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Authors

Bleem, LE

Crawford, TM

Ansarinejad, B

et al.

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CMB/kSZ and Compton- γ Maps from 2500 deg² of SPT-SZ and Planck Survey Data

L. E. Bleem^{1,2}, T. M. Crawford^{2,3}, B. Ansarinejad⁴, B. A. Benson^{2,3,5}, S. Bocquet^{6,7}, J. E. Carlstrom^{1,2,3,8,9}, C. L. Chang^{1,2,3}, R. Chown¹⁰, A. T. Crites^{2,3,11}, T. de Haan^{12,13}, M. A. Dobbs^{14,15}, W. B. Everett¹⁶, E. M. George^{13,17}, R. Gualtieri¹, N. W. Halverson^{16,18}, G. P. Holder^{19,20}, W. L. Holzapfel¹³, J. D. Hrubes²¹, L. Knox²², A. T. Lee^{13,23}, D. Luong-Van²¹, D. P. Marrone²⁴, J. J. McMahon^{2,3,8,9}, S. S. Meyer^{2,3,8,9}, M. Millea¹³, L. M. Mocanu^{2,3}, J. J. Mohr^{6,7,25}, T. Natoli^{2,3}, Y. Omori^{2,3,26,27}, S. Padin^{2,3,28}, C. Pryke²⁹, S. Raghunathan^{30,31}, C. L. Reichardt⁴, J. E. Ruhl³², K. K. Schaffer^{2,9,33}, E. Shirokoff^{2,3,13}, Z. Staniszewski^{32,34}, A. A. Stark³⁵, J. D. Vieira^{19,20}, and R. Williamson^{2,3,34}

¹ High Energy Physics Division, Argonne National Laboratory, Argonne, IL 60439, USA; bleem@anl.gov

² Kavli Institute for Cosmological Physics, University of Chicago, Chicago, IL 60637, USA

³ Department of Astronomy and Astrophysics, University of Chicago, Chicago, IL 60637, USA

⁴ School of Physics, University of Melbourne, Parkville, VIC 3010, Australia

⁵ Fermi National Accelerator Laboratory, MS209, P.O. Box 500, Batavia, IL 60510, USA

⁶ Faculty of Physics, Ludwig-Maximilians-Universität, D-81679 München, Germany

⁷ Excellence Cluster ORIGINS, Boltzmannstr. 2, D-85748 Garching, Germany

⁸ Department of Physics, University of Chicago, Chicago, IL 60637, USA

⁹ Enrico Fermi Institute, University of Chicago, Chicago, IL 60637, USA

¹⁰ Department of Physics and Astronomy, McMaster University, 1280 Main Street W., Hamilton, ON L8S 4L8, Canada

¹¹ Department of Astronomy & Astrophysics, University of Toronto, 50 St George Street, Toronto, ON, M5S 3H4, Canada

¹² High Energy Accelerator Research Organization (KEK), Tsukuba, Ibaraki 305-0801, Japan

¹³ Department of Physics, University of California, Berkeley, CA 94720, USA

¹⁴ Department of Physics and McGill Space Institute, McGill University, Montreal, QC H3A 2T8, Canada

¹⁵ Canadian Institute for Advanced Research, CIFAR Program in Cosmology and Gravity, Toronto, ON, M5G 1Z8, Canada

¹⁶ Center for Astrophysics and Space Astronomy, Department of Astrophysical and Planetary Sciences, University of Colorado, Boulder, CO 80309, USA

¹⁷ European Southern Observatory, Karl-Schwarzschild-Straße 2, D-85748 Garching, Germany

¹⁸ Department of Physics, University of Colorado, Boulder, CO 80309, USA

¹⁹ Astronomy Department, University of Illinois at Urbana-Champaign, 1002 W. Green Street, Urbana, IL 61801, USA

²⁰ Department of Physics, University of Illinois Urbana-Champaign, 1110 W. Green Street, Urbana, IL 61801, USA

²¹ University of Chicago, Chicago, IL 60637, USA

²² Department of Physics and Astronomy, University of California, Davis, CA 95616, USA

²³ Physics Division, Lawrence Berkeley National Laboratory, Berkeley, CA 94720, USA

²⁴ Steward Observatory, University of Arizona, 933 N. Cherry Avenue, Tucson, AZ 85721, USA

²⁵ Max-Planck-Institut für extraterrestrische Physik, D-85748 Garching, Germany

²⁶ Kavli Institute for Particle Astrophysics and Cosmology, Stanford University, 452 Lomita Mall, Stanford, CA 94305, USA

²⁷ Department of Physics, Stanford University, 382 Via Pueblo Mall, Stanford, CA 94305, USA

²⁸ California Institute of Technology, Pasadena, CA 91125, USA

²⁹ Department of Physics, University of Minnesota, Minneapolis, MN 55455, USA

³⁰ Department of Physics and Astronomy, University of California, Los Angeles, CA 90095, USA

³¹ Department of Physics and Astronomy, Michigan State University, East Lansing, MI 48824, USA

³² Physics Department, Center for Education and Research in Cosmology and Astrophysics, Case Western Reserve University, Cleveland, OH 44106, USA

³³ Liberal Arts Department, School of the Art Institute of Chicago, Chicago, IL 60603, USA

³⁴ Jet Propulsion Laboratory, California Institute of Technology, Pasadena, CA 91109, USA

³⁵ Center for Astrophysics | Harvard & Smithsonian, 60 Garden Street, Cambridge, MA 02138, USA

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Abstract

We present component-separated maps of the primary cosmic microwave background/kinematic Sunyaev–Zel’dovich (SZ) amplitude and the thermal SZ Compton- γ parameter, created using data from the South Pole Telescope (SPT) and the Planck satellite. These maps, which cover the ~ 2500 deg² of the southern sky imaged by the SPT-SZ survey, represent a significant improvement over previous such products available in this region by virtue of their higher angular resolution (1/25 for our highest-resolution Compton- γ maps) and lower noise at small angular scales. In this work we detail the construction of these maps using linear combination techniques, including our method for limiting the correlation of our lowest-noise Compton- γ map products with the cosmic infrared background. We perform a range of validation tests on these data products to test our sky modeling and combination algorithms, and we find good performance in all of these tests. Recognizing the potential utility of these data products for a wide range of astrophysical and cosmological analyses, including studies of the gas properties of galaxies, groups, and clusters, we make these products publicly available at http://pole.uchicago.edu/public/data/sptsz_ymap and on the NASA/LAMBDA website.

Unified Astronomy Thesaurus concepts: Cosmic background radiation (317); Large-scale structure of the universe (902); Galaxy clusters (584)



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1. Introduction

Modern arcminute-scale resolution experiments such as the Atacama Cosmology Telescope (ACT; Swetz et al. 2011),

Planck (Planck Collaboration et al. 2011a), and the South Pole Telescope (SPT; Carlstrom et al. 2011) have been used to make exquisite temperature and polarization maps of the millimeter-wave sky. While the dominant signal in these observations arises from the primary cosmic microwave background (CMB), there is a wealth of additional information encoded in these maps, tracing both the interactions of CMB photons with matter along the line of sight (e.g., CMB secondary anisotropies; see the review by Aghanim et al. 2008), as well as the emission from objects between us and the surface of last scattering. The latter emission is dominated at short wavelengths by the cosmic infrared background (CIB; e.g., Dunkley et al. 2011; Thacker et al. 2013; Viero et al. 2013; Mak et al. 2017; Reichardt et al. 2021 and see Kashlinsky et al. 2018 for a recent review) and at longer wavelengths by synchrotron radiation, primarily from active galactic nuclei (see, e.g., De Zotti et al. 2010; Everett et al. 2020; Gralla et al. 2020).

In this work, we focus on isolating signals from the CMB itself as well as two of the secondary CMB anisotropies: the kinematic and thermal Sunyaev–Zel’dovich (kSZ and tSZ) effects. The kSZ and tSZ effects arise, respectively, from the first-order (Sunyaev & Zel’dovich 1972; Sunyaev & Zeldovich 1980) and second-order terms (Sunyaev & Zel’dovich 1970, 1972) in the equations governing the scattering of CMB photons off moving electrons such as are found in galaxies, groups, and clusters (see, e.g., Birkinshaw 1999; Carlstrom et al. 2002 for a more detailed review). All three of these signals offer powerful probes of cosmology, with the tSZ and kSZ additionally probing a range of astrophysical processes.

The CMB is, of course, one of the observational pillars of modern cosmology, with decades of observations having led to robust evidence for a spatially flat universe that arose from a hot Big Bang and whose composition and evolution today is governed primarily by dark energy and dark matter (e.g., Mather et al. 1994; Hinshaw et al. 2013; Henning et al. 2018; Planck Collaboration et al. 2020a; Adachi et al. 2020; Aiola et al. 2020). Observations of the SZ effects complement this picture by providing probes of the universe at later times, particularly from the epoch of reionization to the present day. The tSZ effect, sourced primarily by the inverse Compton scattering of CMB photons off the hot gas in galaxy groups and clusters (Battaglia et al. 2012; Bhattacharya et al. 2012), enables the compilation of mass-limited cluster samples out to the epoch of cluster formation (e.g., Bleem et al. 2015b; Planck Collaboration et al. 2016a; Huang et al. 2020; Bleem et al. 2020; Hilton et al. 2021). These samples, through growth of structure tests, have been used to provide cosmological constraints competitive with those from CMB and galaxy surveys (Planck Collaboration et al. 2016b; Hasselfield et al. 2013; Bocquet et al. 2019). The tSZ power spectrum, bispectrum, and related observables are also highly sensitive to cosmology (e.g., Komatsu & Seljak 2002; Bhattacharya et al. 2012; Hill & Sherwin 2013; Crawford et al. 2014; George et al. 2015; Horowitz & Seljak 2017; Coulton et al. 2018). Finally, the kSZ effect, while the faintest and thus far least characterized of these three observational probes, offers unique opportunities to explore the reionization history of the universe (Gruzinov & Hu 1998; Shaw et al. 2012; Park et al. 2013; Battaglia et al. 2013; Smith & Ferraro 2017; Reichardt et al. 2021) including a new pathway to constraining the optical depth to reionization, τ (Ferraro & Smith 2018). In combination with next-generation galaxy surveys—e.g., the Dark Energy Spectroscopic Instrument (DESI Collaboration et al. 2016), Euclid

(Amendola et al. 2018), SPHEREx (Doré et al. 2014), the Vera Rubin Observatory’s Legacy Survey of Space and Time (LSST; LSST Science Collaboration et al. 2009), and the Roman Space Telescope (Spergel et al. 2015)—it will also lead to new probes of gravity and dark energy (Bhattacharya & Kosowsky 2008; Keisler & Schmidt 2013; Mueller et al. 2015a), massive neutrinos (Mueller et al. 2015b), and other physics that influences the growth of structure (Bhattacharya & Kosowsky 2007; Sugiyama et al. 2017; Soergel et al. 2018).

Observations of the SZ effects also can be used to constrain astrophysical processes. The redshift-independent nature of these signals makes them highly complementary to other physical probes both alone (CMB-S4 Collaboration et al. 2019), and in combination with other observables (Siegel et al. 2018; Shitanishi et al. 2018; Ruppin et al. 2021; Okabe et al. 2021). In recent work, these signals have been used to provide insight into the “missing baryon” problem (e.g., Tanimura et al. 2019; de Graaff et al. 2019) by tracing the hot gas in filaments between massive galaxies, as well as to constrain astrophysical feedback and the thermal properties of both aggregate samples of galaxies (e.g., Soergel et al. 2016; De Bernardis et al. 2017; Amodeo et al. 2021; Chaves-Montero et al. 2021; Schaan et al. 2021; Vavagiakis et al. 2021) and in high signal-to-noise measurements of individual clusters (Plagge et al. 2010; Planck Collaboration et al. 2012; Romero et al. 2017; Ruppin et al. 2018).

Given the power of these sky signals to probe such a diverse and important range of scientific questions, there has been significant effort in developing techniques to isolate these signals into single-component maps (see, e.g., Remazeilles et al. 2011a, 2011b; Hurier et al. 2013; Bobin et al. 2016; Petroff et al. 2020; Sultan et al. 2021, among many works). In an idealized scenario, such maps would consist only of the desired observables of interest. However, the realities of noise, wavelength coverage (particularly restricted in ground-based observations by available atmospheric windows), limited knowledge of the spectral energy distributions (SEDs) of the various sky components (Tegmark 1998) and/or incomplete differentiability between them, and the finite angular and spectral resolution of the available data all limit the fidelity of the signal map reconstructions. Such limitations typically necessitate tradeoffs between noise and signal purity in the reconstructed component maps.

To optimize the use of available data, a number of works have focused on improving upon the component maps produced using data from Planck (e.g., Planck Collaboration et al. 2016c, 2016d, 2020b; Lenz et al. 2019) by combining data from ground-based experiments with those from Planck to leverage the higher angular resolution of the terrestrial experiments and the superior noise performance and frequency coverage of Planck at large angular scales. An early example of this was Crawford et al. (2016), in which data from Planck were combined with SPT observations to produce arcminute-scale emission maps of the Large and Small Magellanic Clouds for a range of emission spectra. Aghanim et al. (2019) combined Planck data with 148 and 220 GHz ACT data from the 2008–2010 seasons (Swetz et al. 2011; Dünner et al. 2013) to construct a 1.5 resolution tSZ component map using internal linear combination (ILC) techniques. More recently, Madhavacheril et al. (2020) used ILC techniques to construct 1.6 maps of both the tSZ and CMB/kSZ (including a variant of the latter from a “constrained” ILC where the tSZ was nulled) from Planck and 2100 deg² of 98 and 150 GHz data from the 2014–2015 ACTPol observing seasons, and Melin et al. (2021) combined data from a public SPT-SZ

release (Chown et al. 2018) with those from Planck to produce a joint Planck +SPT cluster sample using matched-filter techniques.

