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Modeling enzyme competition in eicosanoid metabolism in macrophage cells using a cybernetic framework

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Abstract Cellular metabolism is a complex process involving the consumption and production of metabolites, as well as the regulation of enzyme synthesis and activity. Modeling of metabolic processes is important to understand the underlying mechanisms, with a wide range of applications in metabolic engineering and health sciences. Cybernetic modeling is a powerful technique that accounts for unknown intricate regulatory mechanisms in complex cellular processes. It models regulation as goal-oriented, where the levels and activities of enzymes are modulated by the cybernetic control variables to achieve the cybernetic objective. This study used cybernetic model to study the enzyme competition between arachidonic acid (AA) and eicosapentaenoic acid (EPA) metabolism in murine macrophages. AA and EPA compete for the shared enzyme cyclooxygenase. Upon external stimuli, AA produces proinflammatory 2-series prostaglandins and EPA metabolizes to antiinflammatory 3-series prostaglandins, where proinflammatory and antiinflammatory responses are necessary for homeostasis. The cybernetic model adequately captured the experimental data for control and EPA-supplemented conditions. The model is validated by performing an F-test, conducting leave-one-out-metabolite cross-validation, and predicting an unseen experimental condition. The cybernetic variables provide insights into the competition between AA and EPA for the cyclooxygenase enzyme. Predictions from our model suggest that the system undergoes a switch from a predominantly proinflammatory state in the control antiinflammatory to an state with EPAsupplementation. The model can also be used to analytically determine the AA and EPA concentrations required for the switch to occur. III The quanenhance understanding titative outcomes of proinflammatory and antiinflammatory metabolism in RAW 264.7 macrophages.

Supplementary key words arachidonic acid • cyclooxygenase • inflammation • lipidomics • lipolysis and fatty acid metabolism •

omega-3 fatty acid • prostaglandin • eicosapentaenoic acid • kinetic modeling

A metabolic system consists of a cascade of chemical reactions that result in the production of diverse metabolites, facilitated by specific enzymes acting on substrates. A comprehensive understanding of metabolic processes is essential for implementing genetic modifications to enhance metabolic performance as well as control biological processes (1, 2). Quantitative modeling of these metabolic processes can be a valuable tool in achieving these objectives (3-12). In cellular metabolism, enzymes are regulated by various mechanisms, including synthesis and modulation of their activity. Mechanistic insights can be gained from models such as flux balance analysis, and kinetic models such as the Michaelis-Menten formulation, adapted for various scenarios including ping-pong kinetics, sequential kinetics, and competitive or noncompetitive enzyme inhibition (9, 13–24). However, these models may not fully incorporate the complex regulatory mechanisms as the specific details of these regulatory processes are often not well understood, which makes it challenging to incorporate them into the models (25–28). The cybernetic modeling approach, a technique used for modeling of cellular metabolic processes, addresses this limitation by defining a biological goal that the system aims to optimize. It also takes into account the dynamics of enzymes, which allows the model to predict enzyme profiles necessary for metabolism, even in cases where enzyme measurements are unavailable (25–27). The biological goal is formulated as the cybernetic goal and refers to the maximization of the sum of fluxes associated with selected metabolites/ processes. The model assumes that the system achieves the formulated goal by adjusting the levels and activities of the enzymes involved in the respective reactions,



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and the reactions compete for available resources necessary for metabolic transformations. To represent this competition, the cybernetic model introduces cybernetic control variables, denoted as u and v, for the participating metabolites. The variable *u* represents the control variable for the enzyme synthesis process and allocates resources for metabolic conversions in the competing reactions. The cybernetic variable v regulates the activity of the corresponding enzyme. These control variables consider both known and unknown regulatory steps and modulate the competing reactions to achieve the specified biological goal (25-27). The cybernetic framework has undergone progressive evolution, surpassing its initial limitations and emerging as a promising approach to comprehensively and quantitatively describe metabolism. Cybernetic models have been successfully applied to describe various biological phenomena in unicellular organisms such as yeast and bacteria cells (29, 30). More recently, cybernetic models have also been used to study the inflammatory responses in mammalian cells (28, 31).

