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1 **SHEARING BEHAVIOR OF TIRE DERIVED AGGREGATE WITH LARGE PARTICLE**
2 **SIZE. I: INTERNAL AND CONCRETE INTERFACE DIRECT SHEAR**

3
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7
8 **ABSTRACT:** Tire-Derived Aggregate (TDA) has been used widely in civil engineering
9 applications such as highway embankments, light rail foundations, landslide repairs, and retaining
10 walls as both a recycled material and a lightweight fill. Although the shearing properties of certain
11 types of TDA have been studied, there is still a need for representative and reliable properties of
12 TDA with large particles, such as Type B TDA with particle sizes ranging from 150 to 300 mm.
13 Direct shear tests were performed on Type B TDA using a new large-scale shearing device to
14 measure properties governing internal shear strength as well as interface shear strength against
15 concrete. The internal failure envelope is nonlinear, with a secant friction angle decreasing from
16 39.6 to 30.2° as the normal stress increased from 19.5 to 76.7 kPa. Negligible shearing rate effects
17 were observed for the internal shear strength of this material. The TDA-concrete interface failure
18 envelope is linear with a friction angle of 22.6°. The dilation angle decreased with increasing
19 normal stress for the TDA internal shear tests, whereas only contraction was observed for the
20 TDA-concrete interface shear tests. Displacements at failure for the TDA internal shear tests
21 ranged from 333 to 439 mm, and were 2 to 3 times larger than those for the TDA-concrete interface
22 shear tests.

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24 **INTRODUCTION**

25 Although waste tires are being generated at high rates in California (CalRecycle 2016a) as well
26 as elsewhere in the U.S., research studies have found that they can be recycled in the form of Tire-
27 Derived Aggregate (TDA) as a light-weight construction material (e.g., Ahmed and Lovell 1993;
28 Geosyntec 2008; Ahn et al. 2014; CalRecycle 2016b). The unit weight of compacted TDA is
29 approximately 5 to 9 kN/m³, which is about one-third to one-half that of most granular backfill
30 soils. Several projects have used tire shreds as a replacement for granular backfill in highway
31 embankments or subgrades (Geisler et al. 1989; Ahmed and Lovell 1993; Bosscher et al. 1993;
32 Bosscher et al. 1997; Hoppe 1998; Dickson et al. 2001; Tandon et al. 2007) and retaining walls
33 (Humphrey et al. 1992, 1993; Tweedie et al. 1998; Xiao et al. 2012). These studies have found the
34 performance of TDA fills to be comparable or better than soil-only fills. Despite the positive
35 findings and recommendations of many full-scale studies, there are still uncertainties regarding the
36 shearing properties of TDA. This is particularly true for TDA with large particles, such as Type B
37 TDA material, which has not been adequately characterized due to limitations in the size and
38 displacement capability of available shearing devices. To address this need, Fox et al. (2017)
39 developed a novel large-scale combination direct shear/simple shear device for Type B TDA that
40 can accommodate specimens measuring 3048 mm × 1220 mm in plan and up to 1830 mm in height.
41 This paper presents the results of TDA internal direct shear and TDA-concrete interface direct
42 shear tests, which are the first to fully characterize the shear stress-displacement relationships and
43 failure envelopes for Type B TDA. A companion paper (McCartney et al. 2017) presents
44 corresponding cyclic simple shear data obtained using the same device in an alternate
45 configuration.

46 **BACKGROUND**

47 TDA is composed of recycled waste tires that are shredded to a standard range of particle sizes.
48 The two main categories of TDA used in practice are Type A TDA, with particle sizes ranging
49 from 75 to 100 mm, and Type B TDA, with particle sizes ranging from 150 to 300 mm (ASTM
50 D6270). Both types have limits on the amount of sidewall tire pieces and the quantity of particles
51 having different lengths of exposed steel wire. However, Type B TDA requires less processing
52 than TDA Type A, and is therefore more cost effective for earth fill applications. To minimize the
53 likelihood for self-heating (Humphrey 1996; Arroyo 2011), fills constructed using Type B TDA
54 are limited to having TDA layers up to 3 m thick, while those constructed from Type A TDA are
55 limited to 1 m (ASTM D6270).

56 The shearing behavior of TDA, and in particular Type B TDA with large particles, is a topic
57 that requires further attention. In the past, TDA shear strength has been typically determined using
58 small direct shear boxes and standard soil testing procedures. A summary of the relevant studies
59 that have reported shear stress-displacement relationships for TDA is presented in Table 1. In one
60 of the earliest studies, Humphrey and Sandford (1993) and Humphrey et al. (1993) tested TDA
61 having a maximum particle size of 76 mm in boxes with net dimensions of 286 × 286 mm and 387
62 × 387 mm in plan, both with a height of 228 mm. A clear peak shear strength value was not
63 measured at the maximum displacement (35 mm) even though the box was approximately 4 times
64 larger than the largest particle size. In a more recent study, Xiao et al. (2013) tested TDA having
65 a maximum particle size of 75 mm in a larger box with dimensions of 790 × 800 mm in plan and
66 1219 mm in height, and clear peak shear strength values again were not clearly measured at the
67 maximum displacement (160 mm), even though the box was 13 times larger than the largest
68 particle size. Similar difficulties in measuring peak shear strengths from internal shear stress-

69 displacement relationships were reported by Foose et al. (1996), Bernal et al. (1997), and Yang et
70 al. (2002). Although one study (Gebhardt 1997) involved a large direct shear box (910 mm square)
71 and observed clear peak shear strength values at a displacement of 230 mm, the TDA material was
72 cut in the form of strips that did not meet the requirements of ASTM D6270. In many of these
73 studies, direct shear tests were performed over a limited normal stress range, making it difficult to
74 observe potential nonlinearity in the failure envelope. As a possible consequence, several studies
75 have reported values of cohesion intercept for TDA internal shear strength (Humphrey and
76 Sandford 1993; Xiao et al. 2013) and Strenk et al. (2007) found large variability of reported values
77 of TDA friction angle in the literature, depending on the normal stress range of the tests.

78 As TDA has a high permeability, its shear strength is typically only characterized for drained
79 conditions. As with soils, volume changes may occur during drained shearing of TDA, and it is
80 relevant to characterize this behavior for the development of constitutive models. Yang et al.
81 (2002) measured the internal shear strength of TDA in direct shear tests, and tracked the vertical
82 change in height to infer shear-induced volume change behavior. They observed relatively large
83 dilation for the specimens tested under low normal stresses. For larger normal stress, initial
84 volumetric contraction was observed followed by a relatively large dilation.

85 Several studies have evaluated the internal shear strength of TDA with small particles (2-51
86 mm) using triaxial compression tests (Bressette 1984; Ahmed 1993; Benda 1995; Masad et al.
87 1996; Wu et al. 1997; Lee et al. 1999; Yang et al. 2002; Jeremić et al. 2004). Triaxial testing has
88 the advantage that strains can be calculated, drainage can be controlled, and volume change can
89 be evaluated for drained conditions. However, unless the specimen is very large (i.e., diameter > 1
90 m), the triaxial compression test would not allow sufficiently high axial strains to mobilize peak
91 shear strength for Type B TDA.

