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# Angular Dependence of Jet Quenching Indicates Its Strong Enhancement Near the QCD Phase Transition

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We study dependence of jet quenching on matter density, using “tomography” of the fireball provided by RHIC data on azimuthal anisotropy  $v_2$  of high  $p_t$  hadron yield at different centralities. Slicing the fireball into shells with constant (entropy) density, we derive a “layer-wise geometrical limit”  $v_2^{max}$  which is indeed above the data  $v_2 < v_2^{max}$ . Interestingly, the limit is reached only if quenching is dominated by shells with the entropy density exactly in the near- $T_c$  region. We show two models that simultaneously describe the high  $p_t$   $v_2$  and  $R_{AA}$  data and conclude that such a description can be achieved only if the jet quenching is few times stronger in the near- $T_c$  region relative to QGP at  $T > T_c$ . One possible reason for that may be recent indications that the near- $T_c$  region is a magnetic plasma of relatively light color-magnetic monopoles.

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*Introduction.*— Recent experiments at the Relativistic Heavy Ion Collider (RHIC) are dedicated to study possible new forms of QCD matter, with increasing energy density. In such collisions the produced matter equilibrates as Quark-Gluon Plasma (QGP)[1] and then cools down through the near- $T_c$  (M) phase (M for mixed/median/magnetic[2]) into the usual hadronic phase (H). To probe the created matter in an externally controllable way, like using X-ray for medical diagnosis is impossible. However, high energy jets are internal probes: propagating through the fireball, they interact – and thus obtain important information about the medium – as proposed long ago in Refs[3–5]. In heavy ion collisions this energy loss can be manifested in the suppression of observed hadron spectra at high transverse momenta  $p_t$ , as well as in the suppression of back-to-back di-hadron correlations with a high- $p_t$  trigger, when compared with pp and d-A collisions. The “jet quenching” phenomenon is one of the major discoveries by the RHIC experimental program[6].

The suppression is quantified by comparison of the inclusive spectra  $d^2N^{AA}/dp_t d\eta$  in ion-ion(AA) collision to a nucleon-nucleon(pp) reference  $d^2\sigma^{NN}/dp_t d\eta$  via the Nuclear Modification Factor  $R_{AA}(p_t)$  :

$$R_{AA}(p_t) \equiv \frac{d^2N^{AA}/dp_t d\eta}{T_{AA} \cdot d^2\sigma^{NN}/dp_t d\eta} \quad (1)$$

with  $T_{AA}$  the nuclear overlap function which scales up single NN cross section to AA according to expected number of binary NN collisions *without* modification. Thus a  $R_{AA}$  smaller(larger) than unity means suppression(enhancement) due to medium effect. At RHIC this ratio at large  $p_t > 6\text{GeV}$  has been measured to be a constant, about 0.2 for the most central AuAu collisions. Accurate calibration of hard processes in pp and dAu collisions, as well as with hard photon measurements (which show no quenching) [6] resulted in quite accu-

rate knowledge of jet production geometry, for any impact parameter  $b$  (or centrality bins, often characterized by the number of nucleon participants  $N_{part}$  in a collision event). While quenching is firmly established as a final state effect, many efforts to understand its microscopic mechanism are not yet conclusive. Those include pQCD gluon radiation with Landau-Pomeranchuk-Migdal (LPM) effect [7], synchrotron-like radiation on coherent fields [8, 9], elastic scattering loss [10], etc. The fate of deposited energy was discussed in Refs[11, 12] led to predictions of “conical flow” correlated with experimentally observed conical structures in correlations involving 2 or 3 particles, for reviews see e.g. [13, 14].

*Jet tomography and the geometric limit.*— In non-central collisions the overlap region of two colliding nuclei has almond-like shape: thus jets penetrating the fireball in different directions lose different amount of energy according to their varying paths. Their yield distribution  $d^2N/dp_t d\phi$  in azimuthal angle  $\phi$  (with respect to the reaction plane) for high  $p_t$  hadrons thus provides a “tomography” of the fireball[15–17]. We will focus on the second Fourier coefficient

$$v_2(p_t, b) \equiv \frac{\int_0^{2\pi} d\phi \cos(2\phi) [d^2N/dp_t d\phi]}{\int_0^{2\pi} d\phi [d^2N/dp_t d\phi]} \quad (2)$$

depending on impact parameter  $b$  for large  $p_t > 6\text{GeV}$  where hard processes dominate and dependence on  $p_t$  is weak[18].

