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# Evaluation of affine fiber kinematics in porcine tricuspid valve leaflets using polarized spatial frequency domain imaging and planar biaxial testing

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# Abstract

Collagen fibers are the primary load-bearing microstructural constituent of bodily soft tissues, and, when subjected to external loading, the collagen fibers reorient, uncrimp, and elongate. Specific to the atrioventricular heart valve leaflets, the collagen fiber kinematics form the basis of many constitutive models; however, some researchers claim that modeling the affine fiber kinematics (AFK) are sufficient for accurately predicting the macroscopic tissue deformations, while others state that modeling the non-affine kinematics (i.e., fiber uncrimping together with elastic elongation) is required. Experimental verification of the AFK theory has been previously performed for the mitral valve leaflets in the left-side heart; however, this same evaluation has yet to be performed for the morphologically distinct tricuspid valve (TV) leaflets in the right-side heart. In this work, we, for the first time, evaluated the AFK theory for the TV leaflets using an integrated biaxial testing-polarized spatial frequency domain imaging device to experimentally quantify the load-dependent collagen fiber reorientations for comparison to the AFK theory predictions. We found that the AFK theory generally underpredicted the fiber reorientations by  $3.1^{\circ}$ , on average, under the applied equibiaxial loading with greater disparity when the tissue was subjected to the applied non-equibiaxial loading. Furthermore, increased AFK errors were observed with increasing collagen fiber reorientations (Pearson coefficient r = -0.36, equibiaxial loading), suggesting the AFK theory is better suited for relatively smaller reorientations. Our findings suggest the AFK theory may require modification for more accurate predictions of the collagen fiber kinematics in the TV leaflets, which will be useful in refining modeling efforts for more accurate TV simulations.

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heart valves; collagen fibers; polarized light collagen imaging; soft tissue biomechanics; collagen reorientations

# 1. Introduction

The mechanical behaviors and material anisotropy of soft tissues are connected to the underlying microstructure, which consists of collagen fibers embedded in a nonfibrous matrix. Constitutive models based on hyperelasticity theory enable modeling of the behaviors of the microstructural components and connecting those microscopic, microstructural, and mechanical contributions to the macroscopic material deformations. Using this approach, constitutive formulation becomes straightforward by including the mechanics of the collagen fibers, elastin fibers, and nonfibrous matrix; however, the proper assumptions for modeling the microstructural contributions, such as the collagen or elastin fiber kinematics and the fiber and nonfibrous matrix coupling, have yet to be systematically determined for some tissues, such as the atrioventricular heart valve (AHV) leaflets. The collagen fibers in the AHV leaflets are naturally crimped with a preferential alignment to the circumferential tissue direction (Kunzelman et al., 1993; Sacks and Yoganathan, 2007). As loading is applied to the tissue, the collagen fibers reorient towards the primary loading direction, which contributes to the low-stress "toe-region" of the stress-stretch behaviors. After reorientation, the fibers uncrimp and elongate, which manifests as the high-stress, asymptotic regime. The collagen fiber kinematics form the basis of many constitutive models, but there remains no consensus on how the collagen model should be formulated: some AHV leaflet models are based on affine fiber kinematics (AFK) (Anssari-Benam and Bucchi, 2018; Jacobs et al., 2013; Lanir, 2017; Lee et al., 2015; Fan and Sacks, 2014), while other models include the non-affine fiber kinematics (non-AFK), especially when tissue viscoelasticity is critical (Bianchi et al., 2020; Dhume and Barocas, 2019; Morin et al., 2018). Herein, AFK is defined as a homogeneous deformation in which the fibers, usually considered as straight fibers without crimp, follow the tissue-level specimen deformation (e.g., parallel fibers in the reference configuration map to parallel fibers in the deformed configuration) (Tadmor et al., 2012). On the other hand, non-AFK is characterized by fibers undergoing inhomogeneous deformations that do not follow the macroscopic tissue deformation, potentially caused by shear deformations or fiber elongation and uncrimping.

Previous studies on soft tissue biomechanics have shown that the use of the AFK theory must be validated on a per-tissue basis. This is exemplified by the finding of a prior study that a modified AFK theory is required for the mitral valve (MV) leaflets (Lee et al., 2015), while other studies of tendons or small intestinal submucosa have noted the AFK theory to be invalid, especially in cases of large strain (Jayyosi et al., 2017; Lake et al., 2012a; Billiar and Sacks, 1997; Gilbert et al., 2006). Moreover, some researchers have noted the *in vitro* tissue testing conditions could affect the observed fiber kinematics. For example, some studies of soft tissues, such as liver, skin, and arteries, conducted bulge/inflation testing and noted minimal fiber reorientations (Cavinato et al., 2017; Jayyosi et al., 2017), while other studies have performed uniaxial testing of tendons and observed significant fiber