92 The above studies on TDA internal shear strength indicate that a large direct shear device is
93 required to test representative specimens of TDA and to reach values of shear displacement
94 corresponding to failure (i.e., greater than 300 mm). Because large-scale testing devices generally
95 have not been available, engineering designs using Type B TDA as backfill have been based on
96 conservative estimates of shear strength, making it less competitive as an alternative fill material
97 for civil engineering applications.

98 Fewer studies have measured the interface shear strengths between TDA and different
99 geomaterials. In many applications, a nonwoven geotextile is placed between TDA and soil to act
100 as a filter, while interfaces between concrete and TDA may be encountered with foundations and
101 retaining walls (Humphrey et al. 1998). Gebhardt et al. (1997) investigated the interface between
102 tire strips and glacial till for normal stresses ranging from 5.5 to 28 kPa. The interface friction
103 angle decreased from 37° to 33° as the compaction water content of the glacial till was increased
104 from 8% to 18-22% (dry to wet of optimum, respectively). This indicates that the characteristics
105 of the interface material can affect interface shear strength with TDA. Bernal et al. (1997) found
106 that the friction angle for a tire shred-woven polyester geotextile interface was 30° , and about 5°
107 lower than the internal friction angle measured at 60 mm of shear displacement. Stark et al. (2010)
108 investigated the interface shear strength between shredded tire pieces (size = 10 to 152 mm) and a
109 nonwoven geotextile and a compacted silty clay. For relatively low normal stresses ranging from
110 4.8 to 19.2 kPa, the friction angles were 59° for the TDA-geotextile interface and 53° for the TDA-
111 soil interface. Xiao et al. (2013) evaluated the interface shear strengths between Type A TDA and
112 sand, concrete, nonwoven geotextile, and geogrid. They found that, different from TDA internal
113 shear strength, shear stress-displacement relationships for these interfaces reached peak shear
114 strength prior to the maximum displacement of the tests. For normal stresses ranging from 24 to

115 96 kPa, Xiao et al. (2013) measured interface friction angles of 39.3° for the TDA-sand interface,
116 35.5° for the TDA-concrete interface, 33.6° for the TDA-geotextile interface, and 18.8° for the
117 TDA-geogrid interface. However, it is difficult to compare these values with the TDA internal
118 friction angle of 36.1° because adhesion intercept values were also reported for the internal and
119 interface tests. The source of adhesion is not apparent and likely indicates nonlinearity in the shear
120 strength envelopes. Overall, the tests on TDA interfaces indicate that the interface friction angle
121 may differ from the internal friction angle, albeit without clear trends.

122 Some studies have evaluated the performance of TDA mixed with soils (e.g., Edil and Bosscher
123 1994; Bosscher et al. 1997), and found that as the TDA percentage increased, the hydraulic
124 conductivity and shear strength also increased. However, mixing TDA with soil requires additional
125 construction effort and cost and may not provide a significant advantage over monolithic TDA
126 fills from a mechanical or environmental sustainability perspective. Due to the minimal processing
127 required, the most economical use of TDA is in monolithic fills with as large of particle size as
128 permitted by regulations.

129 Several researchers have studied the effect of device size on shear strength test results.
130 Humphrey and Sandford (1993) found that two large scale shear boxes ($286\text{ mm} \times 286\text{ mm}$ and
131 $387\text{ mm} \times 387\text{ mm}$) gave nearly identical results for TDA. In-situ large direct shear devices (600
132 $\text{mm} \times 600\text{ mm}$ and $1200\text{ mm} \times 1200\text{ mm}$) were developed by Matsuoka et al. (2001) and used to
133 test natural soils with different maximum particle sizes. They found that a ratio of the maximum
134 particle size to box size of 4 was sufficient to produce consistent results. In addition, the effect of
135 device size on the shear strength of sand having different densities was investigated by Cerato and
136 Lutenecker (2006), who observed that the friction angle decreased as the area of the box increased
137 due to less constraint on the formation of the failure plane. Wu et al. (2007) investigated the effect

138 of specimen length to mean particle diameter ratio L/D_{50} on measured shear strength sand and
139 sandy gravel using containers with $L/D_{50} = 235$ and $L/D_{50} = 4700$. The peak shear strength was
140 observed decreasing with increasing L/D_{50} ratio.

141 **MATERIALS**

142 Information on particle size gradation for the Type B TDA material in the current study is
143 presented in Table 2. Particles ranged in size from 30 to 320 mm, with a mean size D_{50} of 120 mm,
144 and a thickness ranging from 6 to 20 mm. Typical particle shapes are shown in Figure 1. A few
145 particles exceeded the maximum dimension limit of 300 mm, as defined by ASTM D6270. Due to
146 the relatively flat and large size of the particles, these measurements required manual identification
147 and sorting of particles by size as shown in Figure 1. As the particles have different shapes, their
148 size was defined as the maximum dimension (i.e., length). A specific gravity of 1.15 was measured
149 by weighing a porous plastic bag of TDA in air and submerged in water. This value is consistent
150 with the corresponding value for crumb rubber (FHWA 1998) and the typical range of 1.02 to 1.27
151 for TDA (Bressette 1984; Humphrey et al. 1992; Humphrey and Manion 1992; Ahmed 1993).

152 **EXPERIMENTAL EQUIPMENT AND PROCEDURES**

153 **Equipment**

154 Schematic diagrams and a photograph of the large-scale combination direct shear/simple shear
155 device developed by Fox et al. (2017) are shown in Figure 2, and a comparison of the
156 characteristics of the device with those from other devices described in the literature is provided
157 in Table 1. The device was designed to measure the internal shear strength of a full-height TDA
158 specimen, as well as TDA-concrete interface shear strength by placing a large Portland cement
159 concrete block into the bottom section of the box and shearing TDA material over the surface. The
160 box has inside dimensions of 3048×1219 mm in plan and can accommodate specimens with a

161 height up to 1830 mm plus the vertical distance of the shearing gap (typically 65 to 250 mm). As
162 Type B TDA has particle sizes generally ranging from 150 to 300 mm, the minimum dimension
163 of the device is 4 times larger than the maximum particle size. Although ASTM D3080 requires
164 that the minimum specimen size be 10 times greater than the maximum particle size for direct
165 shear tests, a factor of 4 was deemed suitable for Type B TDA because the particles are relatively
166 flat in one dimension. Further, direct shear tests on soils with large particle sizes performed by
167 Matsuoka et al. (2001) found that a factor of 4 was sufficient to obtain consistent shear strength
168 results.

169 The large size of the box allows for a minimum shear displacement of 610 mm, which equals
170 20% of the inside length dimension. The sides of the box in the direction parallel to shear consist
171 of stacked tubular steel members, while the sides of the box in the direction perpendicular to shear
172 consist of vertical solid steel plates. In direct shear mode, the tubular members are restrained using
173 four diagonal beams (i.e., one on each side of the upper and lower sections) so that the upper and
174 lower rectangular sections remain rigid during shear and relative displacement occurs on a
175 horizontal failure plane through the TDA. Two hydraulic actuators are used to provide the
176 horizontal shearing force and are operated in displacement-control mode. Instrumentation includes
177 a load cell on each actuator, four displacement transducers (i.e., one at each corner of the box) to
178 measure vertical displacements, a string potentiometer to measure horizontal displacements, and
179 tiltmeters to measure vertical end plate and actuator rotations. Additional details regarding design
180 and evaluation of the device are provided by Fox et al. (2017) and the companion paper
181 (McCartney et al. 2017).

