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Improved Modeling of β Electronic Recoils in Liquid Xenon Using LUX Calibration Data

The LUX Collaboration

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ABSTRACT: We report here methods and techniques for creating and improving a model that reproduces the scintillation and ionization response of a dual-phase liquid and gaseous xenon time-projection chamber. Starting with the recent release of the Noble Element Simulation Technique (NEST v2.0), electronic recoil data from the β decays of ^3H and ^{14}C in the Large Underground Xenon (LUX) detector were used to tune the model, in addition to external data sets that allow for extrapolation beyond the LUX data-taking conditions. This paper also presents techniques used for modeling complicated temporal and spatial detector pathologies that can adversely affect data using a simplified model framework. The methods outlined in this report show an example of the robust applications possible with NEST v2.0, while also providing the final electronic recoil model and detector parameters that will be used in the new analysis package, the LUX Legacy Analysis Monte Carlo Application (LLAMA), for accurate reproduction of the LUX data. As accurate background reproduction is crucial for the success of rare-event searches, such as dark matter direct detection experiments, the techniques outlined here can be used in other single-phase and dual-phase xenon detectors to assist with accurate ER background reproduction.

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Introduction

The Large Underground Xenon (LUX) Experiment was a dual-phase time projection chamber (TPC) equipped with 370 kg of liquid xenon (LXe), of which 250 kg was an active target. The LUX experiment took place in the Davis Cavern at the 4850' level of the Sanford Underground Research Facility (SURF) in Lead, South Dakota with the primary scientific purpose of detecting WIMP dark matter [1]. As a dual-phase TPC, LUX collected the prompt scintillation signal (S1) with two arrays each consisting of 61 photo-multiplier tubes (PMTs) located at the top and bottom of the detector. The ionized electrons were extracted with an applied electric field into a layer of gaseous xenon, where the electrons were accelerated to produce a secondary light signal (S2). The location of the S2 signal in the top PMT array provides the position of the event in the horizontal plane, x and y , while the time between the S1 and S2 pulses provides the depth of the interaction, z .

While being hosted in the Davis cavern, LUX was used to perform two WIMP searches. The first science run (WS2013) spanned from April to August 2013 [2, 3], while the second run (WS2014-16) started in September 2014 and ended in May 2016 [4]. The total exposure for the combined runs was 3.35×10^4 kg-days. LUX was decommissioned in September 2016.

Throughout the WS2014-16 science run, LUX's drift field experienced significant non-uniformity due to an accumulation of excess charge on the inner detector walls. The distribution of excess charge changed over the course of the WIMP search, creating a temporal and position-dependent drift field. Sophisticated modeling was performed to create accurate three-dimensional maps of LUX's electric fields and is described in detail in Ref. [5]. In addition, the scintillation and electroluminescent gain factors, g_1 and g_2 ², changed throughout the course of WS2014-16 [4]. WS2013 did not experience these detector effects in a significant manner.

In existing and upcoming large target LXe dark matter experiments, the most burdensome backgrounds are those from β decays of Rn daughters [6–9], underscoring the importance of measuring and reproducing the detector response to electronic recoils. In addition, there exist

² g_1 and g_2 are defined with respect to the expectation values, $\langle S1 \rangle = g_1 n_\gamma$ and $\langle S2 \rangle = g_2 n_e$, where n_γ and n_e are the numbers of photons and electrons that escape the interaction site after an energy deposition, respectively.

several dark matter candidate models where the dominant interaction with Standard Model matter occurs via electronic recoils [10, 11]. To characterize the detector response from β decays, LUX underwent multiple calibration campaigns measuring the light and charge yields from incident β particles, including those from ^3H and ^{14}C sources which have energy spectra extending out to 18.6 and 156 keV, respectively. As β -Xe interactions occur via electronic recoils (ER), these calibrations were used to characterize the detector’s response to ER-producing background radiation. There were multiple ^3H calibrations that took place periodically throughout LUX’s stay in the Davis campus, while a single ^{14}C calibration took place after WS2014-16 in August 2016 immediately before LUX was decommissioned. Details of the source injections system and processes can be found in Refs. [12, 13].

With the recent release of the second version of the Noble Element Simulation Technique (NEST v2.0) [14], the ER calibration responses were compared to the new NEST model. This model is based on empirical fits to data sets from virtually all existing photon and electron yield data taken with Xe targets, including the LUX WS2013 ^3H ER calibration data. NEST then provides efficient calculation of the observable detector response after a recoil event.

The NEST v2.0 framework was utilized to create the new LUX analysis package, the LUX Legacy Analysis Monte Carlo Application (LLAMA). LLAMA’s main purpose is to reproduce the detector response after an energy deposition with minimal deviation between the simulation results and actual data. While NEST v2.0 only allows for the simulation of a temporally static detector, LLAMA allows for interpolation of detector parameters as a function of time. Equipped with the detailed three-dimensional electric field maps, LLAMA can use the NEST models to reproduce all LUX data despite the significant spatial and temporal detector effects observed after WS2013. LLAMA also serves as an example of how to expand upon the NEST v2.0 framework in order to simulate a temporally dynamic detector.

Since the empirical models in NEST v2.0 were created by fitting to world data of light and charge yields in LXe, it is understandable to expect that NEST would slightly deviate from the data of a single experiment, especially for data that were not included in the fits. As the WS2014-16 and ^{14}C acquisition data sets were not included during the development of NEST v2.0, the model required additional tuning and optimization to consistently reproduce all LUX data. The purpose of this paper is to develop techniques and methodologies to minimize deviations when modeling ER backgrounds in a LXe detector. Therefore, we will describe in detail the process of optimizing NEST v2.0’s physics models for reproducing LUX data using LUX ER bands in $S1c\text{-}\log(S2c/S1c)$ space, where $S1c$ and $S2c$ are the *corrected* $S1$ and $S2$ signals that take into account possible position-dependence of g_1 and g_2 . In addition, results using temporal interpolation and the complete position-dependent electric field maps with LLAMA will be shown, displaying an expansion of the NEST v2.0 framework that can accurately account for dynamic detector parameters and data-taking conditions.

