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Solid Oxide Fuel Cell-Gas Turbine Hybrid Power Systems: Energy Analysis, Control Assessments, Fluid Dynamics Analysis and Dynamic Modeling for Stationary and Transportation Applications

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**Author** Azizi, Mohammad Ali

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#### UNIVERSITY OF CALIFORNIA, IRVINE

#### Solid Oxide Fuel Cell-Gas Turbine Hybrid Power Systems: Energy Analysis, Control Assessments, Fluid Dynamics Analysis and Dynamic Modeling for Stationary and Transportation Applications

#### DISSERTATION

submitted in partial satisfaction of the requirements for the degree of

#### DOCTOR OF PHILOSOPHY

in Mechanical and Aerospace Engineering

by

Mohammad Ali Azizi

Dissertation Committee: Professor Jacob Brouwer, Chair Professor Scott Samuelsen Professor Ken Mease

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## **DEDICATION**

То

My parents

for their inspiration and encouraging me to follow my dreams

## TABLE OF CONTENTS

				Page
LI	IST O	F FIGU	JRES	vi
LI	IST O	F TABI	LES	xii
A	CKNO	OWLED	OGMENTS	xiii
CI	URRI	CULUN	M VITAE	xiv
Al	BSTR	АСТ О	F THE DISSERTATION	xix
1	Intro	oductio	n and Background	1
	1.1	Introdu	uction	1
		1.1.1	Emergence of SOFC power plants	1
	1.2	Goal a		4
		1.2.1		4
		1.2.2		4
2	Lite	rature l	Review	6
	2.1	SOFC	-GT hybrid system background	6
		2.1.1	Experimental evaluation of Integrated SOFC-GT hybrid systems	8
		2.1.2	Experimental test facilities for hybrid systems	10
		2.1.3	Gas turbine technology applications in SOFC-GT hybrid systems .	21
	2.2	Hybric	SOFC-GT System Design Concepts	21
		2.2.1	Hybrid system configurations	23
		2.2.2	Integration with various cycles	26
	2.3	Model	s for SOFC-GT Hybrid Systems	29
		2.3.1	Early hybrid SOFC-GT model development	29
	2.4	Motiva	ation	39
	2.5	SOFC	-GT dynamics model description	40
		2.5.1	Fuel cell and stack models	40
		2.5.2	Reformer models	46
	•	2.5.3	Combustor models	51
	2.6	Steady	-State Performance Reported	53

	2.7	Compo	onent Modifications for Dynamic Hybrid System Operation	57
	2.8	Practic	al Issues Discussed in Hybrid SOFC/GT Literature	59
	2.9	Hybrid	System Transient Operation and Control	60
		2.9.1	Turbomachinery Controls	60
		2.9.2	Off-design performance of hybrid system using fixed and variable	
			GT speed	62
		2.9.3	Control strategies for compressor surge	78
		2.9.4	Computational stall/surge analysis in hybrid SOFC-GT systems	83
		2.9.5	Gas turbine and compressor models	86
	2.10	Optima	al control and reliability analysis of stationary hybrid SOFC-GT pow-	
		er gene	eration system	98
		2.10.1	System control strategies	99
	2.11	Hybrid	SOFC-GT System Optimization	111
	2.12	Parame	etric Studies	116
		2.12.1	Main parameters for SOFC-GT hybrid system simulation	116
		2.12.2	Exergy based analysis of hybrid systems	122
		2.12.3	Operating pressure effects	124
	2.13	$CO_2$ ca	apture, sequestration and emission reduction	126
	2.14	Investi	gation of alternative fuels	130
า	C	4 - 4.		174
3	2 1		onal huid dynamic Analysis	134
	3.1		Machaniams of Compressor Surge/Stall in hybrid SOEC CT system	134
		3.1.1 2 1 2	Duramia model integrated with CED simulation	130
	37	J.1.2 Diant d		140
	5.2	3 2 1	Dynamic Hybrid System Model	1/1
	33	J.2.1 Transie	ant Dynamic Simulation	141 142
	3.5	Turbon	nachinery Fluid Dynamics Simulation	142
	3.5	Geome	etry Modeling	147
	3.6	Bound	ary Conditions	148
	3.7	Fluid I	Dynamics Model	148
	3.8	Stall/S	urge Results	150
	3.9	Stall/S	urge analysis results	161
	3.10	220 kV	V Siemens-Westinghouse Power Plant	162
		3.10.1	Model Validation Efforts	163
4	Hyb	rid SOF	FC-GT Locomotive System Design	173
		Genera	al System Modeling	173
	4.1			1-0
	4.1 4.2	Hybrid	SOFC-GT system for transportation application	173
	4.1 4.2	Hybrid 4.2.1	I SOFC-GT system for transportation application      Motivation	173 173
	<ul><li>4.1</li><li>4.2</li><li>4.3</li></ul>	Hybrid 4.2.1 Scope	I SOFC-GT system for transportation application	173 173 174
	4.1 4.2 4.3	Hybrid 4.2.1 Scope 4.3.1	I SOFC-GT system for transportation application      Motivation      Research Gap	173 173 174 174

		4.3.3 Locomotive requirements	80
		4.3.4 Fueling Infrastructure for hybrid SOFC-GT locomotives 18	81
		4.3.5 Economic Considerations	84
		4.3.6 Modeling	88
		4.3.7 Total Cost calculation	93
		4.3.8 Cost Model	93
		4.3.9 Development Stages	94
		4.3.10 Cost Results	94
		4.3.11 System Sizing and Evaluation of the First long-haul SOFC-GT system 19	97
5	Moo	ling of Hybrid SOFC-GT system for locomotives 20	04
	5.1	Development of 500 kW small scale lab design	04
6	Hyb	d SOFC-GT Locomotive Dynamics and Control 2	19
	6.1	Dynamic Modeling of hybrid SOFC-GT system for locomotives 2	19
		5.1.1 Objectives	20
		6.1.2Prototype Development22	22
		5.1.3 System Optimization	24
		5.1.4      System Modeling      22	28
		6.1.5Gas Turbine Dynamic Model22	29
	6.2	Route Simulation	31
	6.3	Parametric study for fuel cell power density	37
7	Sun	nary and Conclusions 24	41
	7.1	Summary $\ldots$ $\ldots$ $\ldots$ $2^4$	41
	7.2	$Conclusion  \dots  \dots  \dots  2^4$	44
Bi	bliog	phy 24	45

## LIST OF FIGURES

### Page

2.1	250 kW prototype of hybrid SOFC-MGT system [102]	9
2.2	Long term operation test of the SOFC-MGT system [102]	10
2.3	Emulator test rigs: NETL, University of Genoa and DLR laboratories [103]	11
2.4	Block diagram of HyPer MPC control application [104]	11
2.5	MIMO controller of hybrid SOFC-GT system [111]	13
2.6	Prediction Type Kalman Filter (PTKF) [112]	14
2.7	Simplified flow diagram of hybrid simulation facility at NETL [113]	14
2.8	Load based speed control strategy [116]	15
2.9	The T100 power module modifications for the fuel cell coupling [120]	16
2.10	Test rig plant layout: the blue box is related to the SOFC model [121]	17
2.11	Hybrid cycle design [122]	18
2.12	Transient behavior of MGT with temperature variation at gas preheater [122]	19
2.13	Hybrid power plant test rig at DLR [122]	20
2.14	Basic concept of a fuel cell-gas turbine hybrid system [129]	22
2.15	Schematic of a direct hybrid gas turbine fuel cell topping cycle [30]	23
2.16	Schematic of an indirect gas turbine fuel cell bottoming cycle [30]	24
2.17	Schematic of the SOFC-MGT-ORC cycle [141]	27
2.18	Process concept of combined fermentation and gasification of sewage sludge	
	[148]	28
2.19	Schematic of a recuperated internal-reforming hybrid SOFC-GT system [64]	29
2.20	Plant layout [72]	30
2.21	Pressurized 220 kW SOFC/Gas Turbine Hybrid [30]	33
2.22	Tubular SOFC stack design [30]	34
2.23	Siemens Westinghouse substack basic building block tested at UC Irvine [158]	35
2.24	Siemens Westinghouse hybrid system [158]	35
2.25	320 kWe PSOFC/GT power system [158]	36
2.26	Scheme of the SOFC group, mixer and sensible heat reformer [155]	37
2.27	The hybrid SOFC-GT power plant being developed at DLR [161]	38
2.28	(a) Cell voltage at different temperatures and current densities. (b) 3-D view	
	of the cell voltage variation at different temperatures and current densities [64]	42
2.29	3-D view of SOFC voltage variation at different air inlet temperatures and	
	fuel flow rates [64]	45

2.30	3-D view of stack power output variation at different air inlet temperatures
	and fuel flow rates [64]
2.31	Shaft speed control strategy [190]
2.32	GT power output, model VS experiment data [30]
2.33	Partial load performance of SOFC-GT system with TIT and rotor speed as
	parameters [198]
2.34	Influence of ambient temperature without control system [199] 6
2.35	Hybrid System Part Load Efficiency [199]
2.36	Fuel Cell Part Load Efficiency [199] 6
2.37	Simplified layout of hybrid system (Personal Turbine and SOFC) [200] 6
2.38	Design and part-load performance of a hybrid system versus non-dimensional
	power (fixed turbine speed control system) [200] 7
2.39	Hybrid system inefficiencies versus non-dimensional power (Variable tur-
	bine speed control system) [200]
2.40	Pressurized SOFC hybrid system [201]
2.41	Off-design performance of P-HS (constant speed)[201]
2.42	Off-design performance of fuel cell stack in P-HS layout (constant speed)
	[201]
2.43	Off-design performance of P-HS layout (Variable speed) [201]
2.44	Off-design performance of fuel cell stack in P-HS layout (Variable speed)
	$[201] \ldots 7$
2.45	SOFC-GT hybrid system with fixed speed GT and cathode bypass [175] 7
2.46	Temperature distribution in the SOFC module (a) air stream in the electro-
	chemical reaction process (b) electrolyte and electrodes (c) fuel stream in
	the electrochemical reaction process (d) fuel stream in the reforming process
	$[202]. \ldots \ldots$
2.47	Two important temperatures of SOFC/GT hybrid system operating with VRS
	+ FC and HAB + FC modes: (a) cell temperature; (b) turbine inlet tempera-
<b>a</b> 40	ture [203]
2.48	Pressure losses between the recuperator and the combustor for three different
2 40	conditions: (1) direct line, (11) volume zero, and, (11) modular volume [205]
2.49	Temperature control system scheme (external loop) [206]
2.50	P-I feedback control loops for FC-GT control [181]
2.51	Control overview for synchronous SOFC-GT topping cycle with inlet guide
2.52	vanes (IGV) and bypass [181]
2.52	Stepwise SOFC load change for a constant ratio of G1 load to SOFC load
2 52	[200]
2.33	simulated time promes during a shut down test at valve positions $\alpha_v = 30 \text{ deg}$ standard configuration. (a) $\beta$ : (b) compressor flow rate: (c) turbing flow rate
	standard configuration. (a) $\rho_p$ , (b) compressor now rate, (c) turbine now rate [211]
2 51	[211]
2.54	Schematic of a compressor-fuel cell-combustor- gas turbine engine used in
2.55	[64]
	ל היייייייייייייייייייייייייייי

2.56	Turbomachinery Interpolation strategy [190]	93
2.57	Dual spool compressor pressure profile during mild surge following a pres-	
	sure step dynamic perturbation [215]	98
2.58	Cascade controller design [194]	100
2.59	Catalytic oxidizer control scheme [194]	100
2.60	A kilowatt per second 2.4-4.8 kW load increase with compensated fuel flow	
	combustor temperature control, current fuel cell power control and blower	
	power buffering [221]	102
2.61	SOFC-GT hybrid system integrated with autonomous power system [222] .	102
2.62	PI control structure [222]	103
2.63	Load change, SOFC temperature and fuel utilization during simulation [222]	104
2.64	Control inputs variation during simulation [222]	104
2.65	The proposed power tracking control strategy [225]	105
2.66	Control diagram of power tracking control [225]	105
2.67	Schematic of the closed-loop SOFC/GT plant with the IS-RG controller [227]	106
2.68	SOFC-GT hybrid system [228]	107
2.69	SOFC-GT control system [228]	107
2.70	System emulator layout and interface to the fuel cell stack real-time model	
	[231]	108
2.71	Flue gas temperature control loop in hybrid system [232]	109
2.72	Hybrid cycle layout [189]	110
2.73	Control system of hybrid system [189]	111
2.74	Hydrogen molar flow rate (a), SOFC voltage (b) and current (c) outputs (GT	
	load steps: 37-22.5-44 kW) [260]	115
2.75	Destroyed exergy rate of hybrid system components from Calise et al. [72].	122
2.76	Thermal/Mechanical/Electrical power generation/consumption by each com-	
	ponent from Calise et al. [72]	123
2.77	Exergy destructions per mole of methane consumed for the devices in the	
	integrated system for the illustrative example, where $V_s$ =0.61 V [270]	124
2.78	System layout of the IGCC system with pre-combustion $CO_2$ capture [296]	128
31	Surge chart	135
3.2	Impeller corrosion	136
33	Compressor surge effect on blade corrosion	137
3.4	Types of surge	138
3 5	Surge mechanism due to the high turbine inlet (TIT) temperature	139
3.6	Surge mechanism due to the system emergency shut-down	139
3.7	Hybrid SOFC-GT system power plant schematic [316]	142
3.8	1.7 MW Kawasaki multi-stage gas turbine [317]	143
3.9	1.7 MW Kawasaki gas turbine [317]	144
3.10	1.7 MW Kawasaki compressor geometry model	144
3.11	Applied Fluid Model-Multi Stage Compressor	145
3.12	Mesh generated on the Splitter	146

3.13	Mesh generated on the blade	146
3.14	Mesh generated on the diffuser	147
3.15	Operating point of 4 MW hybrid SOFC-GT at steady state condition	150
3.16	Velocity vector on the whole domain	151
3.17	Pressure distribution in the flow domain on the front and rear impellers of	
	the multi-stage compressor	152
3.18	Pressure development in the diffuser	154
3.19	Pressure development on the front impeller's shroud	155
3.20	Pressure development on the rear impeller's shroud	156
3.21	Front Impeller inlet velocity/mass flow rate oscillation	157
3.22	Rear Impeller inlet velocity/mass flow rate oscillation	157
3.23	Sustained mass flow rate after transient power demand change of the hybrid	
	SOFC-GT system	159
3.24	The front impeller velocity distribution from the leading edge (LE) to the	
	trailing edge (TE)	160
3.25	The rear Impeller velocity distribution from the LE to the TE	160
3.26	Sustained mass flow rate after transient power demand change of the hybrid	
	SOFC-GT system	162
3.27	220 kW Siemens- Westinghouse power plant	163
3.28	Compressor inlet temperature	164
3.29	Observed and simulated turbine inlet, GT1 and GT2 temperatures	164
3.30	Observed and simulated SOFC inlet and outlet temperatures	165
3.31	Modified Siemens Westinghouse Power System	166
3.32	Modified Siemens Westinghouse Control Strategy	167
3.33	Single Stage Compressor Schematic	168
3.34	C-65 (Capstone) operating parameters	169
3.35	C-65 (Capstone) operating parameters	169
3.36	C-65 impeller pressure results	170
3.37	C-65 impeller Velocity Distribution	170
3.38	C-65 impeller otutlet velocity ditribution	171
3.39	C-65 blade Velocity Distribution	171
3.40	Pressure evolution in diffuser over time	172
3.41	C-65 Single Stage Stall/Sure Results	172
4.1	Locations of CNG and LNG stations in the US	175
4.2	Japan Locomotive	176
4.3	North America BNSF Locomotive	176
4.4	North America BNSF Locomotive	177
4.5	Critical locomotive parameters	177
4.6	Chinal PEMFC Locomotive	178
4.7	China Locomotive System Integration	178
4.8	North America fuel cell locomotive system integration	179
4.9	North America fuel cell locomotive system integration schematic	179

4.10	Locomotive Power Demand	180
4.11	Locomotive Power Demand generated by fuel cell, gas turbine and blower .	180
4.12	Locomotive Efficiency	181
4.13	Hydrogen Production from various resources, Source: NREL	182
4.14	Hydrogen Production Potential	182
4.15	Hydrogen Production Potential variation from various resources with Car- load Traffic Density	183
4.16	Hydrogen Production Potential for different states (alphabetical order) ver-	
	sus Carload density	184
4.17	Material Cost	191
4.18	Total unit cost per vear versus volume production per vear	195
4.19	Total unit cost per versus volume production per vear	196
4.20	Cost calculated for different financial sections	197
4.21	Hybrid SOFC-GT system to be used in long-haul locomotive	198
4 22	Hybrid SOFC-GT system to be applied in long-haul locomotive engine	200
4 23	Fuel Cell Assembly to be used in long-haul locomotive	200
4 24	Heat Exchangers for Fuel Preheater	200
4 25	Heat Exchangers for Recuperator	202
4.26	Fuel Cell Stack to be used in long-haul locomotive	202
4.20	Reformer to be used in long-haul locomotive	202
4.27		203
5.1	Bloomenergy fuel cell to be used in a small scale prototype of hybrid SOFC-	
	GT system	205
5.2	Versa 400 kW Current Simulation	205
5.3	Versa 400 kW Voltage Simulation	206
5.4	Versa 400 kW Oxygen utilization Simulation	206
5.5	200 kW capstone microturbine to be used in a small scale prototype of hybrid	
	SOFC-GT system	207
5.6	Pressure response for 500 kW small scale system	208
5.7	Pressure distribution on impeller for 500 kW small scale system at $T = 7,000s$	3209
5.8	Velocity distribution on impeller for 500 kW small scale system at $T = 7,000s$	3209
59	Velocity development on the impeller blades $T = 7000(s)$	210
5 10	Velocity vectors on the impeller inlet	211
5 11	Pressure reduction in the diffuser connected to the impeller outlet $T = 7000(s)$	212
5.12	Impeller outlet velocity and flow rate increase $T = 7000(s)$	213
5 13	The velocity distribution over impellers at $T=3000s$	213
5 14	1st Impeller velocity distribution from LE to TE	215
5 1 5	Pressure variation at $T = 3000(s)$ on diffuser	216
5 16	Impeller outlet velocity reduction at time 3000 (s)	217
5 17	Mass Flow Rate results at $t=3000$ (s) and $t=7000$ (s)	218
5.17	$\frac{1}{1000} + \frac{1}{1000} + 1$	210
6.1	Bakersfield-Mojave Route, Source: Google Earth	221
6.2	Power Duty Cycle of a 1 MW switcher locomotive	223

6.3	Power Duty Cycle of a 3 MW switcher locomotive	223
6.4	Optimal Parametric Study of Fuel Cell Stack	225
6.5	Stack temperature difference with variation of power density and fuel uti-	
	lization	226
6.6	voltage variation at different fuel utilizations and steam to carbon ratio	227
6.7	Stack temperature difference at different oxygen and fuel utilizations	228
6.8	Prototype design of a 1 MW switcher locomotive	232
6.9	Vehicle and Notching dynamic modeling	232
6.10	Notching algorithm	234
6.11	Vehicle dynamics algorithm implementation	235
6.12	Notching dynamics over Bakersfield-Mojave Route	235
6.13	Power Dynamics over Bakersfield-Mojave Route	236
6.14	Acceleration dynamics over Bakersfield-Mojave Route	236
6.15	Speed dynamics over Bakersfield-Mojave Route	236
6.16	Speed dynamics over Bakersfield-Mojave Route	237
6.17	Speed dynamics over Bakersfield-Mojave Route	237
6.18	Fuel cell power Density variation with fuel utilization and time	238
6.19	Fuel cell power Density variation with fuel utilization and cathode outlet	
	temperature	239
6.20	Fuel Cell Power Density data over Bakersfield-Mojave route	240
6.21	Interactive plot of fuel Cell Power Density data, and fuel cell efficiency over	
	Bakersfield-Mojave route	240

### LIST OF TABLES

#### Page 2.1Results from U.S. Department of Energy hybrid systems studies in 1998 [128] 22 2.2 Reformation model constants used by Brouwer et al. [30] . . . . . . . . 50 2.3 Several studied hybrid system efficiencies 56 2.4 64 2.5 94 2.6 96 2.7 116 2.8 System operating specifications and resulting system performance [64] . . . 117 2.9 Hybrid system simulation parameters of Calise et al. [72] . . . . . . . . 119 4.1 184 4.2 Set of equations used for economic analysis of SOFC-GT system . . . . 188 4.3 189 4.4 189 4.5 193 4.6 SOFC-GT locomotive stages of development 194 4.7 Hybrid system component costs 195 4.8 196 6.1 222

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### **CURRICULUM VITAE**

### Mohammad Ali Azizi

#### **EDUCATION**

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GPA: 3.98/4.00		
MS in Mechanical & Aerospace Engineering	2014	
University of California, Irvine	Irvine, CA	
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BS Mechanical Engineering	2012	
Sharif University of Technology	Tehran, Iran	

#### WORK & RESEARCH EXPERIENCE

#### • Graduate Student Researcher

Advanced Power and Energy Program (APEP), UCI; Irvine CA Jan 2014 - 2018 M.S. thesis: - Conducted simulation of high temperature Solid Oxide fuel cell and methane hydrate in deep ocean sediments and assessed the feasibility of methane production using novel high energy efficiency extraction method.

-Multiphase analytical model of water-methane gas dissociation has been developed in MATLAB code.

#### Ph.D. research:

- Cost Estimation of the first hybrid fuel cell- gas turbine system locomotive system - Parametric Study and Optimization of SOFC-GT system in R - Developed High efficiency solid oxide fuel cells (SOFC) software in MATLAB/Simulink.

- Developed full dynamic model of locomotive (powertrain).

- Conducting dynamic simulation of high efficiency SOFC - gas turbine hybrid system for locomotive and stationary applications and assessing the feasibility of such system for distributed generation. In addition, the feasibility of unprecedented hybrid SOFC and ICE is a main topic of the Ph.D research. Computational fluid dynamics (CFD) analysis has been conducted to capture the detail fluid dynamic behavior in transient hybrid system performances.

- Turbomachinery compressor blade design and mesh sensitivity analysis (Using structured and unstructured mesh) for compressor diffuser and impellers. - Hybrid SOFC-GT locomotive system sizing using dynamic model tools of MAT-LAB/Simulink. Several heat exchangers have been sized used ASPEN software modules (HTRI Xchanger Suite).

- Runnging dynamic model of locomotive hybrid system on an elevated path (Bakersfield-Mojave).

- Developed powertrain system for hybid SOFC-GT locomotive system (Locomotive Notching algorithm) in MATLAB/Simulink Platform.

- Leading a hybrid fuel cell-gas turbine locomotive engine research group. Providing quarterly and annual reports for companies, agencies and organizations such as Federal Rail Road Administration, U.S. Department of Energy, U.S. EPA, California Air Resources Board, and South Coast Air Quality Management. District

• Reviewer of ASME Journal of Electrochemical Energy Conversion. 2017

*Work Experience*: *Reviewed a paper with a topic on Hybrid Solid Oxide Fuel Cell Gas Turbine Control at ASME Journal written By National Energy Technology Laboratory (NETL)* 

#### • Controls Engineering Intern

**Bloom Energy**; Sunnyvale CA Jul 2016 - Sep 2016 *Work Experience*: Performed controls (PID) engineering on Bloom Energy Solid Oxide fuel cell systems, Real Time Data Analysis using statistical software (R) and machine learning tools, Performed test measurements using Human Machine Interface (HMI), Developed control codes in MATLAB in interaction with main controller via Python code and optimization of process design.

- Graduate Student Researcher
  National Fuel Cell Research Center (NFCRC), UCI; Irvine CA Jan 2014 2018
- Research Assistant Mechanical & Aerospace Eng. Department, UCI; Irvine CA Jan 2013 - 2018
- Intern Tehran Oil Refining Company, Baghershahr, Iran Summer 2010
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Finite element modeling of facial muscles, **Sharif University of Technology**, Tehran, Iran 2012

#### • B.S thesis research

Micro robot localization using IMU and optic sensors (BS thesis), **Sharif University** of **Technology**, Tehran, Iran 2012 Conducted research on micro robot localization under supervision of Prof. G.R. Vossoughi. Our goal was to increase the localization accuracy by fusing IMU sensor and optical sensors using Kalman Filtering.

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Applied Electronics Laboratory, Mechanical Engineering School, **Sharif University of Technology**, Tehran, Iran 2012 *Building Micro Robots using IMUs; Introductory knowledge of Kalman Filtering* 

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Fluid Mechanics Laboratory, Mechanical Engineering School, Sharif University of<br/>Technology, Tehran, Iran2008-2009Experimented on muddy fluids with high Reynold numbers2008-2009

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#### **TEACHING EXPERIENCE**

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 Fluid Mechanics (MAE 130B)
 Thermal & Fluid Lab (MAE 107)
 Air Quality and Polution control (MAE 164)

#### JOURNAL PUBLICATIONS

- Azizi, Mohammad Ali, and Jacob Brouwer. "Stall/surge dynamics of a multi-stage air compressor in response to a load transient of a hybrid solid oxide fuel cell-gas turbine system". Journal of Power Sources, Volume 365, 15 October 2017, Pages 408418 (Citations:1)
- Azizi, Mohammad Ali, and Jacob Brouwer. "Transient Analysis of 220 kW Solid Oxide Fuel Cell-Gas Turbine Hybrid System Using Computational Fluid Dynamics Results." ECS Transactions 71.1 (2016): 289-301. (Citations:2)
- Azizi, Mohammad Ali, Jacob Brouwer, and Derek Dunn-Rankin. "Analytical investigation of high temperature 1kW solid oxide fuel cell system feasibility in methane hydrate recovery and deep ocean power generation." Applied Energy 179 (2016): 909-928. (Citations: 7)
- Azizi, Mohammad Ali, and Jacob Brouwer. "Progress in solid oxide fuel cell-gas turbine hybrid power systems: System design and analysis, transient operation, controls and optimization." Applied Energy 215 (2018): 237-289.

#### **CONFERENCE PUBLICATIONS**

- M. Azizi, J. Brouwer. Mitigation of compressor stall/surge in a hybrid solid oxide fuel cell-gas turbine system , 4th International SYMPOSIUM on Solid Oxide Fuel Cells (SOFC): Materials, Science and Technology: System design and demonstration*Jan* 22-27, 2017; Daytona Beach, FL.
- M. Azizi, J. Brouwer. 4 MW locomotive hybrid solid oxide fuel cell-gas turbine system dynamic modeling using computational fluid dynamics results, ASME Power & Energy Conference. *June 26- 30, 2016; Charlotte, NC.*
- M. Azizi, J. Brouwer. Design and sizing of a 4 MW hybrid solid oxide fuel cell- gas turbine engine for long haul locomotive operation, ASME Power & Energy Conference. *June 26- 30, 2016; Charlotte, NC.*

#### **POSTER PRESENTATIONS**

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- M. Ali Azizi, J. Brouwer. Powertrain Performance of Solid Oxide Fuel Cell- Gas Turbine Hybrid Engine in long-haul and Test scale locomotive, *to be submitted to Journal of Power Sources*, 2017.
- M. Ali Azizi, J. Brouwer. System sizing and feasibily analysis of long-haul Solid Oxide Fuel Cell Gas Turbine Hybrid Engine, to be submitted to Journal Applied Energy, 2017.

#### SOFTWARE

*Technical:* MATLAB/Simulink, ANSYS (CFX, FLUENT, TurboGrid, Mechanical), Solid-Works, COMSOL, OpenFOAM, Tecplot, R, Python, FORTRAN, Illustrator, T<sub>E</sub>X, LAT<sub>E</sub>X, MS Office; Familiar with: LabVIEW *Languages:* English, Persian.

#### REFERENCES

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### **ABSTRACT OF THE DISSERTATION**

Solid Oxide Fuel Cell-Gas Turbine Hybrid Power Systems: Energy Analysis, Control Assessments, Fluid Dynamics Analysis and Dynamic Modeling for Stationary and Transportation Applications

By

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This research presents a system design and analysis, and transient *control* and optimization of solid oxide fuel cell-gas turbine (SOFC-GT) hybrid systems. The main features of SOFC-GT power systems include high efficiency, virtually zero emission of criteria pollutants, and low acoustic signature compared to conventional power production technologies. Focus of this dissertation is the investigation of control strategies and transient performance characteristics of hybrid SOFC-GT systems, using computational fluid dynamics methods.

A novel control system is developed for a SOFC-GT system to follow dynamic power demands associated with locomotives while keeping all of the components and system operating variables within acceptable limits of performance. The voltage variation is also greater at lower fuel utilization. The stack temperature difference is highly dynamic at low fuel utilization. In addition, detailed analyses of potential SOFC-GT locomotive production and operation costs in comparison to other low pollutant emitting alternatives is accomplished. SOFC-GT locomotives are projected to produce lower operating costs compared to the catenary-electric alternative, and significantly lower operating costs compared to the battery-electric alternative. A part of this research is devoted to a better understanding of turbulent unsteady flows in gas turbine systems that is necessary to design and control compressors for hybrid fuel cellgas turbine (FC-GT) systems. In this study, compressor stall/surge analysis for a 4 MW locomotive hybrid solid oxide fuel cell-gas turbine (SOFC-GT) engine is performed based on a 1.7 MW multi-stage air compressor similar to available commercial compressors. Control strategies are designed and evaluated to prevent the operation of hybrid SOFC-GT beyond the stall/surge lines of the compressor. Computational fluid dynamics (CFD) tools are used to provide a better understanding of flow distribution and instabilities near the stall/surge line. Simulation results show the feasibility of using existing industrial compressors in the hybrid SOFC-GT system operation. The results show that a 1.7 MW system compressor like that of Kawasaki gas turbine is an appropriate choice among the industrial compressors to be used in a 4 MW locomotive SOFC-GT with topping cycle design.

# CHAPTER 1

## INTRODUCTION AND BACKGROUND

#### **1.1** INTRODUCTION

Solid oxide fuel cells (SOFC) are electrochemical devices that convert chemical energy contained in fuel directly into electricity through electrochemical reactions. The SOFC electrochemical reactions occur at relatively high temperatures compared to the other types of fuel cells. The higher temperature operation allows for fuel flexibility. SOFCs can operate on natural gas, hydrogen, biogasses, coal syngas and high temperature also lends itself well to cogeneration schemes which can significantly increase the system efficiency.

#### 1.1.1 EMERGENCE OF SOFC POWER PLANTS

SOFC power plants are a proven clean-tech alternative for electric utility power generation in residential, commercial and industrial applications. SOFCs lend themselves well to stationary power and also to heavy duty transportation (e.g., locomotive) applications [1, 2, 3, 4, 5, 6, 7, 8].

Features of SOFC power systems include production of less harmful chemical and acoustic

emissions at higher efficiencies compared to conventional power production technologies [9, 10, 11, 12]. An electrolyte that is most typically made of yttria-stabilized zirconia (YSZ), eliminates the need to manage the electrolyte evaporation and circulation associated with other non-solid-state fuel cell types. As a result of high operating temperature and oxidizing ion charge carrier (oxygen ion,  $O^{=}$ ), higher fuel flexibility is achievable compared to other types of fuel cells. SOFCs are capable of converting carbon monoxide (CO) to electricity via electrochemical reaction [13], while other types of fuel cells such as proton exchange membrane fuel cells (PEMFC) are vulnerable to CO poisoning [14]. SOFC systems have operated using various types of fuels such as carbon monoxide (CO), natural gas, hydrogen  $(H_2)$ , propane  $(C_3H_8)$ , landfill gas, diesel and JP-8 [15, 16, 17, 18]. Typically, the operating temperature of SOFC is higher than other types of fuel cells such as PEMFC, alkaline fuel cells (AFC), phosphoric acid fuel cells (PAFC), and molten carbonate fuel cells (MCFC) [19, 20]. Higher operating temperature of SOFCs and the presence of nickel catalayst enable them to directly reform natural gas in the anode compartment. SOFC systems convert reformed hydrogen and other gaseous fuel species (e.g., CO) usually produce by reformation of a hydrocarbon fuel through electrochemical reactions that produce electrical power and high grade heat for use elsewhere in the system (e.g., reformation, preheating reactants) and for combined heat and power (CHP) applications. The need for more costly materials construction and insulation that can withstand the high temperature conditions is a disadvantage. Nonetheless, fully integrated SOFC power generation systems have built and operated as stationary power systems in multiple applications in the power production range of 1 kW to 20 MW [21, 22].

