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# **Authors**

Kasen, Daniel Nugent, Peter Wang, Lifan <u>et al.</u>

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# ANALYSIS OF THE FLUX AND POLAR ZATION SPECTRA OF THE TYPE TA SUPERNOVA SN 2001EL: EXPLORING THE GEOMETRY OF THE HIGH-VELOCITY EJECTA

Daniel Kasen<sup>1</sup>, Peter Nugent<sup>1</sup>, Lifan Wang<sup>1</sup>, DA. Howell<sup>1</sup>, J. Craig Wheeler<sup>2</sup>, Peter Hoflich<sup>2</sup>, Dietrich Baade<sup>3</sup>, E. Baron<sup>4</sup>, P.H. Hauschildt<sup>5</sup> dnkasen@panisse.lblgov Draft version November 20, 2016

# ABSTRACT

SN 2001el is the rst norm al Type Ia supernova to show a strong, intrinsic polarization signal. In addition, during the epochs prior to maximum light, the CaII IR triplet absorption is seen distinctly and separately at both norm alphotospheric velocities and at very high velocities. The high-velocity triplet absorption is highly polarized, with a di erent polarization angle than the rest of the spectrum. The unique observation allow sus to construct a relatively detailed picture of the layered geom etrical structure of the supernova ejecta: in our interpretation, the ejecta layers near the photosphere (v 10:000 km s<sup>1</sup>) obey a near axial symmetry, while a detached, high-velocity structure (v 18;000 25;000 km s<sup>1</sup>) with high CaII line opacity deviates from the photospheric axisymmetry. By partially obscuring the underlying photosphere, the high-velocity structure causes a more incomplete cancellation of the polarization of the photospheric light, and so gives rise to the polarization peak and rotated polarization angle of the high-velocity IR triplet feature. In an e ort to constrain the ejecta geom etry, we develop a technique for calculating 3-D synthetic polarization spectra and use it to generate polarization pro les for several param eterized con gurations. In particular, we exam ine the case where the inner ejecta layers are ellipsoidal and the outer, high-velocity structure is one of four possibilities: a spherical shell, an ellipsoidal shell, a clum ped shell, or a toroid. The synthetic spectra rule out the spherical shell model, disfavor a toroid, and nd a best t with the clum ped shell. We show further that di erent geom etries can be more clearly discrim inated if observations are obtained from several di erent lines of sight. Thus, assuming the high velocity structure observed for SN 2001el is a consistent feature of at least a known subset of type Ia supernovae, future observations and analyses such as these m ay allow one to put strong constraints on the ejecta geometry and hence on supernova progenitors and explosion mechanisms.

#### 1. introduction

#### 1.1. Spectropolarim etry of Supernova

The geom etrical structure of supernova ejecta, as determined empirically from observations, can give in portant clues as to the nature of the supernova progenitor system and explosion physics. Spectropolarim etry is a crucial tool in constraining the shape of unresolved supernovae. The scattering atm ospheres found in supernovae can linearly polarize light. For an unresolved, spherically symmetric system the dierently aligned polarization vectors around the disk will cancel, resulting in zero net polarization. If the symmetry around the line of sight is broken, how ever, a net polarization can result due to incom plete cancellation of polarization vectors (Shapiro & Sutherland 1982).

The polarization observations of SN 2001elpresented in W ang et al. (2002) (hereafter Paper I) are the rst observations of a spectroscopically norm al Type Ia supernova (SN Ia) which show a signi cant intrinsic polarization signal. M ost previous observations of SN Ia showed no observable polarization, given the signal-to-noise of the observations (W ang et al. 1996). The only other indication of a clear non-zero polarization in a SN Ia was the sublum inous and spectroscopically peculiar SN Ia 1999by, which show ed an intrinsic continuum polarization of about 0.7% (H ow ell et al. 2001). Chem ical inhom ogeneities were also suggested to explain the rather noisy polarization data of SN 1996x (W ang et al. 1997). In addition, strong intrinsic polarization has been m easured in all types of core collapse supernovae (W ang et al. 1996).

A non-zero intrinsic polarization m easurem ent indicates that a supernova is aspherical, but using the spectropolarim etry to constrain the supernova geom etry usually requires theoreticalm odeling. The detailed theoretical studies so far have been con ned to axisymmetric con gurations. Shapiro & Sutherland (1982) rst estimated the continuum polarization expected from an ellipsoidal, electron scattering supernova atm osphere. Ho ich (1991) used a Monte Carlo code to calculate the continuum polarization from several axisymmetric con gurations, including an o -center energy source embedded in a spherical electron scattering envelope. Calculations of synthetic supernova polarization spectra have also been performed, but usually only for the ellipsoidal geometries (see however Chugai (1992)). In the past, such ellipsoidal models have done a fair job in thing gross characteristics of the available spectropolam etric observations, for example those of SNe 1987A (Je rey 1991), 1993J (Ho ich et al. 1996) and

<sup>&</sup>lt;sup>1</sup> Law rence Berkeley National Laboratory, Berkeley, CA 94720

<sup>&</sup>lt;sup>2</sup> Departm ent of A stronom y, U niversity of Texas at Austin, Austin, TX 78712

<sup>&</sup>lt;sup>3</sup> European Southern Observatory, Karl-Schwarzschild-Strasse 2, D-85748 Garching, Germany

<sup>&</sup>lt;sup>4</sup> Departm ent of Physics and Astronom y, University of Oklahom a, Norm an, OK 73019

<sup>&</sup>lt;sup>5</sup> Departm ent of Physics and Astronom y and Center for Sim ulational Physics, University of Georgia, Athens, GA 30602

SN 1999by (Howellet al. 2001).

SN 2001el presents an exciting development in that no axially symmetric geometry is able to account entirely for the spectropolametric observations. In particular, we suggest that the supernova ejecta consists of nearly axially-symmetric inner layers (v. 15;000 km s<sup>1</sup>), surrounded by a detached, high-velocity structure (v. 20;000 25;000 km s<sup>1</sup>) with a di erent orientation. The analysis of the system therefore requires that we consider the synthesis of polarization spectra for 3-D con gurations.

In this paper we take an empirical approach, and use a param eterized model to try to extract as much model independent inform ation about the high velocity structure in SN 2001el as the observations will perm it. A unique 3-D reconstruction of the geometry is not possible, as this constitutes a kind of ill-posed inverse problem . However, by restricting our attention to various param eterized system s, we can draw som e rather general conclusions about the viability of di erent geom etries. In particular, we exam ine the case where the inner ejecta layers are ellipsoidal and the outer, high-velocity structure is one of four possibilities: a spherical shell, an ellipsoidal shell, a clum ped shell, or a toroid. We develop a technique for calculating 3-D synthetic polarization spectra of the high velocity material. The synthetic spectra rule out the spherical shell model, disfavor a toroid, and nd a best twith the clum ped shell.

Geometrical information extracted empirically from spectropolarim etry must eventually be compared to detailed multi-dim ensional explosion models. A sofyet, none of the computed explosion models appear directly applicable to SN 2001el. 3-D de agration models of a SN Ia in the early phases have been computed by Khokhlov (2000) and Reinecke et al. (2002). These models show a quite inhom ogeneous chem ical structure, with large plum es of burned m aterial extending into unburned m aterial. So far the calculations only cover the early stages of the explosion, before free expansion is reached. It is possible that at som e point the de agration transitions into a detonation wave (Khokhlov 1991). The detonation may smooth out the inhom ogeneities in the chem ical composition by burning away the unburnt material between the plumes (Ho ich et al. 2002; Khokhlov 2000). It could also introduce a globalasym metry if it occurs at an o -center point (Livne 1999). Other possible sources of asymmetry include rapid rotation of a white dwarfprogenitor (M aha y & Hansen 1975), and the binary nature of the progenitor system (Marietta et al. 2000).

#### 12. Supernova SN 2001el

M onard (2001) discovered SN 2001el in the galaxy NGC 1448. The brightness of this nearby supernova ( $m_B$  12 at peak) m ade it an ideal candidate for spectropolarim etry. Spectropolam etric observations were taken on Sept 25, Sept 30, O ct 9 and N ov 9 of 2001. D etails on the observations and the data reduction of the spectra analyzed in this paper can be found in Paper I.

In Figure 1a we show the ux spectrum of SN 2001el for the rst epoch (we have rem oved the redshift due to the peculiar velocity of the host galaxy). The ux spectrum of SN 2001el resembles the norm al SN Ia SN 1994d at about 7 days before m axim um light, with the expected P-Cygni features due to Si II, S II, Ca II and Fe II (see e.g. B ranch et al. (1993)). The blueshifts of the m inim a of these features can be used to estimate the photospheric velocities of SN 2001el, which for all features are found to be  $v_{\rm ph}$  10;000 km s<sup>1</sup>. The only truly unusual feature of the ux spectrum is a strong absorption near 8000 A, which is discussed in detail below.

W e concentrate our analysis on the earliest spectrum (Sept.25), of SN 2001el. A full description of the ux and polarization spectra at all epochs is given in Paper I.

# 1.3. High Velocity Material in SNe Ia

The most interesting feature of SN 2001el is the strong absorption feature near 8000 A. The absorption has a \double-dipped" pro le, consisting of two partially blended m inim a separated by about 150 A. It seems to be a pure absorption feature with no obvious emission com ponent to the red. The feature is still strong on Sept 30, but has weakened considerably by 0 ct 9. By the N ov 9 observations, the 8000 A feature has virtually disappeared (see P aper I).

Hatano et al. (1999) identi ed a much weaker 8000 A feature in SN 1994D as a highly blueshifted Ca II IR triplet. The double-dipped pro le now visible in the Sept 25 SN 2001el spectrum supports this conclusion. The redm ost line of the triplet ( 8662) produces the red-side m inin um while the two other triplet lines ( 8542 & 8498) blend to produce the blue-side m in im um . The synthetic spectra to be presented in x4 con m that the IR triplet can reproduce the shape of the double m in im um . Unfortunately, the early spectra do not extend far enough to the blue to observe a corresponding high velocity component to the Ca II H&K lines. We have investigated all other potential lines that m ight have caused the 8000 A feature, but none were able to reproduce the feature without producing another unobserved line signature som ew here else in the spectrum .

A dopting the IR triplet identi cation for the 8000 A feature, the implied calcium line of sight velocities span the range 18;000 25;000 km s<sup>1</sup>. This should be contrasted with the photospheric velocity of 10,000 km s<sup>1</sup> as measured from the normal SN Ia features in SN 2001el. We therefore make the distinction between the photospheric material, which gives rise to a seemingly normal SN Ia spectrum (hereafter, the \photospheric spectrum "), and the high velocity m aterial (HVM), which produces the unusual8000 A IR triplet feature. In the ux spectrum, there is a clear separation between the photospheric triplet absorption at 8300 A and the HVM feature at 8000 A. In the polarization spectrum, the angle and degree of polarization of the 8000 A feature each dier from the photospheric spectrum. Both of these imply a rather sudden change of the atm ospheric conditions in the HVM .

A high velocity C aII IR triplet feature has been observed in other SN e Ia, albeit rarely and never as strong. The prem ax spectra of SN 1994D (P atat et al. 1996; M eikle et al. 1996), show a sim ilar, but m uch weaker absorption. The SiII and Fe II lines of these spectra also suggest som e m aterial is m oving faster than 25,000 km s<sup>1</sup> (H atano et al. 1999) The earliest spectrum of SN 1990N at day -14 (Leibundgut et al. 1991) has a deep, rounded 8000 A feature, and the spectrum also showed evidence of high velocity silicon or carbon (Fisher et al. 1997). The 8000 A feature has also been observed in the maximum light spectrum of SN 2000cx (Li et al. 2001). In this case, however, the line widths are narrower and the two minima are almost com pletely resolved.

In SN 2001el, the only clear-cut evidence for high velocity material seems to be the 8000 A feature. There is no strong Si II 6150 absorption at v > 20;000, although a weak absorption cannot be nuled out because at this wavelength (5880 A) it would blend com pletely with the neighboring Si II 5958;5979 feature. There is also no clear indication of high velocity Fe II or S II. The blue edge of the Ca II H&K feature on Oct. 9 { the rst available spectrum to go far enough to the blue { is at 27,000 km s<sup>1</sup>. The likelihood of this being HVM is suspect because of the strong possibility of line blending. Since the 8000 A feature is the only unam biguous detection of a high velocity material in SN 2001el, we hereafter refer to it as the HVM feature.