1 Optimizing the Mean Yields Model

Given the energy of the incident particle, the magnitude of the drift field at the interaction point, and the target Xe density, NEST v2.0 calculates the expected total number of particles generated during the interaction, n_q , and then it calculates the total electron yield [14]. The sum of electrons

and photons produced in an ER event is given by $n_q = n_e + n_{ph} = E/W$, where E is electronic recoil energy, and W is the average work function for scintillation and ionization in LXe and is approximately 13.7 eV [15]. By calculating the charge yields separately, the number of produced photons is simply the difference between total quanta and number of electrons. After the mean yields are calculated, fluctuations about the mean are calculated separately and applied to the result.

The NEST v2.0 β ER charge yield equation is a sum of two sigmoidal functions. To create the LUX yields model for use in LLAMA, and following work reported in Ref. [16], the NEST v2.0 double-sigmoid was reformulated as

$$Q_y(E, \mathcal{E}) = m_1 + \frac{m_2 - m_1}{(1 + (E/m_3)^{m_4})^{m_9}} + m_5 + \frac{0 - m_5}{(1 + (E/m_7)^{m_8})^{m_{10}}}, \quad (1.1)$$

where Q_y is the mean electron yield per unit energy, n_e/E . The individual m_i are free parameters that can be field-dependent and are tuned so that the first sigmoid models low energy charge yields and the second sigmoid controls the behavior at higher energies. Note that m_6 is explicitly set to zero; because m_6 controls the low-energy asymptote of the high-energy sigmoid, it has degenerate effects with m_1 , which controls the high-energy asymptote of the low-energy sigmoid. This double-sigmoid approach allows for the reproduction of older yields models based on first-principles approximations: the Thomas-Imel Box model (TIB) for low energy ER and Doke's formulation of Birk's Law (DB) for high-energy particle tracks [17, 18]. The TIB model approximates the recoil as a point-like scatter and assumes spherical symmetry of the produced particle cascade. At higher energies, the DB formulation assumes cylindrical symmetry of the particle cascade about a high-energy particle track. The medium-energy regime between these two idealized approximations is significantly harder to model [19], but the NEST sum of sigmoids allows for a smooth transition in this stitching region.

Using data from the WS2013 and WS2014-16 ^3H calibrations, the deviation between the simulated and actual S1c-log(S2c/S1c) band means was minimized. However, due to the significant temporal and spatial dependencies of the detector's gains and drift field that were observed in WS2014-16, simplifications of the detector geometry were required. Because of the temporal dependencies, the WS2014-16 data was split into four unequal date bins; the ^{14}C calibration that occurred after WS2014-16 is considered to be a part of a fifth separate date bin. In addition, NEST's framework does not allow for straightforward incorporation of the complicated field maps for WS2014-16, so each date bin was divided into four vertical slices of the detector's fiducial volume – each corresponding to a 65 μs window of drift time. The drift time is defined as the time between the beginning of the S1 and S2 pulses and represents the depth of the interaction. Explicitly, from top to bottom of the detector, these four drift windows are: $40 < t < 105$, $105 < t < 170$, $170 < t < 235$, and $235 < t < 300$, where t is the drift time measured in μs . To begin simulating the S1c-log(S2c/S1c) bands with NEST, each of the date bins was provided a mean g_1 and g_2 associated with the data taken in the relevant time period. For each bin of drift times, NEST randomly selects a field value for each event from a uniform distribution with mean and width related to the detailed field maps.

The tuning of the individual m_i reported in Ref. [16] provided a robust ER yields model, thus each m_i was preserved as much as possible while creating the LUX yields model. As charge yields from ^3H β ER fall into the TIB regime and bleed into the medium-energy stitching region, m_1 was

chosen as the free parameter for minimizing the deviation between the model and the data, as it directly affects the shape of the charge yields in the stitching region. Explicitly, m_1 was allowed to float to minimize the test statistic:

$$\Delta_\mu = \left| \sum (\mu_{NEST} - \mu_{data}) \right| + \sqrt{\sum (\mu_{NEST} - \mu_{data})^2}, \quad (1.2)$$

where μ represents the mean value of $\log(S2c/S1c)$ for a given bin of S1c, and the summation is over the total number of S1c bins. The width of the S1c bins was chosen to be 1 phd. Both terms are different representations of the total deviation of the band means; the first term vanishes for a perfect match, assuming that any noise is Gaussian, and the second term is the quadrature sum of the deviations, and was added in the event that the first term fell into a false minimum value. We note here that Δ_μ ignores the deviation in the Gaussian widths of the ER bands, as changes in the mean yields model had minimal effects on the band widths.

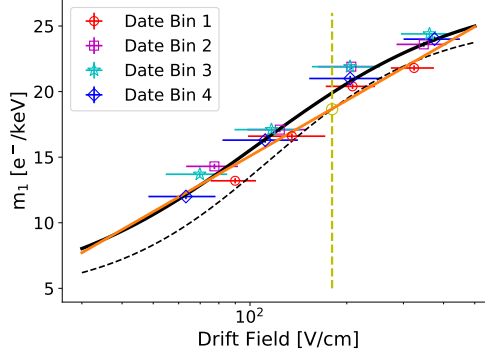


Figure 1. Best fit m_1 values for each bin of drift time associated with the four date bins of WS2014-16, along with the WS2013 best-fit value circled in yellow at 180 V/cm. The dashed black line represents the original m_1 model. The solid black line shows the average sigmoidal best fit to the WS2014-16 data, which disagreed with the result of the WS2013 data. Because WS2014-16 data experienced complex detector effects, the WS2013 m_1 value was used to constrain the fit. A logarithmic function was chosen to split the differences given the constraint, and this final function is shown in orange.