Arachidonic acid (AA) is an omega-6 PUFA, which produces proinflammatory 2-series prostaglandins (PGs) through the action of the cyclooxygenase (COX) enzyme. These 2-series PGs initiate acute inflammation and mediate pain and other symptoms during the inflammatory response (32-34). In contrast, eicosapentaenoic acid (EPA) and docosahexaenoic acid (DHA), which are omega-3 PUFAs, form antiinflammatory metabolites (35-38). While humans can synthesize EPA and DHA from α -linolenic acid to some extent, it is necessary to supplement them through dietary sources such as fish, nutraceuticals, and functional foods (38–41). Consumption of fish or fish oil, which is a significant source of EPA and DHA, reduces the production of proinflammatory 2-series PGs (38, 42, 43). This occurs because EPA and DHA compete with AA by (1) replacing it in the cell membrane phospholipid bilayer, thereby reducing the availability of AA for metabolism, and (2) sharing the COX enzyme. EPA and DHA are metabolized by COX to produce 3-series PGs. Unlike the proinflammatory AA-derived mediators, the 3-series PGs exhibit antiinflammatory actions by decreasing leukocyte chemotaxis, reactive oxygen species levels, and proinflammatory cytokine secretion (44-46). They also reduce adhesion molecule expression and inhibit platelet aggregation (44, 45). The production of proinflammatory lipid mediators from AA and antiinflammatory lipid mediators from EPA metabolism plays a critical role in initiating, progressing, and resolving the inflammatory response. Dysregulation of these processes can lead to chronic inflammation, tissue damage, and impaired healing (33, 34, 47-49). Excessive proinflammatory response contributes to the severity and progression of various diseases, including cancer and coronavirus disease 2019 (COVID-19) (50, 51). The antiinflammatory properties of lipid mediators make them potential therapeutic

agents for these inflammatory conditions. Research suggests that the antiinflammatory nature of EPA and DHA can be beneficial in reducing the severity of diseases such as cancer, cardiovascular effects, and promoting visual and neurological development (37, 52–54). Nonsteroidal antiinflammatory drugs, which inhibit COX, are commonly used pharmacotherapeutic agents for treating inflammation. They exhibit antiinflammatory effects and help to block and alleviate inflammation (31–37). Studies involving humans have reported reduced mortality rates in patients with diseases due to increased intake of EPA-containing diets (55).

Computational kinetic models have proven to be valuable tools for understanding the underlying principles and uncovering novel mechanisms by capturing experimental data. In previous studies, linear or Michaelis-Menten kinetics were commonly used to capture the dynamic measurements of eicosanoid production resulting from AA metabolism (9, 20-24). While some experimental studies have investigated the metabolic analysis of AA profiles upon EPA/DHA supplementation (56-59), fewer studies have focused on modeling the reaction network involving EPA/DHA. Norris and Dennis conducted an experimental study revealing a decrease in 2-series PGs and an increase in 3-series PGs in RAW 264.7 macrophages upon EPA and DHA supplementation (59). The observed phenomenon was attributed to AA and EPA/DHA competition for the enzyme COX. Gupta et al. developed a kinetic model using Michaelis-Menten dynamics to describe the competitive metabolism between AA and EPA/DHA (21). While their model reasonably captured general trends and saturating effects, it failed to accurately predict specific data points that deviated from the Michaelis-Menten behavior. One limitation of the Gupta et al. model was the noninclusion of mechanisms that are associated with metabolic regulation such as transcriptomic, translational, and posttranslational regulation and modifications. Our study suggests that usage of the cybernetic model can improve their model accuracy by incorporating known and unknown regulatory processes. Previous applications of cybernetic models have primarily focused on studying the dynamics of eicosanoids produced from the metabolism of AA during the inflammatory response of mammalian cells. This study aims to develop a cybernetic model for the reaction networks involving AA and EPA/DHA.

We developed a cybernetic model to study the AA and EPA/DHA metabolism in RAW 264.7 macrophage cells during the inflammatory response. AA and EPA/DHA share the enzyme COX to form proinflammatory 2-series and antiinflammatory 3-series PGs, respectively (21, 59). A recent study by Zaid *et al.* (60) observed high levels of both series PGs in intubated COVID-19 patients, emphasizing the critical roles of both stages of inflammation. Building upon these findings, we hypothesized that the biological goal during the

inflammatory response is to maximize the combined proinflammatory and antiinflammatory responses in physiology. The cybernetic goal for AA and EPA/DHA metabolism is formulated to maximize AA and EPA/ DHA consumption rates, as they are precursors of 2series and 3-series PGs, respectively. The measurements are available for three scenarios: (1) the control: nonsupplemented, (2) EPA-supplemented, and (3) DHA-supplemented cases (59). The EPA-supplemented case was used to train the model, and it demonstrated reasonable agreement with the experimental data. It effectively captured the competitive nature between AA and EPA for the shared COX enzyme, represented as e_{COX} . We also validated the model by (1) performing an F-test to evaluate the goodness of fits, (2) performing leave-one-out-metabolite PGD₂ cross-validation, and (3) predicting an unseen case of DHA supplementation. The predictions of enzyme profiles are realistic and corroborate the dynamics observed in the metabolite profiles. The dynamics of the cybernetic control variables effectively reflect the prevailing proinflammatory or antiinflammatory conditions observed in the experimental datasets.