O ur analysis will focus almost entirely on the 8000 A HVM feature. In x2 we give an introduction to polarization in supernova atmospheres; x3 describes a param eterized model that allows us to generate synthetic polarization spectra, and in x4 we use the model to explore various geom etries for SN 2001el. In x5 we consider the signature of each geom etry when viewed from alternative lines of sight. The implication of these constraints on the progenitors and explosion mechanisms of SN e Ia's is discussed brie y in the conclusion.

#### 2. supernova spectropolarimetry

# 2.1. Polarization Basics

The polarization state of light describes an anisotropy in the time-averaged vibration of the electric eld vector. A beam of radiation where the electric eld vector vibrates in one speci c plane is completely (or fully) linearly polarized. A beam of radiation where the electric eld vector vibrates with no preferred direction is unpolarized. Im agine holding a polarization lter in front of a completely linearly polarized light beam of intensity  $\rm I_0$ . The lter only transmits the component of electric eld parallel to the lter axis. Thus as the lter is rotated, the transmitted intensity, which is proportional to the square of the electric eld, varies as I ( ) =  $\rm I_0 \cos^2$ .

The light measured from astrophysical objects is the superposition of many individual waves of varying polarization. Imagine a light beam consisting of the super-position of two completely linearly polarized beam s of intensity  $I_0$ , and  $I_{90}$ , whose electric eld vectors are oriented 90 to each other. If the beam s add incoherently, the transmitted intensity is the sum of each separate beam intensity:

$$I() = I_0 \cos^2 + I_{0} \cos^2 (+90) = I_0 \cos^2 + I_{0} \sin^2$$
(1)

If the beam s are of equal intensity,  $I_0 = I_{90}$ , then the transmitted intensity shows no directional dependence upon

{ i.e. the light is unpolarized. In this sense, we say that the polarization of a light beam is \canceled" by an equal intensity beam of orthogonal { or \opposite" { polarization. If  $I_0 \notin I_{90}$  the cancellation is incomplete, and the beam is said to be partially polarized. The degree of polarization P is de ned as the maximum percentage change

of the intensity; in this case:

$$P = \frac{(I_0 \quad I_{90})}{I_0 + I_{90}}$$
(2)

The polarization position angle (labeled  $\$ ) is de ned as the angle at which the transmitted intensity is maximum .

It is tempting to think of the polarization as a (two dimensional) vector, since it has both a magnitude and a direction. Actually the polarization is a percent di erence in intensity, and intensity is the square of a vector (the electric eld). The polarization is actually a quasivector, i.e. polarization directions 180 (not 360) apart are considered identical. The additive properties of the polarization thus di er slightly from the vector case, as evidenced by the fact that the polarization is canceled by another equal beam oriented 90 to it, rather than one at 180 as in vector addition.

In this case, a useful convention for describing polarization is through the Stokes Param eters, I;Q and U, which m easure the di erence of intensities oriented 90 to each other. A Stokes \Vector" can be de ned and illustrated pictorially as:

$$I = Q = I_0 \qquad I_{45} \qquad I = I_{45} \qquad I$$

where  $I_{90}$ , for instance, designates the intensity m easured with the polarizing liter oriented 90 to a speci ed direction called the polarization reference direction. To determ ine the superposition of two polarized beam s, one sim ply adds their Stokes vectors. A fourth Stokes parameter V m easures the excess of circular polarization in the beam. Non-zero circular polarization has not been m easured in supernova, and no circular polarization observations were taken for SN 2001el; therefore we will not discuss Stokes V in this paper. For scattering atm ospheres without m agnetic elds, the radiative transfer equation for circular polarization separates from the linear polarization equations, allow ing us to ignore V in our calculations (C handrasekhar 1960).

W e further de ne the fractional polarizations: q = Q = I and u = U = I. The degree of polarization, P, and the position angle can then be written in terms of the Stokes P aram eters:

$$P = \frac{p}{\frac{Q^2 + U^2}{I}} = \frac{p}{q^2 + u^2}$$

$$= \frac{1}{2} \tan^{-1} (U = Q) = \frac{1}{2} \tan^{-1} (u = q)$$
(4)

A single plot that captures both the change of polarization degree and position angle over a spectrum is the q-u plot of Figure 2. Each point in this gure is a wavelength element of the spectrum, and for each point we can read o P and at that wavelength much as we would read a polar plot. A coording to Equation 4, the degree of polarization P is given by the distance of the point from the origin, while the position angle is half that of the plot's polar angle. In this sense q and u can be thought of as the two components of a two dimensional polarization quasi-vector.

#### 2.2. Polarization in Supernova Atmospheres

The major opacities in a supernova atmosphere are due to electron scattering and bound-bound line transitions. The continuum polarization of supernova spectra is attributed to electron scattering. The line opacity can create features (either peaks or troughs) in the polarization spectra.

To understand the polarizing e ect of an electron scattering, note that an electron scatters a fully polarized beam of radiation according to dipole sin<sup>2</sup> angular distribution, where is the anglem easured from the incident polarization direction. Now unpolarized light can be represented by a super-position of two equal intensity, fullypolarized orthogonal beam s. U pon electron scattering, the two di erently oriented beam s get redistributed according to di erently oriented dipole patterns; thus in certain directions they are no longer equal and do not cancel. The scattered light is therefore polarized with the percent polarization depending upon the scattering angle between incident and scattered rays:

$$P = \frac{1 \cos^2}{1 + \cos^2}$$
(5)

Light scattered at 90 is fully polarized, while that which is forward scattered at 180 remains unpolarized. The direction of the polarization is perpendicular to the scattering plane de ned by the incom ing and outgoing photon directions.

D eep enough within the supernova atm osphere, the light becom es unpolarized for two reasons: (1) B elow a certain radius, known as the therm alization depth, the absorptive opacity dom inates the scattering opacity and photons are destroyed into the therm al pool. The energy is subsequently re-em itted as blackbody radiation which, being the result of random collision processes, is necessarily unpolarized. (2) D eep within the atm osphere, the radiation

eld becom es isotropic. Because the radiation incident on a scatterer is then equal in all directions, the net polarization of scattered light will cancel.

The polarization of the radiation occurs above the inner unpolarized depth, where the election scattering opacity dom inates and the radiation eld becomes an isotropic due to the escape of photons out of the supernova surface. We call this region the electron-scattering zone. The surface above the electron scattering zone at which point photons have a high probability of escaping the atm osphere, is the supernova photosphere. Form ation of the well-know P-C ygni line pro les in supernovae is due to line opacity from material primarily above the photosphere. This region is called the line-form ing region.

Figure 3 illustrates how the polarization of specic intensity beams emergent from an spherical, pure electron scattering photosphere m ight bok. The double-arrows indicate the polarization direction of a beam, with the size of the arrow indicating the degree of polarization (not the intensity). Note the following two facts: (1) The polarization is oriented perpendicular to the radial direction. This follows from nature of the anisotropy of the radiation eld. At all points in the atm osphere (except the center) m ore radiation is traveling in the radial direction than perpendicular to it. Because the polarization from electron scattering is perpendicular to the scattering plane, the dom inant scattering of radially traveling light w ill produce an excess of polarization perpendicular to the radial direction. (2) The light from the photosphere lim b is more highly polarized than that from the center. This is because the radiation eld at the lim b is highly anisotropic { i.e. highly peaked in the outward (radial) direction. In addition, photons scattered into the line of sight from the supernova lim b, have generally scattered at angles closer to 90.

If the projection of the supernova along the line of sight is circularly symmetric, as in Figure 3a, the polarization of each emergent specic intensity beam will be exactly canceled by an orthogonal beam one quadrant away. The integrated light from the supernova will therefore be unpolarized. A non-zero polarization m easurem ent dem ands som e degree of asphericity; for example in the ellipsoidal photosphere of Figure 3b, vertically polarized light from the long edge of the photosphere dom inates the horizontally polarized light from the short edge. The integrated speci c intensity of Figure 3b is then partially polarized with q > 0. Because an axisymmetric system has only one preferred direction, symmetry dem ands that the polarization angle is aligned either parallel or perpendicular to the axis of sym m etry, thus u = 0 for the geom etry of Figure 3b.

The e ect of line opacity on the polarization spectrum can be complicated. In general, light resonantly scattered in a line can become polarized in much the same way as described above for electrons. However because random – izing collisions tend to destroy the polarization state of an atom during an atom ic transition, the light scattered from lines in supernova atm ospheres is often assumed to be completely unpolarized (e.g. Ho ich et al. (1996) { we discuss this assumption in more detail in x3.4). In ellipsoidal models, it has been shown that the e ect of depolarizing line opacity is primarily to create a decrease in the level of polarization in the spectrum (Ho ich et al. 1996). Because SN Ia have more lines in the blue, the polarization in such m odels typically rises from blue to red.

In general, how ever, the fact that a line is depolarizing does not m ean it necessarily produces a decrease in the degree of polarization in the spectrum . The actual e ect will depend sensitively upon the geometry of the line opacity and the electron scattering m edium . For example, suppose the electron-scattering regim e is spherical, but in an outer, detached layer there is an asym metric clum p of line optical depth, as shown in Figure 3c. Because the line obscures light of a particular polarization, the cancellation of the polarization of the photospheric speci c intensity beam s will not be complete. The line thus produces a peak in the polarization spectrum and a corresponding absorption in the ux spectrum. We call this e ect of generating polarization features the partial obscuration line opacity e ect or just partial obscuration. In the case of Figure 3c, the clum p prim arily absorbs diagonally polarized light, so we expect the polarization peak to have a dom inant com ponent in the u-direction.

A non-axially symmetric supernova is shown in Figure 3d. The electron scattering medium is ellipsoidal, so the continuum spectrum will be polarized in the q direction. The clump of line opacity, which breaks the axial symmetry, preferentially obscures diagonally polarized light so the line absorption feature will be polarized primarily in the u direction. As we see in the next section, this type of two-axis con guration is a relevant one for SN 2001el.

#### 2.3. The Polarization of SN 2001el

#### 2.3.1. Polarization of The Photospheric Spectrum

The q-u plot of SN 2001el is shown in F igure 2. In order to interpret the intrinsic supernova polarization, one must rst subtract o the interstellar polarization (ISP), caused by the scattering of the radiation o aspherical dust grain along the way to the observer. The ISP has a very weak wavelength dependence, (Serkow skiet al. 1975) and therefore choosing the magnitude and direction of the ISP is basically equivalent to choosing the zero point of the intrinsic supernova polarization in the q-u plane of F igure 2. The particular choice of ISP can dram atically a ect the theoretical interpretation of the polarization data (see Leonard et al. (2000); H ow ell et al. (2001)).

The choice of the ISP that leads to the sim plest theoretical description is shown as the green square in Figure 2. In this case the photospheric part of the spectrum (open circles), apart from som e scatter, draw s out a straight line in the q-u plane { i.e. the degree of polarization changes across the photospheric spectrum but the polarization angle remains fairly constant. This would be the case if all of the photospheric material followed the same axial symmetry. The intrinsic polarization spectrum (i.e. percent polarization versus wavelength) of SN 2001el using this choice of ISP is shown in Figure 1b. The degree of polarization rises from blue to red, as expected in ellipsoidal m odels due to the higher line opacity in the blue. The level of continuum polarization in the red is about 0.4%, and the SiII 6150 line represents a depolarization by about the sam e am ount. M odels of ellipsoidal electron scattering atm ospheres indicate that level of polarization m ay roughly correspond to an deviation from spherical symmetry of about 10% (Ho ich 1991).

A lthough the square in Figure 2 is favored by sim plicity argum ents, it is preferable to make a direct measurem ent of the ISP, if possible. At late epochs it is believed that the supernova ejecta becom es optically thin to electron scattering. The intrinsic supernova continuum polarization would then be zero, and the observed polarization due only to the ISP. Paper I estimated the ISP in this way, using observations taken on Nov 9. Assuming the intrinsic supernova polarization is zero at this time, the determ ined ISP (with an estimated error contour) is shown as the green triangle in Figure 2 . A lthough the ISP thus determ ined is not grossly inconsistent with the simplest choice, it seems to indicate that the polarization zero point lies o of the main q-u line. If this is true, the angle across the photospheric spectrum is no longer constant. The photospheric material approximates an axial symmetry, but an o -axis, sub-dom inant com ponent (e.g. a photospheric clump) must exist to account for the o set of the q-u line.