Figure 1 shows the resultant best fit m_1 found by minimizing Δ_μ using ^3H data from each of the 16 date-drift bins of WS2014-16, as well as for WS2013. The original m_1 model used a field-dependent sigmoid and agreed with the WS2013 data, therefore the WS2013 best fit value was used to constrain the final field-dependence of m_1 . However, re-tuning the m_1 model after including the WS2014-16 data did not comply with the WS2013 constraint. Therefore, the functional form was changed to be linear in log-field space to force agreement with WS2013 while simultaneously splitting the differences seen in the WS2014-16 data. With the simplifications made to model the LUX detector during WS2014-16 inside the NEST v2.0 framework, this additional emphasis on the WS2013 data was necessary, since it was more straightforward to fully model the detector conditions from WS2013.

This new functional form for m_1 grows infinitely with field strength, however, data from Doke *et al.* [20] of measured charge yields from 976 keV Compton scatters from ^{207}Bi suggest that m_1 reaches a maximum at large fields. Fitting to this data, a high-field asymptote was added to the m_1

model, and the comparisons to the ^{207}Bi light and charge yields can be seen in Figure 2. Although Compton scatters are γ ER, the difference in yields between γ and β interactions in LXe is likely due to the energy-dependent photoabsorption component of γ interactions. Data from Compton scatters should not have a significant photoabsorption component, thus, Compton scatters should largely mimic β interactions [13, 21]. While the field magnitudes where this cut-off is necessary are irrelevant to LUX data, this was included to allow extrapolation beyond LUX’s conditions for comparison with other detectors.

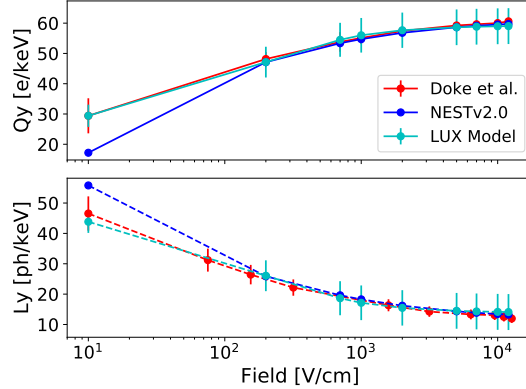


Figure 2. (Top) Comparison to the Doke *et al.* [20] charge yield data from 976 keV Compton scatters with the public version of NEST v2.0 and the optimized LUX ER Model. This data set was used to set a limit on the new m_1 model, at fields much larger than seen in any of the LUX acquisitions. The change to the m_1 and m_5 models also created a much better agreement with the low field data from this data set. (Bottom) Comparison to the Doke *et al.* light yield data with the public version of NEST v2.0 and the optimized LUX ER Model. This comparison highlights the anti-correlated behavior of light and charge yields, as NEST calculates light yields by subtracting charge yields from the total quanta produced in an energy deposition.

Note that as the amount of deposited energy becomes large, Equation 1.1 reduces to $Qy \approx m_1 + m_5$. Therefore, changing m_1 effectively alters the role of m_5 in the high-energy regime. For this reason, m_5 was constrained using the theoretical maximum charge yield. As $(n_e + n_\gamma) = E/W$, where n_e and n_γ are the total numbers of produced electrons and photons that leave the interaction site. Then, $Qy \equiv n_e/E = \frac{1}{W} \cdot [1 + \frac{n_\gamma}{n_e}]^{-1}$. The maximum charge yield occurs when the probability of recombination vanishes, causing $n_\gamma/n_e = \alpha$, where α is the ratio between excited and ionized xenon atoms and is constant for electronic recoils at the relevant energy scale for this analysis [19]. Therefore at large enough energies, $m_1 + m_5 \approx \frac{1}{W} \cdot [1 + \alpha]^{-1}$. The shape of the charge yields model in the Doke-Birks regime was also slightly re-tuned to compensate for this changing of asymptotes, which only required small modifications to the field-dependence in the original m_{10} model. The remaining m_i were untouched, as the original double-sigmoid model in Ref. [16] provided strong comparisons with world ER data, and only a slight re-tuning of the model in the medium-energy stitching region was needed.

2 Modeling the LUX Detector

After tuning the β ER yields model to better match LUX data, the focus was shifted to finding nominal g_1 and g_2 values for each date bin. While g_1 represents the total light collection efficiency and is a fundamental property of the TPC, g_2 is a product of other fundamental detector properties. Explicitly:

$$\begin{aligned} g_2 &= SE \cdot \epsilon_{ext}(\mathcal{E}_{gas}) \\ &= g_1^{gas} \cdot Y_e(\mathcal{E}_{gas}, \Delta z_{gas}) \cdot \epsilon_{ext}(\mathcal{E}_{gas}), \end{aligned} \quad (2.1)$$

where \mathcal{E}_{gas} is the applied electric field in the gas layer; Δz_{gas} is the height of the gas layer; g_1^{gas} is the collection efficiency of light produced in the gas layer; ϵ_{ext} is the efficiency to extract liberated electrons; and SE is the mean number of photons produced by a single extracted electron. Both SE and g_2 were measured multiple times throughout the course of LUX's science runs. With these, it was possible to provide NEST with starting values for g_1^{gas} and \mathcal{E}_{gas} after calculating the extraction efficiency using methods reported in [22]. For finding the best-fit values of g_2 , g_1^{gas} was chosen to be the free parameter, and the \mathcal{E}_{gas} values for each date bin were left untouched. These best-fit gain factors could then be used to create the continuous temporal g_1 and g_2 for use in LLAMA's temporal interpolation.

Also, with the simplifications made to the WS2014-16 electric field maps for use in the NEST v2.0 framework, it was expected that the mean fields used in each vertical slice of drift time would need to slightly shift from the mean values from the field maps. As mentioned in the preceding section, each drift bin was provided a range of electric fields that are associated with the mean and standard deviation of the fields in that drift bin from the relevant field map. For each modeled interaction, NEST selects the electric field from that range using a uniform random distribution. To find effective fields that allowed for proper reconstruction of the S1c-log(S2c/S1c) bands in this simplified framework, the mean field of each drift bin was treated as a free parameter. However, the mean field value in each bin was not allowed to deviate from the original value by more than one standard deviation. The widths of the field ranges were left fixed. This method was also used for the four drift bins associated with the ^{14}C acquisition. These effective fields can provide a weighting of the field maps in LLAMA to assist in data reproduction by fitting the best-fit field means with a continuous function of drift time. The WS2013 data did not require this spatial binning since significant field fringing was not observed during the first science run. Thus, a WS2013 effective field was not required and the full 3D position dependence was implemented.

