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Impacts of longitudinal air velocity and fuel flow rate on flame radiative fraction in tunnel

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ABSTRACT

Fires in tunnels have attracted special attention in recent years due to catastrophic fires, which cause huge human and economic losses. For accurate fire modelling and ventilation system design, it is critical to understand the correct radiative fraction (X_r) of the flame. Recent study has proved that X_r decreases with the increase of longitudinal air velocity in heptane pool fires. However, the impacts of longitudinal air velocity and fuel flow rate on X_r in propane or liquefied petroleum gas tunnel fires have not been studied. To fill the gap, this paper conducts two sets of fire experiments in a 1/20 reduced-scale wind tunnel using a porous burner. Unique visible flame shapes are observed and described by the ‘back-to-back conical frustum’. The geometric parameters and their variations with the momentum flux ratio are discussed. In comparison with the experimental results, the radiation model using the proposed flame shape shows an 80% accuracy. The predictive radiative fractions of the two tests are calculated and compared with other tests from literature. The coupling effects of longitudinal air velocity and fuel flow rate on the flame radiative fraction are studied in detail. And their influences on key parameters of smoke extraction system are analyzed.

Keywords:

tunnel fire; radiative fraction; longitudinal air velocity; fuel flow rate; experiment

Nomenclature

A_f	Area of flame surface (m ²)	s	Offset distance of the visible flame (m)
C_T	Temperature correction factor (-)	v_{cri}	Critical velocity of longitudinal ventilation (m/s)
D_1	Diameter of the bottom surface of visible flame (m)	v_{in}	Longitudinal air velocity (m/s)
D_2	Diameter of the top surface of visible flame (m)	v_j	Fuel velocity at burner exit (m/s)
D_{max}	Maximum diameter of visible flame (m)	X_r	Radiative fraction (-)
D_s	Diameter of fire source (m)	z	Height above the fire source (m)
D_e	Hydraulic tunnel height (m)	ρ_j	Density of fuel (kg/m ³)
E_f	Average emissive power at the flame surface (kW/m ²)	ρ_{in}	Density of longitudinal airflow (kg/m ³)
F	Geometric view factor (-)	α	Flame tilt angle (degree)
G_j	Volume flow rate of fuel (l/h)	α_f	Tilt angle of flame axis (degree)
H	Flame length (m)	η	Combustion efficiency (-)
H_f	Length of flame axis (m)	τ	Effective atmospheric transmissivity (-)
H_{ef}	Vertical distance above fire source	ΔH_c	Combustion heat of fuel (MJ/kg)
		ΔT_{max}	Maximum excess gas temperature beneath tunnel ceiling (K)

	bottom (m)		Subscript
J	Momentum flux ratio (-)	c	Convective
m_j	Mass flow rate of fuel(kg/s)	f	Flame
m_{flume}	Fire plume mass flow rate (kg/s)	j	Fuel
Q	Total heat release rate (kW)	hf	Heat flux meter or radiometer
Q_c	Convective heat release rate (kW)	in	Air flow
Q_r	Radiative heat release rate (kW)	p	Predicted theoretically
Q_c^*	Dimensionless heat release rate (-)	r	Radiative
q	Radiant heat flux (kW/m ²)		

26 1. Introduction

27 During the past decade, several tunnel fires with heavy casualties and property losses occurred
 28 in Europe: such as Mount Blanc (1999), Tauern (1999) and Gotthard (2001) (Lu, 2006,
 29 EBERL,2001). For example, 39 people were killed in the 1999 Mont Blanc Tunnel fire. The
 30 maximum heat release rate reached 300 MW and destroyed three quarters of a mile of the concrete
 31 dome. The repairs took three years to complete with a total loss of \$200 million (Isolatek
 32 International,2020). After a series of severe fire accidents, fire safety in the tunnel attracts significant
 33 attentions and becomes a very important issue.

34 In the engineering design of ventilation and evacuation systems, the total heat release rate of
 35 fire(Q), especially its convective part (Q_c) is a key parameter. Its value directly affects the smoke
 36 flow rate (Li, Lei, & Ingason, 2011), smoke temperature (Tang, He, Chen, & Li, 2019; Yi, Wang,
 37 Yang, Wang, & Zhou, 2020) and critical velocity of longitudinal ventilation (Kennedy & Parsons,
 38 1996) etc.

39 In order to facilitate the analysis and design, the radiative fraction (X_r) is introduced to
 40 characterize the radiation characteristics from the flame. Since the radiative heat is lost at the source,
 41 only the convective heat release rate (Q_c) transfers with the smoke flow in tunnel. Q_c can be
 42 calculated using X_r as follows:

$$Q_c = (1 - X_r)Q \quad (1)$$

43 To determine the value of Q_c , former studies mainly focused on understanding fire development
 44 and the influences of tunnel conditions on Q . The value of X_r is usually assumed to be a constant
 45 number, with a range of 0.2-0.4 (Yi, Wang, Yang, Wang, & Zhou, 2020; Ingason, Li, & Lönnemark,
 46 2015; Mégret & Vauquelin, 2000; Liu, Yang, Xiao, Mao, & Yang, 2018). However, this assumption
 47 is based on oil pool fire data in the open still air (Koseki & Hayasaka, 1989; Markatos, Malin, &
 48 Cox, 1982). For tunnel fires, the follow questions still need to be explored: 1. Whether the values of
 49 X_r also vary with tunnel conditions, especially with different longitudinal air velocity? 2. As the air
 50 velocity changes, does X_r increase or decrease? 3. Whether X_r will further affect the design of the
 51 smoke exhaust system in the tunnel?



Fig.1 Flame images at different longitudinal air velocities for a 60cm heptane pool fire (Hu, L. et al.,2016)

52 As exhibited in Fig.1, the shape, volume and luminosity of the flame change significantly with

53 the variation of the longitudinal air velocity (Hu, Zhang, Delichatsios, Wu, & Kuang, 2017). It
54 demonstrates that, under the influence of the longitudinal air flow, X_r may depart from the usually
55 assumed constant value of 0.2-0.4 (Turns, 2011; Delichatsios, & Orloff, 1989). This hypothesis has
56 been recently proved by experiments (Zhang, Hu, Wu, Kostiuk, 2019). For the medium size square
57 heptane and acetone pool fires, Zhang et al. found that X_r decreased with the increase of longitudinal
58 air velocity. The decrease was observed to be more prominent as the pool size became smaller, and
59 a bit more prominent for heptane than for acetone.