B ecause the m ain purpose of this paper is to explore the geom etry of the HVM, not the photosphere, we will sim – plify our discussion by ignoring any o -axis photospheric components. We will assume the polarization zero point of the axially-sym m etric component is given by the square and that the photosphere can be approximately modeled as an ellipsoid. A lthough the paricular ISP choice has im – portant im plications for the geom etry of the photospheric

m aterial, it does not greatly a ectour analysis of the  ${\rm H\,VM}$  feature.

# 2.3.2. Polarization of The HVM Feature

The HVM ux absorption feature is associated with a polarization peak in the spectrum (Figure 1b). Unlike the ux absorption pro le, the polarization peak does not show a clear double feature. A lthough the noise of the polarization spectrum makes it di cult to analyze the line pro le, it appears that a peak due to the red triplet line (8662) is absent or suppressed com pared to the blue lines (8498 & 8542).

In Figure 2, the wavelengths corresponding to the HVM feature are shown with closed circles. The HVM polarization angle deviates from the photospheric one, pointing instead mostly in the u-direction. The HVM feature also shows an interesting looping structure { as the wavelength is increased, the polarization moves counterclockwise in the q-u plane. q-u loops" such as these have been observed before, for example in the H-alpha feature of SN 1987A (Cropper et al. 1988).

The dierent polarization angle of the HVM feature means that the geometry of SN 2001el cannot be completely axially symmetric. The Stokes U parameter changes sign upon re ecting the system about the polarization reference axis (see Equation 3) and therefore must be zero for any system with a re ective symmetry, such as the axially-symmetric system of Figure 3b. The non-zero u-polarization can not solely be a kinem atic e ect either, for although the SN ejecta is expanding, the velocity law is supposed to be a spherical, hom ologous one (v / r) which preserves the re ective symmetry. As the supernova expands and evolves the density contours of the system may change as outer layers thin out and revealdi erent parts of the underlying material; however unless the velocity law deviates from homology and shows some preferential direction, the re ective symmetry will always be preserved and we must have u = 0 at all times. In order to get a non-zero u com ponent, we must break the re ective sym metry of the geometry with an o-axis component, such as the clum p of F igure 3d.

A natural explanation of the relatively large degree of polarization and change of polarization angle of the HVM feature is partial obscuration of polarized photospheric light, som ewhat like Figure 3d. We nd in x4 that this interpretation can also account for the q-u loop. In the next section we describe a technique for calculating partial obscuration that allows us to directly compare synthetic polarization spectra to the data. O ther m echanism s could presum ably be invoked to explain the HVM polarization peak, but in this paper we only consider the e ects of partial obscuration.

#### 3. the two-component polarization model

To compute polarization in multi-dimensions most investigators have employed M onte C arb m ethods (C ode & W hitney 1995; W ood et al. 1996; Ho ich 1991). This approach has the bene ts of generality and ease of coding, but with the draw back of extrem e computational expense. A very large number of photons must be followed to escape along each line of sight in order to overcom e the random Poisson noise. This noise must be kept much less than a fraction of a percent in order to confront the small observed polarization levels. It is therefore cum bersom e to use M onte C arlo codes in a param eterized way to explore the huge param eter space available with 3-D geom etries.

In the case of the HVM , a simplication is possible that allows for a much faster and more insightful computation. A ssum ing that the electron densities in the HVM regime are around  $10^7$  cm<sup>3</sup>, the optical depth to electron scattering through the HVM shell is  $_{\rm es}$  =  $n_{\rm e}$   $_{\rm t}R_{\rm sh}$   $10^{-3}$ . Therefore one can ignore electron scattering in the HVM and the radiative transfer problem separates naturally into the two regimes of photosphere and HVM. The photosphere acts as a source of polarized light illum inating a region of basically pure line optical depth in the HVM. A ssum ing the lines are depolarizing, the only e ect of the HVM is to obscure som e of the polarized photospheric light and re-em it som e unpolarized light into the observer's line of sight.

Because the model makes a sharp distinction between an inner polarized source (the photosphere) and an outer line-form ing region (the HVM), we call this approach the two-component model. The model is basically a way to form alize the sim ple pictures of Figure 3. The two-com ponent model is constructed to apply to the detached layers of the HVM . For line form ing material near the photosphere a sharp separation of the two regimes would be articial since electron scattering is not entirely negligible in the line form ing region. Because the two-component model does not account for the multiple scattering between lines and electrons, photospheric spectra synthesized with it m ay be incorrect. On the other hand because the model captures som e of the essential features of various geom etries, som e qualitative insight may still be gained with respect to the lines form ed near the photosphere. As we are only concerned with the HVM in this paper, this is not relevant for the present work.

#### 3.1. The Sobolev Approximation

The Sobolev approximation is a method for computing line formation in atmospheres with large velocity gradients. Sobolev models (under the assumption of a sharp photosphere plus line forming region) have frequently been used to analyze supernova ux spectra. Typically spherical symmetry is assumed (e.g. (Branch et al. 1983; Hatano et al. 1999)) but the method has also been applied in 3D (Thom as et al. 2002). Derivations of the Sobolev method and justication of the approximation in the modeling of supernova atmospheres can be found in (Rybicki & Hum – mer 1978; Castor 1970; Je ery & Branch 1990); here we only quote the important results.

The geom etry used in the models is shown in Figure 4. We use a cylindrical coordinate system, (p; ;z) or alternatively a Cartesian one (x;y;z). In either case the observer line of sight is chosen as the z axis with z decreasing tow and the observer (i.e. the observer is at negative in nity). The polarization reference axis is chosen to lie along the = 0 (or y) direction, which is also the photosphere symmetry axis.

For atm ospheres in general expansion, such as supernovae, the wavelength of a propagating photon is constantly redshifting with respect to the local comoving fram e of reference. The insight behind the Sobolev approximation is that the photon will only interact with a line in the sm all region of the atm osphere where the photon is Doppler-shifted in resonance with the line. The radiative transfer problem then becomes localized to such \resonance regions". Free expansion is established in supernova atm ospheres shortly after the explosion; the veboity vector at a point in the atm osphere is in the radial direction and is given by  $v = (r r_0) = t\hat{r}$ , where r is the radius at time t since explosion, and  $r_0$  is the initial radius which is usually small and can be ignored. Consider a beam of radiation em anating from the photosphere and propagating through this atm osphere in the z direction, at an impact parameter p and azim uthal angle . Such a beam was illustrated pictorially as a double-arrow in Figure 3; here we quantify it with a Stokes speci c intensity vector  $I_0$  ( ;p; ). If the wavelength of the beam in the observer frame is , then the wavelength in the local com oving atm osphere fram e is given by the (non-relativistic) Doppler form ula:

$$l_{\rm loc} = 1 + \frac{\Psi}{c} \frac{\hat{z}}{c} = 1 + \frac{z}{ct}$$
 (6)

Suppose the only opacity in the atm osphere is due to one line with rest wavelength  $_0$ . A beam of radiation will come into resonance with the line when  $_{loc} = _0$ , which by Equation 6 is at a point:

$$z_r = ct(_0 = 1)$$
 (7)

For each wavelength in an observed spectrum there is thus a unique point in the z-direction at which the beam com es in resonance with the line. A coording to the Sobolev approximation, the emergent Stokes speci c intensity I that reaches the observer at in nity after passing through the line form ing region is given by:

I(;p;) =  $I_0$ (;p;) e + (1 e)S(;p;;z\_r) (8) where is the Sobolev line optical depth at the point (p;;z\_r) and S is the Stokes source-function of the line at this point. B oth quantities will be explained further in the sections to come. The rst term in Equation 8 represents photospheric light attenuated by the line optical depth; the second term represents light scattered or created to emerge into the line of sight by the line. Equation 8 is identical to the usual, unpolarized expression for the Sobolev approximation (see Rybicki & Hummer (1978)), except now the terms in boldface are all Stokes vectors.

To generate the observed spectrum of an unresolved object, the speci c intensity of E quation 8 m ust be integrated over the projected surface of the atm osphere, i.e. over the p plane. A wavelength in the observed spectrum thus gives us inform ation about the line optical depth and source function integrated over a plane at  $z_r$ . Such a plane, which is perpendicular to the observer's line of sight, is called a constant-velocity (CV) surface.

In the case of an monotonically expanding atmosphere with more than one line, a beam of radiation will come into resonance with each line one at a time, starting with the bluest line and moving to the red. In this case Equation 8 is readily generalized:

$$I(;p;) = I_{0}(;p;) exp$$

$$i$$

$$i = 1$$

$$X^{N}$$

$$X^{N}$$

$$X^{1}$$

$$S_{i}(;p;) [1 e^{i}] exp$$

$$j$$

$$i = 1$$

$$j = 1$$

$$(9)$$

where the indices i and jrun over the lines from red to blue. Before considering the integration of E quation 9 over the CV planes, we discuss in m ore detail the term s  $\rm I_0$ , S, and

### 3.2. The Photospheric Intensity

In this section we calculate the intensity and polarization of speci c intensity beam s emergent from an electron scattering photosphere. We rst consider  $I_0$  (p; ) in the case that photospheric regime is spherical (as in F igure 3a) and later show how to adapt the result to the ellipsoidal case. From the circular symmetry, the intensity and degree of polarization of a speci c intensity beam can only depend upon the in pact parameter p and not on . Let  $I_z$  (p) represent the speci c intensity in the 2 direction at p, and  $P_z$  (p) the degree of polarization of this beam . The polarized speci c intensity is  $I_z$  (p) $P_z$  (p) which will be divided between the Q and U Stokes parameters.

For = 0, the polarization points in the horizontal, or negative Q direction { i.e. Q (p; = 0) =  $I_z$  (p)P<sub>z</sub> (p) while U (p; = 0) = 0. The Q and U components at arbitrary are derived by rotating this expression by . The resulting Stokes vector is:

The fact that the trigonom etric rotation terms depend on 2 rather than rejects the fact that the polarization is actually a quasi-vector (Chandrasekhar 1960).

In the two-component model one must pre-compute the functions  $I_z(p)$  and  $P_z(p)$ . Chandrasekhar rst obtained the result for a pure electron scattering, plane-parallel atm osphere (C handrasekhar 1960); in that case  $I_z$  (p) follows closely the linear limb darkening law, while the degree of polarization  $P_{z}$  (p) rises from zero in the center to 11:2% at the limb; how ever, the plane-parallel approxim ation is not a good one for supernovae, which have extended atm ospheres (i.e. the thickness of the electron scattering zone is a sizable percentage of its radius). In an extended atm osphere the radiation eld tends tow and a more an isotropic distribution, peaking in the outward direction. This increased an isotropy of the radiation eld leads to generally higher limb polarizations. Cassinelli & Hummer (1971) solved the polarized radiative transfer Equation for extended, spherical electron scattering spheres with density power laws of index n=2.5 and n=3. They nd the polarization can become higher than 50% at the limb.

W e model the photospheric regin e as an inner unpolarized boundary surface, surrounded by a pure electron scattering envelope with a power law electron density / r<sup>n</sup>. W e choose n = 7, a density law motivated by SN Ia explosion models and one that has been often used in direct spectral analysis (N om oto et al. 1984; B ranch et al. 1983). The optical depth (in the radial direction) from the inner boundary surface to in nity is set at  $_{\rm es}$  = 3. The assumption of a pure electron scattering atmosphere should be a good one for the wavelength range we are interested in. The photons that redshift into resonance with the high velocity IR triplet are those with wavelengths from 8000-8500 A, and there are no strong lines or absorptive opacities in this region of the spectrum (see P into & E astm an (2000)). At other wavelengths the presence of additional opacities in the photospheric regime will decrease the polarization from the pure electron scattering results presented here.

U sing a M onte C arlo code, we com puted the functions  $I_z$  (p) and  $P_z$  (p) for the above scenario. Unpolarized photons were emitted isotropically from the inner boundary surface. The polarization of these photons were tracked as they scattered multiple times through the electron scattering zone. Photons that were back-scattered onto the inner boundary surface were assumed to be re-absorbed and were om itted from the calculation. The M onte C arlo code used in this calculation is a new one developed to further study supernova polarization in cases where the twocomponent model is not applicable. A detailed description of the M onte C arlo code will be presented in a future paper. We note that the output has been checked against the results of C handrasekhar (1960) and C assinelli & H um m er (1971), and several other cases including H illier (1994) and the analytic results of Brown & McLean (1977).