In this work we describe the construction and public release of a series of maps constructed through the combination of data from the Planck mission with those from the 2500 deg² SPT-SZ Survey (Story et al. 2013). These products include component maps of the tSZ and the CMB/kSZ useful for cluster detection and for cross-correlation analyses in which bias from foregrounds is expected to be minimal, as well as component maps where various contaminating sky signals have been significantly reduced or removed that are more optimal for, e.g., CMB lensing reconstruction (van Engelen et al. 2014; Osborne et al. 2014; Madhavacheril & Hill 2018) or other analyses in which the contaminating components could create significant biases in the quantities of interest. We also provide with this release the 95, 150, and 220 GHz SPT-SZ maps used in this work. Similar to the maps used in the production of the SPT-SZ cluster sample (Bleem et al. 2015b), these maps are both slightly deeper and have higher resolution than the maps presented in Chown et al. (2018), which conservatively used maps subject to the more stringent cuts from SPT power spectrum analyses (e.g., George et al. 2015) and were further degraded to 1'75 resolution.

This work is organized as follows. In Section 2 we describe the data used to construct and validate the component-map products. In Section 3 we detail the process by which we construct the component maps and in Section 4 we describe the resulting products. In Section 5 we describe the results of several validation tests of the maps. Finally, in Section 6 we summarize and conclude. All public data products in this paper are available on the SPT page of the NASA/LAMBDA website³⁶ and on the public SPT website.³⁷

2. Data and Processing

The Compton- y parameter and CMB/kSZ maps presented in this work are constructed using data from two surveys: the 2500 deg² SPT-SZ survey and the Planck all-sky survey, as represented in the 2015 Planck data release.³⁸ The SPT and Planck data play highly complementary roles in this work: data from the SPT have higher resolution and lower noise at small scales, while the Planck data have lower noise at larger scales (multipole $\ell \lesssim 1700$) as well as enhanced frequency coverage. Additional data from the HI4PI survey (HI4PI Collaboration et al. 2016) and the Herschel Space Observatory SPIRE instrument (Pilbratt et al. 2010; Griffin et al. 2003) were used to perform systematic checks of the map products. In this section we summarize these data and their processing as relevant to the component-map construction.

2.1. The South Pole Telescope SZ Survey

The South Pole Telescope (Carlstrom et al. 2011) is a 10 m telescope located approximately 1 km from the geographic

South Pole at the National Science Foundation Amundsen–Scott South Pole Station in Antarctica. To date, three different generations of instruments have been deployed on the telescope to conduct arcminute-scale observations of the millimeter-wave sky; the data used in this work were obtained between 2008 and 2011 with the SPT-SZ receiver. This receiver was composed of six subarrays (or “wedges”) of feedhorn-coupled transition-edge bolometer sensors, with each wedge sensitive at either 95, 150, or 220 GHz. The resulting SPT-SZ survey covers a ~ 2500 deg² region extending from 20^h to 7^h in R.A. and -65° to -40° in decl.; the full-survey footprint was subdivided and observed in 19 separate fields ranging from ~ 70 to 250 deg² in size (Story et al. 2013). Data were acquired by scanning the telescope back and forth across each field in azimuth and then stepping in elevation, and then repeating the scan and step procedure until each field had been completely covered. One field, centered at R.A. = 21^h, decl. = -50° , was observed in two different modes, with approximately one-third of the data obtained in the azimuth-scanning mode described above, while the remainder was obtained in an analogous process by scanning the telescope in elevation and then stepping in azimuth. One complete pass of a field, lasting roughly two hours on average, is termed an observation, and each field was observed at least 200 times. Two fields, the ra23h30dec-55 and ra5h30dec-55 fields, were observed for roughly twice the total time as the rest of the fields and, as a result, have roughly $\sqrt{2}$ lower noise.

2.1.1. Map Making

The general procedure for converting SPT observation data into field maps is presented in Schaffer et al. (2011); we briefly summarize the process here. Maps are constructed from time-ordered bolometer data acquired during each scan across the field. Each detector’s data are processed to remove sensitivity to the receiver’s pulse tube cooler, cuts are applied based on both noise properties and responsiveness to sources, the data are rescaled based on the detector’s response to an internal calibration source embedded in the telescope’s secondary cryostat, and the data are filtered and binned into map pixels with inverse-variance weighting.

Filtering of time-ordered bolometer data consists of both an effective high-pass filter that reduces sensitivity to atmospheric noise and a low-pass filter that prevents the aliasing of high-frequency noise when the detector data are binned into map pixels. For every scan across the field, a low-order polynomial is fit and subtracted from each detector’s time-stream data, with the order of the polynomial scaled to the length of the scan (roughly three modes per 10 degrees of scan for this work). The effective ℓ -space cutoff of this filter is roughly $\ell = 50$ in the scan direction. For the 220 GHz data, which are more sensitive to large-scale atmospheric fluctuations, we also fit and subtract sines and cosines up to a frequency equivalent to $\ell = 200$ in the scan direction. At each time sample in the observation, an isotropic common-mode filter is applied to data from each wedge. At 95 GHz, this common-mode filter takes the form of subtracting the mean of all the detectors on the wedge from the time streams, while at 150 and 220 GHz, where the low-frequency atmospheric noise is more of an issue, two spatial gradients across the wedge are also subtracted from each detector’s data. Finally, the data are low-pass filtered with a cutoff at angular multipole $\ell \sim 20,000$.

³⁶ https://lambda.gsfc.nasa.gov/product/spt/spt_prod_table.cfm

³⁷ http://pole.uchicago.edu/public/data/sptsz_ymap

³⁸ In this work we make use of a number of temperature foreground products for which the Planck Legacy Archive (https://wiki.cosmos.esa.int/planck-legacy-archive/index.php/Foreground_maps#2018_Astrophysical_Components) recommends using products from the 2015 release. As such, we choose to make use of the 2015 maps in this work to ensure consistency in our analysis and note, given the updates detailed in Planck Collaboration et al. (2020c), we expect minimal impact on analyses for which these maps will be most useful.

In typical SPT analyses, to avoid introducing filtering artifacts around bright sources, sources brighter than a certain threshold are masked during filtering. In this work, because we combine SPT-SZ maps with Planck data on a Fourier-mode-by-Fourier-mode basis, we do not need to mask sources in the filtering steps that predominantly affect modes that can be filled in by Planck. This includes the common-mode filtering, which acts as an isotropic high-pass filter at the detector wedge scale (roughly half a degree). We do still mask sources in the polynomial subtraction (above a threshold of roughly 6 mJy at 150 GHz) because this acts as a high-pass filter in the scan direction only and affects modes that oscillate slowly in the scan direction but quickly along the cross-scan direction and are thus not accessible to the lower-resolution Planck observations. More generally, the fact that these modes are missing from both SPT-SZ and Planck data results in a small bias to the resulting Compton- γ and CMB/kSZ maps, which we discuss in Section 3.4.

Following the filtering, the telescope pointing model is used to project inverse noise-variance weighted detector data into map pixels. For this work the SPT single-frequency maps are made in the Sanson–Flamsteed projection (Calabretta & Greisen 2002) with a pixel scale of $0''.25$. Individual-observation maps are coadded with weights determined by the average detector noise performance in each observation. The coadded maps are absolutely calibrated using data from the Planck mission. This calibration results in a $\sim 0.3\%$ uncertainty on the absolute calibration of the SPT data; see Hou et al. (2018) for details on the calibration procedure. To avoid boundary effects in the map combination process (Section 3) we “pad” the fields by 25% in area by coadding with their neighbors and require coverage at all three SPT-SZ frequencies.³⁹ These requirements reduce the component-map areas compared to e.g., the area searched for clusters in Bleem et al. (2015b) by slightly shrinking the exterior boundary of the survey; the total area is reduced by $\sim 3\%$.

In this work, we use the same data cuts as in Bleem et al. (2015b), leading to depths in the final coadded field maps at $4000 < \ell < 5000$ of approximately 37, 16, and $65 \mu\text{K-arcmin}$ at 95, 150, and 220 GHz respectively, using the Gaussian beam approximation estimation of Schaffer et al. (2011). For a complete listing of field depths, see, e.g., Table 1 in Bleem et al. (2015b).

2.1.2. Noise PSDs

As in a number of previous SPT publications (e.g., Staniszewski et al. 2009), we use a resampling technique to estimate two-dimensional map noise power spectral densities (PSDs). In each resampling, individual observations of a given SPT-SZ field are randomly assigned a sign of ± 1 and coadded; sky signal is highly suppressed in the resulting coadded maps, and we approximate them as pure noise. We compute the PSD of each signal-free coadd, and we use the average of these jackknife PSDs to provide an estimate of instrumental and residual atmospheric noise in the filtered SPT-SZ maps.

³⁹ Owing to asymmetry in wedge locations in the SPT-SZ focal plane (Section 2.1), the 95 and 220 GHz data have slightly reduced coverage at opposite field edges.

2.1.3. Angular Response Function

The SPT-SZ sky maps created as described above are biased representations of the true sky, as the data have been modified by both the finite resolution of the instrument and the filtering processes described above. At each frequency, the instrumental response function (i.e., beam) is to first order well represented as an azimuthally symmetric Gaussian with FWHM equal to $1''.6$, $1''.1$, and $1''.0$ at 95, 150, and 220 GHz, respectively. As described in Keisler et al. (2011) and Schaffer et al. (2011), the beam of the SPT is characterized using a combination of emissive sources in the survey fields and dedicated planet observations. In the process of creating the component maps (described in Section 3), we use the azimuthally averaged Fourier-space beams $B(\ell)$.

To characterize the effect of our map filtering, we simulate the filter response function. Following Crawford et al. (2016), 100 simulated skies are constructed from white noise convolved with a $0''.75$ Gaussian beam. Each sky realization is “mock observed” to obtain detector time-stream data using the telescope pointing model. These time-ordered data are cut, weighted, and filtered in an identical process to the real data to form individual-observation maps. These individual-observation maps are combined with the same weighting as the real data to make final coadded mock-observed maps. For each sky realization the estimate of the filter response function is then determined as the ratio of the two-dimensional power spectrum of the coadded map to the known input power spectrum. The 100 independent ratios are averaged, and this averaged ratio is used as the estimate of the 2D Fourier-space filter response function. Because the filter transfer function is highly similar among all fields except the “el-scan” field (see Section 2.1), we ran the mock observations only on the el-scan field and a single standard-observation field; for the other 17 standard-observation fields we used a regridded version of the standard-field filter transfer function.

2.1.4. Bandpasses

The process of separating a component-map signal from other sky signals and noise relies on a priori knowledge of the desired signal spectrum and, by extension, knowledge of the spectral response of the instruments used to collect the data. The bandpasses of the SPT-SZ detectors were characterized using a Fourier transform spectrometer. Spectra were measured for $\sim 50\%$ of all bolometers on each wedge and, as the spectra were found to be highly uniform (the bandpasses of the SPT-SZ detectors are set by a low-pass metal-mesh filter covering each wedge and a high-pass filter from the waveguide cutoff frequency of precision-machined feedhorns), a weighted-average spectrum for each frequency was computed. Weights were set by the inverse square of each detector’s noise-equivalent temperature.

As the SPT-SZ bands are not infinitely narrow, the response to signals with different SEDs cannot be characterized by a single center frequency. We follow, e.g., Reichardt et al. (2021) and calculate an effective band center for every sky component in the signal model (see Section 3). We define the effective band center for a given source spectrum as the frequency at which the conversion between CMB fluctuation temperature and intensity is equal to the value integrated over the true SPT-SZ bands, weighted by the source spectrum. For a thermal SZ

spectrum, this leads to effective band centers of approximately 99.6, 155.5, and 220.0 GHz for the three SPT-SZ frequencies.

Another consequence of the SPT (and Planck) bands not being infinitely narrow is that the angular response function may not be constant over the band, resulting in effective beams that are different for different SEDs. We have calculated the maximum bias expected for any of our output component maps from this effect at any value of multipole ℓ and find it to be 1.2% (with the typical value over the full ℓ range much lower), and as a consequence we ignore this effect in our analysis.

2.2. Planck

The European Space Agency’s Planck satellite was launched in 2009 with the primary mission of conducting sensitive, high-resolution observations of the CMB (Tauber et al. 2010; Planck Collaboration et al. 2011a). Full-sky maps from 25–1000 GHz were produced over the course of its multiyear mission. We make use of products from the 885 days High Frequency Instrument (HFI) cold mission that are included in the Planck 2015 public release (Planck Collaboration et al. 2016e). HFI data in the 100, 143, 217, and 353 GHz channels are used in the map-making process, and data from the 545 GHz channel are used for several systematic checks. Five surveys, each covering a large fraction of the sky, were conducted over the course of the cold HFI mission; both full- and half-mission maps produced from these surveys are used in this work.

2.2.1. Maps, Angular Response Function, Noise Treatment

For each channel the time-ordered data are converted into maps as described in Planck Collaboration et al. (2014a) and updated in Planck Collaboration et al. (2016f). As detailed in the latter work, the data are calibrated at 100–353 GHz using the time-variable CMB dipole and at 545 GHz using planetary emission from Uranus and Neptune (see also further discussion of the calibration using planets in Planck Collaboration et al. 2017). The absolute calibration of the full-mission HFI maps is determined to [0.09, 0.07, 0.16, 0.78, 1.1(+5 model uncertainty)]% accuracy at [100, 143, 217, 353, 545] GHz.

The Planck maps are processed such that the transfer function can be modeled as an “effective” beam—accounting for the telescope optics, survey scan strategy, and data processing—convolved with the map pixelization window function (Planck Collaboration et al. 2014b). We use the azimuthally symmetric “Reduced Instrument Model” (RIMO) effective beam window functions derived from the 75% of the sky outside the Galactic plane.⁴⁰ We also make use of the beam files provided in Planck Collaboration et al. (2020d) to extend the 217 and 353 GHz beam from $\ell_{\max} = 4000$ to $\ell_{\max} = 8192$. Using a Gaussian approximation the typical FWHM of these effective beams is [9.69, 7.30, 5.02, 4.94, 4.83]’ at [100, 143, 217, 353, 545] GHz (Planck Collaboration et al. 2016g). These maps are provided in HEALPix⁴¹ format (Górski et al. 2005) with $N_{\text{side}} = 2048$, corresponding to 1.7 pixels. The RIMO also provides the Planck bandpasses (Planck Collaboration et al. 2014c).