Focusing on the WS2014-16 ^3H data and the ^{14}C acquisition, the deviation between the band means could be minimized for each bin of drift time. This was done by calculating Δ_μ from Eqn. 1.2 while simultaneously varying g_1 , g_1^{gas} , and the mean electric field, \mathcal{E} , for each drift bin. However, it was necessary to force g_1 and g_1^{gas} to take only one set of values for each date bin and to not differ across the fiducial volumes. This is because the position reconstruction of the S1 and S2 pulses should already take the position dependence of g_1 and g_2 into account. Therefore, the average deviation for all drift bins in a single date bin was minimized. Explicitly for a single date bin,

$$\Delta'_\mu = \frac{1}{4}[\Delta_{\mu 1}(g_1, g_1^{gas}, \mathcal{E}_1) + \Delta_{\mu 2}(g_1, g_1^{gas}, \mathcal{E}_2) + \Delta_{\mu 3}(g_1, g_1^{gas}, \mathcal{E}_3) + \Delta_{\mu 4}(g_1, g_1^{gas}, \mathcal{E}_4)] \quad (2.2)$$

was minimized, where the individual $\Delta_{\mu i}$ are the aforementioned test statistics (Δ_{μ}) for each drift bin. This forces the resultant optimal parameters to have equal g_1 and $g_1^{g^{as}}$ values for all drift time bins in a given date bin while each drift bin gets its own effective field.

For the WS2014-16 ^3H data, minimizing Eqn. 2.2 while varying the three free parameters for each date bin results in g_1 values of 0.0996 ± 0.0035 , 0.0994 ± 0.0032 , 0.0988 ± 0.0023 , and 0.0976 ± 0.0029 for the four date bins in temporal order. Taking the best fit $g_1^{g^{as}}$ values and converting back to g_2 results in g_2 values of 19.21 ± 0.37 , 19.66 ± 0.26 , 19.67 ± 0.22 , and 19.96 ± 0.28 . These results are consistent with those reported in [4]. The shifts needed for the mean field in each drift bin were similar across the four date bins, thus it was possible to obtain a single set of field multipliers for the WS2014-16 data by finding the weighted average with respect to each date bin's event density. In order of increasing drift time (which is the same as decreasing electric field strength,) these averaged multipliers are 0.98, 1.16, 0.96, and 0.86.

For the ^{14}C date bin, the best fit g_1 and calculated best fit g_2 are 0.0931 ± 0.0005 and 18.12 ± 0.09 , respectively, which are in agreement with those reported in [13]. The uncertainties on each g_1 and $g_1^{g^{as}}$ value are the standard deviations of the best fit g_1 and $g_1^{g^{as}}$ values for the four drift bins in the given date bin. The $g_1^{g^{as}}$ uncertainties were converted into uncertainties on g_2 using error propagation with Eqn. 2.1. The effective field multipliers that minimize the deviation between the ^{14}C comparisons are 0.94, 1.11, 0.88, and 0.70 in order of increasing drift time. Figure 3 shows the values of the effective fields compared to the original field means for each of the twenty drift bins.

For reproducing the WS2013 ^3H data, which did not require an effective electric field, the optimal g_1 and g_2 values are 0.1165 and 13.18. While the value for g_1 is in agreement with that previously reported in [12], this g_2 value is increased by 1.4σ . This suggests a possible over-estimation of the previously reported ^3H charge yields. All of the remaining detector parameters used in the NEST framework for WS2013, WS2014-16, and the Post-WS ^{14}C acquisition are included in Table 1.

3 Modeling Yield Fluctuations

All of the aforementioned model optimization compared only the deviation between the band means of the LUX data and simulated events in $S1c\text{-log}(S2c/S1c)$ space, ignoring comparisons between the Gaussian band widths. This was because changes in the mean yields model, g_1 , g_2 , and the mean drift field resulted in little change in the band widths. However, after the improved comparison between the band means, disagreements remained between the band widths, especially for data with larger S1s. This suggested that NEST's fluctuations models needed their own optimization to reproduce LUX data, and careful consideration of the possible contributions to fluctuations in S1 and S2 pulses was taken. Three sources of pulse fluctuations were identified: statistical quantum fluctuations in the total produced quanta, n_q , recombination fluctuations from ionized electrons recombining with xenon atoms before extraction, and additional random noise in pulse areas due to experimental detector effects. The first of these creates a correlated fluctuation in the S1 and S2 areas; as the total yield fluctuates, the number of electrons and photons should fluctuate in the same direction relative to the mean value. The second source, recombination fluctuations, are anti-correlated, as a recombining electron will excite a xenon atom, eventually leading to de-excitation and possible photon production. These two sources are fundamental to the atomic physics of energy

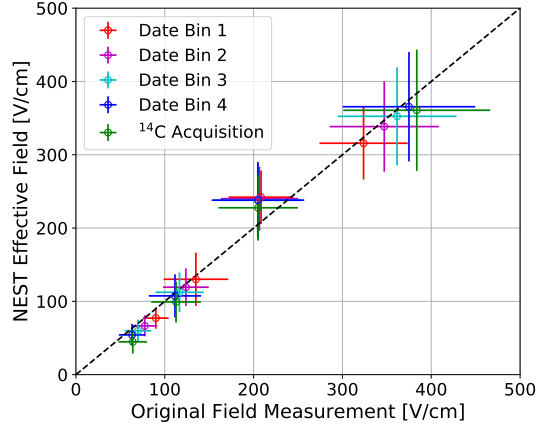


Figure 3. Effective fields for use in the NEST v2.0 framework, compared to the original field means and widths reported in Ref. [5]. The $y = x$ line is shown in dashed black. We note here that the mean and average deviations from the original measurements for WS2014-16 is 16% and 9%, which are more than a factor of two better than previously reported using older versions of NEST. Including the deviations of the ^{14}C effective fields, the maximum and average deviations are 30% and 10%, which are still a large improvement compared to those previously reported that did not include ^{14}C data.