reorientations and non-AFK behaviors (Cavinato et al., 2020; Jayyosi et al., 2017; Lake et al., 2012a). It has also been suggested that interactions between collagen fibers and the nonfibrous matrix could play a role in the accuracy of the AFK assumption. Specifically, a stiffer nonfibrous matrix could result in more non-AFK behaviors as the fibers cannot easily reorient (Zhang et al., 2013). Those observations and theories from previous studies necessitate additional examinations of the AFK theory and further insight to the collagen fiber architecture (CFA) of specific tissues, such as the tricuspid valve (TV) leaflets. While a prior study has been performed to evaluate the AFK of the MV leaflets (Lee et al., 2015), the TV leaflets undergo a lower pressure gradient in the right side of the heart compared to their MV counterpart on the left side of the heart, i.e., 25 mmHg vs. 100 mmHg (Khoiy and Amini, 2016; Pierlot et al., 2015). Thus, these AHV tissues that have different functional environments may have different microstructural properties and behaviors that necessitate their own AFK-based investigations (Jett et al., 2018; Kramer et al., 2019).

In this work, we provide a *first-of-its-kind* evaluation of the AFK assumption for the tricuspid valve leaflets using an integrated biaxial testing-polarized spatial frequency domain imaging (pSFDI) device. The non-destructive collagen fiber imaging technique enabled quantification of the load-dependent changes in the CFA of the TV leaflets, which were then compared to the predictions of the AFK theory to evaluate the viability in capturing the collagen fiber reorientations. Unlike previous studies using small-angle light scattering (Sacks et al., 1997, 1998), our approach is beneficial as the pSFDI modality does not require tissue fixation, allowing for the observation of collagen fiber reorientations and fiber kinematics within the same tissue specimen. Additionally, the biaxial testing scheme was rarely performed in the previous AFK-based experiments for the mitral valve leaflets and the other tissues (Lee et al., 2015; Pham et al., 2017), and thus, our findings could be helpful for understanding differences in collagen fiber kinematics under different experimental testing conditions. The results of this work will be useful for a refined understanding of AFK in the TV leaflets and for future refinement of accurate microstructure-informed constitutive models and TV simulations.

## 2. Methods

## 2.1. Tissue acquisition and preparation

Porcine hearts were obtained from Animal Technologies (Dallas, TX) and stored in a freezer at -14 °C for prolonged tissue storage. Freezer storage of the tissues was performed based on our previous work that demonstrated minimal changes in the observed mechanical properties between the fresh (unfrozen) and frozen tissues (Duginski et al., 2020). At the time of testing, the hearts were thawed, and the tricuspid valves were dissected (Fig. 1a) to retrieve the TV anterior leaflets, posterior leaflets, and septal leaflets (TVAL, *n* = 11; TVPL, *n* = 14; TVSL, *n* = 12). After dissection, the leaflets were further sectioned to obtain a 10×10 mm specimen from the central, belly region of the leaflet (Fig. 1b). The square specimens were then mounted to a commercial biaxial testing device (CellScale, Canada) via tined BioRakes (Fig. 1c), with the tissue's circumferential (Circ) and radial (Rad) directions aligned with the *X*- and *Y*-directions of the BioTester, respectively. The biaxial testing device was further equipped with an in-house pSFDI device (Fig. 1d), which was used in the

quantification of the CFAs of the TV leaflet specimens (see Section 2.3). Once the tissues were mounted to the biaxial testing system, glass beads were used to construct a 2×2 fiducial marker array in the center of the specimen for later tissue strain calculation based on digital image correlation (Jett et al., 2018; Ross et al., 2019). Tissues were then submerged in a 32 °C phosphate-buffered saline bath to emulate the physiological temperature. A temperature level slightly lower than body temperature (37 °C) was used to avoid previously observed issues related to polarizer fogging in the pSFDI portion of the experiment (Jett et al., 2020; Hudson et al., 2020).

#### 2.2. Biaxial mechanical testing

Biaxial mechanical testing was performed following our established protocols (Jett et al., 2018; Laurence et al., 2019). First, tissues were preconditioned through ten equibiaxial loading/unloading cycles to a targeted membrane tension of 50 N/m to emulate the physiologic loading of the valve leaflets (Khoiy and Amini, 2016). After preconditioning, tissue specimens were then biaxially loaded with varying ratios of biaxial tensions:  $T_{Circ}$ :  $T_{Rad} = 1:1, 0.66:1, 0.33:1, 1:0.66$ , and 1:0.33 (Fig. 1e). Each loading ratio was repeated for 4 loading/unloading cycles to ensure repeatability of the stress-strain behaviors, and the final loading cycle was used for tissue stress-stretch analysis. Throughout testing, the load cell readings were recorded and images were captured by a CCD camera at 5 Hz. After biaxial testing was completed, the pSFDI component of the integrated instrument was used to quantify the load-dependent CFAs of the TV leaflet specimens (Hudson et al., 2020; Jett et al., 2020).