While the time-ordered Planck data are approximately “white” with a “ $1/f$ ” contribution at lower frequencies (Planck HFI Core Team et al. 2011), data processing and map

projection can introduce correlations between map pixels (Planck Collaboration et al. 2016f). In this work, as in Crawford et al. (2016), we ignore these nonidealities and model the Planck noise as white noise with levels set on a field-by-field basis. This treatment will not bias the resulting component maps and should have only a minor effect on the optimality of the band combination, as the Planck data primarily serve to fill in the large angular scale modes that have been removed or down-weighted by the SPT filtering. Noise levels are estimated using the square root of the mean of intensity–intensity variance maps in each SPT field. These noise levels typically vary by 5%–10% rms across the SPT-SZ fields (but up to 30% near the south ecliptic pole, where the Planck observation strategy results in very deep coverage). The mean Planck noise level varies by up to a factor of 2 between the SPT-SZ fields (again particularly near the ecliptic pole), but this is taken into account as both the CMB/kSZ and Compton- γ maps are constructed independently in the 19 SPT-SZ fields.

The Planck and SPT data are combined on a field-by-field basis, and then the maps constructed from individual fields are stitched together to form full SPT-SZ survey CMB/kSZ and Compton- γ maps. This field-by-field procedure enables us to more optimally combine the Planck and SPT data sets given noise variations across each survey. To match the SPT projections we first rotate the Planck maps from the Galactic to celestial coordinate system using the HEALPix `rotate_alm` function. The Planck maps are then projected using the Sanson–Flamsteed projection to match each SPT field’s pixelization.

2.3. Treatment of Bright Sources in SPT and Planck Data

While data from Planck are used to fill in missing modes at low ℓ removed during the filtering of the SPT maps (see, e.g., Sections 2.1.1 and 3.4), this compensation is incomplete for time-variable signals or when a foreground source has an SED that is very different from the SED of the desired signal component. The former effect is particularly important for bright sources (dominated by flat- or falling-spectrum blazars at the SPT wavelengths), whose flux could vary significantly between the time of the Planck and SPT observations. Both of these effects can cause a mismatch in the power in the SPT and Planck maps, resulting in artifacts in the output map. To mitigate such artifacts, we “paint in” the regions around the brightest sources in the maps. For sources detected at > 250 mJy at 150 GHz in the SPT maps (as well as six additional sources from the Planck 143 GHz source catalog (Planck Collaboration et al. 2016h) above this threshold in the Planck but not SPT data) we fill in regions of radius $20'$ around each source location in all of the maps using the mean value of the sky temperature computed from annuli extending $15'$ from the in-painting radius. We do the same for sources above 150 mJy at 150/143 GHz but with a $10'$ radius. These painted regions are masked in the provided source mask.

2.4. Herschel

We tune the Compton- γ reconstruction parameters to minimize the correlation with the CIB by using data from the Herschel Space Observatory (Pilbratt et al. 2010) SPIRE instrument (Griffin et al. 2003). The Herschel data consist of observations at 500, 300, and 250 μm that were acquired over a ~ 90 deg² patch centered at (RA, decl.) = (23^h30^m, -55°)

⁴⁰ https://wiki.cosmos.esa.int/planckpla2015/index.php/Effective_Beams

⁴¹ <http://healpix.sourceforge.net>

in the SPT-SZ survey under an Open Time program (PI: Carlstrom). In this study, we make use of the 500 μm maps. The Herschel/SPIRE angular resolution is superior to that of both SPT and Planck—the effective resolution of the 500 μm maps is $36''6$ —enabling us to test CIB contamination at small scales. Further details on these maps and their processing can be found in Holder et al. (2013).

2.5. HI4PI

To validate the removal of Galactic dust from the maps at large scales we make use of data from the HI4PI survey of neutral atomic hydrogen (HI4PI Collaboration et al. 2016). Such H I survey data has long been known to be well-correlated with infrared-to-millimeter-wavelength dust emission (e.g., Boulanger & Perault 1988; Boulanger et al. 1996; Lagache et al. 2003; Planck Collaboration et al. 2014b). The survey maps in the SPT region are from the third revision of the Galactic All Sky Survey (GASS; McClure-Griffiths et al. 2009; Kalberla et al. 2010; Kalberla & Haud 2015) which was conducted in 2005–2006 with the Parkes Radio Telescope. These maps have an angular resolution of $\text{FWHM} = 16'2$ and an rms noise temperature of approximately 43 mK. We utilize the N_{HI} column density maps provided in HEALPix format. These were constructed by integrating over the full velocity range of GASS (with absolute radial velocity $\leq 470 \text{ km s}^{-1}$). Further details on these data products can be found in HI4PI Collaboration et al. (2016).

3. Construction of the CMB/kSZ and Compton- γ Component Maps

In this work we assume the Planck and SPT temperature maps to be composed of sky signal contributions from primary CMB temperature fluctuations, tSZ, kSZ, radio galaxies, the dusty galaxies that make up the CIB, and Galactic dust; and noise contributions from the instrument and—for SPT—the atmosphere. In this section we describe the procedure for extracting an unbiased component map from individual frequency maps; the models we adopt for the instrumental, atmospheric, and astrophysical contributions to the variance in the individual maps and covariance between them; the treatment of the “missing modes” in output component maps; and our procedure for suppressing CIB contamination in the “minimum-variance” Compton- γ maps.

3.1. Linear Combination Algorithm

We use a linear combination of individual frequency maps to construct the Compton- γ map. The practice of linearly combining millimeter-wave/microwave maps to extract individual sky components is common in the CMB field, and there are many approaches (see, e.g., the review by Delabrouille & Cardoso 2009). All millimeter-wave/microwave linear combination (LC) algorithms have a common goal, namely to combine a set of single-frequency maps to produce a map with an unbiased response to a signal with a known frequency spectrum. LC algorithms also generally seek to minimize the variance in the output map from instrument noise, atmospheric fluctuations (if the data are from a ground-based experiment), and sources of astrophysical signal other than the target signal. For some applications, it is preferable to minimize the total variance in the output map, while for other applications it is preferable to explicitly null the response of the output map to one or more signals (assuming the SEDs of those signals are

known perfectly). An example of the latter type of map is a map of the CMB temperature fluctuations that has a null response to tSZ, which can be a significant contaminant to measurements of CMB lensing and the kSZ effect (e.g., Madhavacheril & Hill 2018; Baxter et al. 2019; Raghunathan et al. 2019).

Another choice that must be made in constructing the LC is how to characterize the variance in the individual frequency maps and the covariance between them. One choice is to use models of the various sources of power in the maps, including instrumental and atmospheric noise as well as astrophysical signals. The downside of this approach is that if the models are not perfect, there will be excess residual variance in the output component map(s). Another approach, referred to as “internal linear combination” or “ILC” in the literature, estimates the variance and covariance from the individual frequency maps themselves. The downside to this approach is that it results in a biased output map (e.g., Delabrouille et al. 2009). This “ILC bias” can be mitigated by averaging the covariance estimates over many real-space or Fourier-space pixels. The ILC approach with Fourier-space averaging was used to produce the ACTPol+Planck Compton- γ map in Madhavacheril et al. (2020). We choose to adopt the first approach, preferring to incur a potential noise penalty than a bias in the output map. We estimate the potential excess variance from imperfect modeling in Section 5.1.

Operationally, this approach is identical to the map combination procedure used in the construction of the SPT-SZ cluster sample (e.g., Melin et al. 2006; Bleem et al. 2015b), replacing the β -profile filter used to optimize cluster identification with a profile with a flat response as a function of ℓ . In this approach, each single-frequency map at the sky location \mathbf{n} is characterized as a sum over the various sky signal components, convolved with the appropriate beam and transfer function (see Section 2.1.3), plus instrumental—and in the case of SPT, atmospheric—noise:

$$T(\nu_i, \mathbf{n}) = R(\nu_i, \mathbf{n}) * \sum_j f_j(\nu_i) S_j(\mathbf{n}) + n_{\text{noise}}(\nu_i, \mathbf{n}), \quad (1)$$

where $R(\nu_i, \mathbf{n}) = B(\nu_i, \mathbf{n}) * F(\nu_i, \mathbf{n})$ is the convolution of the real-space beam and filter kernel, and $f_j(\nu)$ is the SED of signal S_j . We choose to work in two-dimensional Fourier space, using \mathbf{l} as the wavenumber-like Fourier conjugate of the sky location \mathbf{n} , in which case we can write Equation (1) as

$$T(\nu_i, \mathbf{l}) = R(\nu_i, \mathbf{l}) \sum_j f_j(\nu_i) S_j(\mathbf{l}) + n_{\text{noise}}(\nu_i, \mathbf{l}), \quad (2)$$

where the $R(\nu_i, \mathbf{l}) = B(\nu_i, \ell \equiv |\mathbf{l}|) F(\nu_i, \mathbf{l})$ is the product of the Fourier-space beam window function (which we approximate as azimuthally symmetric) and filter transfer function (which is manifestly anisotropic for SPT-SZ).

As shown in Melin et al. (2006) and (in an alternate derivation) in Appendix B, under the assumption that the instrumental/atmospheric and astrophysical noise models are correct, the combination of the data that yields the minimum-variance, unbiased map of signal S with SED $f(\nu)$ in two-dimensional Fourier space is

$$\bar{S}(\mathbf{l}) = \sum_i \psi(\nu_i, \mathbf{l}) T(\nu_i, \mathbf{l}), \quad (3)$$

where

$$\psi(\nu_i, \mathbf{l}) = \sigma_\psi^2(\mathbf{l}) \sum_j N_{ij}^{-1}(\mathbf{l}) f(\nu_j) R(\nu_j, \mathbf{l}) \quad (4)$$

is the weight contributed to the output map \bar{S} by band ν_i at angular frequency \mathbf{l} , $\sigma_\psi^2(\mathbf{l})$ is the predicted variance of the output map at angular frequency \mathbf{l} , given by

$$\sigma_\psi^2(\mathbf{l}) = \sum_{i,j} f(\nu_i) R(\nu_i, \mathbf{l}) N_{ij}^{-1}(\mathbf{l}) f(\nu_j) R(\nu_j, \mathbf{l}), \quad (5)$$

and $N_{ij}(\mathbf{l})$ is the two-dimensional Fourier-space version of the band–band, pixel–pixel covariance matrix, including contributions from instrumental and atmospheric noise and from sky signals other than the signal of interest. The model used to construct N is presented in Section 3.2. We normalize N so that the squared, azimuthally averaged Fourier-domain power as a function of $\ell = |\mathbf{l}|$ is equivalent to $C(\ell)$ in the flat-sky limit.

To make a map of the signal S with some other signal formally nulled, we simply replace f in the previous equations with an $N_{\text{bands}} \times N_{\text{components}}$ matrix $f_i(\nu_j)$ encoding the spectral behavior of all signals for which we desire independent output maps. The band-weighting function ψ then becomes an $N_{\text{bands}} \times N_{\text{components}}$ matrix at each two-dimensional Fourier location, and the output component maps \bar{S}_i are given by

$$\bar{S}_i(\mathbf{l}) = \sum_j \psi_i(\nu_j, \mathbf{l}) T(\nu_j, \mathbf{l}), \quad (6)$$

where

$$\psi_i(\nu_j, \mathbf{l}) = \sum_{k,m} C_{\psi,ik}(\mathbf{l}) N_{km}^{-1}(\mathbf{l}) f_j(\nu_m) R(\mathbf{l}, \nu_m) \quad (7)$$

and

$$C_{\psi,ij}^{-1}(\mathbf{l}) = \sum_{k,m} f_i(\nu_k) R(\nu_k, \mathbf{l}) N_{km}^{-1}(\mathbf{l}) f_j(\nu_m) R(\mathbf{l}, \nu_m). \quad (8)$$

We show in Appendix C that for the particular case of two components this band-weighting function is identical to Equation (3) in Madhavacheril et al. (2020), as derived in, e.g., Remazeilles et al. (2011a).

There is an important assumption implicit in this formulation, namely that the statistical behavior of the instrumental/atmospheric noise and the astrophysical contaminants does not vary across the maps. This allows the noise and contaminants to be meaningfully represented in Fourier space and (under the assumption of Gaussianity) means that the Fourier components at different frequencies are independent so that ψ can be computed independently at every value of \mathbf{l} . For many existing and upcoming data sets, particularly those covering a large fraction of the sky, these conditions are not met, and a spatially varying approach such as a needlet ILC (Delabrouille et al. 2009) must be employed. This is, however, a good approximation for the noise and foregrounds in this analysis. The noise in the SPT-SZ survey is well approximated as statistically uniform, particularly because we perform component separation in each of the 19 SPT-SZ fields individually. The SPT-SZ noise in these fields only varies slightly as a function of decl., and the Planck noise across any one of these ~ 200 deg² regions is fairly uniform as well (see Section 2.2.1).

Most of the relevant astrophysical components are both statistically isotropic across the SPT-SZ fields and Gaussian distributed, with the notable exceptions of Galactic dust and

synchrotron and individual bright emissive sources and galaxy clusters. The SPT-SZ fields are at high Galactic latitude and at the angular scales relevant for tSZ studies Galactic foregrounds are negligible in these fields—though at the very largest angular scales, Galactic dust is clearly visible in the resulting Compton- y map if we do not correct for it; see Section 3.3 for details. Meanwhile, we mask all emissive sources down to flux densities of ~ 6 mJy at 150 GHz, significantly reducing the statistical anisotropy and non-Gaussianity of that component. We note that the contribution of the tSZ to the covariance is not actually relevant to this work, because, in all of our output maps, the tSZ is either the signal of interest or one of the signals being nulled.

3.2. Sky and Noise Model

In this section, we describe the model used to construct the spectral behavior matrix $f_i(\nu_j)$ and the two-dimensional Fourier-space covariance matrix $N_{ij}(\mathbf{l})$ used in the LC algorithm described in Section 3.1. $N_{ij}(\mathbf{l})$ includes contributions from astrophysical sources and instrumental and atmospheric noise, and it includes covariance between maps at different observing frequencies. We model the amplitude and angular power spectra of the astrophysical contributions to the SPT-SZ and Planck maps based on recent power spectrum results from the SPT and Planck collaborations, while the noise model is based on the estimates described in Sections 2.1.2 and 2.2.1.