MATERIALS AND METHODS

The reaction network for AA and EPA metabolism is shown in Fig. 1. AA metabolism produces PGH₂, PGE₂, PGD₂, 15d-PGD₂, PGJ₂, and DHK-PGD₂. EPA metabolism forms PGH₃, PGE₃, and PGD₃. The measurements for PGH₂ and PGH₃ are not available because of their highly unstable structure. The experimental data on ATP activated RAW 264.5 is available for three conditions (1) control nonsupplemented, (2) EPA supplemented, and (3) DHA supplemented (59). The measurements are made at 0, 2.5, 5, 10, 15, 30, and 60 min post ATP stimulation. The control scenario has basal level of AA, and for EPA (DHA)-supplemented case, EPA (DHA) is added 24 h before ATP stimulation. ATP is a danger signal and an inflammatory stimulus. It activates cytosolic phospholipase A2, producing free AA through hydrolysis of AA esterified in membrane phospholipids (61). The 2-series PGs, including PGE₂, PGD₂, 15d-PGD₂, PGJ₂, and DHK-PGD₂, are formed due to AA metabolism. The data for the 2-series PGs are measured for the three experimental conditions mentioned above. The data for the 3-series PGs are measured for the control and EPA-supplemented scenarios. In the nonsupplemented (control) condition, the low levels of EPA prevent significant conversion to 3-series PGs, resulting in negligible levels of these metabolites in the control scenario. However, upon supplementation with EPA or DHA, increased levels of EPA or DHA, respectively, are observed. ATP stimulation triggers EPA metabolism to produce 3-series PGs, comprising PGE_3 and PGD_3 (44). The DHA metabolism includes the product electrophile oxo-derivatives (EFOXs) due to the action of the COX enzyme, but the EFOXs measurements are not available for control and DHAsupplemented condition (62). Moreover, Fig. 2 demonstrates the mathematical framework of the cybernetic model for AA and EPA metabolism in mammalian cells, which is discussed in detail subsequently.

Cybernetic goal formulation

The cybernetic model assumes a cybernetic goal, which is the mathematical representation of the defined biological goal. The cybernetic goal aims to maximize the cumulative fluxes of specific metabolites that effectively reflect the desired biological goal. The reaction fluxes of these selected set of n reactions compete to maximize their individual contributions to the cybernetic goal. The cybernetic goal is formulated as Equation 1.

$$\max \sum_{i=1}^{n} \rho_{-i} \tag{1}$$

where ρ_i is the reaction flux for each of these *n* metabolites. In this study, the cybernetic goal for AA and EPA metabolic network is hypothesized as maximizing the sum of AA and EPA consumption rates. PGH₂ and PGH₃ are chosen for the cybernetic goal formulation because they are the precursors of the proinflammatory and antiinflammatory conversions of AA and EPA, respectively. Consequently, the cybernetic goal is to maximize the sum of production rates of PGH₂ and PGH₃, respectively (Equations 2 and 3). This is true because our network includes the conversion of AA and EPA to PGH₂ and



Fig. 1. The arachidonic acid (AA) and eicosapentaenoic acid (EPA) reaction network. AA and EPA metabolism leads to 2-series and 3-series PGs, respectively. The 2-series PGs include PGD₂, PGE₂, dPGD2, and PGJ₂. PGD₃ and PGE₃ are 3-series PGs. Darker blue ovals represent measured metabolites. Light blue ovals represent unmeasured intermediates, PGH₂ and PGH₃. Green-colored dashed boxes represent enzymes. The COX enzyme (e_{COX}) metabolizes AA and EPA. Similarly, e_{Piges} , e_{Pigds} catalyze the conversion of PGH₂ and PGH₃ into downstream products. COX, cyclooxygenase; PG, prostaglandin.

PGH₃ only, respectively. We denote the outflux (consumption rate) of AA and EPA by ρ_{AA}^{out} and ρ_{EPA}^{out} , respectively (Equation 2). Similarly, the influx (production rate) of PGH₂ is denoted by $\rho_{PGH_2}^{in}$, and PGH₃ by $\rho_{PGH_2}^{in}$. The definitions of $\rho_{PGH_2}^{in}$ and $\rho_{PGH_2}^{in}$ are shown in (Equation 3). The cybernetic goal is formulated as follows (Equation 2). [.] represents the concentration.

$$\max \rho_{AA}^{out} + \rho_{EPA}^{out} = \max \left[\rho_{PCH_2}^{in} + \rho_{PCH_3}^{in} \right]$$
(2)

where,

$$\rho_{PGH_2}^{in} = k_{PGH_2}[e_{COX}][AA]; \ \rho_{PGH_3}^{in} = k_{PGH_3}[e_{COX}][EPA]$$
(3)

Cybernetic control variables computation

The computation of cybernetic control variables requires the cybernetic goal formulation. The control variables are defined using the matching and proportion laws (25, 27). The variable v_i modulates the activity of the enzyme catalyzing the formation of P_i . Similarly, u_i is responsible for controlling the synthesis process of the associated enzyme. v_i and u_i are defined for all enzymes involved in *n* reactions considered for the cybernetic goal. v_i is proportional to the related reaction flux, ρ_i . It attains a maximum value of one for the reaction with the highest flux. $v_i = 1$ indicates the enzyme is fully active for the corresponding reaction. u_i is also proportional to reaction flux as more enzyme control is required for reactions with higher flux ($u_i <= 1$). Hence, the sum of u_i for competing reactions (number of reactions: *n*) sum to one. As a consequence, v_i and u_i are defined as follows (Equation 4):

$$v_i = \frac{\rho_i}{\max_i \rho_j} ; \ u_i = \frac{\rho_i}{\sum_{j=1}^n \rho_j}$$
(4)

