sigma_{ij}((x+y)E_{beam})$$
(2.30)

Figure 2.7 shows two examples of PDFs at different energies. The PDFs 343 used in this analysis are estimated using fits to deep inelastic scattering 344 data from the HERA  $e^{\pm}p$  collider and data on single-inclusive jet produc-345 tion, Z rapidity distributions, and asymmetry in the rapidity distribution 346 of the charged lepton in  $W \to \ell \nu$  events from the Tevatron  $p\bar{p}$  collider [12]. 347 Systematic uncertainties on the fitted parameters are provided in the form 348 of alternate PDFs that correspond to one-dimensional 90% confidence level 349 limits. There are 26 free parameters in the fit, and positive and negative 350

variations along a given direction in the parameter space are allowed to be asymmetric, so the total PDF set (central value + systematic variations)

<sup>353</sup> contains 53 functions.

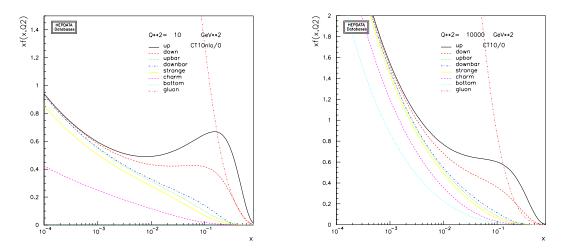


Figure 2.7: CT10 parton distribution functions for  $Q^2 = 10 \text{ GeV}^2$  and  $Q^2 = 10000 \text{ GeV}^2$  [13].

The production of two W boson with the same charge requires an ini-354 tial state with two quarks whose charges must be either both positive or 355 both negative. As can be seen from Figure 2.7, the dominant contribution 356 to  $W^+W^+$  production at the LHC comes from the uu initial state while 357  $W^-W^-$  is most often produced in collisions between two down quarks. If 358 approximate the proton as just consisting of the three valence quarks (uud)359 each carrying an equal fraction of the proton's momentum, a simple count-360 ing of the possible combinations predicts that the cross section for  $W^+W^+$ 361 production will be four times higher for  $W^-W^-$  production. This is not far 362 off from the prediction obtained using the full set of PDFs, which produces 363 a  $W^+W^+/W^-W^-$  ratio of 3.3. 364

#### <sup>365</sup> 2.3 Anomalous Quartic Gauge Couplings

The discovery of a Higgs boson at the LHC marks an important milestone in our understanding of electroweak symmetry breaking, but it does not necessarily represent the finish line. Precise measurements of the couplings of the Higgs to other particles may reveal differences with the Standard Model expectation. This would require some new physics to explain the values of the W and Z masses and to help regulate the scattering of longitudinallypolarized vector bosons. In lieu of a specific theory, the effects of new physics on VBS can be parameterized as anomalous couplings among the gauge bosons.

#### 375 2.3.1 Effective Field Theory

The effective field theory approach assumes that the Standard Model is the 376 correct low-energy theory of nature and estimates the effects of new physics 377 present at high energies using higher dimensional operators constructed from 378 the Standard Model fields. An example of a successful effective field theory 379 is the Fermi theory for weak interactions. Since the action  $S = \int \mathcal{L} d^4 x$ 380 is a dimensionless quantity, terms in the Lagrangian must dimensions of 381  $(mass)^4$ . The mass dimensions of the various fields can then be easily deter-382 mined from the mass terms in the Lagrangian: fermions have dimension- $\frac{3}{2}$ 383 while scalars and vector bosons are both dimension-1. When adding higher 384 dimensional operators to the Lagrangian, the coefficients of these operators 385 acquire dimensions of inverse mass and can be written as  $\frac{c}{\Lambda^{d-4}}$ , where c is 386 a dimensionless coupling,  $\Lambda$  is the energy scale of new physics, and d is the 387 dimension of the operator, determined from the combination of fields and 388 derivatives. Since these operators are suppressed by the energy scale  $\Lambda$ , the 389 Standard Model is recovered in the limit that the collision energy goes to 390 zero. Another important feature to note is that higher-dimension operators 391 are suppressed by greater powers of  $\Lambda$ , so operators of higher dimension than 392 the ones under consideration can be safely neglected. 393

The lowest dimension operators that contribute to aTGCs and aQGCs have dimension six and are listed in Ref. [36]. For operators that give aQGCs without aTGCs, the lowest dimension is dimension eight [35]. The simplest dimension-8 operators that give rise to aQGCs are:

$$\mathcal{L}_{S,0} = \frac{f_{S,0}}{\Lambda^4} \left[ (D_\mu \phi)^\dagger D_\nu \phi \right]^2 \tag{2.31}$$

398

$$\mathcal{L}_{S,1} = \frac{f_{S,1}}{\Lambda^4} \left[ (D_\mu \phi)^\dagger D^\mu \phi \right]^2 \tag{2.32}$$

While there is no general conversion between these parameters and the a parameters of the electroweak chiral Lagrangian, they are related for a given vertex by a simple linear transformation [36]. The relationship for the WWWW vertex is:

$$\frac{f_{S,0}}{\Lambda^4} \frac{v^4}{8} = \alpha_4 \tag{2.33}$$

$$\frac{f_{S,1}}{\Lambda^4} \frac{v^4}{8} = \alpha_4 + 2\alpha_5 \tag{2.34}$$

#### 404 2.3.2 The Electroweak Chiral Lagrangian

The electroweak chiral Lagrangian [14] offers a more general description of 405 electroweak symmetry breaking that starts with only the three scalar degrees 406 of freedom that get cannibalized to become the longitudinal polarizations 407 of the W and Z. Instead of a scalar doublet, a SU(2) matrix is intro-408 duced:  $\Sigma(x) = e^{\frac{-i}{2v}\sigma^a w^a(x)}$ , where v is the symmetry breaking scale. Since 409 this is a unitary matrix, the potential  $V(\Sigma^{\dagger}\Sigma)$  is a constant, leaving terms 410 constructed from derivatives of the  $\Sigma$  fields as the only non-trivial ones that 411 can be added to the Lagrangian. In order for these new terms to be Lorentz-412 invariant, they must have an even number of derivatives.  $\Sigma$  is dimensionless, 413 so the lowest-order operators, which contain two derivatives will be dimen-414 sion 2. Therefore, the coefficients of these operators must have dimensions 415 of  $\Lambda^2$ . The two possible dimension-2 operators that can be constructed are 416  $\mathcal{L}_{0} = \frac{v^{2}}{4} Tr \left[ (D_{\mu}\Sigma)^{\dagger} D^{\mu}\Sigma \right] \text{ and } \mathcal{L}_{1}' = \beta_{1}g^{2}\frac{v^{2}}{4}Tr \left[ (D_{\mu}\Sigma)\frac{\sigma^{3}}{2}\Sigma^{\dagger} \right]^{2}. \mathcal{L}_{1}' \text{ violates}$ custodial symmetry and would cause a deviation from  $\rho = \frac{m_{W}}{m_{Z}c_{W}} = 1$ . Since 417 418  $\rho$  has been measured to be unity to within 0.05% [8], this operator is strongly 419 constrained. By expanding  $\Sigma$  around  $w^a = 0$  we can see that the term  $\mathcal{L}_0$ 420 gives rise to mass terms for the gauge bosons. 421

$$\mathcal{L}_{0} = \frac{v^{2}}{4} Tr \left[ (D_{\mu}(1 + \mathcal{O}(w)))^{\dagger} D^{\mu}(1 + \mathcal{O}(w)) \right]$$
  
$$= \frac{v^{2}}{4} Tr \left[ (ig \frac{\sigma^{a}}{2} W_{\mu}^{a} + i \frac{g'}{2} B_{\mu}) (-ig \frac{\sigma^{b}}{2} W_{\mu}^{b} - i \frac{g'}{2} B_{\mu}) \right] + \mathcal{O}(w) \qquad (2.35)$$
  
$$= \frac{v^{2}}{2} (\frac{g^{2}}{4} W_{\mu}^{a} W^{\mu a} + \frac{g'^{2}}{4} B_{\mu} B^{\mu} + \frac{gg'}{2} W_{\mu}^{3} B^{\mu}) + \mathcal{O}(w)$$

which are exactly the same mass terms we got in Section 2.1.2. This framework is clearly desirable for a theory without a light Higgs, but it is still useful for parameterizing anomalous couplings in theories including a Higgs. A scalar resonance can be added to include the observed Higgs boson. As in the previous section, in order to generate anomalous gauge couplings, we only have to continue to add higher-dimension operators. There are

403

several other operators of dimension 4 that give rise to anomalous triple and quartic gauge couplings (aTGCs and aQGCs). These are listed in Ref. [14]. Several limits exist on the possible size of aTGCs [15–30] and a few on aQGCs [31–34]. This measurement of  $W^{\pm}W^{\pm}jj$  production is used to set limits on two dimension 4 operators,  $\mathcal{L}_4$  and  $\mathcal{L}_5$ , which do not contribute to aTGCs but do contribute to the WWWW coupling. These two terms are:

$$\mathcal{L}_4 = \alpha_4 \, [Tr(V_\mu V_\nu)]^2 \tag{2.36}$$

434

$$\mathcal{L}_5 = \alpha_5 \left[ Tr(V_\mu V^\mu) \right]^2 \tag{2.37}$$

where  $V_{\mu} = (D_{\mu}\Sigma)\Sigma^{\dagger}$ . The first direct limits on the parameters  $\alpha_4$  and  $\alpha_5$  are presented in Chapter 9. While there is no general conversion between these parameters and the  $f_{S,i}$  parameters, they are related for a given vertex by a simple linear transformation [36]. The relationship for the WWWW vertex is:

$$\frac{f_{S,0}}{\Lambda^4} \frac{v^4}{8} = \alpha_4 \tag{2.38}$$

440

$$\frac{f_{S,1}}{\Lambda^4} \frac{v^4}{8} = \alpha_4 + 2\alpha_5 \tag{2.39}$$

#### 441 2.3.3 Unitarization

In the Standard Model, the unitarity of the scattering of longitudinally po-442 larized vector bosons is preserved by a cancellation between diagrams involv-443 ing the vector boson self-interactions and diagrams involving the exchange 444 of a Higgs. In effective theories with anomalous gauge couplings, this is no 445 longer the case. This is not indicative of a problem with effective theories as 446 they are only meant to describe the low-energy effects of some new physics. 447 However, it can lead to an overestimation of the sensitivity of experiments 448 to anomalous couplings. In order to prevent this, there are a few commonly 449 used methods for restoring unitarity to effective theories. 450

One method is the "form factor" method, in which an energy depen-451 dence is added to the anomalous coupling so that it falls off after some 452 cutoff scale,  $\Lambda$ . The cutoff scale and functional form of the form factor are 453 arbitrary choices, but the most common choice for anomalous gauge cou-454 plings is a dipole form factor [16–23, 32],  $1/(1 + \frac{s}{\Lambda^2})^2$ . The unitarization 455 scheme used in this measurement is the K-matrix method [37]. Unitar-456 ity requires that the eigenamplitudes, a(s), for vector boson scattering lie 457 within the Argand circle, |a(s) - i/2| = 1/2. The K-matrix method projects 458

scattering amplitudes calculated in the effective theory onto the Argand circle, causing the cross section to saturate at the maximum value allowed by
unitarity. This avoids the arbitrary choices involved when applying a form
factor. Figure 2.8 shows a comparison of VBS cross sections for a Higgsless
Standard Model with and without K-matrix unitarization applied.

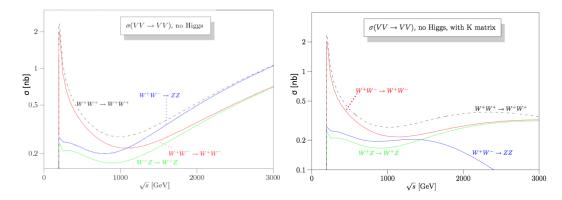


Figure 2.8: Vector boson scattering cross sections (nb) for the Standard Model without a Higgs with (right) and without (left) K-matrix unitarization [37].

#### <sup>464</sup> 2.3.4 Constraints from electroweak precision tests

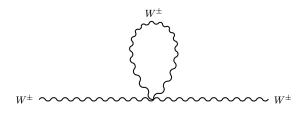


Figure 2.9: Example diagram for one-loop contribution of quartic gauge interactions to the gauge boson self-energies.

If anomalous quartic gauge couplings exist, VBS processes are not the only ones that will be affected. Anomalous quartic couplings will contribute to the self-energies of gauge bosons through the diagram shown in Figure 2.9. Therefore, these couplings also affect the scattering of fermions via exchange of a vector boson. For these processes there is a wealth of data available that can be used to constrain anomalous couplings. The contribution of <sup>471</sup> new physics to the scattering of fermions through its effects on gauge boson <sup>472</sup> propagators is parameterized by the Peskin-Takeuchi parameters, S, T, and <sup>473</sup> U [90]. The measured values of the parameters are given in Ref. [8]:

$$S = -0.03 \pm 0.10$$
  

$$T = 0.01 \pm 0.12$$
  

$$U = 0.05 \pm 0.10$$
  
(2.40)

in excellent agreement with the Standard Model (S = T = U = 0). These have been used to constrain the allowed values of  $\alpha_4$  and  $\alpha_5$  [89]. The  $\alpha_4$  and  $\alpha_5$  parameters to give the following contributions to T:

$$\alpha_{EW}T = \frac{-15\alpha_4}{64\pi^2}g^4(1+c_W^2)\frac{s_W^2}{c_W^2}\log\frac{\Lambda^2}{m_Z^2}$$
(2.41)

$$\alpha_{EW}T = \frac{-3\alpha_5}{32\pi^2}g^4(1+c_W^2)\frac{s_W^2}{c_W^2}\log\frac{\Lambda^2}{m_Z^2}$$
(2.42)

where  $\Lambda$  is the energy scale of the new physics responsible for the anomalous couplings. For  $\Lambda = 2$  TeV, the resulting 95% confidence level limits on  $\alpha_4$  and  $\alpha_5$  are -0.06 <  $\alpha_4$  < 0.30 and -0.15 <  $\alpha_5$  < 0.76.

# Chapter 3

# The Large Hadron Collider

The Large Hadron Collider (LHC) [38] is a circular accelerator with a cir-1 cumference of 26.7 km designed to collide beams of protons with a center-of-2 mass energy of 14 TeV. It is located near Geneva, Switzerland and reuses the 3 tunnel and injection chain from the Large Electron-Positron (LEP) collider. 4 The layout of the LHC in shown in Figure 3.1. The LHC ring has eight 5 straight sections in which beams can be made to collide, only four of which 6 are used for this purpose. The four experiments at the LHC are built around 7 these interaction points. The straight sections are also used for inserting the 8 proton beams, accelerating them, and dumping them. The capture and ac-9 celeration of the beams is done using RF cavities while superconducting 10 magnets are used to bend and focus the beams. 11

Protons are accelerated by the electric field inside superconducting RF 12 cavities. The frequency of EM waves in these cavities is kept at a harmonic 13 of the revolution frequency so that protons experience the same electric 14 field each time they pass through the cavity. The field in the cavity also 15 keeps protons bunched together since protons that are spread out will see 16 different electric fields and will therefore have different accelerations. Each 17 beam is accelerated by a series of eight 400 MHz RF cavities divided into 18 two cryomodules, a schematic of which is shown in Figure 3.2. Each cavity 19 is powered by its own 300 kW klystron and provides a 2 MV accelerating 20 voltage. With each revolution, the beam energy is increased by 485 keV 21 until reaching the final energy for collisions. 22

The LHC uses electromagnets made from superconducting NbTi Rutherford cables that are cooled using superfluid helium to a temperature of 1.9 K. Since the LHC is a proton-proton collider, opposite magnetic fields are needed to direct each beam. However, the LEP tunnel was not designed to

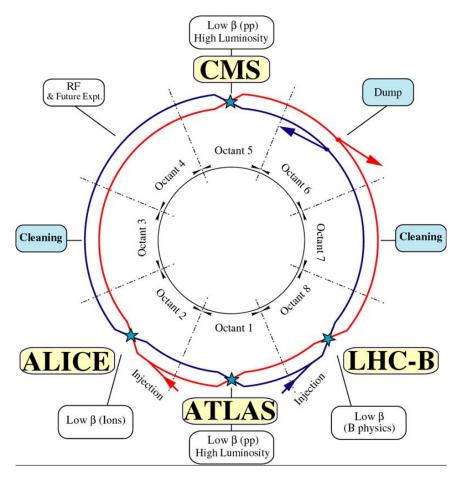


Figure 3.1: Layout of the LHC [38].

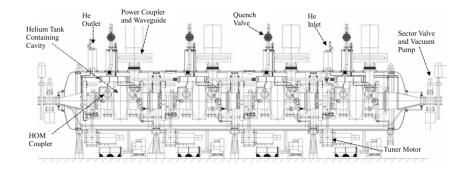
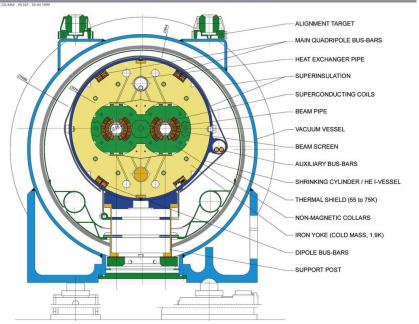


Figure 3.2: Schematic of cryomodule containing four RF cavities [38].

<sup>27</sup> accommodate separate magnet systems for each beam. This led to the adop-

 $_{28}$   $\,$  tion of a "two-in-one" design in which the two beamlines share a common

29 cold mass and cryostat.



#### LHC DIPOLE : STANDARD CROSS-SECTION

Figure 3.3: Cross section of LHC dipole magnet [39].

The cross section of an LHC dipole magnet is shown in Figure 3.3. 1,232 30 of these magnets are used to bend the beams and keep them going in a circle. 31 The cables are wound in such a way that the magnetic field is oriented in 32 opposite directions in each beam pipe. At injection, the current through 33 the cables is 763 A, producing a magnetic field of 0.54 T. The maximum 34 beam energy is limited by the peak field of the magnets, which reach 8.33 T 35 at a current of 11850 A. Rigid collars are used to help maintain structural 36 stability since the electromagnetic forces between cables can reach the level 37 of a few MN. In order for the LHC to work properly, each dipole magnet 38 must be nearly identical: relative variation of the field between magnets 39 cannot exceed  $10^{-4}$ . 40

Focusing of the beam is done using quadrupole magnets. The LHC ring contains 392 main quadrupoles to keep the beam from spreading out as it travels around the ring and several other multipole magnets for making beam corrections. Higher precision quadrupoles are located prior to the  $_{45}\,$  collision points and focus the beams down to a transverse size of about 15  $_{46}\,$   $\mu m.$ 

In addition to reaching unprecedented energies, the LHC is also designed to reach unprecedented luminosity. Luminosity is a measure of the rate of proton-proton collisions. Given a cross section for a particular process, the rate at which those events are produced is given by  $N = L\sigma$ . Luminosity as a function of beam parameters is given by:

$$L = \frac{N_b^2 n_b f \gamma}{4\pi\epsilon_n \beta_*} F \tag{3.1}$$

where  $N_b$  is the number of protons per bunch,  $n_b$  is the number of col-52 liding bunches, f is the revolution frequency,  $\gamma$  is the relativistic Lorentz 53 factor,  $\epsilon_n$  is the transverse beam emittance,  $\beta_*$  is the beta function relating 54 emittance to beam width at the interaction point, and F is a geometric fac-55 tor that accounts for the non-zero crossing angle of the colliding beams. The 56 LHC is designed to circulate beams containing 2808 bunches with a bunch 57 spacing of 25 ns and  $1.15 \times 10^{11}$  protons per bunch at a frequency of 11245 58 revolutions per second. The design values for transverse emittance and  $\beta_*$ 59 are 3.75  $\mu$ m and 0.55 m, and the geometric factor is about 1/40. The peak 60 luminosity reach with all the design parameters is  $10^{34}$  cm<sup>-2</sup>s<sup>-1</sup>. 61

### <sup>62</sup> 3.1 Injection Chain

Protons are produced from hydrogen gas and go through several stages of 63 acceleration before reaching the LHC [41]. The accelerator chain is shown in 64 Figure 3.4. The process begins with hydrogen gas being fed into a duoplas-65 matron ion source, which ionizes the hydrogen atoms to produce a proton 66 beam. A radio frequency quadrupole is used to accelerate and focus the 67 beam before it is injected into the LINAC2. LINAC2 is a 30-meter long 68 linear accelerator that takes protons from an energy of 750 keV to 50 MeV. 69 After LINAC2, the proton beam passes through a series of circular accel-70 erators, starting with the Proton Synchrotron Booster (PSB). The PSB 71 consists of 4 vertically stacked rings with a circumference of 157 meters and 72 accelerates protons to an energy of 1.4 GeV. 73

The next stop is the Proton Synchrotron (PS), which is a 628-meter long ring. In addition to raising the beam energy to 25 GeV, the PS establishes the bunch structure used at the LHC. Bunches are split in two stages, once at 1.4 GeV and once at 25 GeV, by raising the RF frequency to higher multiples of the revolution frequency. The beam leaving the PS consists of

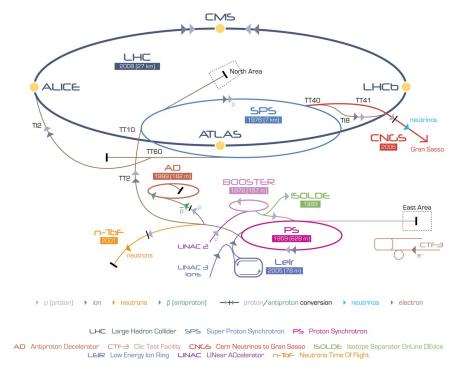


Figure 3.4: Injection chain for the LHC [40].

72 bunches of protons with a duration of about 4 ns and a spacing of 25 79 ns followed 12 empty bunches. The gap left by the empty bunches provides 80 time for the ejection kicker magnet to ramp up. The final accelerator in 81 the injection chain is the Super Proton Synchrotron (SPS). This 7-km long 82 circular accelerator was used to discover the W and Z bosons in 1983. It 83 takes the 25 GeV beam from the PS up to an energy of 450 GeV. Protons 84 are then injected into the LHC and accelerated to their final energy before 85 being made to collide. 86

# <sup>87</sup> 3.2 Run 1 Performance

First collisions at the LHC were delayed by an accident that occurred on 88 September 19, 2008. During powering tests, a quench developed in a region 89 between two magnets, resulting in an electric discharge that ruptured the 90 helium enclosure and damaged magnets and support structures along 700 91 meters of the tunnel. While the machine was being repaired, other con-92 nections between magnets were examined, and the quench detection system 93 was upgraded to include these areas. However, it was decided that further 94 upgrades were necessary before operating the machine at full design energy. 95 In 2010 and 2011, roughly 5  $fb^{-1}$  of data was taken at half of the design 96 energy ( $\sqrt{s} = 7$  TeV). The measurement presented in this dissertation uses 97 the data taken in 2012, which corresponds to  $20.3 \text{ fb}^{-1}$  of data with a center-98 of-mass energy of 8 TeV. In addition to running at lower energy, the LHC ran 99 with about half as many bunches and twice the bunch spacing as designed. 100 However, due to higher beam intensity, the peak luminosity reached,  $7.7 \times$ 101  $10^{33}$  cm<sup>-2</sup>s<sup>-1</sup>, was not far below the design luminosity. The 2012 run also 102 benefited from a  $\epsilon_n \beta_*$  product of 2.5  $\mu m \times 0.6 m = 1.5 mm^2$ , which was 103 about 25% lower than the design value [42]. Figure 3.5 shows the integrated 104 luminosity as a function of time in 2012. The downside to having fewer 105 bunches with more protons per bunch is that each bunch crossing produces 106 more collisions, which makes it harder to reconstruct the rare collisions of 107 interest to physicists. In 2012, there were an average of 20 proton-proton 108 collisions per bunch crossing. 109

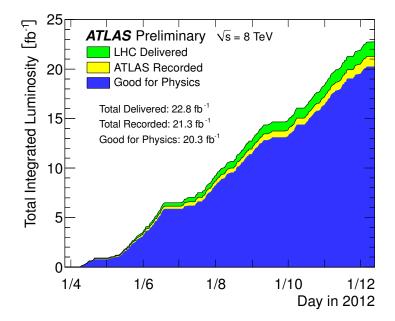


Figure 3.5: Integrated luminosity as a function of time delivered by the LHC and recorded by the ATLAS detector [43].

# Chapter 4

# The ATLAS Detector

The ATLAS detector, shown in Figure 4.1, has an approximately forward-1 backward symmetric cylindrical geometry. It consists of a cylindrical barrel 2 region with endcap disks on either side. In both the barrel and the end-3 cap, the detector is comprised of three systems: the inner detector, the 4 calorimeter, and the muon spectrometer. The inner detector (ID) is used to 5 chart the trajectories of charged particles and measure their momenta. It 6 sits within a solenoid that generates a 2 T magnetic field used to measure 7 momentum in the transverse plane. The calorimeter is positioned outside 8 of the solenoid and is used to measure the energies of both charged and 9 neutral particles. The calorimeter is designed to be thick enough to force 10 electrons, photons, and hadrons to exhaust all of their energy. Outside of 11 the calorimeter sits the muon spectrometer (MS), which is used make a 12 second measurement of muon trajectories. It uses a 0.5-1 T magnetic field 13 produced by toroidal magnets. Details beyond those given in this chapter 14 can be found in Ref. [44]. 15

The coordinate system for the ATLAS detector has its origin at the 16 nominal interaction point, which lies right at the center of the detector. 17 The z-axis points along the beamline in the counterclockwise direction when 18 viewed from above while the x-axis points toward the center of the LHC 19 ring, and the y-axis points upward away from the plane containing the ring. 20 In the plane transverse to the beam direction, radius and azimuthal angle coordinates are defined as  $R = \sqrt{x^2 + y^2}$  and  $\phi = \arctan \frac{y}{x}$ , respectively. 21 22 The polar angle,  $\theta$ , is measured from the positive z-axis. When considering 23 the proximity of a particle's trajectory to the beam direction, it is often 24 more convenient to use rapidity, defined as  $y = \frac{1}{2} \ln \frac{E + p_z}{E - p_z}$ , rather than polar 25 angle because differences in rapidity are independent of boosts along the 26

<sup>27</sup> z-axis. In the case of a massless particle, the rapidity is related to the polar <sup>28</sup> angle simply by  $y = -\ln \tan \frac{\theta}{2}$ . This quantity is taken as the definition of <sup>29</sup> pseudorapidity,  $\eta$ , and is the most commonly used coordinate to described <sup>30</sup> location along the z-axis.