The contributions to the sky signal are modeled as follows:

1. The tSZ appears as a spectral distortion of the CMB spectrum in the direction of energetic electrons, such as those found in galaxy groups and clusters. In this work we follow Sunyaev & Zel'dovich (1972, 1980) where this distortion at a given frequency, ν , is given by

$$\begin{aligned} \Delta T(\nu) &= T_{\text{CMB}} f_{\text{SZ}}(x) \int n_e \frac{k_B T_e}{m_e c^2} \sigma_T dl \\ &\equiv T_{\text{CMB}} f_{\text{SZ}}(x) y_{\text{SZ}}, \end{aligned} \quad (9)$$

where the integral is along the line of sight, $T_{\text{CMB}} = 2.7260 \pm 0.0013$ K is the mean CMB temperature (Fixsen 2009), $x \equiv h\nu/k_B T_{\text{CMB}}$, k_B is the Boltzmann constant, c the speed of light, n_e the electron density, T_e the electron temperature, σ_T the Thomson cross-section, and $f_{\text{SZ}}(x)$ is the frequency dependence of the effect relative to the spectrum of fluctuations of a 2.73K blackbody (note that we assume that all input maps are calibrated such that they have a unit response to CMB fluctuations):

$$f_{\text{SZ}}(x) = \left(x \frac{e^x + 1}{e^x - 1} - 4 \right) (1 + \delta_{\text{rc}}), \quad (10)$$

with δ_{rc} encompassing relativistic corrections (e.g., Wright 1979; Nozawa et al. 2000; Chluba et al. 2012). While these relativistic corrections can have a significant impact on the tSZ signal at, e.g., the locations of hot clusters (e.g., Hurier 2016), in this work, at small angular scales where this new Compton- y map will offer significant advantages over the Planck data previously available in this region, omitting these corrections has negligible impact on the weights in the band combination. At high ℓ (see Figure 1) the y map construction is dominated by a combination of the SPT 95 and 150 GHz channels, and the difference in the relative strength of the tSZ signal in these bands when including relativistic corrections is small (for

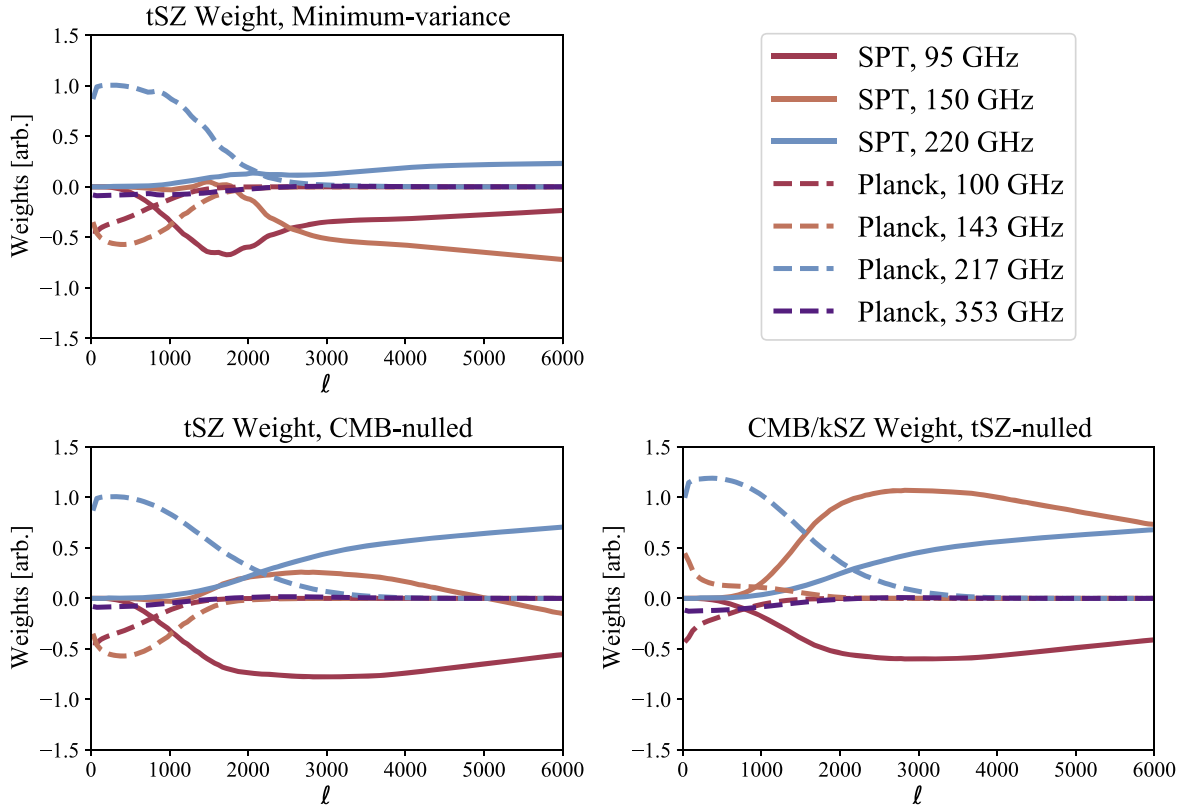


Figure 1. Relative azimuthally averaged band weights for the minimum-variance thermal SZ Compton- y map (upper left), the CMB-nulled y map (lower left), and the tSZ-nulled CMB/kSZ map (lower right).

example, the ratio of f_{SZ} in the 95/150 GHz bands for a 15 keV cluster is 1.70 when including relativistic corrections compared to 1.71 without). The amplitude at the location of hot gas will be biased low, however, e.g., 8% (3.5%) for 15 (5) keV gas (Nozawa et al. 2000).

2. The primary CMB is modeled following the power spectrum results presented in Planck Collaboration et al. (2020e). In particular we use the temperature power spectrum predicted by the best-fit cosmological model to the Planck PLIKHM_TTTEEE_LOWL_LOWE_LENSING data set.
3. The CIB is modeled based on the results of Reichardt et al. (2021) from the SPT-SZ and SPTpol surveys. It is parameterized into two components: a Poisson component whose power spectrum is independent of angular scale and a clustered component that follows the one- and two-halo clustering template of Viero et al. (2013). Both components are assumed to have a scaling with frequency that follows a modified blackbody:

$$\eta_\nu = \nu^\beta B_\nu(T), \quad (11)$$

where B_ν is the blackbody spectrum for a temperature T and β is the dust emissivity index. For a fixed dust temperature of 25 K, Reichardt et al. (2021) constrain $\beta_p = 1.48 \pm 0.13$ for the Poisson component and $\beta_{\text{cl}} = 2.23 \pm 0.18$ for the clustered term with 150 GHz power at $\ell = 3000$ of $D_{3000}^p = 7.24 \pm 0.63 \mu\text{K}^2$ for the Poisson component and $D_{3000}^{\text{one-halo}} = 2.21 \pm 0.88 \mu\text{K}^2$ and $D_{3000}^{\text{two-halo}} = 1.82 \pm 0.31 \mu\text{K}^2$ for the one- and two-halo terms, respectively.⁴²

4. We adopt a two-fold approach to reduce contamination from Galactic cirrus. As described below in Section 3.3, at large angular scales we subtract off a template of the dust emission from each of the single-frequency maps used in the analysis. At smaller angular scales we incorporate the dust signal as a component in our noise covariance matrix. We assume that this cirrus signal is well represented by a modified blackbody that is 100% correlated between bands with a dust temperature of 19 K (Viero et al. 2019), a dust emissivity of $\beta_{\text{cirrus}} = 1.89$ (Martin et al. 2010), and a spatial dependence of $D_\ell \propto \ell^{-1.2}$, which we further reduce at large angular scales to correct for the power removed by the template subtraction. The amplitudes of the cirrus signal at each frequency is set by scaling the results of George et al. (2015).
5. We include a Poisson component for the radio source power based on the results of Reichardt et al. (2021) which found a spectral index, ν^α , $\alpha = -0.76$ and amplitude $D_{3000} = 1.01 \pm 0.17 \mu\text{K}^2$ for sources fainter than 6.4 mJy at 150 GHz in SPT data. We also provide a mask with the location of sources detected above this threshold (Everett et al. 2020). After applying this mask, we discuss residual contamination from sources below this threshold in Section 5.1.

As discussed in the previous section, the intrinsic two-dimensional fluctuation power from all of these signals is expected to be statistically isotropic except for Galactic foregrounds and individual bright emissive sources, which we argue contribute negligibly to the covariance matrix. Sky signals that contribute significantly to the covariance are also

⁴² Where D_{3000} refers to power at $\ell = 3000$ in the convention $D_\ell = \frac{\ell(\ell+1)}{2\pi} C_\ell$.

expected to be isotropic on the sky (no preferred direction). In this case, we can write

$$\langle S_j(\nu_i, \mathbf{l}_1) S_j(\nu_k, \mathbf{l}_2) \rangle = C(\nu_i, \nu_k, \ell_1 = |\mathbf{l}_1|) \delta(\mathbf{l}_2 = \mathbf{l}_1) \quad (12)$$

and characterize the signal power with an independent band–band covariance matrix only dependent on $\ell \equiv |\mathbf{l}|$. As discussed in Sections 2.1.2 and 2.2.1, we can also approximate the SPT-SZ and Planck noise as statistically isotropic (and thus uncorrelated between the different \mathbf{l} modes). Because of the combination of the SPT scan pattern and low-frequency noise from the atmosphere and other sources, the noise part of the covariance matrix is not isotropic on the sky (modes that oscillate quickly along the SPT scan direction are less noisy than those that oscillate slowly along that direction). For this reason we keep the full two-dimensional noise covariance $N_{ij}^{\text{noise}}(\mathbf{l})$.

3.3. Galactic Dust

While the SPT-SZ fields were generally chosen to target areas of high Galactic latitude, there is still appreciable emission at large angular scales from Galactic dust. As this emission is spatially variable across the survey footprint, we choose to subtract a template of this contaminant from each frequency map before including it in our Fourier-based map construction. We explored constructing this template using data from the HI4PI survey (HI4PI Collaboration et al. 2016), the Planck thermal dust map constructed using the generalized needlet ILC (GNILC) technique (Planck Collaboration et al. 2016i), and the CMB-subtracted Planck 545 GHz “foreground” map constructed using the COMMANDER algorithm (Planck Collaboration et al. 2016c).⁴³

Ultimately we settled on using the 545 GHz foreground map smoothed to an FWHM of $16'$ to construct our template, validating the dust removal using the HI4PI survey. We note that while the GNILC thermal dust map has superior dust modeling, its resolution is spatially varying (with FWHM ranging from $5'$ to $21.8'$), and—as the dust levels in the SPT footprint are generally low and well subtracted with our uniform resolution template—the results are changed negligibly in adopting the smoothed 545 GHz map, the uniform resolution of which simplifies modeling. There is a small amount of tSZ in the 545 GHz COMMANDER map, both from the true tSZ signal at 545 GHz and from the tSZ leaked from other frequencies in the process of removing the CMB signal using multifrequency Planck data (see, e.g., discussion in Chen et al. 2018). We use simulations to quantify the level of tSZ in the 545 GHz COMMANDER map and the degree to which this biases our final recovered Compton- y map. We find that the bias to the recovered Compton- y signal is $\sim 1\%$ at $\ell < 200$ and much lower at higher ℓ . In practice, this boost partially offsets the small loss in power caused by our low- ℓ , high- k_x filtering (see Sections 3.4, 4.1).

To determine the scaling between the dust template and each Planck frequency map, we first project both the 545 GHz foreground template map and the COMMANDER foreground map for the Planck frequency of interest onto each of the SPT fields. We smooth each map to a resolution of $16'$ as we are

interested in determining the scaling between Galactic dust and the Planck frequency maps and do not want to include the smaller-scale CIB in our fits and subtraction here. We next rebin the data to $4'$ pixels and mask bright emissive sources detected at $>150\sigma$ in SPT data at 95 or 150 GHz with degree-radius masks to reduce spurious correlations between the maps. We conduct an outlier-resistant polynomial fit over all the SPT-SZ fields to find the global relation (one per frequency for the whole survey) between the intensity in the template and the various smoothed foreground maps, finding a cubic polynomial to provide the best fit. The smoothed 545 GHz foreground maps are then scaled by this relation and subtracted off from each of the Planck full-sky maps before they are used in the LC described above.

We also fit for a similar correlation using the SPT data, this time additionally filtering the 545 GHz template map with the SPT transfer function. However, the high-pass filter applied to the SPT maps has already effectively removed the majority of the large-scale emission and no significant correlation was detected, even reducing the smoothing of the maps to FWHM of $10'$. Given the small SPT data contribution at the ℓ ranges affected (see, e.g., Figure 1), we choose to simply ignore the low- ℓ dust contribution to the SPT maps (but do include a dust covariance matrix as a source of noise in the map combination, as detailed above).

The nature of the Galactic emission is not uniform across the full SPT-SZ survey. In particular, in areas of high dust intensity—such as those found at the western edges of the SPT-SZ fields closest to the Galaxy—this simple cubic polynomial correction breaks down. This is expected, as previous works have shown that regions with bright cirrus also have significant contribution from dust emission associated with molecular gas, which follows a different modified blackbody function from regions correlated with H I (see discussion in, e.g., Planck Collaboration et al. 2011b). Given the relative weights of the frequency channels in the map construction, such incomplete subtraction of dust emission results in a reduction in the recovered tSZ signal at large scales in very dusty regions. While this bias will not affect analyses conducted on smaller-scale features (e.g., cluster detection at $z > 0.25$, tSZ profiles on scales smaller than the emission, etc.) we do include pixel masks encompassing regions of poorer dust subtraction for those who wish to exclude these regions from their analysis. These masks are constructed from the smoothed 545 GHz foreground maps in regions with emission $>1.1 \text{ MJy sr}^{-1}$ for which the residuals of the lower frequency dust-subtracted foregrounds maps are $>3\sigma$ away from zero. As a check of our dust removal, we cross-correlate our minimum-variance and CIB/CMB-nulled Compton- y maps with the H I map provided with the HI4PI survey, finding the cross-correlation power reduced by $7\times$ – $10\times$, respectively following this dust removal procedure. In Figure 2 we show one SPT field, ra5h30dec-55, before and after removing Galactic dust.