Unexpectedly, measured  $v_2(p_t, b)$  happen to be considerably larger than what jet quenching models predicted. The aim of our work is to provide simultaneous description of both  $R_{AA}$  and  $v_2$  at high  $p_t$  based on theoretically known geometry of jet production and bulk matter evolution. One important concept of the analysis is the so called *geometric limit*, first suggested by one of us in [17]: the observed asymmetry should be less than some value  $v_2(\text{large } p_t, b) < v_2^{max}(b)$  provided by the geome-

try of the overlap region of two colliding nuclei. The idea [17] was that for very strong quenching only jets emitted from the surface of the almond can be observed. Two other assumptions were made, namely: (i) quenching is proportional to matter density; (ii) colliding nuclei were approximated by homogeneous sharp-edge spheres. However even early experimental data showed that  $v_2$  is actually well *above* this bound. Subsequent studies by Drees, *et al* [19] relaxed the second assumption, with realistic nuclear shapes, which only made contradiction with data even stronger (see e.g. their Fig.3(d)).

The main lesson from those studies is that quenching is *not* proportional to the matter density, but a nontrivial function of it. Assuming some form of this function, one can then calculate both observables  $v_2(b)$  and  $R_{AA}$ .

*Layer-wise geometrical limit.*— Systematically slicing the (expanding) fireball into shells with the entropy density  $s_a < s \leq s_b$ , we calculate what  $R_{AA}(b)$  and  $v_2(b)$  would result with such single shell being the sole source of quenching by a Glauber simulation of AuAu collisions and jet production as in [17, 19]. With the quenching function  $\kappa(s)$  assumed to be concentrated at this slice  $\kappa_{ab} \cdot \theta(s - s_a) \cdot \theta(s_b - s)$ , the distribution in survival probability  $f$  can be calculated and directly leads to evaluation of  $R_{AA}$ :

$$f = e^{-\int_{path} \kappa[s(l)] s(l) l dl}, R_{AA} = \langle f^{n-2} \rangle, n \approx 8.10 \quad (3)$$

Extra  $l$  in the path corresponds to radiative LPM theory [7]. The power index  $n$  comes from the  $\pi_0$   $p_t$  spectrum in pp collisions, see detailed discussions in [18]. For each density shell the absorption coefficient  $\kappa_{ab}$  (in unit  $fm$ ) is then fixed by  $R_{AA}$  data [18] parameterized by  $R_{AA}(p_T > 5 GeV) = [1 - 8.3 \cdot 10^{-3} \cdot N_{part}^{0.58}]^{n-2}$ . Then we calculate  $v_2$ , by sampling half of the jets travelling in  $x$  directions  $\pm 5^\circ$  and the other half in  $y$  direction and extracting the difference in the respective  $R_{AA}^{x(y)}$  [18]. For the Glauber initial condition we follow hydro calculations (see e.g. [20]) to scale entropy density with local participant density, and for bulk evolution we use 1-D Bjorken dilution which is appropriate till time  $\sim 10 fm/c$  (see e.g. [21]). Jet production points are simulated according to binary collision density. We have 24 entropy shells, (0,1),(1,2),..., (23,24] (in  $fm^3$  units).

The resulting  $v_2$  for three impact parameters  $b = 5, 7, 10 fm$  (bottom-to-top) are shown in Fig.1(a).

(i) Note that certain entropy shells produce  $v_2$  much *larger* than the old geometric limits of refs.[17, 19], corresponding to surface emission (small  $s$  at the left side of the plot).

(ii) the existence of the *maximum*  $v_2^{max}(b)$  leads to *layer-wise geometrical limit*: its dependence on centrality is shown in Fig.1(b) by filled big blue diamonds.