Table 1. Remaining parameters used in for modeling the LUX detector in the NEST v2.0 framework for each time period. In the entries where four values are provided in WS2014-16, each value corresponds to one of the four date bins.

| | WS2013 | WS2014-16 | Post-WS |
|--|------------------|--------------------------------|------------------|
| Primary Scintillation (S1) Parameters | | | |
| Single Photoelectron Resolution | 0.37 | 0.37 | 0.37 |
| Single Photoelectron Threshold [phe] | 0.38 | 0.38 | 0.38 |
| Single Photoelectron Efficiency | 1 | 1 | 1 |
| Gaussian Baseline Noise [phe] | -0.01 ± 0.08 | -0.01 ± 0.08 | -0.01 ± 0.08 |
| Double Photoelectron Emission Probability | 0.173 | 0.173 | 0.173 |
| Ionization and Secondary Scintillation (S2) Parameters | | | |
| g_1^{gas} | 0.1 | 0.0852, 0.0928, 0.0898, 0.0854 | 0.0769 |
| Single Electron Size Fano-like Factor | 3.7 | 0.8, 1.95, 2.49, 2.67 | 2.6 |
| S2 Threshold [phe] | 192.3 | 234.6 | 234.6 |
| Extraction Region Field [kV/cm] | 6.55 | 8.134, 7.95, 8.047, 8.087 | 8.269 |
| Electron Lifetime [μs] | 800 | 735, 947, 871, 871 | 947 |
| Thermodynamic Properties | | | |
| Temperature [K] | 173 | 177 | 177 |
| Gas Pressure [bar] | 1.57 | 1.95 | 1.95 |
| Geometric Parameters | | | |
| Minimum Drift Time [μs] | 38 | 40 | 40 |
| Maximum Drift Time [μs] | 305 | 300 | 300 |
| Fiducial Radius [mm] | 180 | 200 | 200 |
| Detector Radius [mm] | 235 | 235 | 235 |
| LXe-GXe Border [mm] | 544.95 | 544.95 | 544.95 |
| Anode Level [mm] | 549.2 | 549.2 | 549.2 |
| Gate Level [mm] | 539.2 | 539.2 | 539.2 |
| Cathode Level [mm] | 56 | 56 | 55.9 |

depositions in xenon targets. The last source of fluctuations, noise from detector effects, can be different for any experiment and are not currently included in NEST v2.0. These fluctuations are

expected to have uncorrelated impacts on S1 and S2 size.

Comparing the calculated energy resolution in NEST v2.0 with those measured in WS2013 and reported by LUX in Ref. [23], the discrepancy is not significant compared to the differences seen in the simulated and measured S1c-log(S2c/S1c) band widths. Because recombination fluctuations have no significant effect on the combined energy resolution, this suggests that the correlated statistical fluctuations model in NEST v2.0 did not require any additional tuning for the LUX yields model. Therefore, we set our focus on tuning the NEST ER recombination model to reduce the remaining deviation in the S1c and S2c distributions.

Historically, modeling recombination as a binomial process - either an electron recombines or it does not - has been unable to fully explain the observed anti-correlated yield fluctuations in light and charge yields [24]. Reported by LUX in Ref. [23], recombination fluctuations on the number of produced ions, N_{ions} , have a variance of the form:

$$\sigma^2 = r(1-r)N_{ions} + \omega^2 N_{ions}^2. \quad (3.1)$$

The first term can be recognized as a binomial term with recombination probability, r , while the second term is the non-binomial correction weighted by a field-dependent parameter, ω . This is also the same form that recombination fluctuations take in the NEST v2.0 framework, with the weighting parameter, ω , represented by a field-dependent quadratic function of recombination probability which makes use of three free parameters. For optimizing the LUX yields model, NEST's ω representation was adopted, but simplifications were made by reducing the number of free parameters to a single field-dependent variable. Specifically,

$$\omega = -4c\left(r - \frac{1}{2}\right)^2 + c, \quad (3.2)$$

where c is the free parameter. This is useful as it forces the non-binomial variance contributions to vanish when r becomes zero or unity, and reaches a maximum when the probabilities for recombination and escape are equal. In addition, while NEST v2.0 models recombination fluctuations as a Gaussian process, data reveals that the final S2 distribution is more accurately represented by a skewed Gaussian distribution [25]. Therefore, the LUX yields model expanded upon the NEST v2.0 recombination model to incorporate skew in the final S2 distributions.

To begin the optimization process, a new test statistic was required, as the choice for the band mean optimization (Eqn. 2) was agnostic to the changes in the band widths. Therefore,

$$\Delta = \frac{1}{N} \left[\sum |\mu_{NEST} - \mu_{data}| + \sum |\sigma_{NEST} - \sigma_{data}| \right] \quad (3.3)$$

was chosen as the optimization test statistic: the summed average deviations of the band means and band widths. Here, μ is the mean value of log(S2c/S1c) for a given S1c bin, while σ is the standard deviation; μ and σ were found using Gaussian fits. As before, the summation takes place over the number of S1c bins. Although the band means have already been optimized, including the deviation between the means in Δ prevents any changes in the fluctuations adversely impacting the previously accomplished improvements.

Similar to the approach taken in the mean yields optimization, the free parameters were found that minimized the test statistic for each of the WS2013 and WS2014-2016 drift bins using ^3H data.