3.4. Treatment of Missing Modes

As mentioned in Section 2.1.1, the SPT scanning strategy and data filtering results in a set of two-dimensional Fourier modes on the sky being removed from the SPT-SZ maps used here. In particular, the polynomial filtering of the SPT-SZ detector time-ordered data removes modes at low frequency along the scan direction. For nearly all observations, the SPT is scanned along lines of constant elevation, which, at the

⁴³ See also details at https://wiki.cosmos.esa.int/planckpla2015/index.php/CMB_and_astrophysical_component_maps.

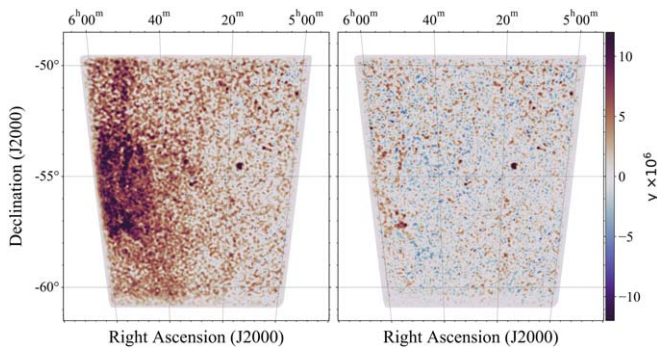


Figure 2. Left panel: minimum-variance Compton- y map for the SPT-SZ `ra5h30dec-55` field constructed without correcting for large-scale dust emission. Right panel: the same field after correcting for this emission as discussed in Section 3.3. The maps are smoothed with a beam of $\text{FWHM} = 5'$ for display purposes.

geographic South Pole, correspond to lines of constant decl. In the Sanson–Flamsteed projection used in this work, lines of constant decl. are parallel to the x -axis; thus, the SPT-SZ maps used here have no information at the lowest values of l_x or angular frequency along the horizontal map direction. Planck data are not missing these modes, so the LC algorithm uses Planck data exclusively in this region of Fourier space. At high $\ell = |\mathbf{l}|$, the Planck data is heavily rolled off by the finite angular resolution of the instrument, and the factor needed to restore these modes to an unbiased estimate of CMB/kSZ or Compton- y multiplies the Planck noise, resulting in the high- l_y , low- l_x part of Fourier space being many times noisier than average.

We have chosen to suppress this noise by applying a two-dimensional Fourier-space filter to the output component maps. This filter is equal to unity everywhere except in the “trough” of modes at low l_x —in this trough the filter is equal to a Gaussian in l_y , with σ_{l_y} set such that the noise is roughly equal to the noise outside the trough. We include two-dimensional (l_x, l_y) and one-dimensional (ℓ -space) versions of this filter as one of the data products in our release; these can be used as an effective transfer function or ℓ -space beam in power spectrum or correlation analyses. For object-based analyses such as aperture photometry, we estimate the bias from this filter in Section 4.1.

3.5. CIB Contamination versus Noise in the “Minimum-variance” y Map

As discussed above, the band weighting in the single-component version of the linear combiner (in which no other signals are explicitly nulled) produces the minimum total variance in the resulting Compton- y map. But some sources of variance are of more concern than others, and for a y map, the presence of CIB in the map is generally of the highest concern, particularly for using that y map in cross-correlation studies. One can attempt to null a component of the CIB with a particular SED, as we do in the three-component version of the map we create, but that results in a fairly high noise penalty and does not fully solve the problem, as the CIB is a combination of many components with different SEDs. Multiple components with different SEDs can be nulled, but this is limited by the number of frequency bands (and further increases the noise penalty).

Here we investigate trading off CIB for noise and CMB variance by artificially increasing the weight of the CIB in the linear combiner—effectively lying to the algorithm about how bright the CIB is. We find that multiplying the CIB part of the covariance by some amount is quite effective in reducing the CIB component in the resulting y map while only causing mild increases in total variance.⁴⁴ We measure the level of CIB in the synthesized “minimum-variance” y map by cross-correlating the Herschel/SPIRE 500 μm map described in Section 2.4 with the y map from the SPT-SZ field that overlaps with the Herschel/SPIRE coverage, keeping in mind that there should be some level of true underlying correlation between the y and CIB fields (e.g., George et al. 2015; Planck Collaboration et al. 2016j).

Figure 3 shows the measured cross-correlation between the synthesized y map and the Herschel/SPIRE 500 μm map as a function of the CIB covariance multiplier. Specifically, the left panel of Figure 3 shows the ratio of the measured 500 μm - y cross-spectrum to the cross-spectrum of the 500 μm map with a y map made just by dividing an SPT-SZ-Planck synthesized 150 GHz map by $f_{\text{SZ}}(150 \text{ GHz})T_{\text{CMB}}$, with different curves representing different values of the CIB multiplier. The right panel shows the ratio of the measured 500 μm - y cross-spectrum to the predictions of the cross-spectrum between y and the CIB at 500 μm from the Y. Omori et al. (in preparation) y and CIB skies painted onto the MDPL2 (Klypin et al. 2016) simulations. Curves are shown for two specific ℓ values ($\ell = 1000$ and $\ell = 4000$) as a function of the CIB multiplier, along with the total map rms relative to the true minimum-variance y map (in which the “CIB multiplier” is unity). In both plots, different curves are shown for band weights synthesized assuming the noise in the normal SPT-SZ field depths and for band weights synthesized assuming the noise in the “double-deep” fields.

It is clear that the contribution to the 500 μm - y cross-spectrum from residual CIB in the synthesized y maps can be reduced significantly with only a mild ($\lesssim 10\%$) noise rms penalty. Using a by-eye metric of where the cross-spectrum appears to asymptote at both ℓ values, we choose a CIB multiplier value of eight for the normal-depth fields and five for the double-depth fields. When we use the term “minimum-variance map” anytime in the rest of this work, we are actually referring to these maps. Finally we note that we do not apply this CIB multiplier to the covariance when we produce y or CMB maps with a component of the CIB formally nulled.

4. The CMB/kSZ and Compton- y Maps

We make and release several versions of component maps resulting from our LC algorithm:

1. A “minimum-variance” y map. This product is constructed using band weights defined in Equations (3)–(5). Assuming the signal and noise models are correct, and with no modifications to the input covariance, this product formally has the lowest variance possible for an unbiased estimate of y on all scales. However, as discussed above, we do modify the covariance to reduce the correlation of this map with the CIB (as traced by 500 μm Herschel/SPIRE data), at the cost of a small

⁴⁴ We note that this is effectively a less mathematically rigorous version of the partially constrained ILC method proposed in Sultan et al. (2021).

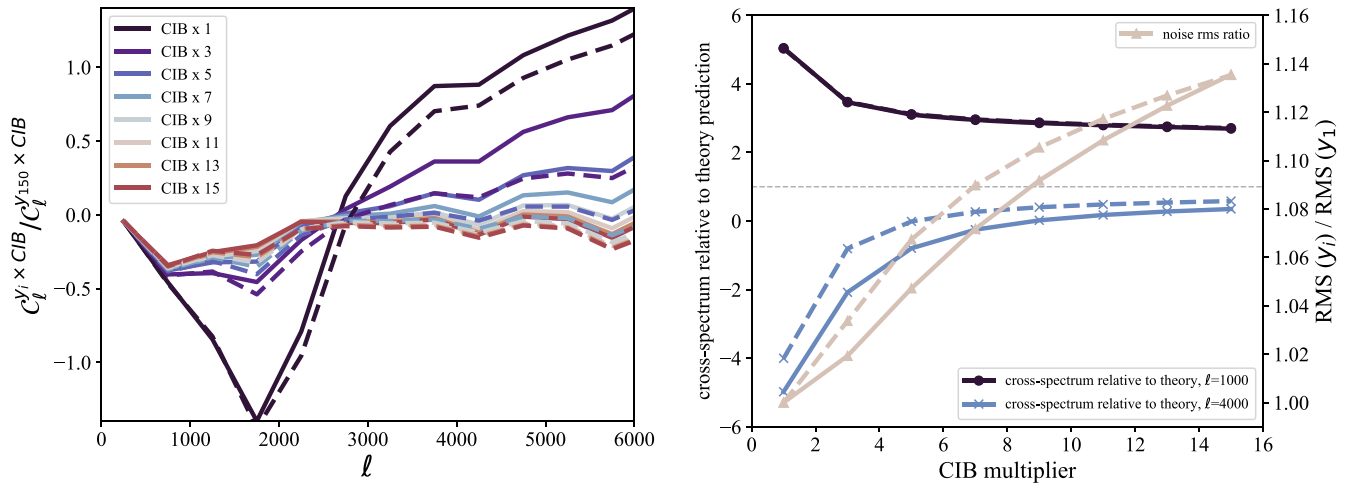


Figure 3. Left panel: y-CIB cross-spectrum for different CIB covariance multiplier values (see text for details) relative to the y-CIB cross-spectrum for a y map made just from dividing a 150 GHz map by the tSZ factor for that frequency. Solid lines show results using band weights created assuming normal-depth SPT-SZ field noise; dashed lines show results using band weights created assuming “double-depth” SPT-SZ field noise. Right panel: y-CIB cross-spectrum ratio at $\ell = 1000$ and $\ell = 4000$ divided by the MDPL prediction for that ratio (see text for details) and total y-map rms as a function of CIB multiplier. As in the left panel, normal-depth and double-depth results are indicated with solid and dashed lines, respectively. (The single- and double-depth results for $\ell = 1000$ are indistinguishable because that multipole range is dominated by Planck data.) From this plot it is clear that a significant reduction in spurious y-CIB correlation (caused by residual CIB in the synthesized y map) can be achieved with a small noise penalty.

(order 10%) penalty in total y-map rms. We nevertheless will refer to this map as the “minimum-variance” map” (or “single-component map”) in the remainder of this work.

2. A “CMB-nulled” y map and the corresponding y-nulled CMB/kSZ map. We also refer to these as the “two-component” maps.
3. A “CMB- and CIB-nulled” y map and the corresponding y- and CIB-nulled CMB/kSZ map and y- and CMB-nulled CIB map. We also refer to these as the “three-component” maps. Because the CIB is made up of many independent emitters at different redshifts and temperatures (and different compositions), it is not possible to null all the CIB emission with a single SED. For our three-component maps, we choose to null CIB emission with an SED equal to the best-fit Poisson-component SED in George et al. (2015), who find that this component is the largest contribution to the $\ell = 3000$ power at 150 GHz. As expected, the noise levels of the two- and three-component products are significantly higher than for the minimum-variance case.

As an example of two of the data products we provide, we show the full-survey versions of the tSZ-nulled CMB/kSZ and the minimum-variance Compton-y maps in Figure 4. We provide flat-sky full and half (survey+mission) maps in each of the 19 SPT fields at 0.25 pixelation as well as combined maps covering the full SPT-SZ footprint in the HEALPix format with $N_{\text{side}} = 8192$. The minimum-variance single-component data products are provided at $1/25$ resolution and the multi-component products at $1/75$ resolution.

Figure 1 shows the relative band weights (ψ from Equation (4) or ψ_i from Equation (7)) as a function of $\ell = |\mathbf{l}|$ for three of the maps discussed above. As expected, the Planck bands provide the bulk of the information at low ℓ (large angular scales), where the SPT-SZ data is contaminated by atmospheric fluctuations. At higher ℓ (smaller angular scales), the higher angular resolution and lower instrument noise levels

of the SPT-SZ data take over. Also notable is the similarity of the single-component and two-component tSZ weights at low ℓ , understandable as the primary CMB is the largest source of variance at these scales. The tSZ-nulled CMB/kSZ weights are dominated at low ℓ by the Planck 217 GHz data, which is close to the tSZ null, but at high ℓ all three SPT-SZ bands contribute, in part because of the higher relative noise in the SPT-SZ 220 GHz data.

4.1. Bias to Aperture Photometry from Missing Modes

As discussed in Section 3.4, the maps produced in this work have two filters applied after the beam-and-transfer-function-deconvolved individual frequency maps have been combined into synthesized component maps. One filter is a simple Gaussian smoothing with a FWHM of $1/25$ for the single-component y map and $1/75$ for the multicomponent maps. The nonstandard filter is an anisotropic low-pass filter that only affects modes that oscillate slowly in the direction of R.A. The motivation for this filter is discussed in Section 3.4; here we calculate the bias incurred to aperture photometry if this filter is ignored.

We estimate this bias by creating simulated galaxy cluster profiles, Fourier transforming, multiplying by this l-space filter, inverse-Fourier transforming, and performing aperture photometry on these simulated profiles. We compare the results of aperture photometry on the filtered profiles to results of aperture photometry on the original cluster profiles and report the difference as the bias from the filter. We perform this calculation on a range of cluster masses and redshifts and using a range of aperture radii. We use the Arnaud et al. (2010) model for the cluster y profile. For cluster masses $0.5 \times 10^{14} M_{\odot} < M < 10 \times 10^{14} M_{\odot}$, redshifts $0.1 < z < 2$, and aperture radii $1.0' < r < 10.0'$, we find a maximum bias of $\sim 3\%$. The bias is larger at smaller apertures (at $r > 5'$ the maximum bias is $\sim 1\%$).

