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Key Points:

- Emissions data involve multiple and interrelated elements that can be more effectively analyzed using multivariate statistical techniques
- By mass conservation, the range of emissions data is inherently constrained, making techniques for compositional data appropriate
- Estimating trace gas emissions using a compositional linear trend based on modified combustion efficiency recognizes these features

Supporting Information:

- Supporting Information S1
- Data Set S1
- Data Set S2Data Set S3
- Data Set S5
- Data Set 54

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Analyzing Wildland Fire Smoke Emissions Data Using Compositional Data Techniques

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Abstract By conservation of mass, the mass of wildland fuel that is pyrolyzed and combusted must equal the mass of smoke emissions, residual char, and ash. For a given set of conditions, these amounts are fixed. This places a constraint on smoke emissions data that violates key assumptions for many of the statistical methods ordinarily used to analyze these data such as linear regression, analysis of variance, and t tests. These data are inherently multivariate, relative, and nonnegative parts of a whole and are then characterized as so-called compositional data. This paper introduces the field of compositional data analysis to the biomass burning emissions community and provides examples of statistical treatment of emissions data. Measures and tests of proportionality, unlike ordinary correlation, allow one to coherently investigate associations between parts of the smoke composition. An alternative method based on compositional linear trends was applied to estimate trace gas composition over a range of combustion efficiency that reduced prediction error by 4% while avoiding use of modified combustion efficiency as if it were an independent variable. Use of log-ratio balances to create meaningful contrasts between compositional parts definitively stressed differences in smoke emissions from fuel types originating in the southeastern and southwestern United States. Application of compositional statistical methods as an appropriate approach to account for the relative nature of data about the composition of smoke emissions and the atmosphere is recommended.

1. Introduction

Wildland fire is a complex phenomenon of chemical and physical processes. Two of the chemical processes which are key to wildland fire are pyrolysis and combustion (Shafizadeh, 1984; Ward, 2001). During pyrolysis, a solid wildland fuel is heated and breaks down into constituent parts consisting of gases, tars, and a solid material called char (Di Blasi, 2008). During combustion, pyrolysis products react with oxygen releasing energy and a large assortment of gaseous and solid chemical compounds (e.g., Akagi et al., 2011; Andreae & Merlet, 2001; May et al., 2014). Oxidation reactions involving atmospheric gases such as nitrogen occur (Crutzen & Brauch, 2016; Lobert et al., 1990). By conservation of mass, the mass of the products is equal to the sum of the masses of the reactants. For the moment we assume that all products can be measured with complete accuracy. The measured masses of the complete list of products simply makes the total mass unknown but does not change the inherent numerical dependency. For example, a simplified balanced global reaction describing combustion of wood containing water and no inorganic content, shows 1 kg dry wood (M = 0) produces 1.82 kg CO₂ and 0.32 kg H₂O for a total mass of products of 2.14 kg (Byram, 1959)

Because of the chemical complexity of wood, Byram approximated the proportion of C, H, and O atoms in wood by $C_6H_9O_4$. Complete combustion with no dissociation is an idealized situation which explains the maximum product mass possible. Incomplete combustion and thermal dissociation will yield additional products and less CO_2 . The foliage of woody plants has a different chemical composition from the wood component which can affect both combustion and combustion products (Hough, 1969; Jolly et al., 2016;



Rogers et al., 1986). The addition of elements such as N and S, and a host of other elements (many inorganic) to the wood, along with inclusion of (a) the oxidation of atmospheric N by fire (Paul et al., 2008) and (b) incomplete combustion changes equation (1) but does not change conservation of mass. The total mass of the products (T) can be partitioned to consist of CO, CO₂, particulate matter (PM), other gases, char, and ash

$$T = CO + CO_2 + other gases + PM + char + ash.$$
(2)

If the masses in equation (2) are transformed into mass ratios by dividing by the total of CO and CO_2 as in

$$\frac{\mathrm{T}}{\mathrm{CO} + \mathrm{CO}_2} = \frac{\mathrm{CO}_2 + \mathrm{CO} + \mathrm{other \ gases} + \mathrm{PM} + \mathrm{char} + \mathrm{ash}}{\mathrm{CO} + \mathrm{CO}_2}$$
$$= \frac{\mathrm{CO}_2}{\mathrm{CO} + \mathrm{CO}_2} + \frac{\mathrm{CO}}{\mathrm{CO} + \mathrm{CO}_2} + \frac{\mathrm{other \ gases}}{\mathrm{CO} + \mathrm{CO}_2} + \frac{\mathrm{PM}}{\mathrm{CO} + \mathrm{CO}_2} + \frac{\mathrm{char}}{\mathrm{CO} + \mathrm{CO}_2} + \frac{\mathrm{ash}}{\mathrm{CO} + \mathrm{CO}_2}, \quad (3)$$
$$= MCE + \frac{\mathrm{CO}}{\mathrm{CO} + \mathrm{CO}_2} + \frac{\mathrm{other \ gases}}{\mathrm{CO} + \mathrm{CO}_2} + \frac{\mathrm{PM}}{\mathrm{CO} + \mathrm{CO}_2} + \frac{\mathrm{char}}{\mathrm{CO} + \mathrm{CO}_2} + \frac{\mathrm{ash}}{\mathrm{CO} + \mathrm{CO}_2},$$

it can be easily seen that modified combustion efficiency (MCE) $MCE = CO_2/(CO+CO_2)$ is part of the total and numerically dependent on the other parts because *T* is fixed. The above example places the masses on a relative basis to the amount of CO and CO₂ produced by a fire, demonstrably two of the three primary products (water being the third). Emissions data have been expressed as relative measures such as emission ratios and emission factors, concentrations, mixing ratios, mole fractions, mass fractions, and volume fractions for a very long time (e.g., Darley et al., 1966; Gerstle & Kemnitz, 1967). However, the statistical properties of relative data have not typically been considered when these data have been analyzed. Compositional data analysis (CoDA) is an approach that explicitly considers the statistical properties of relative data (Aitchison, 1986). Compositional data are contained in the positive orthant of multidimensional real space (Barceló-Vidal et al., 2001). (An orthant is the multidimensional analogue of a quadrant in the more familiar two-dimensional Cartesian space.) A recent paper presented analysis of emissions data using positive matrix factorization, which recognized the nonnegative nature of emissions data (Sekimoto et al., 2018). From a compositional point of view, stoichiometric equations such as (1) have characteristics that discourage, for example, measuring association (correlation) between parts of the composition in the ordinary way (Egozcue et al., 2014).

Individual gases produced during pyrolysis and combustion have long been associated with the different phases or conditions (preignition, flaming, smoldering, and mixed phase) under which the pyrolysis and combustion have occurred (Lobert & Warnatz, 1993; Tangren et al., 1976). Combustion efficiency (CE) and MCE are indices developed to describe the completeness of the conversion of the carbon contained in the fuel to CO_2 (Ward et al., 1980; Ward & Hao, 1991; Yokelson et al., 1997). Theoretically, CE includes all carbon produced; however, the challenge to account for all products and the predominance of CO_2 and CO in smoke emissions led to the development of MCE (Ward & Hao, 1991). It has become common practice to correlate emission factors of products other than CO_2 and CO with MCE (e.g., Amaral et al., 2014; Burling et al., 2010; Ferek et al., 1998; Goode et al., 2000; Janhäll et al., 2010; McMeeking et al., 2009; Shen et al., 2013; Urbanski, 2013; Ward & Hao, 1991; Yokelson et al., 2013) using ordinary linear regression. While linking combustion products to CE and MCE is physically sound, the approach to statistical analysis has to date often ignored the intrinsic multivariate and relative nature of these data. As shown above by equation (3), MCE as an explanatory variable is automatically correlated to every other wildland fire emission (response variable) by its formulation, not because of physical causation.