Several designs of SOFC systems have been experimentally evaluated and demonstrated todate. The typical configurations of SOFC cells include tubular, planar and monolithic [23]. Each of these cell configurations has advantages and disadvantages regarding the thermal shock resistance, manufacturability, power density and potential cost [24]. Among these, the

tubular SOFC design has been manufactured by Siemens Westinghouse Power Corporation, Mitsubishi Heavy Industries, Rolls Royce and LG Fuel Cells Systems, Artex Energy, and others [25, 26, 27, 28]. Monolithic SOFC cell designs have been primarily produced for research and development purposes. By far the most popular type of cell configuration in recent systems is the planar design used by most fuel cell system manufacturers including Bloom Energy, Versa Power, FuelCell Energy, Ceres Power, SolidPower, and many others. More than 100 companies are producing SOFC systems mostly in the U.S., Europe and Japan. The most prominent manufacturer of SOFC systems in the U.S. is Bloom Energy. The typical materials set used in SOFC cells and stacks is remarkably durable and robust even over long periods of time operating at high temperature. For example, the tubular SOFC design of Siemens Westinghouse Power Corporation has shown more than 85,000 hours of operation with low cell degradation and the planar SOFC design has shown power densities up to  $1000 \left(\frac{W}{I}\right)$  [29, 30]. The initial market for the fuel cells is currently limited to areas with strict emission regulations, or where grid electric power is more expensive than the on site power and heat production [31]. The current high capital cost of such fuel cell systems is the main reason that SOFC technology has not become more widely deployed and such capital costs are currently being reduced and also have a significant potential for being reduced.

The SOFC-microturbine hybrid systems are also being considered in auxiliary power units (APU) in commercial airplanes to provide power to all electrical loads [32]. In recent years, the application of SOFC systems has been expanded to deep ocean power generation for methane hydrate recovery [33]. Aguiar et al. developed a High-altitude long-endurance (HALE) hybrid system for UAVs [34]. The overall system efficiency was at 66.3% (LHV) when operating on liquefied hydrogen for a three-stack system. Rajashekara et al., classified hybrid systems into two major types: 1) A high temperature fuel cell combined with other power generation systems such as reciprocating engine, and 2) The combination of fuel cell with wind plant and/or and solar power. Microturbines and gas turbines are being developed in the range of 30 kW to 30 MW and 100 -1000 MW, respectively [19]. In another study by the same group, a 440 kW hybrid system was developed to be used in commercial aircraft, cruise ships and trains. The system had the capability to operate in distributed power generation systems [35]. Chinda et al. presented a model of hybrid systems aimed for a 300-passenger commercial aircraft electrical power unit [36]. The components in the system were sized to meet the 440 kW input electrical load at the sea level full power condition. The parameters that limited the hybrid system performance were the SOFC temperature, TIT, and the exhaust temperature.

### **1.2 GOAL AND OBJECTIVES**

#### 1.2.1 GOAL

Develop understanding of dynamic operation and control of hybrid solid oxide fuel cell gas turbine (SOFC-GT) systems for the design and application to locomotive applications.

#### 1.2.2 Objectives

i. Conduct a thorough literature review on the system design and analysis, transient operation, controls and optimization of solid oxide fuel cell - gas turbine hybrid power systems

ii. Develop and apply a computational fluid dynamic (CFD) approach to better understand the stall-surge dynamics of turbomachinery for SOFC- GT systems

iii. Develop a design for a hybrid SOFC-GT system for locomotive applications and analyze the spatial fitness for the hybrid system for locomotive applications

iv. Apply the CFD approach to the locomotive SOFC-GT system turbomachinery de-

4

sign for analysis of stall-surge

v. Investigate the dynamic behavior and control strategies for locomotive application of hybrid SOFC-GT technology

## CHAPTER 2

## LITERATURE REVIEW

### 2.1 SOFC-GT HYBRID SYSTEM BACKGROUND

Climate change, due to increasing greenhouse gas emissions and reduction in the availability of fossil energy resources, have motivated the gas turbine industry to consider more energy efficient strategies with reduced emissions for stationary power plants. Hybrid fuel cell-gas turbine (FC-GT) systems provide clean energy at high efficiency [37]. FC-GT hybrid power systems theoretically possess the highest efficiency and the cleanest emissions of all fossil fueled power plants in any given size class [38]. Integrated hybrid systems have the potential to operate at higher efficiency than a fuel cell or gas turbine alone. A market study by Research Dynamics Corporation concluded that hybrid systems could compete on electricity cost with other distributed generation (DG) technologies [30]. Technical elements of various SOFC-GT hybrid systems have been published by the ASME International Gas Turbine Institute (IGTI) proceedings including several purposeful hybrid sessions ([39, 40, 41, 42, 43, 44, 45, 46]). SOFC-GT hybrid systems have been called one of the most promising technologies to meet US DOE demands for high efficiency and low emissions power generation [47]: 1) To achieve a higher electrical efficiency, 2) to minimize

environmental pollution, 3) to produce electricity at a competitive cost, and 4) to capture and sequester  $CO_2$ .

In recent years, many hybrid systems have been mentioned in several US patents [48, 49, 50, 51, 52, 53, 54, 55, 56, 57, 58]. The integration of an SOFC stack with a gas turbine has been proven to be a promising concept, since SOFC-GT hybrid systems can achieve a net electrical efficiency and a global efficiency close to 70% and 85%, respectively [59, 60, 61, 62, 63]. Many researchers have accomplished fundamental studies concerning SOFC-GT hybrid systems [64, 65, 66, 67]. Some of them performed thermodynamic analyses of hybrid systems [64, 65, 66, 68]. In addition, exergy analyses of hybrid systems were performed by several authors [69, 70, 71, 72, 73, 74, 75, 76, 77, 78, 79]. In a study by Calise et al., a maximum electrical efficiency of 65.4% was achieved at the full-load operation [70]. Analyses demonstrated that a combined SOFC-GT system could achieve fuel to electricity conversion efficiencies at 65% to 74% for systems under 10 MW, and greater than 75% for larger systems [30, 80, 81, 82, 83, 84]. As fuel cell technology advances, SOFC systems could possibly tolerate higher pressures so that they could be integrated into even more sophisticated hybrid systems with gas turbines characterized by higher pressure ratios and higher turbine inlet temperature (TIT).

In 1999, Rolls Royce funded a study to produce a turbo-generator that was estimated to cost approximately \$400 per kW in full production [27, 30]. When coupled with fuel cells, the turbine could produce 25% of the hybrid system power in the 1 MW to 5 MW class. As a stand-alone device, the turbine could produce 1.5 MW of electric power in a simple cycle mode. In a stand-alone mode, efficiency of the gas turbine system at this scale is approximately 33%. In addition to the stationary power applications of SOFC-GT hybrid systems, they could be useful in supporting the auxiliary and propulsion power needed for the locomotive and mobile applications, ships, aircraft and spacecraft [85, 3, 4, 86, 35, 87, 88, 89, 90]. Since SOFCs operate at high temperatures, hybrid systems are able to operate using various

types of fuels such as natural gas, coal, biomass and other fossil fuels [30, 91, 92, 93, 94]. Using simulation and experimental methods, it was demonstrated that an SOFC can achieve a 50% net electrical efficiency [95]. Thermodynamic analyses have shown that integration of SOFC into multi-kW and multi-MW gas turbine engines in order to achieve higher electrical efficiencies is feasible [10, 96, 30]. The efficiencies of a gas turbine system, a high temperature fuel cell system and a hybrid system have been reported to be approximately 35%, 50% and 70% respectively [97]. Additional analyses on hybrid systems have been performed by the U.S. Department of Energy (DOE) with industry cooperation from FuelCell Energy, General Electric (formerly Honeywell), and Siemens Power Corporation (formerly Siemens Westinghouse) [98, 99, 29, 30, 84]. All of these analysis projects were accomplished for hybrid system designs less than a MW class showing that efficiencies greater than 65% were possible even in this small size class.

## 2.1.1 EXPERIMENTAL EVALUATION OF INTEGRATED SOFC-GT HYBRID SYSTEMS

Experimental evaluation of hybrid FC-GT technologies has been supported by the U.S. DOE. A hybrid system was integrated and tested in the 2004 timeframe that consisted of a 250 kW fuel cell stack and a 30 kW Capstone MTG configured as an indirect bottoming cycle [2]. Experimental data of the Capstone GT C30 have also been used in an SOFC-GT hybrid model [100]. The results of the simulation have been compared to the Capstone C30 for a load step from 30 to 20 kW. In addition, FuelCell Energy designed a 40 MW DFC/T hybrid system [98].

The Siemens Power Corporation 220 kWe PSOFC/MTG produced with Ingersoll-Rand was a hybrid design that was tested at the National Fuel Cell Center (NFCRC) at the University of California, Irvine [101] in the 1999-2003 timeframe. This system comprised the first hybrid SOFC-GT system ever constructed and tested, achieving a fuel-to-electrical conversion

efficiency of 53%. The test included pressurization of the fuel cell in order to provide a net power of 220 kW from the hybrid system. Matching pressure ratios and mass flows were a-mong the technical challenges of the hybrid systems. The test included pressurization of the fuel cell in order to provide a net power of 220 kW from the hybrid system. Since the system was comprised of an existing SOFC module that was integrated with an existing MTG, matching air mass flows and balancing pressure and temperature distribution requirements were among the technical challenges of the hybrid system.

Recently a prototype of 250 kW hybrid SOFC-MGT has been demonstrated by Mitsubishi Heavy Industries in Tokyo Gas Senju Techno Station. The system was stable without voltage degradation for 4100 hours. Fig. (2.1) shows the corresponding system [102].



Figure 2.1: 250 kW prototype of hybrid SOFC-MGT system [102]

Fig. (2.2) shows the operational plot of the corresponding hybrid SOFC-MGT system [102].



Figure 2.2: Long term operation test of the SOFC-MGT system [102]

#### 2.1.2 EXPERIMENTAL TEST FACILITIES FOR HYBRID SYSTEMS

Larosa et al., they investigated a micro gas turbine coupled with a large volume [103]. Such a system is called an "emulator". Hybrid system emulators are integrated and fully functional experimental systems that comprise various parts of a complete hybrid fuel cell gas turbine system with some component or components not present (usually the fuel cell stack is not present), but emulated to account for the effects of that component or components. Such hybrid system emulators can be very helpful in solving integration and control issues associated with fully integrated hybrid fuel cell gas turbine systems. Some research institutes have developed hybrid system emulators, which represent the layout and behavior of real-coupled SOFC-GT power plants, including a micro gas turbine, a real-time fuel cell simulator, and all of the necessary coupling elements and control systems hardware and software. Fig. (2.3) shows the emulators installed in different locations around the world. In particular, the National Energy Technology Laboratory (NETL) of the U.S. Department of Energy, the Thermochemical Power Group of the University of Genoa, and the Institute of Combustion Technology of the German Aerospace Center (DLR) are leading researchers who have each developed and operated experimental test facilities (see Fig. (2.3)).



Figure 2.3: Emulator test rigs: NETL, University of Genoa and DLR laboratories [103]

The experimental facilities developed and operated by NETL are dubbed the HyPer facility. A model predictive control fuel cell/gas turbine hybrid system was also studied by Restrepo et al. based on the experimental data collected on the HyPer facility installed at NETL [104]. In that study, the three main phases of the MPC, identification of the models, control design, and control tuning have been described. One drawback in MPC implementation is the computational time consuming between calculations that made it difficult to apply experimentally [105].



Figure 2.4: Block diagram of HyPer MPC control application [104]

Fig. (2.4) shows the MIMO (Multi-input Multi-output) MPC controller. The MIMO system selected in this work consists of a non-square system of four inputs and two outputs. The

manipulated variables or actuators, (u), in the facility were controlled by the three valves CA, BA, HA, and the electric load. Y represents the output of the system which are turbine speed, the cathode air mass flow and the cathode inlet temperature.

Harun et al. studied the impact of fuel composition transients on SOFC performance in a gas turbine hybrid system [106]. In once study by Harun et al., both open loop and closed loop transient responses of the fuel cell in a solid oxide fuel cell (SOFC) gas turbine (GT) hybrid system to fuel composition changes were experimentally investigated using a cyber-physical fuel cell system [107]. Zaccaria et al. developed a transfer function for SOFC-GT hybrid systems control using cold air bypass [108]. Their tests were performed moving the cold air valve from the nominal position of 40% with a step of 15% up and down while the system was in open loop; without control on turbine speed or inlet temperature. Transfer functions were developed for cathode mass flow, total pressure drop and surge margin. All the system dynamics were approximated as First Order Plus Dead Time (FOPDT) transfer function.

In another study by Zaccaria et al., the gains of the PI controller were determined using a pole placement method. The proportional and integral gains were found to be 0.5 and 0.0035. Control strategies were investigated in order to minimize the degradation effects on the system performance [109]. The results showed that it was possible to maintain a constant voltage while the fuel cell was degrading, reducing the degradation rate over time. In a standalone fuel cell, in order to keep the power constant as the voltage degraded, the current was increased which increased the degradation rate with time. In a hybrid system, the total power output could be maintained constant increasing the turbine load; i.e. the fuel flow to the system. PID controllers were implemented in order to keep the temperature difference constant by manipulating the airflow, while the average temperature of the cell was maintained constant by manipulating the fuel flow of the pre-heating combustor [110]. In one study by Zaccaria et al., a control strategy was implemented in order to keep constant cathode inlet temperature during different operative conditions [109].

Emami et al. analyzed the performance of a 300 kW SOFC-GT pilot power plant simulator using a set of robust PID controllers that satisfy time delay and gain uncertainties of the hybrid system [111]. Fuel cell mass flow rate  $\dot{m}$  and turbine speed  $\omega$  were the controller outputs. Fig. (2.5) shows the MIMO controller design for this study.



Figure 2.5: MIMO controller of hybrid SOFC-GT system [111]

In another study by the same group, operating points of the 300 kW system were estimated using the Multiple Model Adaptive Estimation (MMAE) algorithm [112]. Fig. (2.6) shows the Predictive type KF algorithm used in that study. The figure shows the discrete space-state model followed by the discrete KF.



Figure 2.6: Prediction Type Kalman Filter (PTKF) [112]

Air flow control in the hybrid system was performed using the Hyper hardware simulation facility at NETL [113]. Fig. (2.7) shows the plant flow diagram of this study.



Figure 2.7: Simplified flow diagram of hybrid simulation facility at NETL [113]

Thermal management of a hybrid SOFC-GT system was studied by Zhou et al. using the same Hyper facility at NETL [114]. Responses of the physical subsystem and virtual subsystem to various disturbances were studied. In addition, multi-objective neural network
controller of SOFC-GT hybrid system has been developed by Colby et al. of the same group [115]. A computationally efficient plant simulator was developed based upon physical plant data, that allows rapid fitness assignment. In a study by Harun et al., also of the same group, dynamic performance of a SOFC-GT hybrid system in response to a sudden fuel composition change has been investigated experimentally for both open and closed loop operation [116]. A load based speed control scheme was used in the closed loop test to maintain the turbine speed at 40,500 rpm. Fig. (2.8) shows this control strategy.



Figure 2.8: Load based speed control strategy [116]

Tucker et al. provide details of their Hyper facility and results from cold flow testing accomplished in the facility that was constructed at the NETL [117]. They note that the Hyper facility can experimentally analyze the transient performance dynamics of FC-GT systems [117]. The SOFC-GT test facility was developed at the U.S. DOE NETL in Morgantown, WV as part of the Hyper facility. In order to simulate the thermal output of the SOFC, a natural gas burner controlled by a real-time fuel cell model to predict FC heat (and electricity) production was used. The turbine inertia and viscous drags were determined during the startup conditions for the turbomachinery. The turbine speed for the startup was not significantly affected by the reduction in the amount of energy available to the turbine through the system volume [117]. The facility uses hardware-in-the-loop to simulate the coupled SOFC operation with gas turbine hardware. The SOFC operation was characterized over an extensive range of operation including inert heating and cooling, standard on-design and extreme off-design conditions. The average operating temperature and spatial gradient profile in the simulated SOFC increased due to a step increase in the load [118]. Zhou et al., working with the same NETL group, developed a transfer function to control the cathode airflow in a hybrid SOFC-GT system [119]. The inputs of the hardware system where compressor intake and fuel flow. The fuel flow was controlled by a PID controller to maintain the turbine speed at the nominal speed. An Atlas control system, manufactured by Woodward industrial controls, was used to control a Swift valve (FV-432) that manipulated fuel flow to the system combustor [113]. Turbine rotational speed was controlled using a PID controller demand for the fuel valve using feedback from a optical speed instrument (ST-502). Other bypass valves were also controlled by independent Atlas controllers.

The Thermochemical Power Group (TPG) built at the laboratory of the University of Genoa, Italy, a new high temperature fuel cell - micro gas turbine physical emulator based on commercial machine technology [120]. The focus of the study was on the critical phases of start-up, shutdown and load changes. Fig. (2.9) shows the T100 power module modifications for the fuel cell coupling.



Figure 2.9: The T100 power module modifications for the fuel cell coupling [120]

Fig. (2.10) shows the test rig plant layout of the system built by the Thermochemical Power Group (TPG) in their laboratory at the University of Genoa, Italy.



Figure 2.10: Test rig plant layout: the blue box is related to the SOFC model [121]

Hohloch et al. accomplished experimental analysis of a hybrid SOFC-GT system [122]. The power plant operated at different MGT speeds and SOFC electrical power outputs leading to different SOFC temperatures. Fig. (2.11) shows the hybrid cycle schematic. Fig. (2.12) shows the transient behavior of MGT with temperature variation at the gas preheater. Fig. (2.13) shows the test rig at the German Aerospace Center (DLR) where this study was accomplished.

# CYCLE ARRANGEMENT



Figure 2.11: Hybrid cycle design [122]



Figure 2.12: Transient behavior of MGT with temperature variation at gas preheater [122]



Figure 2.13: Hybrid power plant test rig at DLR [122]

Relative high pressure losses have been reported by researchers at DLR for transient operation of the MGT in hybrid configurations. However, the relative pressure loss was not reported as an indication of instability in the hybrid system. The absolute value of pressure was reported to change with changing preheating temperature. Comparing simulation data with measurement data from the DLR Turbec T100 test rig has led to extensions of the numeric models, on the one hand, and to modifications of the test rig on the other [123]. Lai et al. used two combustors in their experimental setup (Comb A and Comb B) to simulate the high temperature exhaust gas of the SOFC and the condition of the sequential burner [124].

# 2.1.3 GAS TURBINE TECHNOLOGY APPLICATIONS IN SOFC-GT HY-BRID SYSTEMS

Several conventional heat engines have been considered for integration with SOFCs, such as the SOFC-GT hybrid cycle. These include gas turbines, steam turbines and reciprocating engines [19]. The only engines that have been previously tested as an integrated hybrid system with SOFC have been micro-gas turbine generators (MTG). The micro turbine generator has showed promise when integrated with a high temperature SOFC. Among the features that allow the integration of MTG and SOFC, the following were mentioned by Brouwer [30]: 1) the SOFC exhaust temperature and MTG turbine inlet temperature are well-matched; 2) MTGs operate at relatively lower pressure ratios that makes the integration easier; 3) MTGs often use recuperation in order to improve the system efficiency, which well-suits hybrid system integration; 4) MTGs allow fuel cells to operate under higher pressures which improves the cell performance; 5) The thermal energy contained in the SOFC exhaust is sufficient to provide the necessary energy for the MTG components such as the compressor (for fuel cell pressurization) and electric generator (produces additional electricity); and 6) The size of current fuel cell systems match well with the current size of MTGs.

# 2.2 HYBRID SOFC-GT SYSTEM DESIGN CONCEPTS

In 1998, the U.S. DOE Office of Fossil Energy started five studies to evaluate variations of the parameters on the FC-T hybrid concept. These studies included MCFCs, SOFCs, off-the-shelf turbines and conceptual turbines [125, 126, 127, 81, 30]. Four of these cycles were associated with hybrid systems in a power class of 20 MW. The fifth study evaluated them under a MW class. The results of these studies are briefly shown in Table .(2.1). The SOFC-GT hybrid systems concept was first patented in the mid 1970s. By 1998 more than ten hybrid concepts were patented using different types of fuel cells, operating pressures, and system configurations. The basic concept of an SOFC-GT hybrid system is demonstrated in

Fig. (2.14).

Company	FuelCell En-	Siemens	Siemens	M-C Power	McDermott
	ergy	Westinghouse	Westinghouse		
Cycle configuration	MCFC Indi-	SOFC Tur-	Staged SOFC	MCFC	SOFC
	rect	bine Bottom-	Turbine Bot-	Turbine	Indirect
		ing	toming	Bottoming	
Normal Size	20 MW	20 MW	20 MW	20 MW	750 kW
Efficiency	71%	60%	67-70%	66-70%	71%

Table 2.1: Results from U.S. Department of Energy hybrid systems studies in 1998 [128]



Figure 2.14: Basic concept of a fuel cell-gas turbine hybrid system [129]

MCFC and SOFC hybrid systems have been manufactured and operated with reduced emissions at high efficiencies [130, 29]. The primary design concepts for SOFC-GT hybrid systems are as follows [30]: 1) Most of the electricity (approximately 80% of the net generated electricity) is generated through the electrochemical reaction in the SOFC cells, 2) The high pressure produced by the gas turbine is used to improve the cell performance, 3) The high quality heat contained in the SOFC exit gases is used in other components of the hybrid system (e.g., fuel processing, reactant stream preheating), and 4) The remaining heat is converted to compressor power and additional electricity (through a generator). McLarty et al., studied both MCFC and SOFC technology for hybridization with micro-turbines and the larger axial flow gas turbines at steady state [131]. Their study used off-design performance maps produced from the detailed, spatially resolved component models. In the case of no recirculation, the specific fuel cell heating and the specific combustion heating had to match. In addition, the absolute flow rates of the turbine and the fuel cell had to match accurately [131].

### 2.2.1 HYBRID SYSTEM CONFIGURATIONS

Hybrid system configurations are discussed by Buonomano et al. in detail [132]. In general, two common configurations are used in the hybrid FC-GT systems based on the order of components in the hybrid cycle [2, 30]. A fuel cell topping cycle is one in which the energy conversion to make electricity in the fuel cell occurs upstream from the energy conversion to make electricity in the gas turbine portion of the cycle. The schematic of the topping cycle is shown in Fig. (2.15).



Figure 2.15: Schematic of a direct hybrid gas turbine fuel cell topping cycle [30]

A fuel cell bottoming cycle is one in which the gas turbine turbo-machinery energy conver-

sion to produce electricity occurs upstream of the fuel cell energy conversion in the cycle. Fig. (2.16) demonstrates the bottoming cycle. In a direct cycle configuration, upstream flow is used directly in downstream components of the cycle, and the decoupling heat exchangers are not used. It is worth mentioning that the direct cycle typically has higher efficiency than the indirect hybrid cycle configuration. Indirect cycle configuration uses devices such as heat exchangers to decouple the gas turbine and the fuel cell components so that the flow from upstream components do not directly enter the downstream components.



Figure 2.16: Schematic of an indirect gas turbine fuel cell bottoming cycle [30]

Agnew et al. proposed Rolls-Royce's strategies in order to reduce SOFC-GT hybrid cost [133]. The IP-SOFC stack concept had unique design features allowing for stacks to be manufactured through low cost manufacturing processes and with low inventories of material. In addition, the cycles in that study eliminated the expensive recuperators used in the previous systems. Musa et al. analyzed both the high temperature (HT) and intermediate temperature (IT) SOFC performance using Aspen Plus<sup>™</sup> [134]. Two types of combined cycles were compared: 1) Two-staged combination of IT-SOFC and HT SOFC, and 2) Two-staged IT-SOFC. The results showed that the single-staged HT-SOFC and IT-SOFC possessed fuel-to-electricity conversion efficiencies of 57.6% and 62.3 %, respectively. Two-

staged IT-SOFC resulted in a 65.5% fuel-to-electricity conversion efficiency. However, by optimizing the heat recovery and the gas turbine use, this efficiency could be increased to as much as 68.3%. Lundberg et al. presented a conceptual design of 60% efficiency 20 MWeclass PSOFC-ATS-GT HS that integrates Siemens Westinghouese pressurized SOFC and Mercury 50 gas turbine [135]. The system installed cost was estimated \$1170/kWe. While operating on \$3/MMBtu natural gas fuel, it's cost of electricity (COE) was approximately 6% less than the COE of the less efficient and less expensive GT/ST combined cycle system. Saisirirat has studied two different configurations of hybrid SOFC-GT systems [136]. The parameters that limited the cycle performance were found to be SOFC temperature, the turbine inlet temperature and exhaust temperature. The first configuration has been chosen based upon the idea that since combustor exhaust is at high temperature, even the low mass flow rate will be enough to heat the fuel stream to a required temperature. The second configuration is the proposed configuration and the only difference is that here both (fuel and air) the streams are heated by the turbine exhaust. It was shown that configuration 2 had lower steady state performance and configuration 1 gave the better.

Litzinger et al. discussed different configurations of the SOFC-GT hybrid systems [137]. An effective approach was used to fire the GT combustor at a reduced TIT with no change in the GT air intake rate or the SOFC operating point. This reduced the system power output; however, it increased the efficiency. In addition, adding the thermal-trim subsystems increased the net system part-count, complexity and purchase cost from 5% to 15% relative to the ideal-GT system cost. The study concluded that as the SOFC cost decreases, it is preferred to use simpler GT systems and subsystems.

### 2.2.2 INTEGRATION WITH VARIOUS CYCLES

#### INTEGRATION WITH A RANKINE CYCLE

Yan et al. [138] presented an SOFC-GT system integrated with an organic Rankine cycle (ORC) using liquefied natural gas (LNG). The overall electrical efficiency of the system was found to be 67%. Increases in the fuel flow rate increased the net power output; however, the overall electrical efficiency of the system decreased. The compressor pressure ratio increased the overall efficiency. However, increases in the air flow and the S/C had a negative effect on the hybrid system efficiency. Rokni studied a natural gas fed hybrid system in which the SOFC was located on top of the steam turbine [139]. The remaining fuel from the SOFC stacks was combusted in a burner, and the off-gases produced heat for the Rankine cycle. The cycle electrical efficiency was found to be 67%. The SOFC cycle efficiency including the autothermal (ATR) type of reformer was higher than the SOFC cycle with the catalytic partial oxidation (CPO) pre-reformer. Interestingly, however, the hybrid plant efficiency with the CPO reformer was greater than the hybrid plant with the ASR (adiabatic steam reformer). Tuo et al. have conducted a comparative analysis of ORC using different working fluids to recover waste heat from an SOFC-GT hybrid system [140]. The results showed that the actual thermal efficiency of the ORC cycle depends upon the turbine inlet temperature, exhaust gas temperature, and the fluid's critical point temperature. Miyamoto et al. has studied the SOFC triple combined cycle system, integrated with gas turbine (GT) and steam turbine (ST) [102].

Ebrahimi et al., studied a combined SOFC, gas turbine and organic Rankine Cycle to produce power at the 20 kW scale [141]. The overall efficiency was found to be over 65%. Fig. (2.17) shows the corresponding power plant to this study.



Figure 2.17: Schematic of the SOFC-MGT-ORC cycle [141]

Among the six ORC working fluids, toluene, benzene, cyclohexane, cyclopentane, R123 and R245fa, tolouene showed the best thermodynamic performance at favorable hybrid SOFC-GT-organic Rankine cycle system size indicators [142]. Lv et al., studied the mathematical modeling of IT-SOFC-GT hybrid system to study the effects of gasified biomass fuels on the system load characteristics [143, 144]. Choi et al., studied triple power generation system of SOFC-GT-ST [145]. Commercial available F-class and J-class gas turbines were considered in that study. The efficiency of the triple power generation system was shown to be a weak function of the gas turbine class. The efficiency of the F-class based system without carbon capture was slightly over 70%.

#### INTEGRATION WITH GASIFICATION

Jia et al. suggested that an SOFC-GT hybrid system could be integrated with an energy storage unit (e.g., battery) and a dual operating generator/motor G/M [146]. An integrated biomass gasification system with an SOFC-MGT hybrid system has been investigated by

thermodynamic model [147]. Speidel et al., have studied the combination of fermentation and gasification in which dried fermentation waste was converted in a gasifier [148]. Fig.



(2.18) shows the corresponding plant schematic of this process.

Figure 2.18: Process concept of combined fermentation and gasification of sewage sludge [148]

#### INTEGRATION WITH OTHER CYCLES

Integration of an atmospheric solid oxide fuel cell-gas turbine system with reverse osmosis for distributed seawater desalination in a process facility was studied by Eveloy [149]. A hybrid system was studied that included dual fuel cell cycles combined with a gas turbine cycle. The SOFC in question operated at a pressure of 6-15 atms topped the turbine cycle and was used to produce  $CO_2$  for a molten carbonate fuel cell cycle which bottomed the turbine and was operated at atmospheric pressure [150]. Triple combined cycle was predicted to have overall efficiency of more than 75% [151]. An indirect integration of a solid oxide fuel cell, a gas turbine and a domestic water heater was proposed by Mahmoudi [152].

# 2.3 MODELS FOR SOFC-GT HYBRID SYSTEMS

### 2.3.1 EARLY HYBRID SOFC-GT MODEL DEVELOPMENT

Several different model layouts and configurations have been studied before. A review paper by Buonomano [132] has summarized these layouts in detail. Choudhury reviewed the applications of the SOFC technology for power generation [153]. This paper presents a complementary review that focuses upon the transient dynamics and control strategies of hybrid SOFC-GTs system. This section summarizes the previous typical layouts of hybrid SOFC-GT systems.

An early hybrid SOFC-GT power generation system configuration is shown in Fig. (2.19) [64]. The system included an SOFC stack, a combustor, a single spool gas turbine (GT) and a free power turbine (PT), two compressors, two recuperators and an HRSG.



Figure 2.19: Schematic of a recuperated internal-reforming hybrid SOFC-GT system [64]

The mechanical work generated by the gas turbine was used to drive the air compressor. Energy produced by the PT was used for the main application of power generation. During the plant start-up, the electricity required for the air compressor came from the battery or the electric grid. Thus, the power required for the air compressor was considered in calculation of the real system efficiency. Since the range of fuel flow rate was small (up to  $0.044 \frac{kg}{s}$  for the 1.3 MW power plant), a constant fuel compressor efficiency was assumed. Because of the synergistic considerations, the compressed fuel and air were pre-heated in the associated heat exchangers before entering the IR-SOFC stack. Natural gas was internally reformed in the anode compartment. Electrochemical reaction took place at the triple-phase boundary (TPBs) of the anode and the cathode compartments. The high temperature effluent stream of the IR-SOFC was sent to the combustor where the residual fuel (hydrogen, methane and carbon monoxide) reacted with the excess air. The operating temperature of the SOFC was simulated at  $1000^{\circ}C$ , so the exit temperature of the combustor was estimated at  $1200^{\circ}C$ . In that study, a portion of the compressed air was channeled to the combustor in order to reduce the combustor temperature. The produced gas expanded into the turbine to generate mechanical power. The effluent stream of the turbine then was used to preheat the compressed air and fuel through the heat exchangers.



Figure 2.20: Plant layout [72]

Chan et al., performed a study to reduce dependency on experimental data for the plant performance prediction and to extend the code for possible part-load simulation in the future [64]. In another study, Calise's research group [72] studied a hybrid system in which the SOFC stack was based on the tubular technology that was used by Siemens Westinghouse in the 1970s [10]. The steam required for the internal reforming could have been provided by the external heat exchanger (HRSG). Alternatively, it could be provided by recirculating a part of the anode exit steam into the reformer [154, 155, 156, 99, 157]. In the Calise's study, however, the steam was produced in the HRSG by heating up the demineralized water with thermal energy of the fuel heat exchanger exit stream. The gas-fuel heat exchanger exit temperature (node 9) in Fig. (2.20) was high enough to be used for heating up the demineralized water (node 11). The fuel that passed through the heat exchanger (node 17) was mixed with the preheated water to be sent to the SOFC stack for the internal reforming. The DC current generated by the fuel cell was converted to AC current with the appropriate inverter. In the studied system [72], the exothermic electrochemical reaction produced large amount of heat that was used to partially provide heat for the internal reformer, and heat up the anode and the cathode streams. The exit temperature of the HRSG was high enough to be used for co-generation and heat recovery. The assumptions that were applied in that study were as follows: 1) One dimensional flow, 2) Steady state condition, 3) Thermodynamic equilibrium, 4) Negligible kinetic and gravitational terms in the energy and exergy balance equations. The first law and the exergy destruction plant efficiencies are defined in Eq. (4.13)and Eq. (2.2):

$$\eta_{IR-SOFC} = \frac{V_{cell}I \times 10^{-3}}{z|\Delta h_{H_2}|}$$
(2.1)

$$\eta_{ex} = \frac{V_{cell} I \times 10^{-3}}{-(\Delta \tilde{E} x_{ch_A} + \Delta \tilde{E} x_{ch_C} + \Delta \tilde{E} x_{ph_A} + \Delta \tilde{E} x_{ph_C})}$$
(2.2)

Analyzing SOFC-GT hybrid system required several parameters to be evaluated iteratively. The gas turbine exit operating conditions relied on the fuel cell inlet stream conditions and those conditions relied on the GT outlet conditions [72]. These features made analyzing the hybrid system more complicated. This complexity was solved by guessing the value of the fuel cell outlet conditions (i.e. temperature and gas composition). The output of the IR-SOFC system, depended on the operating temperature of the cell, the flow rates and the compositions of the fuel, air and the steam, utilization factors and partial pressures. However, in some cases the system didn't converge [72]. In those cases, the gas turbine was not able to supply enough energy to preheat the fuel and air and to vaporize the water. In that case, system settings needed to be changed and the system was designed to increase the inlet partial pressure of the GT. Alternatively, other changes could be made, including: 1) Water vaporization using an external boiler, 2) Increasing the fuel flow rate and bypassing a portion of the flow to the catalytic burner, 3) Changing the heat exchanger layout, and 4) Increasing the current density or the fuel flow rate.