### 2.3. Quantification of the load-dependent changes in collagen fiber architecture

To quantify the changes in the load-dependent CFA, an in-house pSFDI device was used (Fig. 1d). This device has been used in previous works from our laboratory, and the reader is referred to the pSFDI theory and details about the experimental procedure (Hudson et al., 2020; Jett et al., 2020). Briefly, the imaging modality relies on the polarization-dependent diattenuating properties of collagen fibers to quantify the collagen fiber orientations. The imaging sequence contains:

- a digital light projector casting incident light through a polarizer and onto the specimen at an angle  $\theta_{polarizer}$ .
- the polarized light reflected off of the specimen with an intensity *I*.
- the reflected light passing back through the polarizer at the angle  $\theta_{polarizer}$  and an image captured by a CCD camera.

The sequence is repeated for  $\theta_{polarizer} = 0^{\circ} - 180^{\circ}$  at 5° increments. Then, the light intensity- $\theta_{polarizer}$  response of the tissue was fit with a three-term Fourier series,

$$I = \gamma_0 + \gamma_2 [2(\theta_{fiber} - \theta_{polarizer}) + \gamma_4 [4(\theta_{fiber} - \theta_{polarizer})],$$

(1)

1

(2)

where  $\gamma_0$  represents the mean light intensity, and  $\gamma_2$  and  $\gamma_4$  are the coefficients representing the optical anisotropy. The experimentally measured fiber angle  $\theta_{fiber}$  was determined as the  $\theta_{polarizer}$  corresponding to the peak reflected light intensity *I*. Furthermore, the determined Fourier coefficients were then used to quantify the degree of optical anisotropy (DOA):

$$DOA = \frac{\gamma_2 + \gamma_4}{\gamma_0 + \gamma_2 + \gamma_4}.$$

The DOA is an optically based metric that describes the level of preferential fiber alignment along  $\theta_{fiber}$ . Note that  $\theta_{fiber}$  and the DOA were calculated on a pixel-by-pixel basis, offering a detailed representation of the spatially varying CFA of the TV leaflets. The pSFDI sequence was repeated at the post-preconditioning (PPC) configuration and at the deformation associated with the peak loading of each biaxial tension protocol to obtain the fiber orientations at the unloaded ( $\theta_{PPC}$ ) and loaded configurations ( $\theta_{exp}$ ), respectively. The reorientations of the collagen fibers were quantified via  $\theta_{reorient} = \theta_{exp} - \theta_{PPC}$ , where a positive  $\theta_{reorient}$  indicates a counterclockwise rotation, and a negative  $\theta_{reorient}$  indicates a clockwise rotation.

#### 2.4. Application of the affine fiber kinematics theory

Evaluation of the validity of the AFK theory requires the use of two components of our experimental measurements: (i) the unloaded fiber orientation  $\theta_{PPC}$  and (ii) the deformation gradient **F**. During post-processing of the acquired pSFDI information, we selected the region of interest for the AFK analysis to be within the 2×2 fiducial marker array, as the fiber kinematics would be more realistic than in the fibers near the tine insertion. The selected region of interest was further discretized into an isoparametric 100×100 grid of query points based on the isoparametric mapping concept in the context of finite element methods (Fig. 2a, Hughes (1987)). For each query point,  $\theta_{PPC}$  and  $\theta_{exp}$  were determined by a weighted Euclidean distance-based approach:

$$\theta_{j} = \frac{\sum_{k=1}^{25} w_{k}\theta_{k}}{\sum_{k=1}^{25} w_{k}},$$
(3)

where  $\theta_j$  represents the fiber angle of the  $j^{th}$  query point,  $\theta_k$  denotes the fiber angle at the  $k^{th}$  pixel within the domain of influence associated with the  $j^{th}$  query point, and  $w_k$  represents the weight, calculated as the Euclidean distance from the pixel location (p, q) of the  $j^{th}$  query point:  $w_k = \sqrt{(p - p_k)^2 + (q - q_k)^2}$ . Then, the unloaded fiber direction vector was constructed as  $\mathbf{N}_j = [\cos(\theta_{PPC,j}), \sin(\theta_{PPC,j})]^T$  for the  $j^{th}$  query point in the selected region of interest. Interested readers are referred to Belytschko et al. (1994).

For the deformation gradient **F**, the calculations were made based on the deformation of the fiducial marker array, as tracked via a custom MATLAB program (MathWorks, MA,

USA, Fig. 2b; Sacks (2000); Billiar and Sacks (1997)). The pixel locations of the markers in the undeformed, reference ( $\Omega_{PPC}$ ) configurations and the deformed configurations ( $\Omega_t$ ) were mapped to a parametric domain, and **F** was constructed as:

$$\mathbf{F} = \begin{bmatrix} \frac{\partial x}{\partial X} & \frac{\partial x}{\partial Y} \\ \frac{\partial y}{\partial X} & \frac{\partial y}{\partial Y} \end{bmatrix} = \begin{bmatrix} \lambda_1 & \kappa_1 \\ \kappa_2 & \lambda_2 \end{bmatrix},$$

where *X* and *Y* represent the undeformed marker locations, *x* and *y* denote the deformed marker locations,  $\lambda_1$  and  $\lambda_2$  are the axial stretches in the *X*- and *Y*-directions (i.e., Circ and Rad, respectively), and  $\kappa_j$  represents the shear deformations in the *X* – *Y* or *Y* – *X* directions.

