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Neutron-unbound excited states of ²³N

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Neutron unbound states in ²³N were populated via proton knockout from an 83.4 MeV/nucleon ²⁴O beam on a liquid deuterium target. The two-body decay energy displays two peaks at $E_1 \sim 100 \text{ keV}$ and $E_2 \sim 1 \text{ MeV}$ with respect to the neutron separation energy. The data are consistent with shell model calculations predicting resonances at excitation energies of ~3.6 MeV and ~4.5 MeV. The selectivity of the reaction implies that these states correspond to the first and second 3/2⁻ states. The energy of the first state is about 1.3 MeV lower than the first excited 2⁺ in ²⁴O. This decrease is largely due to coupling with the $\pi p_{3/2}^{-1}$ hole along with a small reduction of the N = 16 shell gap in ²³N.

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I. INTRODUCTION

Spectroscopy of nuclei with extreme N/Z ratios can provide valuable insight into nuclear structure. Due to shifts in the single particle energies of exotic nuclei, classical shell closures can disappear while new shell gaps appear [1,2]. A well-known example of this is the "island of inversion," located around $A \sim 32$, where a quenching of the N = 20 shell gap results in nuclei with ground states occupying the *pf* shell instead of the *sd* shell [3]. In the oxygen isotopes, there is substantial evidence for the breakdown of the N = 20 shell gap, and the appearance of N = 16 as a magic number [4–7]. This shift has been attributed to the tensor component of the *NN* interaction [8,9] as well as three-body forces [10].

As one moves down the N = 16 isotones, the removal of protons from the $\pi 0d_{5/2}$ orbital enables the $\nu 0d_{3/2}$ orbital to move higher in excitation resulting in a large energy difference between the $\nu 1s_{1/2}$ and $\nu 0d_{3/2}$ orbits in oxygen [2]. At present, there are no reports of bound- or unbound-excited states in the lighter isotones ²³N and ²²C. The measurement of these excited states can provide a better understanding of the changing shell structure in this region of the nuclear chart by extending our knowledge of the N = 16 gap into the proton p shell. In this article, we present first experimental information on neutronunbound excited states in ²³N populated via proton-knockout from ²⁴O.

II. EXPERIMENTAL METHOD

The experiment was carried out at the National Superconducting Cyclotron Laboratory (NSCL) where a 140 MeV/nucleon ⁴⁸Ca beam impinged upon a ⁹Be target with a thickness of 1363 mg/cm² to produce an ²⁴O beam at 83.4 MeV/nucleon. The A1900 fragment separator was used to select ²⁴O from the other fragmentation products, and the remaining beam contaminants were removed by time-of-flight in the off-line analysis. The ²⁴O beam proceeded to the experimental area where it impinged on the Ursinus College Liquid Hydrogen Target, filled with liquid deuterium (LD₂). Based on the design of Ryuto *et al.* [11], the LD₂ target is cylindrical with a diameter of 38 mm, a length of 30 mm, and is sealed with 125 μ m-thick Kapton foils on each side.

A one-proton removal reaction from the ²⁴O beam created ²³N in an excited state above the neutron separation energy S_n , which promptly decayed to ²²N. The resulting charged fragments were then swept 43.3° by a 4-Tm superconducting sweeper magnet [12] into a collection of position- and energy-sensitive charged-particle detectors.

Element identification was achieved via a ΔE vs. time-offlight measurement, and isotope identification was obtained through correlations in the time-of-flight, dispersive position, and dispersive angle following the sweeper magnet. Additional information on this procedure can be found in Ref. [13]. The position and momentum of the charged fragments at the target were reconstructed using an inverse transformation matrix, obtained from the program COSY INFINITY [14,15].

The neutrons emitted in the decay of ²³N traveled undisturbed by the magnetic field towards the Modular Neutron Array (MoNA) [16] and the Large-area multi-Institutional

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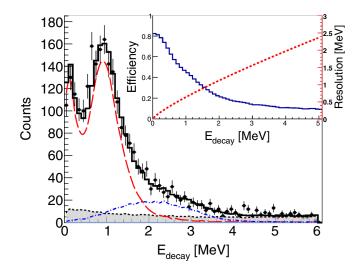


FIG. 1. Two-body decay energy for $^{22}N + 1n$. The best fit includes two-channel Breit-Wigners resulting from two states at 1.1 MeV (dashed-red line) and 2.4 MeV(dot-dashed-blue line). Background contributions are in shaded gray. The efficiency and resolution are shown in the inset as the blue histogram (left scale) and red-dashed line (right scale), respectively.