60 Besides the heptane pool fire, the porous burner using propane or liquefied petroleum gas (LPG)
61 as fuel is often used as the fire source in the reduced scale tunnel experiments (Tang, He, Chen, &
62 Li, 2019; Li, Lei, & Ingason, 2011). For this type of fire source, how to measure the flame radiative
63 fraction in the reduced-scale tunnel experiments? How does the radiative fraction change with the
64 longitudinal air velocity and fuel flow rate? How to evaluate their coupling effect on the value of
65 X_r ? These problems deserve further discussion.

66 The flame radiative fraction, X_r , can be calculated by:

$$X_r = \frac{Q_r}{Q} = \frac{Q_r}{m_f \eta \Delta H_c} \quad (2)$$

67 Where m_f and ΔH_c are the fuel mass flow rate and the heat of combustion, respectively. η is the
68 combustion efficiency of the flame. For data presented by Johnson and Kostiuk (2000), the
69 combustion efficiency of propane diffusion flame was found to be insensitive to crosswind, such
70 that the lowest efficiency would be 99%. In the following analysis, the combustion efficiency of the
71 flame is initially assumed to be 100%. Q_r is the total radiated energy, which cannot be easily
72 measured and is usually inferred from the specific radiation prediction model.

73 The most widely used radiation prediction model is the single point source model (SPS).
74 Sivathanu and Gore (1993) obtained X_r of jet diffusion flames of CH_4 , C_2H_2 , C_2H_4 in open still air.
75 However, the distance between the radiometer and the flame center should be larger than 2.5D (D
76 is the fire source diameter) to satisfy the point source assumption (Modak, 1977). In addition, the
77 radiometer should be positioned at a vertical location equal to 50% of the flame height and
78 perpendicular to the flame axis (Hamins, Klassen, Gore, & Kashiwagi, 1991). This seems to be
79 somewhat more complicated and difficult to implement for the tilted flame in the longitudinal air
80 flow. In Zhang's experiments, the radiometer was not perpendicular to the flame axis. To eliminate
81 this position effect on the results, the horizontal distance between the pool and the radiometer was
82 extended to 11.2~28D. Apparently, such a large distance is not practical in the reduced-scale tests,
83 due to the rapid decrease of heat flux with the increasing distance (Guo, 2019).

84 To overcome the limitations of the SPS model, Hankinson and Lowesmith (2012) proposed the
85 weighted multi-point source model (WMP) by assuming that the radiation emanated from a number
86 of point sources distributed along the flame axis. Unlike SPS model, WMP model can provide good
87 predictions in the near field of the fire source (Zhou, Zeng, Li, & Chaos, 2017). However, the
88 accuracy of the WMP model is highly dependent on the determination of the weighting profile of
89 the point sources, which needs a large number of measurement points. For example, the number of
90 points was 50 in Zhou's analysis (2017). For a tilted flame, keeping the 50 radiometers perpendicular
91 to the flame axis in the experiments is almost impossible. Namely, the WMP model is not suitable
92 to study the influence of longitudinal airflow in the reduced-scale tunnel tests.

93 Because of the above limitations, other alternative methods should be introduced. The solid
94 flame model may be a good option, which has been proved to accurately predict the incident radiant

95 heat flux in near field of fire source (Mudan, 1987; Wan, Gao, Ji, Sun, Zhang, & Li, 2018). The
 96 model assumes that energy emission radiates uniformly over the entire visible flame envelope. The
 97 incident radiation flux, q_{hf} , received by the radiometer, is predicted as below:

$$q_{p,hf} = \tau_{hf} E_f F_{hf-A_f} \quad (3)$$

98 Where τ_{hf} is the effective atmospheric transmissivity between the radiometer and flame. In the near
 99 fire source region (path length less than 10m), $\tau_{hf}=1$ (Wayne, 1991). F_{hf-A_f} is the geometric view
 100 factor from the radiometer to the flame, the detailed calculation method can be found in Guo's paper
 101 (2019). E_f is the average emissive power at flame surface, and can be calculated in the following
 102 manner:

$$E_f = \frac{m_j \Delta H_c X_r}{A_f} \quad (4)$$

103 Where A_f is the area of flame surface, m^2 . Assuming that the measured radiant heat flux by the
 104 radiometer ($q_{m,hf}$) is equal to the predicted value ($q_{p,hf}$) from equation (3), substitution of the
 105 equations (2), (4) into equation (3) results in:

$$X_r = \frac{q_{m,hf} A_f}{m_j \Delta H_c F_{hf-A_f}} \quad (5)$$

106 According to equation (5), the most important step to determine X_r is to accurately describe the
 107 flame shape, and calculate A_f and F_{hf-A_f} . As long as the incident radiant heat flux on the radiometer
 108 position by equation (3) can be well-predicted, this method can be used to determine the flame
 109 radiative fraction. As the radiometer's position is already considered and calculated by the geometric
 110 view factor, it does not matter whether the radiometer in the near area of fire source is perpendicular
 111 to the flame axis or not.

112 In conclusion, the flame radiative fraction is usually assumed to be a constant number, with an
 113 average of 0.3. However, this assumption is based on oil pool fire experiment data in the open still
 114 air, which may not be valid for fires in tunnel. Recent study has proved that X_r decreases with the
 115 increase of longitudinal air velocity in heptane pool fires. To fill the research gaps, this paper studies
 116 the impact of longitudinal air velocity and fuel flow rate on flame radiative fraction in propane or
 117 liquefied petroleum gas tunnel fires.

118 2. Experiments

119 2.1 Motivation of experiments

120 Therefore, a series of experiments are conducted in a 1/20 reduced scale model tunnel,
 121 including different combinations of fuel flow rate and longitudinal air velocity. Two gas burners
 122 with different sizes are chosen as the fire sources in the experiments. The geometric parameters of
 123 visible flame shape are described in detail. The incident radiative flux on the position of radiometer
 124 is predicted using theoretical calculation and compared with the experimental measurements. The
 125 values of X_r are further calculated, and its variations with the longitudinal air velocity and fuel flow
 126 rate are detailed analyzed.