Next, the AFK theory was adopted to determine the fiber orientation at each of the applied biaxial loading states:

$$\mathbf{n}_j = \frac{\mathbf{F} \cdot \mathbf{N}_j}{|\mathbf{F} \cdot \mathbf{N}_j|},$$

(5)

(4)

where  $\mathbf{n}_j = [\cos(\theta_{pred,j})\sin(\theta_{pred,j})]$  is the deformed fiber orientation associated with the  $j^{th}$  query point (Fig. 2c). To determine the AFK prediction errors, the difference between  $\theta_{pred}$  and  $\theta_{exp}$ was calculated as  $\theta_{error} = \theta_{pred} - \theta_{exp}$ , where a negative  $\theta_{error}$  corresponds to an *underprediction* of the AFK theory, and a positive  $\theta_{error}$  demonstrates an *overprediction*.

## 2.5. Statistical analysis

 $\theta_{pred}$  and  $\theta_{exp}$  from the 100×100 *query points* for each of the TV leaflet specimens are reported as the median±interquartile range (IQR). Quantities for all the specimens, including  $\theta_{error}$ and  $\lambda$ , are reported as the mean±standard error of the mean (SEM). To gain insight into the correlation between any two metrics, a Pearson correlation coefficient (*r*) was computed (*r* = 1 indicating a positive linear correlation between the two compared metrics, *r* = -1 signifying a negative linear correlation, and *r* = 0 representing no linear correlation).

# 3. Results

#### 3.1. Biaxial mechanical properties of the tricuspid valve leaflets

From the biaxial testing of the three TV leaflets, we observed the typical nonlinear, anisotropic nature of the soft tissues (Jett et al., 2018; Meador et al., 2020; Khoiy and Amini, 2016; Pokutta-Paskaleva et al., 2019). Stress-stretch curves for the TVAL, TVPL, and TVSL specimens as representative of the behavior of all the datasets are shown in Figure 3a–c. The average PPC and peak stretches for the five loading scenarios are shown in Table 1, whereas the stretches of each individual tested specimen are shown in Table S1. For all the tested specimens, the PPC stretches were: TVAL,  $\lambda_{PPC,Circ} = 1.17 \pm 0.03$ ,  $\lambda_{PPC,Rad} = 1.31 \pm 0.05$ ; TVPL,  $\lambda_{PPC,Circ} = 1.17 \pm 0.03$ ,  $\lambda_{PPC,Rad} = 1.36 \pm 0.04$ ,

and TVSL,  $\lambda_{PPC,Circ} = 1.17 \pm 0.03$ ,  $\lambda_{PPC,Rad} = 1.32 \pm 0.04$ . Under equibiaxial tensions, the tissue stretches were found as: *Circumferential*: 1.31±0.04 (TVAL), 1.38±0.07 (TVPL), 1.49±0.07 (TVSL); *Radial*: 1.48±0.06 (TVAL), 1.62±0.07 (TVPL), 1.72±0.08 (TVSL). We also observed the TVPL to be the most anisotropic among the three TV leaflets, which was quantified by the anisotropic index =  $\lambda_{Rad}/\lambda_{Circ}$ : TVAL, 1.13±0.04; TVPL, 1.21±0.07; and TVSL, 1.16±0.05.

## 3.2. Experimentally measured collagen fiber architectures

The pSFDI-quantified CFA results for the TVAL, TVPL, and TVSL specimens as representative of the behavior of all the datasets are shown in Figure 3. The measured CFA results of all three TV leaflets under the applied *equibiaxial loading* are presented in Table 2, while the findings from the applied *non-equibiaxial loading* protocols are given in Tables S2–S4 of the Supplementary Material section. Generally, an increase in the fiber alignment was observed with increased loading, as exemplified by the DOA; however, there were less drastic changes in the fiber orientation. Specifically, the changes in the fiber orientations between the PPC and the applied equibiaxial loading states were found as: TVAL,  $-2.3^{\circ}\pm 2.7^{\circ}$ ; TVPL,  $4.4^{\circ}\pm 3.4^{\circ}$ ; and TVSL,  $1.5^{\circ}\pm 2.8^{\circ}$ . In the applied non-equibiaxial loading, we observed more fiber reorientations towards the dominant loading direction (e.g., more circumferential fiber orientations under  $T_{Circ}$ :  $T_{Rad} = 1:0.33$ ), with greater reorientations occurring with more disproportionate loading in the two directions (e.g.,  $17.8^{\circ}\pm 4.0^{\circ}$  changes under  $T_{Circ}$ :  $T_{Rad} = 0.66:1$ ).