Scintillator Array (LISA). MoNA and LISA each consist of 144 bars of plastic scintillator with photomultiplier tubes on both ends and provide a measurement of neutron time-of-flight and position. Additional details on the experimental setup can be found in Refs. [17,18]. MoNA, LISA, and the sweeper provide a full kinematic measurement of the neutrons and charged particles emitted in the decay of ²³N.

III. ANALYSIS

The two-body decay energy is defined as

$$E_{\rm decay} = M^* - M_{^{22}\rm N} - m_n$$

where M^* is the invariant mass of the decaying system, $M_{^{22}N}$ the mass of ^{22}N , and m_n the neutron mass. The decay energy, E_{decay} , corresponds to the excitation energy in ^{23}N above the neutron emission threshold. The invariant mass of the twobody system is obtained from the experimentally measured four-momenta of ^{22}N and the first time-ordered interaction in MoNA-LISA. To remove interactions from background γ rays, a time-of-flight gate on prompt neutrons in coincidence with ^{22}N fragments was applied. The observed two-body decay energy for ^{23}N is shown in Fig. 1, and displays two prominent peaks at $E_1 \sim 100$ keV and $E_2 \sim 1$ MeV. The efficiency and resolution of MoNA-LISA for the present setup are shown as a function of the decay energy in the inset.

A Monte Carlo simulation was used to model the decay of ²³N. The simulation includes the beam characteristics, the reaction mechanism, and subsequent decay. The efficiency, resolution, and acceptance of the charged particle detectors, along with the response of MoNA-LISA, are fully incorporated into the simulation. Therefore the results of the simulation are directly comparable to the experimental spectra. The neutron interactions in MoNA-LISA were modeled with GEANT4 [19] and MENATE_R [20]. A modification was made to the ¹²C(n,np)¹¹B inelastic cross section within MENATE_R to better agree with previous measurement [21] at $T_n =$ 90 MeV. No qualitative change was observed in the shape of the simulated one-neutron decay energy spectrum when the inelastic cross sections for neutrons on carbon were increased or decreased by an order of magnitude in MENATE_R.

The input decay energy line shape was an energy dependent Breit-Wigner of the form

$$\sigma_l(E) \sim \frac{\Gamma_l}{(E_0 - E)^2 + \frac{1}{4} (\Gamma_l^2)}$$

where E_0 is the position of the peak and Γ_l the energydependent width. Given that ²²N has two bound excited states [22], it is possible for the neutron decay to branch to multiple final states. To model this, the two-channel form of the Breit-Wigner was used with a common normalization:

$$\sigma_{\text{tot}}(E) \sim \sigma_1(E; E_1) + \sigma_2(E; E_2),$$

where E_i is the energy of each branch, and the width in the numerator Γ_l becomes the partial-width Γ_i . The total widths Γ_i^T replace the width in the denominator and are given by the expressions

$$\Gamma_1^T = \Gamma_1(E) + \Gamma_2(E - E_{12}), \Gamma_2^T = \Gamma_1(E + E_{12}) + \Gamma_2(E),$$

where $E_{12} = E_1 - E_2$ is the energy difference between the channels, with E_1 denoting the higher-energy channel. For simplicity, the shift functions have been neglected.

While it is possible for higher-lying states to be present at $E_{decay} > 3$ MeV, they are not resolved in the data and treated as background. Nonresonant contributions were modeled with a Gaussian decay distribution with a central energy of $E_{decay} = 10$ MeV and a width of $\sigma = 5$ MeV. This choice of line-shape reproduces the relative velocity between the fragment and neutron well and has been used to describe nonresonant contributions in the decay of ²⁴O, populated by knockout from ²⁶F [4].

