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## Title

Effect of Stress on Apparent Coefficient of Expansion

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AUTHOR	R. Meuser	Mechanical	Berkeley	June 22,	1979
PROGRAM	High-Field Mag	net Development	I	• • • • • • • • • • • • • • • • • • •	
	Analysis				

#### A revision, 11-3-80

In the literature, the influence of stress upon the apparent coefficient of linear thermal expansion (CLTE) has been viewed as an independent physical property of a material. It has been postulated, for an extreme case where the sign of the apparent CLTE reversed at high stress, that the change probably resulted from a change in the microstructure of the material. No such abstruse explanation is necessary or warranted; a change in apparent CLTE with stress <u>must</u> occur if the elastic modulus changes with temperature. For a well-behaved elastic material, there is a simple unique relationship between the apparent CLTE, the real CLTE, and the hot and cold elastic moduli.

It doesn't seem possible that this is anything new. But it apparently is not well known, and I don't recall having seen it before. But then, I've forgotten a lot.

We consider first a material having <u>linear</u> thermal and elastic properties, and second, <u>non-linear</u> properties and show that the above statement is applicable to either.

#### Materials Having Linear Properties

We consider a material with the following properties:

At a given stress the length is uniquely determined by the temperature and the behavior is characterized by a constant value of the apparent CLTE. (See "Nomenclature"):

$$\alpha_{ap}(\sigma) \equiv L^{-1}(\partial L/\partial T)$$

At a given temperature the length is uniquely determined by the stress and the behavior is characterized by a constant value of the elastic modulus:

/A

$$E(T) \equiv L (\partial L/\partial \sigma)^{-1}$$

We note that the real CLTE is

$$\alpha = \alpha_{ap}(0)$$

It follows that the change length from one stress-temperature condition to another is independent of the stress-temperature path.

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#### Material Having Non-Linear Properties

As in the linear case, the thermal and elastic behavior must be reversible. At a given temperature, the change in length in going from stress zero to stress  $\sigma_1$  at temperature  $T_h$  is  $\varepsilon_h L$ ; at temperature  $T_c$  it is  $\varepsilon_c L$ ; as illustrated in Fig. 2.

The increase in length,  $\Delta_{i,i}$ , for each leg of the path shown in Fig. 1 is:

Leg 1-2

- Leg 2-3  $\Delta_{23} = -L \int_{T_c}^{T_h} \alpha(T)$
- Leg 3-4
- $^{\Delta}34 = {\begin{subarray}{c} \varepsilon \\ c \end{array}}L$

 $\Delta 12 = - \epsilon_{\rm p} L$ 

Leg 4-1  $\Delta_{41} = \alpha_{ap}(T_h - T_c)L$ 

Again:

$$\Delta_{12} + \Delta_{23} + \Delta_{34} + \Delta_{41} = 0$$

These equations reduce to:



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<u>Example (Linea</u>	<u>r):</u>	· · · · ·			
$E_{\rm b} = 1.0$	x 10 <sup>6</sup>			· · ·	
	1.06			•	.*
$E_{c} = 0.5$	X 10			÷ .	
$\alpha$ = 5.0 x	10 <sup>-5</sup>				
$T_h - T_c =$	100				
~ - 1 0 v	10 4				
0 - 1.0 x		14	· · · · · ·		
•••	-5		•		٣
$\alpha_{ap} = -5.$	$0 \times 10^{\circ} = -\alpha$	* .			
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Nomenclature:		· . · ·			
	-1				
α	CLTE: L ' (ƏL/ƏT	) at $\sigma = 0$	•		
α <mark>a</mark> p	Apparent CLTE: L	-'(ƏL/ƏT) at	ς σ = σ <sub>1</sub>		
σ	Axial stress (+ :	= tension)			,
Ľ	Length of body		· ·		
F	Flastic modulus.	$1^{-1}(21/2\sigma)$	at constant T		
		т (02/00)			
<sup>E</sup> h' <sup>E</sup> c	r at i = ih' i =	'c			
T	Temperature				
∆ij	Increase in leng leg i-j.	th of body f	or temperature	-stress path	
E	Axial strain	(+++	en ston)		

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