Aitchison (2003) showed for illustration how two scientists examining the correlation between animal, vegetable, mineral, and water proportions of a sample can arrive at very different correlations (and conclusions) if one scientist dried the sample removing all water before calculating the correlations between the components. We present a similar example (Table 1) using emission factors previously reported (Radke et al., 1988). The original emission factors (g/kg) comprise a composition of *D* parts which were put on a consistent relative scale by applying the closure operation



Exampl	e Illustrating	How Ordinary	Correlation of	Relative Date	a Such as Emis	sion Factors P	roduces Spurio	us Results
			En	nission factor	rs (g/kg)			
СО		CO ₂	CH_4	C_3H_6	C_2H_6	C_3H_8	C_2H_3	PM
74		1664	2.4	0.58	0.35	0.21	0.32	13.5
75		1650	3.6	0.46	0.55	0.32	0.21	23.0
106		1626	3.0	0.70	0.60	0.25	0.22	6.1
89		1637	2.6	0.08	0.56	0.42	0.19	20.2
Full co	mposition (at	fter closure C)						
4.22E	E-2	9.48E-1	1.37E-3	3.30E-4	1.99E-4	1.20E-4	1.82E-4	7.69E-3
4.28E	E-2	9.41E-1	2.05E-3	2.62E-4	3.14E-4	1.83E-4	1.20E-4	1.31E-2
6.08I	E-2	9.33E-1	1.72E-3	4.02E-4	3.44E-4	1.43E-4	1.26E-4	3.50E-3
5.09E	E-2	9.35E-1	1.49E-3	4.57E-5	3.20E-4	2.40E-4	1.09E-4	1.15E-2
No CO	2 subcompos	ition						
8.10E	E-1		2.63E-2	6.35E-3	3.83E-3	2.30E-3	3.50E-3	1.48E - 1
7.27E	2-1		3.49E-2	4.46E-3	5.33E-3	3.10E-3	2.04E-3	2.23E-1
9.07E	2-1		2.57E-2	5.99E-3	5.13E-3	2.14E-3	1.88E-3	5.22E-2
7.87E	E-1		2.30E-2	7.08E-4	4.95E-3	3.72E-3	1.68E-3	1.79E-1
Pearsor	n correlation							
CO_2	Full (F)		-0.25	0.18	-0.93	-0.49	0.82	0.25
CO	F	-0.88	-0.01	0.19	0.69	0.06	-0.44	-0.68
	Sub (S)		-0.59	0.40	-0.10	-0.67	-0.03	-1.00
CH_4	F			0.19	0.58	0.12	-0.53	0.31
	S			0.29	0.37	0.00	0.01	0.53
C ₃ H ₆	F				-0.17	-0.92	0.51	-0.71
	S				-0.36	-0.95	0.61	-0.47
C_2H_6	F					0.54	-0.93	-0.01
	S					0.38	-0.92	0.09
C_3H_8	F						-0.81	0.65
	S						-0.53	0.72
C_2H_3	F							-0.34
	S							0.01

Table 1

Note. Data from Radke et al. (1988). Shading identifies the gases for which the correlation coefficient changed by 0.25 or more between the full composition and the subcomposition.

$$C(\mathbf{x}) = \frac{[x_1, x_2, ..., x_D]}{\sum_{i=1}^{D} x_i}$$
(4)

which divides the emission for each gas (x_i) by the sum of emissions and express the data as fractions of a fixed total, this being 1 by default to be expressed in proportions but in general any other total by simple multiplication (e.g., $C(\mathbf{x}) \cdot 10^2$ for percentages or $C(\mathbf{x}) \cdot 10^6$ for parts per million). After closure, the CO₂ emission factor of 1,664 g/kg becomes the proportion 0.948.

Regardless of the total, it is important to note that the resulting relativized data vector is equivalent to the original emission factors and lives in what is known as a D part simplex and, hence, statistical analysis on any equivalent representation of the data should provide the same results. In the example in Table 1, D =8 for the full composition. The familiar Pearson correlation coefficient (r) was then calculated for all pairs of gases. In the full composition, CO was negatively correlated with CO_2 (r = -0.88), positively correlated with C_2H_6 (0.69), and not correlated with C_3H_8 (0.06). The emission factor for CO_2 was then removed from the full composition as if it had not been measured and the closure operation was performed on the subcomposition (subset), producing the second set of values, and correlation between the pairs was calculated. Correlation coefficients which changed appreciably are highlighted. Note that CO is now negatively correlated with C_3H_8 (-0.67) and not correlated with C_2H_6 (-0.10). Similarly, CH_4 was negatively correlated with C_2H_3 in the full composition (-0.53) and not correlated (0.01) when CO_2 is not in the composition. The point of this illustration is that this index (Pearson correlation coefficient) that is generally trusted as a measure of pairwise association can produce different results depending on something that should not affect it. This is



an artifact not related to the actual relationship between the variables. Hence, it is not a reliable measure with this type of data, regardless of the magnitude of the difference in a particular case, which will be arbitrarily big or small. That the interpretation of these changing correlations could lead to spurious conclusions is well known (Pearson, 1896). This simple example illustrates the problem using correlation with relative data. Linear regression utilizes correlation so it is also affected by this constraint: measuring associations in terms of proportionality is a coherent and meaningful alternative to ordinary correlation for compositional data (Egozcue et al., 2014, 2018; Lovell et al., 2015).

The use of predictions resulting from correlations and linear regressions that do not account for the relative nature of emissions data may produce misleading estimates in emissions inventories developed by various regulatory agencies. This is true for operational tools such as the Fire Emissions Production Simulator and its successors (Anderson et al., 2004) as well as the First Order Fire Effects Model and its successors. It also represents just one of many sources of potential error in emissions calculations (Ottmar et al., 2008; Surawski et al., 2016). In this paper we therefore propose a different approach to analyze emissions data that reflects their compositional nature. A well-principled methodological body to analyze compositional data has been developed in the past 30 years, and this is an active area of statistical research so we have chosen to apply it to fire emissions data, in particular gas-phase emissions. Interestingly, it has been successfully applied in varied fields but appears to have seldom been applied to combustion or emissions data (Bandeen-Roche, 1994; Billheimer, 2001; Buccianti & Pawlowsky-Glahn, 2006; Speranza et al., 2018).

The relative nature of emissions data defines emissions data as compositional data, which are coherently analyzed using CoDA (Aitchison, 1986; Barceló-Vidal et al., 2001; Lovell et al., 2015; Pawlowsky-Glahn, Egozcue, & Tolosana-Delgado, 2015). CoDA methodology has three underlying principles. The first is scale invariance—vectors with proportional positive components represent the same composition, and form what is known as an equivalence class. This means changing the units should not change relative relationships between the parts nor affect results and scientific conclusions. The second is that inferences about subcompositions, that is, smaller compositions formed from subsets of parts, must not contradict the inferences from the full composition (as in the example in Table 1). The third principle states that the order of the parts of the composition must not affect the inferences. While the initial work on CoDA explicitly assumed in the definition of a composition that the parts sum (are closed) to a constant total, theory has developed to show that this is only a particular representation of the data in a simplex and equivalent nonclosed compositions carry the same relative information (Barceló-Vidal & Martín-Fernández, 2016). So the "conservation of mass" argument presented earlier is not necessary for emissions data to be considered compositional as shown by Egozcue (2009). The structural relationship and interdependence between MCE and other emissions as shown in (3) still holds.

Aitchison (1982) showed that a meaningful approach to compositional data is to analyze log ratios of the parts, which carry the relative information. Aitchison (1986) defined the two basic operations of perturbation (\oplus , analogous to addition or translation with ordinary real-valued data)

$$\mathbf{z} = \mathbf{x} \oplus \mathbf{p} = C[x_1 \cdot p_1, \dots, x_d \cdot p_d]$$
(5)

and power transformation (\otimes , analogous to multiplication by a scalar)

$$\mathbf{z} = \lambda \otimes \mathbf{x} = C[x_1^{\lambda}, ..., x_d^{\lambda}]$$
(6)

where **x** is the initial composition, **p** is a perturbation vector, and λ is a constant. These operations are foundational to CoDA.