127 2.2 Experimental rigs

128 As exhibited in Fig.2, the model tunnel corresponds to a 1/20 scale reduction of a standard two-
 129 lane road tunnel. It has 2 windows (0.5m*0.29m) made of transparent heat-resistant glass through

130 which the flame can be observed. Fr scaling is used in the study and the scaling correlations of the
 131 model tunnel are presented in Table 1. Two porous burners are placed at the center, and align with
 132 the tunnel floor. A porous bed with a honeycomb on its top is located on a# for test 1. A 30mm
 133 diameter Bunsen burner (NG-2411BO0034, JUCHHEIM Inc.) is placed on b# for test 2, whose
 134 primary air is completely turned off during the experiments. The ventilation air is supplied through
 135 an 80mm steel pipe fitted with an orifice plate, providing a useful method to determine the
 136 volumetric flow. The longitudinal ventilation velocity is calculated by dividing the volumetric flow
 137 by the tunnel cross-sectional area. At different locations and aligned with the ground level, four
 138 water-cooled heat flux meters of type Schmidt-Bolter are placed to record the incident radiative flux.
 139 The incident radiant flux values are measured at 1#, 2# for test 1 and 3#, 4# for test 2, respectively.
 140 20 measuring probes are set at the 1-1 section. The data are collected from the 20 sampling probes.
 141 A series of preprocessing are conducted, including condensing, drying, filtering, before the smoke
 142 are mixed to measure the mean concentrations of O₂, CO, CO₂. The schematic of the gas analysis
 143 system is also shown in Fig.2. The oxygen consumption calorimetry is used to determine the heat
 144 release rate in a tunnel fire. The experiments are conducted at different longitudinal air velocities
 145 (v_{in}) and at different fuel flow rates (G_j). The relevant data about the experimental cases and the
 146 chemical composition of LPG used in this paper are listed in Table 2 and Table 3.

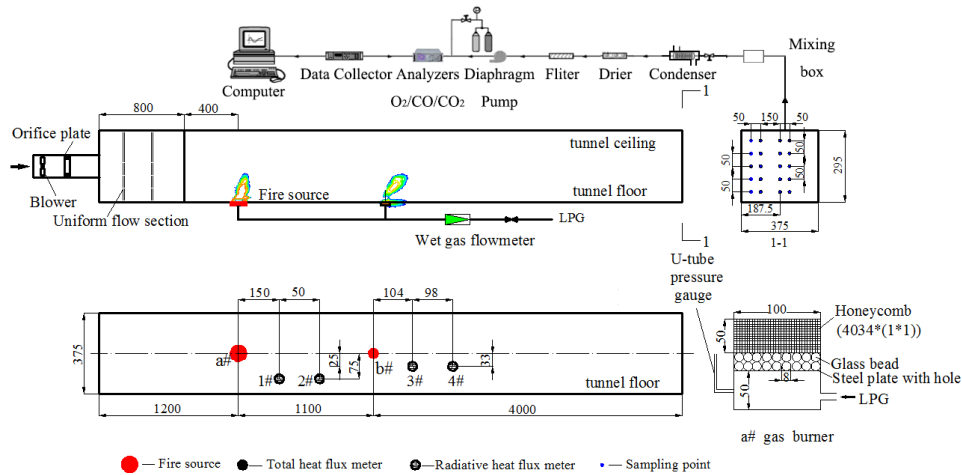


Fig.2. Schematic view of the experimental system (in mm).

147

Table 1

148

A list of scaling correlations for the model tunnel.

Length	Velocity	Flow rate	Heat release rate
1/20	$(1/20)^{1/2}$	$(1/20)^{5/2}$	$(1/20)^{5/2}$

149

Table 2

150

Relevant data of test cases used in this study.

Test	Fire source	D_s/cm	Q/kW	$G_j/l/h$	$v_{in}/m/s$	J^1
test 1	a#	10	2.82~4.92	95~162	0.10~0.37	<0.03
test 2	b#	3	2.22~3.42	74~113	0.15~0.42	0.08-1.33

151

Note: 1. Momentum flux ratio $J = \rho_f v_j^2 / \rho_{in} v_{in}^2$, where ρ_f and ρ_{in} is the density of fuel and air flow, kg/m³. v_j is the fuel velocity at the burner outlet, m/s. According to the criterion identifying the flame configuration modes of jet in cross flow by Huang (1994), the flame behaviors for test 1 and test 2 are affiliated with down-wash and cross-flow dominated mode, respectively.

155

Table 3

156 Chemical composition of LPG used in the tests.

Fuel	Volume fraction	Fuel	Volume fraction	Fuel	Volume fraction	Fuel	Volume fraction
CH ₄	2.88%	C ₃ H ₆	0.01%	C ₄ H ₈	0.38%	C ₅ H ₁₂	0.67%
C ₂ H ₆	0.06%	C ₃ H ₈	1.44%	C ₄ H ₁₀	94.55%	C ₆ H ₁₄	0.01%

157 3. Results and discussion

158 3.1 Description of the flame shape

159 By use of a SONY camera (RX100), the visible flame videos are recorded and the visible flame
160 shapes are distinguished using MATLAB software. And the mean flame shape (flame occurrence
161 probability equals to 0.5 (Zukoski, Cetegen, & Kubota, 1985)), is introduced to describe the
162 boundary of the visible flame to ignore the effect of the flame pulsation. Fig.3(a) and Fig.3(b) shows
163 the sketches of the typical visible flames for test 1 and test 2. Some differences can be observed. In
164 test 2, a region nearest to the fire source burns a blue flame and is almost invisible on the video
165 records. By contrast, the blue flame zone of test 1 is negligible and the luminous yellow flame almost
166 starts from the burner outlet. The reason may be due to different combustion efficiency and soot
167 formation. Because of inadequate air supply and finer honeycomb aperture, for some experimental
168 cases in test 1, large amounts of soot productions are observed in the experiments, as shown in
169 Fig.3(a). Mudan (1987) and Johnson et al. (1994) have proved that thermal radiation from the blue
170 flame region is small compared with that from the luminous yellow flame region. Therefore, the
171 blue flame zone is not included in the flame shape model. Furthermore, as the upward velocity close
172 to the fire source has relatively weak buoyancy compared to the longitudinal airflow, the visible
173 flame is pushed and dragged towards the downwind direction.