## 3.3. Evaluation of the AFK predictivity

The vector plots of the experimentally measured and the AFK-predicted fiber orientations for the representative TVAL, TVPL, and TVSL specimens are shown in Figures 4–6. Comparing the AFK-predicted and the experimental fiber reorientations in the TV leaflets, we observed that the AFK theory generally underpredicted the fiber rotations (Table 2). Specifically,  $\theta_{error}$  from the applied equibiaxial loading protocol: TVAL,  $-1.6^{\circ}\pm 1.6^{\circ}$ ; TVPL,  $-2.9^{\circ}\pm 2.4^{\circ}$ ; and TVSL,  $-4.6^{\circ}\pm 1.0^{\circ}$ . We also noted a greater disparity between the AFK theory and the pSFDI-quantified CFA under the applied non-equibiaxial loading (Tables S1–S3). For example, under  $T_{Cire}$ :  $T_{Red} = 0.33$ : 1,  $\theta_{error}$  was found as:  $-4.0^{\circ}\pm 4.8^{\circ}$  (TVAL);  $-5.0^{\circ}\pm 4.3^{\circ}$  (TVPL), and;  $-7.4^{\circ}\pm 4.0^{\circ}$  (TVSL).

# 4. Discussion

#### 4.1. Differences in experimental and predicted collagen fiber reorientations

In this study, we have evaluated the AFK theory for the TV leaflets *for the first time* using a biaxial testing-pSFDI approach. We observed that the AFK theory generally underpredicted the rotations of the fibers. To elaborate, weak-to-moderate negative correlations were found between  $\theta_{reorient}$  and  $\theta_{error}$  across all the applied loading scenarios: equibiaxial loading, r = -0.36; circumferentially dominant loading, r = -0.29 to 0.07; and radially dominant loading, r = -0.29 to -0.24. By comparing  $\theta_{error}$  and  $\lambda$ , we found weak negative correlations under the applied equibiaxial loading (Circumferential, r = -0.17; Radial, r = -0.02), while under non-equibiaixal loading the correlation was stronger in the dominant loading

direction: circumferentially dominant loading, circumferential direction: r = -0.27 to -0.18; and radially dominant loading, radial direction: r = -0.02 to -0.32. The observed trends suggest that increasing collagen fiber reorientations result in an increased magnitude of underpredictions by the AFK theory, which may be further related to the increasing magnitude of the tissue deformations. This trend can be corroborated with a previous vasculature testing study that reported the AFK errors could be associated with excessive tissue deformations (Cavinato et al., 2020).

Another explanation for the mispredictions could be related to the direction of applied loading with respect to the preferred fiber orientations. A study by Lake et al. (2012a) performed uniaxial testing of human supraspinatus tendons and observed that the AFK predictions were less accurate when the loading was applied transverse to the preferred fiber orientation, and when there was a greater dispersion of fibers. We are unable to demonstrate this finding, however, because: (i) in the present study, we performed biaxial testing, and (ii) our pSFDI device quantifies the *optical anisotropy* of the material, which is not a direct measurement of the fiber dispersion. This imaging modality requires more research to be able to quantify the *structural* fiber dispersion. Regardless, it is worth highlighting that we observed a weak correlation between tissue anisotropy, which may be related to the fiber dispersion and  $\theta_{error}(r = 0.15)$ . Other causes for the AFK mispredictions include the potential for heterogeneous, locally varying affine kinematics (Krasny et al., 2017), the experimental testing conditions inducing varying affine or non-affine fiber kinematics (Jayyosi et al., 2017), or the fiber crimp causing significant AFK prediction errors (Lee et al., 2015).

Mispredictions from the AFK theory could also be related to the coupling between the fibers and the nonfibrous matrix. This idea is supported by a fiber-matrix model from Zhang et al. (2013), in which a more compliant non-fibrous matrix resulted in more fiber reorientations, while a stiffer nonfibrous matrix lead to more fiber stretching. This coupling effect was also observed in the modeling of collagenous gels (Lake et al., 2012b). The refinement of the AFK assumption based on these intricate non-fibrous matrix interactions requires further experimental and modeling efforts.