The measured decay energy can be related to the excitation energy of ²³N by $E^* = E_{decay} + S_n$, where S_n was calculated using the mass excesses from Gaudefroy *et al.* [23]. Their values of $\Delta M_{23N} = 36.72(0.28)$ MeV and $\Delta M_{22N} =$ 31.11(0.26) MeV result in a one neutron separation energy of $S_n = 2.46(0.38)$ MeV. This separation energy is about 700 keV higher than what is obtained using the masses in the 2012 AME [24]. The two-neutron separation energy is $S_{2n} = 4.67(0.30)$ MeV.

Using the mass excesses measured by Gaudefroy *et al.* [23], theoretical predictions for the excited states of ²³N are shown in Fig. 2 with various interactions based on Ref. [25] including the WBP, WBT, WBTM, and WBM Hamiltonians in addition to the continuum shell model (CSM) [26]. The WBTM and WBM interactions contain a 12.5% and 25% reduction of the neutron-neutron interaction strength in the *sd* space. In the lighter nitrogen isotopes, a 12.5% reduction was necessary to reproduce the low-lying levels [22,27], while a 25% reduction was needed for the heavier carbon nuclei [22]. Proton excitations were limited to the *p* shell, while neutron

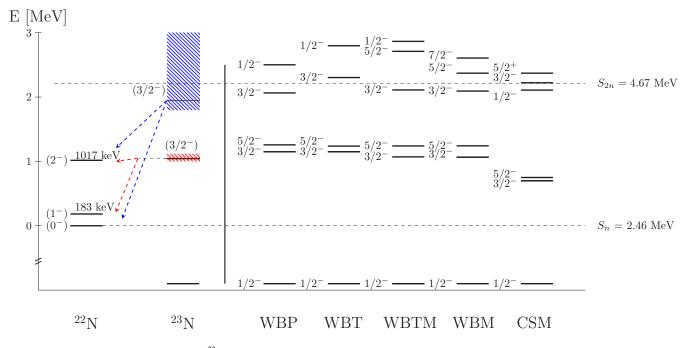


FIG. 2. A possible level ordering in ²³N consistent with the observed spectrum. The arrows indicate transitions from the first- and second-excited $3/2^-$ state in ²³N to various states in ²²N. The hatched areas indicate the experimental uncertainty given the assumptions discussed in the text. The colors correspond to the fit in Fig. 1. The branching from the $3/2^-$ states to the various excited states of ²²N cannot be resolved without γ detection. Shell model calculations for ²³N are shown for comparison on the right.

excitations were restricted to the *sd* shell. These calculations predict several excited states with spin-parity $1/2^-$, $3/2^-$, and $5/2^-$ in the vicinity of 3–5 MeV. Due to the selective nature of the proton removal reaction, it is not likely to populate a $5/2^-$ state in ²³N from ²⁴O. A $5/2^-$ state in ²³N can be made by coupling of the $p_{1/2}$ proton hole to the 2⁺ state of the ²⁴O core, or by coupling of a $p_{3/2}$ proton hole to the 2⁺ or 1⁺ state in the ²⁴O core. The ground state of ²⁴O has very little to no overlap with these configurations in ²³N.

The spectroscopic overlaps C^2S between ²³N and ²⁴O were calculated using the WBP and WBT Hamiltonians in NUSHELLX [28] and are summarized in Table I. The largest overlap is with the ground state of ²³N, which is bound and was not within the acceptance of the sweeper magnet in this

TABLE I. Spectroscopic overlaps between various J^{π} in ²³N and the ground state of ²⁴O, calculated using the WBP and WBT interactions [25].

J^{π}	WBP		WBT	
	$E_{\rm calc}$ (MeV)	$\langle {}^{23}N ^{24}O angle \ C^2S$	$E_{\rm calc}$ (MeV)	$\langle {}^{23}N ^{24}O angle \ C^2S$
$1/2_1^-$	0	1.9328	0	1.9529
$1/2_2^-$	4.961	0.0025	5.257	0
$\sum C^2 S$		1.9578		1.9529
$3/2_1^-$	3.610	1.4645	3.610	0.6893
$3/2^{-}_{2}$	4.525	0.6480	4.764	1.0483
$3/2_{3}^{-}$	5.215	0.1682	5.471	0.0944
$3/2_4^{-}$	6.989	1.4324	6.693	1.8889
$\sum C^2 S$		3.7130		3.7209

experiment. The next strongest overlaps are for the $3/2^-$ states where the single-particle strength is fragmented. Given that the overlap for the first $1/2^-$ excited state is very small, the most likely candidate for the spin-parity of the observed state(s) is $3/2^-$.