In CoDA today, in order to use familiar statistical techniques such as exploratory data analysis, linear regression, multivariate analysis of variance, and other multivariate techniques, the mainstream approach is to transform the parts from the simplex to real numbers using isometric log-ratio (ilr) coordinates (Egozcue & Pawlowsky-Glahn, 2005; Mateu-Figueras et al., 2011; Pawlowsky-Glahn, Egozcue, & Tolosana-Delgado, 2015; van den Boogaart & Tolosana-Delgado, 2013). The linear algebra theory supporting these transformations also provides the underpinnings for "standard" or "classical" statistics routinely used in the sciences (Graybill, 2002). Several texts describe the theory and methods of compositional data analysis (Aitchison, 1986; Filzmoser et al., 2018; Pawlowsky-Glahn & Buccianti, 2011; Pawlowsky-Glahn, Egozcue, &



Tolosana-Delgado, 2015; van den Boogaart & Tolosana-Delgado, 2013). Software to perform compositional data analysis is available, including the stand-alone point-and-click *CoDaPack* package (Thió-Henestrosa & Comas, 2016) (http://www.compositionaldata.com/codapack.php) and comprehensive libraries on the open-source R statistical computing system (R Core Team, 2018): *compositions* (van den Boogaart & Tolosana-Delgado, 2013), *robCompositions* (Templ et al., 2011), and *zCompositions* (Palarea-Albaladejo et al., 2014; Palarea-Albaladejo & Martín-Fernández, 2015).

The above considerations borne in mind, the objectives of this manuscript are to reanalyze the Burling et al. (2010) emissions factors data to (1) determine if parts (individual gases) were proportional to each other (in place of correlated in the usual way), (2) determine if a compositional linear trend can be used to model the data as CE changes (in place of ordinary linear regression using MCE), and (3) determine if the composition of the gases differed between fuel types using analysis of variance within a CoDA framework. We hope to demonstrate that the CoDA approach can shed as much or more light on the relationships in and between the emissions data by applying techniques consistent with the nature of the data instead of using simple linear regression with MCE thus avoiding artifacts derived from the nature of the data.

2. Statistical Methods

Burling et al. (2010) reported emission factors for 18 gases measured using an open-path Fourier transform infrared spectroscopy (FTIR) spectrometer and characteristics of the combustion (fuel moisture content, fuel consumption, and MCE) for 65 laboratory fires (observations) in 15 different wildland fuel types. Each of the 65 observations comprised a vector $\mathbf{x}_i = [x_1...x_{18}]_i$ where parts $x_1...x_{18}$ were the measured emission factors for CO₂, CO, CH₄, C₂H₂, C₂H₄, C₃H₆, CH₃OH, HCOOH, CH₃COOH, HCHO, C₄H₄O, NH₃, NO, NO₂, HONO, HCN, HCl, and SO₂, respectively. In actuality, these 18 gases were a subcomposition of a much larger composition of gaseous and solid emissions sampled from these experimental fires by a variety of methods and instruments described elsewhere (Burling et al., 2010; Chang-Graham et al., 2011; Gilman et al., 2015; Hosseini et al., 2010, 2013; Roberts et al., 2010; Veres et al., 2010; Warneke et al., 2011; Weise et al., 2015; Yokelson et al., 2013). The full composition for this experiment consisted of over 100 parts. The data set resulted from a laboratory study at the United States Forest Service's Missoula Fire Sciences Lab. This Fire Sciences Lab study characterized smoke emissions related to prescribed burning of 15 different shrub and woodland fuel types from the southeastern and southwestern Unites States and described the composition of gas and particulate matter in detail. In the present paper, 18 gases were reanalyzed, which had previously been measured using an open-path FTIR spectrometer (Burling et al., 2010) and then adjusted to field values using MCE (Yokelson et al., 2013). While it is possible to measure H₂O (gas) in smoke emissions using FTIR and while it is a significant product of combustion that can influence flame processes (Ferguson et al., 2013), emission factors for H₂O are not typically reported. The gas-phase data analyzed here are originally available as supporting information to the Yokelson et al. (2013) paper. Furan (C_4H_4O) and hydrochloric acid (HCl) had one and four (1.5% and 6%) instances of below detection limit values, respectively. In order to facilitate statistical analysis, the log-ratio EM algorithm included in the *zCompositions* package was used to impute the below detection limit values with realistically small values while accounting for their compositionality (Palarea-Albaladejo & Martín-Fernández, 2015). In the following, we introduce the basic compositional analyses conducted using these data that are analogous to those commonly conducted on emission data.

2.1. Summary Statistics and Proportionality Associations

The data were closed and compositional summary statistics consisting of the center (geometric mean) and the variation array (Aitchison, 1986) were estimated. The center ($\overline{\mathbf{g}}$) is the closed vector of geometric means for each part estimated as

$$\widehat{\mathbf{g}} = C[\widehat{g}_1, \widehat{g}_2, ..., \widehat{g}_D] \tag{7}$$

where $\hat{g}_j = (\prod_{i=1}^n x_{ij})^{1/n}, j = 1, 2, ..., D$. While there are different measures for the variability of compositional data (van den Boogaart & Tolosana-Delgado, 2013), a common summary is given by the variance (τ_{ij}) of the log-ratio of parts *i* and *j*; the variation matrix **V** is a *D* x *D* symmetric matrix containing elements estimated by



$$\widehat{\tau}_{ij} = \operatorname{var}\left(\ln\frac{x_i}{x_j}\right) \tag{8}$$

where *i* and *j* range from 1 to *D* and var is the usual variance. The total (or metric) variance (Mvar) can be obtained from them as (Egozcue & Pawlowsky-Glahn, 2011; Pawlowsky-Glahn & Egozcue, 2001):

$$Mvar(\mathbf{x}) = \sum_{i} \sum_{j} \hat{\tau}_{ij} = \sum_{i=1}^{D} var[clr_i(\mathbf{x})]$$
(9)

where the centered log-transformation (clr) and its inverse are

$$\operatorname{clr}(\mathbf{x}) = \left[\ln \frac{x_1}{g_m(\mathbf{x})}, \ln \frac{x_2}{g_m(\mathbf{x})}, \dots, \ln \frac{x_D}{g_m(\mathbf{x})} \right], \quad g_m(\mathbf{x}) = \left(\prod_{i=1}^D x_i \right)^{1/D}$$
$$\operatorname{clr}^{-1}(\mathbf{x}) = C[\exp(\operatorname{clr}(\mathbf{x}))] \tag{10}$$

and the metric standard deviation (Mstd) is $\sqrt{\frac{Mvar}{D-1}}$. In general, the smaller the values of $\hat{\tau}_{ij}$, the more proportional are the parts involved.

For noncompositional data, relationships between variables are ordinarily explored by examining correlation (parametric or nonparametric) between the variables. For compositional data, proportionality is the preferred measure to examine relationships between parts of a composition in accordance with their relative scale (Aitchison, 1986; Lovell et al., 2015). As stated in Lovell et al. (2015), "measures of association produce results regardless of the data they are applied to-it is up to the analyst to ensure that the measures are appropriate to the data." They further state that proportional relative abundances imply that the absolute abundances are proportional. Balance association (or b-association for short) was developed as a consistent statistical concept of proportionality (Egozcue et al., 2018). A measure of b-association, ϕ , has been defined and used to formulate a statistical hypothesis test of equality to ± 1 of the slope coefficient of a major or standardized major axis regression model (Warton et al., 2006) relating one log contrast of parts to another log-contrast. This is the so-called unitary slope test, with significance based on a standard F distribution (Egozcue et al., 2018; Lovell et al., 2015). Rejection of the hypothesis suggests that the data are not compatible with b-association (or proportionality) between the parts; however, it does not distinguish whether the slope is positive or negative. Following Egozcue et al. (2018), we rejected the hypothesis when the estimated slope was negative and reported the p value as a minus sign (-).