Employing Equation 4 for n = 2, the control variables for PGH₂ (v_{PGH_2} , u_{PGH_2}) and PGH₃ (v_{PGH_3} , u_{PGH_3}) are defined as Equations 5 and 6.

$$v_{PGH_2} = \frac{\rho_{PGH_2}^{in}}{\max\left(\rho_{PGH_2}^{in}, \rho_{PGH_3}^{in}\right)} ; v_{PGH_3} = \frac{\rho_{PGH_3}^{in}}{\max\left(\rho_{PGH_2}^{in}, \rho_{PGH_3}^{in}\right)}$$
(5)

$$u_{PGH_2} = \frac{\rho_{PGH_2}^{in}}{\rho_{PGH_2}^{in} + \rho_{PGH_3}^{in}} ; \ u_{PGH_3} = \frac{\rho_{PGH_3}^{in}}{\rho_{PGH_2}^{in} + \rho_{PGH_3}^{in}} \tag{6}$$

Kinetic rate balance incorporating cybernetic control for EPA-supplemented case

This section describes the rate balance of all reactions included in the network (Fig. 1). The enzymatic reactions are represented by Equation 7.

$$S_i + e_i \stackrel{R_{P_i}}{\longrightarrow} P_i \tag{7}$$

where S_i is the substrate. The enzymes are denoted by e_i , and the products by P_i , which are formed due to the action of the enzyme e_i on the substrate S_i . k_{P_i} indicates the rate constant of the reaction producing P_i . In our study, the substrates S_i for enzymatic reactions are AA, EPA, PGH₂, PGH₃, and PGD₂. The enzymes e_i are e_{COX} , e_{Plgds} , and e_{Plges} . The products P_i are PGH₂, PGH₃, PGD₂, PGD₃, PGE₂, PGE₃, and dhkPGD₂. We refer to supplemental section 1 for the full set of equations.

Enzymatic reactions with cybernetic control variables. As discussed, AA and EPA utilize the enzyme, COX, and COX levels are represented as e_{COX} . The chemical reaction of AA (Equation 8) and EPA (Equation 9) with e_{COX} leads to the formation of products PGH₂ and PGH₃ with rate constants k_{PGH_2} and k_{PGH_3} , respectively.

$$AA + e_{COX} \xrightarrow{k_{PGH_2}} PGH_2 \tag{8}$$

$$EPA + e_{COX} \xrightarrow{k_{PGH_3}} PGH_3 \tag{9}$$

The measurements of AA and EPA are input to the model. The generic form of the differential equation for enzymatic reactions with cybernetic variables is provided below in Equation 10.

$$\frac{d[P_i]}{dt} = v_{P_i} k_{P_i}[S_i][e_i] - g_{P_i}[P_i] - downstream fluxes$$
(10)

The first term denotes the production rate of P_{i} , and v_{P_i} is the cybernetic control variable for enzyme activity of e_i . g_{P_i} is the degradation rate. The downstream fluxes account for the subsequent metabolism of P_i . The kinetic rate balances of PGH₂ (Equation 11) and PGH₃ (Equation 12) are formulated using Equation 10, and they also include $(1 + k_{ATP}[ATP])$ in the first term.

$$\frac{d[PGH_2]}{dt} = v_{PGH_2} k_{PGH_2} [AA] [e_{COX}] (1 + k_{ATP} [ATP]) - g_{PGH_2} [PGH_2] - k_{PGD_2} [PGH_2] [e_{Ptgds}] - k_{PGE_2} [PGH_2] [e_{Ptges}]$$
(11)

$$\frac{d[PGH_3]}{dt} = k_{PGH_3} v_{PGH_3} [EPA] [e_{COX}] (1 + k_{ATP} [ATP])$$
$$- g_{PGH_3} [PGH_3] - k_{PGD_3} [PGH_3] [e_{Ptgds}] \qquad (12)$$
$$- k_{PGE_3} [PGH_3] [e_{Ptges}]$$

[.] represents the time-varying concentrations. The first term in Equations 11 and 12 is the rate of generation of PGH₂ and PGH₃, from the substrates AA and EPA, respectively, catalyzed by COX. In the expression $1 + k_{ATP}[ATP]$, the first term captures the basal activity (for both enzymes COX1 and COX2), and the second term captures the increase in activity due to ATP stimulation on COX2 (inducible form). The cybernetic control variables are defined for AA and EPA metabolism reactions, forming PGH2 and PGH3, respectively. v_{PGH_2} is the activity control variable for PGH₂, and v_{PGH_3} is for PGH₃. Although the enzyme e_{COX} is the same for AA and EPA, its activity can differ because it can bind with varying affinities to distinct substrates. g_{PGH_2} and g_{PGH_3} are the corresponding decay rates of PGH₂ and PGH₃. The downstream fluxes for PGH₂ and PGH₃ are due to their subsequent conversions, described by Equations 13-16, which are enzymatic reactions without cybernetic control variables. The products