174 To describe the visible flame shape, the tilted cylinder (Mudan, 1987; Hankinson, &
175 Lowesmith, 2012; Palacios, Muñoz, Darbra, & Casal, 2012) and frustum of a cone (Kalghatgi, 1983;
176 Johnson, Brightwell, & Carsley, 1994) models were once used to successfully predict the radiant
177 heat flux. Apparently, these two geometries are not appropriate for the test 1 and test 2. A ‘back-to-
178 back conical frustum’ model is introduced in this paper to describe the visible flame shape, as shown
179 in Fig.3(c). It can be described by one angle (α_f) and six lengths ($H_f, H_{f1}, D_1, D_2, D_{max}, s$). α_f is the
180 angle between the axis of the conical frustum and the flame axis. D_1 and D_2 are the diameters of the
181 conical frustum, and D_{max} is the maximum diameter of the flame. H_{f1} and H_f are the heights of the
182 lower conical frustum and the entire back-to-back conical frustum, respectively. s is the offset
183 distance deviating from the fire source. As mentioned above, due to the occlusion of the tunnel floor,
184 the lower right corner (the part underneath the ground indicated by dotted lines) is eliminated from
185 the ‘back-to-back conical frustum’ model.

186 As exhibited in Fig.3(d) and Fig.3(e), this newly proposed ‘back-to-back conical frustum’
187 agrees well with the visible flame envelopes for buoyant jet diffusion flame (Wang, Fang, Lin, Guan,
188 & Wang, 2017) as well as for pool fire flame (Tang, Li, Zhu, Qiu, & Tao, 2015).

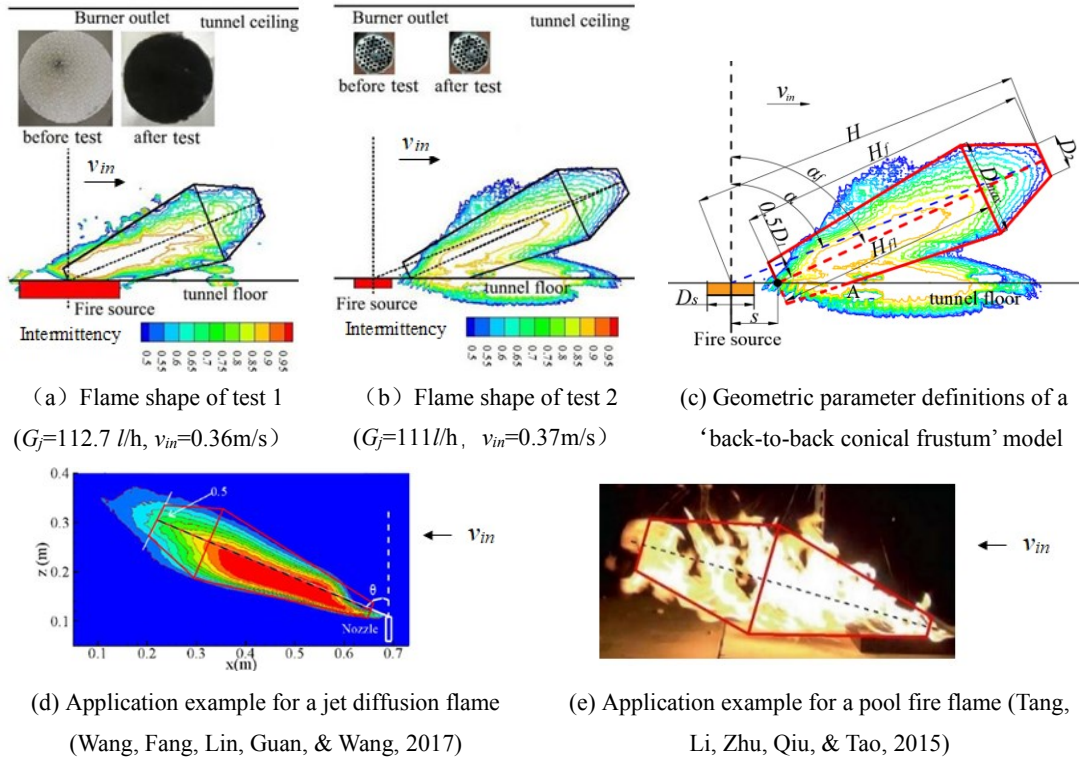


Fig.3. Visible flame shapes of typical experimental cases, the geometric parameter definitions and application examples for a jet diffusion flame, a pool fire flame (elevation view).

189 3.2 Data processing method

190 Essentially, this kind of flame observed in the reduced-scale tunnel fire experiment is somewhat
 191 similar to the combusting gas jets issuing from the stack under a cross flow. Huang and Chang (1994)
 192 conducted experiments to study refinery flare stacks during emergency blow-offs in a chemical plant.
 193 The flame behavior and coherent structure of the combusting propane gas jet in a cross flow were
 194 analyzed. They employed the momentum flux ratio, defined by $J=\rho_j v_j^2/\rho_{in} v_{in}^2$, to identify different
 195 characteristic modes of flame configurations in the stability domain. Inspired by this data processing
 196 method, this paper firstly introduces and uses the momentum flux ratio J in tunnel fire parameter
 197 analysis. The following analysis examines the coupling effect of the longitudinal air velocity and
 198 the fuel flow rate on geometric parameters of the visible flame shape and radiative fraction.

199 3.3 Geometric parameters of the visible flame

200 (1) Flame diameter and flame trailing

201 As seen in Fig.4(a), the flame diameters are non-uniform along the flame axis for two tests,
 202 D_{max} is the much larger than D_1 and D_2 . In comparison with fire source diameter (D_s), the clear
 203 expansion of flame diameter for test 2 is observed, D_{max}/D_s is about 2.5-4. For this reason, the 'back-
 204 to-back conical frustum' model is more suitable than the tilted cylinder model and the frustum of a
 205 cone model. The locations of maximum flame diameters are lower than $4/5H_f$, and decrease with
 206 the increasing J , as exhibited in Fig.4(b).