182

183 **Procedures**

184 Before placement and compaction of the TDA material, the inside walls of the shear box were
185 lined with 2 layers of plastic sheeting. The TDA was compacted in 100 mm-thick loose lifts using
186 a self-propelled rolling and vibrating compactor having a weight of 14.4 kN and 6 passes per lift,
187 resulting in an initial total unit weight of approximately 5.0 kN/m³. The typical compaction process
188 for TDA in the field involves a compactor with a weight of 90 kN and 6 passes per lift (ASTM
189 D6270), but in that case the TDA is not constrained laterally. Manion and Humphrey (1992) found
190 that the compaction energy had only a small effect (less than 5%) on the resulting unit weight of
191 TDA for compaction efforts greater than 60% of the standard Proctor effort. The initial specimen
192 thickness was measured after compaction. A rigid top plate was then placed on the TDA specimen
193 to distribute the vertical load. An array of load cells connected to individual rigid plates used in
194 preliminary tests indicated that the normal stress distribution was uniform using this approach.

195 Normal stress was applied to the TDA specimen by adding dead load weights directly to the
196 top of the rigid top plate for tests with low normal stress (i.e., less than 40 kPa). For higher normal
197 stress, these weights were applied using a rigid “saddle” frame (Fig. 1c) to lower the center of
198 gravity and reduce the potential for tipping instability of the load. The normal stress values reported
199 in this study are all representative of the vertical normal stress on the shearing plane, and include
200 the weight of the TDA overlying the shearing plane and upper box. The change in specimen
201 thickness was measured after the application of normal stress using transducers on the four corners
202 of the box. The normal stress remained on the specimen for a minimum of 12 hours (overnight)
203 before the start of shearing. This was found to be sufficient to accommodate initial creep
204 deformations, such as those observed by Wartman et al. (2007), even though these creep

205 displacements were negligible compared to the immediate settlement under the applied normal
206 stress.

207 After the vertical loading process, four hydraulic jacks were used to raise the top section of the
208 box to form a gap (65-250 mm) and avoid steel-on-steel contact during testing. This process is
209 facilitated by the low friction of the plastic sheeting and by the fact that the normal load rests on
210 the TDA specimen and not on the frame of the device. The gap is less than the maximum TDA
211 particle size, even though most of the TDA particles were observed to be oriented with their flat
212 direction perpendicular to the loading direction (i.e., horizontal). The rigid top plate was then
213 connected to the top section frame so that the entire weight of the top half of the box, including
214 the TDA specimen, frame and dead weights, constituted the vertical load applied to the shear plane.
215 After the static loading period, the specimen was sheared in the air-dry condition and at constant
216 displacement rate.

217 **RESULTS**

218 **Internal Direct Shear**

219 The testing program and results for eight internal direct shear tests on Type B TDA are
220 summarized in Table 3. The first three tests, DS1 to DS3, were performed to investigate the effect
221 of shear displacement rate, ranging from 1 to 100 mm/min, on the shear strength of Type B TDA
222 at constant initial normal stress $\sigma_o \approx 24$ kPa. The remaining five tests, DS4 to DS8, were performed
223 to characterize the failure envelope of Type B TDA over an initial normal stress range of 19.5 to
224 76.7 kPa and a displacement rate of 10 mm/min.

225 Tests DS1 to DS3 were performed first and included an extra compaction lift, resulting in
226 greater unit weights before application of the initial normal stress than in tests DS4 to DS8. After
227 application of the initial normal stress, the TDA specimens in Tests DS1-DS3 had total unit

228 weights of approximately 6.5 kN/m^3 , while the TDA specimens in Tests DS4-DS8 had total unit
229 weights ranging from 6.01 to 8.04 kN/m^3 depending on the normal stress applied. After
230 compaction, the specimens that were loaded to higher normal stresses experienced larger changes
231 in volume, leading to a progressively denser condition. The TDA specimen unit weight was
232 observed to increase immediately after the application of normal stress, followed by a small
233 amount of creep settlement (less than 25 mm). The range of unit weights encountered after
234 application of the initial normal stress are consistent with the general range of unit weights
235 observed in many field applications (CalRecycle 2016b).

236 Values of total unit weight (i.e., dry unit weight due to the negligible water content) after
237 normal stress application and prior to shear are shown in Figure 3(a) for tests DS4 to DS8. A
238 consistent and slightly nonlinear increase in unit weight with initial normal stress is observed, with
239 a maximum value of 8.04 kN/m^3 at $\sigma_o = 76.7 \text{ kPa}$. The corresponding one-dimensional
240 compression curve for this TDA material is shown in Figure 3(b). Compression of the individual
241 TDA particles was neglected in the calculation of the void ratio because the normal stresses were
242 relatively low and the particles have low volume compressibility as indicated by a Poisson's ratio
243 of nearly 0.5 (Feng and Sutterer 2000). The compressibility is approximately log-linear and yields
244 a compression index $C_c = 0.8$. Because the points on the compression curve represent final values
245 (i.e., after application of normal stress) from different tests, a preconsolidation-type yield stress at
246 low normal stress is not observed. Humphrey and Manion (1992) and Ahmed and Lovell (1993)
247 found that particle gradation affects the compression curve of TDA, while Ahmed and Lovell
248 (1993) noted that the slope of the compression curve for TDA may vary with compaction effort.

249 The shear stress-displacement relationships for tests DS1 to DS3 are shown in Figure 4(a),
250 with values of shear stress corrected for changing failure surface area during displacement.

251 Despite the two orders of magnitude difference in displacement rates for these tests, the three
252 relationships are nearly identical, especially up to the peak corrected shear stress value, and display
253 similar values of initial stiffness, peak corrected shear stress, and displacement at peak. The
254 mobilized secant friction angles, shown in Figure 4(b), are also similar, with a peak value occurring
255 at a displacement of 332 to 366 mm. The peak secant friction angle coincides with the maximum
256 principal stress ratio, a commonly used failure criterion for triaxial tests on granular materials (e.g.,
257 Lee and Seed 1967). Peak secant friction angles are used to estimate the factor of safety for limit
258 equilibrium analyses; however, depending on serviceability requirements, failure may be defined
259 for displacements smaller than those at the peak. The relationships in Figure 4(b) are not the same
260 as those in Figure 4(a) because area corrections for both normal stress and shear stress offset when
261 calculating the mobilized secant friction angle. In Figure 4(b), each test displays a post-peak
262 reduction of approximately 10 to 20%. The corresponding volumetric strain relationships for tests
263 DS1 to DS3 are shown in Figure 4(c), where negative values indicate expansion. For each test, the
264 TDA specimens experienced initial compression followed by expansion, which is consistent with
265 the direct shear behavior for medium dense granular soils.