Figure 4 shows the best fit values of c for the 17 LUX bins, and also includes data points from XENON10 and ZEPLIN-III at higher fields than LUX [25, 26]. The inclusion of data from these different experiments allows for extrapolation of the recombination model beyond LUX’s data-taking conditions. These data also indicate asymptotic behavior in c as the drift field increases. Therefore, c was modeled as a field-dependent sigmoid and was fit to the WS2014-16 data. As with the band mean optimization, the WS2013 result was used to constrain the fit because the first science run did not experience significant temporal and spatial detector effects.

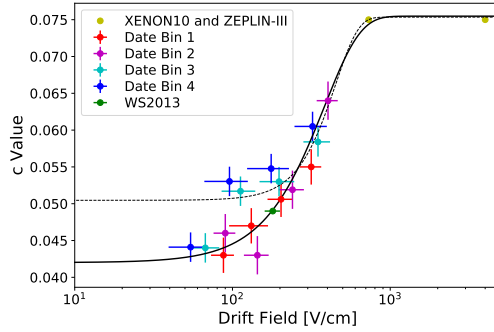


Figure 4. Best-fit c values as a function of field shown as a solid black line, found by fitting to the WS2013 and WS2014-16 ^3H data, as well as XENON10 and ZEPLIN-III data. Because of the similar values for XENON10 and ZEPLIN-III that suggest the need for a high-field asymptote, a sigmoid was chosen as the best fit function. This is the same functional form as used originally for NEST v2.0, indicated by the dashed black line. The fit to the WS2014-16 data was constrained using the WS2013 result, as detector effects were not significant during this data collection campaign.

The data used in the ω model thus far was limited in range of the recombination probability, and as ω depends directly on r , it was important for extrapolation purposes to check the behavior of the model for a large spread of recombination probabilities. Data provided in a dissertation by C.E. Dahl [15] provides recombination fluctuation data for a wide range of electron fraction (defined as $n_e/(n_e + n_{ph})$), which is proportional to $(1 - r)$. Initial comparisons show that while the new LUX yields model provides better agreement with data when recombination is more probable than escape, the original NEST v2.0 model performs better at lower values of the recombination probability. Because of this, the LUX yields ω model was weighted with a recombination-dependent error function. Figure 5 shows this data compared to the NEST v2.0 model and the LUX model, both before and after this final modification. The effects of this change on the LUX data comparisons were negligible for all of the relevant fields and energies, so re-optimization of the LUX model parameters was not necessary.

4 Modeling Detector Noise in S1 and S2 Pulses

With the newly finished recombination model optimized for a wide range of recombination probabilities, the last source of yield fluctuations to address were those from detector effects. It is understandable that this would be necessary for the WS2014-16 and ^{14}C data, as the field non-uniformity and time-dependent light collection efficiencies made proper simulation of the LUX

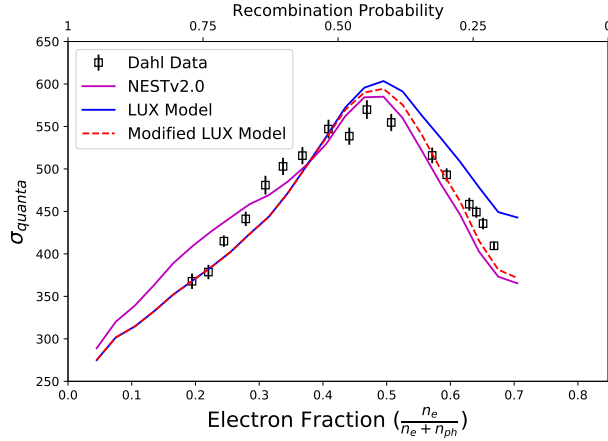


Figure 5. Recombination fluctuations as a function of the ratio of electrons to total quanta compared with the NEST v2.0 model (magenta) and the LUX yields model before and after modification with an error function (solid blue and dashed red, respectively). The electron fraction is equal to $(1 - r)/(\alpha + 1)$, where r is the recombination probability and α is the ratio of excitons to ions produced in the original energy deposition.

data difficult. These fluctuations were modeled as corrections on the S1 or S2 pulse area, A , using a Gaussian smearing with a standard deviation, λA , where λ is a free parameter that encapsulates complicated or unknown detector effects that impact the area of the detected S1 or S2, similar to the techniques used in Ref. [15]. For simplicity, λ was chosen to be identical for smearing of both S1 and S2 pulses.

Best-fit λ values were found for the ^3H data from WS2013 and each WS2014-16 date bin, as well as for the ^{14}C acquisition. Because the effects of this method of modeling detector noise increase as the pulse areas increase, the test statistic (Eqn. 3.3) was minimized using data out to the largest S1s available for a given date bin: 115 phd for WS2013 ^3H data and between 80 and 100 phd for WS2014-16 ^3H data. The WS2014-16 S1 range is less than the maximum S1 for WS2013 because g_1 decreased and was changing during the second science run. For ^{14}C , only data with S1 pulses smaller than 300 phd were used, as the number of events becomes too few beyond this limit. For WS2013, the four WS2014-16 date bins, and the ^{14}C acquisition, the best fit values of λ are: $1.4 \pm 0.7\%$, $1.4 \pm 0.7\%$, $2.3 \pm 0.4\%$, $3.0 \pm 0.6\%$, $4.4 \pm 0.6\%$, and $7.0 \pm 0.1\%$, respectively. This is consistent with the expectation that detector effects were steadily increasing over time. As with the gain factors, g_1 and g_2 , a smooth temporal fit to these λ values can be added into LLAMA for accurate reproduction of the band widths for WS2014-16 and the ^{14}C acquisition.

5 Results

After tuning the NEST v2.0 mean ER charge yields and fluctuations models and finding optimal light collection efficiencies and effective drift fields, final comparisons can be made with the LUX data. Figures 6, 7, and 8 show the comparisons of the final LUX yields model to the WS2013 ^3H data, each of the 16 drift bins associated with the WS2014-16 ^3H data, and the four ^{14}C drift bins. The simulated bands were created with increased statistics to reduce the effects of Poisson fluctuations obscuring the final quantitative and qualitative results.