207 The phenomenon of flame trailing is evidently observed in the tests, which is common for
 208 liquid pool fires. As the density of butane gas (volume fraction >94% as shown in Table 3) is higher
 209 than that of air, it tends to remain at ground level, until it has been heated sufficiently to decrease its
 210 density below air density. Therefore, under the influence of longitudinal air flow, the visible flame

211 is pushed and dragged towards the downwind direction. In this paper, the offset distance of the flame
 212 axis is used to characterize the flame trailing effect. As shown in Fig.4(c), the dimensionless offset
 213 distance (s/D_s) for test 2 is larger than that of test 1. For test 2, s/D is in the range of 0.5~1.6 and
 214 decreases with the increasing J . The horizontal offset effect of the flame axis is more evident for the
 215 experimental cases with a higher fuel flow rate.

216 (2) Length and tilt angle of flame axis

217 For the flame length (H), Majeski et al. (2004) suggested a simple linear correlation between
 218 the composite variable $H/(v_{in}\sqrt{c_f})$ and $\sqrt{\rho_j v_j} D_s / v_{in}$. Where c_f is the dilution of the fuel, for
 219 example $c_f=1$ for undiluted propane fuel.

220 As seen in Fig.4(d), the length of flame axis, H_f , also shows the similar linear correlation as
 221 following:

$$\frac{H_f}{v_{in}} = 12.37 \sqrt{\rho_j v_j} \frac{D_s}{v_{in}} + 0.115 \quad (6)$$

222 The slope of equation (6) is smaller than those proposed by other experimental results. The
 223 difference may be due to the following reasons. Firstly, the values of H_f are smaller than H , as shown
 224 in Fig.3(c). Secondly, the criterion to determine the flame tip is different from each other. The flame
 225 tip is defined at 10% and 50% contours of flame occurrence probability by Majeski et al. (2004) and
 226 Lin (2015), respectively. The same criterion as Lin's (flame occurrence probability equals to 0.5) is
 227 used in this paper. The flame length defined by 10% contour of flame occurrence probability is
 228 larger than that by 50% contour of flame occurrence probability. So the slope of the Majeski's
 229 correlation is much larger. And the flame lengths by Pipkin and Sliepcevich (1964) are obtained by
 230 pure eye observation. The values are between Majeski's correlation and equation (6), as exhibited
 231 in Fig.4(d).

232 As seen in Fig.4(e), the tilt angles of flame axis show a decrease trend with the increasing J . The
 233 maximum α_f is no larger than 60 degrees for test 1 and test 2 cases. For test 2, the values of α_f are
 234 slightly less than Pipkin and Sliepcevich (1964)'s data and the correlation developed by Wang et al.
 235 (2017). It should be noted that Pipkin and Sliepcevich' data are based on the flame tilt angle (α),
 236 which is slightly larger than α_f , as shown in Fig.3(c). It can be easily imaged that the variation trend
 237 of α_f with J for test 2 is in good agreement with the Pipkin and Wang's experimental results.

238 As shown in Fig.4(e), there is large discrepancy between Wang's correlation and α_f values from
 239 test 1. The reason may be due to different jet outlet locations. In Wang's experiment, the tip of the
 240 nozzle is approximately 0.50 m above the floor of the tunnel, while the porous burner used in this
 241 paper is placed align with the tunnel floor. At low jet-to-wind momentum flux ratios as seen in
 242 Fig.3(d), the effects of entrainment and mixing of the fuel and air in the near wake region can no
 243 longer be ignored. Hence, flammable conditions can be established in both the near wake regions
 244 behind the nozzle and deflected jet. For this reason, the flame deflects through a large angle from
 245 the vertical axis of the nozzle. For test 1, the effect of mixing and combustion in the near wake
 246 regions behind the burner does not exist due to the obstruction of tunnel floor. And the values of α_f
 247 lower than that of Wang's correlation is reasonable.