#### 4.2. Considerations for constitutive modeling using affine fiber kinematics

While the exact sources of the errors from the AFK theory are uncertain, the mispredictions should be considered in the formulation of constitutive models. To this end, previous researchers have proposed various improvements to the AFK theory. For example, in the work by Lee et al. (2015) performing biaxial testing and small-angle X-ray scattering of two mitral valve leaflets, they observed that including fiber crimp in the AFK theory yielded a more accurate prediction of the fiber reorientations. This correction may not hold for the TV leaflets, however, due to the mechanical and functional differences between the atrioventricular heart valves that could cause a different microstructure, morphology, and CFA (e.g., fibrillar density and dispersion) between the two AHVs. To date, no comprehensive investigation of the TV leaflet microstructure has been performed to confirm this theory, with only one recent study making a qualitative assessment via second harmonic generation (Pokutta-Paskaleva et al., 2019). Another AFK theory adjustment was made for the experiments and modeling of gelatin co-gels by including a correction factor to

accommodate the AFK errors (Liu et al., 2017). The correction factor implementation may be more robust for imaging modalities that cannot quantify fiber crimp, such as the pSFDI method used in the present study.

While a refinement of the AFK theory could provide a more computationally efficient methodology for modeling the collagen fiber behaviors, the incorporation of the non-AFK behaviors could lead to more accurate cardiac simulations and fiber kinematics predictions. In recent literature, there has been increasing focus on modeling non-AFK, and more work should be performed to realize more accurate and computationally inexpensive models, especially for use in modeling the tissue viscoelasticity (Bianchi et al., 2020; Dhume and Barocas, 2019; Liu et al., 2017; Morin et al., 2018; Chandran and Barocas, 2006). Furthermore, experimental works should be performed to understand the non-AFK (e.g., fiber uncrimping together with fiber elongation), such as through small-angle X-ray scattering combined with biaxial mechanical testing or stress-relaxation testing.

### 4.3. Limitations and future extensions

There are a few limitations of the present work. First, we used the pSFDI modality to determine the CFA of the TV leaflets, and, while the pSFDI modality has been shown to provide accurate quantifications of the collagen fiber orientations (Goth et al., 2016; Jett et al., 2020; Ross et al., 2020), there is the potential for mispredictions caused by surface imperfections on the tissue (glue, dust, etc.), or glare in the polarizer. Future studies are warranted to corroborate our results with additional imaging modalities, such as small-angle scattering or multiphoton microscopy. Second, the presented CFA results depict the average collagen fiber orientation through the thickness of the tissue and there could be mispredictions caused by fiber splay. Further investigations could be made using the spatial frequency domain imaging capabilities of the system to obtain quantifications of the CFA at discrete depths of the tissue thickness, allowing for more detailed AFKbased comparisons. Investigations of the regionally varying CFA and AFK mispredictions are further necessitated by previous studies demonstrated highly heterogeneous fiber reorganizations in the aortic valve cusps (Anssari-Benam et al., 2012) Additionally, we investigated the AFK assumption for the region within the central third of the tissue using only the deformation gradient obtained from the four fiducial markers. A more refined strain field could yield more accurate AFK results (Krasny et al., 2017); however, we could not implement a refined strain field without obstructing the view of the tissue for the pSFDI system. Finally, another future study could be performed using the biaxial testing-pSFDI approach to investigate the collagen fiber reorientations in the leaflets during viscoelastic characterizations, as was observed for the aortic valve cusps (Anssari-Benam et al., 2019).

#### 4.4. Conclusion

In this work, we have utilized the pSFDI technique to provide a detailed characterization of the load-dependent changes in the CFA of the three TV leaflets, and compared the experimentally measured fiber orientations to the AFK theory. To our knowledge, this work is *the first of its kind* for evaluating the AFK theory for the TV leaflets, which provides valuable insight for future computational modeling works that rely on AFK-based constitutive forms to describe the leaflet mechanical and microstructural behaviors.

Furthermore, another key contribution of this study is the use of biaxial testing to evaluate the AFK assumption, which is limited in the previous literature. The results of this study demonstrate the need for future experimental work to quantify the fibrous-nonfibrous matrix coupling or the non-AFK, such as crimping and uncrimping. Through an improved understanding of the collagen fiber kinematics in the TV leaflets, computational simulations can be refined for use in research areas such as tissue growth and remodeling to understand how diseases affect the CFA, which in turn impacts tissue mechanics and organ-level valve function.

# Supplementary Material

Refer to Web version on PubMed Central for supplementary material.

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## Figure 1:

(a) Porcine tricuspid valves dissected to obtain the (b) TV leaflets. A 10×10mm square specimen prepared from the central, belly region of the leaflet and (c) mounted via tined BioRakes to a (d) a coupled pSFDI-biaxial testing device. (e) Schematic of the membrane tension (T) loading ratios in the biaxial mechanical testing.



## Figure 2:

A schematic diagram of the methods used to acquire (a) the pSFDI-measured collagen fiber angles and (b) the experimentally measured deformation gradient  $\mathbf{F}$  from biaxial testing that were used to (c) predict the collagen fiber orientations from affine fiber kinematics theory.

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#### Figure 3:

Representative experimentally measured results from (a) TVAL #11, (b) TVPL #6, and (c) TVSL #10. The experimental photo from the pSFDI camera is provided (*left column*), along with the biaxial mechanical testing results (*middle column*), and the pSFDI-based collagen fiber orientations at the post-preconditioning (PPC) configuration and other applied biaxial tension protocols (*right column*). Note that the region of interest shown is for the full tissue specimen, while the AFK analysis was only performed for the region delimited by the fiducial markers.