2.2. Compositional Linear Trend Analysis

Since its introduction *MCE* has frequently been correlated to single emission factors (*EF*) by linear regression $EF = \beta_0 + \beta_1(MCE)$ (Ward & Hao, 1991), which assumed that the predictor variable *MCE* could be treated separately from the response variable *EF*. As shown above in equation (3), this is not the case, so an alternative method to estimate emission factors developed for compositional data was applied instead. Deriving principal components from multivariate data is a common practice. They were used in von Eynatten et al. (2003) to develop the compositional linear trend method, which we apply to our data using recently developed R code (Rockwell et al., 2014). The basic idea is that compositional data can be projected onto the first principal component to produce a linear trend provided that the first principal component explains a large proportion of the total variance. The projected (or fitted) composition can be transformed back to the original units (Pawlowsky-Glahn, Egozcue, Olea, & Pardo-Igúzquiza, 2015). We chose to apply this method because it has been well established that the composition of smoke changes as the CE changes (Byram, 1957). If the linear trend method works, it could potentially be applied to other data sets to predict composition.

When originally developed, the linear trend method was applied to geological data to model the compositional changes in granitic rocks as they weathered from fresh parent material. The unweathered parent material served as the starting point of the linear trend, which is formulated in the simplex as



$$\mathbf{x} = \mathbf{a} \oplus (k \otimes \mathbf{p}) = \mathscr{C} \left[a_1 p_1^k, ..., a_d p_d^k \right]$$
(11)

and estimated by

$$\widehat{\mathbf{x}} = \mathbf{a} \oplus \left(k \otimes \operatorname{clr}^{-1}[\mathbf{v}_1] \right) \tag{12}$$

where **a** is the starting composition, k is the latent trend, **p** is a perturbation vector estimated by $clr^{-1}(\mathbf{v}_1)$, \mathbf{v}_1 is the first eigenvector derived by noncentral principal component analysis of the original *n* observations $x_1,...,x_n$ after they were adjusted to the starting point **a** by $clr(x_1) - clr(a),...,clr(x_n) - clr(a)$. Noncentral principal component analysis indicates the variances were maximized relative to a instead of to the mean (von Eynatten, 2004). The full mathematical development can be found elsewhere (von Evnatten et al., 2003). The linear trend method describes changes within a compositional data set that are not attributed to variables external to the composition. In the present study, we evaluated three compositions as the potential starting composition a: the highest (High) and lowest (Low) MCE compositions and the center composition of the data set. Linear regressions were not fit for CO and CO₂ since they form MCE. In order to compare the performance of the linear trend to the ordinary linear regression, common error measures were calculated using the observed and predicted emission factors for each gas for each linear regression and linear trend. The estimated values were scaled to the original units (Pawlowsky-Glahn, Egozcue, Olea, & Pardo-Igúzquiza, 2015). The normalized mean absolute error (NMAE) and root-mean-square error (RMSE) of the observed and estimated values were calculated using the modStats function in R (Carslaw, 2015; Carslaw & Ropkins, 2012). Since multivariate linear regression is the extension of linear regression to data with correlated response variables (Fox & Weisberg, 2018, 2019), we performed a multivariate linear regression with all trace gases except CO and CO_2 as the dependent variables and MCE as the predictor variable. The fitted values from the multivariate linear regression were identical to the individual linear regressions so the error measures were identical and are not presented. Multivariate linear regression, even though it takes into the account the correlation structure between the parts of the composition, was still subject to the fact that the MCE ratio was not independent of the other gases in the mixture. To examine the fits of the linear trend and multivariate linear regression for the entire composition, a coefficient of determination (R_{CLT}^2) for the linear trend (Cayuela-Sánchez et al., 2019; van den Boogaart & Tolosana-Delgado, 2013) and the squared multiple correlation coefficient (R_{IR}^2) for the multivariate linear regression (Mardia et al., 1979) were estimated. The metric standard deviation in the original emission factor units exp(Mstd) and the RMSE of the multivariate linear regression (calculated as the square root of the mean of the trace of the residual matrix) estimated $RMSE_{CLT}$ and $RMSE_{LR}$, respectively.

2.3. Multivariate Analysis of Variance

Analysis of variance was used to test for differences in the composition of the gases according to fuel type. Note that because of experimental design deficiencies resulting in a singular design matrix, it was not possible to consider fuel type and region simultaneously. Egozcue and Pawlowsky-Glahn (2005) devised a procedure to obtain sets of ilr coordinates by sequential binary partitioning that can be used to represent comparisons between scientifically meaningful subsets of parts of a composition. These ilr coordinates known as compositional balances \tilde{z}_k are defined as

$$\widetilde{z}_{k} = \sqrt{\frac{r_{k}s_{k}}{r_{k} + s_{k}}} \ln \frac{\left(x_{i_{1}}x_{i_{2}}...x_{i_{r_{k}}}\right)^{1/r_{k}}}{\left(x_{j_{1}}x_{j_{2}}...x_{j_{s_{k}}}\right)^{1/s_{k}}}, \quad k = 1, ..., D-1$$
(13)

where the log-ratio compares the geometric mean of r_k parts in one subset with the geometric mean of s_k parts in another subset. Sequential binary partitioning of a composition containing *D* parts results in *D*-1 balances \tilde{z}_k , k = 1, ..., D-1. The emissions data were then transformed into balance coordinates that partitioned the composition into various meaningful subsets of parts. The matrix used to define the subsets contains 1, -1, or a blank to indicate that the part is in subset 1 (numerator), subset 2



(denominator), or absent from the log ratio, respectively. Once the data were transformed into balance coordinates, analysis of variance was used on them to test for differences in mean according to fuel type. Given the large number of statistical tests performed in this analysis, we chose to adjust the p values to control for false discovery rate (Benjamini & Hochberg, 1995). Statistical significance was assessed at the usual 5% level.

3. Results and Discussion

3.1. Summary Statistics

MCE ranged from 0.91 for the *lit* fuel type to over 0.98 for the *oas* fuel type. The geometric mean of MCE for the data set was 0.96. (Details of the fuel types and fuel consumption in the individual fires have been presented in the original publications (Burling et al., 2010; Hosseini et al., 2010, 2013)). Numerical differences in the MCE values reported by Burling et al. (2010) and Yokelson et al. (2013) due to adjustment for field measurements are described in the latter reference. Unsurprisingly, the chemical compositions changed as CE decreased from high to low (Table 2). Examination of the compositional makeup of the low MCE, geometric mean MCE, and high MCE revealed that relative abundance of all gases except CO_2 , NO, and NO_2 increased as the MCE decreased. By definition, CO_2 increases and CO decreases as the MCE increases. Previously reported gas species associated with flaming combustion (higher MCE) include CO_2 , NO, NO_2 , HCl, SO_2 and HONO; those usually associated with smoldering combustion (lower MCE) include CO, CH_4 , NH_3 , HCN, C_3H_6 , CH_3OH , CH_3COOH , and C_4H_4O (Burling et al., 2010; Goode et al., 2000). Of the species we measured, the remaining ones have been associated with both flaming and smoldering combustion.

Large variation in the emission factor for HCl for this data set was previously reported (Burling et al., 2010). The large log-ratio variance associated with HCl was also readily apparent in a biplot (Aitchison & Greenacre, 2002) produced from the first two principal components of the data set (not shown). This can be also seen with its clr-variance (Table 2). The clr-variance for HCl (1.50) was approximately 25% of the total variance (6.09). The clr-variances for the remaining 17 parts were similar in size, yet small compared to HCl. While there were several low values of $\hat{\tau}_{ij}$ that suggested proportionality, only a few of the unitary slope tests were not statistically significant (Table 2) suggesting that some of the gases might be pairwise proportional. Potential pairwise proportionality relationships include: (1) propene (C₃H₆) with acetic acid (CH₃COOH), formaldehyde (HCHO), furan (C₄H₄O), ammonia (NH₃), and HCN (hydrocyanic acid), all of which have been associated with smoldering combustion; and (2) acetic acid with furan, nitrous acid (HONO) and HCN. The mean log ratios of the five gases potentially proportional with propene ranged from -0.62 (HCN) to 1.61 (acetic acid) suggesting relatively less propene than HCN consistently in the smoke samples and relatively more propene than acetic acid, consistently. While the log-ratio variances for these five gases with propene were similar in size (0.25 to 0.33), the probabilities associated with the F tests ranged considerably (0.07 to 0.94); the higher probability levels provide more support for the potential proportionality of propene with the other hydrocarbons and less support for proportionality with the two N gases (NH_3 and HCN). Note that while the log-ratio variance of CH₃OH with propene was lower than the log-ratio variances for CH₃COOH, HCHO, furan, ammonia and HCN, the slope test rejected potential pairwise proportionality. Other smoldering compounds for which results were compatible with proportionality included (3) formaldehyde with methanol, acetic acid, and furan; (4) ethene (C_2H_4) with methane and ammonia; and (5) HCN with methane and furan. Of the gases associated with flaming combustion, CO2 was potentially proportional with NO2, C2H2, and HONO. It was interesting to note that some gases normally associated with flaming show some level of proportionality with smoldering gases: HONO with acetic acid, SO₂ with CO and ammonia. Because of its large variability, HCl exhibited the lowest proportionality to any other gas in the composition; all tests were rejected since the slope values were negative (Egozcue et al., 2018). All log-ratio means for HCl were negative which indicated that the proportion of HCl in the compositions was relatively smaller than the proportions of the other gases.