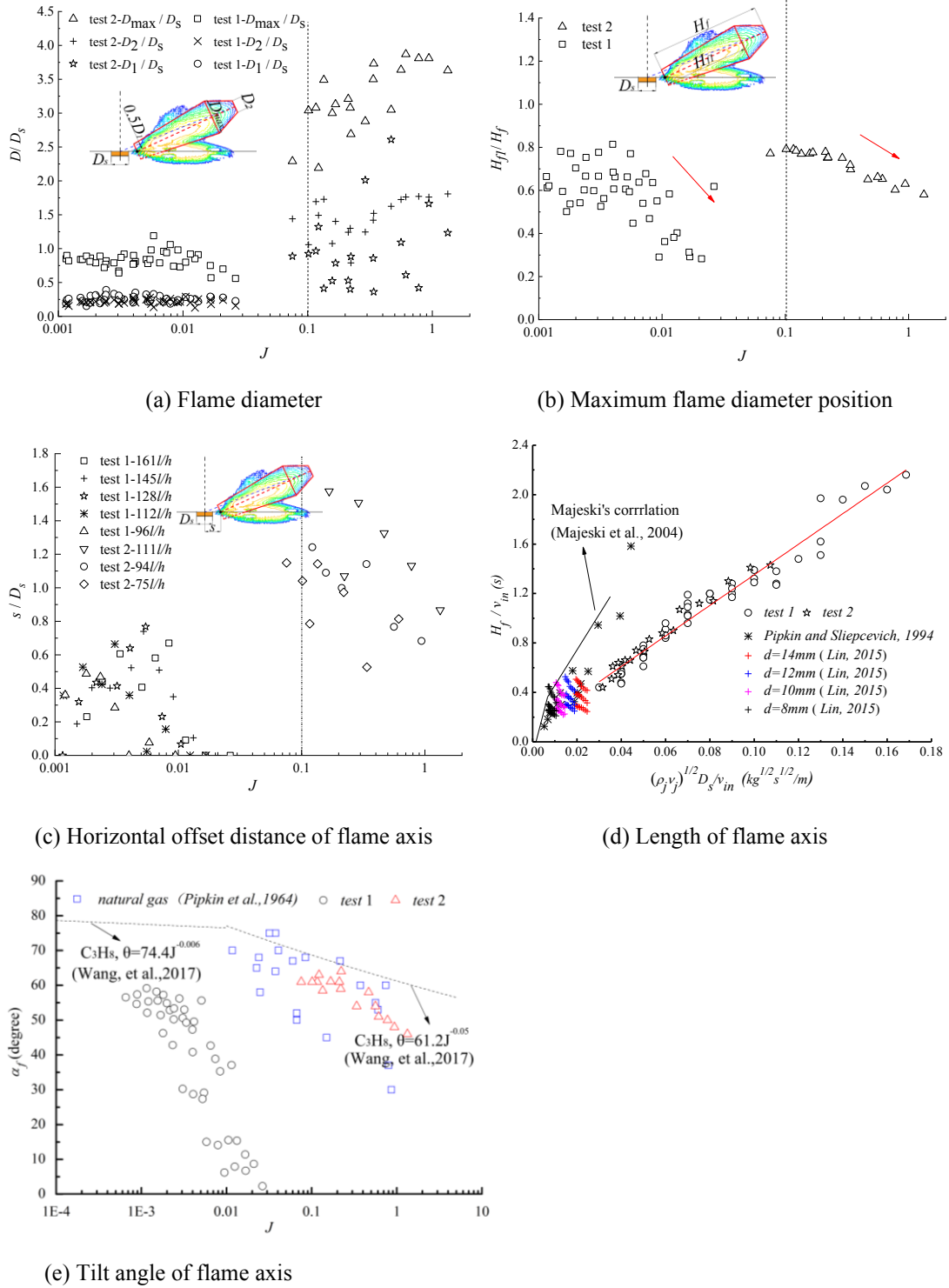


Fig.4 Geometric parameters of the visible flames for test 1 and test 2

248 3.4 Experimental verification of radiation model

249 For test 1, the radiant heat flux at 1# on the ground ($q_{m,1\#}$) is measured, and its value is assumed
 250 to be equal to the predicted value ($q_{p,1\#}$) based on the ‘back-to-back conical frustum’ model.
 251 According to equation (3), the radiant heat flux at 2# ($q_{p,2\#}$) can be predicted as below:

$$q_{p,2\#} = q_{m,1\#} \frac{F_{2\#-A_f}}{F_{1\#-A_f}} \quad (7)$$

252 The geometric view factors from 1# and 2# to the flame can be calculated according to the method
 253 by Guo (2019). The calculation details will not be included in this paper.

254 Similarly, the measured radiant heat flux values at 2#, 3#, 4# are used as the reference. And the
 255 radiant heat flux values at other measuring points can be calculated and compared with the measured
 256 results, as shown in Fig.5. Apparently, the theoretical predictions of $q_{p,1\#}$, $q_{p,2\#}$, $q_{p,3\#}$, $q_{p,4\#}$ based on
 257 the ‘back-to-back conical frustum’ model agree well with the measurements. Most predicted heat
 258 fluxes are distributed within $\pm 20\%$ of the measured values. No predicted values are out of the range
 259 of 50%~150%. The above results show that the radiation model based on the ‘back-to-back conical
 260 frustum’ is accurate and can be used to predict the radiant heat flux and X_r .

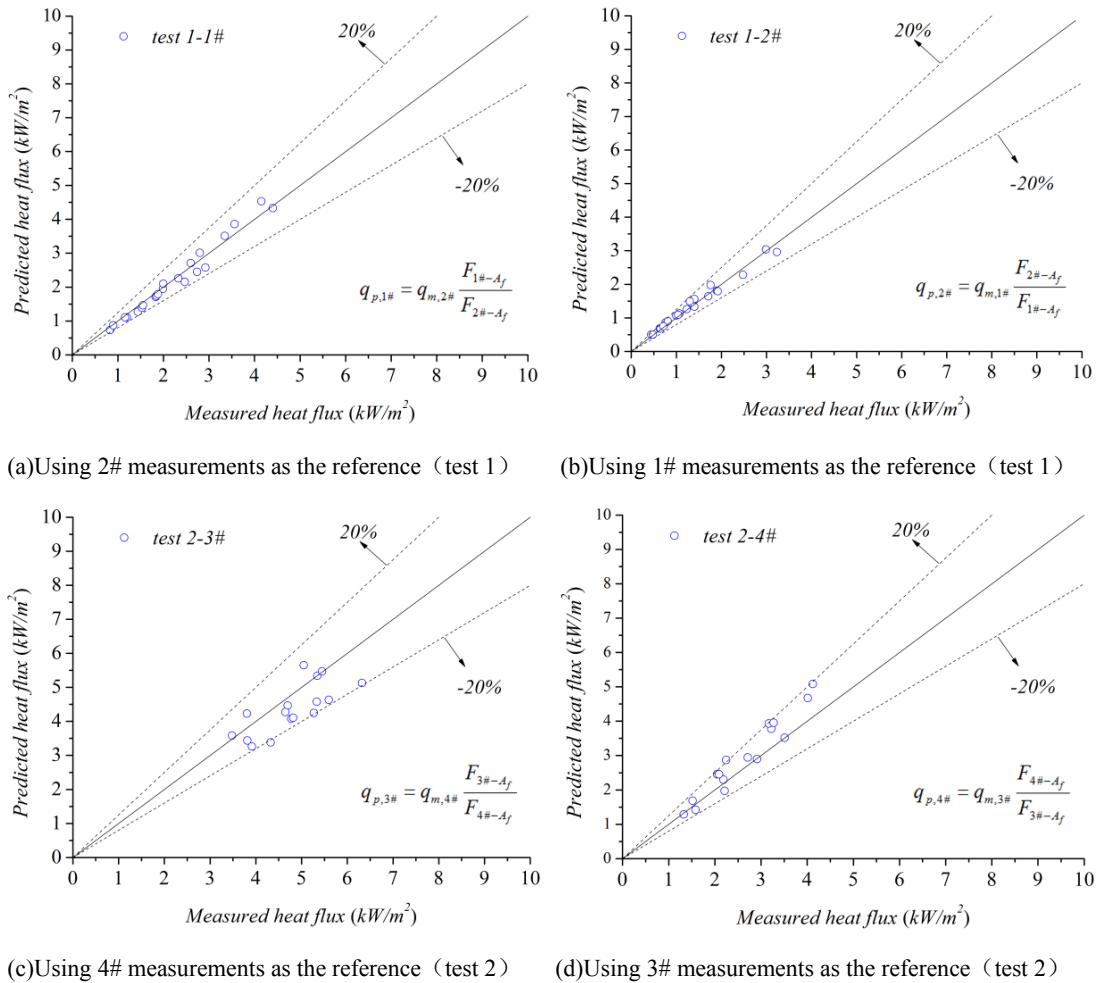


Fig.5 Comparison of measured and calculated radiative heat flux of the measuring points. Note: the solid lines indicate equality of measured and predicted values.