(iii) Interestingly enough, the entropy shells where the maxima occur (for all centralities) correspond to the same interval  $s = 4 - 8 fm^{-3}$ , which is in fact quite spe-

cial: it corresponds *exactly* to the vicinity of the QCD phase transition (see e.g. [24]). These curves reflect not only the geometry of the respective entropy shells, but also their placement relative to the jet production points.

After these studies of single shells, we turn to the compiled high- $p_t$  RHIC data on  $v_2(b)$ , shown in Fig.1(b). We include only data for “hard” hadrons with  $p_t > 6 GeV$  from PHENIX (open green boxes) and STAR (open magenta stars) collaborations. Comparing these data points to our *layer-wise geometrical limit* (filled big blue diamonds), we do observe that all the data points are (within error bars) indeed *below* this proposed bound. We also show  $v_2(b)$  lines which would come out if all jet quenching would be due to two other single entropy shells, with  $s = (11, 12] fm^{-3}$  (filled small purple diamonds) and  $s = (23, 24] fm^{-3}$  (open blue diamonds). Those correspond to the QGP phase, near and far from the transition region: the values of  $v_2(b)$  from those shells are significantly smaller than the maximal. Now we qualitatively understand the experimental trend: going from the more central to the more peripheral collisions, quenching geometry shifts from quenching at high density shells (QGP), to the near- $T_c$  region at  $N_p \sim 100$  (approaching the upper limit). For extremely peripheral collisions we expect  $v_2$  to decrease again, reflecting geometry of the low entropy density shells (the hadronic phase).

*Modelling tomography of jet quenching.*— We now turn from individual shells to realistic models, describing the combined effect of all of them.

**Model A** — a two-phase scenario model, in which we assume the quenching function  $\kappa(s)$  with two parameters: one in the near- $T_c$  region and the other for the QGP phase, i.e.

$$\kappa(s) = \kappa_R \times [1 \cdot \theta(s - s_1^c) \cdot \theta(s_2^c - s) + \lambda \cdot \theta(s - s_2^c)] \quad (4)$$

with  $s_1^c = 3/fm^3$  and  $s_2^c = 11/fm^3$  bracketing the near- $T_c$  region. The parameter  $\kappa_R$  is globally fitted from  $R_{AA}(N_{part})$  (for each given  $\lambda$ ), while  $\lambda$  characterizes the relative quenching strength between the near- $T_c$  region and the QGP, with its best value to be determined from a global fitting for  $v_2(N_{part})$ .

**Model B** — a scenario featuring peaked quenching strength at  $T_c$ , which assumes

$$\kappa(s) = \kappa_R \times [e^{-\left(\frac{s-s_c}{s_w^c}\right)^2} \cdot \theta(s - s_1^c) + \xi \cdot \theta(s - s_1^c)] \quad (5)$$

with  $s^c = 7/fm^3$  and  $s_w^c = 2/fm^3$  spanning the near- $T_c$  region according to lattice results[24].

Schematic sketches of the two models’  $\kappa$  are shown in Fig.2(left) and  $\chi^2/D.o.F$  from fitting the  $v_2$  data (both the PHENIX and the STAR points), with a variety of choices of  $\lambda$  (Model A) /  $\xi$  (Model B), are shown in Fig.2(right). The plots suggest that current  $v_2$  data favors the relative quenching strength  $\lambda = 0.4$  for Model A and  $\xi = 0.2$  for Model B, *both favoring a scenario that in relativistic heavy ion collisions the jets are quenched*