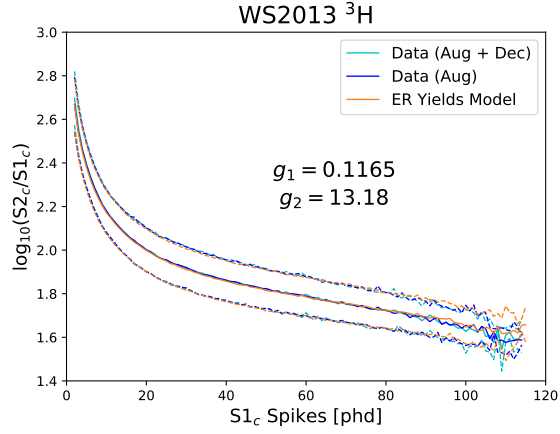


Figure 6. Comparison of the final LUX ER yields model using the NEST v2.0 framework with two different sets of LUX WS2013 ^3H data. The solid lines represent the Gaussian means of $\log(S2c/S1c)$ values inside each S1 bin. Dashed lines show the Gaussian widths of each S1 bin.

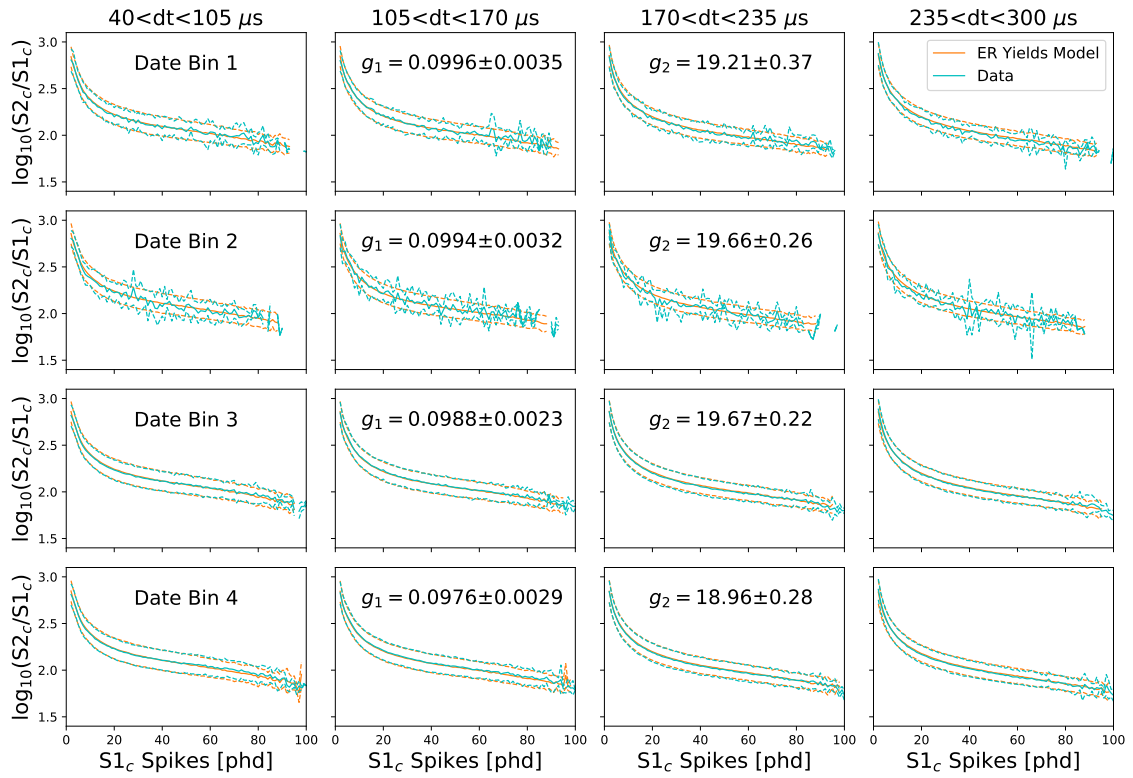


Figure 7. Comparison of the final LUX ER yields model using the NEST v2.0 framework with ^3H data from each of the WS2014-16 drift bins. Each row shows one of the four date bins with the best-fit g_1 and g_2 values, and each column represents one of the four bins of drift time. The solid lines represent the Gaussian means of $\log(S2c/S1c)$ values inside each S1 bin. Dashed lines show the Gaussian widths of each S1 bin.

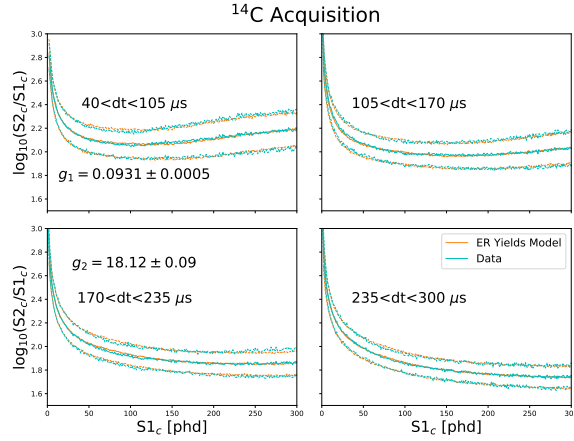


Figure 8. Comparison of NESTv2 and LUX post-Run04 ^{14}C data. Similarly to the Run04 data, ^{14}C data is split into four spatial bins of equal drift time. The solid lines represent the Gaussian means of $\log(S2c/S1c)$ values inside each S1 bin. Dashed lines show the Gaussian widths of each S1 bin. Note that units of S1s are expressed in either S1 spikes or pulse areas in phd. Typically, S1s less than approximately 120 phd will be expressed in terms of spikes, and anything larger will be expressed in terms of standard S1 pulse areas.