3.2. Compositional Linear Trend as an Alternative to MCE Linear Regression

For all gases except CO_2 , NO, and NO_2 , the proportions decreased from the Low MCE fire to the High MCE fire (Tables 2 and 3), which is consistent with previously reported findings (Burling et al., 2010), suggesting



Table 2 Variation Arre	ıy and Ceni	er of Smo	ke Emiss.	ions														
	CO2	СО	CH_4	C_2H_2	C_2H_4	C_3H_6	CH ₃ OH	НСООН	CH ₃ COOH	НСНО	C_4H_4O	$\rm NH_3$	ON	NO_2	ONOH	HCN	HCI	SO_2
CO_2		0.12 (0.00)	0.37	0.50 (0.11)	0.43	0.69	0.65	0.92	0.73	0.71	0.63	0.24 (0.02)	0.06 (0.00)	0.16 (0.23)	0.23 (0.11)	0.95	2.88 (0.00)	0.14 (0.00)
CO	-3.33		0.18	0.33 (0.00)	0.20	0.41	0.33	0.58 —	0.44	0.36 —	0.33	0.17 (0.02)	0.22 (0.00)	0.21 (0.00)	0.21 (0.00)	0.54	2.66 (0.00)	0.10 (0.29)
CH4	-7.05	-3.72		0.36 (0.00)	0.08 (0.45)	0.17 (0.00)	0.17 (0.03)	0.51	0.31 —	0.27	0.35	0.15 (0.03)	0.53	0.38	0.32	0.29 (0.00)	2.92	0.18
C_2H_2	-9.61	-6.28	-2.56		0.28 (0.00)	0.64	0.70	1.05	0.88 —	0.67	0.85	0.42 (0.00)	0.63	0.67	0.48 (0.00)	0.87	2.78 (0.00)	0.44 (0.00)
C_2H_4	-8.28	-4.95	-1.23	1.33	~	0.12 (0.00)	0.19 (0.15)	0.49	0.33 —	0.24 (0.01)	0.35	0.18 (0.15)	0.56	0.42	0.27	0.30 (0.00)	3.13	0.21
C_3H_6	-9.43	-6.10	-2.37	0.18	-1.14		0.16 (0.04)	0.48 (0.03)	0.29 (0.94)	0.25 (0.49)	0.33 (0.81)	0.30 (0.08)	0.86 —	0.58	0.43	0.26 (0.07)	3.47	0.40
CH ₃ OH	-8.48	-5.15	-1.43	1.13	-0.20	0.94		0.21 (0.00)	0.07 (0.00)	0.08 (0.11)	0.17 (0.02)	0.35	0.83	0.44	0.37	0.16 (0.00)	3.31	0.31
НСООН	-10.11	-6.78	-3.05	-0.50	-1.83	-0.68	-1.63		0.13 (0.00)	0.12 (0.00)	0.22 (0.01)	0.74	1.14	0.61	0.49 (0.00)	0.44 (0.56)	3.81 —	0.59
CH ₃ COOH	-7.82	-4.49	-0.76	1.79	0.47	1.61	0.66	2.29		0.09 (0.27)	0.20 (0.85)	0.52	0.94 —	0.43	0.36 (0.35)	0.28 (0.09)	3.53	0.38
НСНО	-8.43	-5.10	-1.38	1.18	-0.15	1.00	0.05	1.68	-0.61		0.17 (0.28)	0.51	0.93	0.48	0.36 	0.28 (0.01)	3.34 —	0.41
C_4H_4O	-10.17	-6.84	-3.12	-0.56	-1.89	-0.75	-1.69	-0.06	-2.35	-1.74		0.45	0.81	0.52	0.46 —	0.33 (0.14)	3.51	0.38
$\rm NH_3$	-8.04	-4.71	-0.99	1.57	0.24	1.38	0.44	2.07	-0.22	0.39	2.13		0.30 (0.00)	0.32	0.31	0.44 (0.00)	2.93 —	0.15 (0.13)
ON	-6.70	-3.37	0.35	2.91	1.58	2.73	1.78	3.41	1.12	1.73	3.47	1.34		0.28 (0.00)	0.34 (0.00)	1.14	3.10	0.21 (0.00)
NO_2	-7.85	-4.52	-0.79	1.76	0.44	1.58	0.63	2.26	-0.03	0.58	2.32	0.19	-1.15		0.19 (0.59)	0.72	2.87 —	0.18 (0.00)
ONOH	-8.87	-5.54	-1.82	0.74	-0.59	0.55	-0.39	1.24	-1.05	-0.44	1.30	-0.83	-2.17	-1.02		0.73	3.33	0.21
HCN	-10.05	-6.72	-2.99	-0.44	-1.76	-0.62	-1.56	0.06	-2.23	-1.62	0.12	-2.01	-3.35	-2.20	-1.17		3.49	0.48
HCI	-10.46	-7.13	-3.41	-0.85	-2.18	-1.04	-1.98	-0.36	-2.65	-2.03	-0.29	-2.42	-3.76	-2.62	-1.59	-0.42		3.01
SO_2	-7.74	-4.41	-0.69	1.87	0.54	1.68	0.74	2.37	0.07	0.69	2.43	0.30	-1.04	0.11	1.13	2.30	2.72	
Low Center	900. 961.	87.4 34.4	2.960 0.830	0.084 0.064	0.565 0.243	0.227 0.077	$1.160 \\ 0.199$	0.375 0.039	1.950 0.387	1.570 0.210	0.345 0.037	0.460 0.309	1.020 1.180	0.214 0.375	0.170 0.135	0.382 0.042	0.036 0.027	0.926 0.417
High clr (variance)	981. 0.29	15.5 0.21	0.287 0.21	0.020 0.35	0.064 0.22	0.017 0.27	0.060 0.24	0.018 0.35	0.181 0.28	0.063 0.26	0.016 0.28	$0.110 \\ 0.24$	$1.610 \\ 0.36$	$0.316 \\ 0.26$	0.093 0.25	0.005 0.32	$0.001 \\ 1.50$	0.363 0.22
<i>Note</i> . The upper rejection of th The lower left tional makeup	er right tria e null hypc triangular (as propor	ngular ma othesis of matrix co tions) for	atrix cont perfect pi ntains the	ains estin roportion e log-ratio st, highe	nates of lo ality. Sha o means; s st, and ce	ig-ratio va ding indic shaded lo nter MCE	rriance $(\hat{\tau}_{ij})$ cates that the g-ratio mea 3 values (X	and (proba) ne hypothes uns correspc 10 ³) and th	bility of F statis sis was not rejeond to the unre- bud to the unre- be clr(variance)	stic for slop cted at the jected valu of each pa	e test of pr 5% signifi es in the u urt.	oportiona cance leve pper triar	lity). The el suggest igular ma	minus (– ing poten trix. The	-) sign den itial propo four botto	notes a neg ortionality om rows a	gative sloj between re the cor	parts. parts. nposi-



Table 3

Starting Point Compositions (a) in Original Units (g/kg) and Estimated Perturbation Vectors (p) for a Compositional Linear Trend Fit to a Data Set of Smoke Emissions From Wildland Fuel