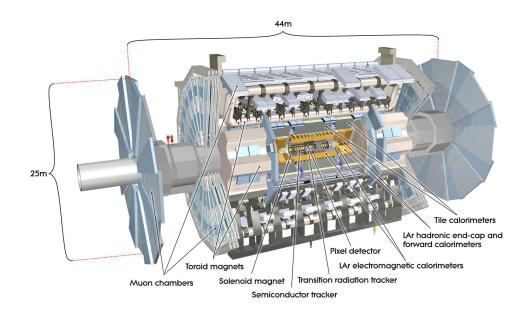


Figure 4.1: Illustration of the ATLAS detector with various subsystems indicated [45].

## 31 4.1 Inner Detector

The ID consists of three subsystems, ordered in increasing distance from the beamline and decreasing resolution: the pixel detector, the semi-conductor tracker (SCT), and the transition radiation tracker (TRT). The pixel and SCT systems use doped silicon sensors held under reverse bias to measure the passage of charged particles while the TRT uses drift tubes interleaved with transition radiation material. The three subsystems are depicted in Figure 4.2.

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Each system makes multiple measurements of the position of a charged particle, and these measurements are used to fit a trajectory (track) for

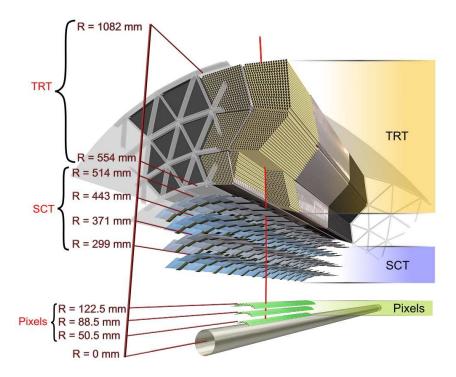


Figure 4.2: View of the barrel region of the ATLAS Inner Detector [44].

the particle as described in Chapter 5. The entire ID sits inside a solenoid that produces a 2T magnetic field oriented along the beamline. As a result, charged particles leaving the interaction point are deflected in the plane transverse to the beam direction, and the tracks measured in the ID are curved. The curvature of a track is then used to determine the transverse momentum of the corresponding particle.

#### 48 4.1.1 Pixel Detector

<sup>49</sup> The pixel detector is the closest detector system to the beamline. It consists <sup>50</sup> of 1774 modules arranged in three cylindrical layers located at a radius of <sup>51</sup> 50.5 mm, 88.5 mm, and 122.5 mm from the beamline and six endcap disks <sup>52</sup> (three on each side) located along the beam direction at distances of 495 mm, <sup>53</sup> 580 mm, and 650 mm from the center of the detector. This arrangement <sup>54</sup> provides three layers of coverage out to  $|\eta| < 2.5$ .

Each module contains a silicon sensor connected to a set of front end 55 chips, each responsible for reading out a set of pixels and a module control 56 chip that communicates with all the front ends. The pixel sensors are made 57 with 250  $\mu$ m thick n-type silicon wafers. High positive and negative dose 58 regions are implanted into opposite sides of the wafer in a rectangular array. 59 Each site on the array is a pixel. A large voltage is applied across the wafer 60 to reverse bias the p-n junction at each pixel. This operating voltage is 61 initially about 150 V but will rise up to 600 V over time due to radiation 62 damage, which will eventually turn the n-type bulk silicon into a p-type 63 bulk. 64

When a charged particle passes through the wafer, it ionizes atoms, and the resulting free electrons are moved to one side of the wafer by the applied electric field. Charge is collected at each pixel, and the resulting analog signal is converted to a digital time over threshold measurement using a comparator with reference voltage set to reject false signals from electronic noise. The threshold is set around 3500 electrons while a minimally ionizing particle typically generates a signal of around 20000 electrons.

Except for a few pixels located next to the front end chips, each pixel is 50  $\mu$ m long in the direction transverse to the beamline and 400  $\mu$ m long in the longitudinal direction. The remaining pixels have a size of 50×600  $\mu$ m<sup>2</sup>. Correspondingly, the pixel modules have a spatial resolution of 10  $\mu$ m in the transverse direction and 115  $\mu$ m in the longitudinal direction.

#### 77 4.1.2 Semi-Conductor Tracker

The SCT is located outside the pixel detector and uses strips instead of pixels 78 to cover a larger area while maintaining a manageable number of readout 79 channels. A total of 4088 modules are arranged in double layers forming 80 four cylinders in the barrel region at a radius of 284 mm, 355 mm, 427 mm, 81 and 498 mm and nine endcap disks on either side at longitudinal distances 82 between 853 mm and 2708 mm. Strips in the first layer are oriented along 83 the beam direction with the second layer tilted at a small stereo angle to 84 obtain resolution in the longitudinal direction that is much better than the 85 strip length of 12 cm. Particles with  $|\eta| < 2.5$  will cross at least four of these 86 double layers. 87

SCT modules use a standard p-in-n silicon sensor with a thickness of 285 88  $\mu$ m. Like the pixel detector, the SCT is operated initially at a bias voltage of 89 150 V that will eventually rise up to 350 V. The barrel modules are made of 90 two 6 cm long sensors put together which are AC-coupled to readout strips 91 with a pitch of 80  $\mu$ m. Modules in the endcaps use strips with a constant 92 azimuth and mean pitch of about 80  $\mu$ m. The spatial resolution for SCT 93 modules is 17  $\mu$ m in the transverse direction and 580  $\mu$ m in the longitudinal 94 direction. 95

#### 96 4.1.3 Transition Radiation Tracker

The final tracking system in the ID is the TRT. The barrel portion consists 97 of 73 layers of drift tubes (also called "straws") interleaved with transition 98 radiation fibers and spans the distance from a radius of 554 mm to a radius 99 of 1082 mm while the endcap has 160 straw planes interleaved with transi-100 tion radiation foils and is situated between 615 mm and 1106 mm along the 101 beamline. Except for the transition region between the barrel and the end-102 cap, which lies at  $0.8 < |\eta| < 1.0$ , particles with  $|\eta| < 2.0$  cross an average 103 of 36 straws. 104

Each straw is a polyimide tube 4 mm in diameter filled with a gas mixture 105 of 70% Xe, 27% CO<sub>2</sub>, and 3% O<sub>2</sub> and with a 31  $\mu$ m diameter gold-plated 106 tungsten wire running down the middle. The tube is made of two polyimide 107 films coated on one side with a thin Al layer and bonded back-to-back using 108 a polyure hane layer and has a total thickness of 70  $\mu$ m. A charged particle 109 passing through the straw tube will leave a trail of ionization behind. The 110 central wire is held at ground and the tube walls at about -1500 V creating 111 an electric field that drives the free electrons towards the wire. Along the 112 way, these electrons ionize more atoms and the newly freed electrons are 113

<sup>114</sup> in turn accelerated by the field in a cascade that continues until the charge <sup>115</sup> reaches the wire, which is connected to readout electronics. TRT straws only <sup>116</sup> measure position in the transverse direction and have a spatial resolution of <sup>117</sup> 130  $\mu$ m.

Transition radiation material between the straws is used to help dis-118 tinguish between tracks left by electrons and track left by pions. When a 119 charged particle crosses the boundary between two materials with different 120 dielectric constants, it will give off an amount of transition radiation pro-121 portional to its Lorentz factor  $\gamma$ . Thus, for a track of a given momentum, a 122 particle with low rest mass will give more radiation than one with a larger 123 rest mass. This radiation can also ionize gas in the straw tubes leading to a 124 larger signal, called a "high threshold hit." The ratio high threshold hits to 125 ordinary hits can then be used to discriminate between electrons and pions. 126

### 127 4.2 Calorimeter

The calorimeter is located outside the ID and solenoid and is composed 128 of four subsystems used to measure the energy of electrons, photons, and 129 hadrons. A high-granularity electromagnetic (EM) calorimeter provides pre-130 cise measurements of electrons and photons and extends out to  $|\eta| < 3.2$ . 131 Hadronic tile and endcap calorimeters (HEC) with a coarser granularity suf-132 ficient for measuring jets of hadrons cover the same  $\eta$  range outside of the 133 EM calorimeter. A forward calorimeter (FCal) extends the coverage out to 134  $|\eta| < 4.9$  with one EM layer and two hadronic layers. The EM calorime-135 ter, HEC, and FCal all use liquid argon (LAr) as an active material while 136 the tile calorimeter uses scintillating tiles. All of the calorimeters also use 137 absorber plates to keep showers contained within the calorimeter and limit 138 punch-through into the muon spectrometer. 139

#### 140 4.2.1 EM Calorimeter

The EM calorimeter consists of two half barrels that extend out to  $|\eta| < 1$ 141 1.475 and outer and inner endcap wheels on either side that cover 1.375 <142  $|\eta| < 2.5$  and  $2.5 < |\eta| < 3.2$ , respectively. The barrel and outer wheel have 143 three layers of cells with the innermost layer having the highest granularity. 144 A schematic for a barrel module is shown in Figure 4.3. The first layer is 145 made of thin strips with  $\Delta\eta \times \Delta\phi = 0.0031 \times 0.098$  while the second and third 146 layers have more square dimensions of  $0.025 \times 0.0245$  and  $0.05 \times 0.0245$ . The 147 inner wheel has only the two more coarse layers. The total depth of the EM 148

calorimeter ranges from 22 radiation lengths  $(X_0)$  to 33  $X_0$  in the barrel and 24-36  $X_0$  in the endcap.

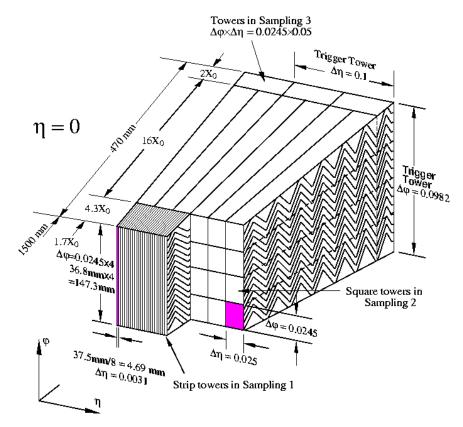


Figure 4.3: Schematic showing the cells in a barrel module of the EM calorimeter [44].

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Modules in the EM calorimeter contain lead absorber plates and copper 152 electrodes in an accordion shape with LAr in the gaps. Charged parti-153 cles and photons ionize argon atoms, initiating a shower of electrons and 154 photons. Charge is then collected at the electrodes, which consist of three 155 copper plates separated by polyimide insulation. The outer two plates are 156 held at high voltage, and the inner plate is used for the readout. Lead 157 absorber plates help keep the shower contained and vary in thickness from 158 1.53(2.2) mm to 1.13(1.7) mm to limit the decreasing in sampling fraction 159 with increasing (decreasing)  $|\eta|$  in the barrel (endcaps). 160

The EM calorimeter has a measured energy resolution [46] of  $\frac{\sigma(E)}{E} = 10\%/\sqrt{E(GeV)} \oplus 0.2\%$  and a spatial resolution of 50 mrad/ $\sqrt{E}$  in  $\eta$ . A presampler located in front of the EM calorimeter for  $|\eta| < 1.8$  also helps correct for energy lost by electrons and photons before reaching the calorimeter. It consists of a thin LAr layer, 11 mm thick in the barrel and 5 mm thick in the endcaps, with readout electrodes and no absorber plates.

### <sup>167</sup> 4.2.2 Hadronic Tile Calorimeter

The tile calorimeter sits outside the EM barrel and contains a central barrel that extends out to  $|\eta| < 1.0$  and extended barrels on either side that span 0.8 <  $|\eta| < 1.7$ . Each barrel is segmented into three layers in depth. The first two layers have a granularity of  $\Delta \eta \times \Delta \phi = 0.1 \times 0.1$  while the last layer has a granularity of  $0.2 \times 0.1$ . The total depth of the tile calorimeter is about 7.4 interaction lengths ( $\lambda$ ).

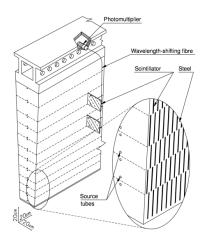


Figure 4.4: Sketch showing the structure of the tile calorimeter [44].

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Modules are constructed from alternating steel plates and doped polystyrene tiles with a ratio by volume of 4.7:1. The steel plates act as an absorber, and polystyrene tiles are the active material. Incoming hadrons interact with nuclei in the tiles to produce hadronic showers. Photons produced in these showers are collected by wavelength-shifting fibers into photomultiplier tubes. The tiles are placed in reflective plastic sleeves to increase light <sup>181</sup> yield and prevent damage. A schematic of this structure is shown in Fig-<sup>182</sup> ure 4.4. The energy resolution of the tile calorimeter has been measured to <sup>183</sup> be within the desired resolution of  $50\%/\sqrt{E} \oplus 3\%$  [47].

#### 184 4.2.3 Hadronic Endcap and Forward Calorimeters

Like the EM calorimeter, both the HEC and FCal use LAr as the active material. The HEC has front and rear wheels covering the range of 1.5  $< |\eta| < 3.2$  and  $1.5 < |\eta| < 2.5$ . Each wheel is separated into two layers. The front wheels use 24 copper plates with a thickness of 25 mm as absorbers while the rear wheels have 16 copper plates with a thickness of 50 mm. Regions with  $|\eta| < 2.5$  have a granularity of  $\Delta \eta \times \Delta \phi = 0.1 \times 0.1$  while the remainder has a granularity of  $0.2 \times 0.2$ .

The FCal covers the range of  $3.1 < |\eta| < 4.9$  and it split into three layers, one for electromagnetic measurement and two for hadronic measurement. The first layer uses copper plates as an absorber. The electrodes are coaxial copper rods that run through holes drilled in the copper plates. The second and third layers used tungsten rods that run between two copper end plates. Tungsten slugs fill the gaps between the rods and are the main absorbing material in these layers.

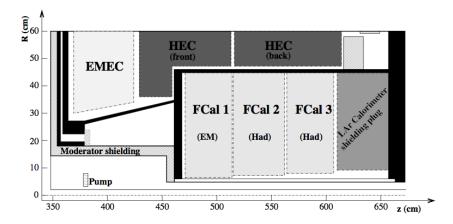


Figure 4.5: Arrangement of endcap and forward calorimeters [44].

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The layout of the endcap and forward calorimeters is illustrated in Figure 4.5. The measured energy resolution of the HEC is about  $21\%/\sqrt{E}$  for electrons and  $70\%/\sqrt{E} \oplus 6\%$  for pions [48]. For the FCal these measurements are approximately  $29\%/\sqrt{E} \oplus 3.5\%$  and  $70\%/\sqrt{E} \oplus 3\%$ , respectively [49].

# <sup>205</sup> 4.3 Muon Spectrometer

The MS contains four subsystems that sit outside the calorimeter. Moni-206 tored Drift Tube chambers (MDTs) and Cathode Strip Chambers (CSCs) 207 are used for precision tracking measurements. The remaining two systems 208 have faster response times and are used for triggering. Resistive Plate Cham-209 bers (RPCs) are used in the barrel region, and Thin Gap Chambers are used 210 in the endcaps. All of these systems work by collecting charge from gas ion-211 ized by the passage of a charged particle. The layout of the muon system 212 is illustrated in Figure 4.6. The chambers are arranged in barrel layers at a 213 radius of 5 m, 7.5 m, and 10 m and endcap disks located at distances of 7.4 214 m, 10.8 m, 14 m, and 21.5 m down the beamline. 215

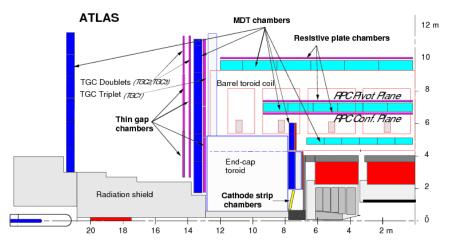


Figure 4.6: Sketch of the ATLAS muon system [50].

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As in the inner detector, a magnetic field is used to bend tracks in the MS in order to measure the muons' momenta. The magnetic field in the MS is provided by a 0.5 T barrel toroid for  $|\eta| < 1.4$  and two 1 T endcap toroids for  $1.6 < |\eta| < 2.7$ . The field in transition region of  $1.4 < |\eta| < 1.6$  is a combination of the barrel and endcap fields. The MS covers a much larger distance than the ID (several meters as opposed to one meter) which allows for precise measurements of muon momentum up to a few TeV.

#### 4.3.1 Precision Chambers

Monitored Drift Tube chambers make up most of the precision tracking 225 chambers in the MS. Except for the innermost layer, they provide coverage 226 out to  $|\eta| < 2.7$ . The first layer extends only out to  $|\eta| < 2.0$  due to the 227 inability of the MDTs to handle the expected hit rate at  $|\eta| > 2.0$ . MDT 228 chambers are made of 3-8 layers of drift tubes. The tubes have a diameter 229 of 50 mm and are filled with 93% Ar and 7% CO<sub>2</sub>. Charge is collected 230 on a central tungsten-rhenium wire held at a potential of approximately 3 231 kV. Individual tubes have a spatial resolution of 80  $\mu$ m, and the average 232 resolution of a chamber in the bending direction is about 35  $\mu$ m. 233

Cathode Strip Chambers are used for the first layer of precision track-234 ing for  $|\eta| > 2.0$ . They are multiwire proportional chambers with 30  $\mu$ m-235 diameter anode wires running radially and two sets of cathode strips, one 236 parallel to anode wires and the other perpendicular. The chamber is filled 237 with a gas mixture of 80% Ar and 20% CO<sub>2</sub> and operated at a voltage of 238 1.9 kV. Charge is collected at each strip and track position is measured by 239 interpolating between them. The disk is made of alternating large and small 240 chambers that have a different spacing between readout strips. Large cham-241 bers have a readout pitch of 5.31 mm in the bending direction and 21 mm242 in the transverse direction. For the small chambers these numbers are 5.56 243 mm and 12.92 mm, respectively. This results in a resolution of 40  $\mu$ m in the 244 bending direction and 5 mm in the transverse direction. 245

#### 246 4.3.2 Trigger Chambers

The short distances and large electric fields used in the RPCs and TGCs result in short drift times that allow these measurements to be used for fast triggering. Both detectors read out a signal in less than 25 ns and have timing resolution of a few ns, which allows the signal to be accurately matched to a bunch crossing. In addition, they provide a measurement of the azimuthal coordinate which is not measured precisely by the MDTs.

Resistive Plate Chambers are used as the trigger chambers out to  $|\eta| < 1.05$ . Rather than using wires with a radial electric field, the RPCs have two resistive plates 2 mm apart with a uniform electric field between them. The plates are held at a potential difference of 9.8 kV, and gap is filled with 94.7% C<sub>2</sub>H<sub>2</sub>F<sub>4</sub>, 5% Iso-C<sub>4</sub>H<sub>10</sub>, and 0.3% SF<sub>6</sub>. Readout strips are attached to the outer faces of the plates with a pitch of 23-35 mm. The resulting spatial resolution is 10 mm in both directions. With the long distance between the first two RPC layers and the third layer, this is sufficient to resolve tracks with momentum up to 35 GeV.

Thin Gap Chambers provide triggering capability for  $1.05 < |\eta| < 2.4$ . 262 They are multiwire proportional chambers with a wire-to-cathode distance, 263 1.4 mm, shorter than the wire-to-wire distance, 1.8 mm and use a highly-264 quenching gas mixture of 55% CO<sub>2</sub> and 45% n-pentane. The wires are held 265 at a potential of 2.9 kV. Better spatial resolution is needed at higher  $|\eta|$  to 266 maintain good momentum resolution. This is achieved by varying the size of 267 the wire groups used to measure the position from 6 to 31 wires. The TGCs 268 have a spatial resolution that varies from 2-6 mm in the radial direction and 269 3-7 mm in the azimuthal direction. 270

## <sup>271</sup> 4.4 Trigger System

ATLAS uses a trigger system to reduce the rate of recorded events from the 40 MHz collision rate to 1 kHz. This is done in three stages, referred to as Level 1 (L1), Level 2 (L2), and Event Filter (EF), each using progressively more information (and therefore taking more time) to render a decision as to whether or not to keep the event. This decision is made based on the presence of high transverse momentum objects (leptons, photons, jets), large missing transverse energy ( $E_{\rm T}^{\rm miss}$ ), or large total transverse energy.

Unlike the later trigger stages, which are purely software systems, the L1 279 trigger is implemented in hardware in order to increase speed. It makes its 280 decision using information from calorimeter towers spanning approximately 281  $0.1 \times 0.1$  in  $(\eta, \phi)$  as indicated in Figure 4.3 and the trigger chambers in the 282 muon system. Electron candidates are made from  $2 \times 2$  clusters of trigger 283 towers, and energy in the surrounding 12 towers is used to determine if the 284 electron is isolated. Muon candidates are formed by looking for a coincidence 285 of hits in the trigger chambers that lie within a road of variable width 286 pointing back to the interaction point. The width of the road depends on 287 the  $p_{\rm T}$  threshold of the trigger. After L1, the output rate is about 75 kHz. 288 That output rate is reduced to 3.5 kHz by the L2 trigger, which selects 289 events based on "Regions of Interest" (RoIs) supplied by the L1 triggers. 290 Each RoI corresponds to an object passing one of the L1 selections. These 291 objects are rebuilt at L2 using information from all subsystems of the detec-292

<sup>293</sup> tor within the RoI, not just the trigger chambers and towers. The final stage

- <sup>295</sup> for offline event reconstruction, which are discussed in Chapter 5. Events
- $_{\rm 296}$   $\,$  passing a set of EF selections are recorded in one or more data streams based
- <sup>297</sup> on what type of object passed the trigger.

# Chapter 5

# Object Reconstruction and Event Selection

# <sup>1</sup> 5.1 Track and Vertex Reconstruction

<sup>2</sup> Tracks are reconstructed from hits in the inner detector and fit for five <sup>3</sup> parameters, which are measured at the point of closest approach to the <sup>4</sup> beamline: the radius of curvature of the track, from which the ratio of charge <sup>5</sup> to transverse momentum  $(q/p_{\rm T})$  can be derived, the azimuthal and polar <sup>6</sup> angles ( $\phi$  and  $\theta$ ) in the ATLAS coordinate system, and the transverse and <sup>7</sup> longitudinal impact parameters ( $d_0$  and  $z_0$ ), which are defined as distance <sup>8</sup> in the transverse plane or on the longitudinal axis between the track and <sup>9</sup> origin/interaction region/vertex.

Track reconstruction in ATLAS begins with an inside-out algorithm that builds track candidates from hits in the pixel detector and the first layer of the SCT [51]. Clusters of nearby hits in each layer are converted into threedimensional space points. Combinations of points define track seeds, and the reconstruction algorithm then looks for points in the last three SCT layers the lie on "roads" extending from the ends of the seeds. Tracks are fit to these collections of points, and outliers are removed.

At this stage, it is possible for a single hit to be associated with more than one track. These ambiguities are resolved by scoring tracks based on how precisely hits match the fitted track and whether the track has any holes (missing hits). Hits shared between tracks are assigned to the highest scoring track, and quality criteria are applied to remove fake tracks.

The remaining tracks are extended into the TRT and refit with the new hits in addition to the hits in the silicon layers. The quality before

and after the refit are compared, and TRT hits resulting in a worse fit are 24 labeled as outliers and removed from the fit (but remain associated with 25 the track). Once the extension of silicon tracks into the TRT is finished, an 26 outside-in tracking algorithm takes unused segments of TRT hits as seeds 27 and attempts to extend them back into the silicon layers. This helps recover 28 efficiency for tracks not originating from the primary interaction. The track 29 reconstruction efficiency as a function of  $|\eta|$  for simulated muons, pions, and 30 electrons with a  $p_{\rm T}$  of 5 GeV is shown in Figure 5.1. Muons have a very high 31 track reconstruction efficiencies while the efficiencies for pions and electrons 32 decrease significantly as the amount of material traversed increases. This is 33 due to hadronic interactions with the detector for pions and bremsstrahlung 34 radiation for electrons. 35

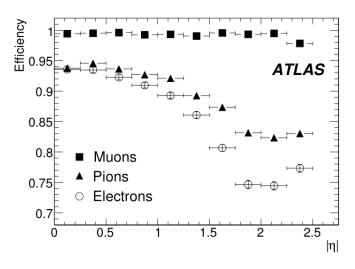


Figure 5.1: Track reconstruction efficiency for tracks belonging to muons, pions, and electrons with a  $p_{\rm T}$  of 5 GeV [51].

Vertex reconstruction is performed using tracks that are consistent with 36 originating from the interaction region. The criteria used to select these 37 tracks are specified in Ref. [52]. An iterative procedure is used to find 38 vertices and fit their position. First, a vertex seed is made by looking for a 39 global maximum in the distribution of the z-coordinate of the selected tracks. 40 Then a  $\chi^2$ -based fitting procedure that down-weights the contribution from 41 outlying tracks is used to determine the vertex position. Multiple iterations 42 of the fit are performed with progressively more down-weighting. Once this 43 is done, all remaining tracks that are incompatible with the fitted vertex 44 by more than  $7\sigma$  are used to seed a new vertex, and tracks associated with 45

the fitted vertex are refit using the vertex position as a constraint. This is repeated until all tracks are associated with a vertex or until no new vertices can be found. The vertex with the highest  $\Sigma p_T^2$  of associated tracks is considered the primary vertex. The efficiency for vertex reconstruction as a function of the number of reconstructed tracks is shown in Figure 5.2, measured for 7 TeV collisions in 2010 [53]. For vertices with three or more tracks, this efficiency exceeds 99%.

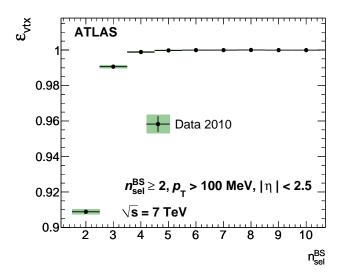


Figure 5.2: Vertex reconstruction efficiency as a function of the number of reconstructed tracks. Figure taken from Ref. [53].