PGD₂ (Equation 13) and PGD₃ (Equation 14) also share the enzyme e_{Pigds} , and PGE₂ (Equation 15) and PGE₃ (Eq. (16)) utilize the enzyme e_{Piggs} . PGH₂ gets converted into PGD₂ and PGE₂ (Equation 11), and PGH₃ gets converted into PGD₃ and PGE₃ (Equation 12). The third and fourth terms in Equation 11 denote the PGD₂ and PGE₂ production rate from the substrate PGH₂, respectively, where k_{PGD_2} and k_{PGE_2} are the rate constants. Likewise, the third and fourth terms in Equation 12 are the formation rates of PGD₃ and PGE₃ from PGH₃, where k_{PGD_3} and k_{PGE_3} are the corresponding rate constants. e_{COX} , e_{Ptgds} , and e_{Ptges} indicate the dynamic enzyme levels. Their rate balance equations are shown later in supplementary section 1. There are no cybernetic variables associated with reactions (Equations 13–16).

$$PGH_2 + e_{Ptgds} \xrightarrow{k_{PGD_2}} PGD_2 \tag{13}$$

$$PGH_3 + e_{Plgds} \xrightarrow{k_{PGD_3}} PGD_3 \tag{14}$$

$$PGH_2 + e_{Ptges} \xrightarrow{k_{PGE_2}} PGE_2 \tag{15}$$

$$PGH_3 + e_{Ptges} \xrightarrow{k_{PGE_3}} PGE_3 \tag{16}$$

Consequently, the fluxes downstream (third and fourth terms) of PGH_2 arise from the synthesis of PGD_2 and PGE_2 , while for PGH_3 , they are a result of PGD_3 and PGE_3 formation.

Enzyme balance in the cybernetic modeling framework

The rate balance for the enzyme, e_{COX} , shared by PGH₂ and PGH₃, is given by Equation 17.

$$\frac{d[e_{COX]}}{dt} = \alpha + u_{PGH_2} \frac{k_{ePGH_2}[AA]}{Km_{AA} + [AA]} + u_{PGH_3} \frac{k_{ePGH_3}[EPA]}{Km_{EPA} + [EPA]} - \beta[e_{COX}]$$
(17)

 α denotes the constitutive rate of formation of COX1. The second and third terms denote the inducible rate of synthesis of COX2. The cybernetic formulation assumes that enzymes depend on the levels of the substrates they react with. Hence,

Michaelis-Menten constants for AA and EPA, respectively. The enzyme balance for e_{Plgds} , e_{Plges} , and e_{dhkPGD_2} are included in supplemental section 1.

Simulation strategy

The model comprised a system of 13 ordinary differential equations (ODEs) and involved 41 parameters. To estimate these parameters, a two-step hybrid optimization approach was used. The initial parameter estimation used the pattern search method (implemented using the MAT-LAB® function "patternsearch"), followed by further parameter optimization using the fmincon function ("fmincon" in MATLAB®). Due to the instability of intermediates PGH₂ and PGH₃, no measurements were available for these metabolites. Therefore, their concentrations were assumed to be less than 10 pmol/ μ g DNA, and their profiles were constrained accordingly. Additionally, the initial conditions for these intermediates were forced to be the same for both experimental conditions, as all other metabolites had similar starting levels at zero minutes. The experimental data consisted of 8 time points spanning a duration of 60 min. These data points were used to determine the model parameters. The scaled fit-error between the experimental data $(y_{i,j,exp})$ and the simulated data $(y_{i,j,pred})$ was minimized using Equation 18, which served as the cost function.

$$\operatorname{Min}_{K,X_{0}}\left(\sum_{i=1}^{nsp}\left(\sum_{j=1}^{ni}\frac{\left(y_{i,j,exp}-y_{i,j,pred}(K,X_{0})\right)^{2}}{\max\left(y_{i,j,exp}\right)}\right)\right)$$
(18)

where K represents the parameters, X_0 denotes the initial condition of enzyme concentrations, ni is the number of time points, 8 (indexed as *j*), and *nsp* is the total number of species (indexed as *i*). The odel5s was used to solve the ODEs in MATLAB (2019, Natick, MA). The parameters were optimized, and the EPA-supplemented scenarios for all metabolites were simulated using the estimated parameters.