Siemens Power Corporation manufactured the first pressurized internal reforming IRSOFC-GT hybrid system using a tubular SOFC stack design [30]. The system schematic is demonstrated in Fig. (2.21). This system was tested and operated at the NFCRC at the UCI for over 2900 hours and produced up to 220 kW at fuel to electricity conversion efficiency of 53%. Simulation and control models have been developed at the NFCRC in order to predict the system response to the load demand. Dynamic and steady state data were gathered during the system operation. Nominal fuel cell electricity production has been reported at 180 kWe of the total power while 40 kWe for the gas turbine. Dynamic data from this study have been gathered during the start up and shut down of the system. The purpose of the study was to demonstrate the continuous operation of the hybrid system for 3000 hours of steady state without evaluating the responses to the perturbations. The SOFC stack was pressurized to 3 atm that resulted in an improved performance through a better electrode kinetics and increased output (through the increased partial pressure of reactants). The stand-alone SOFC stack produced 100 kWe at an atmospheric pressure, while it produced 180 kWe in the hybrid configuration [158].



Figure 2.21: Pressurized 220 kW SOFC/Gas Turbine Hybrid [30]

Fig. (2.22) shows the tubular SOFC stack design used in that study. Note the air delivery tubes anode off-gas recirculation by an ejector pump, tubular fuel cells, and combustion zone of the stack design.



Figure 2.22: Tubular SOFC stack design [30]

The developed model at the NFCRC was based on the fundamental mass, momentum and energy conservation principles and the detailed solution of the electrochemical and the chemical reactions and heat transfer equations. The bulk model represented the performance of the pressurized SOFC system. However, it was reported that a more detailed spatial model was required to accurately simulate the hybrid system behavior.

Fig. (2.23) shows the Siemens Westinghouse substack system tested at the UC Irvine. Each substack consisted of fuel ejector, ducting, fuel pre-reformer, and a zone above the stack for combustion of the electrochemically unreacted fuel. The gas turbine, a recuperated two shaft machine was supplied by Northern Research and Engineering Company (NREC). Fig. (2.24) shows the integrated Siemens Westinghouse SOFC-gas turbine system.



Figure 2.23: Siemens Westinghouse substack basic building block tested at UC Irvine [158]



Figure 2.24: Siemens Westinghouse hybrid system [158]

The approximate overall dimensions of the system were 7.4 (m) in length, 2.8 (m) in depth, 3.9 (m) in height [158]. The stack consisted of two 576-cell sub-stacks and was of the design used in the 100 kWe atmospheric pressure SOFC-CHP system. In order to adjust the stack design for the pressurized system, no significant modifications were needed. The gas turbine speed in that study was 70,000 rpm. The power turbine shaft speed was 44,000 rpm. The SOFC generator was valved to permit the airflow around the cell stack (i.e., allow air to bypass the stack for independent control of cathode mass flow and temperature, required because the turbo machinery was not well matched to the SOFC flow requirements). The

gas turbine could be started by firing the gas turbine combustor before the SOFC during the startup and air could be directed around the SOFC generator. The exhaust heat was available when the turbine started in order to aid in heating up the SOFC. As the steady state condition at the maximum efficiency was achieved, the fuel flow to the GT combustor and the air heater was blocked.

Considering the commercial product design, the pressurized PSOFC/T hybrid cycle power systems have competitive advantage due to their higher efficiency and potential for lower installed cost and higher power density in the distributed generation market in the range of 200 kWe to 10 MWe. In one study by Veyo et al., the AlliedSignal Parallon 75 turbo-generator was used and the SOFC generator was sized to match the turbine. The results were a power system concept that was rated at 300 kWe and efficiency of 57%. Another study by Veyo et al. was conceptualization of the hybrid power system with the rating of at least 1 MWe. Gas turbines are under development by Solar Turbines and NREC that could be deployed in the system concept that resulted in the net AC efficiency of projected 60%. Higher power outputs and efficiencies were projected for the mature product SOFC technology in future [158]. The schematic of the 300 kWe class hybrid power system if Veyo et al. is shown in Fig. (2.25).



Figure 2.25: 320 kWe PSOFC/GT power system [158]

The Costamagna research group analyzed variable speed control and efficiency behavior at

part-load in depth [155]. The thermal efficiency of the 250/300 kWe hybrid system was higher than 60% at the design point and very high at part-load conditions. The SOFC schematic of their study is shown in Fig. (2.26) as a bundle of tubular cells; however, no specific details of tubular geometry were considered in the simulation.



Figure 2.26: Scheme of the SOFC group, mixer and sensible heat reformer [155]

In Fig. (2.26), M represents the mixer where the fuel and the recycled fuel were mixed and ejected to the reformer and C represents the anode off-gas combustor. Their SOFC system simulations accounted for all sub-modules of the overall plant model which required many iterations before convergence. Campanari et al. [154], proposed predictive evaluations of the SOFC behavior based on the interpolation of experimental data of measured reactor behavior under different operating conditions. Due to the high number of operating variables (e.g., temperature, current density, reactant utilization, pressure, etc.), a complete experimental database of the SOFC system performance under the different operating conditions was difficult to obtain and no data were available in the open literature at the time. In the Costamagna et al. analysis, some assumptions were made that simplified the simulation as follows: 1) All of the components were assumed to operate adiabatically in the SOFC stack group, 2) The temperatures were assumed to be uniform in the SOFC group, 3) The cathodic flow con-

sisted of  $O_2$  and  $N_2$ , 4) The anodic flow was composed of  $CH_4$ , CO,  $CO_2$ ,  $H_2$ ,  $H_2O$ , 5) The reforming and shift reactions were assumed to be in equilibrium, and 6) The electrochemical oxidation of CO was not considered in the simulation. However, it was known that this was not the case in the transient analysis. Costamagna et al., used energy and mass balance in the form of partial differential equations and integrated them numerically to obtain the parameters (i.e., distributions of the physical and chemical variables) [155]. Ghezel-Ayagh et al. summarized the recent progress in the evolution of Direct FuelCell/Turbine<sup>®</sup> (DFC/T<sup>®</sup>) [159]. The proof-of-concept tests on a sub-MW class DFC/T power plant were performed. By integration of the microturbine with the fuel cell, higher efficiencies were achieved that were associated with the additional power produced by the gas turbine and reduction in auxiliary power consumption by the air blower. In another study, Ghezel-Ayagh et al. mentioned the key features of large-scale DFC/T systems including: electrical efficiencies of up to 75% on natural gas and 60% on coal gas and reduced carbon dioxide release to the environment [160]. In addition, the design of a 40 MW power plant together with a site plan was completed. The German Aerospace Center (DLR) also contributed significantly to the advancement of hybrid SOFC/GT technology. This institute aims to build and operate a prototype hybrid SOFC-GT power plant with an electrical power output of 30 kW [161].



Figure 2.27: The hybrid SOFC-GT power plant being developed at DLR [161]

Several researchers have studied natural gas fueled and methane fed integrated internal reforming solid oxide fuel cell-gas turbine (IRSOFC-GT) power generation systems [64, 73, 72, 162, 163]. Liese et al., compared internal reforming and external reforming in SOFC-GT hybrid system [164]. Chan and Calise assumed that, the only participating fuel in the electrochemical reaction was  $H_2$  [64, 72]. Another assumption was that unreacted gases were fully oxidized in the combustor downstream of the SOFC stack. The main components of the system in these studies were SOFC stack, downstream combustor, gas turbine, power turbine, fuel compressor, air compressor and heat recovery steam generator (HRSG). The main results of the study demonstrated that the system could achieve a net electrical efficiency greater than 60% and the total system efficiency (counting the heat recovery for steam generation) of more than 80% [64]. The developed fuel cell model in that study was based on a tubular natural gas-fed design. However, it could be customized to accept different types of feedstock. Minh et al., studied direct electrochemical reaction of hydrocarbons in the SOFC anode compartment [162]. They determined that the key challenge in the direct oxidation of hydrocarbons at the Ni/YSZ anode is carbon deposition.

# 2.4 MOTIVATION

With reduction in fossil energy resources, increasing environmental pollution, greenhouse gases, and as a result increased goal warming, gas turbine industry has focused on higher efficiency. Hybrid fuel cell-gas turbine systems might enable US to provide clean energy at high efficiency and reduced emissions of their stationary power plants.

# 2.5 SOFC-GT DYNAMICS MODEL DESCRIPTION

## 2.5.1 FUEL CELL AND STACK MODELS

The basic reversible potential of the fuel cell was calculated in the Chan et al. study from Eq. (2.3) [64]:

$$E_r = E^{\circ} + \Delta E = \frac{-\Delta G^{\circ}}{2F} + \frac{RT}{2F} \ln \frac{p_{H_2} p_{O_2}^{\frac{1}{2}}}{p_{H_2O}}$$
(2.3)

From Eq. (2.3), it can be observed that in order to achieve the highest value of reversible voltage, the partial pressures of the reactants ( $H_2$  and  $O_2$ ) should be high enough, while the steam partial pressure should be as low as possible. This is the reason that fuel and oxidant utilization can never reach 100% [11]. Three irreversible polarizations that reduce the cell voltage in all types of fuel cells are as follows [30]: 1) Activation polarization ( $\eta_{Act}$ ), 2) Ohmic polarization ( $\eta_{Ohm}$ ), and 3) Concentration polarization ( $\eta_{Conc}$ ). Hence, the actual cell potential is typically expressed in the form of Eq. (2.4) by subtracting all of the polarizations from the reversible voltage:

$$E = E_r - (\eta_{Act} + \eta_{Ohm} + \eta_{Conc})$$
(2.4)

Where, the  $\eta_{Act}$  is derived from the Butler-Volmer equation and is expressed as a function of

exchange current density  $(i_0)$  in the simplified form of Eq. (2.5):

$$\eta_{Act} = \frac{R_u T}{\alpha n F} ln(\frac{i}{i_0})$$
(2.5)

 $\eta_{ohm}$  is expressed in the from of Eq. (2.6).

$$\eta_{ohm} = iR_{eff} \tag{2.6}$$

Where  $R_{eff}$  is the effective overall cell resistance and *i* is the current density. Moreover, the model of the entire stack was made using the "unit cell" assumption that all cells act in a similar fashion [66, 64]. Fig. (2.28) demonstrates the performance curve of the SOFC produced by Chan et al. using these expressions [64].



Figure 2.28: (a) Cell voltage at different temperatures and current densities. (b) 3-D view of the cell voltage variation at different temperatures and current densities [64]

Increasing the operating temperature of the SOFC stack, resulted in an increase in the limiting current density and a reduction of the over-potentials. Hence, the efficiency and power density of the fuel cell improved. The drawback was the reduced open-circuit voltage when temperature was increased. In the Song et al. model, both  $H_2$  and CO generated by the steam reforming process, participated in the SOFC electrochemical reactions, as shown in Eq. (2.7), Eq.(2.8) and Eq. (2.9) [165]:

$$\frac{1}{2}O_2 + 2e^- \to O^=$$
 (2.7)

$$H_2 + O^= \to H_2 O + 2e^-$$
(2.8)

$$CO + \frac{1}{2}O_2 \to CO_2 \tag{2.9}$$

A complete polarization model of a fuel cell is presented by Chan et al. [166]. In one study, the combined anode and cathode activation polarization was modeled using Eq. (2.10), which was described as due to the sluggish kinetics at the electro-catalytic sites because of low temperature or lack of active sites [30]:

$$\eta_A = \frac{R_a T}{\alpha n F} \ln(\frac{i}{i_0}) \tag{2.10}$$

The exchange current density,  $i_0$  is associated with the catalytic activity at the interfaces of

the electrodes and the electrolyte.  $\alpha$  represents the distribution of the intermediate species at the TPB, and usually has a value between 0 and 1 (usually taken as 0.5). Concentration polarization was modeled by Chan et al. as in Eq. (2.11):

$$\eta_C = -\frac{R_u T}{nF} \ln(1 - \frac{i}{i_L})$$
(2.11)

The limiting current density,  $i_l$ , corresponds to the maximum current that fuel cell can produce to balance the maximum supply speed of reactants. A fuel cell usually operates at lower current densities than the limiting current density. Several fuel cell parameters affect the cell resistance including inherent electrolyte ionic conductivity, electrolyte thickness, electrode and interconnect electronic conductivities and geometry of the electrolyte [30].

The Advanced Power Systems Analyses Tools (APSAT) modeling package is described in a study by Yi et al. [167]. In that study, the performance of the developed tool for the analysis of the tubular SOFC power systems was compared to the observed hybrid operation data. The stack model that has been developed by the Chan research group consisted of four reactors that each could serve as heat sources or heat sinks to calculate the stack temperature [64]: 1) Heat generated through the electrochemical reactions in the cells, 2) Heat consumed by the internal reforming, 3) Heat transferred to the reactants, and 4) Heat loss to the surroundings. Hence, the reaction heat was expressed in the form of Eq. (2.12):

$$Q_{rxn} = i \sum \eta + T\Delta S \tag{2.12}$$

Where  $\Delta S$  represents the entropy difference between the reactants and the products.

Under steady state operation of the SOFC stack, a portion of the heat produced by the electrochemical reaction was consumed by the internal reforming process and to heat up the reactants using recuperating heat exchangers. Effects of air inlet temperature and fuel flow rate on the SOFC voltage and the stack power output were also investigated in the Chan et al. study. These results are shown in Fig. (2.29) and Fig. (2.30).



Figure 2.29: 3-D view of SOFC voltage variation at different air inlet temperatures and fuel flow rates [64]



Figure 2.30: 3-D view of stack power output variation at different air inlet temperatures and fuel flow rates [64]

Chan et al. found that at a fixed fuel utilization rate, increasing the fuel flow rate caused an increase in the cell current density. Hence, by looking at the polarization curve in Fig. (2.28(a)), the cell voltage drops. Results showed that the increased inlet air temperature improved the cell efficiency since the voltage was increased. Fig. (2.30) illustrates the output power of the stack that increased with the higher flow rate and inlet air temperature. Selimovic et al., suggested that by networking the fuel cell stacks, increased efficiency, improved thermal balance, and higher total reactant utilization can be achieved. In such a combination, the stacks were operating in series in the fuel flow direction. In one study, the SOFC configuration using the multistage oxidation concept was analyzed. As a result, the stack efficiency was increased due to smaller variation in the Nernst voltage across the cell area [168].

### 2.5.2 **Reformer models**

For a natural gas fed hybrid SOFC-GT system, both internal or external reformers can be used in the system. Due to expenses of providing additional cooling to the SOFC stack in external reforming, an internal reformer has tended to be preferred over an external reformer in the literature. For practical reasons of high temperature gradients when using only internal reforming, many research groups have considered both external and internal reforming for their hybrid SOFC/GT systems. Chan et al., have studied the internal reforming feasibility in SOFC-GT hybrid systems [64]. The approach taken in that study, was vaporization of feedwater by using the stack waste heat (HRSG), to produce the steam required for the reformer. The reaction mechanisms of internal reforming are expressed in Eq. (2.13) to Eq. (2.15):

Reforming reaction:  $CH_4 + H_2O \leftrightarrow CO + 3H_2$ 

(2.13)

Shifting reaction: 
$$CO + H_2O \leftrightarrow CO_2 + H_2$$

(2.14)

Electrochemical reaction: 
$$H_2 + \frac{1}{2}O_2 \rightarrow H_2O$$
 (2.15)

In the mentioned study, the equilibrium constants for the reforming and shifting reactions depend upon the operating temperature and can be expressed by a polynomial form shown in Eq. (2.16):

$$logK_p = AT^4 + BT^3 + CT^2 + DT + E$$
(2.16)

The constants A, B, C, and D are listed in the work performed by Bossel [169]. Assuming that the reforming and shifting reactions were always in equilibrium, the equilibrium constants were calculated as a function of partial pressures of the reactants and the products as expressed in Eq. (2.17) and Eq.(2.18):

Reforming: 
$$K_{pr} = \frac{p_{H_2}^3 p_{CO}}{p_{CH_4} p_{H_2O}}$$
 (2.17)

Shifting: 
$$K_{ps} = \frac{p_{H_2}p_{CO_2}}{p_{CO}p_{H_2O}}$$

(2.18)

Eq. (2.19) and Eq. (2.20) express the reforming and the shifting reaction net required heat as a function of enthalpies of the reaction participants.

$$Q_r = x(h_{CO} + 3h_{H_2} - h_{H_2O} - h_{CH_4})$$
(2.19)

$$Q_s = y(h_{CO_2} + h_{H_2} - h_{CO} - h_{H_2O})$$
(2.20)

Since both of the reforming and the shifting reactions are endothermic, the total heat transfer from the stack was calculated by subtracting the reforming and shifting heat from the generated heat in the electrochemical reaction as shown in Eq. (2.21):

$$Q = Q_{rxn} - Q_r - Q_s \tag{2.21}$$

Where,  $Q_{rxn}$  is the heat generated through the electrochemical reaction. Calise et al. used the shift reaction equilibrium constant as follows [72]:

$$K_{p,shift} = \exp(\frac{4594}{T} - 4.35)$$
(2.22)

The reaction constant increases as temperature decreases. Several previous studies have shown that the solid, anode and cathode outlet streams' equilibrium temperatures reach the same value [63, 69, 154, 155].

In the Brouwer et al. study [30], the rates of the reforming and the shift reactions have been determined as in the Eq. (2.23) and Eq. (2.24):

$$R_{1} = k_{1} \left(\frac{P_{CH_{4}}P_{H_{O}}}{P_{H_{2}}^{2.5}} - \frac{P_{CO}P_{H_{2}}^{0.5}}{K_{p1}}\right) / DEN^{2}$$
(2.23)

$$R_2 = k_2 \left(\frac{P_{CO}P_{H_2O}}{P_{H_2}} - \frac{P_{O_2}}{K_{p2}}\right) / DEN^2$$
(2.24)

Where,

$$DEN = 1 + K_{CO}P_{CO} + K_{H_2}P_{H_2} + K_{CH_4}P_{CH_4} + \frac{K_{H_2O}P_{H_2O}}{P_{H_2}}$$
(2.25)

The reaction constants have been calculated from the Arrhenius equation as in Eq. (2.26):

$$k_i = A_i \exp(-\frac{E_i}{RT})$$
(2.26)

Where *i* represents the species (i.e,  $CO, CH_4, H_2O$  and  $H_2$ ). The constants in the Brouwer et al. model are presented in Table 2.2.

Rate Constant	Activation	Pre-	Rate constant	Heat of	Pre-exponential factor
	energy	exponential		adsorption	
	(kJ/mol)	factor		(kJ/mol)	
		$(kmol.MPa^0$	$^{.5}/kg_{cat}.h)$		
$k_1$	240.1	$1.336 \times 10^{15}$	K <sub>CO</sub>	-70.65	$8.23 \times 10^{-4} (MPa^{-1})$
$k_2$	67.13	$1.955 \times 10^7$	$K_{CH_4}$	-38.28	$6.65 \times 10^{-3} (MPa^{-1})$
$k_3$	243.9	$3.22 \times 10^{14}$	$K_{H_2O}$	88.68	$1.77 \times 10^5 (unitless)$
			$K_{H_2}$	-82.9	$6.12 \times 10^{-8} (MPa^{-1})$

Table 2.2: Reformation model constants used by Brouwer et al. [30]

Energy balance between the electrodes and the electrolyte and the cell materials were modeled using Eq. (2.27):

$$\frac{d\rho C_{mass}TV_{cv}}{dt} = \dot{E}_{in} - \dot{E}_{out} + Q_{gen}$$
(2.27)

Where the generated heat in the electrochemical reaction was expressed as Eq. (2.28):

$$Q_{GEN} = \left(\frac{\Delta H_{f,H_2O(g)}}{nF} - V_{cell}\right) \times i$$
(2.28)

The study assumed that gas stream flows were fully developed and laminar. Thus the mo-
mentum conservation equation that was used is in the form of Eq. (2.29):

$$\Delta P = f \frac{l}{D_h} \frac{\rho \nu^3}{2} \tag{2.29}$$

Where  $\Delta P$  is the pressure drop, f is the friction factor, L is the characteristic length,  $\rho$  represents the density,  $\nu$  is the average velocity and  $D_h$  is the hydraulic diameter. Chemical kinetic representations of SMR (steam methane reformation) and WGS (water gas shift) reactions have also been presented in another study by Campanari et al. [170]. Detailed electrochemical models for either  $H_2$ -only and  $H_2 - CO$  oxidation were also presented in that study.

#### 2.5.3 COMBUSTOR MODELS

Chan et al., assumed that all the residual anode off-gas fuel constituents of the IR-SOFC stack were fully oxidized in the combustor (i.e.,  $CH_4$ , CO and  $H_2$ ). Eq. (2.30) to Eq. (2.33) show the chemical reactions proposed in that study [64]:

$$CH_4 + 2O_2 = CO_2 + 2H_2O + \Delta H_{rxn,H_4}$$
(2.30)

$$CO + \frac{1}{2}O_2 = CO_2 + \Delta H_{rxn,CO}$$

(2.31)

$$H_2 + \frac{1}{2}O_2 = H_2O + \Delta H_{rxn,H_2}$$
(2.32)

$$\sum_{j} H_{p,j} - \sum_{i} H_{r,i} = \Delta H_{rxn,CH_4} + \Delta H_{rxn,CO} + \Delta H_{rxn,H_2}$$
(2.33)

In order to determine the exit temperature of the combustor  $(T_p)$ , Eq. (2.34) was used:

$$\left(\sum_{i} H_{r,i} + \Delta H_{rxn,CH_4} + \Delta H_{rxn,CO} + \Delta H_{rxn,H_2}\right)\epsilon_{eff} = \sum_{j} n_j \int_{T_c}^{T_p} c_{p,j} dT$$
(2.34)

Where,  $\epsilon_{eff}$  is the combustion efficiency. The maximum possible heat exchanged from the heat exchanger was calculated using Eq. (2.35):

$$Q_{max} = [min(\dot{n}_c \times c_{p,c}, \dot{n}_h \times c_{p,h})] \times (T_{h,i} - T_{c,i})$$
(2.35)

Where h and c represent the hot and the cold streams. So the net heat exchange was calcu-

lated from Eq. (2.36):

$$Q = \epsilon_{ex} \times Q_{max} \tag{2.36}$$

Calise et al., have modeled a catalytic burner [72]. In that study, gas-fuel and the gas-air heat exchangers were simulated on a counter flow basis using the effectiveness number of transfer units  $\epsilon - NTU$  method. The impact of the heat exchanger on the SOFC-GT hybrid system was investigated in another study by Magistri et al. [171]. Several configurations in terms of the cycle layout were presented and the most promising configurations were identified. It was suggested that the primary surface-type and some plate-fin-type recuperators could be used in order to increase the compactness and minimize the capital cost of hybrid systems. The high temperature heat exchangers, operated in the inlet temperature range of  $750 - 1100^{\circ}C$  required the use of advanced materials such as nickel-based alloys, cobalt-based alloys and ceramics. In addition, Magistri et al. indicated that the typically higher pressure drop in ceramic heat exchangers can significantly reduce the efficiency of the cycle.

### 2.6 STEADY-STATE PERFORMANCE REPORTED

Efficiencies associated with several hybrid systems are shown in Table. (2.3). In general, high operating pressure can significantly improve the system performance and efficiency.

Туре	Performer/year	Stack	SOFC	Net	Total	Electrica	l Total
		Pres-	Power	Tur-	Power	Effi-	Efficiency
		sure		bine		ciency	
				Power			
SOFC/GT hy-	Palsson et al., 2000		311 k-	173 k-		60%	86%
brid	[59]		W	W			

Atmospheric	Veyo et al. 2002	1 atm				+45%	75%
SOFC	[158]						
PSOFC/GT	Veyo et al. 2002		Total			59%	
hybrid	[158]		Pow-				
			er:MWe				
			class				
IRSOFC/GT	Chab et al., 2003[66]	5 atm	1.3	437.8		60.6%	80.5%
hybrid			MW	kW			
			Power				
			Plant				
$SOFC/\mu GT$	Uechi et al., 2004		23.6 k-	6.4 k-		66.5%	
hybrid	[172, 173]		W	W			
IRSOFC/GT	Song et al., 2005		176 k-	47 kW		57%	
hybrid	[165]		W				
SOFC/GT hy-	Rajashekara et al.,	3atm	441	161kW			68.6%
brid	2005[19]		kW				
			SOFC				
IRSOFC/GT	Yi et al., 2005 [174]	50 bar	450	177		75.8%L	HV
hybrid			MW	MW			
			SOFC				
			Power				
IRSOFC-GT	Calise et al., 2006				1.47	65.4%	
	[70]				MW		
SOFC/GT	Roberts et al., 2006				350 K-	66%	
(variable	[175]				W		
speed)							
SOFC/GT	Roberts et al., 2006				350 K-	53%	
(fixed speed)	[175]				W		

IRSOFC/GT	Bavarsad et al., 2007	3-7 at-	221.73	98 kW		53.34%	65.62%
hybrid	[73]	m	kW				
			SOFC				
SOFC/GT hy-	Lim et al., 2008	3.5 at-	5 kW				
brid	[176]	m					
SOFC-ST	Rokni, 2010 [139]		31.13	9.21	40.34	67%	
(ASR)			MW	MW	MW		
SOFC/GT	Li et al,., 2010 [177]	10.1	247.77	63.38	238.62	61.5%	
		bar	MW	MW	MW	(HHV)	
SOFC/GT	Li et al., 2010 [177]	1.1 bar	229.91		202.69	52.2%	
			MW		MW	(HHV)	
heat pipe in-	Santhanam et al.,				100 k-	72%	
tegrated Gasi-	2010 [178]				W		
fierSOFCGT							
IT-SOFC	Romano et al., 2011	14 bar	330.9	123.6	493.4	51.95%	
based IGFC	[179]		MW	MW	MW	LHV	
IT-SOFC	Romano et al., 2011	23 bar	183.8	246.3	515.8	54.29%	
based IGFC	[179]		MW	MW	MW	LHV	
SOFC-GT-	Yan et al., 2013 [138]		3126	1642		67%	
ORC			kW	kW			
SOFC-	Rokni, 2013 [180]				order	60%	
Stirling					of 10		
hybrid system					kW		
SOFC/GT	McLarty et al., 2014					>	
	[181]					65%	
SOFC-GT	Caliandro, 2014					>	
(fuelled with	[182]					70%	
gasified lig-							
nocellulosic							
biomass)							

SOFC-GT	Lv et al., 2014 [183]			144-	50 -	
(gassified				160	55%	
biomass				kW		
fueled)						
SOFC-GT	Speidel et al., 2015	7.74	3.96	11.70	54.2%	
	[148]	MW	MW	MW		
SOFC-MGT-	Ebrahimi et al., 2016	15.5 k-	1.25 k-		60.95%	65.77%
ORC	[141]	W	W			
SOFC-GT	Yi et al., 2016[151]	368.7	98.3	467	72.8%	
		MW	MW	MW		
SOFC/GTCC	Yi et al., 2016 [151]	367.8	96.1	486.4	76%	
		MW	MW	MW		
SOFC/GT	Facchinetti et al.,				63%	
	2016 [184]					
SOFC-MGT	Isfahani et al., 2016				51.5%	
	[185]					
SOFCGT	Saebea et al., 2017	388.28	111.9	100 k-	56.8%	
(high tem-	[186]	kW	kW	W		
perature heat						
exchanger)						
SOFCGT	Saebea et al., 2017	388.27	117.39		62.48%	
(cathode	[186]	kW	kW			
exhaust gas						
recirculation)						
SOFC-blade	Choudhary et al.,				73.46%	
cooled gas	2017 [68]					
turbine						

Table 2.3: Several studied hybrid system efficiencies

Veyo et al., showed that the pressurized SOFC-GT hybrid system had 10 efficiency points

advantage over the atmospheric hybrid system [158]. Fuel cells and gas turbines must maintain efficient operation and electricity production while protecting the equipment during the perturbations that happen when the system is connected to the utility grid network. A creative control strategy is needed to ensure a flexible system with a robust dynamic operation. Velumani et al. proposed a combined heat and power (CHP) SOFC-microturbine-absorption chiller system for 230 kWe power demand of a building which acheived a thermal efficiency of 70-75%, where the waste heat could be used for local heating and cooling [187]. The installation costs were reported in the range of 400 US\$/kWe and 4000-5000 US \$/kWe for the microturbine and the SOFC, respectively. Barelli et al., have mentioned that the integrated SOFC-GT efficiency can be significantly increased during load following operation [188]. The developed hybrid system model permitted 54.5% mean efficiency on a daily basis, with short rapid dynamic response and wide part-load operating limits (down to 42.8% of nominal system power).

## 2.7 Component Modifications for Dynamic Hybrid

#### System Operation

Many of the components desired for hybrid systems require significant advancement before the systems are introduced as commercial products. In addition, the system integration and control of a hybrid fuel cell-gas turbine system needs significant advancement for improving their dynamic response. For example, compressors are sensitive to air density, so that the compressor work demand increases as air temperature increases. Since the fuel cell operates at a fixed temperature, some researchers have found it challenging to maintain sufficient compressor mass flow at high ambient temperature. If the gas turbine operates at a fixed speed, then there are few options available to control the mass flow [30]. As a result, the total power output of the system must often be sacrificed (by lowering the load demand), so that the fuel cell could operate at a relatively fixed temperature. Understanding several factors could help to improve the fuel cell performance in hybrid systems. These include pressurized operation, effects of significant pressure differentials and pressure fluctuations, integration with oxidizers for the increased thermal output to the heat engine, increased fuel cell power density and material improvements for the increased current density, cost reduction, electrode kinetics improvements and durability. The effects of decreasing the air to fuel ratio compared to stand-alone fuel cell operation, so that the hybrid system is able to operate at a higher combustor firing temperature are worthy of investigation. Research that could contribute to the fuel flexibility of the fuel cell component in order to improve the fuel cell tolerance to contaminants (especially those present in coal gasification products) is important. Using a modulatable (0-100% load) combustor, which can withstand the constant heat flux of the high temperature fuel cell effluent gases through the inactive combustor in the steady state condition without cooling air, could improve the current state of the combustor application in the hybrid systems. The integration of inverters, converters, and power electronics with the hybrid power plant is also in need of understanding and advancement. Using low cost and simplified inverters and understanding the effects of the inverter on the power quality could contribute well to hybrid systems advancement.

It's known that heat engines exhibit better performance at higher temperature and pressure in stand-alone applications. However, integration with fuel cells requires specific modifications such as lower temperature and lower pressure operation that may be better for overall hybrid system performance. Hence heat engine modifications that may be preferred could have the following features: 1) High performance under low quality heat input of the fuel cell (i.e., lower TIT ( $< 900^{\circ}C$ ) in comparison to that typically delivered by a combustor ( $900^{\circ}C$ )), 2) Ability to withstand the long duration of the fuel cell thermal cycling, 3) Ability to perform under the low pressure ratios, 4) Ability to operate with the increased surge margin, and 5) Improvement in compatibility with slow response time of the fuel cell.

# 2.8 PRACTICAL ISSUES DISCUSSED IN HYBRID SOFC/GT

#### LITERATURE

In general fuel crossover is a phenomenon that occurs when a specific amount of gaseous fuel diffuses from the anode compartment to the cathode compartment through the electrolyte or seals without reacting electro-chemically. This is considered as an important factor in the SOFC-GT hybrid systems performance degradation since sealing may be more difficult at higher pressure operation. Fuel crossover results in a direct reaction of the gaseous fuel with the oxidant and produces heat that may lead to temperature gradients and degradation. Electronic conduction through the electrolyte, which affects the cell net electrical current density and efficiency is another mechanism of degraded performance expressed in the literature that especially plagues certain types of electrolyte materials (e.g. ceria- and bismuth-oxides). Pressurizing the cell increases the overall system efficiency. However, the technical challenges associated with development of a robust SOFC cell and stack design for operating under very high pressures is challenging and the development costs could be significant. It is important to note that pressurization of an SOFC stack leads to reductions in several polarization losses that result in increased efficiency for any given operating current, which subsequently require less air flow for cooling and additional balance of plant loss reductions that together increase overall efficiency. Yi et al. reported that increases in operating pressure increase overall system efficiency. However, the technical challenges in developing an SOFC with a very high operating pressure as well as the associated development costs were reported to possibly be quite high. They concluded that there is a balance between the development cost and the efficiency. In their work, the system efficiency was the only factor considered [174]. Stiller suggested that specific incidents should be avoided for a safe operation of the hybrid systems [189]. Some of these incidents have been reported as: compressor surge or cell degradation due to thermal cycling or large temperature gradients,

carbon deposition and anode compartment blocking, and backflow of gas from the burner to the anode compartment, exposing the anode to oxygen.