The computed functions  $I_z$  (p) and  $P_z$  (p). are shown in Figure 5. Here p is given in units of the photosphere radius, de ned as the radius at which the optical depth to electron scattering equals 1. The intensity and polarization for p < 1 do not diermuch from the plane-parallel case, with  $P_z = 13$ % at p = 1. The photospheric speci c intensity does not, how ever, term inate sharply at the photospheric radius as is usually assumed in Sobolev models; rather a signi cant am ount of light is scattered into the line of sight out to p 1:4. Since this limb light is highly polarized (up to 40%) it is important to include it in our calculations. A ctually most of the polarized ux com es from an annulus at the edge of the photosphere.  $\rm I_z$  (p) has become negligible out at the HVM distances of 2, which con m s that we can m ake a clear separation between the photospheric and HVM regimes.

In Figure 5 we also compare the n = 7;  $_{es} = 3$  results to other models with di ering density laws and optical depths. From the similarity of the n = 7 and n = 5 models in Figure 5a and 5b it is clear that the calculations will not depend sensitively on our choice of power law index. Even if the index were as low as n = 3, (or worse, not even described by a strict power law) the behavior of  $I_z$  (p) and  $P_z$  (p) should still show the same qualitative trends. From Figure 5c and 5d we see the results also do not depend much on  $_{es}$  as long as  $_{es} \& 3$ .

The results given so far have not taken into account the asphericity of the photosphere in SN 2001el. One could redo the M onte C arlo calculations for various axisym m etric con gurations, but the sm all degree of polarization in SN 2001el suggests a rather sm all ( 10%) deviation from spherical symmetry, so it is not a bad approximation to apply the spherically symmetric speci c intensities to a slightly distorted photosphere. This technique of using spherical results to calculate the polarization from distorted atm ospheres has been used, in various manners, by m any other authors (Shapiro & Sutherland 1982; M cC all 1984; Je rey 1991; C assinelli & H aisch 1974).

In ourm odels we will only consider the case of an oblate ellipsoidal atm osphere with axis ratio E and viewed edgeon. We de ne an ellipsoidal coordinate:

$$= \int \frac{p}{x^2 + E^2 y^2}$$
(11)

Our approximation is that the emergent Stokes inten-

sity from a position ; is given by Equation 10 with  $I_z$  (p = ; = ) and  $P_z$  (p = ; = ). In this case we nd an axis ratio of E 0:9 is necessary to produce the 0:4% polarization observed in the red continuum of SN 2001el. This result agrees with previous, 2-D calculations (Je rey 1991; Ho ich 1991).

W hile the above photospheric model provides a sim – ple and rather general description of an axially symmetric photosphere, there is no easy way to assure ourselves that this photospheric model is unique. The actual speci c intensity emergent from an ellipsoidalatm osphere can depend on the depth and shape of the inner boundary surface, as well as the inclination of the system . Moreover, the polarization of the photospheric spectrum of SN 2001el could arise from a di erent kind of asphericity altogether, for instance an o-center N i<sup>56</sup> source, or a clum py atmosphere. In the absence of a single preferred photospheric model, we proceed with the above model, but reiterate that it remains just one of many possible scenarios. O ther choices of  $I_z$  (p; ) and  $P_z$  (p; ) must be investigated on a case by case basis.

# 3.3. The Line Optical Depth

In our synthetic spectra ts, we take the optical depth of the 8542 line, as a free parameter  $_1$ . The optical depths of the other two lines (8662, 8498) are derived from  $_1$ . All three triplet lines come from nearly degenerate lower levels, so in LTE the relative strength of each line depends only upon the weighted oscillator strength gf of the atom ic transition. Even if the level populations deviate from LTE, one expects the deviation to a ect each of the nearly degenerate levels in the same way. The 8542 line has the largest gf value; 8662 is 1.8 tim es weaker, and 8498 10 tim es weaker.

### 3.4. The Line Source Function

The line source function represents light scattered by the line, created from the therm alpool or from NLTE effects. Scattering in a line can polarize light { as in the case of electron scattering, the e ect is due to the anisotropic redistribution of the di erent polarization directions. The angular redistribution depends in general on the angular m om entum J of the upper and low er levels of the atom ic transition.

Ham ilton (Ham ilton 1947) has considered the linear polarization from a resonance line, free from collisions. He showed that the angular redistribution function from such a line could be written as the sum of an isotropic and dipole term, the relative contributions depending upon the angularmomentum of the transition levels. The dipole contribution has exactly the same polarizing elect as an electron scattering, while the isotropic contribution is unpolarized. The nalpolarizing e ect is thus generally diluted as com pared to the electron scattering case, and can be described by a polarizabilty factor W 2, which varies from 0 for a depolarizing line to 1 for a line that polarizes like an electron (Sten o 1994). Because the Ham ilton approach provides a simple prescription for estimating the intrinsic polarizing e ects of line scattered light, it has often been used outside its scope to calculate polarized line pro les for nonresonance lines (Je rey 1991).

The Ham ilton prescription does not take into account

the e ect of collisions. A fler a photon has excited the atom, the atom is in a polarized state with a speci c m agnetic sublevelM. If the collisional time scale is shorter than the lifetime of the transition, collisions will destroy the polarization state of the atom by redistributing the atom over all the nearly degenerate m agnetic sublevels, thereby producing an spherically symmetric con guration. The scattered light will thus be isotropic and unpolarized. This is the assumption m ade in the m odels of H ow ellet al. (2001) (and references therein).

In this paper we use exclusively an isotropic, unpolarized line source function. In addition to the depolarizing e ect of collisions, we suggest two further reasons why the e ect of intrinsic line polarization is likely a small e ect in the case of the HVM feature. (1) If we evaluate the polarizability factor for the lines of the IR triplet we nd that W  $_2$  is almost zero for 8542 (W  $_2$  = 0:02) and exactly zero for 8662. A coording to the Ham ilton prescription, only the 8498 line has a moderate polarizing e ect (W  $_2 = 0.32$ ), but this line is by far the weakest of the three. Note however that since the IR triplet lines are not resonance lines, the Ham ilton prescription does not strictly apply and complicated NLTE polarizing e ects could be operative (Trujillo Bueno & Manso Sainz 1999). (2) For optically thick lines, photons will multiple scatter within a resonance region before escaping. On average the num ber of scatters in the resonance region is given by N =  $1=P_{esc}$ where the escape probability P<sub>esc</sub> is given by the Sobolev formalism :

$$P_{esc} = \frac{1 e}{(12)}$$

This multiple scattering has two depolarizing e ects: (1) the radiation eld in the line tends toward an isotropic distribution (2) the probability of the destruction of a photon into the therm alpool will be increased. For optically thick lines the line-scattered light will then tend to be unpolarized. On the basis of the spectral ts of x4, we will argue that the lines of the IR triplet are saturated ( $_1 \& 5$ ) for the HVM in front of the photosphere and thus largely unpolarized.

For an isotropic, unpolarized source function the Stokes vector is: !!

$$S = \begin{array}{c} S_{1} & S_{0} \\ S = \begin{array}{c} S_{2} & = \\ S_{1} & 0 \end{array}$$
(13)

where  $S_0$  is the unpolarized source function. The actual value of  $S_0$  requires a full NLTE computation of the atom ic levels. For our purposes a useful parameterization is:

$$S_0 = (1 \ ^0)J + \ ^0B (T)$$
 (14)

The rst term represents in pinging light scattered by the line, and so depends upon the mean local radiation eld in the line J; the second term represents light created from the therm al pool and so depends upon the P lanck function B and the temperature T. The relative in portance of the two factors is governed by <sup>0</sup>, the probability a photon is destroyed into the therm al pool on traversing the resonance region of a line. In the Sobolev approximation <sup>0</sup> is given by:

$$^{0} = \frac{1}{P_{esc} + (1 P_{esc})}$$
 (15)

where is the usual static atm osphere destruction probability. In NLTE models of supernova atm ospheres one nds between 0.05 and 0.1 (Nugent 1997). Note as the probability of a photon's escape ( $P_{esc}$ ) decreases, the chances that it gets therm alized (<sup>0</sup>) increases.

For the value of J in the HVM, we use the radiation incident from the photosphere, ignoring multiple scattering of photons between the triplet lines (for a discussion of this approximation, see Thomas et al. (2002)). The photospheric radiation in the HVM is geometrically diluted by a factor of roughly  $r_{ph}^2 = 4 r_{H \ V M}^2$  1=16. Thus for a pure scattering line ( $^0 = 0$ ), the intensity of the line source function is about 16 times weaker than the average photospheric intensity. At the other extreme, for a thermalized line ( $^0 = 1$ ) and an HVM temperature of 5500 K, the line source function is about 4 times weaker than the average photospheric intensity.

B ecause the line source function light is unpolarized and relatively weak, we nd in the end that it has little a ect on the synthetic line proles. The exact value of is thus not of great in portance. In our models, we use = 0.01.

#### 3.5. The Integrated Spectrum

To obtain the observed Stokes uxes at a certain wavelength one must integrate the speci c intensity over the CV planes of each line. For those CV planes behind the photosphere, we must also account for the attenuation of the line source function light due to scattering o electrons as the beam passes through the photospheric region. If we de ne  $_{es}$  (p; ;z) as the electron scattering optical depth along the z-direction from the point (p; ;z) to the observer, then a fraction (1 e  $^{es}$ ) of photons will be scattered out of the line of sight on their way to the observer. We assume these photons are sim ply rem oved from the beam and are not subsequently re-scattered into the line of sight.

For a single line atm osphere, the integrated Stokes uses at wavelength correspond to material from the CV plane  $z_r$  and are given by: 7, 7

$$F_{I}() = I_{z}(p; )e +$$

$$(1 e) S_{0}(p; ;z_{r})e^{es} pdpd$$

$$Z Z$$

$$F_{0}() = P_{z}(p; )I_{z}(p; )\cos(2)e pdpd$$

$$Z Z$$

$$F_{U}() = P_{z}(p; )I_{z}(p; )\sin(2)e pdpd$$

$$(16)$$

The integrals can be easily generalized for the case of multiple lines by applying Equation 9.

Given our scenario of how the high velocity CaII polarization is formed by partial obscuration, Equations 16 give us some insight into what extent the HVM geometry is constrained by the polarization measurements. For sim – plicity, consider the formation of a single, unblended line, above a spherical photosphere, and suppose we are trying to reconstruct the distribution of Sobolev line optical depth (p; ;z) over the entire ejecta volume. The Stokes ux at a certain wavelength gives us information about over the corresponding CV plane at  $z_{\rm r}$ . A s Equations 16 demonstrate we obviously will not be able to uniquely reconstruct the distribution of over this plane, because all of the information gets integrated over to give the three

quantities we measure:  $F_{I}();F_{Q}()$ , and  $F_{U}()$ . W hat we do measure can be thought of as certain \moments" of the distribution over each CV plane.  $F_{I}$  is a type of \zeroth m om ent", which depends mostly upon how much material is covering the photosphere, with little dependence on its geometrical distribution. On the other hand the  $F_{Q}$  and  $F_{U}$ , because of the cos2 and sin2 factors, behave some what like \ rstm om ents", and are sensitive to how is distributed over the photosphere. Because the angle factors cos2; sin2 are rather low-frequency, sm aller scale structures will be averaged out over the integrals, and the polarization measurements will only constrain the large scale structures in the HVM.

Before proceeding with the spectral synthesis calculations let us sum marize the assumptions that go into the two-component model. (1) The electron scattering opacity in the HVM is negligible. (2) the photospheric regime is reasonably well described by a pure electron scattering, power law atmosphere, surrounding a nite, unpolarized source at  $_{\rm es}$  3. (3) For sm all (10 percent) deviations from sphericity in the photosphere, the angular dependence of the polarized radiation eld does not deviate signi cantly from the spherical results (4) The line source function light is unpolarized (5) M ultiple scattering am ong the triplet lines and between the HVM and photospheric regim e can be ignored.