Model validation

F-test. We performed F-test, using Equation 19, to assess the goodness of fits of simulated profiles to the experimental observations for AA and EPA-supplemented cases (20).

$$F = \frac{\left(\sum_{j=1}^{nt} \left(Y_{j}^{tnt} - \overline{X}_{j}^{tnt}\right)^{2} + \sum_{j=1}^{nt} \left(Y_{j}^{ctnl} - \overline{X}_{j}^{ctnl}\right)^{2}\right) / (ne \times nt)}{\left(\sum_{j=1}^{nt} \sum_{i=1}^{nr} \left(X_{ij}^{tnt} - \overline{X}_{j}^{tnt}\right)^{2} + \sum_{j=1}^{nt} \sum_{i=1}^{nr} \left(X_{ij}^{ctnl} - \overline{X}_{j}^{ctnl}\right)^{2}\right) / (ne \times nt \times (nr-1))}$$
(19)

the inducible rate (second and third terms) for e_{COX} is a function of AA and EPA. It follows Michaelis-Menten kinetics and accounts for the enzyme synthesis control for products PGH₂ and PGH₃ by the variables u_{PGH_2} and u_{PGH_3} , respectively (27). k_{ePGH_2} and k_{ePGH_3} are the maximum rates for Michaelis-Menten kinetics, modulated by u_{PGH_2} and u_{PGH_3} , respectively. β is the degradation rate of the enzymes. Km_{AA} and Km_{EPA} are

where X_j , \overline{X}_j , and Y_j denote the experimental data, mean experimental data, and simulated (fitted) data at time point j, respectively. nr is the number of replicates (nr = 3, indexed as i), nt is the number of time points (nt = 7, index j). ne is the number of experimental conditions used, and trt and ctrl are treatment (EPA supplemented) and control groups, respectively (ne = 2). The degrees of freedom for determining the F distribution are $df_1 = (ne \times nt)$ and $df_2 = (ne \times nt \times (nr - 1))$.

Leave-one-out-metabolite PGD_2 cross-validation. The leave-oneout metabolite cross-validation method is used to assess the performance of the cybernetic model developed. In this case, a prediction is made for a metabolite not used to train the model. For instance, the metabolite PGD_2 is removed from the objective function, Equation 18, and the profiles for other metabolites are predicted. The goodness of fit of the predicted PGD_2 profile to the experimental data determines the model performance (21).

Prediction for an unseen case of DHA supplementations. The cybernetic model developed for EPA-supplemented situation can be modified to study the previously unobserved case of DHA-supplemented scenarios. The AA and DHA metabolism network include the AA branch (as shown in Fig. 1) and a downstream product of DHA, PD, an EFOX (62). The measurements are unavailable for downstream DHA products (59). We assumed that P_D has no further conversions. Following the AA and EPA case, the proposed cybernetic objective for AA and DHA metabolic network is to maximize the combined rates of AA and DHA consumption. This cybernetic goal is equivalent to the optimization of the combined production rates of PGH_2 and P_D (Equations 20 and 21). We depict the outflux (consumption rate) of AA and DHA by ρ_{AA}^{out} and ρ_{DHA}^{out} , respectively (Equation 20). Similarly, the influx (production rate) of PGH₂ is denoted by $\rho_{PGH_2}^{in}$, and P_D by $\rho_{P_D}^{in}$ (Equation 20). The definitions of $\rho_{PGH_2}^{in}$ and $\rho_{P_D}^{in}$ are shown in Equation 21. The cybernetic goal is (Equation 20):

$$\max\left[\rho_{AA}^{out} + \rho_{DHA}^{out}\right] = \max\left[\rho_{PGH_2}^{in} + \rho_{P_D}^{in}\right]$$
(20)

where

$$\rho_{PGH_2}^{in} = k_{PGH_2}[e_{COX}][AA]; \quad \rho_{P_D}^{in} = k_{P_D}[e_{COX}][DHA]$$
(21)

The modified control variable definitions for PGH₂ (v_{PGH_2} , u_{PGH_2}) and P_D (v_{P_D} , u_{P_D}) are shown in Equations 22 and 23, respectively.

$$v_{PGH_2} = \frac{\rho_{PGH_2}^{in}}{\max(\rho_{PGH_2}^{in}, \rho_{P_D}^{in})}; \quad v_{P_D} = \frac{\rho_{P_D}^{in}}{\max(\rho_{PGH_2}^{in}, \rho_{P_D}^{in})}$$
(22)

$$u_{PGH_2} = \frac{\rho_{PGH_2}^{in}}{\rho_{PGH_2}^{in} + \rho_{P_D}^{in}}; \quad u_{P_D} = \frac{\rho_{P_D}}{\rho_{PGH_2}^{in} + \rho_{P_D}^{in}}$$
(23)

The rate balance for all the metabolites of the AA branch, PGH₂, PGD₂, PGE₂, dhkPGD₂, PGJ₂, and dPGJ₂, are in accordance with the kinetic balance equations observed in the EPA-supplemented scenario (included in supplemental section 1). Similar to the EPA-supplemented case, a cybernetic variable is associated with the enzyme forming P_D from substrate DHA (Equation 24). The downstream fluxes of P_D are zero.