## 53 5.2 Electron Reconstruction

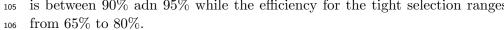
Electron candidates within the tracking acceptance  $(|\eta| < 2.47)$  are recon-54 structed from a combination of an energy cluster in the EM calorimeter and 55 a track [54]. A sliding-window algorithm with a window size corresponding 56 to a  $3 \times 5$  block of cells in the middle layer of the calorimeter is used to look 57 for clusters of cell towers with a total transverse energy  $(E_{\rm T})$  greater than 58 2.5 GeV. Tracks are extrapolated to the middle layer of the calorimeter, and 59 at least one track is required to be within  $|\Delta \eta| < 0.05$  and an asymmetric 60  $|\Delta \phi|$  window that is 0.1 on the side where the track bends and 0.05 on the 61 other side. If multiple tracks fit this criteria, the track with the smallest 62  $\Delta R = \sqrt{\Delta \eta^2 + \Delta \phi^2}$  is selected. 63

After the initial candidates are found, the clusters are rebuilt using a 64  $3 \times 7$  block of towers in the barrel and a  $5 \times 5$  block in the endcap. The total 65 energy of the cluster is then calculated as the sum of the measured energy in 66 the cluster plus estimates of the amount of energy lost before reaching the 67 calorimeter, deposited in cells outside the cluster, and deposited behind the 68 EM calorimeter. These estimates are parameterized as function of measured 69 energies in the presampler and each layer of the EM calorimeter within the 70 cluster using simulations of detector response. The four-momentum for the 71 electron candidate is then constructed using the energy of the rebuilt cluster 72 and the  $\eta$  and  $\phi$  of the associated track. 73

Outside of the tracking acceptance, electron candidates are reconstructed 74 from a calorimeter cluster only. These clusters do not have a fixed size and 75 are formed using the significance of measured energy over expected noise 76 to group neighboring cells together. To be reconstructed as an electron, 77 the cluster is required to have a small hadronic component and a transverse 78 energy greater than 5 GeV. Since there is no associated track, the electron di-79 rection is determined by the average position of cells in the cluster, weighted 80 by the energy in each cell. The remainder of this section will focus on central 81 electrons since forward electrons are not used in this measurement. 82

Electron candidates are identified as electrons using several selections 83 on shower-shape and tracking variables. Three categories of electrons are 84 defined (loose, medium and tight) in order to have good acceptance and 85 progressively higher background rejection. The loose category imposes re-86 quirements on the ratio of energy in the hadronic calorimeter to energy in 87 the EM calorimeter and on the transverse shower shape in the middle layer 88 of the EM calorimeter. The medium category adds further requirements on 89 the shower width in the first layer of the EM calorimeter and on the number 90 of silicon hits and transverse impact parameter of the electron track. The 91 tight category builds on the medium requirements, imposing stricter re-92 quirements on track-cluster matching and transverse impact parameter and 93 adding selections on the number of TRT hits and the ratio of high-threshold 94 to total hits. Tight electrons are also required to have a hit in the first layer 95 of the pixel detector and not be matched to any photon conversions. 96

<sup>97</sup> The efficiency for electron reconstruction and identification has been <sup>98</sup> measured in 8 TeV collision data using a selection designed to pick out <sup>99</sup>  $Z \rightarrow ee$  events [55]. The results are shown in Figure 5.3 as a function <sup>100</sup> of  $E_{\rm T}$  for electrons within the tracking volume and as a function of  $\eta$  for <sup>101</sup> electrons with  $E_{\rm T} > 7$  GeV. The efficiencies of interest for this measurement <sup>102</sup> are the efficiencies for the loose selection (used for estimating non-prompt <sup>103</sup> background and third lepton veto) and the tight selection (nominal electron identification used in the analysis). Typical efficiency for the loose selection
 is between 90% adn 95% while the efficiency for the tight selection ranges



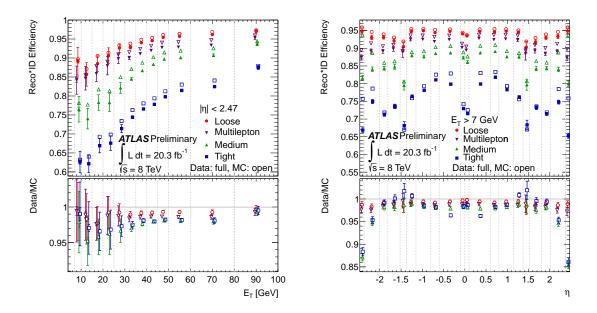


Figure 5.3: Electron reconstruction and identification efficiency as a function of  $p_{\rm T}$  (left) and  $\eta$  (right). Filled points show the efficiencies measured in data while efficiencies measured in MC are indicated by the open points. Figure taken from Ref. [55].

# 107 5.3 Muon Reconstruction

<sup>108</sup> Muons are reconstructed in three categories based on whether the muon has <sup>109</sup> a track in the MS, ID, or both [51]. Standalone muons consist only of a <sup>110</sup> track in the muon spectrometer. Tracks are formed in the MS starting with <sup>111</sup> a  $0.4 \times 0.4$  region in  $(\eta, \phi)$  space centered on a hit in the RPC/TGC trigger <sup>112</sup> chambers [57]. Each precision tracking station that intersects this area is <sup>113</sup> used to look for straight-line track segment that point approximately back

to the interaction region. A straight line can be used for the track segments 114 because of the small distance between hits in a station. Track candidates are 115 first formed from segments with a second-coordinate hit (RPC/TGC/CSC 116 hit) by extrapolating between segments in different stations using a scan 117 around a rough estimate of the muon's momentum from one segment. If a 118 match is found, a track is fit to the two segments and the refined momentum 119 estimate is used to extrapolate to other stations. Once the full track has 120 been constructed, it is refit using the raw hit information instead of the 121 straight-line segments and taking into account the matter traversed by the 122 muon. 123

<sup>124</sup> Combined muons are formed by matching a track in the muon spectrom-<sup>125</sup> eter to a track in the inner detector. Tracks are matched using a  $\chi^2$  that <sup>126</sup> is defined as the difference in track parameters between the two tracks at <sup>127</sup> the point of closest approach to the beamline weighted by the combined <sup>128</sup> covariance matrix. If a match is found, a combined track is made that is a <sup>129</sup> statistical combination of the track parameters of the ID and MS tracks.

Tracks in the ID that are not associated with a combined muon and unused track segments in the MS can be used to form tagged muons. This is done by extrapolating ID tracks out to the muon system and looking for nearby track segment. In this case, the momentum of the muon is taken from the ID track.

Figure 5.4 shows the efficiency for a muon to be reconstructed as a com-135 bined muon (CB) and for a muon to be reconstructed as either a combined 136 or tagged (CB+ST) muon, measured in 8 TeV collisions using  $Z \rightarrow \mu\mu$ 137 events [58]. The reconstruction efficiency for combined muons is about 95%138 or better across most of the detector but suffers greatly for  $|\eta| < 0.1$ , where 139 room must be left for the services for the ID and calorimeter, and  $1.1 < \eta <$ 140 1.3, where the installation of muon chambers was not completed before the 141 first run of the LHC. The inclusion of tagged muons recovers the lost effi-142 ciency for  $1.1 < \eta < 1.3$  but only brings the efficiency up to about 65% for 143  $|\eta| < 0.1.$ 144

# <sup>145</sup> 5.4 Jet Reconstruction

Jets are formed by combining topological clusters of energy deposits in the calorimeter [59]. Clusters are seeded by cells with a signal that is at least four times greater than the expected electronic noise. Any adjacent cell with a signal-to-noise ratio greater than 2 is added to the cluster until there are no such cells remaining. Then all cells adjacent to those cells are added. An energy-weighted average of cell positions is used to define the position of thecluster.

<sup>153</sup> Clusters are combined using the anti- $k_t$  algorithm [60], which works by <sup>154</sup> comparing distances between objects,  $d_{ij}$ , to the distance between an object <sup>155</sup> and the beam,  $d_{iB}$ . These distances are defined as follows:

$$d_{ij} = \min(\mathbf{k}_{t,i}^{-2}, \mathbf{k}_{t,j}^{-2}) \frac{\Delta_{ij}^2}{\mathbf{R}^2}$$
(5.1)

$$d_{iB} = k_{t,i}^{-2} (5.2)$$

where  $k_{t,i}$  is the transverse momentum of object i,  $\Delta_{ij} = \sqrt{(y_i - y_j)^2 + (\phi_i - \phi_j)^2}$ , 157 and R is a parameter used to restrict the size of jets. These distances are 158 calculated starting with the cluster with the highest transverse energy. If 159 the minimum distance is one of the  $d_{ij}$ , then object j is added to object i, 160 and the distances are recomputed. Otherwise, object i is considered a com-161 plete jet and removed from the algorithm. This process continues until there 162 are no more clusters left to be combined. The factor of  $\frac{\Delta_{ij}^2}{B^2}$  in Equation 5.1 163 prevents the addition low-energy clusters outside a radius of R from the jet 164 center. Jets used for this measurement are clustered with R=0.4. 165

The efficiency for jet reconstruction (with a radius parameter of 0.6) 166 with respect to "truth" jets is shown as a function of the true jet  $p_{\rm T}$  for 167 jets with  $|\eta| < 1.9$  in Figure 5.5. Truth jets are defined using the same 168 clustering algorithm used for jet reconstruction, but instead of energy de-169 170 posits in the calorimeter, the inputs are stable particles from the MC truth record. All particles with a lifetime longer than 10 ps are included in the 171 clustering of truth jets with the exception of muons (which deposit little 172 energy in the calorimeter) and neutrinos (which escape undetected). Truth 173 jets give a good approximation of the object that would be reconstructed 174 if the calorimeter was perfectly efficient. The measured efficiency for jet 175 reconstruction is better than 99% for truth jet  $p_{\rm T}$  above 20 GeV. 176

After jets are formed, the jet energy must be recalibrated to account 177 for the difference in detector response between electromagnetic showers and 178 hadronic showers. Two methods of jet energy calibration are used in this 179 analysis. The simplest method, EM+JES, starts by treating every clus-180 ter as an electromagnetic shower. A correction is then applied based on 181 the measured jet energy at the electromagnetic scale. The second method, 182 LCW+JES, classifies individual clusters as electromagnetic or hadronic and 183 applies energy corrections at the cluster level. After these local corrections 184 are done, a second correction is applied to the jet as a whole. Figure 5.6 185 shows the fractional energy resolution measured in di-jet events in the 2011 186

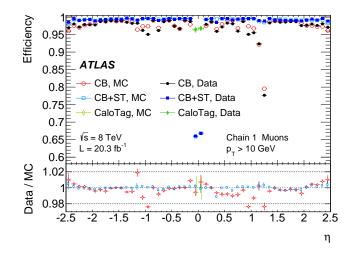


Figure 5.4: Muon reconstruction efficiency as a function of  $\eta$ . Filled points show the efficiencies measured in data while efficiencies measured in MC are indicated by the open points. Figure taken from Ref. [58].

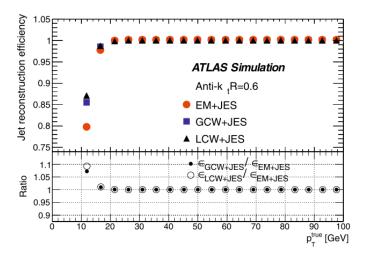


Figure 5.5: Jet reconstruction efficiency as a function of truth jet  $p_{\rm T}$  for jets with  $\eta < 1.9$  [59].

dataset [61] using two different techniques described in Ref. [62]. The energy resolution ranges from about 20% for jets with a  $p_{\rm T}$  of 30 GeV to 5% for jets with a  $p_{\rm T}$  of 1 TeV.

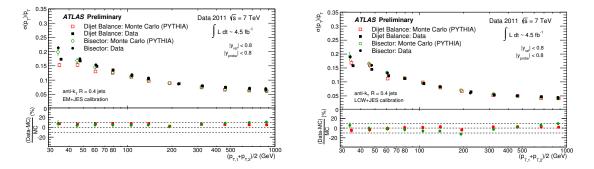


Figure 5.6: Jet energy resolution as a function of the average  $p_{\rm T}$  of the two jets in the event for jets calibrated using EM+JES (left) and LCW+JES (right). Filled points show the resolution measured in data while the resolution measured in MC is indicated by the open points. Figure taken from Ref. [61].

For jets with  $|\eta| < 2.5$ , tracks are also associated with the jets for sub-190 sequent use in identifying jets initiated by a b quark (see Section 5.4.1) 191 and rejecting jets originating from pileup interactions. Tracks are assigned 192 to jets via ghost association [63], which includes tracks in the anti- $k_t$  jet 193 clustering but assigns them all very low  $p_T$  so that they are only added to 194 nearby jets without otherwise influencing jet formation. Jet vertex fraction 195 (JVF) is defined as the ratio of the sum of the momenta of all tracks in 196 the jet that are associated with the primary vertex to the sum of the mo-197 menta of all tracks in the jet that are associated with some vertex in the 198 event. This quantity is used to reject jets originating from extra pp interac-199 tions. Figure 5.7 shows the number of reconstructed jets in  $Z \to \ell \ell$  events 200 measured in 7 TeV collisions as a function of the number of reconstructed 201 vertices with and without a requirement that jets have JVF greater than 202 0.75 [64]. Adding the JVF cut creates a nearly flat distribution, indicating 203 good rejection of pileup jets. 204

#### <sup>205</sup> 5.4.1 Tagging b jets

Due to the small mixing between the third generation of quarks and the first two generations, hadrons containing b quarks have relatively long life-

times and can travel a measurable distance before decaying. Typical life-208 times/distances traveled before decaying for B hadrons are around 1.5 ps/450 209  $\mu$ m. ATLAS has several algorithms that exploit this fact to identify jets ini-210 tiated by b quarks by using tracks associated to the jet to look for evidence 211 of a B hadron decay [65]. The IP3D algorithm compares 2D distributions 212 of transverse and longitudinal impact parameter significance, defined as the 213 ratio of the impact parameter to its uncertainty, to Monte Carlo templates 214 for b jets and light jets. A likelihood ratio between the two hypothesis is 215 then used to classify the jet in question. Two other algorithms, SV1 and 216 JetFitter, work by reconstructing secondary vertices inside the jet. SV1 217 only attempts to make one vertex for the B hadron decay while JetFitter 218 also attempts to resolve the subsequent D hadron decay. Both algorithms 219 classify jets using a likelihood from the comparison of several variables re-220 lated to secondary vertices (e.g. decay length significance, invariant mass of 221 tracking making the vertex) to simulated distributions. In addition to b jets 222 and light jets, JetFitter has a third classification for c jets. Jets used in this 223 analysis are classified using a neural network that combines IP3D, SV1, and 224 JetFitter called MV1. Figure 5.8 shows the efficiency in simulated  $t\bar{t}$  events 225 for b, c, and light jets to pass a selection on the MV1 output calibrated to 226 have an efficiency of 70% for b jets with  $p_{\rm T}$  greater than 20 GeV and  $|\eta| <$ 227 2.5 [66]. 228

# $_{229}$ 5.5 $E_{\mathrm{T}}^{\mathrm{miss}}$ Reconstruction

Although they don't interact with the detector, the presence of one or more neutrinos in an event can be deduced from an observed momentum imbalance in the transverse plane, referred to as missing transverse energy  $(E_{\rm T}^{\rm miss})$ . Longitudinal momentum imbalances cannot be used in the same manner since particles moving collinear with the beamline do not hit the detector.  $E_{\rm T}^{\rm miss}$  is reconstructed from topological clusters in the calorimeter and reconstructed muons [67].

Cluster energies are calibrated according to which (if any) reconstructed 237 object the cluster belongs to. Clusters matched to photons are calibrated 238 at the EM scale, jets with  $p_{\rm T}$  less than 20 GeV are calibrated at the LCW 239 scale without applying a subsequent JES correction, and all other objects 240 use their default calibration. Clusters not belonging to any reconstructed 241 object are also calibrated at the LCW scale. Muons are added using the 242 measured track momentum. In the case of isolated combined muons, energy 243 deposited in the calorimeter is taken into account by the combination of the 244

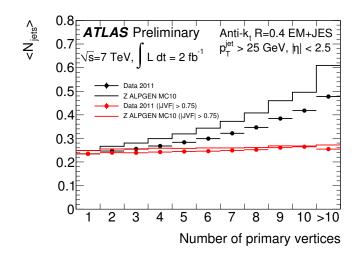


Figure 5.7: Number of reconstructed jets as a function of the number of reconstructed vertices with and without requiring the jet vertex fraction to be greater than 0.75. Figure taken from Ref. [64].

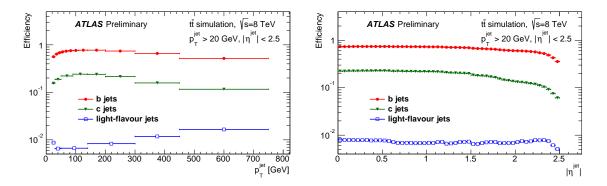


Figure 5.8: Efficiency as a function of  $p_{\rm T}$  (left) and  $|\eta|$  (right) in simulated  $t\bar{t}$  events for b, c, and light jets to pass a selection on the MV1 output calibrated to have an efficiency of 70% for b jets with  $p_{\rm T}$  greater than 20 GeV and  $|\eta| < 2.5$ . Figure taken from Ref. [66].

ID and MS tracks, so clusters associated with the muon are removed from the calculation. Figure 5.9 the  $E_x^{\text{miss}}$  and  $E_y^{\text{miss}}$  resolution as a function of the scalar sum of all transverse energy in the calorimeter and the transverse momenta of any muons in the event [68]. Similar resolutions of about 5 GeV for events with 50 GeV of transverse energy to about 25 GeV for events with 1 TeV of transverse energy are seen for several types of simulated collisions containing one or more energetic neutrinos.

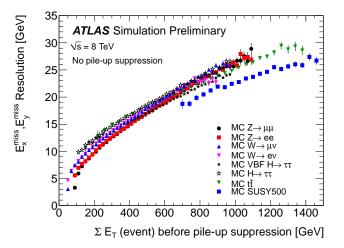


Figure 5.9:  $E_{\rm x}^{\rm miss}$  and  $E_{\rm y}^{\rm miss}$  resolution as a function of the scalar sum of all transverse energy in the calorimeter and the transverse momenta of any muons in the event. Figure taken from Ref. [68].

## 252 5.6 Event Selection

Events are collected using four single-lepton triggers, two which require the 253 lepton to be isolated and two which do not. The two isolated lepton triggers 254 require an electron or muon with  $p_{\rm T} > 24$  GeV while the remaining triggers 255 have higher thresholds of 36 GeV for muons and 60 GeV for electrons. Events 256 that pass these triggers are subjected to a number of quality requirements 257 before being considered for analysis. They are only used if they are included 258 in a "good runs list," a list of times when the detector was fully operational. 259 This selection is extremely efficient, rejecting less than 5% of recorded data. 260 Further checks are made that the event was written out correctly and that 261 there are no bursts of noise in the calorimeter [69] that interfere with the 262

event. The primary vertex in the event is required to have at least three tracks.

In the remaining events, electrons, muons, and jets are selected from 265 available reconstructed objects. Three types of selection criteria are defined 266 for leptons: a "tight" selection used to select the two same-sign leptons, 267 a "veto" selection used to find additional leptons present in  $W^{\pm}Z$  or ZZ268 events, and a "loose" selection used to estimate the background from events 269 with a single prompt lepton. Tight electrons must satisfy identification 270 criteria similar to the tight selection in Ref. [54] and are subject to several 271 additional requirements. They must have transverse energy greater than 272 25 GeV and  $|\eta| < 2.47$  with the transition between EM barrel and endcap 273 calorimeters excluded (1.37 <  $|\eta| < 1.52$ ). The transverse and longitudinal 274 impact parameters must satisfy  $\left|\frac{d_0}{\sigma(d_0)}\right| < 3$  and  $|z_0 \times \sin \theta| < 0.5$  mm. Finally, 275 calorimeter and tracking isolation selections are applied as follows: the sum 276 of the transverse energy of all calorimeter clusters  $(E_{\rm T}^{\rm iso})$  and the sum of the 277 transverse momenta of tracks  $(p_{\rm T}^{\rm iso})$  within a cone of radius R=0.3 in  $(\eta, \phi)$ 278 space are required to be less than 14 percent and 6 percent of the electron's 279 transverse energy, respectively. 280

In the veto and loose selections, electrons are only required to pass a loose identification selection. The  $E_{\rm T}$  threshold is lowered to 7 GeV, and the tracking isolation requirement is removed for veto electrons. For loose electrons, the impact parameter requirements are loosened to  $\left|\frac{d_0}{\sigma(d_0)}\right| < 10$ and  $|z_0 \times \sin \theta| < 5$  mm, and the isolation criteria are reversed but with a new upper limit that the ratio of transverse energy/momentum in the isolation cone to the electron's transverse energy must be less than 2.

Tight muons are required to be reconstructed as combined muons with 288 the same charge measured in the ID and MS. They must have  $p_{\rm T} > 25$ 289 GeV and  $|\eta| < 2.5$ . The ID tracks associated with these muons must pass a 290 number of quality requirements. The number of hits or dead sensors crossed 291 in the pixel detector must be at least one, and the same quantity for the 292 SCT must be at least five. For muons with  $0.1 < |\eta| < 1.9$ , the track 293 must have at least six hits in the TRT, and the fraction of these which 294 are outliers must not exceed 0.9. Tight muons also have the same impact 295 parameter requirements as tight electrons and similar isolation requirements 296 of  $E_{\rm T}^{\rm iso}/p_{\rm T}^{\mu} < 0.07$  and  $p_{\rm T}^{\rm iso}/p_{\rm T}^{\mu} < 0.07$ . 297

The selection of veto muons includes standalone and tagged muons. The  $p_{\rm T}$  threshold is lowered to 6 GeV, the calorimeter isolation requirement is dropped, and the track isolation selection is loosed to be less than 15 percent of the  $p_{\rm T}$  of the muon. Loose muons still must be combined, but just as for loose electrons, the impact parameter requirements are loosened,
and isolation requirements are reversed. In the remaining chapters, "tight"
and "loose" will be used to refer to the analysis selections rather than just
identification criteria unless otherwise specified.

Jets are required to have  $p_{\rm T}$  (calibrated with EM+JES) greater than 30 306 GeV and  $|\eta| < 4.5$ . In order to reduce the probability of selecting a jet from 307 a pileup interaction, jets with  $|\eta| < 2.4$  and  $p_{\rm T} < 50$  GeV are required to 308 have a jet vertex fraction greater than 0.5. Jets passing these selections are 309 tested with the MV1 algorithm. If the MV1 output exceeds a working point 310 with an efficiency of 70 percent for b jets, then the jet is classified as a b jet. 311 To avoid the case where a single particle is reconstructed as more than 312 one object, some removal of overlapping objects is performed. If the event 313 contains a tight electron and a jet with  $\Delta R(e, jet) < 0.3$ , then the jet is 314 removed. If the same is true for a jet and a tight muon, the event is rejected 315 since the muon is likely to originate from the decay of a hadron within the jet. 316 When estimating the background due to such hadron decays, jets are also 317 removed if they fall within  $\Delta R < 0.3$  of a loose lepton that is one of the two 318 highest- $p_{\rm T}$  leptons. For tight electrons and tight muons lying within  $\Delta R <$ 319 0.1 of each other, the electron is removed. This  $\mu/e$  overlap removal is also 320 extended to loose leptons within the leading two leptons when estimating 321 the non-prompt background. 322

After overlaps are resolved, events are selected with exactly two tight 323 leptons with the same electric charge and an invariant mass  $(m_{\ell\ell})$  between 324 them greater than 20 GeV. To reduce background from  $W^{\pm}Z$ , events with a 325 third lepton passing the veto selection are rejected. In the case where the two 326 tight leptons are both electrons, an additional requirement is made that the 327 invariant mass of the two electrons differs from the mass of the Z boson by 328 at least 10 GeV. Since two neutrinos are also expected in the event,  $E_{\rm T}^{miss} >$ 329 40 GeV is also required. Events are required to have at least two jets, but 330 in order to reduce the non-prompt background, the event is rejected if any 331 jet is classified as a b jet. Remaining events with an invariant mass between 332 the leading two jets  $(m_{ij})$  greater than 500 GeV are kept. This selection is 333 referred to as the inclusive signal region (Incl SR), and both the electroweak 334 and strong production mechanisms of  $W^{\pm}W^{\pm}ii$  are treated as signal in this 335 region. An addition signal region, called the VBS signal region (VBS SR), 336 is defined to consist of events in the inclusive signal region for which the 337 separation in rapidity between the two leading jets  $(|\Delta y_{ij}|)$  is greater than 338 2.4. In this region only the electroweak production is considered signal. 339

# Chapter 6

# Signal and Background Estimation

Events populating the signal regions come from a variety of physical pro-1 cesses. Estimates of the number of events produced by each process that 2 are selected by this analysis are necessary in order to obtain a meaningful 3 measurement of the  $W^{\pm}W^{\pm}ii$  process. These estimates are made with a 4 combination of Monte Carlo (MC) and data-driven techniques. Modeling 5 of background processes is tested in a variety of control regions designed to 6 be similar to the signal region but with a few selections changed to greatly enhance the contributions from particular backgrounds with respect to the 8 signal. 9

Processes that produce prompt same-sign leptons and  $W^{\pm}\gamma$  events are 10 estimated using Monte Carlo simulation. Events are generated in two steps: 11 the hard scattering of constituents within the proton followed by the hadroniza-12 tion of outgoing quarks and gluons. After events have been generated, the 13 interaction of particles with the detector is simulated [70] using GEANT4 [71]. 14 The event is then reconstructed from the simulated detector signals in the 15 same manner as for actual data. Following reconstruction, several small cor-16 rection factors are applied to make the simulation more accurately mimic 17 the data. Corrections are applied for the average number of pileup inter-18 actions, the average z position of vertices, the identification efficiencies of 19 leptons, the energy/momentum scale and resolution for leptons and jets, 20 and the b-tagging efficiency and mis-tag rate for jets. 21

Processes that produce just one prompt lepton or two opposite-sign leptons can enter the signal region due to secondary decays and instrumental effects. Contributions from these processes are estimated using data-driven techniques. In each case, the expected number of events in the signal region is determined by extrapolating from observed events in a very similar control region with a different lepton selection. The extrapolation factor between the regions is measured by comparing lepton selections in other control regions that are enriched in the background process of interest. These estimates are described in more detail in Sections 6.2.1 and 6.3.