		Starting point (a	h)	P	erturbation ((p)
Gas	Low MCE (0.911)	Center	High MCE (0.984)	Low MCE	Center	High MCE
CO ₂	1584.6780	1739.8798	1745.3486	0.0716	0.0572	0.0722
CO	153.7918	62.2174	27.5268	0.0552	0.0558	0.0569
CH ₄	5.2066	1.5030	0.5105	0.0500	0.0521	0.0525
C_2H_2	0.1473	0.1167	0.0358	0.0654	0.0583	0.0510
C_2H_4	0.9946	0.4395	0.1144	0.0553	0.0503	0.0491
C ₃ H ₆	0.3993	0.1402	0.0299	0.0515	0.0472	0.0464
CH ₃ OH	2.0335	0.3601	0.1060	0.0434	0.0472	0.0506
НСООН	0.6595	0.0708	0.0317	0.0380	0.0442	0.0572
CH ₃ COOH	3.4240	0.7000	0.3222	0.0448	0.0457	0.0574
НСНО	2.7553	0.3799	0.1128	0.0408	0.0471	0.0507
C_4H_4O	0.6071	0.0666	0.0282	0.0387	0.0465	0.0563
NH ₃	0.8104	0.5600	0.1948	0.0627	0.0539	0.0534
NO	1.7903	2.1428	2.8557	0.0736	0.0572	0.0785
NO ₂	0.3762	0.6791	0.5613	0.0795	0.0548	0.0680
HONO	0.2986	0.2439	0.1652	0.0651	0.0503	0.0651
HCN	0.6733	0.0754	0.0086	0.0386	0.0468	0.0389
HCl	0.0631	0.0497	0.0025	0.0689	0.1327	0.0273
SO ₂	1.6302	0.7546	0.6450	0.0569	0.0528	0.0686

Note. The starting points after closure are contained in Table 2.

the possibility of fitting a compositional linear trend (equation (11)). The three possible starting compositions (**a**) for the linear trend and the estimated perturbation vector (**p**) for each are contained in Table 3. The goodness of fit of the linear trend to the data (determined by the first eigenvalue λ_1 as a percentage of the total variation) was 72.9%, 77.5%, and 50.1% for the High, Low and GM starting points, respectively. Of the three linear trends, using the Low MCE composition as the starting point produced the smallest absolute errors, lowest RMSE, and highest correlation between the observed and predicted values for 14 of the 18 gases (Table 4). While Low MCE produced the lowest mean bias (NMB) for eight of the gases and GM for six gases, NMB was similar for several gases for all three linear trends. Using the GM as the starting point provided a better fit for NO₂, HONO, and HCl. There was no correlation between observed and predicted values for C₂H₂ from any of the three linear trends. The observed and predicted values for NO₂ and HCl were negatively correlated for the Low MCE trend.

When compared to the fitted ordinary linear regressions for each gas, the Low MCE compositional trend had smaller errors (NMAE) for 12 of the 18 gases, lower RMSE for 8 of the 18 and higher correlation (r) for 13 of the 18 gases (Table 5). Overall, the geometric mean NMAE for the CLT (0.26) was less than LR (0.30) indicating the linear trend estimates had less error than the linear regression estimates; however, the CLT was negatively biased. Bias for linear regression was 0 in all cases because the residuals $(\hat{y}_i - y_i)$ sum to 0 for every linear regression with an intercept term (Draper & Smith, 1981). Mean RMSE for the CLT and LR were equal. The correlations between observed and estimated values for most of the trace gases were similar between the linear trend and the linear regression models. For the linear trend, correlation between observed and predicted values was not significant for C₂H₂ and NO; for linear regression there was no significant correlation between observed and predicted values for NO2 and HCl. In some cases (such as HONO), the EF was fairly constant (Figure 1). For 9 of the 16 gases, correlation for the CLT was larger than for the LR. For the overall measures, the coefficient of determination R_{CLT}^2 for the Low MCE linear trend (0.283) was lower than the comparable measure R_{LR}^2 for the multivariate linear regression (0.933). It is interesting to note that R_{CLT}^2 for the GM linear trend was 0.501. Because R_{CLT}^2 is a measure of the entire composition projected onto the first principal component, parts of the composition (gases) more strongly associated with other principal components would contribute to the lack of fit of the linear trend. Preliminary analysis of the data using a biplot (Aitchison & Greenacre, 2002) suggested that HCl was not strongly associated with



Table 4

Ordinary Measures of Fit Based on Observed and Predicted Emission Factors for Compositional Linear Trends That Started at the High, Low, or Geometric Mean (GM) Value of MCE for Gases Associated With Smoke From Wildland Fire

Gas		NMB			NMAE ^a			RMSE			r	
	High	Low	GM	High	Low	GM	High	Low	GM	High	Low	GM
CO ₂	0.00	0.00	0.00	0.01	0.01	0.01	26.16	16.65	26.60	0.94	0.98	0.94
СО	-0.07	0.04	-0.05	0.26	0.20	0.24	22.35	16.26	22.77	0.38	0.78	0.08^{N}
CH_4	-0.15	-0.04	-0.14	0.40	0.30	0.42	1.08	0.68	1.10	0.32	0.79	0.24
C_2H_2	-0.23	-0.24	-0.24	0.52	0.53	0.54	0.15	0.15	0.15	0.16 ^N	0.12^{N}	-0.10^{N}
C_2H_4	-0.21	-0.19	-0.18	0.50	0.37	0.47	0.49	0.42	0.47	0.17^{N}	0.58	0.30
C ₃ H ₆	-0.28	-0.26	-0.23	0.59	0.41	0.55	0.17	0.14	0.17	0.24	0.74	0.32
CH ₃ OH	-0.29	-0.12	-0.24	0.63	0.27	0.55	0.51	0.23	0.50	0.25	0.92	0.29
НСООН	-0.40	-0.11	-0.32	0.73	0.28	0.68	0.14	0.06	0.14	0.17^{N}	0.92	0.27
CH ₃ COOH	-0.33	-0.21	-0.26	0.67	0.34	0.60	1.11	0.66	1.08	0.20^{N}	0.87	0.28
НСНО	-0.31	-0.07	-0.27	0.65	0.26	0.59	0.58	0.24	0.56	$0.19^{ m N}$	0.91	0.32
C_4H_4O	-0.33	0.02	-0.27	0.63	0.23	0.56	0.12	0.03	0.12	0.22^{N}	0.96	0.27
NH ₃	-0.12	-0.12	-0.09	0.37	0.33	0.36	0.30	0.27	0.29	0.29	0.43	0.12^{N}
NO	0.00	-0.01	-0.02	0.17	0.16	0.18	0.48	0.47	0.50	0.31	0.18^{N}	-0.21^{N}
NO ₂	-0.08	-0.17	-0.07	0.32	0.37	0.32	0.32	0.39	0.31	0.18^{N}	-0.43	0.21^{N}
HONO	-0.16	-0.16	-0.09	0.41	0.35	0.35	0.16	0.14	0.14	-0.02^{N}	0.58	0.41
HCN	-0.38	-0.14	-0.37	0.73	0.36	0.68	0.17	0.08	0.17	0.27	0.92	0.28
HCl	-0.17	-0.47	-0.02	0.42	0.77	0.35	0.08	0.14	0.06	0.85	-0.32	0.90
SO ₂	-0.05	-0.01	-0.05	0.27	0.20	0.28	0.31	0.20	0.30	-0.03^{N}	0.75	0.25

Note. Highlighted values indicate the best value for each measure by gas.

^aNMB is normalized mean bias, NMAE is normalized mean average error, RMSE is root-mean-square error, and *r* is Pearson correlation coefficient—N indicates that *r* is not significantly different from 0 at 5% significance level based on *t* test.

 $\text{NMB} = \frac{1}{n} \sum_{i=1}^{n} (\hat{y}_i - y_i) / \overline{y}$

$$\text{RMSE} = \sqrt{\frac{1}{n} \sum_{i=1}^{n} (\widehat{y}_i - y_i)^2}$$

where $y_i, \hat{y}_i, \overline{y}$ are observed, predicted, and mean emission factor (g/kg); *n* is number of observations.