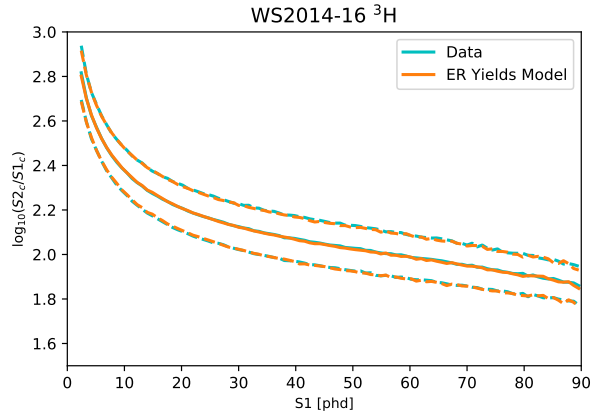


Figure 9. Comparison of the final LUX ER yields model using LLAMA with the WS2014-16 ^3H data. LLAMA uses the temporal dependence of g_1 and g_2 found with the four date bins. In addition, the full time-dependent and position-dependent field map is used and is weighted with the optimized effective field multipliers found with the discretized approach.

In addition to this discretized approach, Figures 9 and 10 show the comparison using LLAMA for the total WS2014-16 band and the ^{14}C band. Using the best-fit detector parameters and creating continuous temporal functions for each one allows LLAMA to take the newly modified NEST ER models and accurately reproduce the LUX data, despite the significant detector pathologies that affected the data.

Table 2 shows the remaining net average relative deviation between each comparison. For the band means, the average deviations never become larger than 1%, quantitatively indicating good agreement between the data and simulations. The magnitude of the net deviations for the band

Table 2. Average signed deviation between the NEST simulation and LUX data for each acquisition period for both the means and widths, calculated as $(X_{NEST} - X_{LUX})/X_{NEST}$, since the LUX data was limited in statistics and dividing by a data point with a significant downward fluctuation would inflate the calculated deviations. The sub-percent deviations along with the variation between positive and negative values indicate that there is no systematic offset between the simulation and the data. The large deviation in the widths for the lowest field bin in Date Bin 2 is due to low statistics in the data, and this can be seen in the corresponding pane of Figure 7.

| LUX Acquisition | Drift Time Bin | Max S1 | Avg Deviation: Means | Avg Deviation: Widths |
|-------------------------|----------------|--------|----------------------|-----------------------|
| Run 3 | - | 105 | 0.01% | -0.31% |
| Run 4: Date Bin 1 | 1 | 70 | 0.11% | 2.06% |
| | 2 | 70 | -0.21% | 2.19% |
| | 3 | 70 | 0.37% | -1.12% |
| | 4 | 70 | 0.65% | 2.13% |
| Run 4: Date Bin 2 | 1 | 70 | 0.33% | -5.77% |
| | 2 | 70 | -0.25% | -2.94% |
| | 3 | 70 | 0.39% | -2.85% |
| | 4 | 70 | 0.34% | 16.10% |
| Run 4: Date Bin 3 | 1 | 70 | 0.11% | 1.83% |
| | 2 | 70 | -0.22% | -0.40% |
| | 3 | 70 | 0.39% | -4.51% |
| | 4 | 70 | 0.20% | -0.90% |
| Run 4: Date Bin 4 | 1 | 70 | -0.09% | 1.62% |
| | 2 | 70 | -0.30% | 0.12% |
| | 3 | 70 | 0.38% | -4.71% |
| | 4 | 70 | 0.35% | 0.91% |
| Run 4: C-14 Acquisition | 1 | 300 | -0.10% | -0.31% |
| | 2 | 300 | -0.33% | -1.25% |
| | 3 | 300 | 0.01% | -5.47% |
| | 4 | 300 | -0.22% | 3.72% |
| Averages | - | - | 0.09% | -1.79% |

widths are on average larger than those for the band means. This is due to larger Poisson fluctuations and relative uncertainties in the band width calculations and measurements. These values also show that the remaining deviation does not appear to be systematically offset. Importantly, these final values reveal that very little additional progress can be made beyond the improvements presented here.

Conclusion

The final LUX backgrounds model requires an ER yields model that can mimic the data collected throughout the LUX experiment. The techniques and methods described in this paper present a detailed and robust application of NEST v2.0 for use in accurately reproducing light and charge yields from TPCs with xenon targets. With minimal tuning of the NEST v2.0 models, it was possible to reproduce LUX ER calibration data from each of the different acquisition time periods. Even with the significant field fringing and time-dependent light collection efficiencies present in the

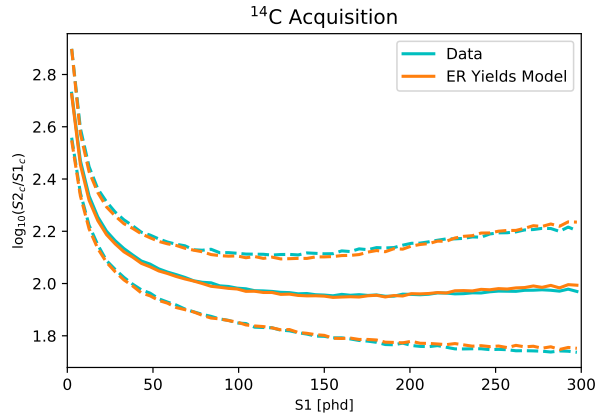


Figure 10. Comparison of the final LUX ER yields model using LLAMA with the ^{14}C acquisition data. This comparison uses the full position-dependent field map and is weighted with the optimized effective field multipliers found for the ^{14}C data with the discretized approach.

data beyond WS2013, the NEST v2.0 framework was able to accurately and efficiently encapsulate these effects with simplified geometry after binning the detector spatially and temporally, while also providing nominal values of g_1 and g_2 for each time bin and nominal effective electric field ranges. The results found using the temporal and spatial binning of the LUX detector were interpolated to create smooth functions for the relevant detector parameters. Expanding upon the NEST v2.0 framework to create LLAMA for simulating a temporally dynamic detector, this final model can accurately reproduce all LUX ER data, despite the significant detector pathologies observed in later data acquisitions. The completed LLAMA framework equipped with the final LUX ER model will be used for all future background modeling in upcoming LUX analyses.

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