261 3.5 Radiative fraction of flame

262 According to equation (5), the flame radiative fraction can be calculated and the values are
 263 shown in Fig.6 and Fig.7(a). Most of the experimental cases in test 1 and test 2 have two heat flux
 264 meters. For each measurement point, a radiative fraction is calculated. Their average value is taken
 265 as the final flame radiative fraction. For a small number of experimental cases of test 1, only one
 266 radiant heat flux (2#) is measured. Under this circumstance, the flame radiative fraction is calculated
 267 only based on 2# data. The error bar is also shown in Fig.6. It is observed that the calculated X_r
 268 based on different measurement points are consistent, which proves that the calculation method of

269 radiation fraction is reliable and robust.

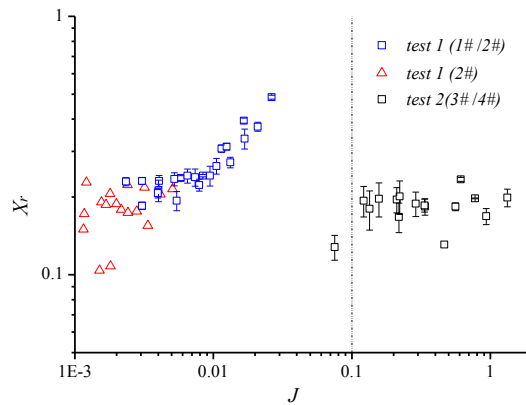


Fig.6 Relationship between radiative fraction and momentum flux ratio

270 3.6 Impact of X_r on tunnel ventilation and smoke extraction system

271 As exhibited in Fig.7(a), for the same fuel flow rate, the flame radiative fraction decreases with
 272 the increase of longitudinal air velocity. When the longitudinal air velocity increases in the same
 273 range, the value difference of X_r for the larger fuel flow rate is much higher than that of the smaller
 274 fuel flow rate.

275 Taking experimental cases ($G_f=1611/h$) as an example, as the air velocity increases from 0.1m/s
 276 to 0.36m/s, the values of X_r decrease from 0.45 to 0.1. According to equation (1), the convective
 277 heat rate of fire will increase from $0.55Q$ to $0.9Q$. This means that some key parameters of tunnel
 278 ventilation and smoke extraction system will increase simultaneously, as shown in Table 4.

279 **Table 4**

280 Variations of some key parameters of tunnel smoke exhaust system with the changes of X_r .

Key parameters	Empirical formula ¹	Parameter variation ²	Reference
Fire plume mass flow rate m_{plume} (kg/s)	$m_{plume} = 0.071 \frac{Q_c^{1/3}}{z^{5/3}}$ $v' \leq 0.19$	$m_{plume,2}/m_{plume,1} = 1.178$ $m_{plume,3}/m_{plume,1} = 1.083$ $m_{plume,3}/m_{plume,2} = 0.92$	Ingason et al. (2015)
Maximum excess gas temperature beneath tunnel ceiling ΔT_{max} (K)	$\Delta T_{max} = 14.1 C_T \frac{Q_c^{2/3}}{H_{ef}^{5/3}}$ $v' \leq 0.19$	$\Delta T_{max,2}/\Delta T_{max,1} = 1.389$ $\Delta T_{max,3}/\Delta T_{max,1} = 1.175$ $\Delta T_{max,3}/\Delta T_{max,2} = 0.846$	Ingason et al. (2015)
Critical velocity of longitudinal ventilation v_{cri} (m/s)	$\frac{v_{cri}}{\sqrt{gD_e}} = 0.4 \left(\frac{Q_c^*}{0.2} \right)^{1/3}$ $Q_c^* \leq 0.2$	$v_{cri,2}/v_{cri,1} = 1.178$ $v_{cri,3}/v_{cri,1} = 1.083$ $v_{cri,3}/v_{cri,2} = 0.92$	Wu et al. (2000)

281 Note: 1. $Q_c=(1-X_r)Q$, assuming a constant total heat release rate Q .

282 2. The subscript '1', '2' and '3' correspond to the $X_r=0.45$, $X_r=0.1$ and $X_r=0.3$ case, respectively.

283 As mentioned above, the values of X_r in the former references are usually assumed to be
 284 0.2~0.4, with a mean value of 0.3. Based on this value, the key parameters listed in Table 4 will
 285 underestimate by 8%-15.4% for the $X_r=0.1$ case, or overestimate by 8.3%-17.5% for the $X_r=0.45$
 286 case.

287 Moreover, as exhibited in Fig. 7 (a), the influence of the fuel flow rate on the radiative fraction
 288 is presented in two ways: when $v_{in}>0.22m/s$, the radiative fraction is independent with the fuel flow
 289 rate; when $v_{in}<0.12m/s$, the radiation fraction increases significantly with the increase of the fuel

290 flow rate. The potential cause of the higher X_r is the lower combustion efficiency.

291 According to the data by Johnson and Kostiuik (2000), the combustion efficiency of the flame
 292 in the above analysis is assumed to be 100%. In fact, the combustion efficiency may also be affected
 293 by the longitudinal air velocity and fuel flow rate. Some typical experimental cases for test 1 are
 294 chosen, and the total heat release rates of fire (Q) are measured according to the method of oxygen
 295 consumption calorimetry (Ingason, Li, & Lönnemark, 2015). In combination with the flow rate and
 296 combustion heat of fuel, the combustion efficiency of the flame is calculated further and shown in
 297 Fig.7(b). It should be noted that the sampling method of combustion gases used in this paper may
 298 lower the mean O_2 , CO , CO_2 concentrations, due to the natural stratification in the direction of
 299 tunnel height at the 1-1 section. For this reason, the total heat release rate (Q) and combustion
 300 efficiency (η) are also underpredicted. But the difference of combustion efficiency with longitudinal
 301 air velocity cannot be ignored. And the variation trend of η with the increasing air velocity is
 302 opposite to X_r . This means that for the cases of low longitudinal air velocity, X_r may become larger.