## 2.9 HYBRID SYSTEM TRANSIENT OPERATION AND CON-TROL

#### 2.9.1 TURBOMACHINERY CONTROLS

The turbomachinery used in hybrid SOFC-GT system can typically operate in two different manners; fixed speed (synchronous) or variable speed (asynchronous) [190]. In the synchronous mode the shaft is directly driving the electrical generator at some multiple of the grid frequency. The advantage of this method is elimination of costly power conditioning hardware and additional operating losses of the power conditioning equipment. For the synchronous configurations the shaft speed of the turbomachinery in the hybrid system models is typically controlled to a specified speed using a feedback loop with PI controller as shown in Fig. (2.31).



Figure 2.31: Shaft speed control strategy [190]

Brouwer et al., acquired the experimental data of an SOFC-GT hybrid system during the

system start-up. During this period of operation, the hybrid system was slowly ramped up in power to minimize the mechanical stresses from thermal dynamics of the fuel cell [30]. Fig. (2.32) demonstrates the control moves in their study, which included the SOFC load, the recuperator, the SOFC bypass valve positions, and the fuel flow to the system. The bypass valves were used to independently control the temperature and the mass flow rate of the air entering the SOFC stack. The recuperator bypass was used to control the inlet temperature of the air entering the stack, while the SOFC bypass was used to control the air mass flow through the SOFC stack. In that study, the hybrid system utilized a dual shaft turbine. The SOFC ramped up from 147 kW to 158 kW over a period of 100,000 seconds. In the experiments, a sudden drop in the SOFC power was observed as the SOFC bypass allowed more air to bypass the SOFC. At low load, the model couldn't capture this sudden drop, due to the uncertainties in the exact flow dynamics and the flow amounts altered by the SOFC bypass valve. Also the first degrees of movement of the valve significantly changed the amount of mass flow being bypassed. As more air bypassed the SOFC stack, the turbine inlet temperature (TIT) was reduced which resulted in lower gas turbine power output [30].



Model Inputs for the 220 kW SOFC/GT Hybrid

Figure 2.32: GT power output, model VS experiment data [30]

The model of the Brouwer et al. followed the experimental data quite well, except at the few load values where the SOFC bypass valve was being adjusted. The model demonstrated that the turbine inlet temperature (TIT) was the most effective parameter for changing the turbine power output. The model simulated the temperature at each point of the cycle and they were fairly close. There was a 5% difference in the compressor mass flow, which caused the model to predict lower temperatures. However, the model predicted higher temperature because of the lack of accounting for the system heat loss. The only heat loss that has been accounted for in the simulation was from combustor 1 and 2 where there was significant heat loss [30].

Rastrepo et al. proposed a model predictive control strategy [105]. The constraint airflow valves and the electric load were used in the simulation to control the constraint turbine speed and the cathode airflow (CAF). Ferrari et al. studied a plant, comprising the coupling of a tubular solid oxide fuel cell stack with a microturbine that was equipped with a bypass valve able to connect the compressor outlet with the turbine inlet duct for rotational speed control [191]. The main difficulty that Ferrari et al. found in implementing their control system is the difference between the small mechanical inertia of the microturbine shaft compared to the very large thermal capacitance of the fuel cell stack [192]. Jia et al. used GT shaft speed control to stabilize the system [193]. In that study, a PI-type shaft speed controller, was implemented to stabilize the hybrid system.

#### 2.9.2 OFF-DESIGN PERFORMANCE OF HYBRID SYSTEM USING FIXED

#### AND VARIABLE GT SPEED

In a study by Roberts et al., transient performance and control analysis of atmospheric hybrid systems with MCFCs were investigated [194]. Load perturbation was applied to evaluate the system behavior. It was suggested that additional control strategies were required to study the system behavior. The variation of the fuel utilization was the control method that was

studied in that paper. Variable speed of the GT was tested and showed that it could be a promising control variable but limited to a system with lower power demand. For a larger turn down in the system power, a bypass or an additional combustor was needed [195]. It was shown that the variation of the GT speed was a required control method both for the pressurized [30] and atmospheric [196] conditions in the part-load operation. The reason was that the variation in the GT speed provided a better control over the compressor mass flow. Brouwer et al. [30] developed a 1.15 MW pressurized SOFC-GT hybrid model. The system was designed around the variable speed Capstone C200 MTG. The design parameters of that system are presented in Table. (2.4).

Design Parameter	Value	Unit
System Power	1150	kW
Combustor Efficiency	1	
Recuperator Effectiveness	1	
Heat Exchanger Effectiveness	0.4	
System Efficiency	0.73	
Shaft Speed	60000	RPM
Turbine Inlet Temperature	950	C
Turbine Efficiency	1	
Mass Flow	1.3	$\frac{kg}{s}$
Compressor Inlet Temperature	1500.0	C
Compressor Discharge Pressure	43569.8	kPa
Compressor Efficiency	75.0%	
Gas Turbine Power Mechanical Loss (Shaft)	$RPM^2 \times 8.33 \times 10^{-10}$	kW
Gas Turbine Power Electronics Efficiency	98% and 14 kW load	
Compressor Leakage	0.02	
Compressor Filter Loss	0.02	
SOFC Stack Power	960	kW
SOFC Active Area	320	$m^2$
Current Density	4,000	$\frac{A}{m^2}$
SOFC Operating Voltage	0.75	V
SOFC Power Electronics	100.0%	
Anode Recirculation	80.0%	
SOFC Stack Fuel Utilization	85.0%	
SOFC Average Operating Temperature	900	C

Table 2.4: Design parameters of SOFC/GT system [30]

The electrochemical performance of the SOFC that was developed in this model was based on the parameters in the Kim's et al. study [197]. Two different scenarios were investigated in the model: 1) A base-load system exposed to ambient temperature changes, and 2) A load following system exposed to ambient conditions. For the base-load case the system maintained 1.15 MW of total electricity production during ambient temperature changes. The ambient temperature in the model was varied from  $-5^{\circ}C$  to  $35^{\circ}C$  in order to imitate large diurnal temperature fluctuations. In the second case (i.e., load-following), a sinusoidal demand of power with the maximum at 1150 kW and the minimum at 950 kW was applied. For the base-load case the gas turbine power changed significantly in order to control the speed. The SOFC power was being changed to compensate for changes in the gas turbine power. The effects of the ambient temperature were demonstrated on the SOFC temperature. A high ambient temperature increased the compressor exit temperature and reduced its mass flow rate. The mass flow rate of the compressor increased as the shaft speed increased. Two major parameters increased the shaft speed: 1) The ambient temperature was at the design inlet temperature of the compressor that resulted in a more efficient compressor, and 2) When the TIT increased, it provided more power to the shaft. As the bypass valve opened, the turbine inlet temperature and turbine power were lowered. In the load following case, the simulated system showed an excellent performance in following the power demand. The gas turbine maintained 140 kW during the day unlike the base-load case.

Palsson used a planar design of the SOFC stack component in a 500 kW natural gas fed system. They achieved high efficiencies at low pressure ratios. Their work focused on off-design calculations and varying the part load behavior of the system. Due to the mismatch between the required cooling flow of the SOFC and the flow provided by the compressor, cooling or heating the air was necessary in some cases, which typically reduced the system performance [198]. Fig. (2.33) shows the partial load performance of SOFC-GT system with turbine inlet temperature and rotor speed as parameters.



Figure 2.33: Partial load performance of SOFC-GT system with TIT and rotor speed as parameters [198]

Magistri et al. defined the design point of the pressurized hybrid system based on Rolls-Royce's integrated planar solid oxide fuel cell (IP-SOFC) [199]. The hybrid system size was about 2 MWe and the design point analysis was performed using two different IP-SOFC models developed by the Thermochemical Power Group (TPG) at the University of Genoa: 1) A general model, where the transport and balance equations of the mass, energy and electrical charges were solved in the lumped volume at constant temperature, 2) A detailed model where all of the equations were solved using finite difference approach inside the single cell. The ambient conditions effects on the IP-SOFC hybrid system performance were investigated in that study. The part-load performance of the IP-SOFC hybrid system at a fixed and variable turbine speed was analyzed. Fig. (2.34) shows the influence of ambient temperature without control system. The operating temperature of the plant are strongly affected by ambient conditions. The increase of 15°C can result in the 4% increase in the maximum temperature of the IP-SOFC.



Figure 2.34: Influence of ambient temperature without control system [199]

The main results of this Magistri et al. work are as follows: 1) The generic stack model was useful for the preliminary investigations, 2) The design point conditions defined with the simplified model were modified to take the calculated cell internal temperature distribution into account, 3) Part-load performance of the system was assessed. In the case of no modifications in the cell parameters, ambient temperature increase affected hybrid system performance. On the other hand, for the case of modified cell parameters, the fuel flow rate and the current density were included in the calculations to avoid the cited infeasible operating conditions. Fig. (2.35) and Fig. (2.36) show the hybrid system and fuel cell part load efficiency of Magistri et al. [199].



Figure 2.35: Hybrid System Part Load Efficiency [199]



Figure 2.36: Fuel Cell Part Load Efficiency [199]

In another study from the same group (Magistri et al.), a hybrid system comprised of a 5 kW microturbine coupled with a small size SOFC stack (31 kW) was analyzed [200]. The power of the whole system was 36 kW depending upon the stack design parameters. A modular code named "HS-SOFC" was used to obtain the design and off-design performance of the

hybrid system. The hybrid system plant is shown in Fig. (2.37).



Figure 2.37: Simplified layout of hybrid system (Personal Turbine and SOFC) [200]

The system demonstrated potential efficiency at 56% at the design point. Two different speed controls were used for the turbine's rotational speed: 1) Fixed and 2) Variable. In the fixed turbine speed control system analysis, the supplied power of the system was changed by varying the fuel flow rate fed to the system. However, the fuel utilization of the fuel cell stack was kept constant at 0.85. Fig. (2.38) shows the part-load performance of the hybrid system at fixed turbine speed control system in the range of 55% load to full load. The relative importance of component contributions have been reported as follows: the SOFC and PT expander supply 31 kW and 17.3 kW, respectively, the air compressor consumes 9.7 kW, and the other losses account for 2.6 kW at the design point.



Figure 2.38: Design and part-load performance of a hybrid system versus non-dimensional power (fixed turbine speed control system) [200]

The typical operation mode of large-size gas turbine plants does not usually involve the possibility of changing the rotational speed of the turbine. The reason for this is that typical plants do not include an inverter, and thus the rotational speed of the turbine is fixed through the gear-box and generator to match the alternating frequency required by the end user/electrical network. On the contrary, a hybrid fuel cell system requires an inverter to convert the direct electrical current produced by the fuel cell and often also contains a rectifier and inverter to convert the gas turbine electricity produced by a variable high-speed alternator. Thus, this typical configuration allows the operation of the gas turbine at variable rotational speed. Fig (2.39) shows the hybrid system performance using variable turbine speed control system [200].



Figure 2.39: Hybrid system inefficiencies versus non-dimensional power (Variable turbine speed control system) [200]

The turbomachinery design characteristics for a hybrid system have been discussed in a study by Traverso et al. [201]. Radial compressors represent an established technology for gas turbine cycles of small and medium size due to their lower cost compared to axial compressors for small size and lower pressure ratios. The choice of the study focuses on radial compressors because it is expected that they will be employed by the first generation of commercial fuel cell hybrid systems, which are likely to address the 100kW - 1 MW size class for stationary power production. In that study, the power of the system was modified using two different control strategies: 1) Control of the fuel flow rate, 2) Simultaneous control of fuel flow rate and the rotational speed of the gas turbine. Fig. (2.40) shows the corresponding power plant for the control study.



Figure 2.40: Pressurized SOFC hybrid system [201]

The main parameters of the hybrid system that had to be monitored were mentioned by Traverso et al. as follows: 1) Thermal gradient of the fuel cell stack, 2) The pressure difference between anode and cathode, 3) The composition of natural gas entering the fuel cell ducts, 4) Shaft overspeed and 5) Compressor surge. Traverso et al. investigated the impact of variation in the exhaust composition on the expander performance [201].  $c_P$ , R and k were shown to be subject to variations in dry air up to 7.6%, 2.6% and 1.7%, respectively. Fig. (2.41) and Fig. (2.42) show the off-design performance of the Traverso et al. hybrid system and fuel cell at constant speed [201].



Figure 2.41: Off-design performance of P-HS (constant speed)[201]



Figure 2.42: Off-design performance of fuel cell stack in P-HS layout (constant speed) [201] Fig. (2.43) shows the efficiency advantage of a hybrid system compared to a traditional micro gas turbine plant at design point and under part-load conditions.



Figure 2.43: Off-design performance of P-HS layout (Variable speed) [201]

Fig. (2.44) shows the off-design performance of the SOFC in hybrid system determined by Traverso et al. Note that as the fuel cell efficiency increases, the turbine rotational speed decreases [201].



Figure 2.44: Off-design performance of fuel cell stack in P-HS layout (Variable speed) [201]

Roberts et al., used two similar control strategies, (i.e., fixed speed operation and variable speed operation) [175]. The system efficiency they reported was greater than 66% for variable speed operation compared to 53% efficiency for fixed speed operation. Fig. (2.45) shows the plant at the gas turbine fixed speed operation.



Figure 2.45: SOFC-GT hybrid system with fixed speed GT and cathode bypass [175]

For the fixed speed operation additional actuators (cathode bypass or auxillary combustor) were required in order to maintain the SOFC operating temperature. However, for the variable speed operation, the additional actuators were not required [175]. Komatsu et al., used the variable MGT rotational speed operation control for the part-load operation [202]. The primary reason for the system performance degradation at part-load was due to the operating temperature reduction of the SOFC component. The operating temperature reduction was caused by the reduction in the fuel supply and the heat generated in the cells. The variable MGT speed control required flexible airflow requirements that could lead to high system efficiency. Fig. (2.46) shows the calculation results of temperature distribution in the SOFC module at the design point. The horizontal axis is the normalized distance from 0 to 1. The gas flow directions are the same as one of the segment length. This figure shows the temperature distribution for performance analysis of the part-load operating condition of the hybrid system.



Figure 2.46: Temperature distribution in the SOFC module (a) air stream in the electrochemical reaction process (b) electrolyte and electrodes (c) fuel stream in the electrochemical reaction process (d) fuel stream in the reforming process [202].

In a study by Yang et al., the power production from the gas turbine was much less than that of the SOFC. However, its role in the hybrid system efficiency become more important under part-load operating conditions [203]. Maximizing the produced power from the most efficient component in the hybrid system (the SOFC) lead to the highest system efficiency. Fig. (2.47) shows the two important temperatures of the Yang et al. SOFC-GT hybrid system operating with VRS + FC (variable rotational speed with fuel control) and HAB + FC (hot air bypass with fuel control) part-load control modes.



Figure 2.47: Two important temperatures of SOFC/GT hybrid system operating with VRS + FC and HAB + FC modes: (a) cell temperature; (b) turbine inlet temperature [203]

Controlling the air through a pressurized solid oxide fuel cell (SOFC) stack in a SOFC-GT pressurized hybrid system was studied by Traverso et al.[204]. The results showed that a variable speed microturbine was the best option for off-design operation of a SOFC-GT hybrid system.

#### 2.9.3 CONTROL STRATEGIES FOR COMPRESSOR SURGE

Ferrari et al., [205] designed and installed a high temperature fuel cell-micro gas turbine physical emulator in the framework of the European Integrated Project (FELICITAS) at the Thermochemical Power Group (TPG) located in Savona. The focus of the study was to minimize the viscous pressure loss in order to: 1) Reduce the pressure imbalance and dynamics between the compressor and the expander, 2) Maintain an accurate measurement, and 3) Have an effective plant efficiency. A modular high temperature volume was designed using computational fluid dynamics (CFD) tools to achieve a high uniformity in the flow distribution inside the volume and to minimize the pressure losses. Their research showed that surge occurred during the shutdown for a particular configuration. Fig. (2.48) shows the pressure losses between the recuperator and the combustor for different conditions. The modular volume line values, obtained at different loads with all the volume pipes connected to the machine, were compared with the volume zero and direct line experimental data to show the loss increase. However, the data obtained with the whole volume show that the objective of minimizing the additional pressure losses has been completely reached. The tests operated at volume zero configuration focusing the attention on a 75 kW load rejection. The preliminary tests operated with modular volume connected with the machine. The paper showed that he surge happened during a shutdown at this configuration.

In another study by Ferrari et al., strategies to avoid surge or excessive stress during the start-up and shutdown phases were proposed [206]. They concluded that a new control study for managing the valve responsible for controling the inlet temperature ramp during the hybrid system start-up and shutdown emulation was needed. Fig. (2.49) shows the temperature control system scheme. The internal loop controls the valve pneumatic actuator to reach the requested position. The difference between the command and the signal from the valve position sensor is the input of a proportional integral (PI) controller optimized for an overdamped valve reaction. The external loop controls the fuel cell cathode inlet temperature



to reach the temperature command value, which is the heating or cooling ramp.

Figure 2.48: Pressure losses between the recuperator and the combustor for three different conditions: (i) direct line, (ii) volume zero, and, (iii) modular volume [205]



Figure 2.49: Temperature control system scheme (external loop) [206]

In a study by Mclarty, controls were utilized to mitigate the spatial temperature variation and the stall risk during the load following [181]. The results showed that using the combined feed-forward, PI and cascade control strategy, 4:1 (SOFC) turn-down ratio could be achieved and a 65% efficiency could be maintained throughout the operating regime. Fig. (2.50) and Fig. (2.51) show the different control strategies used for the hybrid system.



Figure 2.50: P-I feedback control loops for FC-GT control [181]



Figure 2.51: Control overview for synchronous SOFC-GT topping cycle with inlet guide vanes (IGV) and bypass [181]

Azizi et al. studied the surge for a 1.7 MW gas turbine for a stationary hybrid SOFC-GT

system using computational fluid dynamics tools [207]. Hildebrandt and Assadi conducted a the compressor sensitivity analysis associated with transient SOFC-GT hybrid system operation [208]. The reduced Moore and Greitzer model was used for the compressor modeling. The results showed that transient part-load operation was sensitive to the characteristics of the compressor speed-lines and the load change procedure. Fig. (2.52) shows the SOFC load change for a constant ratio of GT load to SOFC load. In another study, Hildebrandt et al. stated that at the shut-down with no control strategy, the slow thermal SOFC transients could result in compressor surge [209].



The National Energy Technology Laboratory developed an experimental facility entitled the Hyper Facility that is able to emulate hybrid power systems in the range of 300 kW to 900 kW. Tucker et al. were able to show that thermal management of the fuel cell improved through controlling the cathode air flow during load transient operation. The increased pres-

Figure 2.52: Stepwise SOFC load change for a constant ratio of GT load to SOFC load [208]

sure losses introduced by the heat recuperation and the large cathode volume between the compressor and the turbine, were challenging to manage to avoid compressor surge during the hybrid system startup [210]. In that study, compressor bleed air control was used to avoid compressor surge during the hybrid system startup.

Taccani and Micheli studied an experimental setup of an SOFC-GT hybrid system at the University of Trieste, Italy [211]. As a result of the relatively large volume of the pressurized portion of the plant and the shape of the stall characteristic of the compressors, they determined that fluid dynamic instabilities could happen in the plant. Mild compressor surge vents were detected in the off-design transient operation of the hybrid system during the plant dynamic control, start up and shut down, as shown for example in Fig. (2.53).



Figure 2.53: Simulated time profiles during a shut down test at valve positions  $\alpha_v=30$  deg standard configuration. (a)  $\beta_p$ ; (b) compressor flow rate; (c) turbine flow rate [211]

Sieros and Papailiou examined the gas turbine behavior at the design point and the part-load

operation regimes of a hybrid SOFC-GT system [212]. They mentioned that the prediction of surge was not reliable on the 1-D simulation basis (i.e., the actual surge margin might be smaller than the predicted one of the 1-D simulation). They suggested using components with variable geometries in their study.

# 2.9.4 Computational stall/surge analysis in hybrid SOFC-GT systems

Placing the fuel cell in the high pressure section between the compressor and turbine increases the fuel cell efficiency by increasing the reactant partial pressures and lowering some polarization effects. The topping cycle design that is used for dynamic simulations in this study, introduces the need for a pressure vessel of significant volume and increases the potential for compressor stall/surge. Under steady-state conditions the compressor supplies a specific mass flow rate of air at every combination of shaft speed and pressure ratio. These values are typically normalized and compiled into tables or plotted in compressor maps. Compressor performance in gas turbines is limited by two main lines that are typically plotted on compressor maps: 1) a choke line at high air flow rate and, 2) a surge line at low air flow rate. The surge limit depends upon the compressor design and system configuration and especially upon the pressure dynamics downstream of the compressor. The dynamics of compressor surge/stall are significantly affected by introducing a fuel cell in the place of a combustor, making it difficult to predict surge. Reaching the surge limit might reduce the compressor performance temporarily or permanently and could introduce violent pressure and physical perturbations during stall/surge operation that could damage fuel cell. Therefore, control strategies are needed to keep the compressor performance in safe operating condition away from surge line (often called the surge margin). At specific pressure ratios and shaft speeds compressor surge occurs when reversal of flow direction is caused by excess back pressure on the compressor. The series of operating points that result in a surge event are collectively grouped into the surge line that is plotted on compressor maps [190]. Such surge events are often followed by compressor stall and highly dynamic and stressful compressor conditions that can cause a complete mechanical failure of th fuel cell, gas turbine and/or the entire hybrid system. Researchers at the National Energy Technology Laboratory (NETL) have showed the benefits of compressor bleed and cold air bypass for controlling the compressor mass flow rate during transient behavior [38]. The HYPER hybrid system simulation facility was able to emulate hybrid systems in the range of 300 kW to 900 kW. The thermal management of the fuel cell improved through controlling the cathode air flow during the load transient operation. The increased pressure losses introduced by the heat recuperation and the large cathode volume between the compressor and the turbine, were challenging during the hybrid system startup [210]. In that study, the compressor bleed air was used to avoid the compressor surge during the hybrid system startup. Ferrari et al. designed and installed an SOFC-GT physical emulator in the framework of a European Integrated Project [205]. The focus of their study was to minimize the viscous pressure loss in order to: 1) Reduce the unbalance between the compressor and the expander, 2) Maintain an accurate measurement, and 3) Have an effective plant efficiency. A modular high temperature volume was designed using computational fluid dynamics (CFD) tools to achieve a high uniformity in the flow distribution inside the volume and to minimize the pressure losses. The paper concluded that surge occurred during the shutdown for a particular configuration. In another study, strategies to avoid surge or excessive stress during the start-up and shutdown phases were proposed [206], which found that a new control strategy was required for managing the valve responsible for volume inlet temperature ramp during the hybrid system start-up and shutdown emulation. McLarty et al. studied the dynamic operation of an SOFC-GT topping cycle and showed that the pressurized hybrid topping cycles exhibited increased stall/surge characteristics particularly during off-design operation [131, 181]. In another study by McLarty et al. controls were utilized to mitigate the spatial temperature variation and the stall risk during load following [181]. The results showed that using the combined feed-forward, PI and cascade control strategy, 4:1 (SOFC) turn-down ratio could be achieved and a 65% efficiency could be maintained. Stiller et al. suggested that specific incidents should be avoided for safe operation of hybrid systems [189]. Some of these incidents are: compressor stall/surge or cell degradation due to thermal cracking or high temperatures, carbon deposition and anode compartment blocking, and backflow of gas from the burner to the anode, exposing the anode to oxygen. In that study, a new control strategy for managing the valve was used to generate the requested inlet temperature ramp during the hybrid system start-up and shutdown emulation. Roberts et al. have mentioned some important disturbances in the hybrid carbonate fuel cell-gas turbine system due to the changes in the ambient temperature, fuel flow variation induced by supply pressure disturbances, fuel composition variability, and power demand fluctuations [194]. In that study, the predicted fuel cell operating temperature, fuel utilization, fuel cell and GT power, shaft speed, compressor mass flow and temperatures in the cycle were considered as the controlled response to the fuel cell voltage increase. Panne et al. demonstrated the steady state analysis of an SOFC-GT hybrid cycle test rig [213]. The cycle could be evaluated without the risk of damaging the cell. The effects of the ambient conditions or the pressure losses were investigated. The maximum compressor pressure ratio, the supplemental fuel mass flow and the SOFC air bypass were the three different limitations in the choice of cycle configuration. The additional pressure losses and piping had significant impact on the surge margin. Hilderbrandt studied the compressor sensitivity analysis of the transient SOFC-GT-HS operation [208]. The reduced Moore and Greitzer model was used for the compressor modeling, showing that the transient part-load operation was sensitive to the characteristics of the compressor speed-lines and the load change procedure. In another study, it was stated that at the shutdown with no control strategy, the slow thermal SOFC transients could result in the compressor surge [209]. Stiller studied a multi-loop control strategy for hybrid SOFC-GT system [189]. Fuel flow could be

controlled by controlling the fuel valve. Air flow could be controlled by controlling the shaft speed, variable inlet guide vanes or variable compressor bleed. Their effects on the system have been reported to be similar. In the mentioned study, shaft speed control was selected. Power was controlled by manipulating the SOFC current, fuel utilization was controlled by manipulating the fuel flow, air flow was controlled by manipulating the shaft speed and cell temperature was controlled by adjustment of the air flow setpoint. Taccani et al. studied an experimental setup of SOFC-GT-HS at University of Trieste, Italy [211]. As a result of the relatively large volume of the pressurized portion of the plant and the shape of the stall characteristic of the compressors investigated, the fluid dynamic instabilities were found to occur in the plant. A surge could be detected in the off-design transient operation of the hybrid system during the plant regulation, start-up and shutdown. Sieros et al. examined the gas turbine behavior at the design point and the part-load operation regimes [212]. They mentioned that the prediction of surge was not reliable on the 1-D basis (i.e., the actual surge margin might be smaller than the predicted one). Using the components with variable geometries was suggested in that study. The literature suggests that two kinds of stall/surge are common in industrial compressors, which are labeled as "deep surge and mild surge. Deep surge is the result of complete reversal of flow in the compressor impeller at a specific time. This type of surge significantly reduces the compressor performance which could result in the complete system failure. The other more common type of the compressor surge is mild surge which is characterized by an oscillatory mass flow rate at the impeller inlet and outlet caused by partial reversal of flow which causes reduced performance and efficiency of the compressor. However, mild surge is not as severe as deep surge.

#### 2.9.5 Gas turbine and compressor models

Gas turbine systems are the most common technology for producing power around the world today. Different types of turbo-machinery are operated today including those using water in a hydroelectric plant, steam in nuclear and coal plants (and some gas plants using the Rankine
cycle), and air, such as those used in natural gas-fired combined cycle plants and jet-fueled aircraft. Computer programs that calculate the performance of gas turbines typically need a description of the turbine and compressor performance as a function of speed and mass flow or pressure (usually provided in the form of maps) as an input. These maps are either calculated or derived from a turbine rig test. The data from the turbine rig test usually are not evenly distributed over the tested speed range and sometimes the distance between speed lines is large. As a result, interpolation and extrapolation of the measured data is often required [214].

For the gas turbine transient model developed by Brouwer et al., calculations were performed at each time step [30]. Eq. (2.37) and (2.38) have been used to simulate the gas turbine shaft speed dynamics given the dynamic turbine and the compressor powers ( $P_T$  and  $P_C$ ), rotational inertia J, and rotational speed  $\omega$  as follows:

$$\frac{d\omega}{dt} = \frac{1}{J\omega} (P_{T_1} - P_C)$$
(2.37)

For hybrid systems that considered a the second turbine (i.e., power-only turbine without compressor), the same equations have been used in order to calculate the temperatures and the enthalpies. The second shaft had the generator load instead of the compressor load as shown in Eq. (2.38):

$$\frac{d\omega}{dt} = \frac{1}{J\omega} (P_{T_2} - P_{Load})$$
(2.38)

In the study by Brouwer et al, the generator operated at 3600 RPM for 60 Hz AC electricity production. Thus, the rotational speed of the turbine was adjusted and maintained by controllers to a value as close as possible to 3600 RPM. A transient gas turbine model was developed in their simulation of the hybrid Siemens Westinghouse pressurized system. The dynamic expressions that account for gas compressibility and mass storage have been solved in different diffuser volumes as shown in Fig. (2.54).



Figure 2.54: Dynamic simulation approach of gas turbine and compressor [30]

During the simulation, the generator load was applied to the turbine shaft. Their model was flexible in importing the empirical data of any gas turbine operation. The semi-empirical data that was used in their model was in the form of non-dimensional compressor and turbine maps. These maps provided steady state mass flow, pressure ratio and efficiency as a function of the rotational speed of the shaft. The first map plotted the pressure ratio versus dimensionless mass flow at a fixed rotational speeds. The second map gave the normalized isentropic efficiency versus dimensionless mass flow at a fixed rotational speed. The non-dimensional mass flow in that study was defined as in Eq. (2.39):

Non-dimensionalized mass flow rate= 
$$\frac{\dot{m}R\sqrt{\gamma RT_{01}}}{D^2 P_{01}}$$
 (2.39)

Where  $\dot{m}$  is the fluid mass flow, R is the universal gas constant,  $\gamma$  is the ratio of the spe-

cific heats,  $T_{01}$  and  $P_{01}$  are the stagnation temperature and pressure at the inlet and D is a characteristic length. Dimensionless rotor speed has been defined in the form of Eq. (2.40):

Dimensionless rotor speed = 
$$\frac{ND}{\sqrt{\gamma RT_{01}}}$$
 (2.40)

Where N is the rotational speed. For any inlet condition  $(T_{01}, P_{01})$ , discharge pressure and speed, the mass flow rates were determined from the turbine and the compressor maps. An iterative solution method was used until the pressure ratio guessed matched the ratio of the discharge pressure to the inlet pressure. After finding the mass flow rate, the isentropic efficiency of the turbine and the compressor was found from the second map. Knowing the isentropic efficiency, the compressor and the turbine exit temperature were determined from the isentropic efficiency relations. The exit temperatures were found from Eq. (2.41):

$$T_{02} = T_{01} \left( 1 + \frac{1}{\eta_{comp}} \left( \left( \frac{P_{02}}{P_{01}} \right)^{\frac{\gamma - 1}{\gamma}} - 1 \right) \right)$$
(2.41)

The specific heat was determined as a function of temperature for the gas mixture containing the seven species. The compressor work was calculated as in Eq. (2.42):

$$P_c = \dot{m}_{Comp}(h_{01} - h_{02}) \tag{2.42}$$

Chan et al., have used centrifugal compressors and axial turbines in their model [64]. Fig. (2.55) demonstrates the compressor-SOFC stack-combustor-gas turbine configuration in their study.



Figure 2.55: Schematic of a compressor-fuel cell-combustor- gas turbine engine used in [64] The actual work demand of the compressor was determined using Eq. (2.43):

$$\frac{\Delta h_{c,a}}{\theta_{01}} = \frac{c_{pc} T_{std}}{\eta_c} \left[ \left(\frac{p_{02}}{p_{01}}\right)^{(k-1)/k} - 1 \right]$$
(2.43)

Where, std represents the standard conditions and  $\theta_{01} = T_{01}/T_{std}$ . The actual power of the gas turbine was determined using Eq. (2.44):

$$\frac{\Delta h_{gt,a}}{\theta_{03}} = c_{pt} T_{std} \eta_t \left[ 1 - \left(\frac{p_{02}}{p_{01}}\right)^{(1-k)/k} \right]$$
(2.44)

Where,  $\theta_{03} = T_{03}/T_{std}$ . It was assumed that the heat capacity of the compressor and the

turbine are the same. The power output of the power turbine was in the form of Eq. (2.45):

A 7

$$\frac{\Delta h_{pt,a}}{\theta_{04}} = c_{pt} T_{std} \eta_{pt} \left[ 1 - \left(\frac{p_{04}}{p_{05}}\right)^{(1-k)/k} \right]$$
(2.45)

In the study by Chan et al. [64], typical compressor/turbine maps (DLR centrifugal compressor and NASA-CR-174646 axial turbine) have been used in order to verify the operation characteristics of the turbo-machines. In the described configuration, the speed of the compressor was the same as the gas turbine speed. The simulation of a smaller or larger power plant, only required the standard mass flow rate to be changed.