266 The area-corrected shear stress-displacement relationships for tests DS4 to DS8 under different
267 normal stresses are shown in Figure 5(a). Similar to natural soils, clear increases in both shear
268 stiffness and peak corrected shear stress are observed with increasing normal stress. Although peak
269 corrected shear stress values were observed for each test, the relationships for mobilized secant
270 friction angle, shown in Figure 5(b), provide a better indication of failure conditions.
271 Displacements at the maximum corrected shear stress [Fig. 5(a)] ranged from 370 to 587 mm,
272 whereas displacements at the peak secant friction angle [Fig. 5(b)] ranged from 337 to 439 mm
273 and occurred significantly before the maximum displacement of the direct shear box. The

274 corresponding volumetric strains for tests DS4 to DS8 are shown in Figure 5(c), and again indicate
275 expansion (dilation) after an initial contraction. In general, increasing levels of normal stress
276 produce greater initial contraction and less dilation (expansion) thereafter, which is consistent with
277 the shear-induced volume change behavior for natural granular soils (Lee and Seed 1967).

278 **Concrete Interface Direct Shear**

279 The testing program and results for the Type B TDA-concrete interface are summarized in
280 Table 4. Four interface direct shear tests were performed to characterize the failure envelope. The
281 range of initial normal stresses were similar to those evaluated for the TDA internal strength tests,
282 but the initial unit weight after application of normal stress was slightly greater ($\approx 6.0 \text{ kN/m}^3$). The
283 total unit weights for all four tests after application of normal stress were relatively consistent with
284 an average of 7.3 kN/m^3 . The trend in total unit weight with normal stress is not as consistent as
285 in the TDA internal tests, which may have occurred because the TDA was compacted to an initially
286 higher total unit weight.

287 The area-corrected stress-displacement relationships for tests DSII1 to DSII4 are shown in
288 Figure 6(a). These relationships show a clear yielding point at a displacement of 50 to 120 mm,
289 but do not indicate peak corrected shear stress values due to the decreasing area and increasing
290 normal stress during shear. On the other hand, the relationships for mobilized secant friction angle,
291 shown in Figure 6(b), indicate clear peak values at displacements of approximately 130 to 255
292 mm. The displacements at the peak secant friction angle are significantly smaller than those
293 measured in the TDA internal tests because the particles were observed to slide across the concrete
294 surface in the TDA interface tests, whereas they were observed to twist around one another due to
295 interlocking in the TDA internal tests. The results in Figure 6(b) indicate that the evolution of
296 mobilized secant friction angle throughout each test is similar, with slightly higher values and

297 earlier peak displacements for lower normal stress levels. The corresponding volumetric strain-
298 displacement relationships for tests DS11 to DS14 shown in Figure 6(c) also display similar and
299 nearly linear behavior with continuous contraction throughout the shearing process. The maximum
300 volumetric strain values for the TDA-concrete interface shear tests are larger than for the TDA
301 internal shear tests, which is attributed to the absence of interlocking-induced dilation for the
302 interface tests.

303 **ANALYSIS**

304 **Failure Evaluation**

305 The TDA direct shear results indicate that area corrections have a significant effect on the
306 values of shear stress and peak corrected shear stress values may not be reliable for defining the
307 failure envelope or making comparisons among tests. However, the mobilized secant friction
308 angles show a much clearer peak value for both the TDA internal and the TDA-concrete interface
309 tests, and this was used as the failure criterion when evaluating stress-displacement relationships.
310 Accordingly, the area-corrected normal stress and shear stress values at the displacement
311 corresponding to the peak secant friction angle were defined as failure conditions, and are
312 summarized in Table 2.

313 A plot of TDA internal shear strength as a function of shear displacement rate is shown in
314 Figure 7. The shear strength values are nearly identical with small differences attributed to the
315 different initial conditions. Accordingly, and also considering Fig. 3(b), it can be concluded shear
316 displacement rate has a negligible effect on the shear strength of Type B TDA at low normal stress
317 (e.g., at approximately 24 kPa).

318 The failure points for the five TDA internal shear strength tests performed at different normal
319 stress levels and a rate of 10 mm/min are shown in Figure 8(a). Although the trend in Figure 8(a)

320 appears approximately linear, a nonlinear relationship is indicated from the evaluation of the peak
 321 secant friction angles. Values of peak secant friction angle are shown in Figure 8(b) and follow a
 322 clear decreasing trend with increasing normal stress. Dry TDA particles are not expected to have
 323 inter-particle forces leading to cohesion, so this assumption together with the decreasing peak
 324 secant friction angle indicates that the failure envelope is nonlinear. This nonlinearity is further
 325 investigated using the shear strength model of Duncan et al. (1980):

$$\tau_f = \sigma_f \tan(\phi_{sec}) \quad (1)$$

326 where the secant friction angle variation with the normal stress at failure is:

$$\phi_{sec} = \Delta\phi \log\left(\frac{\sigma_f}{p_{atm}}\right) + \phi_0 \quad (2)$$

327 where P_{atm} is atmospheric pressure (101.3 kPa) and $\Delta\phi$ and ϕ_0 are fitting parameters. The semi-
 328 logarithmic plot shown in Figure 8(c) indicates that this model provides a good fit to the internal
 329 shear strength data for Type B TDA. This analysis allows for direct interpretation of the nonlinear
 330 failure envelope and thus differs from approaches taken in previous studies on TDA shear strength.

331 Average dilation angles were calculated from the relationship:

$$\psi = \sin^{-1}\left(\frac{\tan(\alpha)}{2 + \tan(\alpha)}\right) \quad (3)$$

332 where α is the slope of the change in height versus displacement curve, as follows:

$$\alpha = \tan^{-1}\left(\frac{\text{Maximum Contraction} - \text{Maximum Dilation}}{\text{Displacement at Maximum Contraction} - \text{Displacement at Maximum Dilation}}\right) \quad (4)$$

333 The average dilation angle for the TDA internal shear tests ranges from 1.2° to 3.1° as shown in
 334 Figure 8(b). The dilation angle is small compared with the secant friction angle, and displays a
 335 clear decreasing trend with increasing normal stress consistent with the behavior of granular soils
 336 (Lee and Seed 1967).

337 The failure points for the TDA-concrete interface are shown in Figure 9(a). Different from the
338 internal TDA failure envelope, the TDA-concrete failure envelope is linear and has zero intercept.
339 The corresponding secant friction angles, shown in Figure 9(b), display a slight decrease with
340 increasing normal stress. In this case, the shear strength can be represented using the conventional
341 equation for frictional soils:

$$\tau_f = \sigma_f \tan(\phi) \quad (5)$$

342 where ϕ is constant. For the Type B TDA-concrete interface, an average secant friction angle ϕ_{sec}
343 of 22.9° was calculated, and is close to the best-fit value of 22.6° to the data points shown in Figure
344 9(a). Only contraction was observed for the TDA-concrete interfaces, so the dilation angle can be
345 assumed to be zero for the TDA-concrete interface.