$$\frac{d[P_D]}{dt} = k_{P_D} v_{P_D} [DHA] [e_{COX}] (1 + k_{ATP} [ATP]) - g_{P_D} [P_D]$$
(24)

where k_{P_D} is the rate constant of the reaction, v_{P_D} is the cybernetic variable for modulating enzyme activity, and g_{P_D} is the decay rate of P_D . Due to the absence of subsequent conversions

of product P_D , the modified enzyme rate balances for AA and DHA scenario are Equation 25. Readers are referred to supplemental section 3 for the full set of equations. Equation 25 demonstrates the enzyme balance for e_{COX} . The inducible rate is due to the substrates AA and DHA. k_{eP_D} is the maximum inducible rate and Km_{DHA} is the Michaelis-Menten constant for DHA. The other constants hold the same meaning mentioned previously. We simulated the system using the above-mentioned simulation strategy and determined the parameters.

$$\frac{d[e_{COX}]}{dt} = \alpha + u_{PGH_2} \frac{k_{ePGH_2}[AA]}{Km_{AA} + [AA]} + u_P \frac{k_{eP_D}[DHA]}{Km_{DHA} + [DHA]} - \beta[e_{COX}]$$
(25)

RESULTS

Simulation results

The cybernetic model captures and explains the competition between enzymes in the metabolism of AA and EPA, leading to the formation of 2-series and 3series PGs, respectively. The estimated parameters are included in supplemental section 2. The enzyme COX (e_{COX}) is involved in both AA and EPA metabolism, while e_{Ptgds} is associated with PGD₂ and PGD₃, and e_{Ptges} is linked to PGE_2 and PGE_3 (21, 53, 59). To simplify the model, we focus on the initial level of enzyme competition, where COX (e_{COX}) is shared by AA and EPA. Consequently, we define cybernetic variables (u_{PGH_9}, v_{PGH_9}) and (u_{PGH_9}, v_{PGH_9}) for PGH₂ and PGH₃, respectively. Experimental data are available for cases where the cells are supplemented with EPA and DHA. The cybernetic model is trained using EPA supplementation data and predictions are made for the DHA supplementation scenario. The results for EPA supplementation are presented in Fig. 3, which demonstrates a good fit between the model prediction and experimental data. However, measurements for PGH₂ and PGH₃ are not available due to their inherent instability. Hence, the simulated profiles of PGH₂ and PGH₃ in Fig. 3A, G are constrained to be less than 10 pmol/ μ g DNA. The plots reveal higher levels of 2-series PGs in the control (Ctrl) scenario (red curve, Fig. 3B–F), and the presence of EPA in the EPA-supplemented case reduces the synthesis of 2-series PGs (green curve, Fig. 3B-F). In contrast, negligible levels of 3-series PGs are observed in the control scenario (red curve, Fig. 3 3H, I), while their concentrations increase with EPA supplementation (green curve, Fig. 3H, I). These findings are consistent with the competitive nature of AA and EPA for the same enzyme COX shown in Figs. 1 and 2. Similarly, the profiles of PGH_2 (Fig. 3A) and PGH_3 (Fig. 3G) are also consistent with the enzyme competition, with PGH₂ decreasing upon EPA addition while PGH₃ increases. Upon supplementation of EPA, the levels of AA and EPA become similar, and the reaction flux (represented as ρ) resulting from EPA metabolism to form PGH₃ is higher than that of AA producing PGH₂. This difference can be attributed to the higher



Fig. 2. The schematic demonstrates the mathematical framework of the cybernetic model for AA and EPA metabolism in mammalian cells. The cybernetic control is introduced to the conversion of AA and EPA, leading to PGH_2 and PGH_3 , respectively. A portion of the reaction network is shown on the top right. The biological goal is hypothesized to maximize the proinflammatory (exhibited by AA metabolism) and antiinflammatory (characteristic of EPA metabolism) responses. The model development includes formulating the cybernetic goal (step 1), which is the mathematical form of the biological goal, computing the cybernetic control variables (step 2), writing the rate balance forms for metabolites and enzymes (step 3), and training for the EPA supplemented case (step 4) and validating (step 5) the model by performing F-test and leave-one-out-metabolite cross-validation method. The final step is applying the developed model to an unseen DHA supplementation case with suitable modifications. AA, arachidonic acid; DHA, docosahexaenoic acid; EPA, eicosapentaenoic acid.

rate constant of PGH₃ formation (k_{PGH_3}) compared to the rate constant for PGH₂ formation (k_{PGH_2}). The elevated flux of PGH₃ indicates that the enzyme COX (e_{COX}) exhibits a greater enzyme activity for EPA than AA when EPA is supplemented (21). This competitive behavior sheds light on the mechanistic relationship between the enzymes and substrates involved. The dynamics of the cybernetic variables governing enzyme activity and synthesis support this observation. These dynamics will be elaborated upon in the subsequent section, providing further insight into the implications of enzyme activity plots. The nonlinear trends of the 2-series PGs (Fig. 3B–F) and 3-series PGs (Fig. 3H, I) are accurately captured by our cybernetic model, as indicated by the F-test values (discussed later). The nonlinearity in the kinetics of PGH₂ and PGH₃ arises from the influence of the cybernetic control variables. The profiles of AA and EPA, which serve as inputs to our model, can be found in the supplementary material (supplemental Figs. S1 and S2). In both experimental scenarios, the AA profile follows similar trends, resulting in comparable behaviors of the red and green curves for the 2-series PGs. The AA levels increase significantly until 30 min, after which