A compressor supplies a specific mass flow rate of air at every combination of shaft speed and pressure ratio. These values are often normalized and compiled into tables or plotted on maps. At specific pressure ratios and shaft speeds, compressor surge occurs. Compressor surge is known as the reversal of flow direction due to the excess back pressure on the compressor and could cause a complete failure of the gas turbine. The series of operating points that result in the surge are collectively grouped into the surge line and added to the compressor map plots. The shaft speed, the pressure ratio and the flow rate as plotted in these maps are normalized using Eq. (2.46) to (2.48) [190]:

$$N_{RPM} = \frac{RPM}{\sqrt{\frac{T_{stag}}{T_{des}}} \cdot RPM_{des}}}$$
(2.46)

$$N_{Flow} = \frac{Flow}{Flow_{des}} \cdot \frac{\sqrt{\frac{T_{stag}}{T_{des}}}}{\frac{P_{in}}{P_{des}}}$$
(2.47)

$$PR = \frac{P_{out}}{P_{in}.PR_{des}}$$
(2.48)

Where, the parameters were defined by McLarty using the Eq. (2.49) to Eq. (2.52):

Stagnation temperature: 
$$T_{stag} = T_{in}.(1 + M^2(\frac{\gamma - 1}{2}))$$
  
(2.49)

Mach Number: 
$$M^2 = \frac{R_u \gamma T_{in}}{M V_{in}^2}$$
 (2.50)

Velocity: 
$$V_{in} = \frac{\dot{n}R_u T_{in}}{A_{in}P_{in}}$$

(2.51)

Specific gas constant: 
$$\gamma = \frac{C_p}{C_v} = \frac{C_p}{C_p - R_u}$$
 (2.52)





Figure 2.56: Turbomachinery Interpolation strategy [190]

Where the parameters defined by McLarty et al. are shown in Table. (2.5):

Parameter	Description
N <sub>RPM</sub>	Normalized Shaft Speed
$N_{Flow}$	Normalized Flow Rate
RPM	Actual Shaft Speed
$RPM_{des}$	Design Shaft Speed
Flow	Actual air flow rate
$Flow_{des}$	Design Air Flow Rate
$T_{in,des,stag}$	Inlet, Design or Stagnation Temp
P <sub>in,out,des</sub>	Inlet, Outlet or Design Pressure
PR	Normalized Pressure Ratio
$PR_{des}$	Design Pressure Ratio
M	Molar Mass
Vin	Inlet Velocity
'n	Actual Flow Rate
A <sub>in</sub>	Cross Sectional Area of Inlet

Table 2.5: Turbomachinery parameters [190]

The input parameters for the compressor were the ambient temperature, the species concentrations, the shaft speed and the inlet/exit pressures. For the compressor, two energy conservation models were considered by McLarty [190]. The first was regarding the working fluid and the second included the compressor solid mass demonstrated in Eq. (2.53) and (2.54).

$$\frac{dT_g}{dt} = \frac{\dot{W}_C + (h.\dot{n})_{out} + h_c A_{sur}(T_s - T_g)}{C_p \cdot \frac{P_{out}V}{R_I T_q}}$$

$$\frac{dT_s}{dt} = \frac{h_c A_{sur}(T_g - T_s) + \epsilon \sigma A_{sur}(T_{amb}^4 - T_s^4)}{C_p . m}$$
(2.54)

(2.53)

Where, the compressor work demand and the isentropic temperature were determined from Eq. (2.55) and Eq. (2.56):

$$\dot{W}_C = \dot{n}_{out} \cdot \left(\frac{h_{isen} - h_{in}}{\eta_{isen}}\right)$$
(2.55)

$$T_{isen} = \left(PR.PR_{des}\right)^{\frac{\gamma-1}{\gamma}} \tag{2.56}$$

Table. (2.6) demonstrates the compressor parameters used in the study by McLarty [190].

Parameter	description
$\dot{W}_C$	Shaft Power
$h_{rac{in}{out}}$	Flow Enthalpy
$\dot{n}_{rac{in}{out}}$	Flow Rate
$h_c$	Convection Coefficient
$A_{sur}$	Surface Area
$T_{s,g}$	Solid and Gas Phase Temperature
$T_{g}$	Air Flow Temperature Out
$T_{isen}$	Isentropic Temperature
V	Volume of Compressor
$\epsilon$	Emissivity of Metal
σ	Boltzman Constant
m	Mass of Compressor

Table 2.6: Compressor parameters [190]

Typically, a micro-turbine generator (MTG) is a relatively small gas turbine power generator made of several components including: centrifugal compressor, inflow expander, combustion chamber, recuperator, centrifugal turbine, electrical generator and natural gas compressor. The simulation of such an MTG compressor module has been accomplished by McLarty based on the experimental maps (efficiency and pressure ratio versus non-dimensional flow rate) [190]. The input data of the compressor module were: the air inlet pressure and temperature, rotational speeds and the first guess pressure ratio. Turbine modeling was similar to the compressor modeling with different known initial conditions. The known parameters for the turbine were the mass flow rate and the inlet temperature. The outlet pressure of the turbine was known from the back calculation of the downstream components of the system. Hence, the turbine inlet temperature, the shaft power produced, turbine outlet temperature and the inlet pressure could be calculated. The inlet pressure of the turbine was calculated iteratively. The inlet pressure was used to find the pressure ratio, and was applied to the turbine map to find the mass flow rate which was iteratively solved to match the incoming flow to maintain a constant pressure at any given time step. Axial and radial turbomachinery can operate the compressor and turbine on a single shaft. In this case, the turbine and the compressor are rotating at the same shaft speed. Typical electric generating turbomachinery operates synchronously at some multiple of 60 Hz (50 Hz in Europe), or asynchronously, requiring power conversion, inversion, and/or conditioning devices to prepare the electricity for interconnection with the grid network. Knowledge of the turbomachinery moment of inertia has been reported to be a significant factor for simulating high speed dynamics [190]; determining how quickly it will spool up or down in rotational speed, and affecting stall/surge behavior. The dynamic rotational speed operation of the shaft has been solved by McLarty is in the form of Eq. (2.57):

$$\frac{d\omega}{dt} = \frac{\dot{W}_t - \dot{w}_c - \dot{w}_{gen}}{\omega I_0}$$
(2.57)

Azizi et al., have studied the dynamics of a gas turbine in a hybrid SOFC/GT configuration using computational fluid dynamics (CFD) results [215]. A pressure step corresponding to a hybrid system dynamic perturbation was applied to the CFD model in order to examine the potential surge response in the compressor. Fig. (2.57) shows the results of that study for a dual spool centrifugal compressor analysis.



Figure 2.57: Dual spool compressor pressure profile during mild surge following a pressure step dynamic perturbation [215]

# 2.10 OPTIMAL CONTROL AND RELIABILITY ANALYSIS OF STATIONARY HYBRID SOFC-GT POWER GENERATION

### SYSTEM

One main purpose of a SOFC-GT hybrid system implementation is for distributed power generation applications. Therefore, this study investigates the possible extension of a SOFC-GT hybrid system to multi-MW power cases. Based on commercially available gas turbines, control strategies for SOFC-GT hybrid system are investigated for different stationary applications in distributed generation. Risk analysis of surge in hybrid SOFC-GT power system is assessed while operating in transient pre-load and post-load mode. Possible cycle analyses including different types of reformer (SMR and CPOX) and different cycle configurations (anode recirculation included and without anode recirculation) are compared in this study. The focus of this paper is reliability analysis of Hybrid SOFC-GT system while operating in grid-connected mode. Optimal PID control algorithms have been developed in order to predict the system behavior in sudden load demand changes. Possible integration of hybrid

SOFC-GT system with other components of distributed generation system (Chiller, thermal storage, batteries, solar PVs and wind turbines) is discussed in this paper and the effect of these components on the hybrid SOFC-GT system behavior, specifically regarding stall/surge phenomenon is discussed. Several different cases such as base load, diurnal peaking, energy storage shift and load following have been studied in order to predict the hybrid system behavior. High surge risk of gas turbine is associated in pre-load to post-load transition.

### 2.10.1 System control strategies

Controlling SOFC-GT systems has several challenges that are quite thoroughly considered and addressed in the literature. For example, control strategies have been proposed to minimize the transient SOFC temperature gradients during start-up and shut-down procedures, follow rapid load (power demand) transients, compensate for load disturbances, control the SOFC temperature during part-load and dynamic operation, independently control the air flow and temperature entering the SOFC, manage power transients while controllers are in conflict (e.g., power demand increases requiring higher air flow which reduces power output from the turbo-machinery), maintain the turbine speed, handle and utilize the large thermal mass of the SOFC, and address the power partitioning issue between the SOFC and GT. Roberts et al., have mentioned some important disturbances in a hybrid carbonate fuel cellgas turbine system due to changes in ambient temperature, fuel flow variation induced by the supply pressure disturbances, fuel composition variability, and power demand fluctuations [194]. In that study, the predicted fuel cell operating temperature, fuel utilization, fuel cell and GT power, shaft speed, compressor mass flow and temperatures in the cycle were considered the controlled responses to a fuel cell voltage increase perturbation (current decrease perturbation). Fig. (2.58) and Fig. (2.59) show the cascade controller design and catalytic oxidizer control scheme, respectively used by Roberts et al.



Figure 2.58: Cascade controller design [194]



Figure 2.59: Catalytic oxidizer control scheme [194]

Kemm et al. investigated the temperature limitations of SOFC in transient and steady state operation of the hybrid system [216]. In order to minimize the transient SOFC temperature gradients during start-up and the shut-down procedures, a stepwise heat-up and cool-down procedure was proposed. The time needed for the hybrid system start-up and shut-down was affected by the slow response characteristics of the SOFC that were limited by temperature stress considerations. Mueller et al. presented a control design for a bottoming 275 kW SOFC-GT hybrid system. Their dynamic model captured all the physics sufficient for the dynamic simulation of the processes that affected the system with time scales greater than

10 ms [217]. In another study by the same group, it was demonstrated that the hybrid system could be controlled to reach the transient capability greater than the Capstone 60 kW recuperated gas turbine engine alone [218]. The characteristic voltage transient due to the changes in the SOFC exit hydrogen concentration had a time scale that was shown to be on the order of seconds and the characteristic temperature transient was on the order of hours [219]. In another study by the same group, a control strategy was developed for rapid load following of a hybrid SOFC-GT system [220]. The control strategies were analyzed in a quasi-two-dimensional integrated dynamic system model that captured the physics of mass convection, electrochemistry, chemical kinetics and heat transfer. The maximum instantaneous current increase that the SOFC could safely manage was quantified based upon several parameters [221]. Fig. (2.60) shows the load increase with compensated fuel flow combustor temperature control, current fuel cell power control and blower power buffering.



Figure 2.60: A kilowatt per second 2.4-4.8 kW load increase with compensated fuel flow combustor Kandepu et al., developed control relevant models for an autonomous SOFC-GT-based pow-temperature control, current fuel cell power control and blower power buffering [221]



Figure 2.61: SOFC-GT hybrid system integrated with autonomous power system [222]

It was reported that a load change could affect the SOFC temperature that affects the SOFC material durability. A control system was designed in order to compensate for the load disturbances. Fig. (2.62) shows the PI control structure of the strategy proposed by Kadepu et al.. Fuel Utilization (FU) and SOFC temperature were used as set points in that study. In another study, Kandepu et al. included the important interactions between the SOFC-GT hybrid system and the grid in their model. The study showed that the system could be controlled using blow-off to control the SOFC temperature during the part-load operation, although efficiency was reduced under these conditions [223].



Figure 2.62: PI control structure [222]

Fig. (2.63) and Fig. (2.64) shows the output and input of controller design.



Figure 2.64: Control inputs variation during simulation [222]

A multipurpose real-time (RT) model was developed for SOFC hybrid systems by Ghigliazza

et al. [224]. The developed model was compared to the experimental data from the startup heating phase of an SOFC hybrid system and the results were found to be satisfactory, avoiding surge/stall events. Xu et al. proposed a power tracking control method to address



Figure 2.65: The proposed power tracking control strategy [225]



Figure 2.66: Control diagram of power tracking control [225]

Luecht et al. presented a dynamic model of the pressurized SOFC system that integrated several control loops for fuel and air and power management [226]. The system must be able to operate safely (that is, avoiding fuel starvation) while fuel utilization should be maintained as high as possible to achieve high system efficiencies. When controlling the voltage of a solid oxide fuel cell to achieve these conditions, it is important to keep the voltage above the electrochemical nickel oxidation voltage in order to avoid irreversible anode degradation. Tsourapas et al. mentioned the challenges in the transient load following due to the intricate coupling dynamics of the SOFC and GT [227]. In that study, an IS-RG (Incremental step reference governor) closed-loop reference governor controller was proposed to address the challenges associated with the power shut-down during a sudden load change in the generator. Fig. (2.67) shows the schematic of the closed-loop SOFC/GT plant with the IS-RG controller.



Figure 2.67: Schematic of the closed-loop SOFC/GT plant with the IS-RG controller [227]

In a recent study by Baudoin et al., a hybrid power system was controlled by single Three-Level Neutral Point Clamped (3LNPC) inverter [228]. Digital R-S-T type controllers were used to regulate the SOFC power in DC side of the inverter.



Figure 2.68: SOFC-GT hybrid system [228]

The control strategy was designed to manage the SOFC-GT by using only one converter between the hybrid power system and the microgrid. Two main objectives of the study were: 1) The DC side controller had to regulate the SOFC power by offset and, 2) The AC side controllers had to regulate the AC voltage and frequency through the duty cycles.



In another study by Vechiu et al., a control strategy was designed in order to allow managing the power produced by two separate sources to meet the power demand [229]. In another study by the same group (Camblong et al.), a control model was identified and a robust digital controller was designed using the Tracking and Regulation with Independent Objectives method [230]. Larosa et al., used two model predictive control (MPC) systems instead of a traditional PID control system [231]. Fuel cell power and cathode inlet temperature were the controlled variables. Fuel cell bypass flow rates, current and fuel mass flow rates were the manipulated variables. The MPC control method was tested against the PID controllers method. The MPC controller was able to reduce the mismatch between the actual and the target values of the cathode inlet temperature from 7 K maximum of the PIC controller to 3 K maximum, and showed more stable behavior in general.



Figure 2.70: System emulator layout and interface to the fuel cell stack real-time model [231]

Jia et al. proposed a sprinter SOFC-GT system to meet the fast and efficient load-following [193]. Ferrari presented a control tool which combines feed-forward and standard proportionalintegral techniques, and controls the system during load-following thereby avoiding failures and stress conditions [191]. Using the new control system, a better performance was achieved in controlling the fuel cell temperature (maximum temperature gradient was reduced). The control system also allowed for the pressure gap between the anode and cathode to be reduced during the transient operation, and a higher safe margin for the Steam-to-Carbon ratio was generated. Wu studied the control design of hybrid SOFC-GT system combined with compressed-fuel processing unit (CFPU) [232]. Fig. (2.71) shows the flue gas temperature control loop in the hybrid SOFC-GT system consisted of temperature transmitter (TT), temperature controller (TC) and a heater that was added to control the flue gas temperature by manipulating the external energy duty ( $Q_H$ ).



Figure 2.71: Flue gas temperature control loop in hybrid system [232]

Milewski et al. determined the ranges of possible system operation conditions of the SOFC-HS with part- and over-load operation, and adequate maps were given and described [233]. Effects of SOFC exhaust gas recirculation on hybrid system performance were studied by Saebea et al. [234]. In another study, the inlet fuel composition effect on the hybrid system performance was studied by Zabihian et al. [235]. The analysis of the operation of the system when fueled with a wide range of fuel types demonstrated that the hybrid SOFCGT cycle efficiency can be between 59% and 75%, depending on the inlet fuel type. Oh et al. studied the power shutdown when the load was changed abruptly [236]. They studied the operating parameters of the 5kW-Class SOFC-GT hybrid system in single-shaft and dual-shaft gas turbine designs. Under the same load change condition, the responses to the load change for the dual-shaft design were more robust against shutdown than the single-shaft design. McLarty et al., compared their hybrid simulation results to dynamic experimental data and showed a favorable agreement [237]. The predictions of the component temperatures, pressures, voltage and system power showed 5°C, 2 kPa, 2 mV, and 0.5% errors, respectively. They found that a  $15^{\circ}C$  ambient temperature perturbation caused a  $30^{\circ}C$  variation in the stack temperature.

Stiller et al. studied a multi-loop control strategy for a hybrid SOFC-GT system [189]. Fig. (2.72) shows the corresponding power plant. Fuel flow is controlled by manipulating the fuel valve. Air flow is controlled by manipulating generator power to affect the shaft speed, or by manipulation of variable inlet guide vanes or variable compressor bleed. The effects of each of these control strategies on the system performance is reported to be similar. In the mentioned study, shaft speed control by generator power manipulation was selected as preferred [189].



Figure 2.72: Hybrid cycle layout [189]

Control design objectives were mentioned by Stiller et al. as follows: 1) Safe operation

of the system: Avoiding incidents that can damage fuel cell or system such as compressor surge. 2) Quick load following and high efficiency, 3) Long life-time of fuel cell, and 4) Governing external influences such as compressor fouling or fuel cell degradation. Fig. (2.73) shows the multi-loop control strategy used by Stiller et al.. Power was controlled by manipulating SOFC current, Fuel utilization was controlled by manipulating the fuel flow, air flow was controlled by manipulating the shaft speed and cell temperature was controlled by adjustment of air flow setpoint.



Figure 2.73: Control system of hybrid system [189]

## 2.11 HYBRID SOFC-GT SYSTEM OPTIMIZATION

Several authors have accomplished studies on hybrid SOFC-GT optimization. Yi et al. studied a system consisting of an IR-SOFC and an inter-cooled gas turbine (ICGT) [174]. An optimization strategy including the design of experiments (DOEx) was applied to the hybrid system. The optimization results demonstrated that an electrical efficiency higher than 75% was achieved when the system was designed to operate under 50 bara pressure and with low percent excess air (55%) in the SOFC. Increase in the operating pressure increased the overall system efficiency. Calise developed a thermodynamic model of the hybrid system by introducing capital cost functions [238]. The synthesis/design (S/D) optimization of the plant was accomplished based on the traditional single-level approach based on a genetic algorithm. Their results showed that optimization of the stack as an isolated device should be avoided, due to the significant inefficiencies in the turbomachinery and the balance of plant (BOP). McLarty et al. used seven different design parameters for the design optimization of sub MW and 100 MW systems with efficiencies more than 70% [239]. Their study confirmed that the systems that required less cathode recirculation and produced most of the net power in the fuel cell, achieved higher efficiencies. In one study, the results showed that the final optimal design of the plant leaded to an exergetic efficiency of 65.11% [240].

Several researchers performed thermo-economic optimization on the SOFC-GT hybrid systems [241, 242, 243, 244, 182, 245, 246, 247]. Auttssier et al. used the thermo-economic multi-objective optimization approach to compute the integrated system performance, size and cost [241]. The study had two optimization objectives: minimizing the specific cost and maximizing the efficiency. The results proved systems could be created at costs from 2400\$/kW at 44% efficiency to 6700\$/kW at 70% efficiency. In addition, high system efficiencies could be obtained with low fuel utilization. Cheddie et al. studied the SOFC indirectly coupled with a 10 MW power plant operating at 30% efficiency. The method of Lagrange Multipliers in the thermo-economic was used to optimize the system performance. The net power output of 18.9 MW at 48.5% efficiency was predicted [242]. Romano et al. performed analyses of integrated gasification fuel cells plant in which a simple gas turbine cycle operated in the hybrid cycle with a pressurized intermediate temperature SOFC, a coal gasification, a syngas cleanup island and a bottoming steam cycle, in order to optimize the heat recovery [179]. They calculated a net electric LHV efficiency in the range of 52%-54%. The best solution was the 26% bypass of the fuel to the gas turbine, operating the SOFC at

23 bar, and 60% fuel utilization. This lead to the highest plant efficiency at 54.29%. In one study, the turbine inlet temperature (TIT) was shown as the key parameter that limited the efficiency of the hybrid power plant [248]. Increasing the number of the cells, increased the TIT and the power generation efficiency of the hybrid cycle. At a fixed number of the cells, the operating temperature of the SOFC needed to be increased in order to achieve a higher electrical efficiency. Increasing the utilization factor improved the system performance. Additionally, an increase in the S/C ratio decreased the efficiency and the TIT. Shirazi analyzed the thermo-economic model of the IRSOFC-GT system. The genetic algorithm was used as an optimization algorithm [243]. Multi-objective optimization was used in that study. The exergy efficiency, total cost rate of the system and social cost of air pollution were considered as the objective functions. Exergy efficiency at the final optimal design point was at 66.06% for the objective function I, 57.64% for the objective function II, and at 65.60% for the multi-objective optimization. Bakalis optimized the compressor and the turbine components in the hybrid SOFC-GT system [249]. At full load operation the system achieved an exergetic efficiency of 59.8% [250]. For the part load operation, two control strategies were implemented by maintaining either the SOFC stack temperature or the turbine exit temperature constant [251]. Najafi studied the SOFC-GT system integrated with a multi stage flash (MSF) desalination unit [244]. A Multi-objective genetic algorithm (MOGA) was used to find the optimal design parameters of the plant. The exergy efficiency and the total cost rate of the system were considered as the objective functions. The optimal design resulted in 46.7% exergetic efficiency and a total cost of 3.76 million USD/year. The payback time of the design was about 9 years. The results showed that the MSF desalination unit was significantly irreversible with an exergy efficiency in the range of 3.05% to 3.61%.

Multi-objective optimization, optimal design analysis and Pareto optimization of a hybrid system has been investigated in several other studies [252, 253, 254, 255]. Sharifzadeh et al. developed an optimization framework that ensures process safety and simultaneously

optimizes energy-efficiency, quantified in economic terms [256].

Koyama et al. developed an internet-based modeling infrastructure called DOME (distributed object-based modeling environment) in order to create the integrated models from independent simulation models for power production technologies [257]. DOME was used to combine the SOFC-GT system with a power generation capacity and dispatch optimization model. The study concluded that the SOFC micro-turbine hybrid system might reduce the  $CO_2$  emissions in Japan by about 50% when a  $CO_2$  to cost ratio of 3000 ¥/t-C is adopted in addition to the removal of the lower limits for LNG and Oil.

Thermodynamic, kinetic, geometric and cost models of the hybrid SOFC-GT-steam turbine power plants were developed in the range of 1.5 MWe to 10 MWe [258]. A syngas-fed SOFC and an irreversible GT optimization model was studied by Zhao et al. [259]. The developed model was able to predict the performance characteristics of hybrid systems in the range of 2000 to 2500  $\frac{W}{m^2}$  with efficiencies between 50% and 60%.

Barelli et al., developed a complete dynamic model of a the hybrid system in order to optimize the plant components [260]. The interactions between the system components were analyzed during the transients and inertial effects of the gas turbine and the heat exchangers on the fuel cell were considered. The study concluded that the SOFC transient behavior was influenced by delays in the inputs (i.e. the cathode input air and the  $H_2$  flow rate). In addition, the SOFC current delivery was affected by a non-negligible delay in the case of the GT load following. Fig. (2.74) shows the hydrogen molar flow rate, SOFC voltage and current outputs during transient operation that Barelli et al. studied [260].



Figure 2.74: Hydrogen molar flow rate (a), SOFC voltage (b) and current (c) outputs (GT load steps: 37-22.5-44 kW) [260]

Kanarit et al. optimized the SOFC-GT performance using total cost rate and system efficiency as the objective functions [261]. Khani studied multi-objective optimization of a hybrid SOFC-GT system using a genetic algorithm to determine the optimal design point in which exergy efficiency was maximum [262]. Wu et al. showed that the IMC-based multi-loop control scheme can efficiently regulate the total system power and control  $CO_2$  emissions per kWh of electricity as well [263].

## 2.12 PARAMETRIC STUDIES

## 2.12.1 MAIN PARAMETERS FOR SOFC-GT HYBRID SYSTEM SIMULA-TION

One of the most detailed parametric SOFC-GT hybrid systems analyses found in the literature is the study by Chan et al., which used the parameters shown in Table. (2.7) to simulate a 1.3 MW IRSOFC-GT power plant with 40,000 tubular solid oxide fuel cells.

Reforming	Shifting
Air pressure ratio	5
Fuel pressure ratio	4
Stack air flow rate (kmol/h)	120
Cooling air flow rate (kmol/h)	50
Fuel (NG) flow rate (kmol/h)	10
Fuel utilization	0.85

Table 2.7: System operating specifications [64]

The main results of their simulations are presented in Table. (2.8):

Cell voltage (V)	0.684
Cell current density $(\frac{mA}{cm^2})$	205
SOFC stack AC power output (kW)	1084
SOFC stack working temperature (K)	1197.5
Plant exit gas temperature (K)	410
Plant exit gas pressure (bar)	1.06
Air compressor power (kW)	232
Fuel compressor power (kW)	11
Turbine inlet flow temperature (K)	1221
Power turbine AC output (kW)	262.5
Heat rate recovery (kW)	529
Plant electrical efficiency (LHV)	61.9%
Total plant efficiency (LHV)	86.4%

Table 2.8: System operating specifications and resulting system performance [64]

The results of the Chan et al. study prove the advantage of integrating a gas turbine as the bottoming cycle of an SOFC/GT hybrid to increase the net plant efficiency. The results showed that a total power of 505.5 kW was generated from the turbines, from which about 45.9% (232 kW) was used to drive the air compressor and 2.2% (11 kW) that was used to drive the fuel compressor. The net power output of the gas turbine was 263 kW (i.e., about 20% of the plant total electrical generation).

Calise et al. found that increasing the cell temperature would increase the operating voltage of the cell and described it using their simulated polarization curves [72]. This result has been achieved while keeping the other parameters constant (e.g. total pressure, hydrogen, water and oxygen partial pressures). Also, the cell voltage increased by raising the cell

operating pressure, or by reducing the anode water molar fraction. Increasing the operating pressure resulted in improved performance, even if more auxillary power was required for the compressors. In order to simplify the model, limiting current density was assumed to be constant. However, more detailed analyses by Chan et al., Costamagna et al., Tanaka et al., and Bedringaas et al. showed that the limiting current density increased by raising the operating temperature [64, 155, 264, 265, 266]. Their results showed that the activation loss of the cathode was much more than the anode loss. The goal of one study was to find the most irreversible components in the plant using second law of thermodynamics analyses [72]. In addition, the model determined the temperature, pressure, enthalpy, entropy, exergy and the gas compositions at each node of the cycle. The very high combustor exit temperature was notable in the system operation. The simulations showed that combustor temperatures could rise substantially using a low fuel utilization factor or a high working current density that generates large amount of heat. Some of the major parameters are shown in Table (2.9):

Combustor efficiency	0.98
Inverter efficiency	0.95
Pump isentropic efficiency	0.80
Fuel compressor isentropic efficiency	0.80
Air compressor isentropic efficiency	0.80
Gas turbine isentropic efficiency	0.80
Limiting current density (mA/cm2)	900
Internal current density (mA/cm2)	2
Methane inlet molar flow rate (kmol/s)	0.0028
Water inlet molar flow rate (kmol/s)	0.0057
Oxygen inlet molar flow rate (kmol/s)	0.0070
Cell operating pressure (bar)	7
Environment pressure (bar)	1
Environment temperature (C)	25
Fuel utilization factor	0.85
Minimum steam-to-carbon ratio	2
Cell current density (mA/cm2)	100
Anode thickness (cm)	0.010
Electrolyte thickness (cm)	0.010
Cathode thickness (cm)	0.190
Interconnection thickness (cm)	0.004
$\gamma_{anode}(mA/cm^2)$	$2.13 \times 10^7$
$\gamma_{cathode}(mA/cm^2)$	$1.49 \times 10^{7}$

Table 2.9: Hybrid system simulation parameters of Calise et al. [72]

Because of the unreacted streams in the reformer and the significant amount of  $H_2O$  produced in the anode compartment, the steam partial pressure was very high. The simulations have shown that the low amount of CO that was produced in the reformer and not reacted in the anode compartment was completely converted in the catalytic burner, and as a result raised the combustor exit temperature.

Zhang et al. modeled the SOFC of a hybrid system based upon the Exponential Decay Function and the Exponential Associate Function [267]. The model was developed using the Aspen Custom Modeler simulation tool and the current density of the SOFC was considered as a disturbance variable during the dynamic simulations. The simulation results showed that the SOFC exit temperature was directly related to the current density. However, the relation was inversed for the SOFC air inlet temperature and turbine inlet temperature. The effects of the oxygen utilization, fuel utilization, operating temperature and efficiencies of the gas turbine components on the system performance of the recuperative heat exchanger (RHE) and the exhaust gas recirculated (EGR) cycles were determined [268]. The study concluded that, increasing the fuel utilization or the oxygen utilization reduced the fuel cell efficiency but improved the system efficiency for both of the RHE and EGR cycles. Tsuji et al. introduced the concept of the Inter Cooled Multistage SOFC-GT hybrid system in order to maximize the fuel heat input to the system [269]. The combination of the F-class GT (TIT=1350°C) and a 5-stage SOFC configuration was used and a 77% efficiency based on the fuel LHV was achieved at a high pressure ratio. It was suggested that increasing the number of the SOFC stages allowed the input of more fuel into the SOFC leading to the increased system thermal efficiency.

In hybrid SOFC-GT systems, Calise et al. found that the air mass flow rate depends upon the electrochemical rate of reaction, cell temperature control, and combustion reaction requirements [72]. In that study, the lower air flow rate caused better performance mostly due to the higher stack temperature (the lower cooling effect of the air flow. The fuel to air ratio was an important factor, since operating in the unreasonable range could damage the cell material due to the higher temperature. The capital cost of the SOFC stack depended upon its operating temperature. The results showed that the plant irreversibilities could be reduced by operating the system at higher fuel-to-air ratio, mainly due to the increase in the stack temperature, which decreased the cell overpotentials. On the other hand, the higher SOFC temperature meant higher heat flow of the HRSG and as a result, higher exergy destruction in HRSG.

The study by Calise et al. proposed that the steam to carbon ration (S/C) had to be kept at low levels in order to achieve higher electrical and net efficiencies. Higher S/C ratio means more steam and more required heat that resulted in lower plant efficiency. Also, electrical efficiency decreased as a result of the higher S/C, which produced higher produce concentrations in the anode compartment. In a model presented by Ferrari et al. [192], a part of the anodic exhaust gases were fed to the anode inlet in order to generate the right temperature for the reforming reactions and avoid carbon deposition in the reformer and the stack. They found that if the S/C ratio was reduced too much, carbon deposition would damage both the reformer and the cell stack [192].

The purpose of most of the plant designs in the literature is to keep the fuel utilization factor at as high a level as possible. The results of the work performed by Calise showed that the higher fuel utilization caused higher efficiency and lower irreversibility destruction rate [72]. The higher  $U_f$  resulted in lower chemical energy available for the burner, thereby reducing the combustion irreversibilities. In general, the study concluded that increasing fuel utilization increases the net and electrical efficiencies.

Yi et al. showed performed a system optimization analysis using Stat-Ease and showed that the highest system efficiency can be achieved when the overall pressure ratio is high, excess air is low, and the pressure ratio of the LPC is low [174].

#### 2.12.2 EXERGY BASED ANALYSIS OF HYBRID SYSTEMS

Several researchers have accomplished exergy analyses of hybrid systems [72, 270, 271, 142, 69, 71, 70, 73, 75, 76, 78, 79]. Fig.(2.75) produced by Calise et al. is characteristic of the analyses which demonstrate that the components that involved chemical and electrochemical reactions, had the most irreversibility (exergy destruction) contributions to the plant (i.e., the SOFC stack and the catalytic burner, or combustor).



Destroyed Exergy Rate

Figure 2.75: Destroyed exergy rate of hybrid system components from Calise et al. [72]

Calise et al. reported that the ratio of the SOFC to the catalytic burner rate of exergy destruction (irreversibility) depended upon the fuel utilization factor since high fuel utilization results in less fuel left over for the burner to combust [72]. On the other hand, lower fuel utilization resulted in lower electrical power generation and overall lower first law efficiency. Gas turbine exergy destructions were not significant in the Calise et al. study because
of the high isentropic efficiency assumed for the compressor and turbine. The SOFC stack produced 985 kW of electrical power. The thermal, mechanical and electrical power generation/consumption details of the Calise et al. study are presented in Fig.(2.76). *Thermal/Mechanical/Electrical Power* 



Figure 2.76: Thermal/Mechanical/Electrical power generation/consumption by each component from Calise et al. [72]

The electrical and the net efficiency of the system was calculated at 55% and 65% by Calise et al. [72]. The stack performance was kept at a high level, as most of the power was produced by the stack. The shape of the polarization curve in that study showed that in order to achieve a high performance, it was necessary to keep the current density at a low value even if that resulted in a greater cell cost due to the larger cell area required. At lower current densities, a lower amount of heat was available, so that the cell exit temperature was lowered, which caused lower cell voltage as well. Moreover, lower current density caused a lower exergy destruction rate. Due to the small amount of mass flow rate in the fuel compressor, the fuel-gas heat exchanger, and the pumps, the exergy destruction in these types of components was typically found to be negligible. In another study, Dincer et al., studied exergetic performance of hybrid SOFC-GT system [270]. The energy and exergy

efficiency of the integrated system were reported to be 70% and 80% respectively.