346 **Failure Envelope Comparison**

347 A comparison of TDA internal and TDA-concrete interface failure envelopes is shown in
348 Figure 10. Normal stresses at failure vary for these envelopes because the maximum mobilized
349 secant friction angles are reached at different values of shear displacement. The failure envelopes
350 indicated by Equations (1) and (5) are also shown and are in good agreement with the experimental
351 data. The nonlinearity of the TDA internal failure envelope is more apparent when compared with
352 the linear TDA-concrete interface failure envelope. Although TDA-concrete interface shear
353 strength is nearly one-half that of TDA internal shear strength over the range of normal stresses
354 evaluated, the TDA-concrete interface friction angle is higher than soil-concrete interface friction
355 angles measured for silt (14°), silty sand or clayey sand (17°), and clean sand ($17-22^\circ$), as reported
356 in NAVFAC DM7 (NAVFAC 1986). Differences between the internal and interface failure
357 envelopes are attributed to dilatancy and particle interlocking for the TDA internal tests versus
358 sliding of particles over the rough surface in the TDA-concrete interface tests. A comparison of

359 the TDA internal shear stresses at failure with data reported from other studies in the literature is
360 shown in Figure 11. Shear stress values at failure from the current study are in close agreement
361 and lie toward the upper bound of other published values.

362 **Initial Stiffness**

363 Values of TDA initial shear stiffness, as obtained from the hyperbolic model of Duncan et al.
364 (1980), are presented in Figure 12. The corrected shear stress-displacement relationships were
365 normalized by dividing the shear displacement by the corrected shear stress, and then plotting
366 versus the shear displacement. The inverse of the slope of this normalized corrected shear stress-
367 displacement relationship corresponds to the initial stiffness of the corrected shear stress-
368 displacement relationship. In each case, the fitting process was based on the corrected shear stress-
369 displacement data preceding the peak secant friction angle. Shear stiffness increases with
370 increasing normal stress for both the TDA internal and TDA-concrete interface tests, with
371 significantly higher values for the TDA-concrete interface. Initial shear stiffness is larger for the
372 TDA-concrete interface tests because failure occurred at smaller displacements.

373 **CONCLUSIONS**

374 This study investigated shear stress-displacement relationships and failure envelopes for large-
375 size (Type B) tire derived aggregate (TDA). Large-scale direct shear tests were performed to
376 measure the properties governing TDA internal shear strength as well as interface shear strength
377 with Portland cement concrete. The internal failure envelope was nonlinear, with a peak secant
378 friction angle that decreases from 39.6° at low normal stresses (19.5 kPa) to 30.2° at high normal
379 stresses (76.7 kPa). The unit weight of TDA in these tests ranged from 6.01 to 8.04 kN/m³, which
380 is about 25 to 50% of the unit weight of typical natural backfill soils. Negligible displacement rate
381 effects were observed for TDA internal shear strength.

382 The TDA-concrete interface failure envelope was linear, with a friction angle of 22.6°. The
383 TDA-concrete interface friction angle is higher than typical values for interfaces between concrete
384 and silt, clayey sand, or clean sand. Similar to granular soils, the dilation angle decreased with
385 increasing normal stress for the internal TDA direct shear tests. Only contraction was observed
386 during the TDA-concrete interface direct shear tests. The initial shear stiffness from the TDA-
387 concrete interface shear tests was greater than from the TDA internal shear tests. These higher
388 shear stiffness values correspond to a displacement at failure of approximately 130 to 255 mm for
389 the TDA-concrete interface shear tests as opposed to a displacement at failure of 332 to 439 mm
390 for the TDA internal shear tests.

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398 **APPENDIX I. REFERENCES**

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Table 1: Summary of direct shear testing programs for TDA internal shear strength.

Test Parameters and Results	Humphrey and Sandford (1993) and Humprey et al. (1993)	Foose et al. (1996)	Bernal et al. (1997)	Gebhardt (1997)	Yang et al. (2002)	Xiao et al. (2013)	This Study
Box shape	Square	Circular	Square	Square	NR	Rect.	Rect.
Shear box areal dimensions (mm)	286×286 and 387×387	279 (dia)	300×300	910×910	NR	790×800	3048×1219
Shear box height (mm)	228	314	225	810	NR	1219	1830
Box width to maximum particle size ratio	3.8-5.0	2.1	6	2.1	NR	10.5	4
Maximum shear box displacement (mm)	35	90	60	230	25	180	690
Shearing rate (mm/min)	7.6	1.3	1	1	1	22	1-100
Maximum TDA size (mm)	76	150	50	432	10	75	320
Average unit weight (kN/m ³)	5.5	5.9	5.9	5.6	5.73	7.91-13.2	5.04-8.04
Normal stress range (kPa)	17-68	9-50	7-54	5.5-28		24-96	19.5-76.7
Maximum normal stress (kPa)	68	80	54	28	83	96	88.4
Internal friction angle (degrees)	19-26	30	35*	38	32	36.1	30.2-41.1
Apparent cohesion (kPa)	4.3-11.5	3	0	0	0	14.3	0

*Reported at the end of shearing

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518

519 **Table 2:** Particle size information for Type B TDA material.
 520

Parameter	Value
Range of particle size	30-320 mm
Range of particle thickness	6-20 mm
D ₁₀ *	70 mm
D ₃₀ *	105 mm
D ₅₀ *	120 mm
D ₆₀ *	155 mm
Coefficient of curvature, C _z	1.02
Coefficient of uniformity, C _u	2.21

521 *D₁₀, D₃₀, D₅₀, and D₆₀ are the largest TDA particle dimensions at 10%, 30%, 50%, and 60%
 522 finer by dry weight.
 523

524 **Table 3:** Summary of Type B TDA internal direct shear testing program and results.
 525

Test	Initial* Normal Stress, σ_o (kPa)	Initial* Total Unit Weight (kN/m ³)	Initial* Void Ratio	Displacement Rate (mm/min)	Values At Peak Secant Friction Angle				Average Dilation Angle, ψ (deg)
					Normal Stress, σ_f (kPa)	Shear Strength, τ_f (kPa)	Secant Friction Angle, ϕ_{sec} (deg)	Displacement, δ_f (mm)	
DS1	23.8	6.45	0.75	1	27.0	23.5	41.0	366	3.6
DS2	23.8	6.60	0.71	10	26.7	23.1	40.8	337	4.7
DS3	24.3	6.56	0.72	100	27.3	22.9	40.0	332	3.7
DS4	19.5	6.01	0.87	10	21.9	17.7	38.8	337	2.9
DS5	22.9	6.11	0.85	10	25.8	21.3	39.6	344	3.1
DS6	38.8	6.95	0.62	10	44.6	31.4	35.1	400	2.6
DS7	60.8	7.58	0.49	10	71.0	46.5	33.3	439	1.3
DS8	76.7	8.04	0.40	10	88.3	51.5	30.2	403	1.2

526 *Initial values are at the start of shearing
 527
 528
 529

530
531

Table 4: Summary of Type B TDA-concrete interface direct shear testing program and results.

Test	Initial* Normal Stress, σ_o (kPa)	Initial* Unit Weight (kN/m ³)	Initial* Void Ratio	Displacement Rate (mm/min)	Values At Peak Secant Friction Angle			
					Normal Stress, σ_f (kPa)	Shear Strength, τ_f (kPa)	Secant Friction Angle, ϕ_{sec} (deg)	Displacement, δ_f (mm)
DSI1	22.3	7.26	0.55	10	23.3	10.2	23.7	130
DSI2	39.5	7.12	0.58	10	42.0	17.5	22.6	185
DSI3	55.4	7.40	0.52	10	58.2	24.9	23.1	148
DSI4	77.0	7.38	0.53	10	83.9	34.4	22.3	255

532
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*Initial values are at the start of shearing

534 **LIST OF FIGURES**

535 **FIG. 1:** Photograph of typical Type B TDA particles

536 **FIG. 2:** Large scale combination direct shear/simple shear device in direct shear mode: (a)
537 Elevation view diagram; (b) Dimensions; (c) End view diagram; (d) Photograph

538 **FIG. 3:** Properties of Type B TDA: (a) Unit weight - applied normal stress; (b) Compression
539 curve

540 **FIG. 4:** TDA internal shear behavior for three displacement rates: (a) Shear stress-displacement;
541 (b) Mobilized secant friction angle-displacement; (c) Volumetric strain-displacement.