It is important to note that ²²N has two bound excited states, one at 183 keV, and another at 1017 keV [22]. Although the spin-parities of these states are unknown, the tentative assignments of the ground, first, and second excited states are 0^- , 1^- , and 2^- , respectively. Thus, the observed peaks in the two-body decay energy could correspond to transitions to the 2^- excited state of ²²N instead of the ground state or the first excited 1^- state. Although there are neutron-unbound states in ²²N that ²³N could decay to, the selection of ²²N in the sweeper eliminates any contributions from these branches in the two-body spectrum of ²³N.

As it is not possible to discern between any number of degeneracies or level orderings that could produce the observed spectrum without measuring the emitted γ rays, one has to rely on theoretical calculations. For this reason, the data are interpreted and fit within the context of the shell-model predictions.

Of the interactions considered here, none predict a state near threshold (see Fig. 2). The lowest $3/2^-$ state is predicted to be at approximately 1 MeV above S_n , with the second $3/2^$ being about an MeV higher. The 100 keV peak then does not correspond to a decay to the ground state but rather a transition to the 2^- state in ²²N, while the $E_2 \sim 1$ MeV peak is comprised of transitions to both the first-excited and ground state of ²²N. While there are three possible final states, the splitting between the ground and first-excited state cannot be resolved due to the experimental resolution for decay energies above 1 MeV. For this reason, the 0⁻ and 1⁻ states are treated as a single state at their average energy. Since the spacing between the two $3/2^-$ states is expected to be about an MeV, another state was assumed to be around ~2 MeV. In addition, because the final states in ²²N are only tentatively known, the ℓ values are chosen to be consistent with the interpretation.

The assumption of a second excited state is qualitatively supported by the data, as the high-energy tail cannot be described without excessive widths. In order to fit the spectrum with a single two-channel Breit-Wigner, it is necessary for the 1 MeV peak to have $\ell = 2$ and a width of $\Gamma \sim 1.5$ MeV. In this scenario, it is also necessary for the 100 keV branch to be $\ell = 0$ as the relative intensity of the peaks is driven by the partial widths. The cross section for $\ell = 2$ drops rapidly as E_{decay} approaches zero and the 100 keV peak cannot be $\ell = 2$ in the presence of another broad channel unless it has an even larger width.

The spectrum can also not be described with both channels being $\ell = 0$, because the widths are coupled and the penetrability for $\ell = 0$ is constant. Thus, if the 1 MeV channel is made excessively broad so too is the 100 keV branch and the fit fails to describe the data.

The single-particle decay width for the decay to the ground state is 200 keV for $\ell = 2$. Examining the spectroscopic factors in Table I, we note that the $3/2^-$ single-particle strength is fragmented indicating that these states are mixed in their neutron configurations. Thus one would expect widths less than the single-particle width, and so the solution with a single state is neglected due to the large necessary width. The data are fit with two-channel Breit-Wigners resulting from two $3/2^-$ states separated by approximately 1 MeV.

Since the branching ratios are not constrained without the knowledge of the γ -ray decays in ²²N, there are too many free parameters to uniquely describe the data. Therefore a set of narrow widths was chosen to reduce the parameter space. These widths are $\Gamma_i = 150 \text{ keV}$ for the low-energy branches of the two states ($\ell = 0$) and 400 keV ($\ell = 0$) and 300 keV ($\ell = 2$) for the high-energy branch of the first and second 3/2⁻ states, respectively.

The energies of the two $3/2^-$ are then minimized simultaneously after fixing the partial widths. In addition, the energy of each branch is required to be consistent during the minimization. The best-fit energies for the two $3/2^-$ states are $E_{\text{decay}} = 1070 \pm 100$ keV, and $E_{\text{decay}} = 2500^{+500}_{-700}$ keV. The errors in the fit parameters are approximate due to the fixed partial widths. They are purely statistical and are determined by the 1σ limit in the χ^2 minimization. Accounting for the separation energy places the first excited $3/2^-$ at $E_x = 3530 \pm 100$ (stat) ± 400 (sys) keV.