# **31 6.1 Prompt Processes**

### 32 **6.1.1** $W^{\pm}W^{\pm}$

The electroweak and strong production of  $W^{\pm}W^{\pm}jj$  events are simulated 33 separately using the SHERPA [72] event generator and normalized to next-34 to-leading-order (NLO) cross sections calculated in two fiducial regions de-35 signed to mimic the signal regions of this analysis. The fiducial regions are 36 defined as follows: Events must contain two leptons  $(e/\mu)$  with the same 37 electric charge,  $p_{\rm T}$  greater than 25 GeV, and  $m_{\ell\ell} > 20$  GeV. There must also 38 be two truth jets found using the anti- $k_t$  algorithm with a radius parameter 30 of R=0.4 with a  $p_{\rm T}$  greater than 30 GeV and  $|\eta|$  <4.5, and the transverse 40 energy of the vector sum of the momenta of all neutrinos in the event must 41 be greater than 40 GeV. For any pair of leptons or lepton-jet pair,  $\Delta R(\ell, \ell)$ 42 or  $\Delta R(\ell, j)$  is required to be greater than 0.3. Events with  $m_{jj} > 500 \text{ GeV}$ 43 form the inclusive region while an additional requirement of  $|\Delta y_{ij}| > 2.4$ 44 defines the VBS region. 45

Cross sections in these two regions ("fiducial cross sections") are calcu-46 lated using POWHEGBOX [73,74] with CT10 [12] parton distribution functions 47 (PDFs) and with PYTHIA8 [75,76] used for parton showering and underlying 48 event. The acceptance, the fraction of generated events that pass fiducial 49 region selections, of the SHERPA samples is then used to convert the fiducial 50 cross sections into cross sections corresponding to the phase space in which 51 the samples are generated, which are then used to normalize the samples to 52 the correct luminosity. The electroweak process has predicted fiducial cross 53 sections of  $1.00 \pm 0.06$  fb and  $0.88 \pm 0.05$  fb in the inclusive and VBS re-54 gions, respectively. For the strong process, the corresponding cross sections 55 are  $0.35 \pm 0.05$  fb and  $0.098 \pm 0.018$  fb. The uncertainties on these num-56 bers account for uncertainties from several sources: PDFs, parton shower 57 modeling, choice of renormalization and factorization scales, and the differ-58 ence between cross sections calculated with POWHEGBOX and VBFNLO [77]. 59 The derivation of these uncertainties is described in detail in Chapter 7. 60 In the absence of a NLO calculation for the combined (both electroweak 61

and strong production)  $W^{\pm}W^{\pm}jj$  process, the effect of interference between 62 electroweak  $W^{\pm}W^{\pm}jj$  and strong  $W^{\pm}W^{\pm}jj$  is determined at leading order 63 with SHERPA by comparing the cross section of the combined process to the 64 sum of the cross sections of the two sub-processes. Interference is found to 65 increase the total cross section by 12 percent in the inclusive region and 7 66 percent in the VBS region. The prediction for the electroweak production 67 of  $W^{\pm}W^{\pm}ii$  is scaled up to include the contribution from interference, and 68 the uncertainty on the interference component is taken to be 50%. 69

## 70 **6.1.2** $W^{\pm}Z$

As for  $W^{\pm}W^{\pm}jj$  production, the  $W^{\pm}Z$  process is split into electroweak and 71 strong production processes which are simulated separately and normalized 72 to NLO cross sections in each fiducial region. SHERPA is again used for the 73 event generation, and the fiducial cross sections are calculated using VBFNLO. 74 Since VBFNLO cannot be interfaced with a parton showering program at 75 NLO, the normalization is done at the parton level. The truth record in 76 SHERPA is used to identify the products of the hard scatter, and only those 77 objects are used to calculate the acceptance. By normalizing the samples 78 this way, the effect of showering on the fiducial cross sections is taken directly 79 from Sherpa. 80

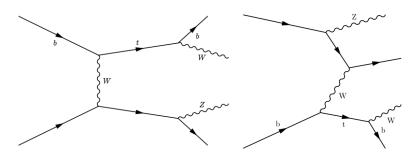


Figure 6.1: Representative diagrams for tZj production with the subsequent top decay yielding WZ plus two jets.

The normalization of the electroweak production of  $W^{\pm}Z$  contains a further complication. This cross section receives a contribution from the associated production of a top quark with a Z boson and an additional parton, illustrated in Figure 6.1, where a W is produced in the top decay. This class of diagrams is neglected by VBFNLO due to the requirement of a b quark in the initial state, but they account for almost a third of events

$\leq 1$ jet Control Region				
	ee	$e\mu$	$\mu\mu$	Total
$W^{\pm}W^{\pm}$ jj ewk+strong	$2.72\pm0.30$	$8.2\pm0.8$	$4.2\pm0.4$	$15.1 \pm 1.5$
OS prompt leptons	$152 \pm 17$	$24 \pm 4$	—	$177 \pm 21$
$W\mathrm{Z}/\gamma^*,\!Z\mathrm{Z}$	$46 \pm 8$	$130\pm23$	$75 \pm 13$	$251 \pm 43$
$W{+}\gamma$	$39 \pm 11$	$59 \pm 17$	$0.04\pm0.04$	$98 \pm 29$
$t\bar{t}+W/Z$	$0.34 \pm 0.15$	$0.8\pm0.4$	$0.56\pm0.25$	$1.7 \pm 0.7$
Other non-prompt	$38 \pm 15$	$65\pm26$	$8\pm5$	$111 \pm 30$
Total Predicted	$278\pm28$	$288 \pm 42$	$88 \pm 14$	$654 \pm 69$
Data	288	328	101	717

Table 6.1: Event counts in the  $\leq 1$  jet control region.

populating the fiducial regions. To account for this, a new normalization
is derived by splitting the sample into events that contain a b quark in the
initial state and events without an initial b quark. The formula for the cross
section used to normalize the SHERPA sample is:

$$\sigma_{norm} = \sigma_{fid}^{\text{VBFNLO}} / A_{ME}^{without-b} + \sigma^{\text{SHERPA}} \times f_b \tag{6.1}$$

where  $\sigma_{fid}^{\text{VBFNLO}}$  is the fiducial cross section calculated using VBFNLO,  $A_{ME}^{without-b}$  is the parton-level acceptance of the SHERPA subsample without any b quarks in the initial state,  $\sigma^{\text{SHERPA}}$  is the total sample cross section calculated with SHERPA, and  $f_b$  is the fraction of generated events that contain a b quark in the initial state. In this way, the "without-b" subsample is normalized to the VBFNLO cross section while the SHERPA cross section is used for the "with-b" subsample.

Predictions for the  $W^{\pm}Z$  background are tested in two control regions 98 (CRs), referred to as the < 1 jet CR and the tri-lepton CR. The < 1 jet 99 CR is defined by inverting the signal region selection on jet multiplicity to 100 accept only events with fewer than two jets. Subsequent selections on jet-101 based quantities are also dropped. This region is used to test the modeling 102 of lepton kinematics in events where one of the leptons from the Z decay is 103 not reconstructed. Figure 6.2 shows lepton  $p_{\rm T}$  and  $\eta$  distributions for the 104  $e\mu$  and  $\mu\mu$  channels (the *ee* channel is dominated by conversion background, 105 to be discussed in Section 6.2). The number of data events in this control 106 region is shown in Table 6.1. Good agreement is observed between the data 107 and the prediction. 108

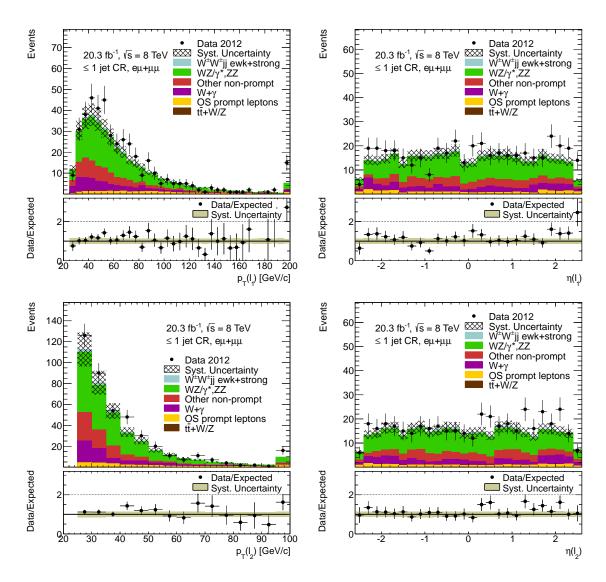


Figure 6.2: Lepton  $p_{\rm T}$  (left) and  $\eta$  (right) distributions for the leading (top) and sub-leading (bottom) leptons for  $e\mu$  and  $\mu\mu$  events in the  $\leq 1$  jet control region.

Tri-lepton Control Region				
	$e^{\pm}e^{\pm}\ell^{\mp}$	$e^{\pm}\mu^{\pm}\ell^{\mp}$	$\mu^{\pm}\mu^{\pm}\ell^{\mp}$	Total
$W^{\pm}W^{\pm}$ jj ewk+strong	$0.01\pm0.01$	$0.11\pm 0.02$	$0.00\pm0.00$	$0.12 \pm 0.02$
$WZ/\gamma^*$	$32 \pm 5$	$96\pm16$	$57 \pm 10$	$186 \pm 31$
$ZZ \rightarrow 4l$	$2.2 \pm 0.6$	$5.3 \pm 1.3$	$1.8\pm0.5$	$9.2 \pm 2.1$
Non-prompt	$0.48\pm0.32$	$6 \pm 5$	$0.00\pm0.00$	$7\pm5$
$t\bar{t}+W/Z$	$0.65\pm0.28$	$2.4\pm1.0$	$1.0\pm0.5$	$4.1 \pm 1.7$
Total Predicted	$36 \pm 6$	$110 \pm 18$	$60 \pm 10$	$206\pm33$
Data	40	104	48	192

Table 6.2: Event counts in the tri-lepton control region.

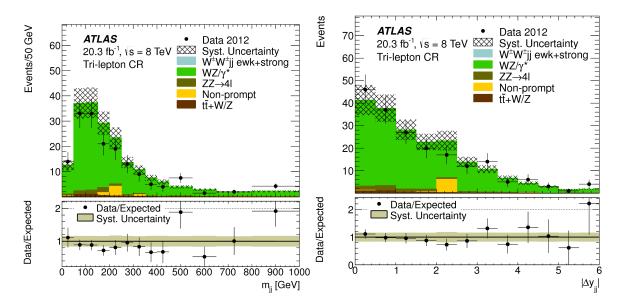


Figure 6.3: Di-jet invariant mass distribution (left) and rapidity difference distribution (right) for events in the tri-lepton control region.

The tri-lepton CR is defined by inverting the third lepton veto. Events 109 containing a fourth lepton passing the veto lepton definition are still rejected. 110 Since the  $W^{\pm}Z$  process contains an electroweak component that is sensitive 111 to the same aQGCs that affect  $W^{\pm}W^{\pm}jj$ , the  $m_{ij}$  and  $|\Delta y_{ij}|$  selections 112 are dropped. This region provides a test of the modeling of jet kinematics 113 in the  $W^{\pm}Z$  MC. Event counts are shown in Table 6.2, and the  $m_{ij}$  and 114  $|\Delta y_{ij}|$  distributions are shown in Figure 6.3. A slight excess is visible in 115 the tail of the  $m_{ii}$  distribution with a statistical significance of  $1.9\sigma$  if a cut 116 is placed at  $m_{ii} > 500$  GeV. As previously mentioned, this region is not a 117 good control region because event counts here would be enhanced by the 118 same anomalous couplings that would enhance rates in the signal regions. 119 Nonetheless, many distributions were checked for evidence of mismodeling 120 of event kinematics. No evidence of mismodeling was found, and the excess 121 is attributed to a statistical fluctuation. 122

#### 123 6.1.3 Other Prompt Backgrounds

 $W^{\pm}Z$  production accounts for about 90% of the prompt background. Other 124 sources of prompt same-sign leptons include the associated production of 125 a  $t\bar{t}$  pair and a W or Z, ZZjj production, and multiple parton interac-126 tions (MPI) where each interaction contributes some of the leptons/jets (e.g. 127  $W^{\pm}j + W^{\pm}j$ ).  $t\bar{t}V \ (V = W, Z)$  events are generated with MADGRAPH [78] 128 and showered with PYTHIA8. ZZjj is simulated using SHERPA. Several 129 MPI processes capable of producing two same-sign leptons and two jets are 130 simulated with PYTHIA, and this contribution is found to be negligible. 131

# <sup>132</sup> 6.2 Background from Photon Conversions

## 133 6.2.1 Charge Misidentification

Events that contain two prompt opposite-sign leptons can enter the sig-134 nal regions if the charge of one of the leptons is misidentified. The domi-135 nant mechanism for charge misidentification ("charge misID") of electrons 136 is the "trident" process, shown in Figure 6.4, in which the prompt electron 137 radiates an energetic photon that subsequently converts into an  $e^+e^-$  pair. 138 The rate of charge misID in combined muons has been found to be negligible 139 and is therefore not considered in this analysis. Events entering the signal 140 regions due to charge misID consist mainly of fully leptonic  $t\bar{t}$  decays and 141 Drell Yan lepton pair production according to simulation. However, this 142 background is estimated using a data-driven technique. 143

First, the rate of charge misID is measured in a data sample enriched 144 in  $Z \to ee$  events. This sample is selected by looking for two tight elec-145 trons with a di-lepton invariant mass  $(m_{\ell\ell})$  between 70 GeV and 100 GeV, 146 with no requirement made on the lepton charges. An asymmetric window 147 around the Z mass is used account for energy lost to the soft electrons that 148 are not reconstructed when the trident process causes an electron's charge 149 to be misidentified. Contributions to this region from other processes are 150 estimated and subtracted using the sidebands of 40 GeV  $< m_{\ell\ell} < 70$  GeV 151 and 100 GeV <  $m_{\ell\ell}$  <130 GeV. The size of the subtraction is less than 1%152 of the total number of events. 153

A likelihood fit is used to measure the charge-misID rate as a function of  $p_{\rm T}$  and  $\eta$ , taking into account that either electron in a same-sign pair could be the misidentified one. The number of total events and same-sign events are counted in bins of  $p_{\rm T}$  and  $\eta$ , and charge-misID rates are chosen for each bin in order to maximize a Poisson-based likelihood given the observed counts:

$$ln(\mathcal{L}(\epsilon|N, N_{SS})) = \sum_{i,j} N_{SS}^{i,j} ln(N^{i,j}(\epsilon^i + \epsilon^j)) - N^{i,j}(\epsilon^i + \epsilon^j)$$
(6.2)

where N is the total number of events,  $N_{SS}$  is the number of same-sign 160 events,  $\epsilon$  is the charge-misID rate, and the superscripts i and j refer to the 161  $\eta/p_{\rm T}$  bin of the first and second electron, respectively. Charge-misID rates 162 are shown in Figure 6.5. Since the rates for bremsstrahlung and photon 163 conversion depend on the amount of material traversed, the rate for charge 164 misID exhibits a strong  $\eta$  dependence. This likelihood assumes that the 165 probability to obtain a same-sign event is  $\epsilon^i + \epsilon^j$ , which ignores the possibility 166 that both electrons have their charge misidentified. This is justified by the 167 low charge-misID rate, which is a few tenths of a percent over most of the 168  $\eta$  range and is still only about 2% near  $|\eta| = 2.5$ . 169

The measured charge-misID rate is used to predict the amount of back-170 ground from charge misID by weighting opposite-sign events. Data events 171 are selected using all of the signal region criteria except that the requirement 172 that the leptons have the same charge is changed to require opposite charges. 173 Then, for each electron in the event, a charge-misID event is added to the 174 background estimation, weighted by the charge-misID rate in the  $\eta/p_{\rm T}$  bin 175 corresponding to that electron. This accounts for the ambiguity in the ee 176 channel as to which electron had its charge misidentified. 177

In addition to the rate of charge misID, an energy correction is determined using  $Z \rightarrow ee$  MC. For each electron, the difference between the true

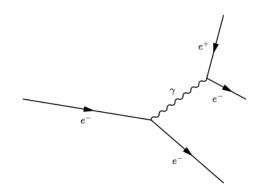


Figure 6.4: Illustration of the "trident" process. If most of the energy of the original  $e^-$  ends up with the  $e^+$ , it is likely that only the  $e^+$  will be reconstructed. Since the momentum of this lepton is very similar to that of the original prompt lepton, this is referred to as charge misidentification.

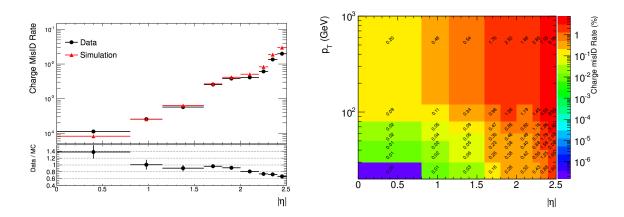


Figure 6.5: Charge-misID rates derived for electrons as a function of  $|\eta|$  (left) and as a function of both  $|\eta|$  and  $p_{\rm T}$ .

energy and the reconstructed energy is obtained by matching reconstructed 180 electrons to the original prompt electron in the MC truth record. The dis-181 tribution of this energy difference is shown in two  $\eta$  bins in Figure 6.6 for 182 reconstructed electrons that have the same/opposite charge as the original 183 prompt electron. The difference in the mean of these distributions is used to 184 correct the energy of an electron in a charge-misID event, and the quadrature 185 difference in resolution is used to apply a Gaussian smearing to the energy 186 of these electrons. These energy corrections are shown as a function of  $|\eta|$  in 187 Figure 6.7. The invariant mass distribution of same-sign di-electron events, 188 shown in Figure 6.9, is used to further calibrate the energy corrections. The 189 size of the energy shift is increased by 35%, and the smearing is increased 190 by 25% to make the predicted Z peak agree with data. These energy cor-191 rections are applied before kinematic selections to allow for migration into 192 or out of the signal regions. 193

Charge misID (denoted "OS prompt leptons" in tables and figures) pro-194 vides the main source of background for events with two same-sign electrons 195 prior to the  $m_{ii} > 500$  GeV selection. The *ee* channel of the  $\leq 1$  jet CR 196 is used to test the predicted rate and lepton kinematics. Figure 6.8 shows 197 the  $\eta$  distributions for electrons in this region. The agreement observed in 198 these distributions validates the measured charge-misID rates. Derivation of 199 systematic uncertainties for this background estimate is discussed in Chap-200 ter 7. The total uncertainty varies between 15% and 30% depending on 201 region and channel and comes mainly from a comparison of predicted and 202 observed counts of same-sign di-lepton events in  $t\bar{t}$  MC. 203

### 204 **6.2.2** $W^{\pm}\gamma$

Events with a W boson and on-shell photon can produce same-sign leptons 205 if the photon converts in the detector and one of the leptons is not recon-206 structed.  $W^{\pm}\gamma$  production can be separated into strong and electroweak 207 processes, which are estimated using ALPGEN [79]+HERWIG/JIMMY [80,81] 208 and SHERPA, respectively. The uncertainty on the total cross section (strong 209 + electroweak) is taken to be 17% following a measurement of this cross sec-210 tion in  $\sqrt{s} = 7$  TeV collisions [17]. A comparison of charge-misidentification 211 rates measured in data and MC is used to test the modeling of the conversion 212 rate vs.  $\eta$  since the emission and subsequent conversion of a photon is the 213 dominant mechanism for charge misID. Observed differences are translated 214 into an uncertainty on the  $W^{\pm}\gamma$  yield as described in Chapter 7. 215

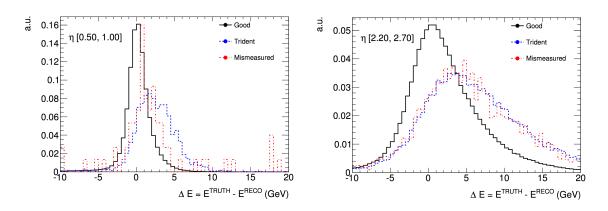


Figure 6.6: Difference between true energy and reconstructed energy for electrons reconstructed with the correct charge (black), electrons reconstructed with the wrong charge due to the trident process (blue), and electrons reconstructed with the wrong charge when no trident was evident in the MC truth record (red).

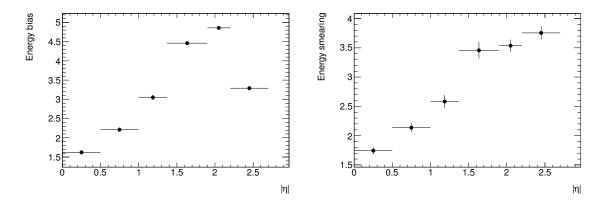


Figure 6.7: Energy bias (left) and smearing (right) corrections in units of GeV derived using  $Z \rightarrow ee$  MC.

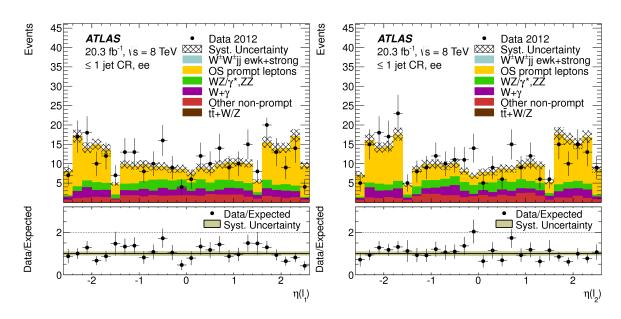


Figure 6.8: Electron  $\eta$  distributions for the leading (left) and sub-leading (right) electrons in the  $\leq 1$  jet control region.

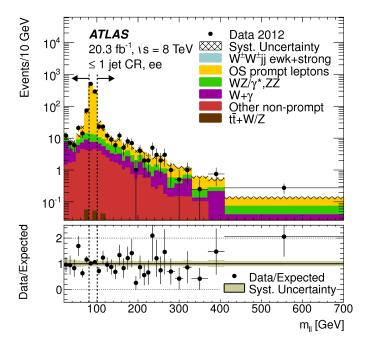


Figure 6.9: Di-electron invariant mass distribution for events in the  $\leq 1$  jet control region.

# <sup>216</sup> 6.3 Other Non-prompt Background

Non-prompt background in which one or both leptons come from hadron 217 decays or hadrons misidentified as leptons is estimated using a data-driven 218 method. In a manner similar to the estimation of the charge-misID back-219 ground, a rate for an isolated lepton to result from hadronic activity is 220 measured from data in a control region enriched in such events, and this 221 rate is applied to data in regions very similar to the signal regions in order 222 to predict the non-prompt background. A "tight + loose" (TL) region used 223 to predict this background is defined by requiring one of the leptons to pass 224 the loose selection instead of the tight selection. Since the loose leptons are 225 non-isolated, the vast majority of them come from hadronic activity. The 226 small contribution from prompt leptons is subtracted using MC. To obtain 227 the number of events that enter the signal region with two tight leptons, 228 events in the TL region are weighted by a "fake factor." 229

The fake factor used is the ratio of the number of tight leptons to the 230 number of loose leptons measured from data in a region where both tight 231 and loose leptons come predominantly from hadrons. This analysis uses a 232 "di-jet" region which requires one lepton and one jet, each with  $p_{\rm T}$  greater 233 than 25 GeV, with additional kinematic selections to pick out events that 234 are likely to be misreconstructed di-jet events. The transverse mass formed 235 using the lepton and  $E_{\rm T}^{\rm miss}$  is required to be less the 40 GeV, and  $\Delta \phi(\ell, j)$ 236 must be greater than 2.8. Figure 6.10 shows the transverse mass distribution 237 for events with a tight lepton after all other cuts have been applied. The 238 remaining contribution from processes with prompt leptons, which comes 239 mainly from W+jets and Z+jets, is estimated using MC and subtracted. 240 This prompt contamination accounts for about half of the events with a 241 tight lepton. 242

The single leptons triggers used for the analysis have isolation require-243 ments for low- $p_{\rm T}$  leptons and cannot be used to select an event with a single 244 non-isolated lepton. Therefore, different triggers are used to select the di-245 jet sample. Electron plus jet events are selected using a trigger that looks 246 for calorimeter clusters with energy greater than 20 GeV that passes loose 247 electron identification requirements. Muon + jet events are selected using 248 a trigger similar to the nominal single muon trigger but with no isolation 249 requirements. Due to the track quality requirements in this trigger and the 250 loosened impact parameter requirements of the loose muon selection, this 251 trigger is still expected to have some inefficiency for loose muons with re-252 spect to tight muons. The efficiency of the trigger for each type of muon 253 was compared using a tag-and-probe method and found to be 10% higher 254

b-tag Control Region					
	ee	$e\mu$	$\mu\mu$	Total	
$W^{\pm}W^{\pm}$ jj ewk+strong	$0.81\pm0.10$	$2.57\pm0.28$	$1.55\pm0.18$	$4.9 \pm 0.5$	
OS prompt leptons	$22 \pm 5$	$27 \pm 6$	—	$49 \pm 11$	
$t\bar{t}+W/Z$	$7.1\pm3.1$	$18 \pm 8$	$11 \pm 4$	$36 \pm 15$	
$WZ/\gamma^*, ZZ$	$2.3\pm0.5$	$4.9\pm0.9$	$2.2\pm0.4$	$9.4 \pm 1.6$	
$W{+}\gamma$	$1.7\pm0.7$	$2.3\pm0.9$	—	$4.0 \pm 1.4$	
Other non-prompt	$6.7\pm2.5$	$20 \pm 8$	$10 \pm 5$	$37 \pm 10$	
Total Predicted	$40 \pm 6$	$75 \pm 13$	$25\pm7$	$140 \pm 22$	
Data	46	82	36	164	

Table 6.3: Event counts in the b-tag control region.

<sup>255</sup> for tight muons. This difference is applied as a correction to the measured <sup>256</sup> fake factor.