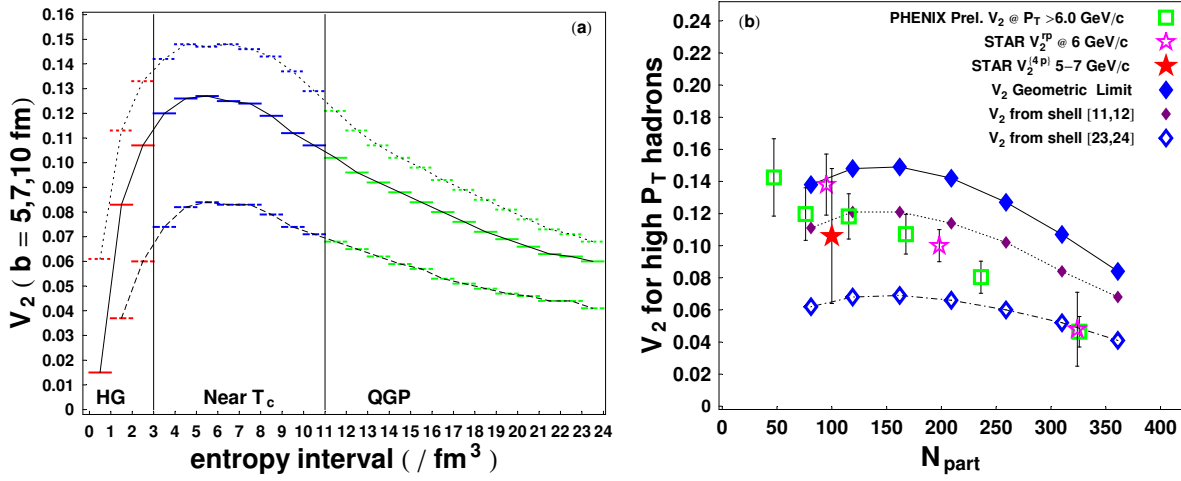


FIG. 1: (color online) (a) The  $v_2$  obtained for each entropy shell at  $b = 5 \text{ fm}$  (dashed),  $7 \text{ fm}$  (solid), and  $10 \text{ fm}$  (dotted) respectively; (b)  $v_2^{max}$  for high  $p_T$  hadrons calculated at different  $N_{part}$  as compared with available RHIC data from [18, 22] and [23].

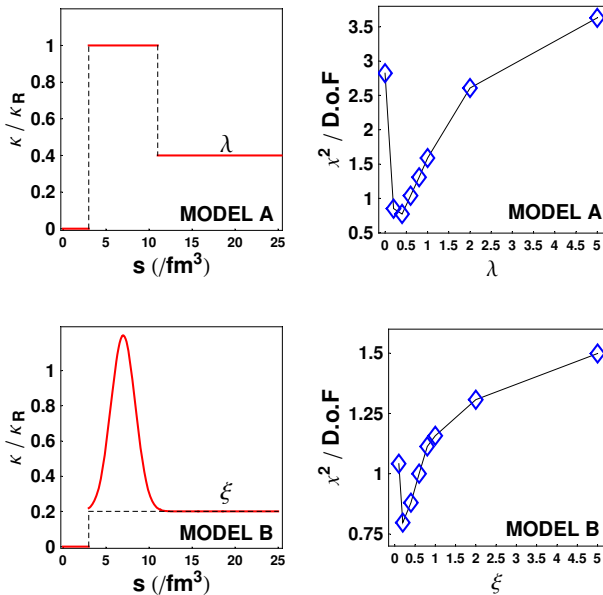


FIG. 2: (color online) (left) Schematic demonstration of the quenching functions of our Model A and B; (right) The  $\chi^2/D.o.F$  when fitting the  $v_2$  data with different values of parameters  $\lambda$  ( $\xi$ ) in our Model A (B), see text.

about 2-5 times stronger in the near- $T_c$  region than the higher- $T$  QGP phase.

We also plot in Fig.3 the  $v_2(N_{part})$  obtained with the above optimal parameters: Model A with  $\kappa_R = 0.00435 \text{ fm}$  and  $\lambda = 0.4$ , Model B with  $\kappa_R = 0.00745 \text{ fm}$  and  $\xi = 0.2$ . Both of them describe current data very well and predict rapid dropping of  $v_2$  at the very peripheral end  $N_p \ll 100$ .