NMAE = $\frac{1}{n}\sum_{i=1}^{n} |\widehat{y}_i - y_i| / \overline{y}$

the first principal component (not shown), which decreased the amount of variability that the linear trend would account for thus reducing its predictive ability. Recall that the clr-variance for HCl was nearly 25% of the total variance. The fitted values of HCL by both the linear trend and the linear regression were relatively constant (Figure 1). The $RMSE_{CLT}$ ranged from 0.426 to 0.511 for the three starting points which was much smaller than $RMSE_{LR}$ (2.658). It is important to note that because compositional data are restricted to the positive upper orthant, predictions from the linear regression in Figure 1 are the fitted values, not predictions made outside the range of the data. The fitted linear regressions for 6 of the 18 gases produced values below zero. Scatterplots for all 18 gases are available in the supporting information. Generally, the CLT performed equal to or superior to the LR based on MCE. This coupled with the fact that the compositional nature of emissions data were analyzed using techniques appropriate to the type of data indicates the value of this analytical approach.

The data set used to demonstrate this technique was one that was readily available to the authors. There are several compilations of emission factor data that could be used to explore if smoke composition changes linearly as efficiency of a fire changes (Akagi et al., 2011; Lincoln et al., 2014; Yokelson et al., 2013). If a linear trend can be successfully fit for a larger data set producing better goodness of fit measures, such a linear trend could be used to reliably estimate emissions of gases not typically measured if the log-ratio variance of the parts is relatively low.



Table 5

Measures of Goodness of Fit^a of Estimates for the Low MCE Compositional Linear Trend (CLT) and Linear Regression (LR) With Observed Smoke Emissions From Wildland Fire

	NM	IAE	NMB	RM	SE	r	
	CLT	LR	CLT	CLT	LR	CLT	LR
CO ₂	0.01		0.00	16.65		0.98	
СО	0.20		0.04	16.26		0.78	
CH ₄	0.30	0.30	-0.04	0.68	0.66	0.79	0.80
C_2H_2	0.53	0.55	-0.24	0.15	0.14	0.12^{N}	0.35
C_2H_4	0.37	0.34	-0.19	0.42	0.39	0.58	0.59
C ₃ H ₆	0.41	0.45	-0.26	0.14	0.12	0.74	0.69
CH ₃ OH	0.27	0.41	-0.12	0.23	0.26	0.92	0.86
НСООН	0.28	0.55	-0.11	0.06	0.08	0.92	0.81
CH ₃ COOH	0.34	0.50	-0.21	0.66	0.70	0.87	0.76
НСНО	0.26	0.42	-0.07	0.24	0.30	0.91	0.85
C_4H_4O	0.23	0.52	0.02	0.03	0.06	0.96	0.84
NH ₃	0.33	0.32	-0.12	0.27	0.25	0.43	0.47
NO	0.16	0.15	-0.01	0.47	0.45	0.18^{N}	0.35
NO ₂	0.37	0.31	-0.17	0.39	0.31	-0.43	0.24^{N}
HONO	0.35	0.41	-0.16	0.14	0.14	0.58	0.34
HCN	0.36	0.51	-0.14	0.08	0.09	0.92	0.83
HCl	0.77	0.82	-0.47	0.14	0.13	-0.32	0.04^{N}
SO ₂	0.20	0.21	-0.01	0.20	0.21	0.75	0.73
Mean	0.26	0.30	-0.13	0.33	0.33		

^aNMB is normalized mean bias, NMAE is normalized mean average error, RMSE is root-mean-square error, and *r* is Pearson correlation coefficient—N indicates that *r* is not significantly different from 0 at probability = 0.05 based on Student's *t* test.

$$NMB = \frac{1}{n_{i=1}^{n}} (\widehat{y}_i - y_i) / \overline{y} \qquad NMAE = \frac{1}{n_{i=1}^{n}} |\widehat{y}_i - y_i| / \overline{y} \qquad RMSE = \sqrt{\frac{1}{n_{i=1}^{n}}} (\widehat{y}_i - y_i)^2$$

where y_i, \hat{y}_i, \bar{y} are observed, predicted, and mean emission factor (g/kg); *n* is number of observations. Mean value of NMAE calculated as geometric mean, mean RMSE calculated square root of mean of squared RMSE.

3.3. Testing the Effects of Fuel Type on Compositional Data

In the original report (Burling et al., 2010), effects of fuel type on subsets of the emissions were inferred from bar plots and error bars, but no formal hypothesis testing was presented. The fuel types were representative of major local vegetation types in the southwestern and southeastern United States. The pine litter fuel type was the sole type composed of only dead pine needles (*Pinus* spp.) and branches. All other fuel types included live foliage and branches in addition to dead fuels. In the present study compositional Balances 1 to 7 were designed to test meaningful observations reported in Burling et al. (2010), whereas balances 8 and 17 were necessary to obtain the full projection of the compositions from the simplex into real-valued ilr coordinates but are not defined according to any particular scientific relevance (see supporting information). The intercept term, which is the mean for the 1-year rough fuel type due to ANOVA parameterization, was statistically significant for 5 of the 7 balances of interest (Table 6). For the significant intercepts, a positive value indicated that the numerator of the balance was on average relatively larger than the denominator, while a negative value indicated it was relatively smaller.

For example, there was relatively less N compared to the other compounds (hydrocarbons, C oxides, etc.; Balance 1) but relatively more NOx than other N compounds (Balance 2) for the 1-year rough fuel type. The estimated effect for a fuel type is the sum of the intercept and the fuel type value. Thus, the estimate of Balance 1 for pine litter was -2.02 (-1.18 + -0.84); because the fuel type value was significant, the composition of the emissions for pine litter had relatively even less N compared to other compounds; similarly, the oak savanna and woodland fuel types had relatively more N compared to other compounds since the balance estimate was close to -0.2 for these fuels. For Balance 1, the relative amount of N versus the other compounds for the other fuel types was not significantly different from the 1 year rough. In addition to the





Figure 1. Comparison of observed emission factors (EF) for several wildland fire gases with fitted EF from a compositional linear trend (CLT) and a linear regression (LR) using modified combustion efficiency as the predictor variable.

smoke containing relatively more NOx compared to the other N compounds (Balance 2 intercept), eight of the southwestern fuel types had relatively more NO_x compared to other N compounds than five of the six southeastern fuel types. Not surprisingly, there were relatively more C oxides than organic C compounds (Balance 5). We observed CH₄ in relatively higher quantities compared to the nonmethane organic compounds (balance 6). While overall NMHC and OVOC relative abundances were statistically comparable for the 1-year fuel type (Balance 7 is not significantly different from zero), a significant negative difference with respect to this baseline was concluded for seven of the other fuel types, suggesting that relatively more OVOC compared to NMHC was observed on average for those fuel types. The relative amount of NH_3 to NO_x (Balance 3) did not differ significantly between all fuel types except