The probability for a non-prompt lepton to be isolated depends on the 257 kinematics of both the lepton and the jet that gave rise to that lepton (the 258 "underlying jet"). The first dependence is taken into account by binning 259 the fake factor in lepton  $p_{\rm T}$  and  $|\eta|$ , as shown in Figure 6.13, but the second 260 is more difficult to deal with since the underlying jet is usually not recon-261 structed. In the di-jet region used to measure the fake factor, the  $p_{\rm T}$  of this 262 jet can be inferred from the  $p_{\rm T}$  of the jet on the opposite side. Events in this 263 region are used to derive a relationship between lepton  $p_{\rm T} + E_{\rm T}^{\rm iso}$  and the 264 average  $p_{\rm T}$  of the underlying jet. Average jet  $p_{\rm T}$  as a function of lepton  $p_{\rm T}$  + 265  $E_{\rm T}^{\rm iso}$  is shown in Figure 6.11. This relationship is found to be linear and is 266 applied to the loose leptons in events in the TL region to obtain the  $p_{\rm T}$  dis-267 tribution for underlying jets in those events. In order to increase statistics 268 for this distribution, the  $m_{ij}$  and  $|\Delta y_{ij}|$  cuts are not applied. Events in the 269 di-jet region are then re-weighted so that the jet  $p_{\rm T}$  distribution matches the 270 distribution for underlying jets in the TL region. The effect of re-weighting 271 the jet  $p_{\rm T}$  distribution on the lepton isolation distributions is shown in Fig-272 ure 6.12. After re-weighting, the isolation distribution for loose leptons in 273 the di-jet region agrees much better with the TL region. 274

Since non-prompt leptons originate mainly from *B* hadron decays, the non-prompt prediction is tested in a b-tag CR, which is defined by inverting the b-jet veto to require the presence of at least one b-tagged jet. The  $m_{jj}$ and  $|\Delta y_{jj}|$  selections are also dropped to increase statistics. Event counts for this region are shown in Table 6.3. Transverse momentum distributions for

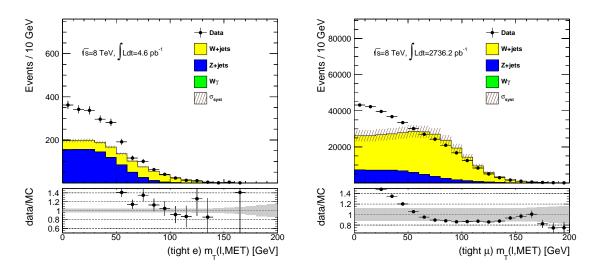


Figure 6.10:  $m_{\rm T}(\ell, E_{\rm T}^{\rm miss}$  distribution for events with a tight electron (left) or muon (right) after all other di-jet selections have been applied.

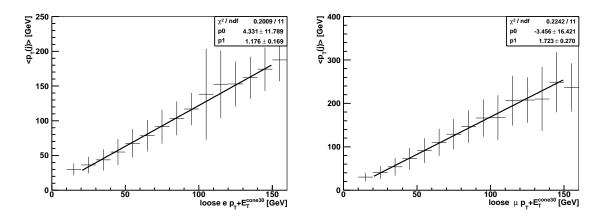


Figure 6.11: Average  $p_{\rm T}$  of the jet vs. loose lepton  $p_{\rm T} + E_{\rm T}^{\rm iso}$  for events passing the di-jet selection.

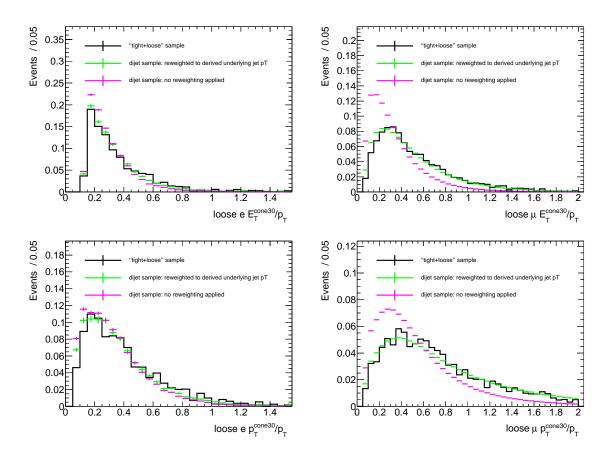


Figure 6.12:  $E_{\rm T}^{\rm iso}$  (top) and  $p_{\rm T}^{\rm iso}$  (bottom) as fractions of lepton  $p_{\rm T}$  for loose electrons (left) and muons (right). The black curve shows the distribution for the TL region while the pink and green points show the distribution for the di-jet region before and after re-weighting.

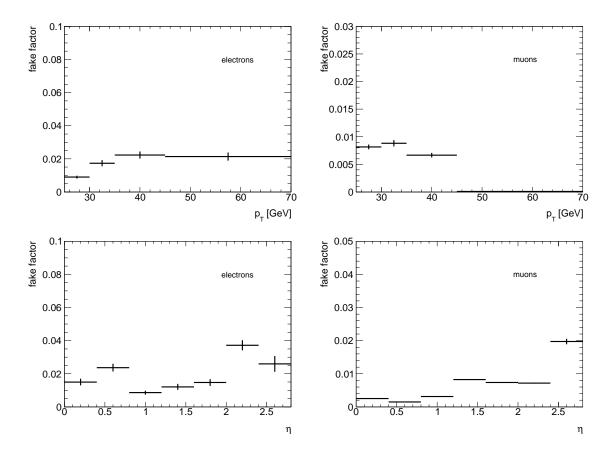


Figure 6.13: Fake factors as a function of lepton  $p_{\rm T}$  (top) and  $|\eta|$  (bottom) for electrons (left) and muons (right).

the leading and sub-leading leptons are given in Figure 6.14. Uncertainties

 $_{281}$  on the non-prompt prediction vary from 35% to 50% depending on channel

<sup>282</sup> and are mainly due to contamination from prompt leptons in the di-jet region

and the jet  $p_{\rm T}$  re-weighting. These will be discussed in detail in Chapter 7.

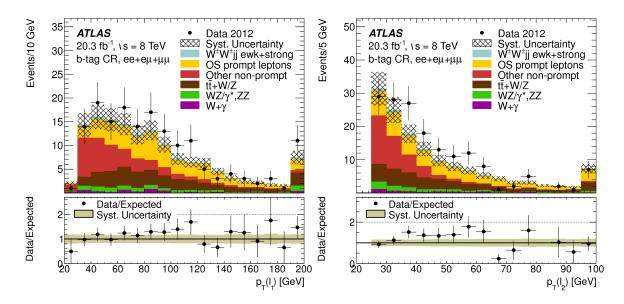


Figure 6.14: Lepton  $p_{\rm T}$  distributions for the leading (left) and sub-leading (right) leptons in the b-tag control region.

# Chapter 7

# Systematic Uncertainties

Estimates of background and signal yields in the signal regions have several 1 sources of systematic uncertainty. For MC-based predictions, these sources 2 can be grouped into two categories: theoretical uncertainties on the cross 3 section used to normalize the Monte Carlo, and uncertainties on correction 4 factors applied to make reconstructed objects in MC more accurately match 5 the data. None of these systematic uncertainties apply to backgrounds that 6 are estimated using data-driven techniques. For these backgrounds, the 7 uncertainty comes mainly from the purity of the data sample and the ex-8 trapolation to the signal region. 9

## <sup>10</sup> 7.1 Uncertainties due to Theoretical Modeling

Together,  $W^{\pm}W^{\pm}jj$  and  $W^{\pm}Zjj$  make up about three quarters of the total 11 predicted events in the signal regions, so a good understanding of the uncer-12 tainties on their cross sections is needed in order to compare the prediction 13 with data. Sources of uncertainty common to these processes include the 14 uncertainty on the parton distribution functions of the proton, the depen-15 dence of the calculated cross section on the choice of renormalization and 16 factorization scales, and the dependence of event kinematics on the show-17 ering model. The total uncertainties for these four diboson processes are 18 summarized in Table 7.1. 19

Parton distribution functions are not known from first principles and must be measured from fits to collider data as described in Chapter 2. Uncertainties on PDF parameters from these fits translate into uncertainties on cross sections predicted using these PDFs. PDF uncertainties are evaluated by repeating the cross section calculation several times using alternate

PDFs with parameters varied up or down by their 90% C.L. intervals. The 25 differences between the cross sections obtained using the alternate PDFs 26 and the central value are then summed in quadrature and scaled down to 27 obtain 68% C.L. uncertainties. Assuming the systematic uncertainty fol-28 lows a Gaussian distribution, this scale factor is 1.645. Scale uncertainties 29 are derived by independently varying the renormalization and factorization 30 scales by a factor of 2 in either direction. The two cases where one scale has 31 been halved and the other doubled are excluded, and the spread in cross 32 section among the remaining variations is used as the uncertainty due to 33 higher order QCD corrections. Two models for simulating parton showers 34 are compared. PYTHIA uses  $p_{\rm T}$  ordering, it generates QCD radiation in order 35 of descending  $p_{\rm T}$  until reaching the scale of confinement, while HERWIG++ 36 generates radiation in order of decreasing emission angle. Fiducial cross 37 sections are obtained using each model, and the difference is taken as an 38 uncertainty. 39

The use of different NLO generators for  $W^{\pm}W^{\pm}jj$  and  $W^{\pm}Zjj$  was made necessary by the fact that neither generator had an NLO calculation available for all 4 process. The only process to be implemented in both was the electroweak production of  $W^{\pm}W^{\pm}jj$ . The predictions of the two generators for this process were compared and found to agree within 5%. The difference between them is taken as an uncertainty on the  $W^{\pm}W^{\pm}jj$  cross sections.

The electroweak production of  $W^{\pm}Zjj$  has a large additional uncertainty due to the tZj component, which is missing from VBFNLO. This component is estimated at LO using SHERPA, and a 50% uncertainty is taken. This translates to a 20% uncertainty on the total electroweak  $W^{\pm}Zjj$  cross section and is the dominant systematic uncertainty for this process. However, the effect on the total  $W^{\pm}Zjj$  uncertainty is very small due to the dominance of strong production.

The strong production of  $W^{\pm}Z$  + jets is unique among these processes in 54 that there exist diagrams with zero or one jet in the final state. This process 55 therefore receives an additional contribution from  $W^{\pm}Z + 1$  jet events where 56 a second jet is produced from the parton shower. The uncertainty of this 57 component is estimated using a LO MADGRAPH  $W^{\pm}Z + 1$  parton sample. 58 This sample is then showered with both PYTHIA8 and HERWIG++, and 59 the difference is taken as an uncertainty. The resulting uncertainty on the 60  $W^{\pm}Z_{jj}$  cross section is 6%. 61

The uncertainty on strong  $W^{\pm}\gamma$  production is derived from the uncertainties on the 2-jet and 3-jet bins of a  $d\sigma_{W\gamma}/dN_{jets}$  measurement performed by ATLAS using 7 TeV data [17] as well as the uncertainty on the inclusive

Theoretical uncertainties (%)				
Region	$W^{\pm}W^{\pm}jj$ ewk	$W^{\pm}W^{\pm}jj$ strong	$W^{\pm}Zjj$ ewk	$W^{\pm}Zjj$ strong
Inclusive SR	6	14	23	16
VBS SR	6	18	27	12

Table 7.1: Total theoretical uncertainties for the  $W^{\pm}W^{\pm}jj$  and  $W^{\pm}Zjj$  processes in the Inclusive and VBS signal regions (SR).

cross section from the same measurement. The resulting uncertainty is 17%. 65 A 100% uncertainty is taken on the electroweak component. Uncertainties 66 on  $t\bar{t}V$  production due to PDF uncertainties and scale choice have been 67 previously studied [82], and a conservative uncertainty of 30% is assigned. 68 Unlike,  $W^{\pm}W^{\pm}jj$  and  $W^{\pm}Zjj$ , ZZjj is only estimated at leading order. 69 Its uncertainty is estimated assuming that it has a similar ratio of NLO to 70 LO cross sections and similar scale/PDF uncertainties to the other diboson 71 processes. The total estimated uncertainty for ZZjj production is 19%. 72

# 73 7.2 Systematic Uncertainties from Object Recon 74 struction/Identification

75 Another source of uncertainty on MC-based prediction comes from the simulation on the interaction between particles produced in a proton-proton 76 collision and the detector. Each reconstructed object has some uncertainty 77 on its energy scale and resolution. If it has been required to pass some 78 particle identification, there is also an uncertainty associated with the effi-79 ciency of these selections. The uncertainties affecting this measurement are 80 listed below. In order to estimate the effect of these per-object uncertainties 81 on the event yield in the signal regions, the analysis is repeated twice for 82 each source of uncertainty, with that parameter varied up or down by its 83 uncertainty. The difference between the event yields with the variation and 84 the nominal yield is taken as the uncertainty due to that parameter. The 85 contributions from different sources of uncertainty vary by process, but their 86 relative importance can be seen in Tables 7.9 and 7.10. 87

- Jet energy scale/resolution (JES/JER): separate variations for lightflavor and heavy-flavor jets
- Jet vertex fraction cut efficiency

- Jet b-tag inefficiency
- Electron energy scale/resolution
- Muon momentum scale/resolution
- Electron identification efficiency
- Muon identification efficiency
- Identification efficiency for leptons passing the "veto" selection
- Single lepton trigger efficiencies
- $E_{\rm T}^{\rm miss}$  scale/resolution
- Energy scale of clusters not associated with reconstructed objects

### 100 7.2.1 Jet Uncertainties

The jet energy scale and its uncertainties are estimated using a variety of 101 in situ techniques that use an object recoiling off of a jet as a reference for 102 the true  $p_{\rm T}$  of the jet [83]. Z+jet and  $\gamma$ +jet events are used for central jets 103 while di-jet events for forward jets. Studies of JES performance using Z+jet 104 events are discussed in more detail in Chapter 8. For jets with  $p_{\rm T}$  greater 105 than 1 TeV, uncertainties are estimated from events where a high- $p_{\rm T}$  jets 106 recoils against multiple low- $p_{\rm T}$  jets and from the calorimeter response to 107 single hadrons measured using test-beam data and minimum bias collisions. 108 Figure 7.1 shows these uncertainties for different  $\eta$  and  $p_{\rm T}$  ranges. 109

Additional uncertainties are estimated for specific effects, including cor-110 rections for pileup, close-by jets, at the type of parton that initiated the 111 jet. The effects of pileup are studied by examining the dependence of the 112 reconstructed jet  $p_{\rm T}$  on the number of reconstructed primary vertices and on 113 the average number of interactions per bunch crossing. The reconstructed 114  $p_{\rm T}$  can be compared to either the true  $p_{\rm T}$  in MC or the  $p_{\rm T}$  of a recoiling ob-115 ject. The difference in the corrections derived using each reference is taken as 116 an uncertainty and ranges from about 0.5% to 1.5% per vertex/interaction 117 depending on jet  $p_{\rm T}$  and  $\eta$ . 118

An uncertainty due to close-by jets is evaluated by comparing the ratio of reconstructed jet  $p_{\rm T}$  to the  $p_{\rm T}$  of an associated track jet, a jet clustered using tracks instead of calorimeter clusters, for isolated and non-isolated jets. A jet is considered isolated if the distance in  $(\eta, \phi)$  space to the nearest other jet is greater than 2.5 times the radius parameter used to cluster the

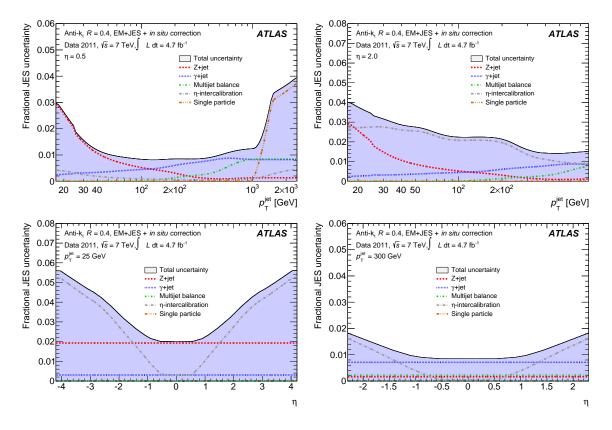


Figure 7.1: Relative uncertainty on in situ JES corrections as a function of  $p_{\rm T}$  (top) for jets with  $|\eta|$  around 0.5 (left) and 2.0 (right) and as a function of  $\eta$  (bottom) for jets with  $p_{\rm T}$  near 25 GeV (left) and 300 GeV (right). Figure taken from Ref. [83].

<sup>124</sup> jets. This comparison is made for both data and MC, and the fractional <sup>125</sup> difference is taken as the uncertainty due to close-by jets. This uncertainty <sup>126</sup> is about 3.5% for 30 GeV jets with another jet within a distance of 0.5 and <sup>127</sup> decreases with increasing distance to the nearest jet and increasing jet  $p_{\rm T}$ .

Differences in physical characteristics, like the average number of charged 128 particles and average jet width, between jets initiated by a quark or by a 129 gluon can be used to construct a tagging algorithm for separating quark jets 130 from gluon jets. The dependence of the jet energy scale on the operating 131 point of the tagger (corresponding to different purities of the tagged sam-132 ple) is compared between data and MC, and the difference is taken as an 133 uncertainty due to jet flavor and ranges from 1% to 3% depending on jet 134  $p_{\rm T}$  and whether the sample is dominated by gluon jets or quark jets. 135

<sup>136</sup> Uncertainties from the in situ calibrations are the dominant contribution <sup>137</sup> to the total uncertainty for jets with high  $p_{\rm T}$  or high  $\eta$ , which is expected for <sup>138</sup> events passing the signal region selections. Below 50 GeV, uncertainties from <sup>139</sup> close-by jets and pileup become important, and the uncertainty due to jet <sup>140</sup> flavor is largest for jets with  $|\eta| < 1$ . When propagated through the analysis, <sup>141</sup> the resulting uncertainty on the event yield is 10-15% for background and <sup>142</sup> 6% for signal.

Events with a jet recoiling against a high- $p_{\rm T}$  (> 30 GeV) Z boson are 143 also used to measure the efficiency of jets originating from the primary 144 vertex to pass the JVF selection [63]. Z+jet events are used to obtain a 145 sample of jets with little contamination from pileup. The difference between 146 the efficiency observed in data and MC is about 1% and is taken as an 147 uncertainty. Variations of the JVF selection around the nominal value that 148 change the efficiency in MC by this difference are used to propagate the 149 uncertainty to physics analyses. The effect of this uncertainty on the final 150 predictions is less than 1%. 151

The efficiency for b-tagging jets is measured as a function of  $p_{\rm T}$  using 152 di-leptonic  $t\bar{t}$  decays [84], which produces a sample of jets enriched in b jets. 153 The uncertainty on the b-tagging efficiency is due mainly to the kinematic 154 modeling of  $t\bar{t}$  and background processes in MC. The relative uncertainty 155 is less than 4% for jets with 30 GeV  $< p_{\rm T} < 200$  GeV and 8% for jets 156 with  $p_{\rm T}$  greater than 200 GeV. The rate for mistakenly tagging light-flavor 157 jets (mis-tag rate) is measured in an inclusive jet sample by comparing the 158 nominal rate of b tags to the rate when the signs of track impact parameters 159 and secondary vertex decay length are reversed [66]. For jets with  $p_{\rm T}$  below 160 140 GeV, the main source of uncertainty is the modeling of track multiplicity 161 in jets while uncertainties on the efficiency to tag b and c jets form the 162 dominant contribution for jets with  $p_{\rm T}$  greater than 140 GeV. The total 163

uncertainty on the mis-tag rate varies from 15-25% depending on jet  $p_{\rm T}$  and  $\eta$ . Uncertainty on the b-tagging efficiency/mis-tag rate translates into an uncertainty on the signal region predictions of about 1%.

#### <sup>167</sup> 7.2.2 Lepton Uncertainties

The electron energy scale and resolution and their uncertainties are evalu-168 ated using  $Z \to ee$  events [56]. Muon momentum scale and resolution cor-169 rections and their uncertainties are evaluated using  $J/\psi \rightarrow \mu\mu$  and  $Z \rightarrow \mu\mu$ 170 events [58]. In both analyses templates of the invariant mass distribution of 171 the lepton pair are constructed using MC with free parameters for scale and 172 resolution corrections in bins of  $p_{\rm T}$  and  $\eta$ . These parameters are then de-173 termined using a maximum likelihood fit to the invariant mass distribution 174 observed in data. Uncertainties on the energy/momentum scale for leptons 175 are less than 1%. 176

Identification efficiency scale factor and their uncertainties are also deter-177 mined using Z boson decays to charged leptons [55, 58]. This measurement 178 uses a tag-and-probe method in which one lepton (the tag) is required to 179 pass all identification criteria and to form a Z candidate with a second ob-180 ject (the probe) that has not yet been required to pass identification. The 181 efficiency of the ID selections is then determined using the sample of probe 182 leptons in bins of  $p_{\rm T}$  and  $\eta$ . Uncertainties on the efficiency are estimated 183 by varying the event selections used to select Z decays. The impact of lep-184 ton energy and identification uncertainties on the predicted yields is 1-2%185 depending on channel. The tag-and-probe studies are also used to measure 186 single-lepton trigger efficiencies. Again, the tag leptons are required to have 187 fired the trigger, and the efficiency of the trigger requirements is evaluated 188 on the probe leptons. The uncertainty from trigger efficiency is less than 189 1%. 190

# <sup>191</sup> 7.2.3 $E_{\rm T}^{\rm miss}$ Uncertainties

Since missing transverse energy is evaluated using the measured transverse 192 energies of other objects in the event, the uncertainties on those measured 193 energies also affect the calculated  $E_{\rm T}^{\rm miss}$ . This effect is included when prop-194 agating these uncertainties to the predicted event yield. The remaining 195 uncertainty on  $E_{\rm T}^{\rm miss}$  comes from the energy scale and resolution of energy 196 deposits in the calorimeter that are not part of another object (soft terms). 197 Two methods are used to estimate the uncertainties due to soft terms, both 198 of which use  $Z \to \mu \mu$  events [68]. One compares the average  $E_{\rm T}^{\rm miss}$  measured 199

in data and MC for events without any jets, where the only contributions to  $E_{\rm T}^{\rm miss}$  come from the muons and soft terms. The second estimates the true soft term contribution using truth information and compares this to the reconstructed soft term. The uncertainty from the soft term on the predicted event yield is about 2%.

### 205 7.2.4 Additional Uncertainties

In addition to the uncertainties listed above, there are a few other experi-206 mental uncertainties that affect MC-based predictions. In order to have a 207 chance of correctly describing data, MC estimates must be normalized to 208 match the integrated luminosity of the recorded data sample. Luminosity is 209 measured using dedicated detector systems located at large pseudorapidities, 210 and these measurements are calibrated with beam-separation scans similar 211 to those described in Ref. [85]. Sources of uncertainties in the luminosity 212 calibration include the measured product of the two bunch charges, jitter 213 in the beam position, precision of lengths measured in the inner detector, 214 emittance growth during the scans, and dependence on the number of inter-215 actions per bunch crossing. The estimated uncertainty of the luminosity of 216 the data used for this measurement is 2.8%. 217

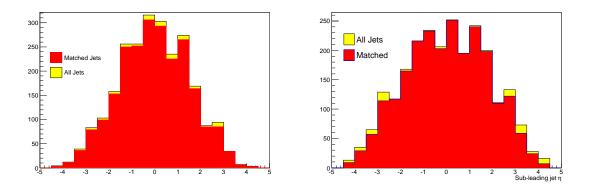


Figure 7.2: Jet  $\eta$  distributions for the leading (left) and sub-leading (right) jets in WZ MC. The yellow histogram contains all events while the red histogram contains only events in which both jets are matched to the primary interaction using truth information. The difference between the two is taken as a systematic uncertainty.

Event yields can also be affected by the presence of "pileup jets," jets that originate from additional proton-proton collision occurring within the

same bunch crossing. For example, an event with only 1 jet may still pass 220 analysis selections if a pileup jet is mistaken for another jet from the primary 221 collision. To account for uncertainty from potential mismodeling of pileup 222 interactions, MC truth record information is used to reject pileup jets, and 223 the difference between the resulting event yield and the nominal one, shown 224 in Figure 7.2 for WZ, is taken as an uncertainty. The effect is measured to 225 be 8% in  $W^{\pm}Z$  MC, and this is used as a common uncertainty for diboson 226 processes that have fewer than 2 jets at leading order. For  $W^{\pm}W^{\pm}jj$  and 227  $t\bar{t}V$  production the effect is of order 1%. 228

The  $W^{\pm}\gamma$  yield has an additional uncertainty due to the modeling of 229 photon conversions in the detector. The extent of this uncertainty is eval-230 uated using scale factors between charge-misID rates measured in data and 231 MC. The discrepancy in charge-misID rates is a good proxy for the pho-232 ton conversion rate since charge-misID occurs primarily due to the trident 233 process depicted in Figure 6.4. Jet-based selections are relaxed to increase 234 statistics, and two variations are performed using the charge-misID scale 235 factors. First, scale factors are only applied if they are greater than 1 to ob-236 tain the maximum possible upward variation. This process is then repeated 237 for scale factors less than 1. These variations are shown in Figure 7.3. This 238 procedure avoids random cancelations between large and small scale fac-239 tors to give a conservative estimate of the size of the effect. The resulting 240 uncertainty is +22%/-13% on the  $W^{\pm}\gamma$  yield. 241

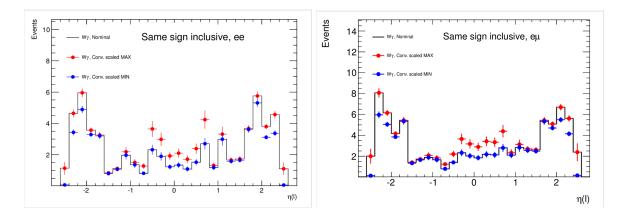


Figure 7.3: Electron  $\eta$  distribution for the *ee* (left) and *eµ* (right) channels. The red(blue) points show the effect of scaling events by charge-misID scale factors when those scale factors are greater(less) than one.

Uncertainties on charge-misID background (%)				
Source	Signal regions	Control regions		
misID rate statistics	4.3	4.5		
closure test	2.1	2.6		
background subtraction	0.2	2		
double-counting	+0, -2.5	+0, -0.2		
energy corrections	+5.5, -3.1	+9.3, -6.2		
Drell-Yan CR tests	6	6		
Total	+9.4, -8.6	+12.4, -10.3		
$t\bar{t}$ CR tests, $ee$ channel	12	18(b-tag CR)/1(Others)		
$t\bar{t}$ CR tests, $e\mu$ channel	31	20(b-tag CR)/11(Others)		

Table 7.2: Summary of uncertainties on the charge-misID background. The final two rows indicate channel-specific uncertainties that are applied in addition to the uncertainty given in the "Total" row. This final uncertainty varies considerably depending on the fraction of the charge-misID background in a given region/channel that is expected to come from  $t\bar{t}$  events.