At present the uncertainties are too large to uniquely determine the contributions from the possible branchings two $3/2^-$ states would produce. In order to completely disentangle the spectrum, one would need to measure the emitted γ rays in a triple-coincidence measurement $(n + \gamma + {}^{22}N)$.

IV. DISCUSSION

The present measurement alone is not sufficient to fully determine the size of the N = 16 shell gap in ²³N. In ²⁴O

the N = 16 shell gap was calculated by taking the (2J + 1)weighted average of the 1⁺ and 2⁺ excited states, as they are composed of 1p-1h excitations above the ²⁴O ground state [4]. Similarly, the same can be done in ²³N, but one needs to take into account four states as the 2⁺ and 1⁺ configuration of neutrons, $(\nu 1s_{1/2})^1 \otimes (\nu 0d_{3/2})^1$, can couple with the unpaired $\pi 0p_{1/2}$ proton to give $(5/2^-, 3/2^-)$ and $(3/2^-, 1/2^-)$, respectively. The situation is further complicated by the fact that the 1p-1h neutron configuration in ²³N will mix with the $\pi 0p_{3/2}$ hole, lowering its energy.

In the WBP, WBT, WBTM, and WBM interactions, the lowest $3/2^-$ state in ²³N is indeed a mixture, with the occupation numbers giving a significant proton hole in the $\pi p_{1/2}$ and $\pi p_{3/2}$ orbitals, and a $(\nu 1s_{1/2})^1 \otimes (\nu 0d_{3/2})^1$ configuration of neutrons. One may write the wave function for the $3/2^-$ state as

$$\begin{split} {}^{23}\mathrm{N}\rangle_{3/2-} &= \alpha p_{3/2}^{-1} \otimes |^{24}\mathrm{O}\rangle_{\mathrm{g.s.}} \\ &+ \beta p_{1/2}^{-1} \otimes |^{24}\mathrm{O}\rangle_{2+} + \gamma p_{1/2}^{-1} \otimes |^{24}\mathrm{O}\rangle_{1+} \,, \end{split}$$

where α , β , and γ are coefficients constrained by the normalization $\alpha^2 + \beta^2 + \gamma^2 = 1$. According to the WBP calculation, the pure $\pi p_{3/2}^{-1}$ configuration comprises of roughly 37% of the total wave function ($\alpha \sim 1/\sqrt{3}$), with the remaining amplitude shared equally between the 2⁺ and 1⁺ configurations.

Thus the energy of the lowest $3/2^{-}$ state depends on both the N = 16 shell gap and the energy of the $\pi 0 p_{3/2}^{-1}$ hole, which is dictated by the spin-orbit splitting. The splitting between the $d_{3/2}$ - $s_{1/2}$ and $p_{1/2}$ - $p_{3/2}$ orbitals can be altered within NUSHELLX to study this dependence.

Let Δ denote the change in energy for either the $d_{3/2}$ or $p_{1/2}$ orbital for both protons and neutrons from their initial values in the WBP calculation, using the same model-space restrictions as before. Figure 3 shows the energy of the lowest $3/2^-$ state as

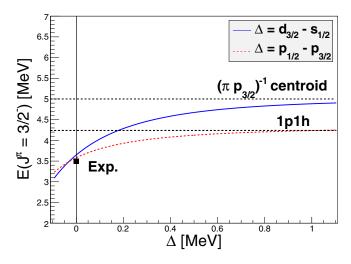


FIG. 3. Energy dependence of the first-excited $3/2^{-}$ state on the shift, Δ , on the energy of the $d_{3/2}$ orbital (solid-blue line) or $p_{1/2}$ orbit (dashed-red line). The dotted black lines denote the energies of the pure 1p-1h or $\pi p_{3/2}^{-1}$ configurations in the initial calculation ($\Delta = 0$). The experimental energy determined in this work is denoted by the black square.