Rad



#### Figure 4:

Comparisons of the AFK-predicted and pSFDI-measured collagen fiber orientations for a representative TVAL specimen (TVAL #11) at the (a) PPC deformation (experimental only) and at the peak deformation of various applied biaxial loading states: (b)  $T_{Circ}$ :  $T_{Rad} = 1:1$ , (c)  $T_{Circ}$ :  $T_{Rad} = 1:0.66$ , (d)  $T_{Circ}$ :  $T_{Rad} = 1:0.33$ , (e)  $T_{Circ}$ :  $T_{Rad} = 0.66:1$ , and (f)  $T_{Circ}$ :  $T_{Rad} = 0.33:1$ . Dashed lines denote the predicted and experimentally measured collagen fiber orientations for some selected pixels, the grayscale gradient represents the absolute error between the predicted and experimental findings, and the black circles represent the positions of the fiducial markers. Histograms denote the probability for the experimental collagen fiber orientations at each five-degree increment.

# (a) Unloaded (PPC)



Rad



#### Figure 5:

Comparisons of the AFK-predicted and pSFDI-measured collagen fiber orientations for a representative TVPL specimen (TVPL #6) at the (a) PPC deformation (experimental only) and at the peak deformation of various applied biaxial loading states: (b)  $T_{Circ}:T_{Rad} = 1:1$ , (c)  $T_{Circ}:T_{Rad} = 1:0.66$ , (d)  $T_{Circ}:T_{Rad} = 1:0.33$ , (e)  $T_{Circ}:T_{Rad} = 0.66:1$ , and (f)  $T_{Circ}:T_{Rad} = 0.33:1$ . Dashed lines denote the predicted and experimentally measured collagen fiber orientations for some selected pixels, the grayscale gradient represents the absolute error between the predicted and experimental findings, and the black circles represent the positions of the fiducial markers. Histograms denote the probability for the experimental collagen fiber orientations at each five-degree increment.



#### Figure 6:

Comparisons of the AFK-predicted and pSFDI-measured collagen fiber orientations for a representative TVSL specimen (TVSL #10) at the (a) PPC deformation (experimental only) and at the peak deformation of various applied biaxial loading states: (b)  $T_{Circ}$ :  $T_{Rad} = 1:1$ , (c)  $T_{Circ}$ :  $T_{Rad} = 1:0.66$ , (d)  $T_{Circ}$ :  $T_{Rad} = 1:0.33$ , (e)  $T_{Circ}$ :  $T_{Rad} = 0.66:1$ , and (f)  $T_{Circ}$ :  $T_{Rad} = 0.33:1$ . Dashed lines denote the predicted and experimentally measured collagen fiber orientations for some selected pixels, the grayscale gradient represents the absolute error between the predicted and experimental findings, and the black circles represent the positions of the fiducial markers. Histograms denote the probability for the experimental collagen fiber orientations at each five-degree increment.

## Table 1:

The post-preconditioning (PPC) stretches and peak stretches of the TVAL, TVPL, and TVSL specimens under the five applied biaxial tensions ( $T_{Circ}$ :  $T_{Rad}$ ). Results are presented as the mean±SEM.

	TVAL		TV	PL	TVSL	
Loading Protocol	Circ	Rad	Circ	Rad	Circ	Rad
PPC	1.17±0.03	1.31±0.05	1.17±0.03	1.36±0.04	1.17±0.03	1.32±0.04
1:1	1.31±0.04	1.48±0.06	1.38±0.07	1.62±0.07	$1.49{\pm}0.07$	1.72±0.08
1:0.66	1.33±0.05	1.44±0.06	$1.40{\pm}0.08$	$1.57{\pm}0.07$	$1.53 \pm 0.07$	1.65±0.07
1:0.33	1.36±0.05	1.33±0.05	1.43±0.08	1.43±0.06	$1.58 \pm 0.07$	1.47±0.06
0.66:1	1.27±0.04	$1.50{\pm}0.07$	1.34±0.07	1.64±0.07	1.43±0.06	1.75±0.08
0.33:1	1.15±0.03	1.58±0.08	1.25±0.06	1.69±0.07	1.26±0.05	1.85±0.08

## Table 2:

Comparisons of the collagen fiber angle between the pSFDI measurements and AFK predictions at the postpreconditioning (PPC) and peak equibiaxial deformations ( $T_{Circ}$ :  $T_{Rad} = 1:1$ ) for all TVAL, TVPL, and TVSL specimens. The  $\theta_{median}$  and IQR are provided for the 100×100 grids considered for each specimen, and the  $\theta_{error}$ between the measured and predicted fiber orientations at the peak deformation are expressed as the mean±SD.