#### 4. the geometry of the high velocity material

The speed of the two-component model allows us to explore many di erent con gurations for the HVM. We report on four possibilities here, each of which may approximate a structure that is the result of some particular physicalmechanism: (1) A spherically symmetric shell (2) A nellipsoidal shell with an axis of symmetry rotated from the photosphere axis of symmetry. (3) A clumped spherical shell (4) A toroidal structure with a symmetry axis rotated with respect to the photospheric axis. The geom – etry used in the models is shown in Figure 4.

The photosphere is modeled as discussed in x3.2, as an oblate ellipsoid with axis ratio E = 0.91, viewed edgeon. It is not the purpose of this paper to explore the detailed geometry of the photosphere, therefore the ellipsoidal model was chosen as the simplest possibility that captures the essential features of the axisym metric photosphere. The photosphere symmetry axis is the y-axis, which is also the polarization reference direction. The photospheric intensity is assumed to follow a blackbody distribution with a tem perature  $T_{bb} = 9000$  K chosen to t the slope of the red continuum . We do not attach any physical signi cance to the value of  $T_{bb}$ , but consider it only a convenient t parameter.

The param eterization of the various HVM geom etries is kept sim ple and general. The HVM is chosen axially sym – m etric, with the orientation of the HVM axis de ned by the two angles and . The velocities y and  $v_2$  denote the inner and outer radial boundaries of the HVM, while is the opening angle (see F igure 4). The reference optical depth  $_1$  of the 8542 line is assumed constant throughout the de ned structure boundaries. A lthough this is an idealization of the real HVM, it allows us to isolate the de ning geom etrical features of each structure individually. Table 1 summarizes the tted param eters of each

HVM geometry considered in the sections to follow. Before considering the speci c models, we rst discuss the general constraints that must be met by any HVM model.

# 4.1. GeneralConstraints

Figure 6 is a diagram of the form ation of the CaII IR triplet feature in SN 2001el. The HVM has for illustration been shown as a spherical shell. The atm osphere can be divided into three regions, the high-velocity material in each region having a di erent a ect on the spectrum . (1) The absorption region: Material in the tube directly in front of the photosphere absorbs photospheric light and em its line source function light into the line of sight. Since the line source function intensity is usually weaker than the photospheric intensity, this e ect produces an absorption feature in the spectrum . (2) The em ission region : m aterial in the outer lobes does not obscure the photosphere but only adds line source function light; this produces an em ission feature to the red of the absorption. (2) The occluded region: Material in the tube behind the photosphere is occluded by the photosphere and is not visible.

Because in our models it is the partial obscuration of polarized photospheric light that gives rise to the HVM polarization feature, all of our geom etrical information on the HVM will be about the distribution of CaII in the absorption region. Whether there is any HVM CaII in the emission region, and if so, what its geom etry may be, will be very di cult to say. In addition we will have absolutely no information about the material in the occluded region. In the spherical HVM shell of Figure 6, about 5% of the material is in the absorption region, 5% is in the occluded region, and 90% is in the emission region. Thus we only probe a small portion of the potential HVM .W e now consider the general constraints of these regions in more detail.

#### 4.1.1. Constraints on the Absorption Region Material

W e can list 4 general constraints on the HVM absorption region m aterial that are directly deducible from the Sept. 25 spectra:

(1) The width of the HVM ux absorption feature constrains  $_1$  to be non-zero only over the line-of-sight velocity range 18;000 25;000 km s<sup>1</sup>.  $_1$  is thus con ned to a relatively thin region that is signi cantly detached from the photosphere. The edges of the ux feature are sharp, suggesting that the boundaries of the HVM are well-de ned.

(2) At them inim um of the HVM absorption the ux has decreased by 43% from the continuum level. For geometries where the HVM covers the entire photosphere, the optical depth in plied is  $(3.0 \text{ n} \text{ the other hand, som e geometries may have higher optical depths and smaller covering factors, the minimal covering factor being <math display="inline">f_{m \ in} = 43\%$  for when the lines are completely opaque. Note that in this context the term \covering factor" denotes the percent of the photospheric area obscured by the slice of HVM on a plane perpendicular to the line of sight, corresponding to the resonance surface of a certain wavelength. Since this di ers from the traditional usage of the term , we hereafter call this the z-plane covering factor.

We can use the double-dipped ux prole to constrain the z-plane covering factor of the HVM .Because the 8542blue triplet line is intrinsically stronger than the 8662 red triplet line (with a gf value 1.8 tim es larger), the blue m inim a of the IR triplet feature will be about twice as deep the red one unless both lines are saturated. Because the m inim a in the HVM feature are of about equaldepth, we conclude that the two lines are indeed saturated (i.e. 1 & 5) and the z-plane covering factor is in fact the m inim alone,  $f_{\rm m\ in}=43\%$ .

(3) The shape of the ux pro lem ay also constrain the value  $_1$ . Note that two m inim a in the ux pro le have roughly equal widths. On the other hand if all three triplet lines are saturated the blue m inim a will tend to be wider than the red, due to the blending of the 8498 with the

8542 line. This suggests that the 8498 line is weak while the other two lines are strong, a situation that occurs when  $1 \quad 5$ .

(4) Finally, the HVM polarization feature points primarily in the u-direction. This means the distribution of the HVM is weighted along the 45 line to the photosphere symmetry axis.

#### 4.1.2. Constraints on the Emission Region Material

The material in the emission region may be observable as a ux emission feature to the red of the HVM absorption. If, for example, the HVM was a spherical shell, this em ission feature would extend from about z =20;000 to z = 20;000, or over 1000 A. The em ission from a shell is then very broad, but because the line source function is much less than the photospheric intensity, the feature is typically weak and di cult to detect in the spectrum . A serious problem, evident from Figure 6, is that the HVM em ission feature overlaps with the photospheric triplet absorption and emission, making it di cult to separate the two contributions. Only for the HVM material with z & 15;000 (i.e. > 8700 A) is the HVM emission feature not blended with the photospheric. Unfortunately the available spectra of SN 2001el do not extend that far to the red.

The emission region material also a ects the polarization level by diluting the photospheric light with unpolarized line source function light, thus creating a depolarization feature in the spectrum . O focurse this depolarization feature gives no additional clue as to the orientation of the emission region material, as the unpolarized line light carries no directional information. The polarization spectrum of SN 2001el does have a signi cant depolarization to the red of the HVM peak, but since the overlapping photospheric triplet feature may also depolarize at these wavelengths, it is again not easy to use this to directly constrain the HVM emission region material. In ourm odels, we do not attempt to t the region redward of 8200 A, where the HVM feature is blended with the photospheric feature.

We nd that the red em ission/depolarization feature is not a very sensitive diagnostic of em ission region m aterial. The e ect on the spectrum is shown in Figure 7 for a spherical shell with various values of the destruction probability . For a pure scattering line (= 0) the em ission is hardly visible. For the therm alized line (= 1) and a tem - perature T = 5500K, the em ission would be substantial but di cult to separate from the photospheric component. A value = 1 is also un likely for supernova atm ospheres; NLTE models nd 0:05.

The best way to constrain the amount of emission region materialis by line of sight variations (see x5). The material in the emission region from one line of sight, becomes material in the absorption region from another. W ith a larger sample of supernovae one may be able to piece together a picture of the entire volume of high velocity ejecta.

### 42. Spherical Shell

The rst HVM geometry we consider is a spherically symmetric shell. We take the boundaries of the spherical shell to be  $v_1 = 20;200 \text{ km s}^1$  and  $v_2 = 25;300 \text{ km s}^1$  in order to reproduce the line width. Because the shell curves around, these dimensions actually give an extension in the z-direction of 18;000 25;000 km s<sup>1</sup>, consistent with constraint (1) of x4.1.1. The z-plane covering factor is found to be 1, and the optical depth necessary to t the line depth  $_1 = 0:77$ .

The triplet lines are not saturated in the spherical shell, so the model does not satisfy constraint (2) of x4.1.1 and willnot well reproduce the ux prole. In Figure 8 we com – pare the synthetic spectra to the observed data. While the overall t of the ux feature is decent, the redside minimum is not well reproduced. We will not better the to the double-dipped prole using non-spherical geometries with smaller z-plane covering factors and saturated lines. Thus the ux spectrum alone suggests a deviation from spherical symmetry, although the evidence is rather subtle.

The e ect of the spherical shell on the polarization is demonstrated by the slice plots of Figure 9. At the blue end of the absorption feature (slice a), the line obscures the weakly polarized, central light, allowing highly polarized, edge light to reach the observer. This creates a peak in the polarization spectrum. Further to the red of the feature (slice b), the line obscures the edge light and thus depolarizes the spectrum. Even further to the red (slice c), the line no longer obscures the photosphere, but the emission region materialemits unpolarized line source function light into the line of sight, and a sm all level of depolarization continues. This polarization feature resembles an inverted P-C ygnipro le, as discussed by Je rey (1989).

In Figure 8b we see that the spherical shell naturally reproduces the correct shape and size of the HVM polarization peak. The fact that the synthetic polarization feature has only a single peak is the result of a line blending e ect: the red-side depolarization of the 8542 feature suppresses the peak due to the 8662 line. Note that while the observed depolarization m inim um near 8400 A is not well t, this is not necessarily a weakness of the m odel. As discussed in x4.1.2 the feature at these wavelengths is produced mostly by the calcium near the photosphere, which has not been included in the m odel. In any case, the spherical shell, which follows the axial symmetry of the photosphere, does not change the polarization position angle as is observed (Figure 8c). This rules it out as a potentialm odel for the HVM.

### 4.3. Rotated Ellipsoidal Shell

The good tto the polarization level in F igure 8 suggests that a shell-like structure may be a viable candidate for the HVM, as long as the shell is somehow distorted from perfect spherical symmetry to account for the rotation of the HVM polarization angle. The simplest scenario is one

where the HVM layers of the ejecta are ellipsoidal with the same oblateness as the photospheric layers, but with a rotated axis of symmetry. Exactly how such a relative rotation of the outer layers could arise from an SN Ia explosion is not obvious. One might envision that the rapid rotation of a white dwarf progenitor coupled with a deagration to detonation transition at an o -center point (Livne 1999) could produce som ething like this geometry.

The e ect of the rotated ellipsoidal shell on the polarization spectrum is demonstrated in the slice plots of Figure 10. The slices closely resemble those of the spherical shell (Figure 9) except that now the cross-sections of the HVM are ellipses. The shape and size of the ux and polarization features are thus very similar to the spherical case. For = 0 (HVM and photosphere axis aligned) the system is axially symmetric and the HVM polarization feature points in the q-direction. As is increased, the ellipses begin to absorb diagonally polarized light and the HVM polarization feature rotates into the u-direction.

The synthetic spectra for = 25;  $_1 = 0.77$  are shown in Figure 11. The ellipsoidal shell, like the spherical one, fails to meet constraint (2) and does not reproduce the double-dipped ux pro le. This problem cannot be xed by changing the ellipticity of the shell. On the other hand, the ellipsoidal shell is able to t the polarization peak and the change of polarization angle.

Even m ore interestingly, the ellipsoidal shell produces a q-u loop sim ilar to that observed in the data. In our m odels, we nd that a q-u loop is a common signature of partial obscuration in two-axis system s. The absorption of the photospheric light typically produces a peak in both the q and u polarization. The partial obscuration e ect on the q and u polarizations is distinct, so that in general these features do not peak at the sam e wavelength, but rather are out of phase. W hen plotted in the q-u plane, this phase o set m akes a loop.

#### 4.4. Clum ped Shell

W e param eterize a clum ped shell as the section of the spherical shell lying within a cone of an opening angle (a \bow l" shaped structure, see Figure 4). A single clum p like this could perhaps arise if the calcium in the HVM was produced by nuclear burning that occurred along a preferential axis. The clum ped shell could also represent one piece of a shell broken into num erous clum ps by an instability, a possibility discussed in m ore detail at the end of this section.

In deciding on the appropriate values for the clum p param eters, we are guided by the constraints listed in x4.1.1. The opening angle is constrained to 25, so as to achieve the m inim alz-plane covering factor (constraint 2). The orientation of the clum p axis is chosen so that the clum p lies in between the observer and the photosphere, obscuring the photosphere's diagonal (constraint 4).