a function of either the N = 16 shell gap (solid-blue line) or the spin-orbit splitting (dotted-red line). By increasing the energy of the $d_{3/2}$ or $p_{1/2}$ orbitals independently, the mixing between the configurations is reduced until they are separated at the asymptotes. In the case of the $d_{3/2}$ orbit, increasing the N = 16 shell gap causes the 1p-1h configuration to be prohibitively costly in energy thus the $3/2^-$ state is comprised entirely of the $\pi p_{3/2}^{-1}$ hole. Likewise, increasing the spin-orbit splitting causes the promotion of a particle from the $\pi p_{3/2}$ to the $\pi p_{1/2}$ to be too energetic, and the lower energy configuration is instead the 1p-1h configuration across the N = 16 shell gap.

Evidence for the size of the N = 16 shell gap in ²⁴O can be deduced from the energy of the first excited 2⁺ state as shown in Figure 4 of Ref. [4]. In order to calculate the equivalent energy in ²³N one has to take the (2J + 1) weighted average of the first $3/2^-$ and $5/2^-$ states. All Hamiltonians considered in Fig. 2 predict these two states to be nearly degenerate, thus the excitation energy of the $3/2^-$ measured in the present experiment can be used to estimate the equivalent 2⁺ energy.

The most recent ENSDF evaluation lists the excitation energy of the first 2^+ in ²⁴O as 4.79(11) MeV [29], corresponding to the weighted average of 4.82(11) [4] and 4.75(14) [5]. A more recent measurement of 4.70(15) MeV [30] agrees with this evaluation.

The present value of the excitation energy of about 3.5 MeV for the $3/2^-$ state in ²³N is 1.3 MeV lower than the 2^+ state in ²⁴O. In the limit of no mixing from the $p_{3/2}^{-1}$ hole configuration, [$\Delta(p_{1/2}) \sim 1$], the energy of the lowest $3/2^$ increases from 3.61 MeV to 4.24 MeV which is 500 keV lower than the excitation of the 2^+ in ²⁴O. The N = 16 shell gap, or the (2J + 1) average of the four lowest states in the 1*p*-1*h* multiplet, is around 4.53 MeV when the contributions from the $p_{3/2}^{-1}$ configuration are removed. This value is 300–400 keV lower than in ²⁴O where this average was found to be 4.95(16) MeV [4], thus the shell gap in ²³N is comparable to ²⁴O. The shift in the effective 2^+ energy is largely due to the coupling to the $p_{3/2}$ hole. In order to confirm this experimentally the excitation energy of the $5/2^-$ state in ²³N should be measured.

V. CONCLUSIONS

Neutron unbound excited states in ²³N were populated via proton knockout from an ²⁴O beam on a deuterium target. The two-body decay energy of ²³N displays two prominent peaks at $E_1 \sim 100$ keV and $E_2 \sim 1$ MeV. Because the daughter nuclide ²²N has two bound excited states, it is not possible to distinguish between degeneracies or multiple level schemes that may produce the observed energy differences in the two-body spectrum of ²³N. A triple coincidence experiment detecting the ²²N fragments, neutrons and γ rays is necessary to measure the branchings to the different final states.

The data are consistent with several shell model interactions which predict a $3/2^-$ state at ~1 MeV and ~2 MeV above S_n in ²³N. Similar to the first excited 2⁺ state in ²⁴O, the first of these two $3/2^-$ states can be used to estimate the N = 16 shell gap. Its excitation energy of about 3.5 MeV is significantly lower than the ²⁴O 2⁺ state at 4.8 MeV, however this reduction is largely due to configuration mixing with the $\pi p_{3/2}^{-1}$ hole, thus indicating only a slight a reduction of the N = 16 gap in nitrogen.

Finally, in order to compare these data directly it is necessary to measure the first excited $5/2^{-}$ state in ²³N. A future experiment designed to populate this state, for example inelastic excitation of ²³N, would be valuable. In addition, the distribution of single-particle strength for the $3/2^{-}$ will be vital to determining the $\pi p_{3/2}^{-1}$ centroid experimentally and further understanding the mixing between the 1p1h and $\pi p_{3/2}^{-1}$ configurations.

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