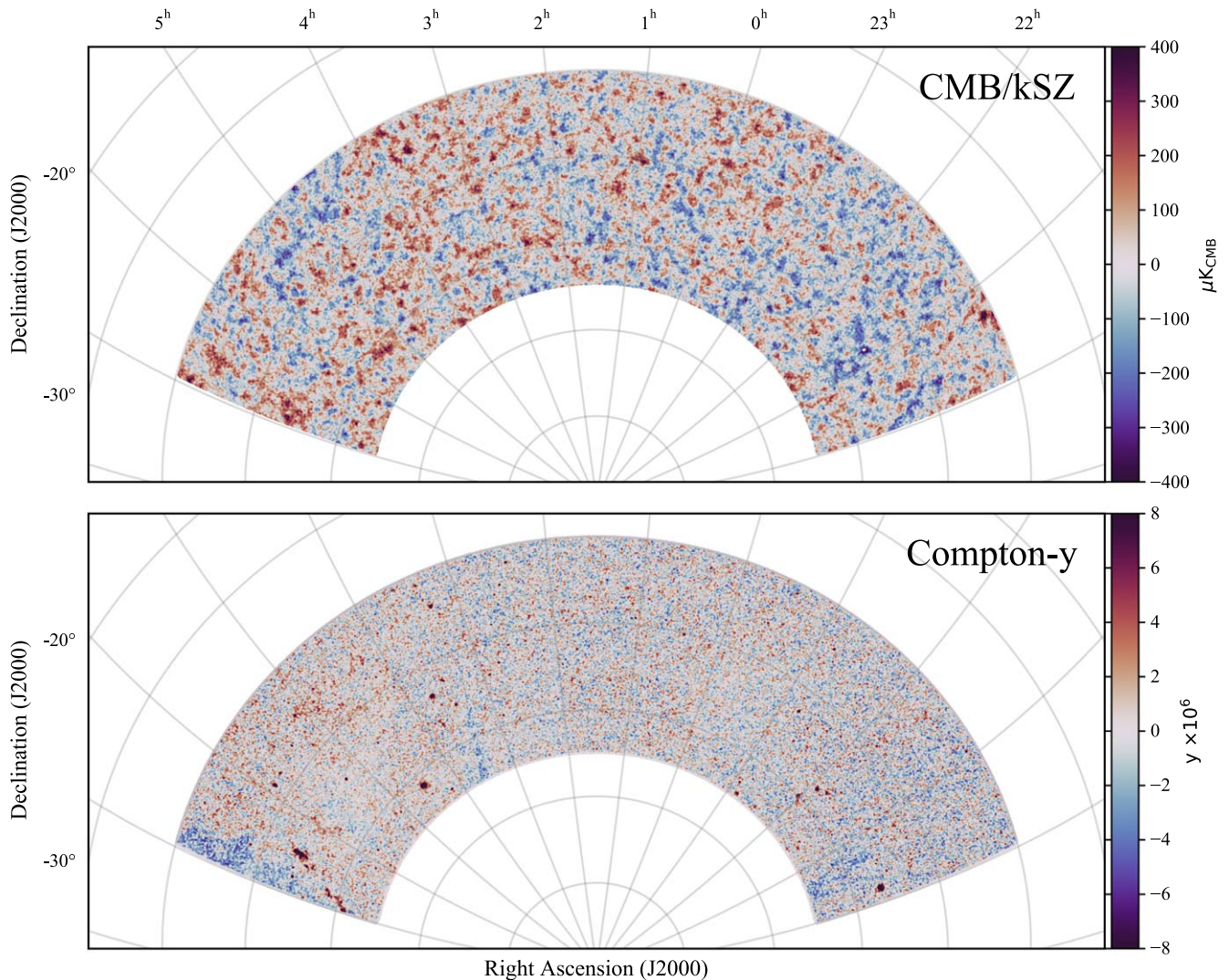


Figure 4. Two examples of component maps provided in association with this work. (Top) tSZ-nulled CMB/kSZ map constructed using observations from the SPT-SZ survey and Planck HFI. (Bottom) Minimum-variance Compton- y map from the same. Both of these maps are smoothed here for display purposes; we provide minimum-variance map products at $1'.25$ resolution and map products with other signals nulled at $1'.75$ resolution in the data release.

4.2. Comparison to Other Releases

To date, the only other publicly available Compton- y maps in the SPT-SZ survey footprint are derived from Planck data products (particularly Planck Collaboration et al. 2016d). As expected, the addition of SPT data products significantly improves both the angular resolution (from $10'$ to $1'.25$ or $1'.75$, for the minimum-variance and component-nulled versions, respectively) as well as the noise performance at small scales. We provide a qualitative demonstration of this effect in Figure 5 where we highlight the ability of the new data products to constrain arcminute-scale features in the pressure profile of Abell 3667 (Duus & Newell 1977; Abell et al. 1989) at redshift $z = 0.0556$ (Struble & Rood 1999) for which the improved angular resolution allows us to resolve features on ~ 80 kpc scales. This significant improvement in resolution will also aid in the detection of higher-redshift clusters; we detail the results of a blind cluster search below in Section 5.2.

As mentioned in the introduction, arcminute-scale component maps—including minimum-variance and CMB-nulled Compton- y maps and a y -nulled CMB/kSZ map—constructed from Planck and ACT data were presented in Madhavacheril

et al. (2020). In Figure 9 of that work, the authors showed that the power spectra of the y and CMB/kSZ maps including ACT data were (as expected) signal-dominated to much higher multipole values (smaller scales) than corresponding maps from Planck alone. In turn, we compare the power spectra of the maps in this release to those from the two sky regions in Madhavacheril et al. (2020)—the ~ 1600 deg² BOSS North or BN field and a deeper ~ 500 deg² field referred to as D56—in Figure 6.

There are many features worth noting in Figure 6. First, the agreement in the signal-dominated multipole regions—in particular of the CMB/kSZ map (bottom left panel)—demonstrates that the output maps from the two works are statistically consistent at the 10% level or better. This is not surprising, especially because the maps from both works are dominated by Planck data at these angular scales, but it is a rough validation of both pipelines.

The amplitudes of the power spectra in the noise-dominated multipoles merit further discussion. As shown in Figure 1 in this work and Figure 5 in Madhavacheril et al. (2020), the high- ℓ ($\ell \gtrsim 3000$) “minimum-variance” y -map weights are dominated by the 150 GHz SPT/148 GHz ACT data. The typical

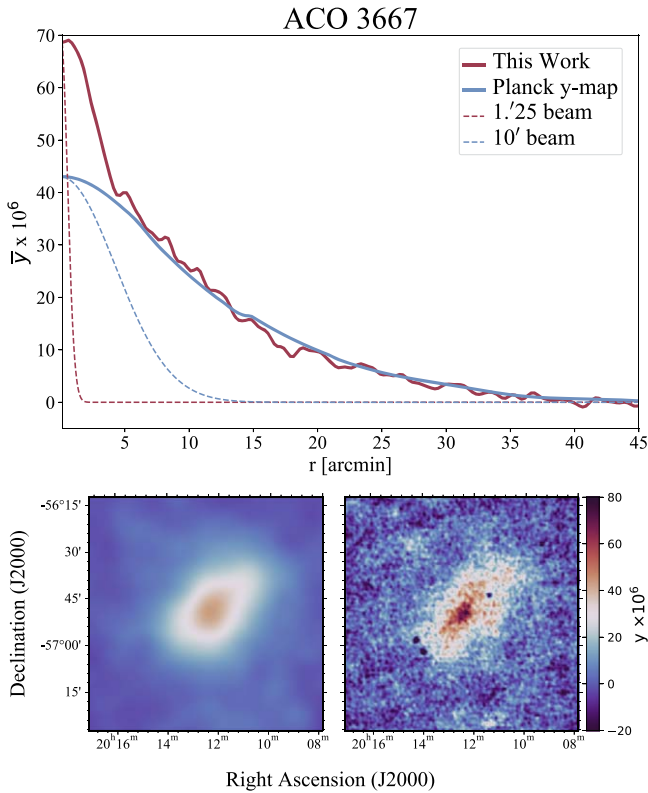


Figure 5. Top panel: azimuthally averaged Compton- y profiles for ACO 3667 at $z = 0.0556$. Bottom panels: on the left is a cutout from the Planck Compton- y map (Planck Collaboration et al. 2016d) centered on the cluster. We make a similar cutout on the right from the minimum-variance Compton- y map presented in this work. The arcminute-scale circular decrements in this image are located at the locations of bright radio sources readily detected in SPT data, enabling us to mask these regions when measuring the cluster’s pressure profile.

SPT-SZ noise level at 150 GHz ($\sim 16 \mu\text{K}\text{-arcmin}$) is between the 148 GHz noise levels in the two ACT regions (~ 25 and $\sim 10 \mu\text{K}\text{-arcmin}$ in BN and D56, respectively; see Table 1 in Madhavacheril et al. 2020), so it is not surprising that the high- ℓ power spectrum of the SPT-SZ “minimum-variance” y map lies in between that of the two ACT regions. By contrast, the SPT-SZ high- ℓ power spectrum is below that of both ACT regions for both components of the two-component linear combination (the CMB-nulled y map and the y -nulled CMB/kSZ map). This is especially surprising given that the 98 GHz ACT noise levels in the D56 region ($\sim 17 \mu\text{K}\text{-arcmin}$) are significantly lower than the SPT-SZ 95 GHz noise.

The two features of the data used in the SPT-SZ linear combination that could account for this are (1) data from the SPT-SZ 220 GHz band are included; (2) the SPT-SZ data are at slightly higher resolution, owing to the 10 m SPT primary mirror compared to the 6 m ACT primary (though the diameter of the primary region illuminated by the SPT-SZ camera is closer to 8 m). In the bottom-right panel of Figure 6, we show that both of these features contribute to the lower SPT-SZ noise in the two-component maps. The dotted-dashed line shows the predicted ACT D56 y -nulled CMB/kSZ power spectrum if 220 GHz data (with roughly the SPT-SZ noise level) are added, and the dotted line shows that power spectrum if 220 GHz data are added and if the resolution in all bands is improved by a factor of 1.33 (the ratio of the diffraction limits of 6 m and 8 m

apertures). This result demonstrates the utility of higher-frequency data and higher angular resolution in component separation, particularly for the goal of extracting the tSZ-nulled kSZ signal out to $\ell \sim 4000$.

5. Validation of the Component Maps

In this section we detail several characterization analyses of the SPT-SZ + Planck component maps described in the previous section. As discussed in Section 4.2, a rough validation of the maps, particularly the y -nulled CMB/kSZ map is provided by comparing the power spectrum of maps from this analysis to the power spectrum of ACT+Planck maps in Figure 6; we apply more quantitative measures in this section. These tests include validation of our assumptions for the input signal model, tests of the blind detection from SZ clusters in the maps, and finally, a cross-check of our tSZ nulling in the CMB/kSZ map products.

5.1. Validation of the Input Signal Model

As discussed in Section 3, the linear combination algorithm we use relies on models of the power in various sky components, including the cross-power between different frequencies. Even if these models are wrong, the resulting CMB/kSZ or Compton- y map (or other component maps) will still have an unbiased response to the desired signal (provided the instrument bandpasses are correctly measured), but the linear combination of bands used may not be optimal, i.e., there can be excess variance induced by the incorrect modeling of sky signal.

Figure 7 shows a simple check of the signal modeling, namely the power spectrum of the output y map in the case where the CMB/kSZ and one component of the CIB are explicitly nulled. The data points are an average over power spectra from the 19 individual SPT-SZ fields, calculated using the cross-spectrum of one-half of the data against the other to eliminate noise bias. The data points are corrected by the 1.75 smoothing beam and the “trough filter” (see Section 3.4) applied to the maps, but no other corrections are made (e.g., for mode coupling). Error bars are calculated using resampling (with replacement) of the values from the individual fields. Overplotted is the expected power from various sky signals given the input model and the real band weights $\psi_i(\nu_i)$ returned by the linear combiner. The model for the tSZ is the best-fit model from Reichardt et al. (2021). The subtraction of the dust template described in Section 3.3, constructed by smoothing the Planck COMMANDER 545 GHz foreground map to 16’ resolution, will affect the low- ℓ CIB power in the output y map; for the purposes of this plot we bracket the possible effect by multiplying the residual CIB power in the model by a 16’ FWHM Gaussian, subtracting that from the model, and plotting the result as a second set of model lines. The shaded area between the unmodified and modified models thus indicates the modeling uncertainty introduced by the dust-cleaning step. Because of this uncertainty and the lack of correction for, e.g., mode coupling, we do not report a formal goodness of fit to the model; we simply note that at the 10% level the total power in the model appears to agree with the data, particularly above $\ell = 1000$.

Somewhat more formally, we use the linear combination framework to investigate the potential impact on y -map variance from incorrect signal modeling. The signals in