Through trial and error, a reasonable t to the data was found for = 24;  $_1 = 5$ ; = 83:5; = 42 The synthetic spectra are shown in Figure 12. Because the lines are now saturated, the clump is able to reproduce the two equal m inim a of the ux absorption. The clumped shell also reproduces the important features of the polarization spectrum { i.e. the level of polarization, the polarization angle, and the q-u loop. On the other hand, the red edges of the synthetic ux and polarization spectra do not quite m atch the observed. In the polarization spectrum, the peak due to the 8662 feature is not suppressed by blending as it was in the shell m odels. This suggests that our param eterized clum p geom etry m ay be too sim ple and a m ore realistic m odel m ay involve a com plicated superposition of clum ps and shell.

In the geometry described above, the clump axis was chosen almost, but not quite, perpendicular to the photosphere axis ( = 83.5). One might wonder if the two axes could possibly be orthogonal ( = 90). Such a scenario is permissible if the clump axis remains at an angle = 4.2 to the line of sight and the whole system is rotated to be observed at an inclination i = 90 83.5 = 6.5. One might imagine this geometry as a blob of material that was ejected in the equatorial direction of the ellipsoidal photosphere.

A lthough our clum ped shellm odel consists of only a single clump, it is possible that m any m ore clum ps exist in the em ission region of the shell as the extra clum pswould leave no obvious signature on the spectra (see x4.1.2). C lum piness in a shell could be caused by various hydrodynam ical instabilities. The expected scale of such clumpiness is unknown { it could perhaps take the form of a single large clump or it could be in the form of num erous sm aller clumps. As we noted in reference to Equation 16 (see x3.5), the polarization feature due to partial obscuration is not sensitive to small scale structure, giving rather the integrated \m om ents" of the optical depth distribution. Thus we will not be able to empirically constrain the small scale structure of the clum piness. We can say two things though: (1) W hatever the size of the clum ps, their angular distribution must be weighted along the clump axis de ned above. If the clum ps were instead sm all structures distributed uniform ly over the shell, when integrated up they would average out to the uniform spherical shell analyzed in the previous section, which did not show a rotation of the polarization angle. (2) This weighted angular distribution of the clum ps cannot vary in the radial direction. If it did, the polarization angle of the HVM feature { which is set by how ever the random ly placed clum ps happen to be distributed over the photosphere { would vary random ly across the HVM feature rather than forming a q-u loop oriented in the u-direction. Both of these suggest that the scale of the clum piness is not much smaller than the single clump used in the model.

### 4.5. Toroid

A toroid would be an especially interesting structure to nd in the ejecta of a SN Ia, as it m ight give a hint as to the binary nature of the progenitor system . In the currently preferred progenitor scenarios (see Branch et al. (1995)), SN e Ia are the result of a white dwarf accreting m aterial either from the Roche-lobe over ow of a companion star or the coalescence with another C-O white dwarf. The orientation of the accretion disk axis naturally suggests an independent orientation of the outer ejecta layers, and this could provide a natural explanation why the HVM of SN 2001el deviates from the photospheric axis of symmetry.

W hether an accretion disk could maintains a toroidal structure after the supernova explosion can only be addressed by multi-dimensional explosion modeling. Here we can calculate what e ect such a structure would have on the ux and polarization spectrum, and whether it could possibly account for the HVM feature in SN 2001el. We parameterize the toroid as the ring of a spherical shell lying within opening angle (see Figure 4).

We rst consider a system where the toroid is observed edge-on. We set = 30, giving the minimal z-plane covering factor, and  $_1 = 5$ . We orient the torus axis at = 45 to preferentially absorb the diagonal light. The results are shown in Figure 13. The ux feature is a good m atch to the double-dipped pro le, but the polarization peak at 5% is much too large. The reason is clear from the slice plot in Figure 14 { the edge-on toroid, which occludes opposite sides of the photosphere, is very e ective at blocking light of a particular polarization.

A good t to the polarization feature can still be sought by changing the inclination of the toroid. As the inclination is increased, the toroid rotates o the photodisk and both the ux and polarization feature decrease. The boundaries of the toroid and the opening angle must then be readjusted to properly t the ux feature. In the present model a perfect t cannot be found for any inclination. For all cases where the ux feature is well t, the polarization feature is too strong. A comprom ise t is shown in Figure 15. Here  $v_1 = 20;500, v_2 = 24;750$ = 45, = 43, and = 35. The ux feature is too

weak, and the polarization too strong.

# 5. the high velocity material from other lines of sight

P revious discussions have pointed out that several different geom etrical con gurations are capable of providing reasonable ts to both the ux and polarization HVM features. The degeneracy problem is two-fold: (1) D i erent distributions of absorbing material in front of the photosphere can lead to similar polarization features (see the discussion in x3.5) (2) There is no strong diagnostic of the amount and distribution of material in the emission region (x4.1.2). In this section we consider how the degeneracy problem can be overcom e by observing the HVM from multiple lines of sight.

One di culty in exploring line of sight variations is that the number of possible con gurations in a two-axis system is enormous. Even holding the boundaries of the HVM xed, we still have as free parameters the angle between the photosphere and HVM symmetry axis and two angles specifying the line of sight. There is no easy way to catalog all the possibilities. Therefore to keep the discussion sim ple and general, in the following calculations we choose the underlying photosphere to be spherical. The HVM axis can then be aligned in the z-y plane (i.e. = 0). leaving as the only free parameter the inclination . The polarization is then in the q direction. Note that in light of Equation 3, a positive q-polarization indicates the net ux is vertically polarized, while a negative q-polarization indicates it is horizontally polarized.

The ellipsoidal shell of x4.3 shows only subtle variations with inclination (Figure 16). A ux absorption is visible from all lines of sight, with the absorption prole barely changing with inclination. The only elect on the prole is a small shift of the minimum to the red as the short (ie slow) end of the shell moves into the line of sight. For = 0 (shell view ed edge-on) the polarization is a maximum at 0.8%; this level is comparable to the HVM feature of SN 2001el. As is increased, the polarization feature decreases m onotonically. For = 90 (shell view ed pole on) circular sym m etry is recovered and the polarization is zero.

The clumped shell of x4.4, on the other hand, shows strong variations with inclination (Figure 17). The ux absorption is deepest for = 90, when the clump is viewed top on, directly in between the photosphere and observer. At this inclination, the system is circularly sym metric and the polarization cancels (the perfect cancellation is of course the unnatural result of our simple \bow like" clum p param eterization; a m ore irregularly shaped clump would show a small polarization feature). As is decreased, the clum p m oves to the edge of the photodisk, where it covers lower intensity, more highly-polarized light. As a result, the ux absorption gets weaker while the polarization feature becom es stronger. A strict inverse relationship holds for the inclinations 90 70 and provides an important signature for the single clump model. For inclinations smaller than 60 the polarization begins to decrease, but still rem ains much stronger than the ux feature. An especially striking signature occurs for the line of sight = 40. Here the ux feature is barely visible while the polarization feature is strong ( 1%). The observation of this type of feature would clearly rule out an ellipsoidal shell and favor a single clum p HVM geometry.

The variety of possible ux pro les from the clumped shell model correspond nicely to the variety of pro les that have already been observed in som e other supernova. As the inclination is decreased from 90 , the clump extends further in the z-direction { the two lines therefore become broader and the twominim a more blended. When the clump is viewed directly on (=90), the two minin a are largely resolved, which is not unlike the feature in SN 2001cx (Liet al. 2001). At slightly sm aller inclinations 80) we found the best ts to the partially blended ( minima of SN 2001el. For = 40 the feature is weaker and the twom in in a are alm ost com pletely blended, resem bling the rounded feature of SN 1990N (Leibundgut et al. 1991). For = 20, the feature is very weak and about the depth that it was observed in SN 1994D (Meikle et al. 1996; Patat et al. 1996). Thus the clum ped shellm ay be a singlem odel capable of reproducing the full range of available observations on the HVM ux feature. M ore observations are necessary, how ever, to determ ine if the variety of ux pro les is indeed a line of sight e ect or rather represents individual di erences in the high velocity ejecta.

The most obvious signature of the toroidal geometry (Figure 18) is the high levels of polarization (5%) when viewed near edge-on (= 0). An edge-on toroid occludes vertically polarized light from the edges of the photosphere, giving a polarization feature with q < 0. As the toroid is inclined, the structure rotates o the photodisk and both the ux absorption and polarization peak weaken (in contrast to the clum ped shell model). At inclinations greater than 20, the toroid begins to occlude the horizon-tally polarized light from the bottom of the photosphere { q then ips sign and become spositive.

### 6. summary and conclusions

H igh quality spectropolam etric observations of supernova m ay allow us to extract detailed information on the geom etrical structure of the ejecta. Interpreting the polarization observations through m odeling is a di cult endeavor, how ever, largely because of the the enorm ous num – ber of con gurations available in arbitrary 3-D geom etries. The huge param eter space and multiple lines of sight m ake a direct com parison of data and rst principle calculations di cult, not to m ention com putationally expensive. A param eterized approach is therefore useful in understanding the general polarization signatures arising from di erent geom etrical structures. W e have taken this approach here and calculated the polarization features expected from several geom etries potentially relevant to SN 2001el.

The models computed in this paper highlight the wide range of spectropolam etric features possible when asphericalgeom etries are considered. Depolarizing line opacity in the supernova atm osphere does not in general produce sim – ple depolarization features in the polarization spectrum. A symmetrically distributed line opacity offen creates a polarization peak by partially obscuring the underlying photosphere. In systems where the line opacity follows a di erent axis of symmetry from the electron scattering medium, the resulting polarization feature generally creates a loop in the q-u plane. The two-component model described in this paper provides a convenient approach for quickly calculating and gaining intuition into the types polarization features arising from partial obscuration.

For the case of the high velocity material in type Ia supernova, partial obscuration will be a dom inant e ect on the line features, resulting in large polarization peaks ( 1%) for practically any geometry considered. We have therefore explored to what extent partial obscuration alone can explain the CaII IR triplet polarization peak in SN 2001el. Our picture of the SN 2001el ejecta consists of nearly axially sym m etric photospheric m aterial surrounded by a detached, asymmetric structure at high velocity. W e have investigated four possible geom etries for the HVM : (1) A detached spherical shell is ruled out because it cannot account for the change of polarization angle over the HVM feature. The spherical shell also does not t the shape of double-dipped ux absorption pro le. (2) An ellipsoidal shell, with axis of symmetry rotated 25 from the photosphere symmetry axis, can account for all the general features of the HVM polarization spectrum { the level of polarization, the polarization angle, and the q-u loop. However the ellipsoidal shell, like the spherical one, does not well t the shape of the ux absorption prole. (3) A clumped shell, which could represent a single clum p or a piece of a clum py shell, can account for all the general features of the ux and polarization spectra. (4) A toroid, in the present model, produces a polarization

feature that is larger than observed. D i erent HVM geom etries can be clearly discrim inated by observing them from varying lines of sight. D epending upon the HVM geom etry, a ux absorption sim ilar to that of SN 2001el will be observed in SN Ia with di erent frequency. For a shell-like m odel, the ux signature will be observed from all lines of sight, while for the toroid and clum p, only a fraction of the lines of sight produce the signature absorption. Under the assumption that the HVM has a sim ilar structure in all (or at least a known subset) of SN Ia's, it may be possible to constrain the geometry with a statistical sample of early ux spectra. Because the different m odels leave even m ore dram atic signatures on the polarization spectra, only a few well-observed supernova like SN 2001el are needed to discrim inate the various scenarios (see x5).

W e have not attempted in this paper to constrain the detailed geom etry of the photospheric material. Because this material dem onstrates a near axial sym metry, we have adopted the sim ple and generalm odelofan edge-on oblate ellipsoid with a power law electron density pro le. The actual photospheric geom etry is likely more com plicated, and may deviate from a strict axial symmetry. Given a more complicated photospheric structure, one could use the technique described here to calculate the HVM partial obscuration e ect. Detailed monte-carlo studies on the structure of the photospheric material are under way; because the overall asym metry of the photospheric material is rather sm all, how ever, our m ain conclusions about the HVM likely hold even when a more complicated photospheric geometry is used.

A lthough m ore observations are necessary to pin down the exact geometry of the HVM, one can begin to speculate as to its origin. Two questions in particular must be addressed: W hy is the HVM feature geom etrically detached from the photospheric material? And: W hy does the HVM deviate from the dom inant axis of symmetry of the photospheric m aterial?