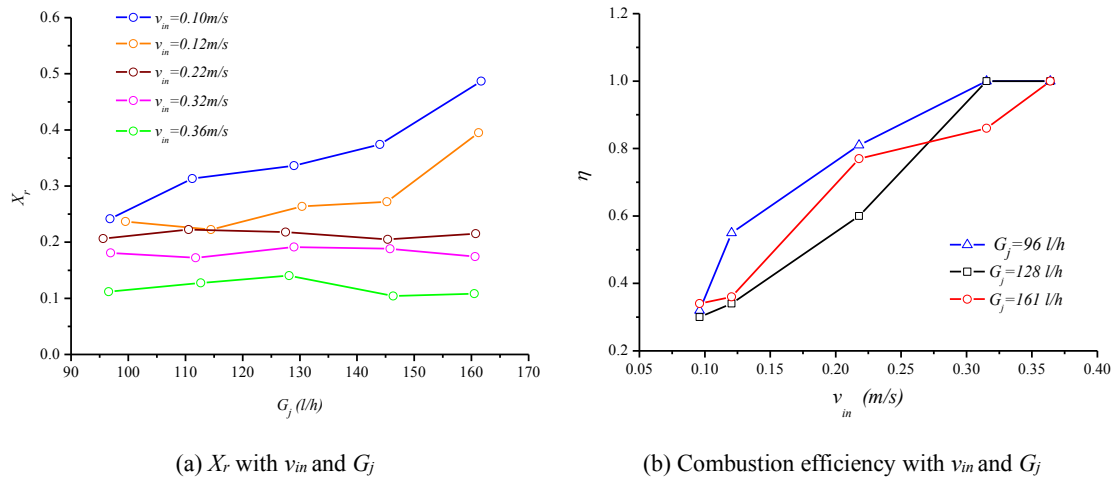


Fig.7 Radiative fraction and combustion efficiency against longitudinal air velocity and fuel flow rate of typical experimental cases (test 1)

303 3.7 Correlation of flame radiative fraction with composite variable

304 As exhibited in Fig.6, with the change of J , the values of X_r for test 1 are between 0.15 and 0.5,
 305 showing a positive correlation. For test 2, the values of X_r are between 0.15 and 0.25, the increase
 306 trend is not evident because of the high combustion efficiency and low soot formation.

307 To support engineering design, a regression equation is derived using our measurement data.
 308 Using equation (8) as follows, engineers can quickly estimate X_r values under different mass flow
 309 rate and ventilation velocity scenarios for ventilation and evacuation systems design.

$$\frac{X_r^{16} m_j^4}{v_{in}^{11}} = 14.497 \left(\frac{\sqrt{m_j}}{v_{in}} \right)^2 - 0.7196 \frac{\sqrt{m_j}}{v_{in}} + 0.0169 \quad (8)$$

$$R^2=0.93$$

310 Where m_j is the mass flow rate of fuel, kg/s; v_{in} is the longitudinal air velocity, m/s. As shown in
 311 Fig.8, the above regression equation agrees well with the data by Brzustowski et al. (1975) and Lin
 312 (2015).

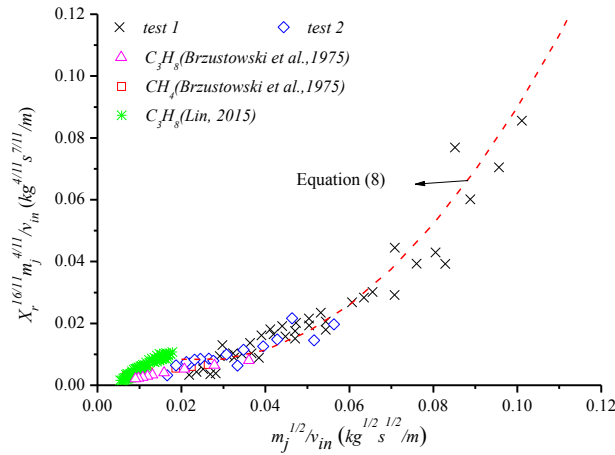


Fig.8 The regression equation of X_r , v_{in} and m_j .

313 4. Conclusions

314 In this paper, two sets of tunnel fire tests are conducted in a 1/20 reduced scale model tunnel. The
 315 flame videos are recorded and the incident radiative flux on tunnel floor are measured. Hereby, a
 316 theoretical model is proposed to predict the radiative fraction of tunnel fire. The main conclusions
 317 are:

318 (1) This paper introduces a novel ‘back-to-back conical frustum’ model to describe the visible
 319 flame shape of porous burner. In comparison with the experimental results, the radiation model
 320 using the proposed flame shape shows an 80% accuracy. It is used to predict the radiant heat flux of
 321 measuring points and to calculate the value of X_r .

322 (2) The momentum flux ratio J is used in this paper to examine the coupling effect of the
 323 longitudinal air velocity and the fuel flow rate. This data processing method has never been used in
 324 tunnel fire parameter analysis before in literature.

325 (3) The flame radiative fraction decreases with the increasing longitudinal air velocity. When
 326 v_{in} increased in the same range, the value difference of X_r for the larger fuel flow rate is much larger
 327 than that of the smaller fuel flow rate.

328 (4) For the cases of $G_j=161$ l/h, with the air velocity increasing from 0.1m/s to 0.36m/s, the
 329 values of X_r decrease from 0.45 to 0.1. Correspondingly, the fire plume mass flow rate, maximum
 330 excess gas temperature beneath tunnel ceiling and the critical velocity of longitudinal ventilation
 331 would increase by 17.8%, 38.9% and 17.8%, respectively.

332 (5) Large departure of X_r from the usually assumed constant value influenced the reliability of
 333 smoke extraction system. The key parameters listed in Table 4 are underpredicted for the case of X_r
 334 $=0.1$ by 8%-15.4%, or overpredicted for the case of $X_r=0.45$ by 8.3%-17.5%.

335 (6) The influence of the fuel flow rate on the radiative fraction is presented in two ways: when
 336 $v_{in}>0.22$ m/s, the radiative fraction is independent with the fuel flow rate; when $v_{in}<0.12$ m/s, the
 337 radiation fraction increases significantly with the increase of the fuel flow rate.

338 (7) A regression model is derived to support ventilation and evacuation systems design. Engineers
 339 can quickly estimate X_r values by considering the coupling impact of different mass flow rates and
 340 ventilation velocities.

341

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