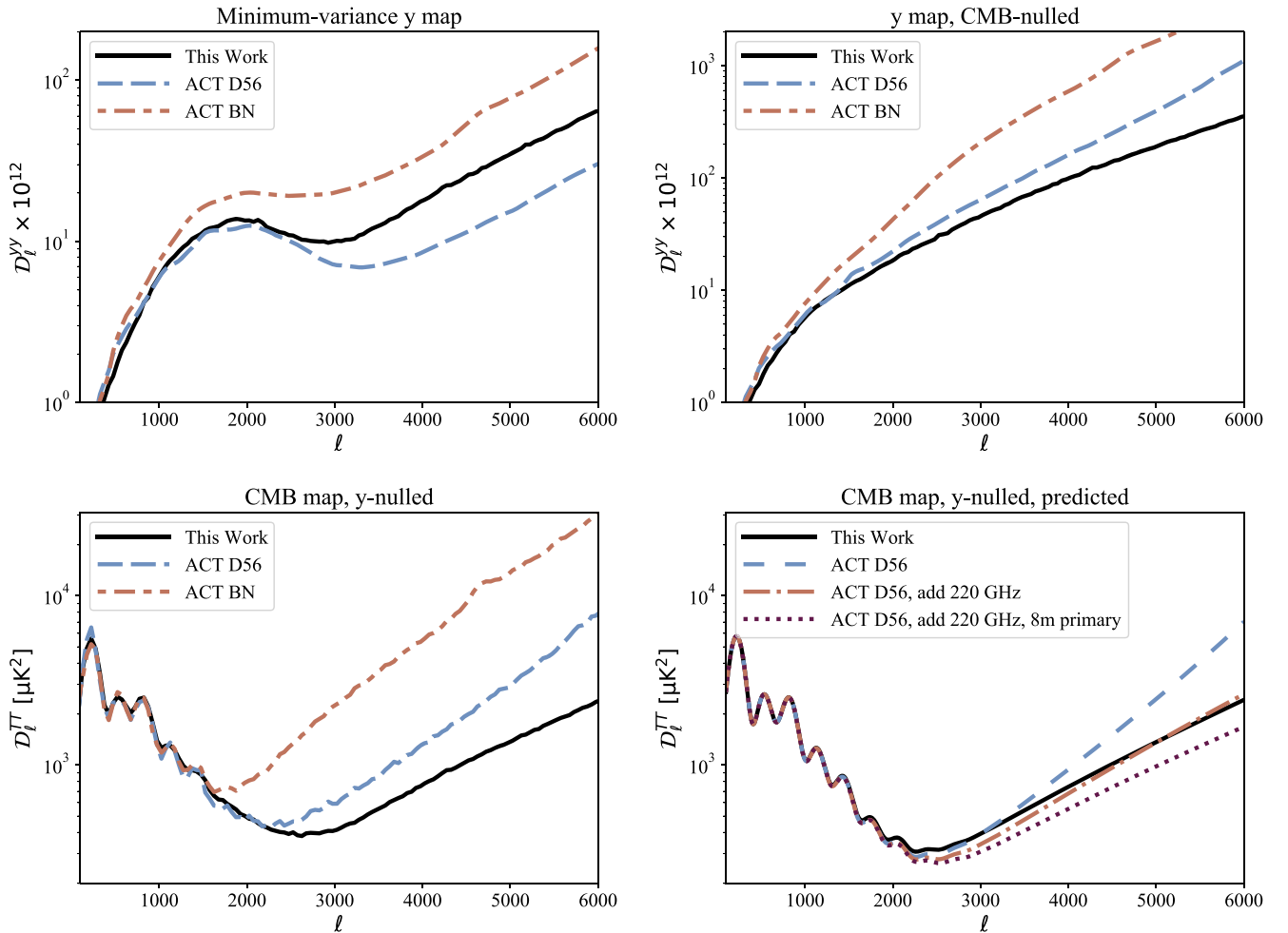


Figure 6. Angular power spectra of selected output maps, with results from ACT+Planck (Madhavacheril et al. 2020) shown for comparison. The agreement between the three curves in the signal-dominated multipole region ($\ell \lesssim 2200$ for SPT and ACT D56, $\ell \lesssim 1500$ for ACT BN) provides a rough validation of both sets of data products. The differences in the noise-dominated multipole region are discussed in the text. Top left: power spectra of the minimum-variance y maps from this work and from the two different sky regions used in Madhavacheril et al. (2020). Top right: similar for the CMB-nulled y map. Bottom left: similar for the y -nulled CMB/kSZ map. Bottom right: predicted power spectra for the y -nulled CMB/kSZ map from SPT and the ACT D56 region, using noise levels reported in this work and Table 1 of Madhavacheril et al. (2020). To demonstrate the importance of high-frequency data and angular resolution in the component-separation process, curves for the ACT D56 noise levels are shown in the hypothetical scenario in which 220 GHz data (at the rough noise levels of the SPT data) are added and in which the resolution of the ACT data is improved (see text for details).

question have been reasonably well characterized in previous studies. The primary CMB temperature anisotropy has been measured at the percent level in bins of $\Delta\ell \sim 50$ (assuming a smooth power spectrum) by Planck (Planck Collaboration et al. 2016k) and high-resolution ground-based experiments such as ACT (Choi et al. 2020) and SPT (Story et al. 2013). At $\ell = 3000$, Reichardt et al. (2021) measure the relevant secondary and foreground signals, namely the CIB and residual radio galaxy power after masking, with $\sim 10\%$ precision. We create several sets of band weights using different signal model inputs, modifying each input component by an amount that is in mild tension with current data. For each of these sets of band weights, we compute the predicted variance in the output maps under the assumption that the modified inputs are correct and under the assumption that the original signal model was correct.

Specifically, we modify the primary CMB power spectrum by $\pm 2\%$ in amplitude and $\pm 2\%$ in spectral index, both of which are four to five times the marginalized error bar on the associated cosmological parameter or parameter combination ($A_s e^{-2\tau}$ and n_s , respectively). We modify the amplitude of the

input CIB model by $\pm 20\%$, and we double the model radio power. We run the test described above in the one-, two-, and three-component cases. In all of these permutations, we find that the fractional excess variance from assuming the wrong model is never greater than 0.6%. We conclude that, for the noise levels and the size of the sky patch in this analysis, the suboptimality of using models for the sky signal components is minimal.

5.2. Detection of Clusters by the tSZ Effect

One natural test of the quality of a constructed Compton- y map is its efficacy for the blind detection of clusters via the tSZ effect. As noted in the Introduction, there have been several recent analyses undertaking cluster searches on combined Planck and ground-based data using ACT (Aghanim et al. 2019) and SPT-SZ data (Melin et al. 2021). These works have both noted significant improvement in cluster detection over data from each sample alone, with Melin et al. (2021) particularly quantifying such improvements as a function of redshift. Here we will present the results of such a cluster

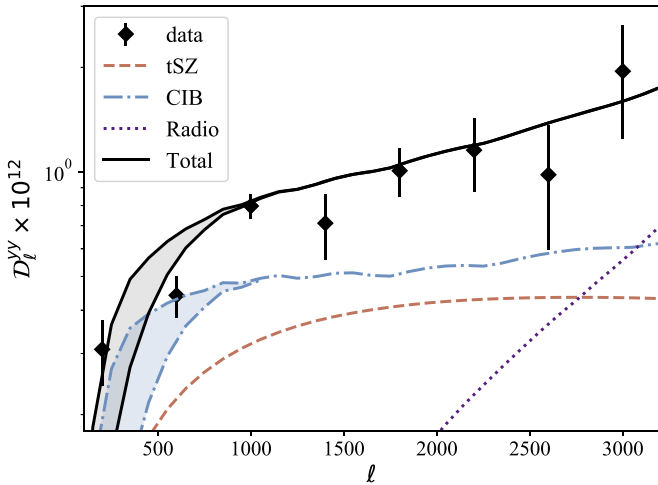


Figure 7. Power spectrum of the CMB-CIB-nulled y map. The data points show the measured power spectrum of the y map from the three-component analysis in this work. The power spectrum is estimated using independent halves of the data to avoid noise bias. Error bars are estimated using resampling of the values from the individual SPT-SZ fields. Lines show the expectation for power from various components in the y map, given the signal models used in the linear combination algorithm. These are calculated by multiplying the model power spectra at each band by the band weights for the CMB-CIB-nulled y map and summing. The blue and gray shaded areas indicate the possible effect of dust cleaning on the CIB (see text for details). The by-eye agreement between the solid black line (sum of all model components) and the data points indicates that the signal variance models are roughly representative of the true signals in the data.

search on our minimum-variance Compton- y map, comparing our results to cluster samples reported by the SPT-SZ (Bleem et al. 2015b) and Planck collaborations (Planck Collaboration et al. 2016a).

To conduct this search, we adopt an essentially identical procedure to that used in previous searches for clusters in SPT data (see, e.g., Bleem et al. 2015b for a more detailed description of the process). Our search is based on the spatial-spectral filtering method presented in Melin et al. (2006) and, as the y -map construction has already isolated the tSZ signal, we simply make use of a spatial filter designed to optimally extract the cluster signal in the presence of noise. We adopt a projected spherical β -model with β fixed to 1 (Cavaliere & Fusco-Femiano 1976) as the model of our cluster profile:

$$\Delta T = \Delta T_0 (1 + \theta^2/\theta_c^2)^{-(3\beta-1)/2}, \quad (13)$$

where the normalization ΔT_0 is a free parameter and the core radius, θ_c , is allowed to vary in 12 equally spaced steps from $0'.25$ to $3'$ (as in previous SPT works) and additionally include θ_c values of $5'$, $7'$, $9'$, and $12'$ to allow for the detection of clusters of larger angular extent (the latter now enabled by the inclusion of the Planck data). This filtering corresponds to scales of θ_{500c} of approximately $1.25'$ to $60'$ in the commonly used Arnaud et al. (2010) model of cluster pressure profiles.

We run our cluster identification algorithm on the flat-sky version of each of the 19 SPT-SZ fields, adopting a $1'.25$ beam as our transfer function. The noise in these maps is composed of the astrophysical, instrumental, and atmospheric noise that remains after the map combination process. We estimate this noise by summing the power from each component of our sky + noise model (Section 3.2) with the appropriate 2D Fourier-space weights for each frequency map included in the y map.

We also heavily penalize the noise at low k_x , high k_y , where we are missing modes in the maps (Section 3.4).

The resulting SZ candidate list has 418 detections at signal-to-noise $\xi > 5$ (compared to 423 in Bleem et al. 2015b, but detected in 3% less area; see Section 2.1.1) and 677 $\xi > 4.5$ (versus 696). Fifty-five new SZ cluster candidates at $\xi > 5$ (the 95% expected purity threshold) that are not in the Bleem et al. (2015b) sample are identified. Recognizing there will be scatter between detection significances for given clusters between the lists owing to the inclusion of the Planck data, the addition of radio power in the noise covariance matrix used in the map construction (this power was not included in the Bleem et al. 2015b noise model), as well as the additional masking around bright sources (Section 2.3), we match our new candidate list at $\xi > 4$ to the published SPT-SZ list at $\xi > 4.5$. Associating detections within $2'$ we recover 473 matches with an average ratio in the detection significance ($\xi_{\text{new}}/\xi_{\text{SPT-SZ}} = 1.0$ and standard deviation of this ratio of 0.2). We recover all confirmed SZ clusters (those with redshifts reported in Bleem et al. 2015b) above $\xi = 6.1$ within the unmasked Compton- y footprint and 94% (85%) of confirmed clusters at $\xi > 5$ ($\xi > 4.5$). Examining the locations of the Bleem et al. (2015b) clusters not detected in our new search at $\xi > 4$ in the signal-to-noise maps produced by the cluster finder, we find a median difference of $\Delta\xi = 1.4$; there are no significant redshift or θ_c trends in the unmatched clusters compared to the matched.

We note that a quick reading of this work may imply that the addition of Planck data did not contribute in a meaningful way to the detection of these systems. However, we remind the reader that we have adopted a weighting scheme in the map construction that minimizes the cross-correlation of the y map with the CIB (see Section 3.5) and adds a noise penalty to these maps compared to a true minimum-variance y map. The addition of the Planck data (and to a much lesser extent the SPT-SZ 220 GHz data) essentially compensates for this choice.

Moving on to comparisons with the Planck SZ cluster sample (Planck Collaboration et al. 2016h), we associate our new SZ candidate list with confirmed Planck clusters within the larger of $4'$ or the Planck positional uncertainty, finding 103/117 matches at $\xi > 4$ and Planck detection signal-to-noise ratio > 4.5 with a median improvement in the signal-to-noise ratio of the detection of $1.25\times$. This is an improvement over a similar matching exercise undertaken with the Bleem et al. (2015b) sample for which 83 SPT-SZ clusters in the Compton- y map footprint had matches to confirmed clusters in the Planck catalog (see also discussion comparing properties of the Planck and SPT-SZ and SPT-ECS samples in Bleem et al. 2020). The most significant gains were found, as would be expected, for low- z clusters with the larger angular extent on the sky for which the inclusion of Planck data provides enhanced sensitivity. While the typical signal-to-noise ratio of the combined map SZ detections is higher than those from Planck alone, our simplified treatment of the Planck noise—both in the map combination procedure and the cluster extraction (see e.g., discussion in Planck Collaboration et al. 2014d, 2016h for more optimal treatment of Planck data)—leads to lower detection significances for the lowest-redshift clusters.

5.3. tSZ Nulling in the CMB/kSZ Maps

We perform one final validation test regarding the efficiency of the tSZ nulling in the CMB/kSZ component maps. While

the derivations governing both nulling and the thermal SZ spectrum are unambiguous, this test will probe both our constraints on the bandpasses and calibration of our maps as well as the presence of correlated signals not explicitly canceled (from, e.g., cluster member galaxies) at the locations of clusters; we note that as these are SZ-selected clusters this is not a strong test of the presence of such associated emission in the general cluster population (though see a discussion of such effects in, e.g., Section 3.5 of Bleem et al. 2020). As our baseline we construct a true minimum-variance CMB/kSZ map and sum the temperature values in this map at the location of 504 confirmed SPT-SZ clusters with $\xi > 4.5$ that are not affected by the masking used in this work. We find the mean temperature and its uncertainty at these cluster locations to be $-34 \pm 1.5 \mu\text{K}$. Performing this exercise on the CMB/kSZ maps with the tSZ- and tSZ/CIB-model nulled we find $-3 \pm 3 \mu\text{K}$ and $7 \pm 7 \mu\text{K}$, respectively.

Sharpening our sensitivity to cluster scales, we then repeat this exercise, performing compensated aperture photometry on the three maps with $2'$ apertures at the cluster locations. We again find a significant average temperature decrement in the minimum-variance CMB map ($-1.16 \pm 0.025 \times 10^{-5} \mu\text{K}\text{-sr}$, 45σ), a small decrement in the tSZ-nulled maps ($-3.1 \pm 0.4 \times 10^{-6} \mu\text{K}\text{-sr}$; 7.5σ) and no significant detection in the tSZ/CIB-nulled maps ($3 \pm 2 \times 10^{-6} \mu\text{K}\text{-sr}$; 1.5σ increment). As expected, the minimum-variance CMB map shows a significant temperature decrement at the stacked location of these massive systems in both tests, and the results from tSZ/CIB-nulled maps are consistent with zero. At first glance, the significant decrement in the stack in the tSZ-nulled map may indicate a problem in this map. However, we note that owing to noise bias in the tSZ selection we would not have expected complete cancellation in the tSZ-nulled CMB map. Recall the CIB is one of the dominant sources of astrophysical noise in the SPT maps at small scales (Reichardt et al. 2021) and indeed a stack of the SPT 220 GHz maps (whose effective frequency is at the tSZ null, Section 2.1.4) shows a small, but significant, average temperature decrement, demonstrating that the SPT-SZ cluster detection is slightly biased to areas with lower levels of CIB. Based on the weights in the CMB/kSZ two-component map (Figure 1) we would expect a slight temperature decrement to remain at the location of SPT-selected clusters.