The detachment of the HVM indicates that the atmospheric conditions change rather suddenly at high velocity. Three possible changes (or a combination thereof) could result in an HVM feature (see Hatano et al. (1999)): (1) A spike in the overall density in the HVM : In the SN Ia deagration m odelW 7, the m aterial at high velocity consists of unburnt carbon and oxygen with a solar abundance of calcium. The densities of these layers during the epoch in question are too low to produce an optically thick Ca II IR triplet. NLTE models (Nugent et al. 2002) show that { all other things being equal { a density increase at high

velocity of more than an order of magnitude is necessary to produce an HVM feature. (2) A spike in the calcium abundance: For the W 7 densities, the calcium abundance must be increased by 10<sup>3</sup> from solar in order to produce an HVM feature (Nugent et al. 2002). This could, for example, be the result of blob of ejecta material that had undergone explosive oxygen burning, which increases the calcium abundance by  $10^4$  (K hokhlov et al. 1993) (3) A sudden change in the ionization/excitation of the calcium : The optical depth of the IR triplet is a decreasing function oftem perature (due to the increased ionization of C a II to C a III). Thus it is possible that a tem perature decrease in the outer ejecta layers could make the IR triplet optically thick at high velocity. However it seems unlikely in this case that this optical depth spike would have sharp geom etrical boundaries that persisted over several epochs of observations, as found for SN 2001el.

The distinct orientation of the HVM as compared to the photospheric material could be (1) the result of random processes in the explosion physics/hydrodynam ics such as Raleigh-Taylor instabilities producing large scale clum piness or (2) an indication of a preferred direction in the progenitor system . For example, the photospheric dom inant axis could represent the rotation direction of the white dwarfwhile the HVM axis could represent the orientation of an accretion disk. Further explosion and hydrodynam icalm odeling is necessary to assess the plausibility of various scenarios.

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Table 1 Fitted parameters for HVM models

| N am e            | $v_1^{a}$       | $v_2^a$         | E <sup>b</sup> | 1 <sup>C</sup> | d  | e    | е   | t- gure |
|-------------------|-----------------|-----------------|----------------|----------------|----|------|-----|---------|
| spherical shell   | 20 <b>,</b> 200 | 25 <b>,</b> 300 | 1.0            | 0.83           | _  | _    | -   | 8       |
| ellipsoidal shell | 21,200          | 24,800          | 0.91           | 1.20           | _  | 25   | 90  | 11      |
| clum ped shell    | 20,600          | 24,300          | 1.0            | 5.0            | 23 | 83:5 | 4:2 | 12      |
| edge-on toroid    | 20,900          | 24,500          | 1.0            | 5.0            | 30 | 45   | 90  | 13      |
| inclined toroid   | 20,500          | 24,700          | 1.0            | 5.0            | 35 | 45   | 43  | 15      |

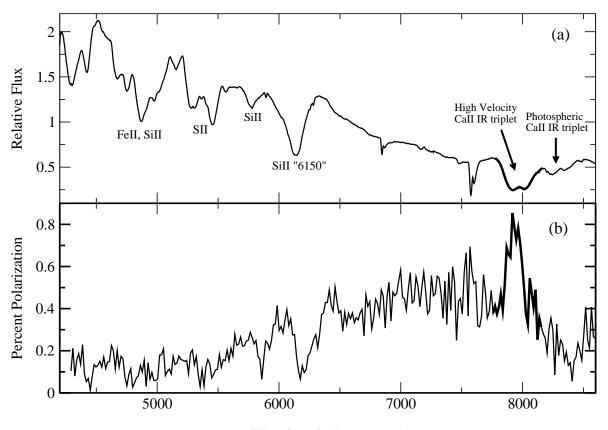
 $^{a}v_{1}$  ,  $v_{2}$  : inner/outer radial or sem i-m a jor boundary in km  $\,$  s  $^{1}$ 

<sup>b</sup>E: A xis ratio

 $c_1$ : optical depth of reference line (8542)

<sup>d</sup> : opening angle (see Figure 4)

<sup>e</sup> ; : angles de ning orientation of HVM symmetry axis (see Figure 4)



# Wavelength (Angstroms)

Fig. 1.| Flux and polarization spectrum of SN 2001el on Sept 25. The HVM feature is shown in bold lines. The polarization spectrum has been ISP subtracted using the ISP shown as the square in Figure 2.

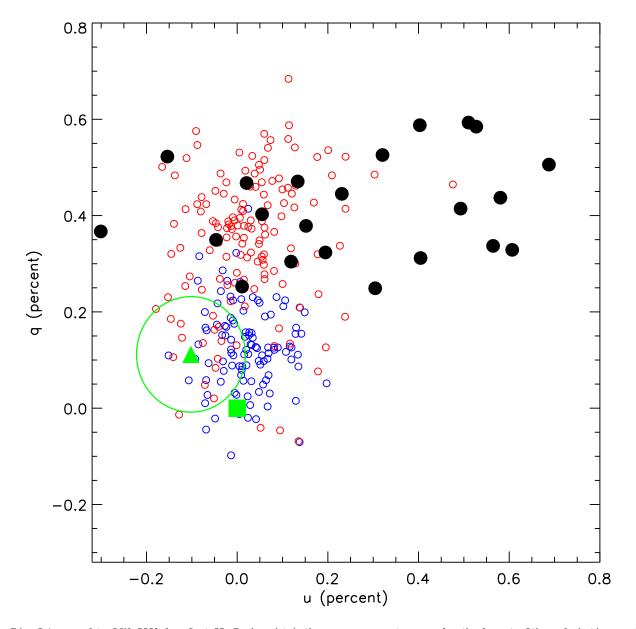


Fig. 2.| q-u plot of SN 2001el on Sept 25. Each point in the gure represents a wavelength element of the polarization spectrum. Large led circles are points from the HVM feature (7800-8100 A). Sm all open circles are points from photospheric spectrum, where the blue open circles come from the wavelength range (4000-6000 A) and the red ones from (6000-8500 A). The green square at the origin represents the choice of the ISP leading to the sim plest theoretical interpretation, and the one used in the paper. The green triangle is the ISP determ ined using later time observations and assuming the intrinsic supernova polarization is zero at this time. The green circle is the rough estim ated error on the ISP determ ined in this way.

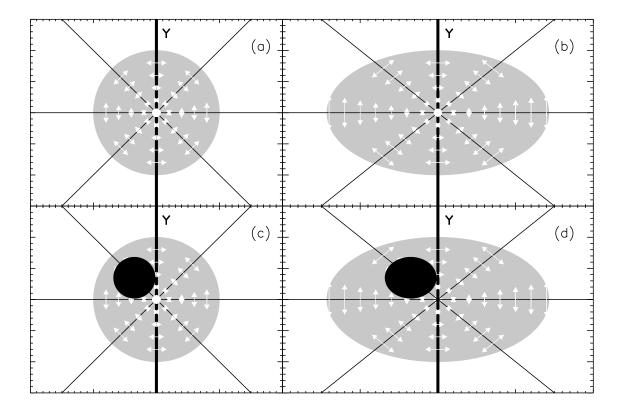


Fig. 3.| The polarization from supernova atm ospheres. Each double arrow in the gure represent a Stokes speci c intensity beam emerging from the photosphere in the observers line of sight. Larger arrows indicate a higher degree of polarization, not a higher intensity. The Y -axis is the polarization reference direction. (a) A spherical photosphere; the polarization of each beam is exactly canceled by another one quadrant away so the net polarization is zero. (b) An ellipsoidal photosphere; vertically polarized light from the long edge exceeds the horizontally polarized light from the short edge so q > 0. (c) A spherical photosphere with a clum p of line optical depth; the continuum polarization cancels but the obscuration of diagonally polarized light by the line leads to a polarization peak feature with u > 0 (d) An ellipsoidal photosphere with a clum p of line optical depth; the continuum is polarized in the q direction and the line in the u direction.

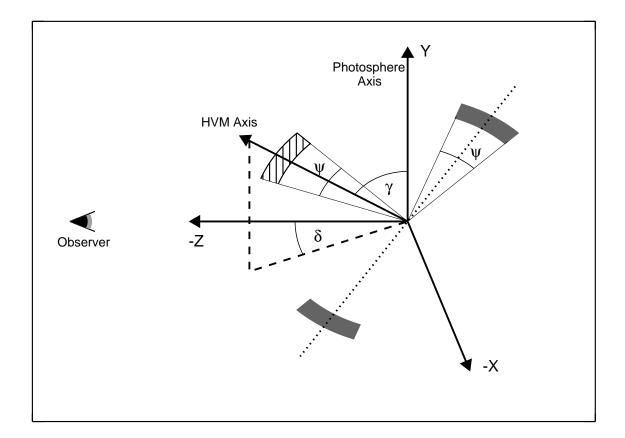


Fig. 4.| Geometry used in the models. The line of sight is in the negative z-direction. The y-axis is both the polarization reference direction and the photosphere symmetry axis. The angles and de ne the orientation of the HVM symmetry axis, where is the angle between the y-axis and the HVM axis, and is the angle between the line of sight and the projection of the HVM axis onto the z-x plane. denotes the opening angle of the clump (hashed arc) and the toroid (solid arc). The two structures are generated by spinning the arcs about the HVM axis.

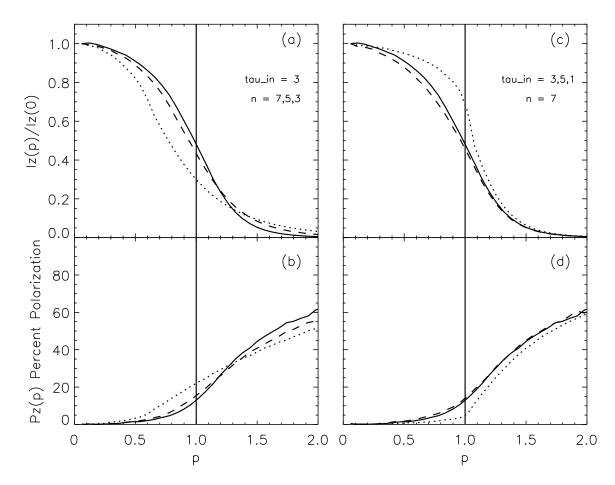


Fig. 5.| The intensity and polarization of speci c intensity beam s emerging from the spherical electron scattering photosphere described in section x3.2. The impact parameter p is given in units of the photospheric radius, de ned as continuum optical depth of one. The solid lines are the values used in the paper and the others lines show comparisons with slightly di erent models. (a,b) show the dependence on the power law index n assuming  $_{ez}$  = 3; solid line: n= 7, dashed line: n= 5, dotted line: n= 3. (c,d) show the dependence of inner optical depth  $_{ez}$  assuming n = 7; solid line:  $_{ez}$  = 3, dashed line:  $_{ez}$  = 5, dotted line:  $_{ez}$  = 1.

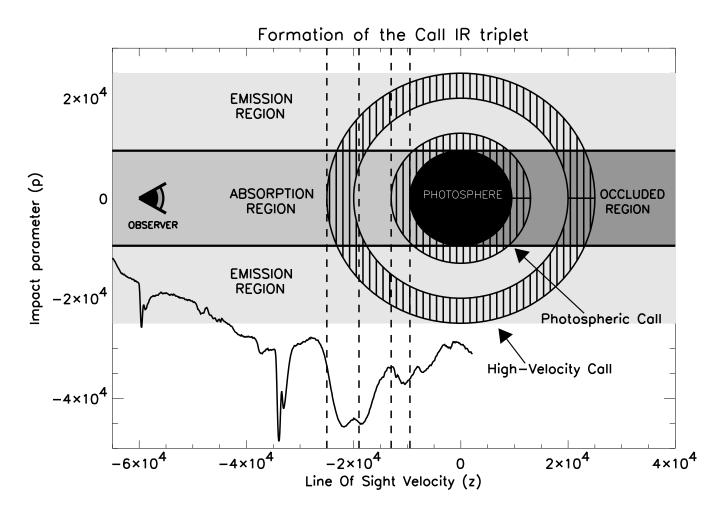


Fig. 6.| Schem atic diagram of line form ation of the CaII IR triplet feature in SN 2001el. The HVM has for illustration been shown with a spherical shell con guration. The line pro le below is the actual ux spectrum of the HVM feature on Sept 25. The vertical lines represent a few of the CV planes of the 8542 line. Each CV plane corresponds to unique wavelength in the spectrum, given in the gure by the wavelength at which they intersect the line pro le.