*Conclusions and discussion.*— We started with the calculation of the “layer-wise geometric limit” for models

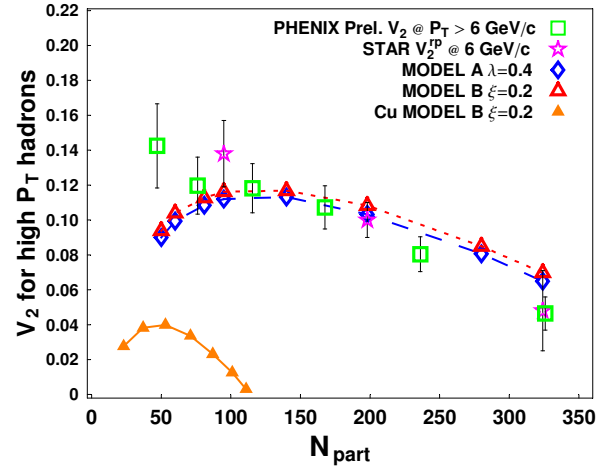


FIG. 3: (color online) Comparison between  $v_2$  experimental data and  $v_2$  calculated from our models, see text.

describing jet quenching

$$v_2(b) < v_2^{max}(b) \quad (6)$$

where the r.h.s. is shown by the filled big blue diamonds in Fig.1(b) and corresponds to particular density shells. Unlike previously proposed bounds, this one is indeed satisfied by all available data (for large enough  $p_t$ , within error bars). The limit can be reached only when the jet quenching is overwhelmingly dominated by the matter shells with the entropy density  $s = 4 - 8 \text{ fm}^{-3}$  since only those have the right geometrical properties: the data points suggest this seems indeed to be the case for the AuAu collisions at RHIC at  $N_p \sim 100$ .

While previous models[17, 19] failed to reproduce the high  $p_t$   $v_2$  and  $R_{AA}$  simultaneously, we now presented two models which can do so. The key is the nontrivial dependence of quenching on the (entropy) density. We

concluded that the angular dependence of jet quenching indicates its strong enhancement near the QCD phase transition, about several times stronger than in the QGP.

Why can it be so? Perhaps a near- $T_c$  peak in jet quenching should not be too surprising, as we already saw similar peaks/sharp-valleys around  $T_c$  for other properties of QGP, from trace anomaly, specific heat and speed of sound[24] to shear and bulk viscosities[25]. Recently the jet quenching strength was found to inversely related to shear viscosity in weakly coupled QGP[26] — such relation if naively extrapolated and combined with the minimum of shear viscosity at  $T_c$  would also point to a near- $T_c$  peak of jet quenching. It was also proposed in [27] that switching on quenching only after a *global* time  $\tau_q \sim 2 fm$  one can obtain better values of the asymmetry: such effect is incorporated by near- $T_c$  dominance in a much more plausible manner via *local* density evolution.

A microscopic explanation may be provided by recent magnetic scenario for the near- $T_c$  QCD plasma, in which this narrow T-region is treated as a **magnetic plasma** of light monopoles[2]. In the same region quarks/gluons are few times heavier and thus get less energy for the same momentum transfer. When a fast electric charge (the jet) penetrates such plasma, its strong transverse magnetic field easily accelerates the abundant light monopoles into an overheated magnetic “coil” behind it via the dual Faraday effect, leading to substantial energy loss of the jet [28].

It will be interesting to extend the present study to different colliding nuclei A and beam energy  $\sqrt{s}$ : the data are becoming available (see e.g.[29]) and the phenomena are rich as the jet production, the bulk evolution, and the pp reference all scale differently with A and  $\sqrt{s}$ . In Fig.3 we have included the prediction for high  $p_t v_2$  of CuCu 200GeV collisions from our model B fixed by AuAu (orange filled triangle), to be tested by data. More dedicated studies (including different initial scaling, different path length dependence, etc) will be reported in [30].

**Note added:** After the Letter was submitted, PHENIX run7 preliminary data were released[22]. They are now included in Fig.1(a) and Fig.3 (squares): as one can see they agree with our model well. As also shown in [22], most other models of quenching give  $v_2$  2-3 times smaller than data.

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