Figure 2.77: Exergy destructions per mole of methane consumed for the devices in the integrated system for the illustrative example, where  $V_s$ =0.61 V [270]

Comprehensive analysis of an SOFC-GT hybrid system regarding energy and exergy analysis has also been accomplished by Hosseini et al. [271]. An increase in the steam pressure resulted in a lower steam mass flow rate generated in the heat recovery steam generator. Rao et al. proposed the second law efficiency in order to assess the performance of the electrochemical processes [272] as in Eq. (2.58):

$$\eta_{II} = \frac{\sum X_{out} + Q_{out}(1 - \frac{T_0}{T_{out}}) + W_{out}}{\sum X_{in} + Q_{in}(1 - \frac{T_0}{T_{in}}) + W_{in}}$$
(2.58)

Sedaghat concluded that the main exergy loss in a hybrid SOFC-GT system is associated with the external reformer [273].

#### 2.12.3 **OPERATING PRESSURE EFFECTS**

THe effects of pressure on the SOFC stack have been studied by several researchers. Burke showed an 1.2% absolute efficiency increase at 30 psia operation versus ambient pressure for a planar solid oxide fuel cell stack [274]. Gandiglio et al. showed that SOFC pressur-

ization is beneficial to plant performance and should be considered by plant manufacturers and SOFC technology developers in view of future ultra-efficient plants that convert NG into electricity [275]. Hashimoto et al. showed that the power density of the cell was improved by pressurization [276]. A study by Henke et al. showed that activation polarization was reduced with increasing pressure as adsorption of reactants on the electrode surfaces was enhanced supporting the charge transfer kinetics [277]. In another study, Henke et al. showed that the activation and concentration overpotentials are reduced with increasing pressure [278]. Results from another study by the same group showed that power density can be increased significantly (an increase up to 100% was measured) at constant efficiency [279]. The behavior of pressurized solid oxide fuel cells using reformates as fuel was also examined [280, 281].

Many researchers have modeled and tested the pressurized hybrid fuel cell and gas turbine system [282, 48, 50, 49, 283, 101, 196, 284, 285, 286, 287, 288, 289, 290]. Calise et al. studied the operating pressure variation effect on the hybrid plant keeping the other parameters constant. Increasing the pressure resulted in an increase in the system efficiency at a fixed temperature (for both the net and the electrical efficiencies). It also reduced of the exergy destructions. A higher operating pressure resulted in a higher cell voltage. Massardo et al. demonstrated that their system efficiency was in the range of 65 - 70% for the atmospheric cells and compared to the range of 74 - 76% for the pressurized cells [71]. A study by M-cLarty et al. showed that higher system pressure improved the voltage and the efficiency, but required sturdier components and axial flow geometry for the turbomachinery [239]. Singhal et al. showed that the pressurized operation of the SOFC-GT power system achieved an efficiency close to 70% which, resulted in the reduced fuel consumption and the reduced capital cost per unit of the power output [291]. Panne et al. discussed the selection of the atmospheric ic and the pressurized hybrid system based upon the Turbee T100 micro gas turbine and the tubular SOFC stack [292]. They studied both pressurized and atmospheric hybrid system. The pressurized cycle was preferred since the heat for the gas turbine had to be supplied by an expensive high temperature heat exchanger that had a low effectiveness compared to a standard heat exchanger. Improvement of the Nernst potential was another advantage of the pressurized system that was mentioned in that study. The same group, demonstrated the steady state analysis of an SOFC-GT hybrid cycle test rig [213]. The cycle could be evaluated without the risk of damaging the cell. The effect of ambient conditions and the pressure losses throughout the cycle were investigated. The maximum compressor pressure ratio, the supplemental fuel mass flow and the SOFC air bypass were the three different limitations in the choice of cycle configuration. The additional pressure losses and piping of the hybrid system had a significant impact on the surge margin.

Rao et al. analyzed the hybrid system as originally proposed by  $SureCell^{TM}$  [293]. The results of that analysis showed that the thermal efficiency of the cycle was relatively insensitive to pressure ratio, increasing from 65.5% to 66.6% based on the fuel LHV as the pressure ratio decreased from 15 to 6.5. In one study by Friedrich, results generally showed that the pressure influence is stronger at low pressures up to 0.5 - 1 MPa and weakens towards higher pressures [294]. Results showed that pressure can strongly influence the power density of SOFC. Henke et al. found that SOFC performance is strongly influenced by changes in operating pressure. Depending upon the operating conditions, SOFC power density can be strongly increased with increasing operating pressure [295].

## 2.13 $CO_2$ CAPTURE, SEQUESTRATION AND EMISSION RE-

#### DUCTION

One of the applications of hybrid SOFC-GT systems described in the literature involves power generation with capture and sequestration for emissions reduction. In SOFC systems with oxide ion conduction, fuel conversion takes place in the anode compartment to utimately produce a stream of and water.  $CO_2$  can be separated from most of the water by simply

cooling the stream to produce concentrated  $CO_2$  for sequestration. This is in contrast to systems in which air and fuel are mixed (e.g., combustion) to produce a very dilute  $CO_2$  stream (diluted mostly with nitrogen from the air), which separation process is energy intensive and costly. As a result, SOFC technology offers the potential for reducing the capture penalty in terms of efficiency and costs. Several researchers have conducted research on  $CO_2$  capture applications for SOFC-GT hybrid systems [296, 297, 298, 299, 300, 63, 156, 301, 185, 302, 303, 300, 145]. Park et al. integrated an SOFC and an oxy-fuel combustion technology [296]. Fig. (2.78) shows the system layout of that study. The system was compromised of an SOFC, gas turbine, oxy-combustion bottoming cycle, and the  $CO_2$  capture and compression process. The steam expander inlet temperature and the condenser pressure in the oxy-fuel combustion system were determined through parametric analysis. The integrated system could be designed to have almost the same efficiency as the simple SOFC-GT system. With the voltage at 0.752 V, temperature at 900°C and the pressure at 8 bar for the operating conditions of the SOFC, a system efficiency of 69.2% was predicted. The efficiency penalty due to the  $CO_2$  capture and compression was 6.1%. An optimal condensing pressure existed, as the condensing pressure needed to be as low as possible. On the other hand, lowering the condensing pressure increased the power consumption for the  $CO_2$  compression. The optimal pressure was found to be 20 kPa.



Figure 2.78: System layout of the IGCC system with pre-combustion  $CO_2$  capture [296]

Jansen and Dijkstra introduced hybrid SOFC-GT system as a promising solution for the high penalties associated with the  $CO_2$  capture in power generation systems [297]. The water gas shift membrane reactor burner (WGSMR-burner) concept was used in that study. The carbon capture penalty calculated in that study was less than 50% of the state of the art  $CO_2$ capture systems. Dijkstra studied several concepts including the pre-fuel cell  $CO_2$  capture, post-fuel cell  $CO_2$  capture and post fuel cell oxidation [298]. WGSMR-afterburner was used for the  $CO_2$  capture in the SOFC system. Thermodynamic analysis of the SOFC-based IGFC hybrid system with  $CO_2$  capture was performed by Spallina et al. [299]. The system efficiency reached was within the range of 47.1%-47.6% with  $CO_2$  capture, which was about 6% points less than the reference IGFC cycle. The system achieved 96.5% lower specific  $CO_2$  emissions. The oxy-fuel IGCC cycle with  $CO_2$  capture reached a net efficiency of 40.1% and 7.2% points lower than the reference IGCC under the same conditions. The hybrid system with  $CO_2$  capture was optimized by Möller et al. using a genetic algorithm

[300]. An electrical efficiency of more than 60% was obtained with part  $CO_2$  capture. Inui et al. studied the closed MHD/noble gas turbine cycle as a bottoming cycle as the temperature of the combustion gas reached about 2300 K [63]. The total thermal efficiency of the system using natural gas (methane) reached to 63.66% (HHV) or 70.64% (LHV). The efficiency was high compared to others in the literature, since the system included  $CO_2$  recovery. The inlet and outlet temperatures of the SOFC in that study were 1194 K and 1344 K, respectively. The inlet temperature of the closed cycle MHD generator was at 2280 K. Campanari studied  $CO_2$  separation in the SOFC-GT hybrid system, where  $CO_2$  was separated with absorption systems or with adoption of a second SOFC module as an afterburner [156]. The system achieved efficiency close to 70% with 90% CO<sub>2</sub> removal, without having high TIT and NOx emissions. The plant with unreacted fuel shift and absorption possessed a higher efficiency. However, the double-SOFC configuration demonstrated best performances in the case that the second SOFC produced positive power output. In another study, it was reported that the SOFC-GT hybrid systems with  $CO_2$  capture decreased  $CO_2$  emission to 13.4% of the traditional  $CO_2$  emission [304]. The Campanari group has studied SOFC power plants at the 100 MW scale with  $CO_2$  capture. The theoretical LHV efficiencies with and without CO2 capture exceeded 70% and 78% respectively [302, 303]. In another study, process simulation of an Intermediate-temperature  $(660 - 730^{\circ}C)$  SOFC system has been accomplished [305]. Hybrid SOFC-GT system with  $CO_2$  capture and a three-reactors chemical looping for hydrogen generation (TRCL) from natural gas using three reactors was studied [185]. They found that efficiency could reach up to 51.4% on an LHV basis. An interesting concept that includes  $CO_2$  capture has been presented by Li et al. [177], which integrates hydrogasification with an SOFC-GT hybrid system and steam bottoming cycle. They found that high methane content from the hydro-gasifier together with recirculation of hydrogen to the gasifier allowed the capture of  $CO_2$  with very little efficiency penalty. The overall efficiency range for the  $CO_2$  capture systems that Li et al. found was more than 60%.

#### 2.14 INVESTIGATION OF ALTERNATIVE FUELS

Several researchers have conducted hybrid system analysis using alternative fuels instead of natural gas or methane [306, 78, 94, 307, 308, 93, 100, 183, 184, 309]. Santin et al., studied a 500 kW class SOFC-GT system fed by kerosene and methanol fuels [306]. The WTEMP software developed by the University of Genoa was used for this purpose. Both tubular and planar SOFC were studied with different temperature rise along the air path. Compared to the methane-fueled case, the methanol-fueled systems demonstrated lower efficiencies (0.5-7 percentage points), but attractive economic performance (up to 0.5 years reduction in payback period (PBP)). The Kerosene fueled systems demonstrated lower efficiencies (0.5-15% points) and poor economic performance (at least 3.4 years increase in PBP). Fernandes et al. presented the results of the "Well-to-Wing" efficiency analysis of a liquid hydrogen produced by biomass gasification for aviation [78]. The system consisted of a biomass gasification plant, a hydrogen liquefaction plant, and an SOFC-GT hybrid system. The conventional hydrogen liquefaction process introduced a significant exergy destruction that resulted in a lower overall efficiency.

The integration of fluidized bed steam gasification of biomass and an IRSOFC-gas turbine hybrid cycle were studied using the IPSEpro software package [94]. The model of gasification and gas conditioning section in that study was based upon data from the 8 MW plant in Guessing/Austria. Electric efficiencies up to 43% were calculated for the combined heat and power application. Kaneko et al. studied the transient behavior of a biomass gas fueled SOFC-micro turbine system [307]. An unstable power output due to the fluctuation of the gas composition in the fuel was observed when the system was fed biomass gas. A fuel controller was used to follow the step change in the power demand from 32 to 35 kW, but also stably maintained the system power output at 35 kW during fuel composition changes. The SOFC and the MTG power contribution were 85% and 15%, respectively. The system

total efficiency was at 56.3% at the design point operating on methane. In addition, Kaneko et al. designed a controller for the hybrid system that enabled it to rapidly follow the power demand while maintaining correct system temperatures. A PID controller was used to manipulate the fuel flow rate to control the power output of the system.

Wongchanapai et al. studied a direct-biogas SOFC-micro gas turbine system to evaluate the potential use of biogas as the main source of energy for a direct-biogas SOFC-MGT hybrid CHP system [308]. The key parameters in that study were, the SOFC and reformer temperatures, the fuel utilization factor, the turbine inlet temperature (TIT) and the compression ratio. Steam was more preferable for the reforming agent of the SOFC regarding the material limitations and the SOFC efficiency compared to the air-steam mixture fraction. However, adding a small amount of air enhanced the useful heat output and generated electricity through the MTG without affecting the net system efficiency. Integrated biomass gasifier-SOFC-GT systems have been studied by several authors [178, 310]. Maximum energy and exergy efficiencies of the gasification-based system have been reported by Santhanam et al.. The energy and exergy efficiency for the SOFC-MGT cycle with biomass gasification were reported as 58.3% and 69.6% as reported by Hosseini et al. [310]. Four different systems based on SOFC-GT and biomass gasification were modeled in order to evaluate the influence of the gasification, gas cleaning and the system scale on the overall system performance by Toonssen et al. [93]. The results showed that a large scale system based upon the pressurized direct air gasification and high temperature gas cleaning had the highest electrical exergetic efficiency at 49.9%. The gasification technology had no significant effect on the system overall performance. In addition, the large-scale systems had higher efficiencies than the small-scale systems, due to larger exergy losses that were mainly associated with balance of plant components. The effect of different biomass gases on the hybrid system performance was studied by Lv et al. [183]. Electrical efficiency could reach up to over 50% with four types of gasified biomass studied in that paper. The system efficiency for the system fueled by wood chip gases was higher than the systems fueled by corn stalk gas, cotton wood gas and grape seed gas. The speed of the gas turbine had a significant impact on the hybrid performance such as the output power and efficiency. Hydrothermal gasification for the hybrid SOFC-GT cycle was studied by Facchinetti et al. [184]. The hydrothermal gasification required heat at 673-773 K, while the SOFC contained excess heat in this high temperature range due to the limited electrochemical fuel conversion. Thus, the integration of the two technologies was technically feasible. Wet waste biomass conversion into electricity had a first law efficiency of up to 63% while separating the biogenic carbon dioxide. An SOFCbased hybrid system integrated with a coal gasification process was studied by Romano et al. [311]. The proposed SOFC-based power system achieved the efficiency gain of 7 to 11 percentage points compared to the advanced IGCC based upon the state-of-the-art-technology. Methanol and di-methyl-ether (DME) fuels were used in a SOFC-MGT hybrid system studied by Cocco et al. [309]. Since the reforming temperature of methanol and DME (200-350°C) was lower than that of natural gas (700-900°C), the reformer could be located outside of the stack, which resulted in improved exhaust heat recovery and a higher voltage produced by the greater hydrogen partial pressure at the anode inlet for this case.

Martinez et al. compared the SOFC-GT freight locomotive fueled by natural gas and diesel with on-board reformation [5]. Route-averaged fuel-to-wheels system efficiencies of 60% and 52% were calculated for natural gas and diesel fuel, respectively. Compared to the state-of-the-art locomotive technology, SOFC-GT operation could provide a 98% reduction in NOx for both fuels, a 54% reduction in  $CO_2$  emissions for operation on natural gas and a  $30\% CO_2$  reduction for the operation on diesel fuel. Direct-alcohol SOFCs (e.g., methanol, ethanol and propanol) and the effects of the fuel impurities were investigated by Sasaki et al. [16]. Saebea et al. studied a SOFC-GT hybrid system supplied by ethanol fuel [312]. The recirculation of anode and cathode exhaust gas in the hybrid SOFC-GT system was proposed to improve the heat management in the system. In order to control the turbine inlet

temperature, fuel and air were added to the combustor. In another study, they analyzed a pressurized hybrid SOFC-GT system fed by ethanol with the recycle of a cathode exhaust gas [313]. The highest system electrical efficiency was achieved in the range of 4-6 bar. Rokni studied a 10 kW combined SOFC-Stirling engine power system for an average family home [180]. The results of natural gas (NG), ammonia, di-methyl ether (DME), methanol and ethanol operation were presented and analyzed in that study. Compared to the standalone SOFC plant, the overall power production of the combined SOFC-Stirling engine and the fuel utilization, the power produced from the bottoming cycle of the Stirling engine and the overall plant efficiency were increased. Reducing the SOFC operating temperature decreased the plant efficiency for all of the fuels except ammonia. The increase in the plant efficiency fueled by natural gas was more significant than the other fuels; methanol, ethanol and DME. In addition, the estimated cost of this type of hybrid system was 2060 \$/kW.

Three coal-based SOFC-GT configurations were evaluated for the thermal management of the main power block by Tucker et al. using steady state numerical simulations [314]. Consistent syngas composition was assumed in each case. A 240 MW rated fuel cell module was used in each of configurations. The recuperated cases were highly efficient and possessed excellent potential for thermal management control strategies. This was because the recuperation provided the means to increase the power contribution of the turbine while maintaining high efficiency [315]. Saebea et al. analyzed a pressurized hybrid SOFC-GT system fed by ethanol with the recycle of cathode exhaust gas [313]. The highest system electrical efficiency was achieved in the 4-6 bar range.

## Chapter 3

# COMPUTATIONAL FLUID DYNAMIC ANAL-YSIS

## 3.1 MOTIVATION FOR USING CFD TO ANALYZE SURGE

Using CFD to explore and understand compressor stall and surge could help to understand the fluid behavior in the hybrid SOFC-GT system. Compressor performance in gas turbines is limited by two main lines: 1) a choke line, 2) a surge line. Fig. (3.1) shows the typical compressor map. The surge limit depends upon the compressor design and system configuration and especially upon the pressure dynamics downstream of the compressor. Compressor surge could result in impeller and blade corrosions as shown in Fig. (3.2) and Fig. (3.3).



Figure 3.1: Surge chart



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Figure 3.2: Impeller corrosion





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Figure 3.3: Compressor surge effect on blade corrosion

Fig. (3.4) shows the typical types of stall/surge in the compressor, including mild and deep surge.



Figure 3.4: Types of surge

## 3.1.1 MECHANISMS OF COMPRESSOR SURGE/STALL IN HYBRID SOFC-

#### GT SYSTEM

There are two main mechanisms of compressor surge/stall in hybrid SOFC-GT systems that has been previously studied by McLarty et al..

Surge due to the high turbine inlet temperature:

Fig. (3.5) shows the surge mechanism due to the high turbine inlet (TIT) temperature.

1) Turbine inlet temperature rises

2) The mass flow rate through turbine decreases due to the lower density of the hotter inlet gases

3) Mass flow from the compressor persists causing a pressure buildup at the turbine inlet

4) Stall/Surge occurs. This is numerically simulated when the stall line is reached on the compressor map.

5) Compressor mass flow rate and torsional load become negligible

6) Shaft speed increases suddenly while the pressure at the turbine inlet drops



Figure 3.5: Surge mechanism due to the high turbine inlet (TIT) temperature

Surge due to the system emergency shut-down:

Fig. (3.6) shows the surge mechanism due to the system emergency shut-down.

1) Fuel input to the combustor is cut off.

2) Turbine inlet temperature drops as does turbine power slowing rotational speed.

3) Shaft speed reduction occurs faster than the turbine can expel the mass stored in the system to maintain surge margin.

4) Surge line is reached



Figure 3.6: Surge mechanism due to the system emergency shut-down

#### 3.1.2 DYNAMIC MODEL INTEGRATED WITH CFD SIMULATION

This research addresses compressor stall/surge, one of the most significant challenges corresponding to commercialization of hybrid solid oxide fuel cell-gas turbine (SOFC-GT) systems, using a novel approach. This study models a multi-stage compressor using computational fluid dynamics (CFD) tools and subjects the CFD computations to dynamic inlet and outlet perturbations that result from a dynamic SOFC-GT system model. One of the main causes of compressor stall/surge in hybrid SOFC-GT systems is turbine inlet temperature rise due to the transient increase in power demand in a small period of time. As the power demand rises from steady state to a specific higher power in a short time period, turbine inlet temperature (TIT) increases so that the gas turbine can meet the power demand and ramp up to meet the higher air flow required. Thus, the mass flow rate at the turbine inlet decreases due to the lower density while the mass flow rate from the compressor keeps building up pressure at the turbine inlet. As a result, reversal of flow in the impellers can occur, which is recognized as deep surge. However, the mass flow rate from the compressor persists causing a pressure buildup at the turbine inlet, increasing the local pressure. As a result of this pressure build up in the compressor outlet, an oscillatory flow rate could occur in the impellers that is recognized as mild surge.

Several researchers have addressed stall/surge in hybrid SOFC-GT systems and control methods have been developed in order to address stall/surge issue in the compressor. In one study, Azizi has studied compressor surge in a 220 kW hybrid system [215]. A CFD model was used in that study to address stall/surge in the single-stage centrifugal compressor. The feasibility of the compressor integration in the hybrid system was determined in that study. The overall approach of this research is based upon dynamics modeling of a hybrid SOFC-GT system in MATLAB/Simulink software, in order to solve the dynamics of turbine inlet pressure. The system-level dynamic modeling is followed by CFD modeling of a multistage compressor of a 1.7 MW gas turbine system to capture the fluid dynamics properties throughout the compressor impellers during transient operation in order to determine whether the compressor operation can feasibly avoid stall/surge in the hybrid SOFC-GT system. Transient dynamic CFD results from simulation of the 1.7 MW gas turbine are analyzed to determine whether these types of multi-stage centrifugal compressors could be used in future SOFC-GT locomotive engines. This study: 1) verifies the previously developed control methods for safe operation of radial compressors; 2) suggests that the control methods can be applied to any type of centrifugal compressor of similar design, and 3) presents CFD results for a specific compressor design that provide insights relevant to any industrial compressor used in a hybrid SOFC-GT system.

## 3.2 PLANT DESCRIPTION

#### 3.2.1 DYNAMIC HYBRID SYSTEM MODEL

Fig. (3.7) shows the model of a 4 MW hybrid power generation system that has been previously developed at the National Fuel Cell Research Center (NFCRC) at the University of California, Irvine using MATLAB/Simulink tools. This model was used to show that such systems, when properly designed and controlled, possess higher efficiency than previously tested SOFC-GT systems in power generation applications. The model consists of a compressor, a turbine, a blower, an SOFC, a combustor, three mixers and several bypass valves. This model has been previously studied for different applications of SOFC-GT hybrid systems ([316, 131, 181, 237]). The model includes one fuel cell bypass and several heater bypasses.



Figure 3.7: Hybrid SOFC-GT system power plant schematic [316]

## 3.3 TRANSIENT DYNAMIC SIMULATION

In this paper, a power demand profile used by Martinez et al. [3] is used in order to investigate the compressor behavior during a sudden increase in the power demand. Due to the complexity of the computation and turbomachinery complexity, only one step of the power demand profile is considered in the CFD simulations included in this study. The step power demand from 3 MW to 3.5 MW is applied to the dynamic model, and the pressure of the plenum node at the turbine inlet is solved in the MATLAB/Simulink platform. As the power demand rises from steady state at 3 MW to 3.5 MW in a short time period, the turbine inlet temperature (TIT) increases so that the gas turbine and fuel cell could ramp up to ultimately meet the power demand.

### 3.4 TURBOMACHINERY FLUID DYNAMICS SIMULATION

Turbomachinery CFD modeling is used to explore and understand stall/surge phenomenon in the same 4 MW hybrid fuel cell-gas turbine system. CFD analysis is applied on a multi-stage compressor configuration and its operational feasibility to meet the hybrid locomotive system step power demand increase observed during transient operation. The gas turbine design that could be integrated with an SOFC to produce the power studied in the system model includes the multi-stage design of a compressor that is similar to the 1.7 MW Model GPB15/17 gas turbine manufactured by Kawasaki industries in design. Fig. (3.9) shows the associated gas turbine system. This choice of compressor is based upon selecting turbomachinery that can approximately produce 20% of the net hybrid system power and match the air flow requirements of a corresponding SOFC. The design air mass flow rate required for the 4 MW hybrid system is 7 kg/s which is in the range of mass flow rates that the 1.7 MW gas turbine can deliver. Using this design mass flow rate, the SOFC-GT hybrid model design conditions are calibrated for the 40,000 rpm rotor condition. The blades and diffuser are sized for the net 7 kg/s air mass flow rate at 40,000 rpm.



Figure 3.8: 1.7 MW Kawasaki multi-stage gas turbine [317]



Figure 3.9: 1.7 MW Kawasaki gas turbine [317]

1.7 MW Kawasaki gas turbine consists of two stages of centrifugal compressor section, three stages of axial turbine section, short rotor span, single combustion chamber. The geometry considered in this study consists of two impeller each pressurizes air (2.5 pressure ratio). Blades and splitters are designed for 4000 RPM and overall pressure ratio of 8 atm. Diffuser has been designed similar to the Kawaski 1.7 MW compressor.



Figure 3.10: 1.7 MW Kawasaki compressor geometry model



Figure 3.11: Applied Fluid Model-Multi Stage Compressor

The fluid model is similar to 1.7 MW Kawasaki two stage compressor. The design conditions are as follows: 1) 22,000 RPM rotational speed, 2) 7.8 overall pressure ratio, 3) 6-8 kg/s air mass flow rate, 4) In order to reduce computational cost, periodic boundary condition is used. Fig. (3.14) to Fig. (3.14) below shows the mesh generated on the fluid model. Structured Mesh is used on the blades. Unstructured mesh is used on the diffuser.



Figure 3.12: Mesh generated on the Splitter



Figure 3.13: Mesh generated on the blade



Figure 3.14: Mesh generated on the diffuser

## 3.5 GEOMETRY MODELING

Due to their complex geometry, centrifugal compressors can be difficult systems to analyze using CFD. Specifically the multi-stage centrifugal compressor has a mid diffuser section that makes additional interface connections in the geometry. The simulation of these connections leads to a slower rate of solution convergence. The configuration considered in this study, includes two fast rotating impellers coupled to a stationary diffuser located between the impellers. In order to simulate each compressor stage, two sections (i.e., the rotating impeller and the stationary diffuser) must be modeled together. The impeller blade was designed for an overall pressure ratio of 3, so that the two impellers generate an overall pressure ratio of 9, and a rotating speed of 40,000 rpm. The geometry consists of two impellers and a diffuser located between the two impellers. In order to reduce the computational costs, full symmetrical boundary conditions are used to model only one flow passage of the compress-

sor. Each of the rotating and stationary sections were meshed independently. The impellers were meshed by the structured hexahedral method in ANSYS TurboGrid meshing software [318], while the diffuser was meshed using unstructured tetrahedrals with boundary layer refinements. The three separate mesh grids were connected by defining proper interfaces between the rotor and diffuser sections.

## **3.6 BOUNDARY CONDITIONS**

Stage averaging is used as a method of interface connection between the diffuser and impeller. In this method a circumferential averaging is applied at the interface between the rotor and stator. In order to apply correct boundary conditions on the fluid domain, a subsonic uniform air flow rate boundary condition with atmospheric pressure and temperature is applied to the inlet. The turbulent intensity was set to 5%. The pressure dynamic perturbation that resulted from step load change applied to the hybrid SOFC-GT system simulation, is applied to the domain outlet. Since the diffuser domain is stationary and the impellers are rotating, two interface boundaries are defined between the rotating impellers and the stationary diffuser.

## 3.7 FLUID DYNAMICS MODEL

A Reynolds Averaged Navier-Stokes (RANS) based model of shear stress transport (SST),  $k - \omega$ , is used to close the system of equations that describe the turbulent flow that is simulated. Using the  $k - \omega$  model instead of the  $k - \epsilon$  model allows for better resolution of boundary layers, especially under adverse pressure gradients. However, in the current study, the SST model was more difficult to converge than the  $k - \epsilon$  model. Nonetheless, the SST model is known to better simulate wall bounded aerodynamic flows, e.g, airfoils, compressors, turbines, and flows with separation due to adverse pressure gradients. In addition, the SST closure model is used to reduce the boundary condition sensitivity. ANSYS CFX [318] was chosen due to the proven ability to tackle complex turbomachinery problems faced in the gas turbine industry. In order to obtain good convergence, first the solver converged to the steady state solution. Following the stationary solution, the transient boundary condition was applied to the model and the system was solved for each time step in the short period of time that the system dynamics produced the pressure perturbation.

Shear Stress Transport Model:

$$\frac{\partial(\rho k)}{\partial t} + \frac{\partial(\rho u_j k)}{\partial x_j} = P - \beta^* \rho \omega k + \frac{\partial}{\partial x_j} [(\mu + \sigma_k \mu_t) \frac{\partial k}{\partial x_j}]$$
(3.1)

$$\frac{\partial(\rho\omega)}{\partial t} + \frac{\partial(\rho u_j\omega)}{\partial x_j} = \frac{\gamma}{\nu_t} P - \beta \rho \omega^2 + \frac{\partial}{\partial x_j} [(\mu + \sigma_\omega \mu_t) \frac{\partial\omega}{\partial x_j}] + 2(1 - F_1) \frac{\rho \sigma_{\omega 2}}{\omega} \frac{\partial k}{\partial x_j} \frac{\partial\omega}{\partial x_j}$$
(3.2)

$$P = \tau_{ij} \frac{\partial u_i}{\partial x_j} \tag{3.3}$$

$$\tau_{ij} = \mu_t (2S_{ij} - \frac{2}{3} \frac{\partial u_k}{\partial x_k} \delta_{ij}) - \frac{2}{3} \rho k \delta_{ij}$$
(3.4)

## 3.8 STALL/SURGE RESULTS

Transient dynamic operation of hybrid fuel cell-gas turbine system while maintaining the locomotive power requirement, is analyzed using computational and dynamics tools. Fig. (3.15) demonstrates the operating point of the hybrid system near the stall/surge line at a steady state condition. Control strategies were developed at NFCRC in order to prevent system operation beyond the surge line, using only the compressor and turbine maps. Fig. (3.15) demonstrates that the operating point is below the surge line and in the safe region. The implemented control algorithms produced system operating dynamics that met the power demand dynamics without allowing the compressor to operate in a deep surge condition. However, the fluid dynamics of a realistic industrial compressor performance must be investigated while operating in the hybrid system.



Figure 3.15: Operating point of 4 MW hybrid SOFC-GT at steady state condition

The dynamic pressure step perturbation due to the transient power demand variation in a small time period is applied to the rear impeller outlet. This perturbation results in the development of higher pressure in the diffuser and impellers as a function of rotor revolution (time). The pressure development is shown in Fig. (3.17). The pressure in the diffuser

and the impellers increases over time during the transient CFD computation. High pressure development takes time to reach the front impeller due to the stabilized flow in the middle stationary diffuser located between the two rotating impellers. The pressure development shown in Fig. (3.17) takes 25 rotor revolutions. The disrupted velocity vectors that are formed on both impellers reduce the compression efficiency. Higher pressure on the rear impeller follows the fuel cell pressure step increase, which over time (over a number of rotor revolutions) results in higher pressure in the diffuser and the front impeller. Ongoing mass flow rate through the front impeller and an increase in back pressure on the rear impeller causes a pressure accumulation in the diffuser causing a secondary stall/surge in the front impeller.

Fig. (3.16) shows that higher pressure at the 2nd Impeller outlet causes lower velocity in the 2nd Impeller and consequently in the 1st Impeller. Due to the high pressure, temporary instabilities in flow direction will occur at the 2nd impeller inlet.



Figure 3.16: Velocity vector on the whole domain



Figure 3.17: Pressure distribution in the flow domain on the front and rear impellers of the multi-stage compressor

The higher pressure at the rear impeller outlet causes lower velocity in the rear impeller and consequently lower mean velocity in the front impeller. Due to the higher pressure, temporary instabilities in the flow direction occur at the rear impeller inlet. Lower tangential velocity at the front impeller outlet causes lower mass flow rate at the front impeller inlet. High outlet pressure causes temporary blockage of a portion of the air flow at the impeller outlet. In addition, due to the high pressure, temporary instabilities in the flow direction occur in the region from the impeller inlet toward the leading edge. Vortices form on the blade that reduce the impeller compression efficiency. During the computational period, the radial velocity at the impeller outlet decreases. As a result, the mass flow rate leaving the rear impeller decreases causing mild compressor stall/surge. Fig. (3.19) and Fig. (3.20) show the pressure development on the shroud and the mild surge dynamics over the front and rear impellers over time. Comparing these figures, note that the pressure on the rear impeller reaches a steady state condition faster than the front impeller. In addition, the significant volume of the diffuser between the two impellers, delays the pressure increase in the front impeller. Thus, whenever a fast transient power demand is required, the-mid diffuser delays the initiation of stall/surge on the front impeller and lets the rear impeller return to the normal operation before the second stall/surge event begins in the front impeller. Therefore, this multi-stage configuration allows a time delay between the two stall/surge phenomena that increases the stability of operation during this pressure perturbation dynamic. This results in lower risk of system failure.