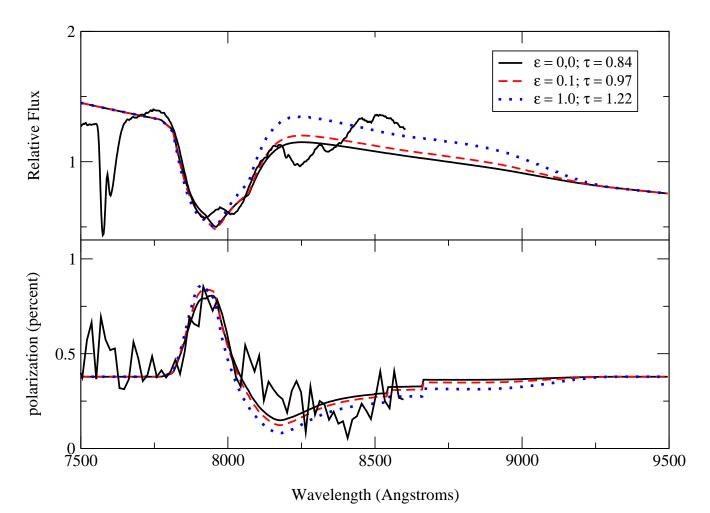


Fig. 7.| The e ect of em ission region m aterial from a spherical shell at a tem perature T = 5500 K. Note that as the line source function is increased, the line optical depth m ust also be increased in order to reproduce the observed line depth. A pure scattering line ( = 0; solid line) does not produce a visible em ission feature. A therm alized line ( = 1; dotted line) produces an em ission, but because this will be blended with the photospheric triplet absorption and em ission, it may still be di cult to detect.

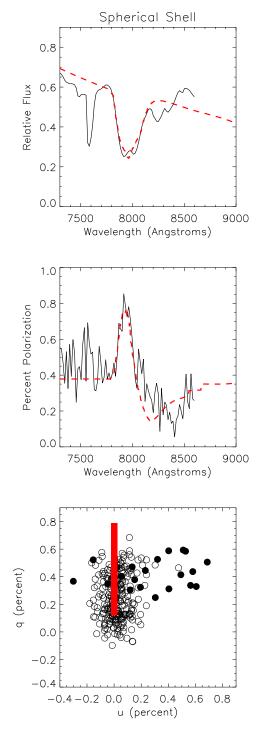


Fig. 8.| Synthetic spectra ts to the observed HVM feature using the spherical shell model of x4.2. In the top two plots, the solid black line is the observed data, and the dashed red line the t. In the bottom q-u plot, the black circles are the data and the red squares the t. The open circles indicate wavelengths corresponding to the photospheric spectrum and the solid circles the HVM feature.

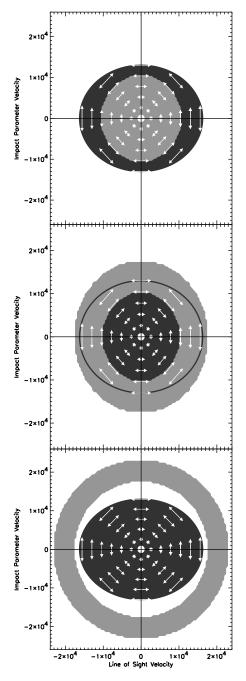


Fig. 9.| Three slices through the spherical shell HVM, which demonstrate how a detached spherical shell e ects the polarization at three di erent wavelengths. Each slice in red is the HVM cross-section on a plane perpendicular to the z (line of sight) axis, corresponding to an CV surface for the 8542 line at a particular wavelength. top:  $v_z = 22;500 \text{ km s}^{-1}! = 7900 \text{ A}$ ; the line obscures the low ly polarized central light, leading to a polarization peak m iddle:  $v_z = 15;500 \text{ km s}^{-1}! = 8100 \text{ A}$ ; the line obscures the highly polarized edge light, leading to a depolarization of the spectrum bottom:  $v_z = 5000 \text{ km s}^{-1}! = 8400 \text{ A}$ ; the line does not obscure the photosphere, but since the line em its som e unpolarized line source function light, thus depolarizing the spectrum . Note: the photospheric axis-ratio has been exaggerated (E = 0.8 rather than E = 0.91) to clarify the asymmetry.

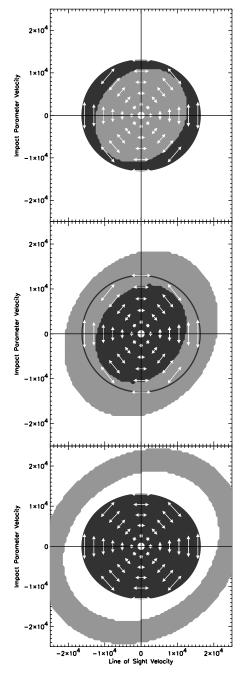


Fig. 10.] Three slices through the rotated ellipsoidal HVM. Panels are the same as in Figure 9. Because the rotated ellipsoidal shell preferentially obscures diagonal light,  $\pm$  will produce a polarization feature with a non-zero u component. The axis ratio of both the photosphere and HVM shell are exaggerated (E = 0.8 rather than 0.91) in order to clarify the asymmetries.

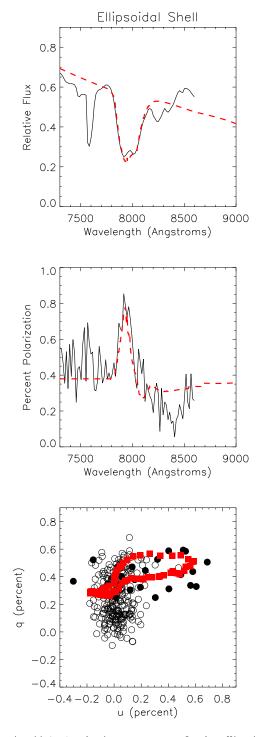


Fig. 11.| Synthetic spectrum ts for the ellipsoidal shell geometry of x4.3. The panels are the same as in gure 8. The ts to the ux and polarization spectra are similar to the spherical shell, but now the HVM feature is polarized primarily in the u-direction. The synthetic feature draws a loop in the q-u plane, which is similar to that in the observed data.

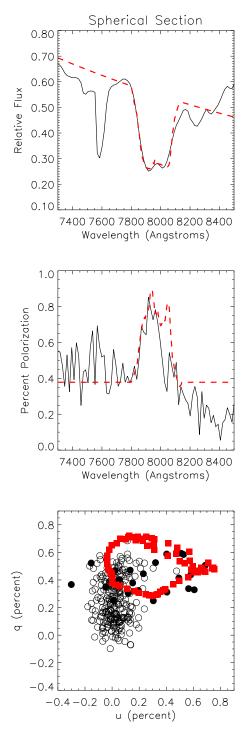


Fig. 12.| Synthetic spectra ts to the HVM feature using the clum ped shell geom etry described in x4.4. Panels are the same as in gure 8

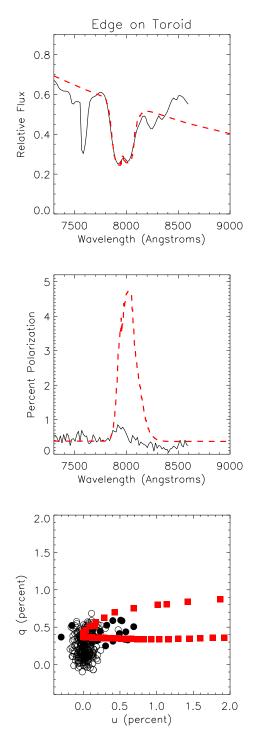


Fig. 13.| Synthetic spectra ts to the HVM feature using the edge-on toroid section geometry described in x4.5. Panels are the same as in gure 8. The polarization feature is much to strong.

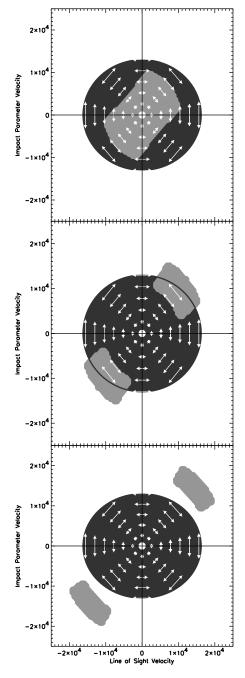


Fig. 14.| Three slices through the edge-on toroid HVM . Panels are the sam e as in Figure 9. Because the toroid is very e ective in blocking light of a particular polarization, it will lead to large polarization peaks.

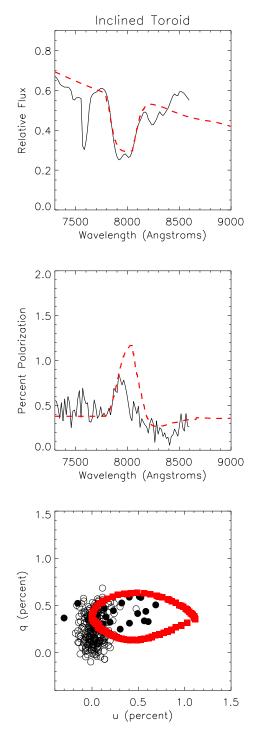


Fig. 15.| Synthetic spectra ts to the HVM feature using the inclined toroid geometry described in x4.5. Panels are the same as in gure 8. The polarization feature is still too strong, while the ux absorption is too weak.

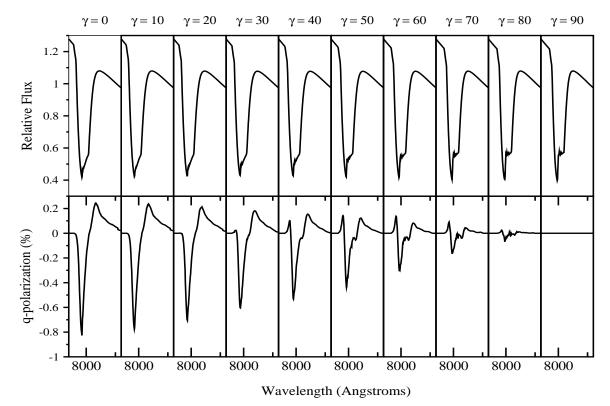


Fig. 16.| Pro le from the ellipsoidal shell model along lines of sight with various inclinations. Positive (negative) q-polarization indicates vertically (horizontally) polarized light. An absorption feature is visible from all lines of sight.

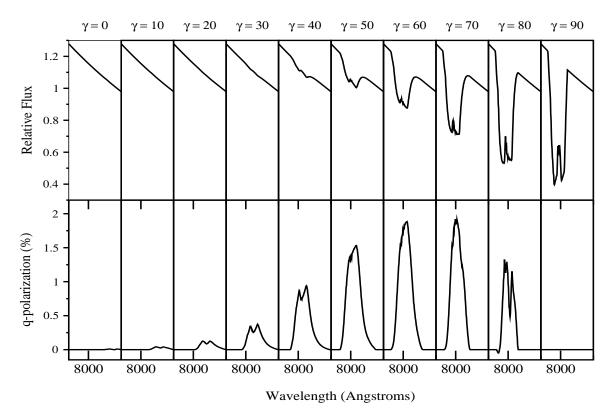


Fig. 17.| Pro le from the clum ped shell model from various lines of sight. As the section moves to the edge of the disk, it blocks lower intensity, highly polarized edge light. The ux feature thus gets weaker while the polarization gets stronger. Note for = 40 the ux absorption is hardly visible while the polarization feature is strong.

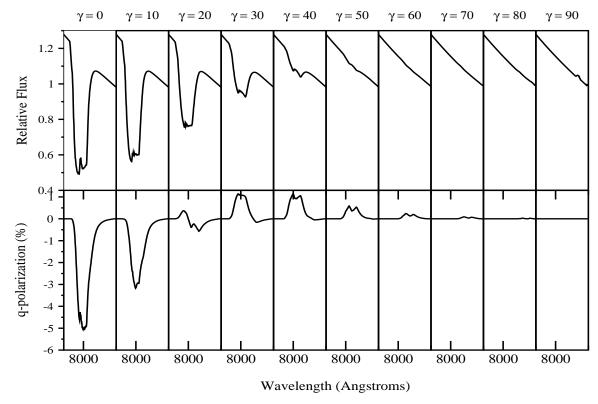


Fig. 18.| Pro les from the toroid model from various lines of sight