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Tab Sign	le 6 ificance of Estimated Fuel	l Type Coeff	ficients fo	r Compositi	onal Balance	es (ilr Coord	linates) of	Smoke Emi	ssions Fro	ım Wildlan	d Fire					
8	Balance	Intercept (1-year rough) ^a	2-year rough	California sagebrush	Ceanothus	Chamise/ scrub oak	Coastal sage scrub	Chipped understory hardwood	Pine litter 1	Manzanita	Maritime chaparral	Masticated mesquite	Oak savanna	0ak woodland	l Pocosin	Jnderstory hardwood
1	N versus other	-1.18^{*}	0.12	-0.08	0.25	0.02	-0.01	0.08	-0.84*	0.15	0.10	0.52	0.97*	0.99^{*}	-0.39	0.39
7	NO _x versus other N	1.17^{*}	0.02	0.48	1.06^{*}	0.70*	0.58*	0.99*	-0.20	1.22^{*}	0.68*	1.01^{*}	1.61^{*}	0.88^{*}	0.53	0.50
3	NH ₃ versus NO _{x}	-0.34	-0.04	0.08	-0.55	-0.44	-0.11	-0.43	0.09	-0.55	0.02	-0.26	-0.94^{*}	-0.23	-0.45	-0.39
4	HCl and SO ₂ versus C	-3.61^{*}	0.59	2.51*	2.10^{*}	0.79	1.96^{*}	1.80^{*}	0.89	2.67*	2.97*	2.26*	0.86	0.15	1.94^{*}	0.42
ŝ	C oxide versus OC	8.17*	0.01	1.01^{*}	1.10^{*}	0.83*	1.34^{*}	1.57^{*}	-0.23	1.83^{*}	1.20^{*}	1.25^{*}	1.75^{*}	1.30^{*}	0.44	0.59
9	CH ₄ versus NMOC	1.65^{*}	0.04	0.42*	-0.01	-0.02	0.58*	0.77*	-0.14	0.09	0.55^{*}	0.63*	0.27	0.35*	-0.15	-0.14
4	NMHC versus OVOC	0.40	-0.90	0.39	-0.97^{*}	-0.74^{*}	0.55*	-0.27	-1.90^{*}	-0.48	0.37	-0.47	-0.95^{*}	-0.06	-1.64^{*}	-1.27*
~	Alkene versus alkyne	1.08^{*}	-0.06	-0.26	-0.18	0.03	-0.23	-0.11	0.05	-0.16	-0.12	0.00	0.04	-0.02	-0.06	-0.04
6	Furan versus OVOC	-1.80^{*}	0.07	0.54^{*}	0.38	0.45*	0.44*	0.57*	0.74^{*}	0.96*	0.67^{*}	0.24	0.59*	0.70*	0.20	0.37
10	Formaldehyde versus OVOC	0.44*	-0.28	-0.02	-0.15	-0.08	0.07	-0.05	-0.17	-0.01	0.04	-0.18	-0.37*	-0.17	-0.22	-0.12
11	HCl versus SO ₂	-2.99^{*}	0.28	1.84^{*}	2.12*	0.78	1.28^{*}	1.52^{*}	0.96	2.05*	2.52*	1.37^{*}	-0.61	-0.90	1.82^{*}	-0.08
12	NO versus NO_2	0.48^{*}	-0.04	0.57*	0.17	0.48*	0.70*	0.08	0.07	0.54^{*}	0.50^{*}	0.37*	0.65*	0.76*	-0.59^{*}	0.04
13	CH3 versus HCOOH	1.47^{*}	0.12	0:30	-0.13	0.07	0.26	0.28	0.02	-0.03	0.46	0.37	-0.08	0.27	-0.10	0.12
14	CH ₃ COOH versus CH ₃ OH	-0.53*	-0.06	0.24*	-0.04	0.07	0.20	0.25*	0.11	0.05	0.18	0.25*	-0.19	0.11	-0.28*	-0.11
15	HONO versus HCN	0.70^{*}	-0.38	0.19	0.62^{*}	0.73*	0.05	0.19	-1.40^{*}	0.48^{*}	-0.12	-0.13	0.82^{*}	0.30	0.30	0.35
16	CO versus CO ₂	-2.20^{*}	0.08	-0.11	-0.15	-0.05	-0.07^{*}	-0.34*	0.37	-0.16^{*}	-0.22^{*}	-0.25^{*}	-0.59^{*}	-0.46^{*}	-0.24^{*}	-0.26^{*}
17	Acetylene versus Propene	-0.18	-0.40	0.60	0.19	-0.33*	1.14	-0.18	-0.70	0.52	-0.11	0.10	0.11	-0.30	-0.18	-0.24*
^a Sta betv inte	ndard ANOVA paramete veen the fuel type mean <i>a</i> rest; light gray shading w	rization on und the inte ith italic fo	balance srcept (1- nt denote	ilr coordina year fuel me es the other	tes—the int ean). *p va balances. Pr	ercept term lue < 0.05. provide the second	estimates Significan alues adju	the mean of difference sted to cont	of the 1-ye s are show rol for fal	ear rough fi wn in gray se discover	uel type and text. Dark g y rate.	l the value s ray shading	hown for t with regul	he other t lar font de	ypes is the notes the t	difference valances of



for the oak savanna fuel type. The overall amounts of HCl and SO_2 observed were much smaller in comparison to the quantities of C compounds (Balance 4); however, eight of the fuel types significantly reduced this difference in relative amounts.

4. Conclusions

Smoke emissions data are inherently multivariate and relative in nature. While this has been recognized for many years, the statistical techniques commonly used to analyze the data ignore these features. This applies not only to the composition of the emissions but also to the different fuel types, which burn to produce the emissions. Since emissions and fuel composition represent parts of a whole, the measured values of the individual parts (elements, chemical species, fuel component, etc.) are intrinsically not independent from each other. The measured values are relative and are only meaningful in relation to each other. Such constraints violate many of the underlying assumptions of ordinary statistical methods. Alternatively, compositional data analysis as a well-developed body of statistical methodology provides models and methods equivalent to traditional ones yet accounts for these special constraining features of relative data. The approach has been used for decades to analyze analogous types of data in the geosciences (Buccianti et al., 2006) and, more recently, in other disparate areas such as molecular biology to analyze sequencing data (Quinn et al., 2018) or physical activity epidemiology for the analysis of daily time-use patterns (Chastin et al., 2015; McGregor et al., 2019). While the statistical theory may be unfamiliar and not typically taught in most statistics courses, recent publications and software have made the use of these techniques both feasible and accessible.

The expression of emissions data as ratio data has long been reported. Even in this early work, conversion of the composition of emissions between different units by simple multiplication was presented, reinforcing the idea that emissions data form an equivalence class. Transformation of data using the arc-sine and square root transformations for count data to enable use of the normal distribution or to stabilize variance in linear regression and the log-odds transformation used in logistic regression are familiar statistical techniques routinely used in the atmospheric sciences and other fields. Linear transformation of data is used to code data to simplify analysis for a variety of statistical calculations. The compositional data approach based on log-ratio coordinates essentially maps the data onto the ordinary real space so that familiar statistical techniques can be appropriately applied. This approach matches analysis techniques to the data type thus reducing the possibility of the reporting of spurious results that may or may not reflect the underlying relationships.

The linear regression approach as it has been typically applied uses one portion of the composition (expressed as MCE) to predict other parts of the composition, which ignores the intrinsic interplay between smoke emissions and can produce predictions beyond the domain of their possible values, for example, negative values. The compositional data analysis approach recognizes the inherently positive-valued nature of the data thus eliminating the need for an analyst to ignore or discount when a fitted model produces negative values. Robust methods have been developed to allow inclusion of parts of a composition that are known to exist but fall below detection limits thus permitting a more complete analysis. We have illustrated how the use of a compositional linear trend to describe changes in the composition of smoke emissions as CE changed yielded predicted emission factors with error (difference between observed and predicted) comparable to and, in some cases, superior to predictions from linear regression models that used MCE as a predictor variable. Moreover, the use of compositional balances to form log-ratios contrasting subsets of parts of interest enabled the use of analysis of variance and hypothesis testing to examine differences in meaningful trade-offs between smoke components with more formal rigor than was previously presented by respecting the very relative nature of the data as derived from underlying natural laws like conservation of mass. We have definitively shown that fuel type affected several different ratios of groups of emissions and are assured that the results are not an artifact of the analysis which can then be used to make various inferences and decisions. Near the end of the article by Burling et al. (2010), there is discussion and hypothesis formation about the impacts of wildland fuel management activities and influence of ocean proximity on the composition of observed emissions. These impacts and hypotheses could be rigorously tested with the techniques presented here. More complex analyses of log-ratios of gas pairs or groupings as functions of external fire behavior variables such fire intensity (heat release rate) and flame residence time are possible. More



rigorous time series and spatial analysis to examine aging smoke composition within the smoke plume and in response to atmospheric processes are possible with compositional data. It is our view and recommendation that future analysis of the composition of smoke emissions and other mixtures of atmospheric pollutants as well as general atmospheric composition should consider the use of compositional data analysis methods to provide more statistically rigorous and consistent results.

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