542 **FIG. 5:** TDA internal shear behavior for five normal stress levels: (a) Shear stress-displacement;
543 (b) Mobilized secant friction angle-displacement; (c) Volumetric strain-displacement

544 **FIG. 6:** TDA-concrete interface shear behavior for four normal stress levels: (a) Shear stress-
545 displacement; (b) Mobilized secant friction angle-displacement; (c) Volumetric strain-
546 displacement

547 **FIG. 7:** Effect of shear displacement rate on TDA internal peak shear strength

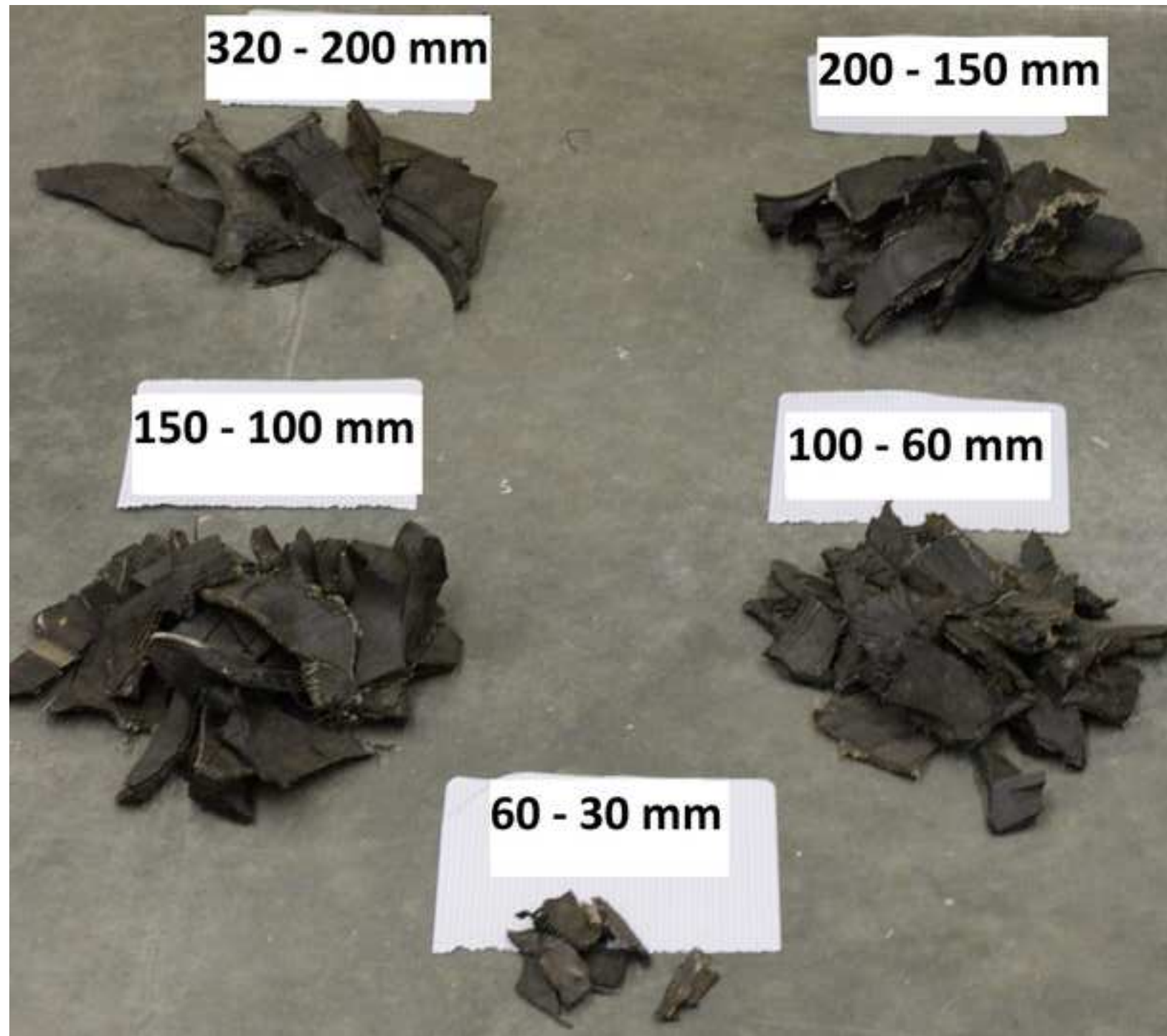
548 **FIG. 8:** TDA internal failure evaluation: (a) Peak shear strength; (b) Peak secant friction angle
549 and dilation angle; (c) Secant friction angle

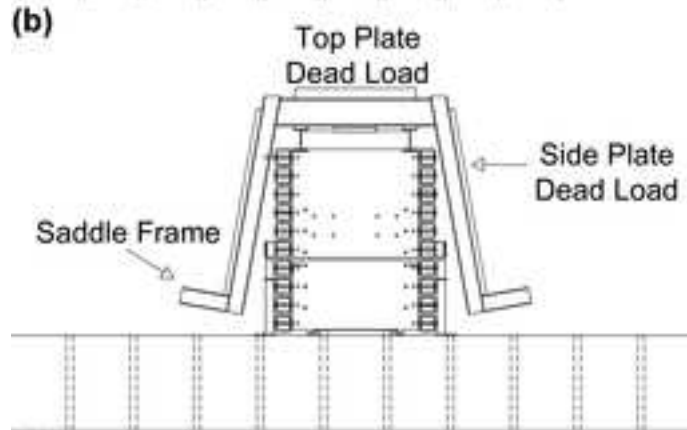
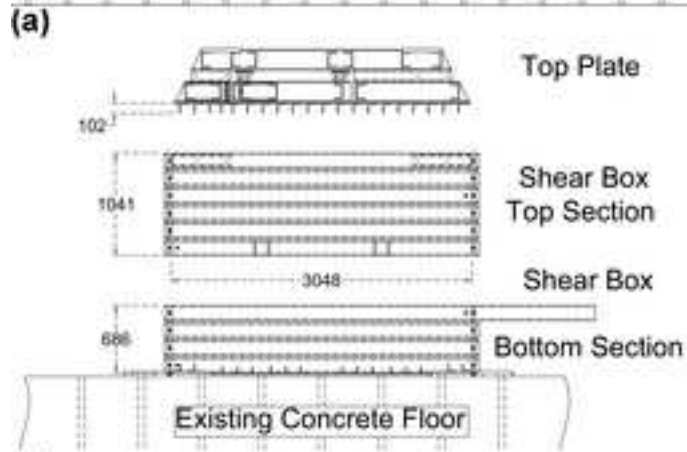
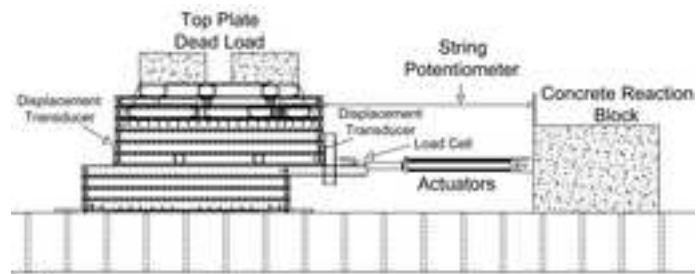
550 **FIG. 9:** TDA-concrete interface failure evaluation: (a) Peak shear strength; (b) Peak secant
551 friction angle