# 7.3 Systematic Uncertainties on Data-Driven Back ground Estimates

### 244 7.3.1 Charge-misID Background

Uncertainties on the charge-misID background come from three areas: un-245 certainty on the charge-misID rate, uncertainty on the energy correction, 246 and uncertainty from potential double-counting of charge-misID in processes 247 that can produce both opposite-sign lepton pairs and same-sign lepton pairs 248 without charge-misID. Uncertainties on the charge-misID rate come from 249 limited statistics, a closure test of the method, background subtraction, and 250 further tests of the method performed in Drell-Yan and  $t\bar{t}$  MC. These un-251 certainties are summarized in Table 7.2. 252

The charge-misID rate is measured in a region that is dominated by  $Z \rightarrow ee$  events and background from other processes is subtracted. Uncertainty from the background subtraction is estimated by measuring the charge-misID rate without background subtraction and evaluating the difference in the predicted yield between the two rates. For the closure test, the charge-misID rate is measured in  $Z \rightarrow ee$  MC using the same method as for data, and the same sample of events is used to test the measured

Region Name	Charge-MisID (OS-scaled)	MC Same-sign Events	Ratio (difference/uncertainty)
SS Z	$14780 \pm 34$	$15650 \pm 260$	$0.94 \pm 0.02$
Low $N_{jet}$ CF	$2026 \pm 15$	$2038\pm95$	$0.99\pm0.05$
VBF-like SS $Z$	$447.4 \pm 7.5$	$452 \pm 43$	$0.99\pm 0.09$
SS Incl.	$1412 \pm 10$	$1503\pm76$	$0.94\pm0.05$
b-tag	$1.7 \pm 0.3$	$4.8\pm3.9$	$0.35 (0.8\sigma)$
Inclusive SR	$1.77\pm0.32$	$8.1 \pm 8.1$	$0.2 \ (0.8\sigma)$
VBS SR	$1.06 \pm 0.23$	$8.1 \pm 8.1$	$0.13 (0.8\sigma)$

Table 7.3: Test comparing the prediction from scaling opposite-sign events by the charge-misID rate to the direct same-sign prediction in Drell-Yan MC. The SS Z region inverts the Z veto used in the signal selection while making no cuts on jets, and the VBF-like SS Z region additionally requires two jets with  $m_{jj} > 150$  GeV. The low N<sub>jet</sub> CF region does not apply a Z veto but is otherwise similar to the  $\leq 1$  jet control region, and the SS Incl. region requires only two same-sign leptons with no further selections.

rate. Events passing the selections for the charge-misID rate measurement are separated into opposite-sign and same-sign events, and the charge-misID rate is applied to the opposite-sign events to get a prediction for the number of same-sign events. The discrepancy between the prediction and the actual number of same-sign events is taken as an uncertainty.

The applicability of this charge-misID rate to other regions and processes 265 is examined by performing the same comparison of opposite-sign events 266 scaled by the charge-misID rate to same-sign events in MC for several control 267 regions and the two signal regions. This is shown for Drell-Yan MC in 268 Table 7.3 and for tt MC in Table 7.4. The largest statistically significant 269 difference seen using Drell-Yan MC is 6% and is taken as an uncertainty. 270 However, this sample lacks sufficient statistics to make this comparison in the 271 b-tag control region and in the signal regions, so  $t\bar{t}$  MC is used to probe these 272 regions. In the  $t\bar{t}$  MC, the number of same-sign events is underestimated by 273 20% in the b-tag control region and 40% in the signal regions. To account for 274 this discrepancy. MC is used to estimate relative size of the contributions of 275 various processes to the charge-misID background, and the  $t\bar{t}$  component is 276 scaled up by 20% in the b-tag control region and 40% in the signal regions. 277 The size of this scaling is then taken as an additional uncertainty on the 278 prediction. In the signal regions,  $t\bar{t}$  events are expected to account for about 279 30% of the charge-misID background in the *ee* channel and 80% in the  $e\mu$ 280

Region Name	Charge-MisID (OS-scaled)	MC Same-sign Events	Ratio (difference/uncertainty)		
	ee channel				
b-tag	$20.9 \pm 0.2$	$26.6 \pm 1.9$	$0.79 \pm 0.06 \; (3.5\sigma)$		
Inclusive SR	$0.57\pm0.05$	$0.91\pm0.39$	$0.63 \pm 0.27 \; (1.3\sigma)$		
VBS SR	$0.52 \pm 0.04$	$0.91\pm0.39$	$0.57 \pm 0.25 \; (1.7\sigma)$		
$e\mu$ channel					
b-tag	$28.5\pm0.3$	$33.1 \pm 2.1$	$0.86 \pm 0.06 \ (2.3\sigma)$		
Inclusive SR	$0.65 \pm 0.05$	$1.15\pm0.43$	$0.57 \pm 0.27 \; (1.6\sigma)$		
VBS SR	$0.60 \pm 0.05$	$0.95\pm0.41$	$0.63 \pm 0.25 \; (1.5\sigma)$		

Table 7.4: Test comparing the prediction from scaling opposite-sign events by the charge-misID rate to the direct same-sign prediction in  $t\bar{t}$  MC.

281 channel.

The energy correction must be increased by 35% to make the same-sign di-electron mass distribution agree with data in the neighborhood of the Z mass. This change is taken as an uncertainty on the energy correction. In addition, energy corrections derived separately in Drell-Yan MC and  $t\bar{t}$ MC differ by 15%. The uncertainty on the predicted background due to the energy correction is therefore estimated by repeating the analysis while varying the energy correction by  $\pm 50\%$ .

Processes that produce either same-sign or opposite-sign di-lepton events, 289 mainly  $W^{\pm}Z$  events where one of the leptons is not reconstructed or fails 290 identification, can also have events migrate from opposite-sign to same-sign 291 due to charge-misID. This contribution would, of course, be included in 292 the data-driven estimate of the charge-misID background. However, the 293 MC used to estimate these backgrounds also contains this effect, creating a 294 double-counting. This double-counting is removed by subtracting the MC 295 prediction for the number of opposite-sign events from the data sample be-296 fore applying the charge-misID rate. The size of the subtraction is then 297 taken as an uncertainty to account for any mismodeling of the charge-misID 298 rate in MC. 299

#### 300 7.3.2 Non-prompt Background

As described in Chapter 6, the non-prompt background is estimated by applying a "fake factor" measured in a "di-jet" control region to events in the "tight+loose" (TL) control region, which is defined to have the same

	Inclusive SR $ee/e\mu/\mu\mu$	VBS SR $ee/e\mu/\mu\mu$
Total non-prompt background	0.61/1.9/0.41	0.50/1.5/0.34
2 non-prompt leptons	0.01/0.02/0.004	0.01/0.02/0.004
2 prompt leptons	0.13/0.13/0.004	0.09/0.10/0.004

Table 7.5: Contribution in weighted number of events from events where both leptons originate from hadronic activity and from events with two prompt leptons compared to the final non-prompt background prediction (including subtraction of these effects).

selections as the signal region except that one lepton is required to be non-304 isolated and pass only loose identification criteria. The TL control region 305 also receives contributions from prompt processes that must be subtracted 306 out, and the modeling of these processes when one lepton is non-isolated 307 presents one source of uncertainty on the non-prompt background predic-308 tion. This uncertainty is conservatively taken to be 50% of the total prompt 309 subtraction, which is shown in Table 7.5. However, due to the small size of 310 the prompt contribution, it has a negligible effect on the total uncertainty. 311 It is also possible for both leptons in the event to originate from hadronic 312 activity, an effect which is actually double-counted by the fake factor method. 313 This double-counting is subtracted using events in a "loose+loose" (LL) re-314 gion scaled the product of the fake factors for each lepton. The size of 315 this subtraction, shown in Table 7.5, is very small and is assigned a 100%316 uncertainty. 317

The remaining uncertainties come from the calculation of the fake fac-318 tor. The di-jet control region used to measure the fake factor also suffers 319 contamination from prompt processes, mainly Z+jets and W+jets. The 320 modeling of these processes is checked in events with  $\Delta \phi(\ell, j) < 2.0$  that 321 pass all other di-jet selections except for the transverse mass cut. The lep-322 ton is also required to pass tight selections. Table 7.6 shows the number 323 of events observed in data as well as the MC prediction for prompt lep-324 tons. Observation and prediction agree within 4% for electrons and 12%325 for muons. The uncertainty from prompt subtraction is then determined by 326 repeating the fake factor derivation while varying the prediction for prompt 327 process up and down by the level of agreement seen for low- $\Delta \phi(\ell, j)$  events. 328 The resulting variations in the fake factor are shown in Figure 7.4. The new 329 fake factors are then used to determine the effect on the predicted yield. 330 The resulting uncertainty is around 20%. 331

Channel	Data	MC Prediction	(Data-MC)/MC
electron	329	$340.5 \pm 1.4$	-0.034
muon	137622	$155770 \pm 670$	-0.117

Table 7.6: Comparison of observed event yields and the MC prediction for processes that produce prompt leptons with no  $m_T$  cut applied  $\Delta \phi(\ell, j)$  required to be less than 2. The relative difference between the predicted and observed event yields is used to estimate the systematic uncertainty on the non-prompt background prediction due to the modeling of prompt contamination in the di-jet sample.

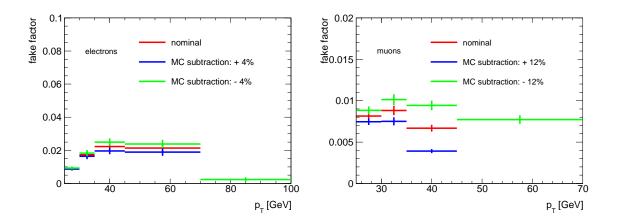


Figure 7.4: Uncertainty on the fake factor for electrons (left) and muons (right) due to the modeling of prompt contamination in the di-jet region.

Uncertainties on non-prompt background (%)					
Source	ee	$e\mu$	$\mu\mu$		
di-jet statistics	10	10	5		
$\Delta \phi(\ell, j)$ cut variation	10	10	5		
$m_{\rm T}(\ell, E_{\rm T}^{\rm miss})$ cut variation	15	10	1		
jet $p_{\rm T}$ cut variation	10	10	20		
jet $p_{\rm T}$ reweighting		25	40		
prompt subtraction		20	20		
Total	35	40	50		

Table 7.7: Summary of systematic uncertainties on the non-prompt background prediction due to uncertainties on the fake factor

The fake factor depends on event kinematics in two ways, through the se-332 lections used to define the di-jet control region and through the jet  $p_{\rm T}$  reweight-333 ing used to extrapolate to the signal region. Each of these creates an ad-334 ditional source of uncertainty. The uncertainty due to event selections is 335 evaluated by independently varying the three selections and repeating the 336 measurement. The  $m_{\rm T}$  and jet  $p_{\rm T}$  selections are each varied by 5 GeV, 337 and the  $\Delta \phi(\ell, j)$  cut is varied by 0.1. Together, the variations, shown in 338 Figure 7.5, give an uncertainty of about 20%. 339

The uncertainty due to the jet  $p_{\rm T}$  reweighting is determined by varying 340 the fitted slope of the line relating lepton  $p_{\rm T} + E_{\rm T}^{\rm iso}$  to the underlying jet 341  $p_{\rm T}$  up and down by 15%. The size of the variation to apply is determined 342 using truth information in two MC samples,  $t\bar{t}$  and W+jets. Events are se-343 lected by requiring one prompt lepton and one lepton from a hadron decay. 344 Taking the nearest jet in the truth record to be the underlying jet is insuf-345 ficient since muons and neutrinos are not included in the clustering, so the 346 true underlying jet momentum is defined as the vector sum of the momenta 347 of all jets, neutrinos, and muons within a radius of 0.3 in  $(\eta, \phi)$  space around 348 the non-prompt lepton. The  $p_{\rm T}$  distribution for the true underlying jets is 349 then compared to the distribution derived using the normal procedure. As 350 shown in Figure 7.6, a 15% variation of the slope is sufficient to make the 351 derived  $p_{\rm T}$  distributions bracket the true distribution. The resulting varia-352 tion in the fake factors is shown in Figure 7.7. After propagating the result 353 to the signal region predictions, this uncertainty is found to be 20% for the 354 ee and  $e\mu$  channels and 40% for the  $\mu\mu$  channel. Uncertainties from the fake 355 factor measurement are summarized in Table 7.7. 356

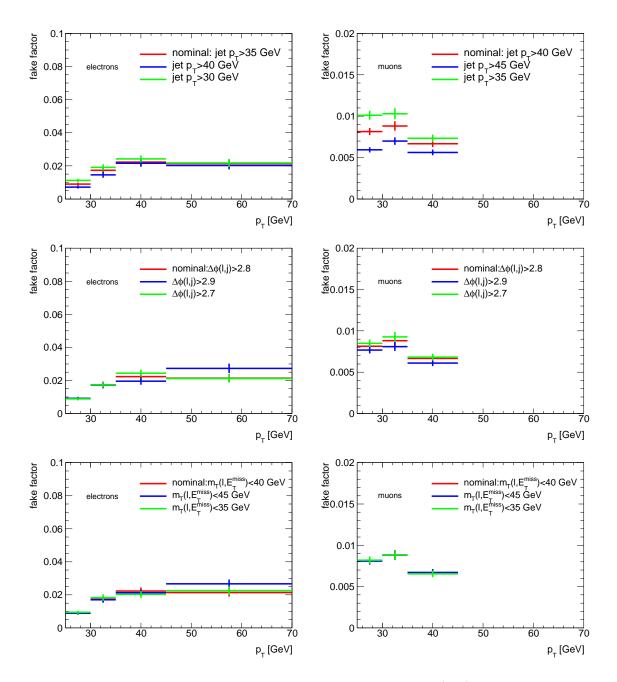


Figure 7.5: Uncertainty on the fake factor for electrons (left) and muons (right) from variations of the selections used to define the di-jet region.

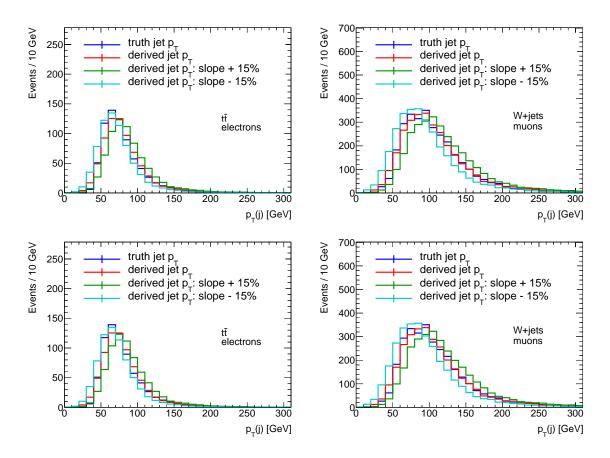


Figure 7.6: Comparison of derived underlying jet  $p_{\rm T}$  distributions to the true distribution for different variations of the slope of the line relating lepton  $p_{\rm T} + E_{\rm T}^{\rm iso}$  to jet  $p_{\rm T}$  for electrons (left) and muons (right) in  $t\bar{t}$  (top) and W+jets MC samples.

Region	Di-jet fake factor	High- $d_0$ fake factor
$\leq 1$ jet CR	$8.4 \pm 0.3$ (stat.) $\pm 4.5$ (syst.)	$12.2 \pm 0.4$ (stat.) $\pm 4.0$ (syst.)
b-tag CR	$10.3 \pm 0.3$ (stat.) $\pm 5.3$ (syst.)	$16.9 \pm 0.5 (\text{stat.}) \pm 5.5 (\text{syst.})$
Low $m_{jj}$ CR	$8.1 \pm 0.3$ (stat.) $\pm 4.2$ (syst.)	$11.8 \pm 0.4$ (stat.) $\pm 3.8$ (syst.)
Inclusive SR	$0.41 \pm 0.06$ (stat.) $\pm 0.21$ (syst.)	$0.67 \pm 0.10$ (stat.) $\pm 0.23$ (syst.)
VBS SR	$0.34 \pm 0.06$ (stat.) $\pm 0.18$ (syst.)	$0.49 \pm 0.09$ (stat.) $\pm 0.17$ (syst.)

Table 7.8: Comparison of non-prompt background predictions for the  $\mu\mu$  channel using fake factors derived in the di-jet region and a "high- $d_0$ " region in which both muons must have  $d_0/\sigma(d_0) > 3$ .

Additional cross-checks are performed to ensure that the estimated un-357 certainties are adequate. Another potential source of uncertainty on this 358 background is the difference in flavor composition between jets in the TL 359 region and jets in the di-jet region. This could cause the actual fake factor 360 in the TL region to be different from the measured one, but this difference 361 would be caused by differences in kinematic distributions between heavy-362 flavor jets and light-flavor jets and should be accounted for by the uncer-363 tainty on the jet  $p_{\rm T}$  reweighting. This is checked by separating the di-jet 364 sample into a subsample containing b-tagged jets and a subsample contain-365 ing light jets and comparing the fake factors measured in each subsample. 366 The difference between the two is found to be within the uncertainty from 367 the jet  $p_{\rm T}$  reweighting, so no additional uncertainty is added. 368

A second method of measuring the muon fake factor is also used as a 369 cross-check. The fake factor is measured using events with two same-sign 370 muons and two jets where both muons are required to have transverse impact 371 parameter significance greater than 3. An extrapolation factor measured in 372 MC is then used adjust the fake factor for the lepton selections used in the 373 TL region  $(d_0/\sigma(d_0) < 3/10$  for tight/loose muons). This method has a 374 larger statistical uncertainty on the fake factor, with additional uncertain-375 ties coming from the extrapolation factor and the subtraction of prompt 376 contamination. Table 7.8 compares the non-prompt background predicted 377 using each method. The two methods agree within uncertainties, so no 378 additional uncertainty is taken from the difference. 379

Systematic Un	certainties $ee/e$	$e\mu/\mu\mu$ (%) - Inclusive SR	
Background		Signal	
Jet uncertainties	11/13/13	Jet uncertainties	5.7
Theory $WZ/\gamma^*$	5.6/7.7/11	Theory $W^{\pm}W^{\pm}jj$ -ewk	4.7
MC statistics	8.2/5.9/8.4	Theory $W^{\pm}W^{\pm}jj$ -strong	3.1
Fake rate	3.5/7.1/7.2	Luminosity	2.8
OS lepton bkg/ Conversion rate	5.9/4.2/-	MC statistics	3.5/2.1/2.8
Theory $W + \gamma$	2.8/2.6/-	$E_T^{miss}$ reconstruction	1.1
$E_T^{miss}$ reconstruction	2.2/2.4/1.8	Lepton reconstruction	1.9/1.0/0.7
Luminosity	1.7/2.1/2.4	b-tagging efficiency	0.6
Lepton reconstruction	1.6/1.2/1.2	trigger efficiency	0.1/0.3/0.5
b-tagging efficiency	1.0/1.1/1.0		
Trigger efficiency	0.1/0.2/0.4		

Table 7.9: Summary of systematic uncertainties in the inclusive signal region. The left column indicates uncertainties as a percentage of the total background prediction while the right column indicates uncertainties as a percentage of the total signal prediction.

### 380 7.4 Summary

Tables 7.9 and 7.10 provide a summary of the systematic uncertainties dis-381 cussed in this chapter. The first column shows the size of various groups 382 of related uncertainties as a percentage of the total background prediction 383 while the second column does the same for signal. The largest systematic 384 uncertainty comes from jet uncertainties, which is dominated by the un-385 certainty on the jet energy scale, followed by the theoretical uncertainty 386 on the  $W^{\pm}Zjj$  cross section and MC statistics. The uncertainty on the 387 non-prompt background also makes a significant contribution in  $\mu\mu$  and  $e\mu$ 388 channels, which have better signal-to-background ratios than the ee channel. 389

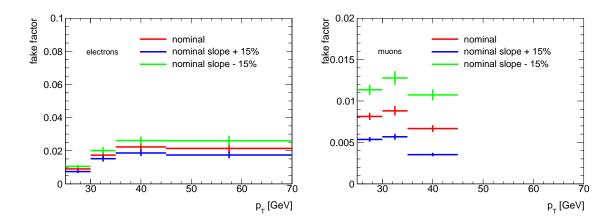


Figure 7.7: Uncertainty on the fake factor for electrons (left) and muons (right) due to the reweighting of the underlying jet  $p_{\rm T}$  distribution.

Systematic Uncertainties $ee/e\mu/\mu\mu$ (%) - VBS SR					
Background		Signal			
Jet uncertainties	13/15/15	Theory $W^{\pm}W^{\pm}jj$ -ewk	6.0		
Theory $WZ/\gamma^*$	4.5/5.4/7.8	Jet uncertainties	5.1		
MC statistics	8.9/6.4/8.4	Luminosity	2.8		
Fake rate	4.0/7.2/6.8	MC statistics	4.5/2.7/3.7		
OS lepton bkg/ Conversion rate	5.5/4.4/-	$E_T^{miss}$ reconstruction	1.1		
$E_T^{miss}$ reconstruction	2.9/3.2/1.4	Lepton reconstruction	1.9/1.0/0.7		
Theory $W + \gamma$	3.1/2.6/-	b-tagging efficiency	0.6		
Luminosity	1.7/2.1/2.4	trigger efficiency	0.1/0.3/0.5		
Theory $W^{\pm}W^{\pm}jj$ -strong	0.9/1.5/2.6				
Lepton reconstruction	1.7/1.1/1.1				
b-tagging efficiency	0.8/0.9/0.7				
Trigger efficiency	0.1/0.2/0.4				

Table 7.10: Summary of systematic uncertainties in the VBS signal region. The left column indicates uncertainties as a percentage of the total background prediction while the right column indicates uncertainties as a percentage of the total signal prediction.

### Chapter 8

# Jet Energy Scale Performance Studies Using Z+jet Events

Since uncertainties on jet energy scale and resolution are the dominant sys-1 tematic uncertainties on the  $W^{\pm}W^{\pm}jj$  measurement, it is important to 2 understand how well these uncertainties are estimated. To check the esti-3 mation of these uncertainties, a method is needed to test how well jet energy is reconstructed. One method for testing this uses Z+jet events where the Z5 decays to a pair of muons. The transverse momentum of the Z can be used 6 to define a reference  $p_{\rm T}$  ( $p_{\rm T}^{\rm ref}$ ) to compare with the measured jet  $p_{\rm T}$  that, 7 since the Z is required to decay to muons, is measured using the muon 8 spectrometer instead of the calorimeters. The ratio  $p_{\rm T}^{\rm jet}/p_{\rm T}^{\rm ref}$  then provides a 9 measure of how accurately jet energy is reconstructed. In an event consist-10 ing of only these two objects, the transverse momenta of the Z and the jet 11 must have equal magnitude, so  $p_{\rm T}^{\rm ref}$  is just the  $p_{\rm T}$  of the Z. Real events are 12 affected by additional soft QCD radiation such as an extra low-energy jet or 13 pieces of the jet that emitted at a wide angle and don't get clustered with 14 the rest of the jet, as depicted in Figure 8.1. To minimize these effects on 15 the measurement,  $p_{T}^{\text{ref}}$  is defined to be the projection of  $p_{T}$  of the Z onto the 16 jet axis. Results are presented for both the EM+JES and LCW+JES cali-17 brations, and the performance is compared between data and four  $Z \to \mu\mu$ 18 MC samples: POWHEG showered with PYTHIA8, ALPGEN showered either 19 with HERWIG++ or PYTHIA8, and SHERPA. The EM+JES calibration has 20 a larger effect on the  $W^{\pm}W^{\pm}ii$  measurement since this is the calibration 21 used for jets in this analysis, but the LCW+JES calibration is also used for 22

calculating  $E_{\rm T}^{\rm miss}$ , so it is important to understand its performance as well.

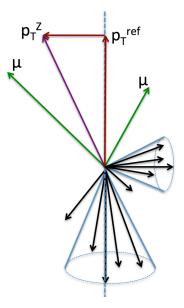


Figure 8.1: The  $p_{\rm T}$  balance between the leading jet and the Z boson is spoiled by additional QCD radiation, so the projection of the Z  $p_{\rm T}$  onto the jet axis is used.

### 24 8.1 Event Selection

Events are collected using the same two single muon triggers used to select 25  $W^{\pm}W^{\pm}jj$  events, as well as a di-muon trigger that requires one muon with 26  $p_{\rm T} > 18$  GeV and another with  $p_{\rm T} > 8$  GeV. The inclusion of the di-muon 27 trigger allows lower  $p_{\rm T}$  thresholds to be used for muons, thereby increasing 28 statistics for this measurement. All of the event quality criteria used in the 29 main analysis are also applied here. Muons are required to pass the tight 30 muon selection, except that the  $p_{\rm T}$  threshold is lowered to 15 GeV. The 31 minimum  $p_{\rm T}$  for jets is also lowered to 15 GeV with jet selection otherwise 32 identical to that used in the  $W^{\pm}W^{\pm}ii$  analysis. 33

Events are selected to have two muons with opposite electric charge, at least one of which must have  $p_{\rm T}$  greater than 20 GeV. The invariant mass of the muon pair is required to be between 66 GeV and 116 GeV. The separation between muons and jets,  $\Delta R = \sqrt{(\eta^{\mu} - \eta^{\rm jet})^2 + (\phi^{\mu} - \phi^{\rm jet})^2}$ , is required to be greater than 0.35. The leading jet in the event is required to <sup>39</sup> have  $p_{\rm T} > 20$  GeV, and events containing a second jet with JVF > 0.75 and  $p_{\rm T}$  greater than 20% of the  $p_{\rm T}$  of the Z candidate formed by the muon pair <sup>41</sup> are rejected. In order to further reduce the effects of additional jet activity, <sup>42</sup> the angular separation of the leading jet and the Z in the transverse plane is <sup>43</sup> required to be within 0.2 radians of  $\pi$ . The ratio  $p_{\rm T}^{\rm jet}/p_{\rm T}^{\rm ref}$  is then measured <sup>44</sup> in several bins of  $p_{\rm T}^{\rm ref}$  and jet  $|\eta|$ .