Figure 3.18: Pressure development in the diffuser



Figure 3.19: Pressure development on the front impeller's shroud



Figure 3.20: Pressure development on the rear impeller's shroud

Fig. (3.21) and Fig. (3.22) demonstrate the mass flow rate oscillation corresponding to the mild surge on the front and rear impeller inlets, showing a sustained flow rate during the hybrid SOFC-GT gas turbine transient operation, which produced pressure dynamic perturbation that is applied as boundary condition to the CFD model. Following the pressure step

change, the system reaches a stead-state operation and mass flow rate continues throughout the front and rear impellers without significant flow reversal.



Figure 3.21: Front Impeller inlet velocity/mass flow rate oscillation



Figure 3.22: Rear Impeller inlet velocity/mass flow rate oscillation

Fig. (3.23) shows the dynamics of stall/surge with higher resolution on the impeller outlet.

At steady state operation, the net mass flow rate is 7 kg/s which is equal to the design mass flow rate of the scaled gas turbine (similar to Kawasaki gas turbine) simulated. As the diffuser outlet pressure rises, the net mass flow rate decreases. However, the tangential velocity increases. The outlet mass flow rate decreases to the point of steady mass flow rate at the impeller outlet, which is the normal operating condition. Fig. (3.23) shows that at the 20th rotor revolution, the net air mass flow rate converges to a steady state and retains its constant value during the rest of this short period of hybrid SOFC-GT system operation. These results show that this type of industrial compressor can handle the type of transient pressure perturbation that a hybrid system could introduce quite well. However, control algorithms must be developed and applied subsequently in the system model to ramp the air flow rate back up to the required flow rate.

Fig. (3.24) demonstrates that as the outlet pressure increases, the flow velocity on the rear impeller gradually decreases at the trailing edge. The blue region shows some locations of zero velocity that is developed from the trailing edge to the leading edge. This situation is accompanied by the vortices that are formed along the blades and the splitters. Development of control algorithms are necessary in order to prevent the local high velocity on the blades.


Figure 3.23: Sustained mass flow rate after transient power demand change of the hybrid SOFC-GT system



Steady operation

Rotor rev=1.5 (Pressure jump)

Figure 3.24: The front impeller velocity distribution from the leading edge (LE) to the trailing edge (TE)



Figure 3.25: The rear Impeller velocity distribution from the LE to the TE

## 3.9 STALL/SURGE ANALYSIS RESULTS

The mass flow rates are calculated at the inlet and outlet of the multi-stage compressor as a function of the number rotor revolutions (time) as shown in Fig. (3.26). Note that, in the multi-stage configuration there is a net and sustained positive mass flow rate through the compressor outlet after the pressure applied and simulated to allow the compressor to respond and return to a new steady state. Notice that the 32 rotor revolutions simulated in the CFD simulation correspond to 0.05 seconds of hybrid system operation. After the compressor relaxes from the applied pressure dynamic (as shown in Fig. (3.26)), the turbomachinery will be "spun-up" (primarily by increasing TIT) over time to deliver the new air flow rate required by the hybrid system model. In the system model, this transient period lasts in order of seconds. During this period the pressure dynamics could also be simulated, but, the dynamics are relatively slow, indicating that CFD simulation of the compressor may not be required.



Time step=  $1/\omega$ 

Figure 3.26: Sustained mass flow rate after transient power demand change of the hybrid SOFC-GT system

# 3.10 220 KW SIEMENS-WESTINGHOUSE POWER PLANT

The Siemens Power Corporation hybrid design consisted of 100 kWe tubular SOFC and 75 kWe Ingersoll-RandMTG [101]. The system was tested at National Fuel Cell Center (NFCR-C) at University of California, Irvine. Siemens-Westinghouse Power Corporation developed the first hybrid system, which integrated a SOFC stack with the gas turbine engines. That pressurized (3 atm) system generated 220 kW of electrical power at a net electrical efficiency of 55%.

The dynamic interdependencies associated with the integration of the fuel cell and the gas turbine are not completely understood and unexpected complications might occur during the plant operation. The results of experimental study of SOFC-GT hybrid system at the University of Trieste, Italy, demonstrate that as a result of the relatively large volume of the pressurized portion of the plant and the shape of the stall characteristic of compressors, fluid dynamic instabilities could happen in the plant [211]. Surge could be detected in off-design transient operation of HS, during plant regulation, start up and shut down. In another study, It has been mentioned that hybrid systems posses large volume of gas between air compressor and turbine [30].



Figure 3.27: 220 kW Siemens- Westinghouse power plant

#### 3.10.1 MODEL VALIDATION EFFORTS

Fig. (3.28) to Fig. (3.30) shows the open loop response to ambient temperature variation during 60 hours operation at fixed current and air bypass previously studied at NFCRC. Compressor inlet temperature, turbines inlet and outlet temperatures, and SOFC outlet temperature show excellent agreement with the experiment measurements.



Figure 3.28: Compressor inlet temperature



Figure 3.29: Observed and simulated turbine inlet, GT1 and GT2 temperatures



Figure 3.30: Observed and simulated SOFC inlet and outlet temperatures

The Siemens-Westinghouse hybrid system has been modified due to the proven higher efficiency of the new system. The system has been developed at NFCRC at UC Irvine. The control strategy for this hybrid system is demonstrated. Fig. (3.31) shows the modified Siemens Westinghouse power system.



Figure 3.31: Modified Siemens Westinghouse Power System

Fig. (3.32) shows the control strategy for modified Siemens Westinghouse power system.



Figure 3.32: Modified Siemens Westinghouse Control Strategy

Conservation of mass and isentropic expression for speed of sound is shown in Eq. (3.5):

$$\frac{dp_p}{dt} = \frac{a_p^2}{V_p} (\dot{m}_c - \dot{m}_t)$$
(3.5)

CFD models are applied to study single-stage and multi-stage compressors. Fig. (3.33) shows the schematic of single-stage problem solved.



Figure 3.33: Single Stage Compressor Schematic

The CFD design is based on the Capstone C65 micro turbine generator. Secondary multi stage compressor CFD design is based on Kawasaki 1.7 MW gas turbine. Surge Results have been compared. Fig. (3.34)shows the operating parameters of Capstone micro-turbine.

Parameter	Unit	C-65
System Power	kW	60
Design Speed	RPM	96,000
Generator efficiency	%	96
Compressor Exhaust Temp	K	471.4
Design Flow	Kg/s	0.49
Pressure Ratio	None	4.0
Compressor Peak efficiency	%	74

Figure 3.34: C-65 (Capstone) operating parameters



Fig. (3.35) shows the capstone micro-turbine C-65 schematic.

Figure 3.35: C-65 (Capstone) operating parameters

Pressure step (jump) due to the sudden load variation has been applied to the diffuser outlet. Development of high pressure based on rotor revolution is demonstrated. The pressure in the diffuser and the impeller rises during the time Fig. (3.41).







Figure 3.37: C-65 impeller Velocity Distribution

Dynamic of surge is shown on the impeller outlet in Fig. (3.38). At the steady state operation, the net mass flow rate is 0.5 kg/s. As the diffuser outlet pressure rises, the net mass flow rate decreases. However, the tangential velocity increases. The outlet mass flow rate decreases till the point of zero mass flow rate at the impeller outlet, which is called deep surge.



Figure 3.38: C-65 impeller otutlet velocity ditribution

High outlet pressure causes temporary blocking of the air flow in the impeller outlet. In addition, due to the high pressure, temporary instabilities in flow direction occur at the impeller inlet to the leading edge. As a result, vortices form on the blade that reduce the impeller compression efficiency.



Figure 3.39: C-65 blade Velocity Distribution



Figure 3.40: Pressure evolution in diffuser over time



Figure 3.41: C-65 Single Stage Stall/Sure Results

# CHAPTER 4

# HYBRID SOFC-GT LOCOMOTIVE SYSTEM DESIGN

# 4.1 GENERAL SYSTEM MODELING

# 4.2 HYBRID SOFC-GT SYSTEM FOR TRANSPORTATION AP-PLICATION

#### 4.2.1 MOTIVATION

The current CNG and LNG stations are potential fueling stations for hybrid SOFC-GT locomotive engines, giving some confidence that an initial deployment that uses natural gas fuel is possible. Natural gas as a potential future fuel for all of their rail operations and has also demonstrated the use of natural gas tenders and natural gas reciprocating (diesel cycle) engines in rail operations.

## 4.3 SCOPE

This thesis covers computational fluid dynamic analysis of a stationary SOFC-GT system for various system sizes, sizing of SOFC-GT engine prototype for locomotive engine and system design and analysis of SOFC-GT system for locomotive system on a sample railroad route from Bakersfield to Mojave. It also covers system integration and development for hybrid SOFC-GT system in 1 MW switcher locomotive. The report addresses prototype system development for this type of switchers. Also a test railroad route (Bakersfield-Mojave) has been chosen in order to analyze the SOFC-GT performance on the route. Parametric studies have been accomplished in order to find the optimal design of the system that can effectively meet the power demand profile.

4.3.1 RESEARCH GAP

:

Zero emission commuter has been a target for many years in several transportation industries including locomotives. The potential benefits of hybrid systems applications in transportation sector are:

1) Enhancement of transient power and tractive force

2) Regenerative braking

3) Reduction of capital cost

The effectiveness of these characteristics relies on the dynamics of duty cycle and the route. These effects will be investigated in future efforts of our center on the path of development of hybrid fuel cell gas turbine systems. Propulsion system design issues and operating constraints will determine the feasibility of applying hybrid fuel cell-gas turbine system in a locomotive engine.

The current model of SOFC-Gas Turbine system works based on natural gas as the main

source of fueling. Hydrogen fueling has an advantage over natural gas as the hybrid system produces lower  $CO_2$  and NOx emissions. However based on the number of current stations installed for hydrogen and natural gas, the prototype system is designed for natural gas.

Fig. (4.1) shows the current compressed liquid and liquefied natural gas stations in the US. The current CNG and LNG stations are potential fueling stations for hybrid SOFC-GT locomotive engines, giving some confidence that an initial deployment that uses natural gas fuel is possible. Natural gas as a potential future fuel for all of their rail operations and has also demonstrated the use of natural gas tenders and natural gas reciprocating (diesel cycle) engines in rail operations.



Figure 4.1: Locations of CNG and LNG stations in the US

#### 4.3.2 FUEL CELL LOCOMOTIVES

To date, several rail vehicles use on-board hydrogen as a source of energy. Existing Fuel Cell Locomotives are shown in Fig. (4.2) to Fig. (4.4).



Figure 4.2: Japan Locomotive



Figure 4.3: North America BNSF Locomotive



Figure 4.4: North America BNSF Locomotive

#### Critical Locomotive parameters are shown in Fig. (4.5).

Critical parameters of the existed fuel cell locomotives.

	LLC & BNS	F					
Item			New Energy (NE)				
Region	North Amer	ica	Japan				
Fuel cell type	PEMFC		PEMFC				
Usage	Mining	Shunting	Experimental railcar				
Power level	14/17 kW	250 kW	2 × 95 kW				
Hybrid power	No	Yes	Yes				
Traction motor	Induced	Induced	Induced				
Year	2002/2009	2007	2006				

Figure 4.5: Critical locomotive parameters

PEMFC operating Temperature is  $80^{\circ}C$ . 23 kg compressed on board hydrogen is used. Maximum operating pressure of the tank is 50 Mpa and 80 Mpa.



Figure 4.6: Chinal PEMFC Locomotive



Figure 4.7: China Locomotive System Integration

The characteristics of the locomotive are as follows: 1) maximum air pressure is at 1.2 bar, 2) differential mode is proportional-integral, 3) closed-loop control strategy was used to adjust air compressor RPM and controls back pressure, 4) stack maximum heat generation of 185 kW, 4) 330 L/min coolant flow, 5) secondary coolant loop for air humidification.

Schematic of North American fuel cell locomotive is shown in Fig. (4.8). The fuel cell manufacturer is Ballard corporation. The type of the switcher used is fuel-battery switcher. The rated power is at 250 KW steady power from PEMFC with 1 MW transient Power.

Carbon fiber aluminum cylinders are used in the system. The system is able to store 35 kg of compressed hydrogen. Maximum air pressure is at 3 atm. Two stage air compression is used. The first stage generates 2.7 atm pressure ratio. The second stage uses variable vane to control the system back pressure and additional pressure boost.



Figure 4.9: North America fuel cell locomotive system integration schematic

#### 4.3.3 LOCOMOTIVE REQUIREMENTS

The power requirement for long-haul locomotive is at 3.5 MW. Martinez et al. studied the feasibility of SOFC-GT for long haul locomotive. Fig. (4.10) and Fig. (4.11) show the locomotive power demand.



Figure 4.11: Locomotive Power Demand generated by fuel cell, gas turbine and blower



Figure 4.12: Locomotive Efficiency

# 4.3.4 FUELING INFRASTRUCTURE FOR HYBRID SOFC-GT LOCOMO-TIVES

In this section, hydrogen fueling Infrastructure for railroad across the US has been developed using data assimilation form National Renewable Energy Laboratory Resources. The potential of hydrogen production potential from various resources including (Coal,Geothemal, Wind, Biomass) is shown in Fig. (4.13). General Mapping theme on a county level has been used to compute the hydrogen production potential across US.



Hydrogen Production From NG Hydrogen Production From Biomass Hydrogen Production From Solar

Figure 4.13: Hydrogen Production from various resources, Source: NREL

Fig. (4.16) shows the estimation of the quantity of low-carbon energy resources required to meet hypothetical future demand levels.



Figure 4.14: Hydrogen Production Potential

Fig. (4.15) shows the estimation of the hydrogen production potential from various resources required to meet hypothetical future demand levels versus carload traffic density.



Figure 4.15: Hydrogen Production Potential variation from various resources with Carload Traffic Density

Fig. (4.15) shows the computed hydrogen production potential for different states.



Figure 4.16: Hydrogen Production Potential for different states (alphabetical order) versus Carload density

#### 4.3.5 ECONOMIC CONSIDERATIONS

Table.(4.1) shows the sample locomotive performance.

Engine Horsepower	44000 HP
Starting tractive effort	183-190 lbs. force
Continuous tractive effort	157-166 lbs.force
Fuel efficiency	500 RTM**/gallon
Fuel tank capacity	5k gallons
Fuel tank range	800-1200 miles

Table 4.1: Sample Locomotive Performance

GE and EMD build 500-1200 locomotives annually for worldwide use. UP and BNSF combined acquired 500 new locomotives annually for US. Transition towards a sustainable energy system requires the development and deployment of new and improved energy technologies. Efficiency has been improved by 50% since 1980 (1.8% /year) [319]. Evolution series locomotives are the result of 10 years, \$ 400 million investment by GE [320]. In 2005, at the time of the GE Evolution series release, GE and other competitors were selling numerous locomotives prices near \$2 million [321]. Back in 2001, prices were from about \$1,500,000 for DC units like the SD70 model to about \$2,300,300 for an AC unit such as SD90MAC, with the average price for a new locomotive at about \$1,700,000 [322]. In 1948, the price for 103 locomotives in the range of 1,000 to 6,000 hp was reported as \$91.7-\$106.1 per hp with average of \$102.42/hp. In 1970, for 173 locomotives ranging from 1,000 to 3,000 hp, the price was reported as \$92.5 to \$150 per hp with the average of \$116/hp. In 1979, the Electro-Motive new unit model (SD-40-2), 3,000 hp cost was reported as \$216.67/hp. In 1983, the Electro-Motive model SD-50, 3,500 hp cost was reported as \$342.90/hp [322]. Elimination of high catenary-wire infrastructure costs by fuel-cell locomotives is the key to economic viability of zero-emission, low-noise electric trains in the low population density regions. The issues are related by the fact that about 97% of the energy for the transport sector (in the US) is based on oil, and more than 60% is imported. Because its primary energy is based largely on combustion of fossil fuels, the transportation sector is one of the largest sources of air pollution. A North American public-private project partnership has developed a prototype fuel-cell-powered switch locomotive [323]. The fuel-cell-hybrid switch locomotive for operation in the LA metro area combines the environmental advantages of an electric locomotive with the lower infrastructure costs of a diesel-electric locomotive.

Fuel-cell stack hardware costs, on-board fuel storage, and fuel infrastructure continue to be challenges for commercial implementation. Fuel cell locomotives are expected to be more energy efficient than diesel locomotives, and because its fuel infrastructure will be homologous to that of a diesel, it should have similar fuel infrastructure costs [324]. Capital cost in some applications may be reduced. Based on an observed locomotive duty cycle, a cost model shows that a hybrid power plant for a switcher may reduce capital cost [325].

Integrated hybrid systems have the potential to operate at higher energy efficiency than fuel cell or gas turbine alone. A market study by Research Dynamics Corporation proposed that hybrid systems could compete on the electricity cost with other distributed generation technologies. The thermal efficiency of SOFC-GT can rise up to 70% comparing to the current diesel locomotive efficiency 40%. The Tier 4 diesel electric locomotive cost has been estimated to be 3\$ million. Evolution series locomotive of the GE use 5% less fuel during its lifetime or enough to power another evolution series for more than half a year. Compared to previous GE transportation models, the evolution series locomotive reduces emissions by more than 40%.

In 1999, Rolls Royce funded a study to produce a turbo-generator that costs approximately \$400 per kilowatt [27, 30]. It was shown that when coupled with fuel cell, the system produced 25% of the power from the turbine in the 1 MW to 5 MW class. As a stand-alone mode, turbine would produce 1.5 MW of electric power in a simple cycle. In stand-alone mode, the efficiency of turbine is approximately 33%. Pressurizing the fuel cell increases the overall system efficiency. However, the technical challenges associated with the development of SOFC with a very high operating pressure and the development costs will be significant. Yi et al. have studied the balance between the development cost and the efficiency [174]. The turbomachinery used in power generation can operate in two configurations; Synchronous ans Asynchronous. In synchronous mode the shaft is directly driving the electrical generator at some multiple of the grid frequency. The advantage of this method is elimination of costly power conditioning hardware and additional losses of the power conditioning module. Velumani et al. proposed a combined heat and power (CHP) SOFC/microturbine/absorption chiller for 230 kWe demand building with thermal efficiency in the range of 70 to 75%, where the waste heat can be used for local heating and cooling [187]. The installation costs are reported to be in the range of 400 US\$/kWe and 4000-5000 US\$/kWe for the microturbine and SOFC respectively. Agnew et al. presented Rolls-Royce strategies in order to

reduce the SOFC-GT hybrid costs [133]. An IP-SOFC stack concept has unique design features, so that stacks can be manufactured through low cost manufacturing processes and with low inventories of material. Lundberg et al. presented a conceptual design of 60% efficiency 20 MWe-class PSOFC-ATS-GT HS that integrates Siemens Westinghouese pressurized SOFC and Mercury 50 gas turbine [243]. The system installed cost was estimated at \$1170/kWe. While operating on \$3/MMBtu natural gas fuel, its cost of electricity (COE) was approximately 6% less than COE of less efficient and less expensive GT/ST comcined cycle system. Initial market of the fuel cells is discussed [31]. The cost of fuel cell systems has a significant potential for being further reduced. Several researchers developed thermo-economic optimization of SOFC-GT hybrid systems [241, 242, 243, 244]. Auttssier et al. used thermo-economic multi-objective optimization approach to compute the integrated system performances, size and cost [241]. Two objectives have been considered in this study: minimizing of the specific cost and maximizing the efficiency. Their results prove the existence of designs with costs from 2400\$/kW for 44% efficiency to 6700\$/kW for 70% efficiency. In addition, high system efficiencies can be obtained with low fuel utilization in their system. Cheddie et al. studied a SOFC indirectly coupled with 10MW power plant with 30% efficiency. The method of Lagrange Multipliers in the thermo-economic has been used to optimize the system performance. The net power output of 18.9MW at 48.5% efficiency has been predicted. A breakeven per-unit energy cost of USD  $4.54kWh^{(-1)}$  for the hybrid system is predicted [242]. Najafi studied SOFC-GT system integrated with a multi stage flash (MSF) desalination unit [243]. Muti-objective genetic algorithm (MOGA) has been used to find the optimal design parameters of the plant. Exergy efficiency and total cost rate of the system were considered as the objective functions. The optimal design resulted in 46.7% exergetic efficiency and a total cost of 3.75 million USD/year. The payback time of the design is reported to be 9 years. Results showed that MSF desalination unit is significantly irreversible with exergy efficiency from 3.05% to 3.61%. Thermodynamic, kinetic,

geometric and cost models of hybrid SOFC-GT-ST have been developed ranging in the size of 1.5 MWe to 10 MWe [244]. It was reported that, higher operating pressure resulted in higher cell voltage and as a result higher system efficiency. It was suggested that higher compressor and turbine costs must be considered at higher operating pressures. Massardo demonstrated that their proposed system efficiencies are high (65 - 70% for atmospheric cells and 74 - 76% for pressurized cells) [71].

#### 4.3.6 MODELING

For the turbo machinery the capital cost is provided by the formula presented by Calise et al. [238]. Table. (4.2) shows the set of equations used for economic analysis of SOFC-GT system.

Gas Turbine Capital Cost	$C_{GT} = (-98.328ln(P_{GT}) + 1318.5)P_{GT}$
Compressor Capital Cost	$C_{compressor} = 91562 \times \left(\frac{P_{compressor}}{445}\right)^{0.67}$
Heat Exchanger Capital Cost	$C_{HE} = 11.6(m_{HE})^{0.95}$
Counter Flow Heat Exchanger Capital Cost	$C_{HEC} = 130 \times \frac{A_{HE}}{0.093}$
Isentropic Relation	$\frac{T_2}{T_1} = \frac{P_2}{P_1}^{(y-1)/y}$

Table 4.2: Set of equations used for economic analysis of SOFC-GT system

Where,  $m_{HE}$  is the heat exchanger mass (kg).  $A_{HE}$  is the surface area of the heat exchanger. In order to find the heat exchanger surface area, we need to calculate the heat required to rise the air temperature from compressor outlet temperature to the SOFC cathode inlet. Using the isentropic relation and assuming the air is ideal gas.

In the Martinez et al. study [3] the hybrid system produced the net 3.5 MW (4693 hp) power. We assume the SOFC and GT characteristics in the study can be used to provide a cost projection that meets GE locomotive requirements (4400 hp). The particular turbine was chosen that determined its power (1.2 MW) and size (9.02  $m^2$ , 21.74  $m^3$ ) were well-matched to the requirements of the hybrid system needed in this application. Two case studies have

been accomplished using the  $H_2$  fuel and natural gas fuel. The Table. (4.4)below shows the characteristics of the modeling:

SOFC stack	# of Units in the hybrid SOFC-GT system
Heat Exchanger	1
Gas Turbine	1
Combustor	1
Compressor	1

Table 4.3: Typical Components of SOFC-GT system

	Case 1 $(H_2)$	Case 2 (Natural gas)
Voltage	0.71	0.64
Current Density, average $(\frac{A}{m^2})$	4203	3712
Power $(\frac{W}{m^2})$	2984	2645
Utilization factor $(U_f)$	0.85	0.85
$T_{tri,max}(C)$	1017	980
$T_{anode,avg}$ (C)	1020	985
$T_{cathode,avg}$ (C)	1007	974

Table 4.4: Martinez Model Characteristics [3]

From that study, we assume and average air mass flow rate of 4 kg/s and the associated pressure ratio of 4. Thus the outlet temperature of the compressor could be calculated at  $170^{\circ}C$ . Thus the total heat exchange from the heat exchanger is:

$$\dot{Q} = \dot{m}c_p \delta T = 4 \times 1 \times (600 - 170) = 1720kW$$
(4.1)

The log-mean temperature difference could be calculated as follows:

$$\Delta T_{LM,k} = \frac{(T^{supply}HCC,k} - T^{target}CCC,k) - (T^{target}HCC,k} - T^{supply}CCC,k)}{ln(\frac{T^{supply}HCC,k} - T^{target}CCC,k}{T^{target}HCC,k} - T^{supply}CCC,k})}$$
(4.2)

Using the average turbine inlet temperature from Martinez study, 1350 (K), the turbine exhaust temperature can be calculated from the isentropic equation to be 900 (K). Assuming the air is preheated to 800(K), the log-mean temperature is calculated as  $\Delta T_{(LM, k)} = \frac{(908 - 800) - (450 - 443)}{ln908 - 800450 - 443} = 36.9.$ 

Assuming a constant overall heat transfer coefficient,  $U = 0.5 \frac{kW}{\circ C.m^2}$ , we could calculate the heat exchanger area as follows:

$$A_{surf} = \frac{Q}{U \times \Delta T_{LM,k}} = \frac{1720}{0.5 \times 36.9} = 93.22(m^2)$$
(4.3)

Thus, the total capital cost of the heat exchanger is estimated as 28400 \$US.

For the SOFC stack capital cost the following equation is used:

$$C_{SOFC} = n_{cell} \pi D_{cell} L_{cell} (2.96 \times T_{cell} - 1907)$$

$$(4.4)$$

 $T_{cell}$  is the cell temperature (°*C*). Capital cost of SOFC power systems is determined in another study [28] for ground based distribution systems, however designed for aircraft application. The nominal power is reported to be 270 kW. The electricity cost for a mass manufactured solid oxide fuel cell could be in the range of 0.07-0.08/kWh based on centralized power production plants. The sputtering approach was investigated to examine the decrease in costs associated with the process. It is reported that the process not only reduces the material cost, but also increases the fuel cell power density by 50%. The increased power density reduces the number of repeat units required to makeup a 270 kW fuel cell stack. Stack costs decreased by 33% at a mass production of 10,000 units per year. Material costs contributed 55% of the total stack manufacturing costs.

	Delivered Cost			
	\$/kg	\$/kg	\$/kg	
Material	Low	Average	High	
Ag Paste	908.28	1,356.00	3.000.28	
Carbon Black (Cancarb N990 Ultrapure)	4.16	4.16	4.16	
Graphite (Asbury 4006)	3.64	3.84	4.04	
SiC (Superior Graphite Grade 1200)	16.05	16.05	16.05	
Yttria Stabilized Zirconia (Unitec 5Y)	10.28	20.28	30.28	
NiO Electronics Grade	28.28	30.78	33.28	
Yttria Stabilized Zirconia (Diiachi 8YSZ)	20.28	35.28	50.28	
Glass Powder (VIOX #1716)	24.20	36.53	53.91	
Al metal powder	13.38	16.88	20.38	
Al metal powder another price	14.01	28.20	42.38	
Phospholan™ PS-236 surfactant	6.29	6.47	6.65	
Polyvinyl Butyral, BUTVAR B-79	17.60	19.75	21.89	
Benzyl n-butyl phthalate	4.01	5.01	6.01	
Ethocelluose (Dow Ethocel 45)	25.20	25.20	25.20	
Di-Butyl Phathalate (Aldrich) - Lab supplier	9.38	9.55	9.73	
Vehicle (Ferro BD75-717)	15.33	15.80	16.28	
Binder (ESL 450) - Electro Science Laboratories	8.00	9.00	10.00	
Ethanol	1.02	1.02	1.02	
Methyl Ethyl Ketone (Fischer) - Lab supplier	0.78	1.38	1.98	
Isopropyl alcohol	3.82	3.82	3.82	
n-Butyl alcohol, 99.9%	7.05	7.54	8.02	
Stainless Alloy 430 or 441	2.25	2.46	2.67	
Ce2(CO3)3*5H2O	50.28	52.78	55.28	
CoCO3	17.28	18.78	20.28	
FeCO3*H2O	1.38	1.58	1.78	
La2(CO3)3*8H2O	60.28	70.28	80.28	
MnCO3	1.54	2.58	2.85	
Sm2(CO3)3	22.28	90.7	91.99	
SrCO3	1.26	2.27	3.28	
Glycine	0.48	1.48	2.48	
Nitric Acid (70%)	1.97	2.33	2.70	
Nickel	16.56	22.42	28.28	
Ferric Chloride	1.03	1.10	1.18	
Soduim Chlorate	0.775	0.875	0.975	
Muriatic Acid	0.455	0.5125	0.57	

In general the capital cost of SOFC manufacturing is reported to be from \$500 to \$700/kW. In order to calculate the capital cost of SOFC based on the Calise et al. study, the active cell area is needed. Motahar et al. studied tubular SOFC based SOFC-GT in a MW-class [76]. Active area of the cell is assumed to be  $834cm^2$ . We use this active area in order to find the capital cost of SOFC. Based on this study, the typical cell voltage for SOFC in a MW-class SOFC-GT hybrid system is approximately 0.69(V) and the current density is  $300mA/(cm^2)$ . Knowing the power produced by SOFC, active cell area, cell current density and the cell voltage, we can calculate the number of the cells. Based on the work of Chan et al. [30] study, the compressor power requirement is approximately one fifth of the produced power by SOFC. We have used this assumption for the compressor power estimation. The capital cost of the SOFC inverter is calculated as follows:

$$C_{inverter} = 100000 \times (\frac{P_{cell}}{500})^{0.7}$$
(4.5)

Where  $P_{cell}$  is the stack power production in kW. The SOFC pre-reformer capital cost is as follows:

$$C_{PR} = 130 \times \left(\frac{A_{PR,f_{in}}}{0.093}\right)^{0.78} + 3240(V_{PR})^{0.4} + 21280.5 \times V_{PR}$$
(4.6)

Where,  $V_{PR}$  is the catalyst volume  $(m^3)$ , and  $A_{PR,fin}$  is the finned exchange area  $(m^2)$ . Since we dont know the exact number of catalysts, diameters and tube length, we refer to Arsalis study for pre-reformer cost. The cost of the reformer does not vary significantly from 1.5 MW to 10 MW hybrid system. Thus we assume, the pre reformer cost would be 40,000\$ US. The capital cost of the auxiliary devices (catalytic combustor, mixer, etc.) can be calculated a as a fixed percentage (15%) of the stack cost.

$$C_{aux,SOFC} = 0.10 \times C_{SOFC} \tag{4.7}$$

#### 4.3.7 TOTAL COST CALCULATION

Assuming an overall 15 year lifetime is considered. The interest rate *i* is assumed to be 0.0929 [258]. Also,  $f_{main}$  is assumed to be 0.06. Similarly, the insurance  $f_{ins}$  and taxation  $f_{tax}$  are chosen as 0.2 and 0.54 percent.

#### 4.3.8 COST MODEL

Table. (4.7) shows the SOFC-GT cost model for hybrid fuel cell gas turbine.

Variable	Variable Description	Model Equation
1	Deprication cost (\$/yr)	$G_{dep} = \frac{C_{pur}}{n_{dep}}$
2	Interest on outside capital cost (\$/yr)	$G_{int} = \frac{C_{pur}}{n_{dep}}i$
3	Maintenance cost (\$/yr)	$G_{mai} = \frac{C_{pur}}{n_{dep}} f_{mai}$
4	Insurance cost (\$/yr)	$G_{ins} = \frac{C_{pur}}{n_{dep}} f_{ins}$
5	Taxation cost (\$/yr)	$G_{tax} = \frac{C_{pur}}{n_{dep}} f_{tax}$
6	Capital cost (\$/yr)	$G_{cap} = G_{dep} + G_{int} + G_{mai} + G_{dep} + G_{tax}$
7	Operating cost (\$/yr)	$G_{ope} = c_f \times V_f N_h$
7	Total cost (\$/yr)	$G_{total} = G_{cap} + G_{ope}$

 Table 4.5: SOFC-GT cost model

Based on Song et al. multi MW-class hybrid system study, the molar flow rate of the system is estimated to be 0.2 kg/s or 1100  $(Nm^3)$ /hr. The price of natural gas is assumed to be 0.25 \$/ $Nm^3$ . In order to project the cost for volume production, the formula proposed by

Georgopoulos et al. [326] is used.

$$C_x = C_y \times \left(\frac{V_x}{V_y}\right)^{-0.36} \tag{4.8}$$

Where,  $C_x$  and  $C_y$  are the total cost at volume production of  $V_x$  and  $V_y$ , respectively.