552 **FIG. 10:** Comparison of TDA internal and TDA-concrete interface peak shear strength
553 envelopes

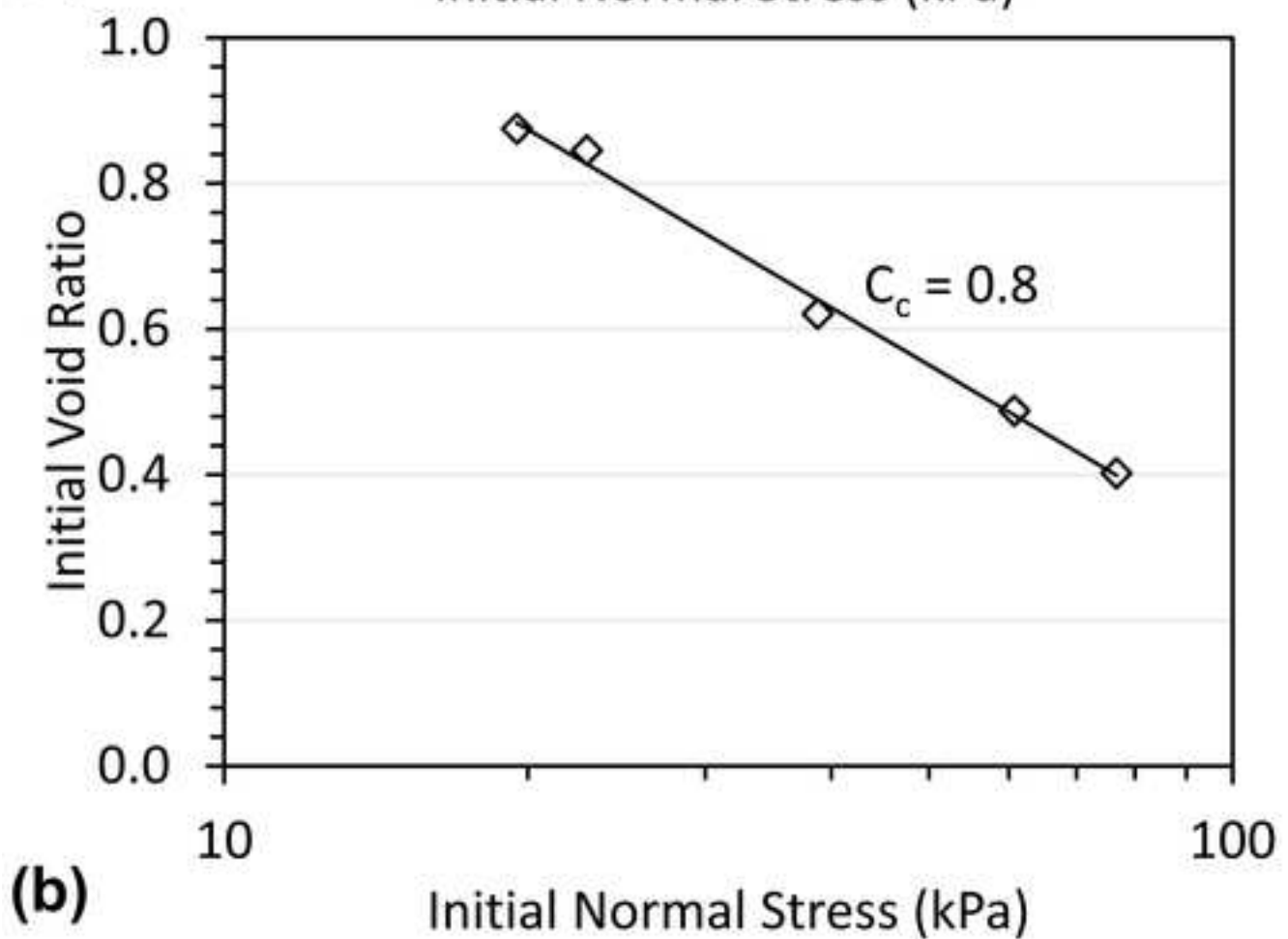
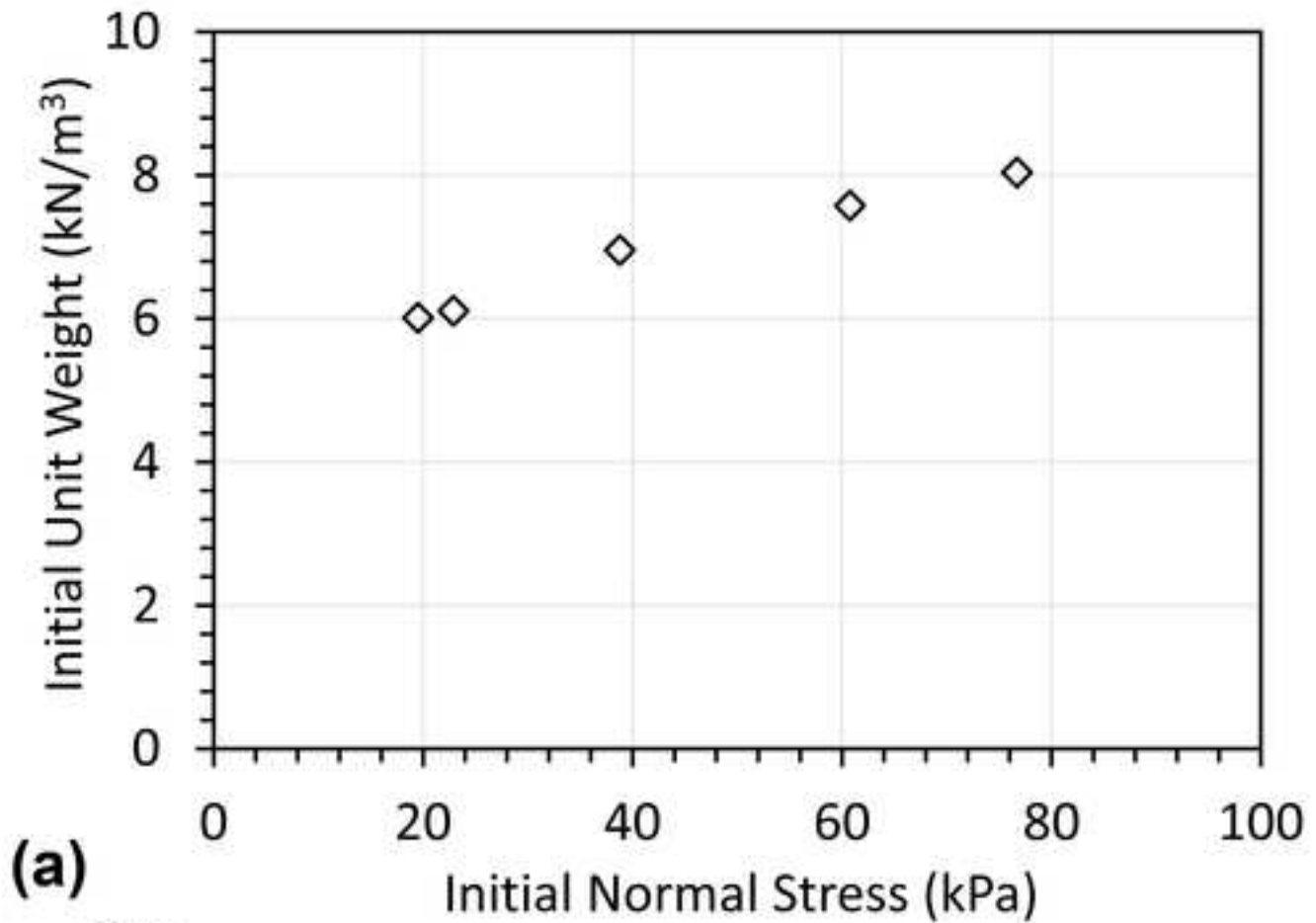
554 **FIG. 11:** Comparison of TDA internal peak shear strengths with published values from the
555 literature