### <sup>45</sup> 8.2 Measuring Average $p_{\rm T}$ Balance

Distributions of the  $p_{\rm T}$  balance ratio in three bins of  $p_{\rm T}^{\rm ref}$  for jets with  $|\eta| <$ 46 1.2 are shown in Figure 8.2. As can be seen in the left-hand plot, bins with 47 low  $p_{\rm T}^{\rm ref}$  have a steep turn-on that is caused by the minimum jet  $p_{\rm T}$  cut. 48 Since the lead jet must have  $p_{\rm T}$  greater than 20 GeV, it is impossible to 49 measure a  $p_{\rm T}$  balance ratio less than  $20/p_{\rm T}^{\rm ref}$  as those events will simply fail 50 to be selected. This doesn't pose a problem as long as  $p_{\rm T}^{\rm ref}$  is sufficiently 51 high, but for bins with  $p_{\rm T}^{\rm ref}$  below 50 GeV, it causes the average  $p_{\rm T}$  balance 52 to be biased above the true mean. 53

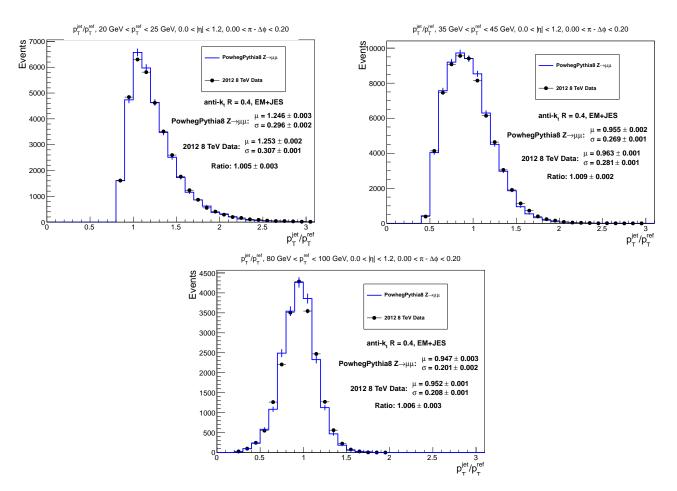


Figure 8.2:  $p_{\rm T}$  balance distributions for jets calibrated with EM+JES with  $|\eta| < 1.2$  and 20 GeV  $< p_{\rm T}^{\rm ref} < 25$  GeV (left), 35 GeV  $< p_{\rm T}^{\rm ref} < 45$  GeV (right), and 80 GeV  $< p_{\rm T}^{\rm ref} < 100$  GeV (middle). The mean ( $\mu$ ) and RMS ( $\sigma$ ) of each distribution is indicated in the text labels along with the ratio of the means.

Two methods have been tried to better measure the average  $p_{\rm T}$  balance in 54  $low-p_T^{ref}$  bins. The first is to fit the distribution with a Poisson distribution 55 convoluted with a linear turn-on function. The turn-on function is taken 56 to be zero below  $20/p_{\rm T}^{\rm ref,max}$  and one above  $20/p_{\rm T}^{\rm ref,min}$ . The mean of the 57 Poisson is then taken as the true mean of the distribution. This method has 58 been found to work well in a previous  $Z+\text{jet } p_{T}$  balance study using the Z 59 decay to electrons in 7 TeV data with a leading jet  $p_{\rm T}$  cut of 12 GeV [86]. 60 However, the motivation for choosing this fit function was purely empirical, 61 and it does not fit the 8 TeV data well when using the same jet  $p_{\rm T}$  cut. This 62 is shown in Figure 8.3. Raising the  $p_{\rm T}$  cut to 20 GeV improves the quality 63 of the fits but results in a loss of sensitivity to the position of the mean in 64 lowest  $p_{\rm T}^{\rm ref}$  bins, where the  $p_{\rm T}$  balance distribution is truncated at values 65 near 1. Fits for three  $p_{\rm T}^{\rm ref}$  bins are shown in Figure 8.4. 66

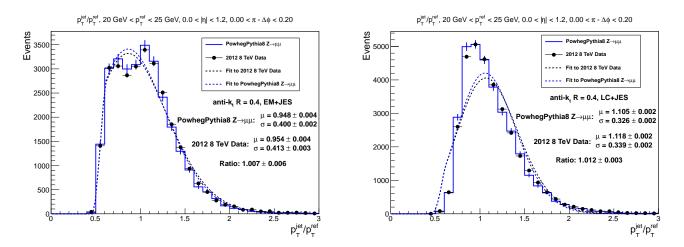


Figure 8.3:  $p_{\rm T}$  balance distributions for  $p_{\rm T}^{\rm ref}$  between 20 GeV and 25 GeV and  $|\eta| < 1.2$  for jets calibrated with EM+JES (left) and LCW+JES (right) when requiring the leading jet to have  $p_{\rm T} > 12$  GeV. Neither shape fits a Poisson with a linear turn-on between  $12/p_{\rm T}^{\rm ref,max} = 0.48$  and  $12/p_{\rm T}^{\rm ref,min} = 0.6$ . The mean ( $\mu$ ) and width ( $\sigma$ ) of Poisson fitted to each distribution is indicated in the text labels along with the ratio of the means.

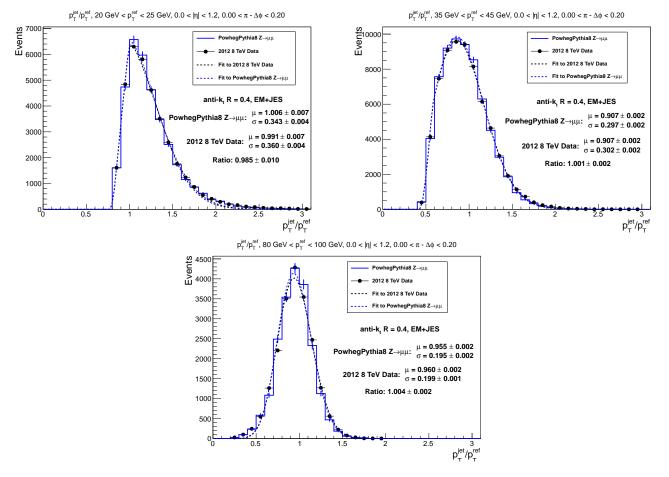


Figure 8.4:  $p_{\rm T}$  balance distributions for jets calibrated with EM+JES with  $|\eta| < 1.2$  and 20 GeV  $< p_{\rm T}^{\rm ref} < 25$  GeV (left), 35 GeV  $< p_{\rm T}^{\rm ref} < 45$  GeV (right), and 80 GeV  $< p_{\rm T}^{\rm ref} < 100$  GeV (middle). Each distribution is fit with a Poisson function convoluted with a linear turn-on. The mean ( $\mu$ ) and width ( $\sigma$ ) of Poisson fitted to each distribution is indicated in the text labels along with the ratio of the means.

Good agreement is seen in the shape of the  $p_{\rm T}$  balance distribution be-67 tween data and MC, and this suggests a more reliable way to fit the data. 68 Instead of choosing an arbitrary function, the data is fit using a template 69 made from the MC. In the fit the template is allowed to shift, and its width 70 is allowed to change. The fitted shift measures the difference in the average 71  $p_{\rm T}$  balance between data and MC. To mitigate the effects of bin-to-bin fluc-72 tuations, the template is smoothed by taking a weighted average of adjacent 73 bins. As shown in Figure 8.5, this method can produce better fits in bins 74 where the Poisson fit struggles, but the value that is obtained in the fit is 75 only the difference between the means. The individual means for data and 76 MC are still biased using this method. This bias is reduced by taking the 77 mean using only the neighborhood where the function is above half its max-78 imum value. Figure 8.6 shows template fits for three  $p_{\rm T}^{\rm ref}$  bins. The template 79 fit shows a bias between those of the Poisson fit and arithmetic mean for 80 the lowest  $p_{\rm T}^{\rm ref}$  bin, and results are otherwise similar to those obtained using 81 the Poisson fit. 82

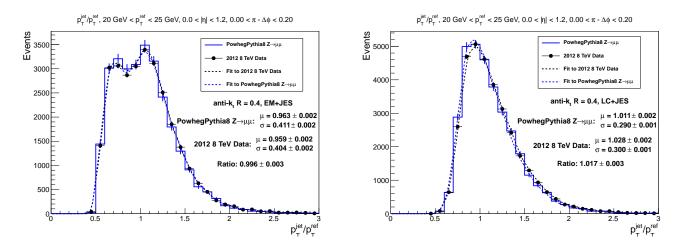


Figure 8.5:  $p_{\rm T}$  balance distributions for  $p_{\rm T}^{\rm ref}$  between 20 GeV and 25 GeV and  $|\eta| < 1.2$  for jets calibrated with EM+JES (left) and LCW+JES (right) when requiring the leading jet to have  $p_{\rm T} > 12$  GeV. The template fit used shows good agreement with the distributions but doesn't fix the bias. The half-width at half of the maximum ( $\sigma$ ) and mean of the template between the half-maxima ( $\mu$ ) are indicated in the text labels for the fit to each distribution along with the ratio of the means.

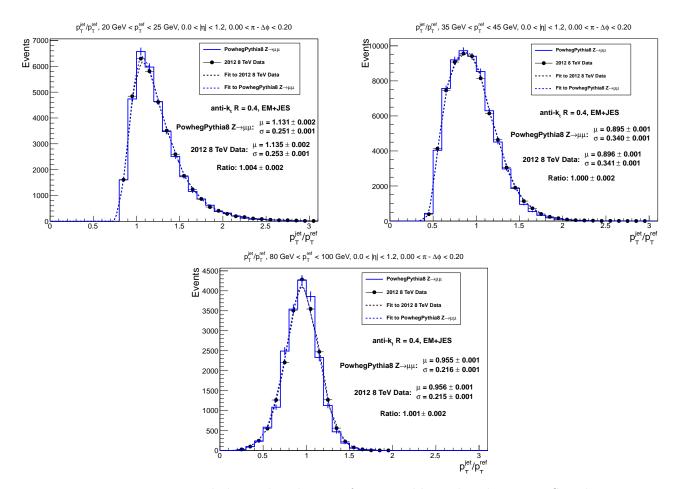


Figure 8.6:  $p_{\rm T}$  balance distributions for jets calibrated with EM+JES with  $|\eta| < 1.2$  and 20 GeV  $< p_{\rm T}^{\rm ref} < 25$  GeV (left), 35 GeV  $< p_{\rm T}^{\rm ref} < 45$  GeV (right), and 80 GeV  $< p_{\rm T}^{\rm ref} < 100$  GeV (middle). Each distribution is fit with a template constructed from the MC. The half-width at half of the maximum ( $\sigma$ ) and mean of the template between the half-maxima ( $\mu$ ) are indicated in the text labels for the fit to each distribution along with the ratio of the means.

### 83 8.3 FCAL High Voltage Problem

One interesting application of this Z+jet  $p_{\rm T}$  balance study was to quantify 84 the effect of a problem with the high voltage (HV) supplies of the forward 85 calorimeters that affected a portion of the 2012 run. In June, 2012 new HV 86 supply units were installed in two quadrants of the first FCAL layer, covering 87  $1.6 < \phi < 3.1$  on either side of the detector ( $|\eta| > 3.2$ ). Unfortunately, the 88 new units supplied 30% less voltage than they were supposed to, and since 80 events were reconstructed assuming the correct voltage, jets in the affected 90 areas were reconstructed with lower energies. The problem was eventually 91 discovered and the old HV modules put back in, but  $1.2 \text{ fb}^{-1}$  of data were 92 93 affected.

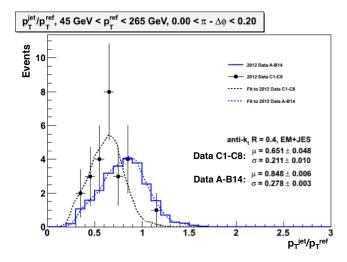


Figure 8.7:  $p_{\rm T}$  balance distributions for data taken before the installation of faulty HV modules (solid line) and data taken while the faulty units were in place (points). Average  $p_{\rm T}$  balance is measured using the template fit method, with the distribution for the data taken with good HV units used for the template. The half-width at half of the maximum ( $\sigma$ ) and mean of the template between the half-maxima ( $\mu$ ) are indicated in the text labels for the fit to each distribution along with the ratio of the means.

Figure 8.7 shows the  $p_{\rm T}$  balance distribution for events with jets in the affected area for data taken before the new units were installed and data taken while they were in place. The dashed lines show fits using the unaffected data as a template. The mean  $p_{\rm T}$  balance for the data with the faulty HV units is observed to be about 20% lower than for the data with <sup>99</sup> good HV units. The data were eventually reprocessed using the actual HV <sup>100</sup> supplied before being used for the  $W^{\pm}W^{\pm}jj$  measurement, eliminating the <sup>101</sup> need to apply a correction, but the ability to see this effect demonstrates <sup>102</sup> the sensitivity of the Z+jet  $p_{\rm T}$  balance method to differences between the <sup>103</sup> calibrated jet  $p_{\rm T}$  and the true jet  $p_{\rm T}$ .

#### 104 8.4 Results

Figure 8.8 shows the average  $p_{\rm T}$  balance for the EM+JES calibration as 105 a function of  $p_{T}^{\text{ref}}$  in four  $|\eta|$  bins using just the mean of the distribution. 106 Corresponding plots for the LCW+JES calibration are shown in Figure 8.9. 107 The data/MC ratio is shown in the bottom panel of each plot along with 108 the fractional uncertainty due to the jet energy scale and resolution. Good 109 agreement is seen between data and MC within the systematic uncertainty. 110 As previously discussed, the average  $p_{\rm T}$  balance is biased towards large 111 values for low  $p_{\rm T}^{\rm ref}$ . Since this is true for both data and MC, the data/MC 112 ratio is biased towards one. While an unbiased measurement of the aver-113 age  $p_{\rm T}$  balance is desirable, it is not necessary in order to evaluate whether 114 the systematic uncertainty is sufficient to cover the observed data/MC dif-115 ferences. The JES/JER systematic is propagated to this measurement by 116 repeating the analysis with the energy of each jet varied up and down by the 117 JES uncertainty or with the jet energy smeared by a Gaussian distribution 118 with a width given by the JER uncertainty. The measurements with the 119 JES variations will also be biased towards large average  $p_{\rm T}$  balance, which 120 means the ratio  $MC \pm 1\sigma^{JES}/MC$  will also be biased towards one. This effect 121 is what causes the fractional uncertainty shown in Figure 8.8 to decrease be-122 low  $p_{\rm T}^{\rm ref} = 50$  GeV even though calorimeter resolution is worse at low energy. 123

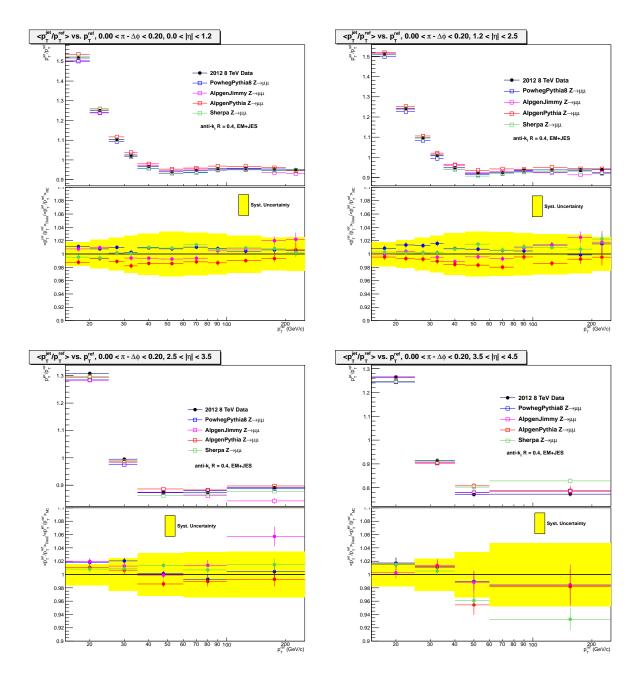


Figure 8.8: Average value of  $\frac{p_T^{jet}}{p_T^{ref}}$  for EM+JES-calibrated jets as a function of  $p_T^{ref}$  for four bins in jet  $\eta$  with the data/MC double-ratio shown at the bottom. The yellow band on the double-ratio plot shows the systematic uncertainty from the jet energy scale.

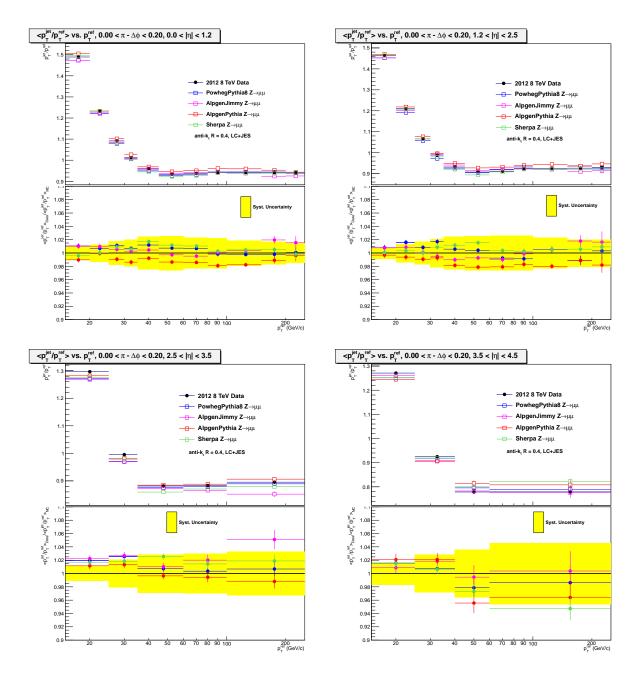


Figure 8.9: Average value of  $\frac{p_T^{jet}}{p_T^{ref}}$  for LCW+JES-calibrated jets as a function of  $p_T^{ref}$  for four bins in jet  $\eta$  with the data/MC double-ratio shown at the bottom. The yellow band on the double-ratio plot shows the systematic uncertainty from the jet energy scale.

### Chapter 9

## Results

### <sup>1</sup> 9.1 Summary of Control Region Observations

In addition to the regions previously described, a low  $m_{jj}$  control region is defined by inverting the  $m_{jj}$  selection and dropping the  $|\Delta y_{jj}|$  selection. The background composition in this region is very similar to the signal regions, but the signal contribution is greatly reduced. This provides a final check of the combined background model in a region very close to the signal regions. The  $|\Delta y_{jj}|$  distribution in the low  $m_{jj}$  control region is shown in Figure 9.1, and event counts are given in Table 9.1.

The results for all control regions are summarized in Table 9.2. They 9 show good agreement between data and prediction. Nine of the twelve sta-10 tistically independent control regions have agreement within the estimated 11 uncertainty while the remaining three all agree within twice the uncertainty. 12 Assuming the measurements follow a Gaussian distribution, the expected 13 numbers of  $1\sigma$  and  $2\sigma$  deviations are roughly 4 and 0.5, respectively. These 14 results give confidence that the background and its systematic uncertainties 15 are properly estimated. 16

### **17** 9.2 Signal Region Observations

Table 9.3 shows the predicted and observed number of events in the two signal regions. A total of 20.1 background events and 21.7 signal events (both electroweak and strong  $W^{\pm}W^{\pm}jj$  production) are predicted in the inclusive SR while 15.9 background events and 13.9 signal events (electroweak  $W^{\pm}W^{\pm}jj$  only) are predicted in the VBS SR. The observed yields are 50 events and 34 events, respectively, a slight excess over the total prediction.

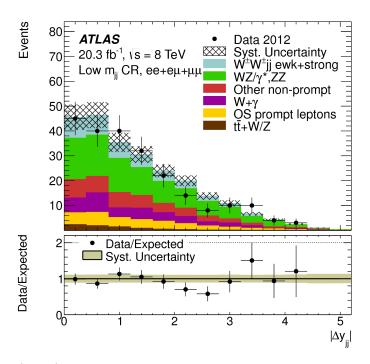


Figure 9.1:  $|\Delta y_{jj}|$  distribution for events in the low  $m_{jj}$  control region. The top panel shows the number of events for the data (points) and the Standard Model prediction (histogram) while the points in the bottom panel show the ratio of data/prediction. The systematic uncertainty on the prediction is indicated by the hatched band in the top panel and solid band in the bottom panel.

Low $m_{jj}$ Control Region					
	ee	$e\mu$	$\mu\mu$	Total	
$W^{\pm}W^{\pm}$ jj ewk+strong	$6.5\pm0.7$	$18.8 \pm 1.9$	$11.4 \pm 1.2$	$37 \pm 4$	
$W\mathrm{Z}/\gamma^*, Z\mathrm{Z}$	$25 \pm 4$	$54 \pm 9$	$18.4\pm3.1$	$98 \pm 16$	
$W{+}\gamma$	$14 \pm 4$	$20 \pm 6$	$0.00\pm0.00$	$34 \pm 10$	
OS prompt leptons	$19.4\pm2.3$	$8.4 \pm 1.4$	—	$27.8 \pm 3.4$	
$t\bar{t}$ + $W/Z$	$1.7\pm0.7$	$3.8\pm1.6$	$2.4\pm1.0$	$7.9 \pm 3.4$	
Other non-prompt	$9 \pm 4$	$21\pm8$	$8 \pm 4$	$39 \pm 10$	
Total Predicted	$76 \pm 9$	$127\pm16$	$40 \pm 6$	$243 \pm 27$	
Data	78	120	30	228	

Table 9.1: Event counts in the low  $m_{jj}$  control region. Observed event yields agree well with the Standard Model prediction.

Cont	rol Region	Trilepton	$\leq 1$ jet	b-tagged	Low $m_{jj}$
ee	pred.	$36 \pm 6$	$278\pm28$	$40 \pm 6$	$76 \pm 9$
	data	40	288	46	78
$e\mu$	pred.	$110 \pm 18$	$288 \pm 42$	$75 \pm 13$	$127\pm16$
	data	104	328	82	120
$\mu\mu$	pred.	$60 \pm 10$	$88 \pm 14$	$25\pm7$	$40 \pm 6$
	data	48	101	36	30

Table 9.2: Comparison of predicted ("pred.") and observed ("data") event counts for all control regions.

	Inclusive Region			VBS Region		
	ee	$e\mu$	$\mu\mu$	ee	$e\mu$	$\mu\mu$
Prompt	$3.0\pm0.7$	$6.1 \pm 1.3$	$2.6\pm0.6$	$2.2 \pm 0.5$	$4.2\pm1.0$	$1.9 \pm 0.5$
Conversions	$3.2\pm0.7$	$2.4\pm0.8$	—	$2.1 \pm 0.5$	$1.9\pm0.7$	—
Other non-prompt	$0.61\pm0.30$	$1.9\pm0.8$	$0.41\pm0.22$	$0.50\pm0.26$	$1.5\pm0.6$	$0.34\pm0.19$
$W^{\pm}W^{\pm}jj$ Strong	$0.89\pm0.15$	$2.5\pm0.4$	$1.42\pm0.23$	$0.25\pm0.06$	$0.71\pm0.14$	$0.38\pm0.08$
$W^{\pm}W^{\pm}jj$ Electroweak	$3.07\pm0.30$	$9.0\pm0.8$	$4.9\pm0.5$	$2.55\pm0.25$	$7.3\pm0.6$	$4.0\pm0.4$
Total background	$6.8 \pm 1.2$	$10.3\pm2.0$	$3.0\pm0.6$	$5.0\pm0.9$	$8.3\pm1.6$	$2.6 \pm 0.5$
Total predicted	$10.7 \pm 1.4$	$21.7\pm2.6$	$9.3\pm1.0$	$7.6\pm1.0$	$15.6\pm2.0$	$6.6\pm0.8$
Data	12	26	12	6	18	10

Table 9.3: Predicted and observed event counts in the signal regions. The "Total background" includes strong  $W^{\pm}W^{\pm}jj$  production in the VBS region but not in the inclusive region, where both strong and electroweak production are treated as signal.

Figure 9.2 shows the di-jet invariant mass distribution just prior to ap-24 plying the  $m_{ij}$  cut and the  $\Delta y_{ij}$  distribution after requiring  $m_{ij} > 500$  GeV. 25 Vector boson scattering processes are characterized by two jets that form a 26 large invariant mass and have a large separation in rapidity. Accordingly, 27 the distribution show an increase in the fraction of predicted events coming 28 from the electroweak production of  $W^{\pm}W^{\pm}jj$  at large values of these ob-29 servables. The data agrees well with the total distribution and disfavors the 30 background-only prediction. 31

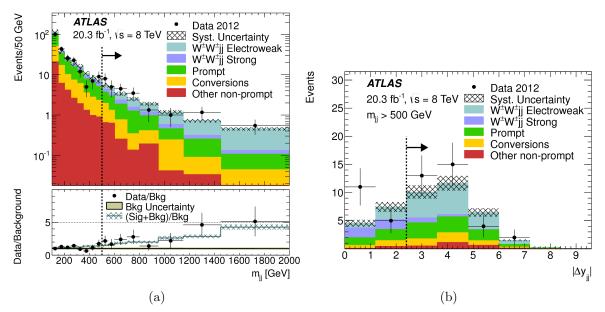


Figure 9.2: (a) The di-jet invariant mass distribution for events passing all signal selections before the  $m_{jj}$  requirement is applied (b) the  $\Delta y_{jj}$  distribution of events in the inclusive SR. In the bottom panel of the  $m_{jj}$  plot, the points show the ratio of data to the predicted background while the line and hatched band give the ratio of the total prediction (signal + background) to the background prediction and the systematic uncertainty on this ratio.

Distributions related to the WW system are shown in Figure 9.3 for the VBS SR. Figure 9.3a shows the transverse mass formed using the two leptons and missing transverse energy. Neglecting the lepton masses, it is defined as  $m_{\rm T} = \sqrt{(p_{\rm T}^{\ell_1} + p_{\rm T}^{\ell_2} + E_{\rm T}^{\rm miss})^2 - (\vec{p}_{\rm T}^{\ell_1} + \vec{p}_{\rm T}^{\ell_2} + \vec{E}_{\rm T}^{\rm miss})^2}$ . The background prediction peaks at low values of  $m_{\rm T}$  while the  $W^{\pm}W^{\pm}jj$  contribution peaks near  $m_{\rm T} = 2m_W$ . The combined distribution agrees well with observation. Figure 9.3b shows the scalar sum of the lepton transverse momenta, which is <sup>39</sup> sensitive to aQGCs. The anomalous couplings operators discussed in Chap-<sup>40</sup> ter 2 contain derivatives of the gauge fields and will be enhanced when the <sup>41</sup> momenta of the gauge bosons are large. The presence of aQGCs would <sup>42</sup> therefore be expected to appear as an excess at large  $\Sigma |p_{\rm T}^{\ell}|$ , as shown in <sup>43</sup> Figure 9.4. The observed data exhibit agreement with uncertainties over <sup>44</sup> the full range of the distribution.