The best way to robustly test these maps is with a large cluster sample selected independently of any signal in the millimeter-wave maps. In lieu of such a sample, we perform a much more restricted test using optically selected clusters from the Blanco Cosmology Survey as presented in Bleem et al. (2015a). Stacking a sample of 169 lower-mass clusters at $0.25 < z < 0.7$ with optical richness $\lambda > 25$, we find a 7σ temperature decrement in the minimum-variance CMB maps ($-1.3 \pm 0.2 \times 10^{-6} \mu\text{K}\text{-sr}$) and no significant detection in the other two maps ($0 \pm 6 \times 10^{-7} \mu\text{K}\text{-sr}$ and $2 \pm 3 \times 10^{-6} \mu\text{K}\text{-sr}$ in the tSZ- and tSZ/CIB-nulled maps respectively). Up to its limited statistical constraining power, this test demonstrates the efficacy of tSZ removal in the tSZ-nulled map; we note that much more constraining tests will soon become possible with the release of eROSITA (Merloni et al. 2012) and Dark Energy Survey (Flaugher et al. 2015) Year 3 cluster samples.

6. Summary

In this work we have presented new CMB/kSZ and Compton- γ component maps from combined SPT-SZ and

Planck data. These maps, which cover 2442 deg^2 of the southern sky, represent a significant improvement over previous such products available in this region by virtue of their higher angular resolution ($1'.25$ and $1'.75$ for the minimum-variance and component-nulled products, respectively) and lower noise at small angular scales. We have detailed the construction of these maps via the linear combination of individual frequency maps from the two experiments, including our technique for limiting the correlation of our lowest-variance Compton- γ map products with the CIB. The new component maps and associated data products, as well as the individual frequency maps from SPT-SZ used to construct these maps, are publicly available at http://pole.uchicago.edu/public/data/sptsz_ymap and the NASA/LAMBDA website.

We have performed several validation tests on the component maps. Our analysis of the CMB-CIB-nulled Compton- γ map power spectrum shows good agreement with expectations from our adopted sky model. A “blind” tSZ cluster search using matched-filter techniques demonstrated the expected performance relative to such searches in SPT and Planck data alone. Finally, a validation test of our tSZ component nulling in the CMB/kSZ maps via stacking such maps at the location of massive SZ clusters demonstrated effective removal of the tSZ signal.

This paper represents the first release of Compton- γ and CMB/kSZ component maps from the SPT collaboration. We expect these maps—in combination with current surveys such as the Dark Energy Survey (Flaugher et al. 2015) and eROSITA (Predehl et al. 2010; Merloni et al. 2012); and near-future galaxy surveys like LSST (LSST Science Collaboration et al. 2009), Euclid (Amendola et al. 2018), and SPHEREx (Doré et al. 2014)—to provide powerful constraints on both cosmology and the evolution of the gas properties of galaxies, groups, and clusters across cosmic time. As detailed in this work, both high-resolution and high-frequency measurements are critical for improving the quality of such component maps. Such measurements will be available in the coming years by the inclusion of low-noise 95, 150, and 220 GHz data from the ongoing SPT-3G (Benson et al. 2014) and Advanced ACTPol (Henderson et al. 2016) experiments, and even wider frequency coverage from future CMB experiments (Simons Observatory Collaboration 2019; CMB-S4 Collaboration et al. 2019).

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Appendix A Data Products

We provide the following data products and instructions for their use at http://pole.uchicago.edu/public/data/sptsz_ymap and the NASA/LAMBDA website.

1. Minimum-variance Compton- y maps and null noise maps at 1’25 resolution. We provide maps in both HEALPix ($N_{\text{side}} = 8192$) and flat-sky (0’25 pixelation) format.
2. CMB-CIB-nulled and CMB-nulled Compton- y full and half maps at 1’75 resolution. HEALPix and flat-sky format.
3. tSZ-CIB-nulled and tSZ-nulled CMB/kSZ full and half maps at 1’75 resolution. HEALPix and flat-sky format.
4. Point-source masks and dust masks.
5. SPT-SZ frequency maps, PSDs, bandpasses, and transfer function plus beam estimates for the SPT-SZ maps used to construct the component maps in this work.

Appendix B Derivation of the Optimal Linear Combination

In this appendix, we provide an alternate derivation of the result that Equations (3), (4), and (5) represent, under the assumptions detailed in Section 3, the minimum-variance unbiased estimate of a map of signal S with SED f from individual frequency maps. As discussed in that section, we model the data in observing frequency ν_i toward sky direction \mathbf{n} as contributions from the signal of interest S and noise (including instrumental and astrophysical noise and astrophysical signals other than S). Ignoring the beam and transfer function for now, we write

$$T(\nu_i, \mathbf{n}) = f(\nu_i) S(\mathbf{n}) + n(\nu_i, \mathbf{n}) \quad (\text{B1})$$

or, assuming pixelized data and using Roman indices for observing bands and Greek indices for map pixels:

$$T_{i\alpha} = f_i S_\alpha + n_{i\alpha} \quad (\text{B2})$$

Adapting the derivation of Haehnelt & Tegmark (1996), we note that the most general linear estimator for S using the data from the individual maps is

$$\bar{S}(\mathbf{n}) = \sum_i \int W_i(\mathbf{n} - \mathbf{n}') T(\nu_i, \mathbf{n}') d^2x', \quad (\text{B3})$$

or

$$\bar{S}_\alpha = \sum_{i,\beta} W_{i\alpha\beta} T_{i\beta}. \quad (\text{B4})$$

We require that \bar{S}_α be an unbiased estimate of S_α :

$$b_\alpha = \langle \bar{S}_\alpha - S_\alpha \rangle = 0, \quad (\text{B5})$$

and we wish to minimize the variance

$$\sigma^2 = \left\langle \sum_{\alpha,\beta} (\bar{S}_\alpha - S_\alpha)(\bar{S}_\beta - S_\beta) \right\rangle. \quad (\text{B6})$$

If the noise in each map has zero mean ($\langle n_{i\alpha} \rangle = 0$), then

$$b_\alpha = \sum_{i,\beta} W_{i\alpha\beta} f_i S_\beta - S_\alpha, \quad (\text{B7})$$

where

$$\sigma^2 = \sum_{\alpha,\beta} b_\alpha b_\beta + \sum_{i,j,\alpha,\beta,\gamma,\delta} W_{i\alpha\gamma} W_{j\beta\delta} \langle n_{i\gamma} n_{j\delta} \rangle. \quad (\text{B8})$$

Using the Lagrange multiplier λ_α to enforce the constraint $b = 0$, we minimize the variance by taking the functional derivative with respect to $W_{i\alpha\beta}$ of the quantity

$$L = \sigma^2 + \sum_\alpha \lambda_\alpha b_\alpha \quad (\text{B9})$$

and setting the result to zero. Even without solving for λ_α , we see that, up to an overall constant, the contribution to the optimal estimator S_α from the map at each individual frequency is simply the tSZ sensitivity weighted by the inverse band–band–pixel–pixel noise covariance matrix:

$$W_{i\alpha\beta} \propto \sum_j \langle n_{i\alpha} n_{j\beta} \rangle^{-1} f_j, \quad (\text{B10})$$

and the proportionality constant is easily obtained by enforcing Equation (B5), yielding

$$W_{i\alpha\beta} = \frac{\sum_j \langle n_{i\alpha} n_{j\beta} \rangle^{-1} f_j}{\sum_{i,j} \langle n_{i\alpha} n_{j\beta} \rangle^{-1} f_i f_j}. \quad (\text{B11})$$

If the various sources of noise in the individual maps can be modeled as Gaussian, random, statistically isotropic fields, then the spherical harmonic transform (or two-dimensional Fourier transform, in the flat-sky limit) of the pixel–pixel–band–band covariance matrix will be diagonal along the spatial frequency direction:

$$\begin{aligned} \text{SHT}\{\langle n_{i\alpha} n_{j\beta} \rangle^{-1}\} &\equiv \langle n_{i\ell} n_{j\ell'} \rangle^{-1} \\ &= C_{\ell j}^{-1} \delta_{\ell\ell'}, \end{aligned} \quad (\text{B12})$$

where $C_{\ell j}$ is the spatial power spectrum of the noise in band ν_i if $j = i$ and the cross-spectrum of the noise in bands ν_i and ν_j if $j \neq i$. In this case, we can rewrite Equation (B4) as

$$\bar{S}_\ell = \sum_i W_{i\ell} T_{i\ell}, \quad (\text{B13})$$

where $T_{i\ell}$ is the spherical harmonic transform (SHT) of the map in band ν_i , \bar{S}_ℓ is the SHT of the estimated Compton- y map, and

$$W_{i\ell} = \frac{\sum_j C_{\ell j}^{-1} f_j}{\sum_{i,j} C_{\ell j}^{-1} f_i f_j}. \quad (\text{B14})$$

Equation (4) is the flat-sky, anisotropic version of Equation (B14), including the beam and transfer function in f , such that $f(\nu_i) \rightarrow f(\nu_i)R(\nu_i, \mathbf{I})$.

Appendix C

Equivalence to Other Formulations

Equation (3) in Madhavacheril et al. (2020), as derived in, e.g., Remazeilles et al. (2011a), gives the following expression for the optimal band weights for one-signal component $a(\nu)$ while explicitly nulling another signal component $a'(\nu)$:

$$w_i = \frac{(a'_j C_{jk}^{-1} a'_k) a_j C_{ji}^{-1} - (a_j C_{jk}^{-1} a'_k) a'_j C_{ji}^{-1}}{(a_j C_{jk}^{-1} a_k) (a'_j C_{jk}^{-1} a'_k) - (a_j C_{jk}^{-1} a'_k)^2}. \quad (\text{C1})$$

In this expression, summing over repeated indices is assumed, and the ℓ subscript has been omitted. Adopting this convention and, as in the previous appendix, ignoring beam and transfer function effects for simplicity, we can write Equation (7) (our expression for multicomponent weights) as

$$\psi_{ij} \equiv \psi_i(\nu_j) = [f^T N^{-1} f]_{ik}^{-1} [f^T N^{-1}]_{kj}. \quad (\text{C2})$$

(Incidentally, this is immediately recognizable as the solution to the least-squares problem, with f as the design matrix and N as the covariance matrix.) For the specific case of two components, we can rewrite f and ψ as

$$f_{ij} \equiv f_i(\nu_j) = \begin{bmatrix} a(\nu_j) \\ a'(\nu_j) \end{bmatrix} \equiv \begin{bmatrix} a_j \\ a'_j \end{bmatrix} \quad (\text{C3})$$

$$\psi_{ij} \equiv \psi_i(\nu_j) = \begin{bmatrix} w(\nu_j) \\ w'(\nu_j) \end{bmatrix} \equiv \begin{bmatrix} w_j \\ w'_j \end{bmatrix}. \quad (\text{C4})$$

Also adopting C for the band-band covariance (as opposed to N), we can write $f^T N^{-1} f$ as

$$[f^T N^{-1}]_{ij} \equiv [f^T C^{-1}]_{ij} = \begin{bmatrix} a_k C_{kj}^{-1} \\ a'_k C_{kj}^{-1} \end{bmatrix}, \quad (\text{C5})$$

and write $f^T N^{-1} f$ as

$$[f^T N^{-1} f]_{ij} \equiv [f^T C^{-1} f]_{ij} = \begin{bmatrix} a_k C_{km}^{-1} a_m & a_k C_{km}^{-1} a'_m \\ a'_k C_{km}^{-1} a_m & a'_k C_{km}^{-1} a'_m \end{bmatrix}, \quad (\text{C6})$$

Inverting this by hand (and noting that C is symmetric) yields




















$$[f^T C^{-1} f]_{ij}^{-1} = \frac{1}{(a_k C_{km}^{-1} a'_m) (a'_k C_{km}^{-1} a_m) - (a_k C_{km}^{-1} a_m)^2} \times \begin{bmatrix} a_m C_{km}^{-1} a'_m & -a_k C_{km}^{-1} a'_m \\ -a_k C_{km}^{-1} a'_m & a_k C_{km}^{-1} a_m \end{bmatrix}, \quad (\text{C7})$$

and applying the result to Equation (C6) yields

$$\begin{bmatrix} w_j \\ w'_j \end{bmatrix} = \frac{1}{(a_k C_{km}^{-1} a_m) (a'_k C_{km}^{-1} a'_m) - (a_k C_{km}^{-1} a_m)^2} \times \begin{bmatrix} (a'_k C_{km}^{-1} a'_m) a_k C_{kj}^{-1} - (a_k C_{km}^{-1} a'_m) a'_k C_{kj}^{-1} \\ (a_k C_{km}^{-1} a_m) a'_k C_{kj}^{-1} - (a_k C_{km}^{-1} a'_m) a_k C_{jk}^{-1} \end{bmatrix}, \quad (\text{C8})$$

the top row of which is recognizable as Equation (C1) or Equation (3) in Madhavacheril et al. (2020).

ORCID iDs

L. E. Bleem  <https://orcid.org/0000-0001-7665-5079>
T. M. Crawford  <https://orcid.org/0000-0001-9000-5013>
B. Ansarinejad  <https://orcid.org/0000-0002-6443-3396>
B. A. Benson  <https://orcid.org/0000-0002-5108-6823>
S. Bocquet  <https://orcid.org/0000-0002-4900-805X>
J. E. Carlstrom  <https://orcid.org/0000-0002-2044-7665>
C. L. Chang  <https://orcid.org/0000-0002-6311-0448>
R. Chown  <https://orcid.org/0000-0001-8241-7704>
M. A. Dobbs  <https://orcid.org/0000-0001-7166-6422>
W. B. Everett  <https://orcid.org/0000-0002-5370-6651>
E. M. George  <https://orcid.org/0000-0001-7874-0445>
N. W. Halverson  <https://orcid.org/0000-0003-2606-9340>
G. P. Holder  <https://orcid.org/0000-0002-0463-6394>
A. T. Lee  <https://orcid.org/0000-0003-3106-3218>
D. P. Marrone  <https://orcid.org/0000-0002-2367-1080>
S. S. Meyer  <https://orcid.org/0000-0003-3315-4332>
L. M. Mocanu  <https://orcid.org/0000-0002-2416-2552>
J. J. Mohr  <https://orcid.org/0000-0002-6875-2087>
S. Raghunathan  <https://orcid.org/0000-0003-1405-378X>
C. L. Reichardt  <https://orcid.org/0000-0003-2226-9169>
E. Shirokoff  <https://orcid.org/0000-0002-2757-1423>
A. A. Stark  <https://orcid.org/0000-0002-2718-9996>
J. D. Vieira  <https://orcid.org/0000-0001-7192-3871>

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