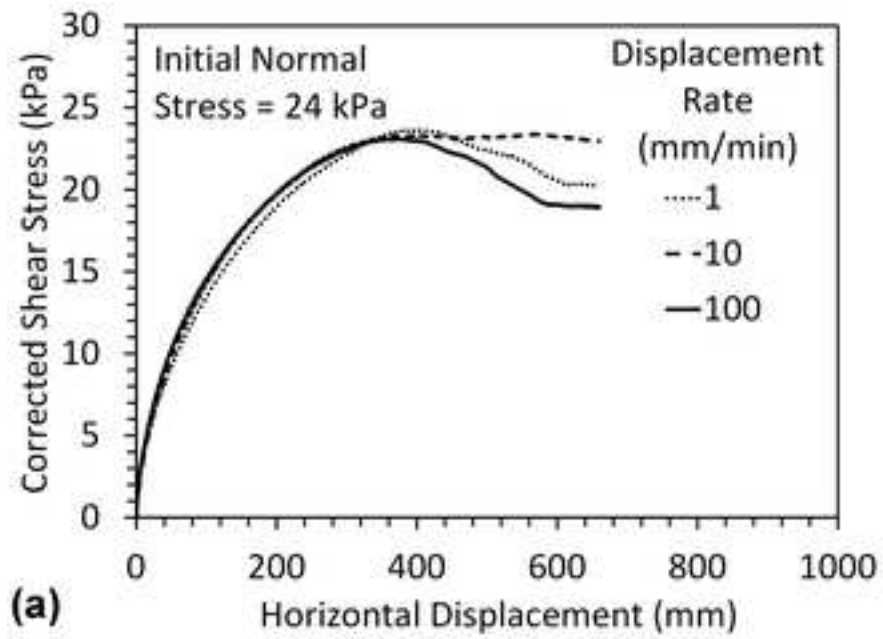
556 **FIG. 12:** Comparison of TDA internal and TDA-concrete interface initial shear stiffness



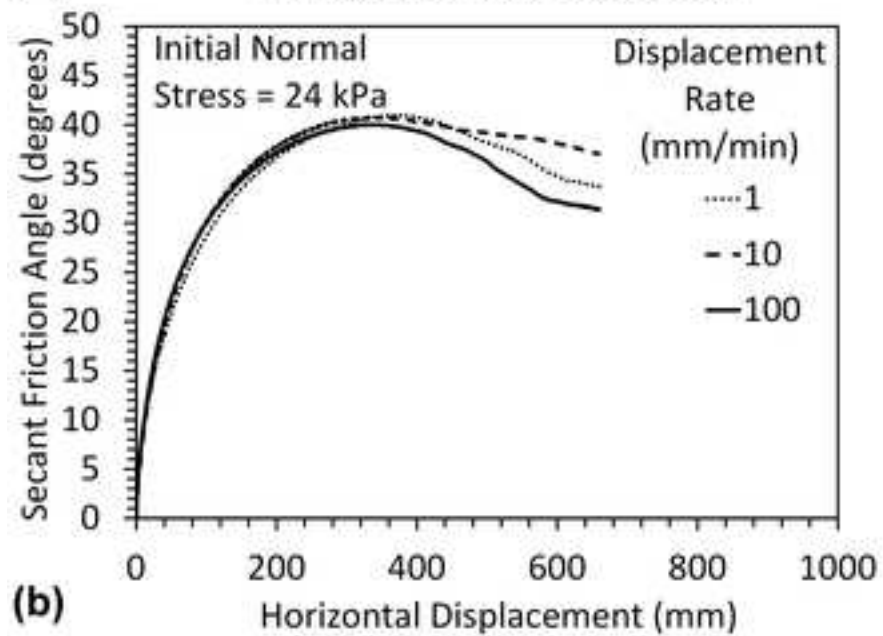


(d)

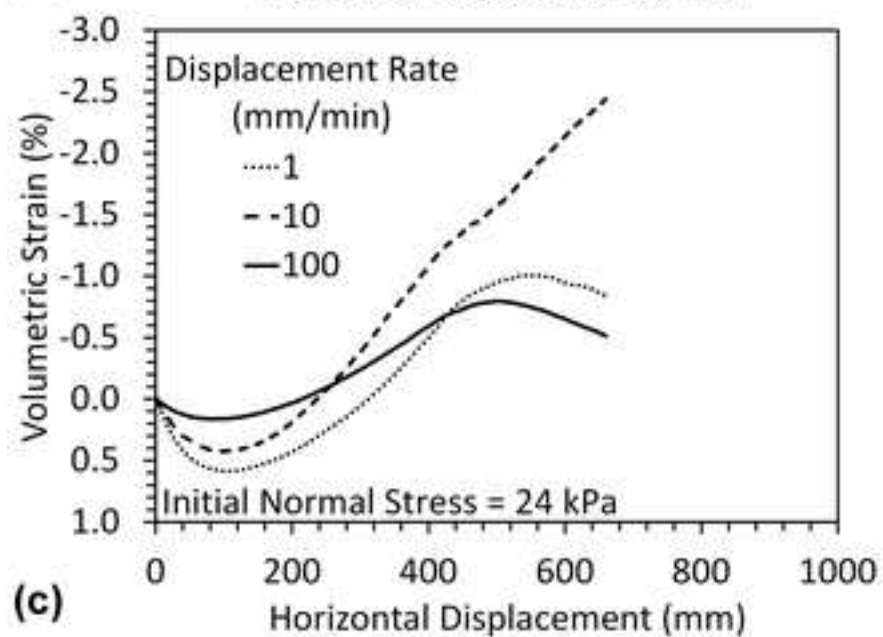




(a)



(b)



(c)