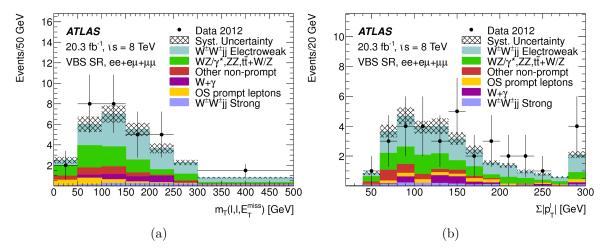


Figure 9.3: VBS SR distributions for (a) the transverse mass formed using both leptons and missing transverse energy and (b) the scalar sum of the lepton momenta.

Figure 9.5 shows two more distributions that give good separation between the strong and electroweak production mechanism. Lepton centrality (Figure 9.5a) is defined as:

$$\zeta = \min[\min(\eta^{\ell_1}, \eta^{\ell_2}) - \min(\eta^{j_1}, \eta^{j_2}), \max(\eta^{j_1}, \eta^{j_2}) - \max(\eta^{\ell_1}, \eta^{\ell_2})] \quad (9.1)$$

where  $\ell_1$  and  $\ell_2$  are the two leptons and  $j_1$  and  $j_2$  are the two highest-48  $p_{\rm T}$  jets in the event. Positive values indicate events in which the pseudo-49 rapidities of the leptons are situated in between the pseudorapidities of the 50 jets, while negative values correspond to events where at least one lepton is 51 not bracketed by the jets. Since the jets in electroweak  $W^{\pm}W^{\pm}jj$  produc-52 tion scatter at smaller angles with respect to the beam direction than the 53 jets in strong production, positive values of lepton centrality are expected to 54 be dominated by electroweak production. The jet multiplicity (Figure 9.5b) 55 for electroweak production is also more sharply peaked at two jets than 56

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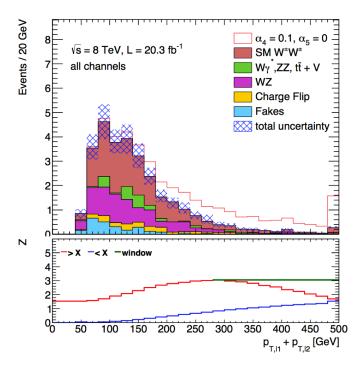
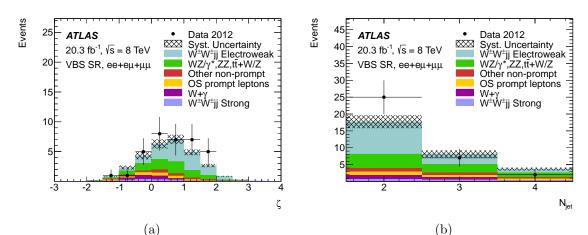


Figure 9.4: Scalar sum of the lepton momenta in the VBS signal region. The Standard Model prediction ( $\alpha_4 = \alpha_5 = 0$ ) is given by the solid histogram, and the red line shows how the prediction would change for  $\alpha_4 = 0.1$ .



<sup>57</sup> for strong production. In both cases, the data agrees well with the total <sup>58</sup> prediction.

Figure 9.5: VBS SR distributions for (a) the lepton centrality and (b) the jet multiplicity, which include the requirement  $|\Delta y_{jj}| > 2.4$ . The points show the observed data while the stacked histogram gives the SM prediction.

As discussed in Chapter 2, the predicted ratio between events with positively charged leptons and events with negatively charged leptons is about 3.3 for  $W^{\pm}W^{\pm}jj$  production. This is much greater than for other process with prompt same-sign leptons (expected ratio less than 2) or non-prompt leptons (expect equal numbers of positive and negative charges). Figure 9.6 shows the sum of the lepton charges for events in the VBS region. The data agrees well with the prediction from MC.

#### <sup>66</sup> 9.3 Testing the Standard Model Hypothesis

The event yields and distributions in the signal regions show a clear pref-67 erence for the Standard Model hypothesis, which includes  $W^{\pm}W^{\pm}ii$ , over 68 the background-hypothesis. The statistical significance of this statement is 69 evaluated using a profile likelihood test [87]. Before considering systematic 70 uncertainties, the likelihood of observing  $N_i^{\text{obs}}$  events in a channel where 71  $N_i^{\text{exp}}$  are expected follows a Poisson distribution. The total likelihood is 72 then a product across the three channels with one unknown parameter, the 73  $W^{\pm}W^{\pm}jj$  cross section, that changes  $N_i^{\exp}$ . 74

$$L(\sigma_{WW}) = \prod_{i} \text{Poisson}(N_{i}^{\text{obs}} | N_{i}^{\text{exp}}(\sigma_{WW}))$$
(9.2)

Systematic uncertainties are taken into account by adding nuisance parameters to Equation 9.2. Uncertainties are assumed to follow a Gaussian distribution, with a shift of 1 standard deviation in the nuisance parameter causing a shift in the expected number of events by the measured value of the associated uncertainty. The leads to the following likelihood function:

$$L(\sigma_{WW}, \vec{\alpha}) = \prod_{\text{chan}} \text{Poisson}(N^{\text{obs}} | N^{\text{exp}}(\sigma_{WW}, \tilde{\alpha})) \prod_{\text{syst}} \text{Gaus}(\alpha | \mu = 0, \sigma = 1)$$
(9.3)

Maximizing the likelihood with respect to all free parameters gives the  $W^{\pm}W^{\pm}jj$  cross section that is most consistent with the data. The consistency of a given hypothesis with the data is then determined by comparing the maximum likelihood for that hypothesis (that is, with a given value of  $\sigma_{WW}$ ) to the unconditional maximum likelihood using a test statistic. The test statistic used is:

$$\lambda(\sigma_{WW}) = -2\ln\frac{L(\sigma_{WW}, \hat{\vec{\alpha}})}{L(\sigma_{\hat{W}W}, \hat{\vec{\alpha}})}$$
(9.4)

Where  $\{\hat{x}\}$  denote the set of parameters that give the overall maximum 86 likelihood, and  $\hat{\vec{\alpha}}$  denotes the set of nuisance parameters that maximize the 87 likelihood for a given  $\sigma_{WW}$ . In the large-statistics limit, this quantity follows 88 a  $\chi^2$  distribution, with values near zero corresponding to measurements that 89 agree well with the hypothesis and large values indicating a measurement 90 that is inconsistent with the hypothesis. The significance with which a 91 hypothesis is rejected using this test is  $Z = \sqrt{\lambda}$ , where Z indicates the 92 likelihood of obtaining a value of the test statistic at least as large as the 93 observed one, translated into units of standard deviations from the mean of 94 a Gaussian distribution. The corresponding probabilities for significances 95 up to 6 standard deviations is shown in Table 9.4. 96

Using this method, the measured fiducial cross sections are  $2.1 \pm 0.5$ (stat.)  $\pm 0.3$ (syst.) fb for the sum of electroweak and strong  $W^{\pm}W^{\pm}jj$  production in the inclusive SR and  $1.3 \pm 0.4$ (stat.)  $\pm 0.2$ (syst.) fb for electroweak production plus interference in the VBS region. These values are in agreement with the Standard Model predictions of  $1.52 \pm 0.11$  fb and  $0.95 \pm 0.06$ 

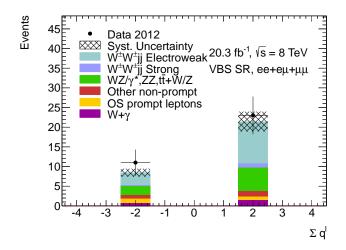


Figure 9.6: Sum of the lepton charges for events in the VBS signal region, which includes the requirement  $|\Delta y_{jj}| > 2.4$ . The points show the observed data while the stacked histogram gives the SM prediction.

α	Z
0.3173	$1\sigma$
$4.55\times10^{-2}$	$2\sigma$
$2.7  imes 10^{-3}$	$3\sigma$
$6.3  imes 10^{-5}$	$4\sigma$
$5.7  imes 10^{-7}$	$5\sigma$
$2.0 \times 10^{-9}$	$6\sigma$

Table 9.4: Probability ( $\alpha$ ) corresponding to a given significance (Z) [8].

fb. The cross sections measured for individual channels are shown in Figure 9.7. The significance with which the background-only hypothesis (which includes strong  $W^{\pm}W^{\pm}jj$  production in the VBS region) is rejected is 4.5 $\sigma$ in the inclusive region and 3.6 $\sigma$  in the VBS region. This constitutes the first evidence for  $W^{\pm}W^{\pm}jj$  production as a whole and for the electroweak process.

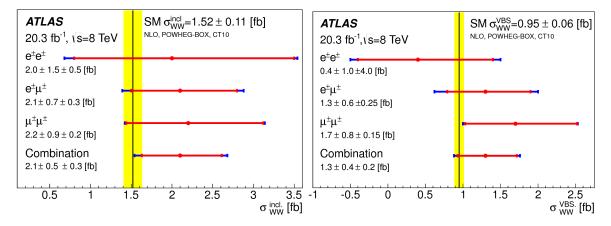


Figure 9.7: Measured fiducial cross sections for electroweak+strong production in the inclusive SR(left) and electroweak+interference in the VBS SR(right). The inner red bands indicate the uncertainties on the measured cross sections due only to statistics while the outer blue bands give the total uncertainty.

#### <sup>108</sup> 9.4 Testing aQGC Hypotheses

The VBS SR is used to test aQGC hypotheses. Using the test statistic 109 defined in Equation 9.4, an aQGC hypothesis, defined by the choice of the 110 parameters  $(\alpha_4, \alpha_5)$ , is rejected at 95% confidence level (CL) if  $\lambda \geq 3.84$ . The 111 WHIZARD [88] event generator interfaced to PYTHIA8 for parton showering is 112 used to derive the fiducial cross section for electroweak  $W^{\pm}W^{\pm}jj$  production 113 for a given choice of  $\alpha_4$  and  $\alpha_5$ . A fine grid of points is used to map out 114 the cross sections in the  $(\alpha_4, \alpha_5)$  plane as shown in Figure 9.8. WHIZARD 115 generates events at leading order in the strong coupling constant. The 116 NLO cross section for the Standard Model point ( $\alpha_4 = \alpha_5 = 0$ ), calculated 117 using POWHEG-BOX as described in Chapter 6, is found to be 1.3 times 118 higher than the WHIZARD cross section. This scale factor is applied to all 119

<sup>120</sup> aQGC points to obtain approximate NLO cross sections. The contribution <sup>121</sup> from interference is also included and is calculated using:

$$\sigma_{VBS}^{INT} = k_{INT} \sqrt{\sigma_{VBS}^{ewk} \sigma_{VBS}^{strong}} \tag{9.5}$$

where  $\sigma_{VBS}^{ewk}$  and  $\sigma_{VBS}^{strong}$  are the cross sections for electroweak and strong production in the VBS signal region, and  $k_{INT}$  is a proportionality factor determined from the Standard Model cross sections to be 0.231.

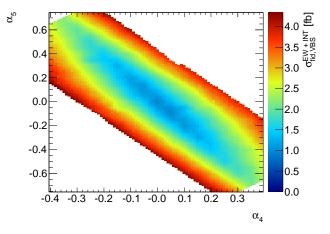


Figure 9.8: Fiducial cross section for electroweak  $W^{\pm}W^{\pm}jj$  production, determined using WHIZARD and scaled to include interference, as a function of  $\alpha_4$  and  $\alpha_5$ . Contours of constant cross section form ellipses in the  $(\alpha_4, \alpha_5)$  plane.

The time required to generate all of these points with full detector simu-125 lation is prohibitive, so a coarse grid of points is used to derive a correction 126 for the efficiency of an event in the fiducial region to be reconstructed in 127 the signal region. The efficiency is found to depend linearly on the fidu-128 cial cross section for electroweak  $W^{\pm}W^{\pm}jj$  production. The linear fits are 129 shown in Figure 9.9. Over the range of aQGC points considered, the effi-130 ciency varies by about 35% in the ee channel and 10% in the  $e\mu$  and  $\mu\mu$ 131 channels. The difference between the efficiency predicted for the Standard 132 Model ( $\alpha_4 = \alpha_5 = 0$ ) using this method and the efficiency derived using the 133 SHERPA sample is taken as an additional uncertainty. 134

The resulting 95% CL exclusion is shown in Figure 9.10. Due to the small excess in the VBS signal region, the observed limits are slightly weaker than expected. Profile likelihoods as a function of  $\alpha_4$  with  $\alpha_5 = 0$  and vice

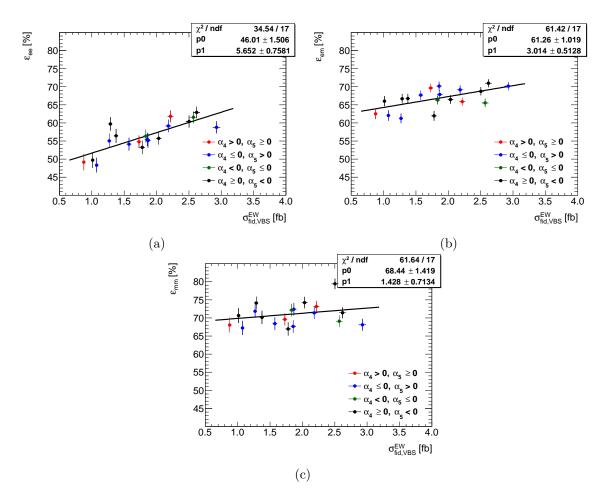


Figure 9.9: Efficiency as a function of the fiducial cross section for electroweak  $W^{\pm}W^{\pm}jj$  production in the VBS SR for (a) the *ee* channel, (b) the  $e\mu$  channel, and (c) the  $\mu\mu$  channel.

versa are shown in Figure 9.11. The resulting one-dimensional limits on the parameters are  $-0.14 < \alpha_4 < 0.16$  and  $-0.23 < \alpha_5 < 0.24$ .

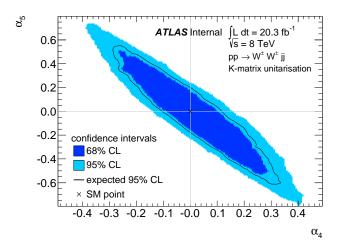


Figure 9.10: Limits on  $(\alpha_4, \alpha_5)$ . Points outside the light blue ellipse are excluded at 95% CL while points outside the dark blue ellipse are excluded at 68% CL.

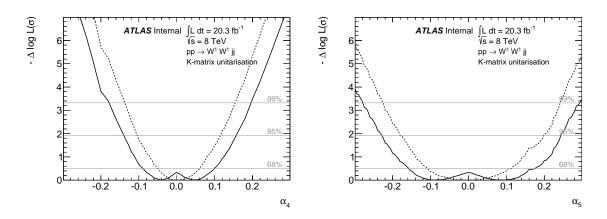


Figure 9.11: Expected (dashed) and observed (solid) profile likelihoods as a function of  $\alpha_4$  (left) and  $\alpha_5$  (right).

### Chapter 10

## **Conclusions and Outlook**

Two measurements of fiducial cross sections for  $W^{\pm}W^{\pm}ii$  production and its 1 electroweak component have been performed using proton-proton collisions 2 with a center-of-mass energy of 8 TeV at the LHC. The collision data used 3 for these measurements was collected in 2012 using the ATLAS detector 4 and corresponds to an integrated luminosity of 20.3 fb<sup>-1</sup>. The fiducial cross 5 section for inclusive  $W^{\pm}W^{\pm}ii$  production has been measured in events with 6 two leptons with the same electric charge, missing transverse energy, and 7 at least two jets with a large invariant mass. The measurement of the 8 electroweak production of  $W^{\pm}W^{\pm}jj$  is performed after making an additional 9 requirement that the two leading jets have a large separation in rapidity. 10

In the inclusive signal region, 50 events are observed with 20 events 11 expected from background process. The statistical significance of the excess 12 in this region is  $4.5\sigma$ . In the VBS signal region, 16 background events are 13 expected and 34 are observed, giving a significance of  $3.6\sigma$ . In both cases, 14 the kinematic distributions of the observed excess are consistent with the 15 Standard Model prediction for  $W^{\pm}W^{\pm}ii$  production. The cross section 16 measured in the inclusive region is  $2.1 \pm 0.5$ (stat.)  $\pm 0.3$ (syst.) fb, and 17 the cross section measured in the VBS region (for electroweak production) 18 is  $1.3 \pm 0.4$ (stat.)  $\pm 0.2$ (syst.) fb. This agrees with the Standard Model 19 predictions of  $1.52 \pm 0.11$  fb and  $0.95 \pm 0.06$  fb. Using the VBS signal 20 region, limits have also been placed on aQGC parameters  $\alpha_4$  and  $\alpha_5$  in 21 the electroweak chiral Lagrangian framework with K-matrix unitarization 22 applied. In the case where one of the two parameters is fixed to zero, the 23 95% CL limits are  $-0.14 < \alpha_4 < 0.16$  and  $-0.23 < \alpha_5 < 0.24$ , which improve 24 on existing upper bounds from electroweak precision measurements of  $\alpha_4 < \infty$ 25 0.30 and  $\alpha_5 < 0.76$ . 26

The LHC will resume running in 2015 starting with a center-of-mass 27 energy of 13 TeV and eventually reaching the design energy of 14 TeV. Run 28 2 is scheduled to go until 2018, followed by another shutdown and another 29 run from 2020-2022. The most exciting possibility for the next run is the 30 possibility of new physics existing at energies of a few TeV, leading to the 31 discovery of new particles. However, even if the energy scale of new physics 32 is too large for direct detection at the LHC, the increase in energy will bring 33 an increase in sensitivity to anomalous gauge couplings that may be induced 34 if the new physics couples to electroweak gauge bosons. Since the dominant 35 uncertainties on the measurement presented in this dissertation are due to 36 statistics, a similar  $W^{\pm}W^{\pm}jj$  measurement in the next run will also benefit 37 just from the increase in the amount of collision data. 38

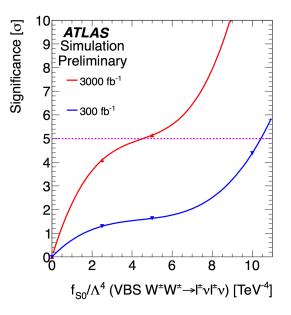


Figure 10.1: Projected sensitivity to the  $\frac{f_{S,0}}{\Lambda^4}$  coupling from future measurements of  $W^{\pm}W^{\pm}jj$  production at the LHC.

The luminosity projected for Run 2 is ~80-100 fb<sup>-1</sup>, with another ~200 fb<sup>-1</sup> of data expected in Run 3. Figure 10.1 shows a projection of the sensitivity to the  $\frac{f_{S,0}}{\Lambda^4}$  parameters with 300 fb<sup>-1</sup> of data at 14 TeV [92], roughly corresponding to the end of Run 3. The number of  $W^{\pm}W^{\pm}jj$  events in this sample with  $m_{jj} > 1$  TeV is expected to be ~500. Anomalous couplings as low as 10 TeV<sup>-4</sup> are projected to be observable at this point. The corresponding value of  $\alpha_4$  is about 0.0046. The increase in statistics will also make

- <sup>46</sup> measurements of differential distributions possible. In short,  $W^{\pm}W^{\pm}jj$  pro-
- 47 duction remains a promising process for the study of electroweak symmetry
- <sup>48</sup> breaking in the next run of the LHC. The current measurement has served
- <sup>49</sup> to again confirm the Standard Model, but hopefully the next run will give
- 50 us a peek at something new.

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### Appendix A

# Description of Author Contributions

The measurement presented in this dissertation is result of the collaborative
effort of thousands of people spanning two decades. The purpose of this
appendix is to highlight the experience that I have gained with a brief description of tasks in which I was directly involved. These can be separated
into three broad categories: hardware, software, and data analysis.

Since the ATLAS detector was already built and taking data by the time 6 I joined the experiment in 2010, my work on hardware has been towards future upgrades. All of my work in this area has been with a next-generation 8 pixel chip, designated the "FE-I4," that was used in the Insertable Barrel 9 Layer (IBL), a fourth layer added to the pixel detector during the shutdown 10 that started in 2013. I performed tests of the digital logic of the chip design 11 using Verilog simulations. The chip has independent parameters for setting 12 the voltage reference and rise time of individual pixels. I contributed to 13 software for tuning these parameters that was used in tests of chip perfor-14 mance. A new feature in the FE-I4 is the presence of self-monitoring signals 15 that track potentially interesting quantities like temperature and leakage 16 currents. I helped write firmware for reading out these signals in the IBL. 17

My involvement in ATLAS software has been confined to monitoring tracking software updates. Developers in ATLAS are continually seeking to improve track reconstruction. Updates are tested nightly by making a standard set of plots with several MC samples. These are compared to those made with previous versions of the software, both to confirm expected improvement and to catch any unexpected changes. In addition to taking shifts monitoring nightly tests, I inherited management of the software package use to make the monitoring plots and have been responsible for updating it as
necessary to remain compatible with newer ATLAS software.

The bulk of my effort has been in data analysis. For the  $W^{\pm}W^{\pm}jj$  mea-27 surement, I performed several studies on optimizing event selections and the 28 isolation criteria for leptons, wrote software for generating plots and tables 29 for each signal and control region, and estimated the impact of experimental 30 uncertainties on the signal/control region predictions. I investigated discrep-31 ancies between data and prediction in the control regions to look for evidence 32 of additional backgrounds or systematic effects that were unaccounted for. 33 I also performed cross-checks of fake rate uncertainties using high-d<sub>0</sub> muons 34 as described in Chapter 7 and jet energy scale uncertainties using the Z+jet 35 studies described in Chapter 8. 36

### Appendix B

## The FE-I4 Chip

The FE-I4 is a new pixel chip [93] that has been used in the Insertable 1 B-Layer (IBL), a fourth barrel layer added to the ATLAS pixel detector 2 during the 2013/2014 shutdown. The main improvement over the FE-I3 3 chip used in the rest of the pixel detector is a smaller pixel size. Pixels 4 on the FE-I4 measure 50  $\mu$ m × 250  $\mu$ m, down from 50  $\mu$ m × 400  $\mu$ m. Ad-5 ditional features of the FE-I4 include on-board monitoring signals, internal 6 error logging counters, and a clock multiplier to support high-speed readout. 7 Two voltage regulators (one for analog voltage and one for digital voltage) 8 mitigate the effect of variations in the supply voltage on the voltage received 9 by the chip. The nominal supply voltage is 1.8 V, but the regulators allow 10 operation anywhere between 1.5 V and 2.5 V. 11

### <sup>12</sup> B.1 Single Pixel

The circuit diagram for a single pixel is shown in Figure B.1. The octagon 13 on the left indicates where the pixel is bonded to the sensor. During normal 14 operation, this is where charge would be collected. For purposes of tuning 15 and testing the pixel, there is a built-in capability to inject charge by sending 16 a voltage pulse, sometimes called a "calibration pulse," across the capacitors, 17  $C_{inj1}, C_{inj2}$ . The input signal goes through a two-stage amplifier before 18 being fed into a comparator. When the amplified input signal exceeds the 19 reference voltage of the comparator, the number of clock cycles for which it 20 remains above the reference voltage is recorded as a 4-bit time-over-threshold 21 (ToT) measurement. 22

The sensitivity pixels can be tuned globally by changing the reference voltages supplied to all pixels  $(V_{th}, V_{fb}, \text{ and } V_{fb2})$  or locally by adjusting

values stored in a local pixel register that are fed into digital-to-analog con-25 verters (DACs) to provide additional reference voltages (FDAC, TDAC). 26 The TDAC and  $V_{th}$  set the reference voltage of the comparator and can be 27 used to shift the threshold charge required to register a hit. The FDAC, 28  $V_{fb}$ , and  $V_{fb2}$  adjust feedback capacitances in the amplifier, affecting both 29 the rise time and the gain. This allows one to tune the ToT corresponding 30 to a given input signal but can also change the threshold. The chip also 31 contains a single analog output, into which the signals of several pixels, at 32 different stages in the analog circuit, are multiplexed. This output can be 33 used to test that a pixel circuit is performing properly. 34

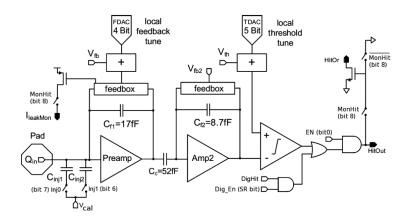


Figure B.1: Schematic of an analog pixel circuit for the FE-I4. Figure taken from Ref. [93]

#### **35** B.2 Overall Structure

Pixels are arranged into 40 double-columns with 336 rows. Pixel hits are 36 stored in memory blocks shared by a  $2 \times 2$  block of pixels while waiting for 37 a trigger to be issued. Each memory block can hold up to 5 hits at a 38 time. If a certain number of clock cycles pass without a trigger a hit will 39 be discarded. This number is called the trigger latency and is configurable. 40 Once a trigger is received, hits are read in time order, formatted, and stored 41 in an asynchronous FIFO (first-in-first-out) register until they are read by 42 the data output block. The FIFO can accommodate up to 8 hits at a time 43 and will assert a "FIFO full" signal to stop output from the data formatter 44 if it becomes full. A global register is used to store configuration data that is 45

- <sup>46</sup> independent of specific pixels, like the trigger latency and reference voltages,
- $V_{th}$ ,  $V_{fb}$ , and  $V_{fb2}$ . It is also used in the readout of the on-chip monitoring
- <sup>48</sup> signals. An illustration of the FE-I4 layout is shown in Figure B.2.

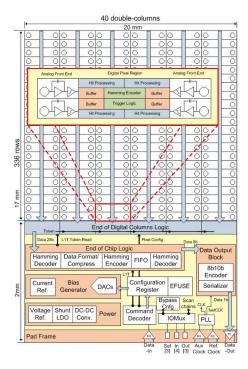


Figure B.2: Schematic drawing showing the layout of the FE-I4 chip, not drawn to scale. Figure taken from Ref. [93]

#### <sup>49</sup> B.3 Generic ADC

Not pictured in Figure B.2 is the 10-bit generic analog-to-digital converter 50 (GADC), which digitizes various analog monitoring signals. The signal to 51 be fed into the GADC is selected using a multiplexer, and the selection 52 bits given to the multiplexer are stored in the global register. The signals 53 that feed into the multiplexer are: the output of a temperature sensor, that 54 reference voltage supplied to the GADC, the analog ground, the analog 55 output, the analog regulator current, the output of a 10-bit DAC used for 56 calibration pulses, half the regulated analog voltage, and leakage current 57 from the pixels, shown on the upper-left in Figure B.1. Output of the 58 GADC is not automatically stored. A command must be sent to the chip to 59

 $_{\rm 60}$   $\,$  write the output to the global register. Then it can be read from the global

<sup>61</sup> register into the FIFO and finally sent out through the data output block.