		РРС		$T_{Circ}$ : $T_{Rad} = 1:1$					
		Measured $\theta_{exp}$		Measured $\theta_{exp}$		Predicted $ heta_{pred}$		0	
Leaflet	Specimen ID	Median	IQR	Median	IQR	Median	IQR	$\theta_{error}$	
	1	149.1°	10.9°	154.4°	7.6°	141.2°	8.7°	-12.6°±22.9°	
	2	115.4°	39.5°	142.5°	45.2°	116.3°	39.9°	-4.5°±21.2°	
	3	38.4°	21.5°	40.9°	11.0°	38.0°	19.3°	-6.9°±23.8°	
	4	162.6°	24.4°	156.7°	62.9°	162.1°	17.2°	-1.8°±28.2°	
	5	96.5°	13.5°	92.2°	9.5°	99.8°	14.7°	-0.3°±12.6°	
TVAL	6	111.2°	11.4°	114.3°	10.5°	113.4°	11.2°	0.4°±7.8°	
	7	80.8°	6.6°	78.2°	5.7°	82.8°	7.4°	-1.2°±20.8°	
	8	151.5°	3.5°	146.5°	4.1°	150.5°	3.7°	5.0°±12.2°	
	9	141.1°	43.1°	144.5°	30.3°	141.5°	43.6°	5.5°±25.5°	
	10	132.4°	13.5°	134.6°	15.3°	129.7°	13.6°	-4.0°±7.5°	
	11	104.9°	14.7°	104.7°	8.6°	103.1°	15.1°	2.4°±13.5°	
TVPL	1	112.6°	10.0°	118.4°	14.7°	115.2°	10.4°	-1.7°±16.8°	
	2	16.8°	144.8°	21.2°	137.3°	19.4°	138.0°	0.1°±20.1°	
	3	157.8°	9.9°	155.8°	9.7°	154.3°	10.3°	-2.2°±13.6°	
	4	124.4°	21.3°	121.8°	21.0°	123.5°	20.7°	2.0°±22.6°	
	5	136.0°	11.1°	94.6°	77.3°	134.3°	11.7°	-30.8°±38.9°	
	6	156.6°	13.3°	152.2°	8.2°	155.4°	14.2°	0.0°±14.9°	
	7	152.2°	15.0°	155.5°	17.6°	152.3°	15.0°	-3.3°±20.2°	
	8	169.6°	14.1°	162.2°	15.4°	166.0°	78.3°	10.0°±20.6°	
	9	121.8°	24.8°	119.6°	26.5°	119.7°	20.8°	-6.0°±14.6°	
	10	132.8°	31.0°	136.9°	34.7°	128.9°	28.6°	-6.7°±13.6°	
	11	80.1°	26.0°	57.9°	41.1°	81.9°	25.6°	$-1.0^{\circ}\pm-0.9^{\circ}$	
	12	136.7°	24.9°	142.5°	28.1°	136.5°	25.4°	-0.9°±20.2°	
	13	78.5°	11.7°	79.9°	13.6°	76.5°	12.1°	-2.9°±12.5°	
	14	73.5°	32.0°	68.6°	36.5°	75.1°	30.1°	2.7°±14.1°	
TVSL	1	113.1°	23.9°	123.8°	32.4°	114.7°	22.6°	-4.9°±21.1°	
	2	147.1°	21.0°	139.0°	64.0°	145.9°	21.3°	$-4.2^{\circ}\pm19.6^{\circ}$	
	3	165.6°	20.6°	148.6°	155.3°	164.8°	23.6°	-6.9°±29.0°	
	4	8.7°	99.3°	10.2°	7.5°	9.6°	94.1°	-12.2°±29.7°	
	5	101.4°	37.8°	108.3°	33.8°	98.1°	39.5°	-4.8°±15.3°	
	6	102.5°	27.3°	100.4°	35.3°	101.7°	24.9°	$-8.9^{\circ}\pm29.5^{\circ}$	

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		РРС		$T_{Circ}:T_{Rad}=1:1$					
		Measured $\theta_{exp}$		Measured $\theta_{exp}$		Predicted $\theta_{pred}$		A	
Leaflet	Specimen ID	Median	IQR	Median	IQR	Median	IQR	Uerror	
	7	124.5°	49.4°	102.1°	74.8°	126.8°	40.7°	-4.4°±38.8°	
	8	34.1°	130.8°	35.6°	128.7°	36.0°	128.0°	-1.6°±24.0°	
	9	106.5°	16.9°	108.2°	17.2°	106.2°	15.8°	-1.4°±12.6°	
	10	15.2°	14.5°	14.2°	14.0°	16.4°	14.7°	-1.0°±19.7°	
	11	92.4°	13.9°	96.8°	70.6°	90.3°	13.3°	-2.5°±47.0°	
	12	156.8°	20.5°	162.7°	13.6°	153.9°	20.6°	-2.8°±32.9°	