#### 4.3.9 DEVELOPMENT STAGES

Table.	(4.6)	shows	the stages	of	develo	pment	for	SOFC-	GT	locomo	tive	engine.
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1	Concept and Design
2	Lab Testing
3	Prototype
4	Small scale demo (1-3 Units)
5	Medium scale demo (5-20 Units)
6	Full scale demo (20-75 Units)
7	Commercialization (500-1200, Locomotive units build by GE and EMD combined)

Table 4.6: SOFC-GT locomotive stages of development

#### 4.3.10 COST RESULTS

Table. (4.7) shows the cost calculated for each of the components of the SOFC-GT system.
Stack cost (\$)	1,424,350.98
Gas turbine cost (\$)	745,660.55
Compressor (\$)	106,807.07
Pre-reformer (\$)	40,000
Heat Exchanger (\$)	28,493.36
AC Inverter (\$)	333,988.58
Auxiliary (Catalytic combustor, mixer, etc.) (\$)	213,652.64
Total (\$)	2,892,953

Table 4.7: Hybrid system component costs

Fig. (4.19) shows the annual locomotive cost (Total unit cost per year versus volume pro-



Figure 4.18: Total unit cost per year versus volume production per year

Stage of Locomotive Development	Years Included	Estimated Budget (\$ US)
Concept/Design	1-2 Years	3,177,330.50 \$
Lab Engine Testing	2-4 Units	745,990.0 \$
Prototype and Demonstration Locomotive (1-5 units)	4 5 Years	3,573,100 \$(1 unit) to
		10,009,000.0 \$ (5 units)
Pre-Production Locomotive Field Tests (20-75 units)	6 7 Years	24,305,000\$ (25 units) to
		56,635,000\$ (75 units)
Commercial Production (500-1200 units annually)	Compliance Date	22,231,000 \$/yr (for 500 u-
		nits/yr) to 38,931,000 \$/yr
		(for 1200 units/yr)

Table 4.8: Estimated budget in different scales of operation

The Fig. (4.19) and Fig. (4.20) shows the total cost for different components and different financial aspects.



Figure 4.19: Total unit cost per year versus volume production per year



Figure 4.20: Cost calculated for different financial sections

# 4.3.11 System Sizing and Evaluation of the First long-haul SOFC-GT system

This section aims to provide an insight into the feasibility of hybrid fuel cell-gas turbine regarding sizing constraints of hybrid solid oxide fuel cell-gas turbine (SOFC-GT) engine for a 4 MW long-haul locomotive engine. The power plant designed for this system consists of a 1.7 MW industrial gas turbine (similar to 1.7 MW Kawasaki gas turbine), a solid oxide fuel cell, two main heat exchangers (fuel pre-heater, and air recuperator), an external diesel reformer, a catalytic combustor and several mixers and valves. The system is designed to fit into current long haul industrial locomotives. Fuel cell system and balance of plant (BOP) is designed in order to provide sufficient fuel flow rate for steady operation of hybrid system engine. Analysis shows that the SOFC module would generate about 80% of the net power of the hybrid SOFC-GT system. Therefore, a 3 MW SOFC module is designed to be used in the hybrid engine in order to generate the required power at the full-load operation. The closest commercial gas turbine, 1.7 MW Kawasaki multi-stage gas turbine, is chosen

to fulfill this operation. Two main heat exchangers of the system are the air preheater and the fuel preheater. Due to the size constraints in the engine tank, fin and plate heat exchangers are designed using available commercial heat exchanger design software (ASPEN). On board steam methane reformer (SMR) has been sized and designed to provide enough hydrogen flow rate for the SOFC stack consumption. Optimized method will be discussed in order to reduce the net size of hybrid SOFC-GT system. Analyses show that packing the hybrid engine in a locomotive engine part will be possible. One of the significant challenges (stall/surge) of this type of hybrid system will be discussed and control algorithms required to tackle this challenge will be presented. At the end, possible industrial partners will be introduced in order to build the first hybrid SOFC-GT engine at a test scale.

Fig. (4.21) shows the plant used for locomotive sizing.



Figure 4.21: Hybrid SOFC-GT system to be used in long-haul locomotive

Eq. (4.9) to Eq. (4.11) shows the equations used for system sizing of reformer. Diesel Reformer:

$$C_{16}H_{34} + 16H_2O \to 16CO + 33H_2$$

(4.9)

Partial Oxidation:

$$C_{16}H_{34} + 8O_2 \to 16CO + 17H_2$$
(4.10)

ATR:

$$C_{16}H_{34} + 16H_2O + 8O_2 \to 16CO_2 + 33H_2$$
(4.11)

Where  $C_{16}H_{34}$  represents the paraffinic compounds at the highest concentration in low-sulfur diesel fuel. Calculations for fuel cell sizing are as follows:

$$\dot{H}_2 = \frac{i}{nF} \times N = 23.72 \frac{mol}{s} = 5.67 \times 10^3 \frac{nm^3}{hr}$$
(4.12)

Based on cetane LHV,  $LHV_{cetane} = 9.96 \frac{MJ}{mol}$ .

$$LHV_{H_2} = 243.5 \frac{kJ}{mol}$$
(4.13)

Fig. (4.22) and Fig. (4.23) show the fuel cell assembly for implementation in locomotive fuel cell - gas turbine hybrid system.



Figure 4.22: Hybrid SOFC-GT system to be applied in long-haul locomotive engine



Figure 4.23: Fuel Cell Assembly to be used in long-haul locomotive

The sizing of the heat exchangers to be implemented in the long-haul locomotive are shown in Fig. (4.24) and Fig. (4.25). System heat exchangers have been sized (Fuel preheater

and Recuperator heat exchangers in hybrid SOFC-GT system). Fin and plate heat exchanger were designed in ASPEN simulation software.



Figure 4.24: Heat Exchangers for Fuel Preheater









Figure 4.25: Heat Exchangers for Recuperator



Figure 4.26: Fuel Cell Stack to be used in long-haul locomotive



Figure 4.27: Reformer to be used in long-haul locomotive

### CHAPTER 5

## MODELING OF HYBRID SOFC-GT SYS-TEM FOR LOCOMOTIVES

5.1 DEVELOPMENT OF 500 KW SMALL SCALE LAB DESIGN Fig. (5.1) shows the bloom energy prototype of SOFC as the potential fuel cell design of the locomotive. 400 kW Versa Power (Fuel Cell energy) is also another potential fuel cell for small scale development of fuel cell - gas turbine system. Micro gas turbine selection is based on the fact that 20% of the net power produced by gas turbine C-200 Capstone micro-turbine. Fig. (5.5) shows the C-200 capstone microturbine system.



Figure 5.1: Bloomenergy fuel cell to be used in a small scale prototype of hybrid SOFC-GT system Fig. (5.2) to Fig. (5.4) show the Versa Power 400 kW performance. At higher S/C, SOFC produces more current.



Figure 5.2: Versa 400 kW Current Simulation



Figure 5.3: Versa 400 kW Voltage Simulation



Figure 5.4: Versa 400 kW Oxygen utilization Simulation





Fig. (5.6) shows the pressure response to power demand profile for the 268 kW Bloom energy SOFC system. This is the pressure dynamics response of our dynamic model to step power demand change in 200 kW C-200 Capstone micro gas turbine.



Figure 5.6: Pressure response for 500 kW small scale system

Transient dynamic operation of hybrid SOFC-gas turbine system components has been investigated, while maintaining the 500 kW lab-scale locomotive power requirements, using MATLAB/Simulink software. Simulation is accomplished in over time span of 10,000 (s). Real industrial compressor performance has to be investigated while operating in a hybrid system.

Fig. (5.7) shows the pressure distribution over C-200 single stage compressor Perturbation results in the development of high pressure in Capstone C-200 impellers as a function of rotor revolution. At time T = 7,000(s) the rotor revolution is equal to 53 revs.

The results would validate the utilization of CFD tools in C-200 and lead to a better understanding of the flow phenomenon within the single-stage centrifugal compressor. Lower pressure on impeller followed by pressure step decrease, results in lower pressure in the diffuser and the first impeller. Ongoing mass flow rate through the impeller and reduction in back pressure on the impeller causes a pressure reduction in the diffuser lowering the risk of surge in the impeller.



Figure 5.7: Pressure distribution on impeller for 500 kW small scale system at T = 7,000s



Figure 5.8: Velocity distribution on impeller for 500 kW small scale system at T = 7,000s

Low outlet pressure causes higher air mass flow at the impeller outlet. In addition, due to the low pressure, temporary higher velocity region develops in flow direction from the impeller inlet toward the leading edge. As a result, vortices previously formed on the blades are reduced resulting in an increased impeller compression efficiency, see Fig. (5.9).



Figure 5.9: Velocity development on the impeller blades, T = 7000(s)

Fig. (5.10) shows the velocity vectors on the impeller inlet over time. Comparing these figures, it could be seen that the net mass flow rate of air is consistent over time showing a sustained flow rate during the sudden power demand reduction. In addition, high volume of the diffuser plays a significant role stabilizing the flow at the impeller inlet. Thus, whenever fast transient power demand is required, the diffuser delays the surge on the impeller and reaches to the normal operation before the second surge begins.



Figure 5.10: Velocity vectors on the impeller inlet

Fig. (5.11) shows the pressure development throughout the diffuser over time. It could be seen that the pressure reduces significantly due to the reduction in power demand reducing the surge risk in the impeller. Stable flow in the diffuser plays an important role in reduction of back pressure on the impeller and as a result keeps the air mass flow rate at a desirable level of 1 kg/s.



Figure 5.11: Pressure reduction in the diffuser connected to the impeller outlet, T = 7000(s)

Fig. (5.12) demonstrates the mass flow rate oscillation corresponding to the mild surge on the impellers outlet, showing a sustained flowrate in C-200 compressor during the hybrid SOFC-GT gas turbine operation. During the time, the radial velocity at the impeller outlet increases and as a result, the mass flow rate through the outlet increases reducing the surge



Figure 5.12: Impeller outlet velocity and flow rate increase, T = 7000(s)

Fig. (5.13) shows the Velocity profile over the impeller at time=3000s, when the power demand increases step wise to 200 kW. More critical case than the previous case as the pressure increases due to power increase. The velocity is reduced, while the mass flow rate is sustained at T=3,000 (s).



Figure 5.13: The velocity distribution over impellers at T=3000s

Fig. (5.14) shows the velocity region on the impeller blades. As the pressure increases, the velocity decreases significantly on the trailing edge. However, after 20 rotor revolutions, the velocity reaches to constant value and as a result a sustained mass flow rate. High vorticity region that was formed at 5 rotor revolution, diminishes on the trailing edge after 20 rotor revolutions.



Figure 5.14: 1st Impeller velocity distribution from LE to TE

As the pressure increases, the velocity decreases significantly on the trailing edge. However, after 20 rotor revolutions, the velocity reaches to constant value and as a result a sustained mass flow rate. High vorticity region that was formed at 5 rotor revolution diminishes. Fig. (5.15) shows the pressure increase in the diffuser at T=3,000 (s).



Figure 5.15: Pressure variation at T = 3000(s) on diffuser

Fig. (5.16) demonstrates as the outlet pressure increases, the flow velocity on the impeller at the trailing edge gradually decreases. This situation is accompanied by the vortices formed along the blades and the splitters. Development of control algorithms are necessary in order to prevent the local high velocity on the blades.



Figure 5.16: Impeller outlet velocity reduction at time 3000 (s)

In the single-stage configuration there is a net and sustained mass flow rate through the compressor outlet after the pressure step is relaxed to a constant value. The calculated values of mass flow rate at different parts of the single-stage C-200 compressor are shown in Fig. (5.17) as a function of the rotor revolutions for two times of t=3000 s and t=7000 s. It could be observed that, in the single-stage configuration there is a net and sustained mass flow rate through the compressor outlet after the pressure step is relaxed to a constant value.



Figure 5.17: Mass Flow Rate results at t=3000 (s), and t=7000 (s)

### CHAPTER 6

## HYBRID SOFC-GT LOCOMOTIVE DYNAM-ICS AND CONTROL

#### 6.1 DYNAMIC MODELING OF HYBRID SOFC-GT SYSTEM

#### FOR LOCOMOTIVES

The National Fuel Cell Research Center (NFCRC) analyzed first prototype of the hybrid SOFC-GT system on the route from Bakersfield to Mojave. The system is designed in MAT-LAB/Simulink platform. The modeling process is divided into two sections of modeling the switcher and modeling the long haul locomotive. The switcher modeling is used in order to develop small 1 MW order prototype system. In the current study, 8 notches have been modeled for the control system. System of the locomotive is designed for a 1 MW switcher similar to EMD RS 1325. A single vehicle model is developed in MATLAB/Simulink platform. The total distance on the rail yard is calculated based on double integration of traction force. The net force on locomotive is calculated based on rolling resistance, air and axle resistance and the switcher weight. The system development

for the locomotive is based on two main components of vehicle dynamics and notch calculation. The notch system takes speed of the locomotive, grade of the route, acceleration and traction/brake force as an input. Several assumptions have been made in implementation of the notching algorithm: 1) The maximum desired train velocity was 60 miles per hour, 2) The minimum desired train velocity was 10 miles per hour, 3) The power notching progressed by one notch at a timestep (increasing or decreasing), (This decision is made by the locomotive driver), 4) Notching does not alternate rapidly between the timesteps, 5) The sign of the grade has an effect on the decision making.

#### 6.1.1 **OBJECTIVES**

The objectives of the research accomplished herein are as follows:

- Development and analysis of small scale 1 MW SOFC-GT engine for switcher locomotive and 3 MW SOFC-GT system for long-haul locomotive

- Testing the developed model on the Bakersfield to Mojave Railroad,

- Develop control algorithms in order to pass the switcher through the route,

- Finding the optimal design of the system that can be manufactured for the prototype,

- Conduct comparative the fuel economy testing of the developed model for Natural gas and hydrogen fuels

- Establish final P&ID design of the hybrid SOFC-GT system that can be use in manufacturing process.

The overall approach of this section is control system development for SOFC-GT hybrid systems that are required to pass the 1 MW switcher locomotive through the Bakersfield-Mojave Route. PID controllers are implemented to control the RPM, compressor inlet guide vanes, fuel cell fuel flow rate and fuel cell power. Specific gains for these controllers are specified in order to pass the switcher through the route. Due to highly dynamic nature of the power duty cycle, the control systems are required in order to follow the power demand in

the short periods of times. The highly dynamic power cycle is due to the algorithm that keeps the switcher at constant speed during the whole route. Other algorithms can be implemented in order to produce less dynamic profile of the power duty cycle at which the controllers have better performance in following the power demand.

This section covers system integration and development for hybrid SOFC-GT system in 1 MW switcher locomotive. The report addresses prototype system development for this type of switchers. Also a test railroad route (Bakersfield-Mojave) has been chosen in order to analyze the SOFC-GT performance on the route. Parametric studies have been accomplished in order to find the optimal design of the system that can effectively meet the power demand profile.



Fig. (6.1) shows the tested route for hybrid SOFC-GT Simulation.

Figure 6.1: Bakersfield-Mojave Route, Source: Google Earth

Table shows the list of switchers for hybrid SOFC-GT system modeling. The following shows the total produced and the power output of the locomotives. The table shows the total units of the switcher produced and the power output per kW.

Model Designation	Build Year	Total Produced	Power Ouput
EMC pre SC	1935	2	600 hp (447 kW)
NW 1	1937-1939	27	900 hp (671 kW)
NW 2	1939-1949	1,145	1,000 hp (750 kW)
NW3	1939-1942	7	1,000 hp (750 kW)
TR	1940	3	2,000 hp (1,490 kW)
TR 1	1941	2	2,700hp (2,013 kW)
SW 7	1949-1951	489	1,200 hp (895 kW)
SW 8	1950-1954	815	1,200 hp (890 kW)
SW 9	1950-1953	815	1,200 hp (890 kW)
SW 600	1954-1962	15	600 hp (447 kW)
SW 900	1954-1969	371	900 hp (670 kW)
SW 1500	1966-1974	808	1,1500 hp (1,100 kW)
SW 1200	1954-1969	1,054	1,100 hp (890 kW)

Table 6.1: List of locomotive switchers, Source: Wikipedia

The modeling process is divided into two sections of modeling the switcher and modeling the switcher and modeling the long haul locomotive. The switcher modeling is used in order to develop small 1 MW order prototype system.

#### 6.1.2 **PROTOTYPE DEVELOPMENT**

In order to develop the prototype, a full dynamic model of the locomotive system has been developed in the MATLAB/Simulink platform. Locomotive traction and dynamic braking have evolved over many years. In diesel locomotives, eight notches for the throttle control emerged based on a three-valve fuel control. It should be noted that, more modern locomotives have different numbers of notches and levels of dynamics braking. In the current study, 8 notches have been modeled for the control system. System of the locomotive is designed for a 1 MW switcher similar to EMD RS 1325. A single vehicle model is developed in MAT-LAB/Simulink platform. The total distance on the rail yard is calculated based on double

integration of traction force. The net force on locomotive is calculated based on rolling resistance, air and axle resistance and the switcher weight. Fig. (6.2) and Fig. (6.3) shows the power duty cycles for long-haul and switcher locomotives with maximum power of 1 MW.



Figure 6.2: Power Duty Cycle of a 1 MW switcher locomotive



Figure 6.3: Power Duty Cycle of a 3 MW switcher locomotive

The dynamic traction force is calculated from the equation:

For: 
$$F_{t/db} \times v < \left(\frac{N^2}{64}\right) \times P_{max}, F_{t/db} = \frac{N}{8} \times Te_{max} - k_f \times v$$
  
(6.1)

Else: 
$$F_{t/db} = \left(\frac{N^2}{64}\right) \times \frac{P_{max}}{v}$$
(6.2)

Where N is the throttle setting in notches, 0-8;  $P_{max}$  is the maximum locomotive traction horsepower in watts;  $Te_{max}$  is the maximum locomotive traction force, N and  $k_f$  is the torque reduction, N/(m/s).

A control system has been developed in this study. The system development for the locomotive is based on two main components of vehicle dynamics and notch calculation. The notch system takes speed of the locomotive, grade of the route, acceleration and traction/brake force as an input. The notching algorithm Several assumptions have been made in implementation of the notching algorithm: 1) The maximum desired train velocity was 60 miles per hour, 2) The minimum desired train velocity was 10 miles per hour, 3) The power notching progressed by one notch at a timestep (increasing or decreasing), (This decision is made by the locomotive driver), 4) Notching does not alternate rapidly between the the timesteps, 5) The sign of the grade has an effect on the decision making.

Fig. (6.10) shows the algorithm implemented for the notching system. The algorithm is developed by Martinez et al. [327].

#### 6.1.3 SYSTEM OPTIMIZATION

In order to optimize the system, the research group has done parametric analysis on the fuel cell design. We have changed the parameters of PEN average temperature, stack temperature difference, hydrogen and oxygen utilizations, voltage and current densities. In order to optimize the system, the research group has done parametric analysis on the fuel cell design. We have changed the parameters of PEN average temperature, stack temperature difference, hydrogen and oxygen utilizations and voltage and current densities.

Parametric study in order to find the optimal fuel cell configuration for the prototype manufacturing of the first hybrid SOFC-GT engine to be used in a 1 MW switcher has been accomplished. There are linear correlation between power and current, power and voltage, power and stack temperature difference, power and hydrogen utilization and power and oxygen utilization. As a result the set-point for hydrogen and oxygen utilization has been changed to the optimal value that maintains the maximum amount of hydrogen and oxygen utilization and maintains the stack temperature difference in a limited range (the relation between the power and hydrogen utilization, power and oxygen utilization and power and stack temperature difference is positively linear). The prototype system developed at NFCRC consists of solid oxide fuel cell (SOFC), gas turbine system, fuel preheater, fuel cell bypass and heat exchanger bypass valves. Fig. (6.4) to Fig. (6.7) the parametric analysis of the fuel cell design with respect to various fuel cell characteristics.



Figure 6.4: Optimal Parametric Study of Fuel Cell Stack

Fig. (6.5) shows the variation of stack temperature over time. At higher power density

the stack temperature difference is greater as the more power requirements lead to higher chemical reaction rates and higher level of operating temperatures. At high fuel utilization, the variation in the stack temperature difference is lower due to the fact that the stack operates more efficient.



Figure 6.5: Stack temperature difference with variation of power density and fuel utilization

Fig. (6.6) shows the variation of fuel cell voltage with steam to carbon ratio. At low steam to carbon ratio, the fuel cell operates at higher voltage due to the higher concentration of methane in the stream.



Figure 6.6: voltage variation at different fuel utilizations and steam to carbon ratio

Fig. (6.7) shows the stack temperature gradient at different levels of oxygen utilizations. At lower fuel utilization, the stack temperature gradient is higher. The oscillation of stack temperature difference is higher at low fuel utilization.



Figure 6.7: Stack temperature difference at different oxygen and fuel utilizations

#### 6.1.4 System Modeling

The prototype system developed at NFCRC consists of solid oxide fuel cell (SOFC), gas turbine system, fuel preheater, fuel cell bypass and heat exchanger bypass valves.

The compressor module consists of compressor map that calculates flow rate and efficiency of the compressor and gets the air flow rate, outlet pressure of the compressor and the rotational speed of the compressor as an input. The model solves the energy balance of the compressor. The system consists of fuel cell bypass.

Fuel cell mathematical modeling:

The mathematical modeling of the fuel cell stack has been developed in several studies by McLarty et al.. The system is consisted of 3D model that resolves heat transfer and fluid dynamics equations through in electrode and electrolyte layers. Eq. (6.3) to Eq. (6.4) governs the temperature state of the solid portion of heat exchanger, and includes the heat

transfer from both fluids and the conductive heat transfer between adjacent segments.

$$Q_{HT} = h_c A_{surf} \left(\frac{T_{in} + T_{out}}{2} - T_{solid}\right)$$
(6.3)

$$\frac{dT_{out}}{dt} = \frac{(h.\dot{n})_{in-out} - h_c A_{sur}(\frac{T_{in} + T_{out}}{2} - T_{solid})}{C_p V_{node} C}$$
(6.4)

The spatial discretization is generalized into n control volumes. The fuel cell modeling includes 2-D spatial discretization of the heat exchanger.

#### 6.1.5 GAS TURBINE DYNAMIC MODEL

A dynamic compressor and turbine model developed utilizing dynamic conversation equations and industry standard performance maps. The approach solves a dynamic torque balance equation for the shaft and includes mass storage for stall/surge analysis. The compressor model inputs include inlet temperature, pressure, and species concentrations, shaft speed, and an exhaust pressure. The flow rate supplied by the compressor and compression efficiency are determined from the empirical correlations using turbine speed, pressure ratio, and inlet temperature.

$$N_{RPM} = RPM \sqrt{\frac{T_0}{T_{des}} \cdot RPM_{des}}$$
(6.5)

$$N_{Flow} = \frac{Flow}{Flow_{des}} \cdot \frac{\sqrt{\frac{T_0}{T_{des}}}}{P_{in}/P_{des}}$$
(6.6)

$$PR = \frac{P_{out} \cdot P_{des}}{P_{in} \cdot PR_{des}}$$
(6.7)

The simulated turbine inputs are inlet temperature, inlet species concentration, inlet flow rate, and exhaust pressure.

$$\frac{dP}{dt} = \frac{(\dot{n}_{in} - \dot{n}_{out}).R_u.T_{inlet}}{V_{turb}}$$
(6.8)

$$\dot{n}_{out}\eta_{turb} = f(N_{RPM}, PR, T_{inlet})$$

$$\dot{W}_T = (h\dot{n})_{in} - \dot{n}_{out}[(h_{in} - h_{ises})\eta_T]$$

(6.10)
$$\frac{dT_s}{dt} = \frac{h_c A(T_f - T_s) + \epsilon \sigma A(T_a^4 - T_s^4 c)}{c_p m}$$
(6.11)

$$\frac{d\omega}{dt} = \frac{(\dot{W}_T - \dot{W}_C \dot{W}_{GEN})}{\omega I_0}$$
(6.12)

$$I_0 = \frac{\rho L \pi r^4}{2} \tag{6.13}$$

The recuperated gas turbine models have been calibrated regarding their efficiency and mass flow rate versus power generation for C65 gas turbine. The off-design performance are calibrated to test data at UC Irvine. The model has been compared to NETL facility to validate the open loop control response to fuel valve step change.

### 6.2 ROUTE SIMULATION

The simulated route for the simulation is the railroad from Bakersfield to Mojave. The elevation profile of the map has been obtained from Google API console. This route includes the famous Tehachapi loop. Fig. (6.8) shows the prototype model design of 1 MW solid oxide fuel cell - gas turbine system.



Figure 6.8: Prototype design of a 1 MW switcher locomotive



Fig. (6.9) shows the implementation of notching system.

Figure 6.9: Vehicle and Notching dynamic modeling

Notching Algorithm is as follows:

- The maximum desired train velocity was 60 miles per hour (26.82 meters per second).

- The power notching had to progress by one notch at a time, whether increasing or decreasing notch. This decision could be made at every time step of the overall simulation

- The same restriction was placed on the notching for braking

- A power notch of both zero and one indicated 25% system power; however, notch

- A notch of zero on both power and braking indicated a coasting situation.

- The sign of the grade (whether uphill or downhill) could influence the decision-making process.

- Acceleration influences the decision-making process



Figure 6.10: Notching algorithm

This algorithm has been applied in the MATLAB/Simulink platform, see Fig. (6.11).



Figure 6.11: Vehicle dynamics algorithm implementation





Figure 6.12: Notching dynamics over Bakersfield-Mojave Route

Fig. (6.13) shows the dynamics power requirements over the Bakersfield-Mojave route.



Figure 6.13: Power Dynamics over Bakersfield-Mojave Route

Fig. (6.14) shows the acceleration profile over the Bakersfield-Mojave route.



Figure 6.14: Acceleration dynamics over Bakersfield-Mojave Route

Fig. (6.15) shows the dynamics of the speed that is controlled at 26 m/s.



Figure 6.15: Speed dynamics over Bakersfield-Mojave Route

The current model of SOFC-GT system does not respond to high dynamic power profile. Due to high amount of computation in the system level of the MATLAB/Simulink platform, a less dynamic elevation and power profile has been developed. Fig. (6.16) shows the dynamic profile of the smoothed model.



Figure 6.16: Speed dynamics over Bakersfield-Mojave Route

Fig. (6.17) shows the model follows the load much better than the highly dynamic model.



Figure 6.17: Speed dynamics over Bakersfield-Mojave Route

## 6.3 PARAMETRIC STUDY FOR FUEL CELL POWER DENSITY Fig. (6.18) and Fig. (6.19) show the dynamic plot of the fuel cell power density simulation over Bakersfield-Mojave Route. In order to make the data interpretable, Fig. (6.20) shows the time independent data.



Figure 6.18: Fuel cell power Density variation with fuel utilization and time

Fig. (6.19) shows the data of fuel cell power density based on air flow and fuel utilization for Bakersfield-Mojave railroad path. The data is accumulated over time range of simulation. In general, the data demonstrates strong independency of fuel cell operation from the air flow. However there is strong correlation between the power density and the fuel utilization. At higher load power, where locomotive requires maximum traction force, higher fuel utilization is needed. The graph shows that the locomotive performance needs a high fuel utilization from 0.75 to 0.8. An economic algorithms can be developed to reduce the amount of fuel that is used in the locomotive.



Figure 6.19: Fuel cell power Density variation with fuel utilization and cathode outlet temperature Fig. (6.20) and Fig. (6.21) show the parametric analysis for fuel cell power density over fuel and oxygen utilization over the Bakersfield-Mojave route. The power profile is highly dependent on the fuel and oxygen utilizations. The performance data is accumulated over the time range of the simulation. Power profile is highly dependent on the fuel and oxygen utilizations. The performance data is accumulated over the time range of the simulation. Strong independency of fuel cell operation from the air flow rate is observed.



Figure 6.21: Interactive plot of fuel Cell Power Density data, and fuel cell efficiency over Bakersfield-Mojave route

## CHAPTER 7

# SUMMARY AND CONCLUSIONS

#### 7.1 SUMMARY

This research presents a review of part-load and transient operation, dynamics, control and optimization of hybrid solid oxide fuel cell - gas turbine (SOFC-GT) systems for various system configurations. Different types of stall/surge control strategies have been discussed. System optimization,  $CO_2$  capture and integration of hybrid SOFC-GT system with other cycles are summarized. The main conclusions of this thesis are as follows:

- In this effort, compressor stall/surge is investigated, that could significantly affect hybrid SOFC-GT system performance during sudden power demand perturbations. A multi-stage compressor was designed with a configuration similar to that available in an industrial multi-stage compressor (a similar design can be found in the 1.7 MW Kawasaki gas turbine model GPB17). This type of compressor in a 4 MW hybrid SOFC-GT locomotive engine. The transient operation of this type of industrial centrifugal compressor was analyzed using computational fluid dynamics (CFD) tools, which provided insights regarding the flow distribution in the compressor impellers during dynamic hybrid system operation. A transient pressure boundary condition that resulted from a load perturbation applied in a hybrid system.

tem dynamic simulation was applied to the CFD model of the compressor. The CFD model resolved the compressor dynamics that occurred in response to the pressure perturbation near the stall/surge limit line. The multi-stage compressor was shown to be robust to the pressure dynamics investigated, making it suitable (able to handle pressure perturbation of interest without going into deep stall/surge) for use in hybrid SOFC-GT stationary and locomotive applications. The multi-stage compressor is able to keep the air flow rate positive over the period of transient operation which prevents the flow from entering the severe deep surge region, which could otherwise lead to the hybrid system failure.

- Various design and control concepts for dynamic operation of hybrid SOFC-GT systems have been investigated and have demonstrated viable strategies for safe operation of the system with turbomachinery that exhibits constant shaft speed or variable shaft speed. In the case of variable turbine speed, as the speed of the turbine changes, additional control algorithms are required for handling the pressure fluctuations in the stack, making sure that they are not detrimental to stack operation or degradation.

- Considering the fact that few hybrid SOFC-GT systems have been built to-date, the literature regarding transient operation and control of such systems in remarkably rich. Extensive numerical modeling studies suggest that such hybrid systems can be designed to be quite controllable, robust to handling perturbations of various kinds, and even capable of highly dynamic operation. However, various experimental results show that obstacles are still present, suggesting that additional research and development of control strategies for transient operation may be required. Experimental investigation of transient hybrid operation is especially recommended since only a very limited number of prototype systems have been developed and evaluated to-date.

- The control of SOFC-GT systems has been studied extensively in the literature with models. The main research gap for SOFC-GT system includes robust control systems development that are demonstrated for dynamic operation of physical SOFC-GT systems. The studies show that controlling these systems to meet the power demand is critical and challenging, but possible with proper system design, control architecture, and control parameter selection. This remains a significant need for developing control strategies that can forestall or eliminate various degradation mechanisms, such as steep thermal gradients, fast electrical, flow, or thermal transients, anode fuel starvation, thermal management of all components, compressor stall and surge, etc. Additional challenges in hybrid SOFC-GT systems are associated with compressors that are sensitive to air density, so that the compressor work demand increases as air temperature increases. Since the fuel cell operates at a fixed temperature, some researchers have found it challenging to maintain sufficient compressor mass flow at high ambient temperature.

- The transient operation of industrial centrifugal compressor performance using computational fluid dynamics (CFD) tools was analyzed, which provided insights regarding the flow distribution in the compressor impellers. In order to simulate the real world compressor operation in the 500 kW test hybrid SOFC-GT system, a transient pressure boundary condition that resulted from a previous hybrid system dynamic simulation was applied to the compressor configurations. The pressure step change that resulted from the transient hybrid system response to a load perturbation, corresponded to a sudden change of compressor dynamics near the surge limit line. The single-stage compressor was shown to be robust to the pressure dynamics and would be suitable for use in hybrid SOFC-GT applications. The single-stage compressor is able to keep air flow over the period of transient operation while preventing the flow entering the severe deep surge region, which could otherwise lead to hybrid system failure.

- A MATLAB platform was developed for components of hybrid SOFC-GT system that could capture the transient operation of a hybrid engine in a locomotive as a response to the locomotive power requirements. Initial results of the fuel cell and gas turbine were obtained from the MATLAB code.

- Finally, the feasibility of a hybrid SOFC-GT system was investigated regarding the system sizing. The balance of plant and the main components of the system were sized through de-tailed calculation and a general schematic of the system sizing was generated and compared to the actual size of the GE dash 9 locomotive.

#### 7.2 CONCLUSION

The main conclusions of this dissertation are as follows:

Single-stage compressor, similar to the compressor used in the 200 kW Capstone micro gas turbine (C-200) could be possibly used in 500 kW hybrid SOFC-GT locomotive test engine.
A multi-stage compressor is shown to be robust to the pressure dynamics and suitable for use in hybrid SOFC-GT applications.

Single-stage compressor, similar to the compressor used in 200 kW Capstone micro gas turbine (C-200) could be possibly used in 500 kW hybrid SOFC-GT locomotive test engine
A multi-stage compressor is shown to be robust to the pressure dynamics and suitable for use in hybrid SOFC-GT applications.

- A SOFC - GT can fit the dimensions of conventional long-haul diesel-electric locomotives.
- Compressor stall/surge, can significantly affect hybrid SOFC-GT system performance during sudden power demand perturbations.

- A multi-stage compressor, similar to the compressor used in 1.7 MW Kawasaki (GPB17), is amenable for use in 4 MW hybrid SOFC-GT system long-haul locomotive system.

- The multi-stage compressor maintains air flow over the period of transient operation and thereby prevents the flow entering the severe deep surge region, which could otherwise lead to hybrid system failure. Proper design of control systems that can maintain the compressor mass flow rate can significantly reduce risk stall/surge in hybrid SOFC-GT system.

- Future control algorithms can reduced the delay time between the surge and reaching to the design air mass flow rate.

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