Fig. 3. The cybernetic model simulation results obtained for EPA addition experimental conditions. The model successfully captured the nonlinear trends exhibited by all the metabolites. PGH_2 (A) and PGH_3 (G) measurements are unavailable due to their unstable existence. Their levels are constrained to remain below 10 pmol/µg DNA. With EPA supplementation, there is a decrease in the levels of 2-series PGs (B–F) and an increase in the levels of 3-series PGs (H–I). The change occurs because EPA and PGH₃ become available to contribute to the production of 3-series PGs. This observation highlights the competition for the shared enzyme e_{COX} that reacts with different substrates, AA and EPA. Similarly, PGH_2 (A) decreases upon EPA addition, while PGH_3 (G) increases, further illustrating the effect of the competition between these substrates for the enzyme e_{COX} . AA, arachidonic acid; EPA, eicosapentaenoic acid; PG, prostaglandin.

they plateau, leading to similar downstream behavior of the 2-series PGs. EPA is initially introduced at a relatively high concentration, resulting in significant production of 3-series PGs at 2.5 min. However, as time progresses, the decline in EPA levels also leads to a decrease in 3-series PGs. Similarly, the nonlinear trend observed in the 3-series PGs at later time points follows the EPA profile.

Dynamics of cybernetic control variables

Our cybernetic model accounts for the unknown regulatory steps by introducing the control variables for PGH₂ and PGH₃ formation reactions. The enzyme e_{COX} is responsible for catalyzing the conversion of AA and EPA into PGH₂ and PGH₃, respectively. Since AA and EPA may have different enzyme synthesis

regulation (u_{PGH_2} , u_{PGH_3}) and enzyme activity modulation (v_{PGH_2} , v_{PGH_3}), they are assigned distinct control variables. Following the matching and proportion laws, u_i and v_i are directly proportional to flux (ρ_i), and vary by their respective normalizations. The plots for $u_{PGH_2}(u_{PGH_3})$ and $v_{PGH_2}(v_{PGH_3})$ show a similar trend, and are consistent with the definitions of u and v.

The metabolite with the highest flux is defined as dominant. In the control case (Ctrl) where AA is present at basal levels and EPA is negligible, PGH₂ emerges as the dominant metabolite. This is evident from the comparison $u_{PGH_2} > u_{PGH_3}$ (Fig. 4A, B red curve) and $v_{PGH_2} > v_{PGH_3}$ (Fig. 4C, D red curve). Such dominance of PGH₂ is expected in the context of Ctrl, where EPA levels are insignificant. Conversely, with EPA supplementation, PGH₃ becomes the leading metabolite, as



Fig. 4. The dynamics of cybernetic control variables for $PGH_2(u_{PGH_2}, v_{PGH_2})$ and $PGH_3(u_{PGH_3}, v_{PGH_3})$. PGH_2 is the dominant metabolite for the Ctrl case because $u_{PGH_2} > u_{PGH_3}$ (A and B red curve) and $v_{PGH_2} > v_{PGH_3}$ (C and D red curve). However, upon EPA supplementation, PGH_3 is the leading product because $u_{PGH_3} > u_{PGH_2}$ (A and B green curve) and $v_{PGH_2} > v_{PGH_3}$ (C and D green curve). The switch from PGH_2 to PGH_3 dominance captures the COX enzyme competition. The synthesis and activity of COX prioritize an increased catalytic effect on EPA relative to AA when there is EPA supplementation. AA, arachidonic acid; COX, cyclooxygenase; EPA, eicosapentaenoic acid; PG, prostaglandin.

indicated by $u_{PGH_3} > u_{PGH_2}$ (Fig. 4A, B green curve) and $v_{PGH_3} > v_{PGH_2}$ (Fig. 4C, D green curve). This behavior supports the proposition that COX (e_{COX}) reacts with EPA more potently than AA when the system is supplemented with EPA, owing to enhanced enzyme synthesis and activity control. It is important to note that we observed a switch from dominant proinflammatory PGH₂ action for control to antiinflammatory PGH₃ for the EPA-supplemented case. The reason for the switch is discussed in the next section.

Switching between the dominance of the cybernetic control variables v_{PGH_2} and v_{PGH_3}

The control variables for activity, v_{PGH_2} and v_{PGH_3} (Equations 3 and 5), depend on the AA, EPA, and e_{COX} levels. As e_{COX} is utilized by both AA and EPA, due to the ratio involved, v_{PGH_2} and v_{PGH_3} become independent of the e_{COX} concentration; hence, v_{PGH_3} and v_{PGH_3} can be analytically simplified as $v_{PGH_2}^{simp}$ and $v_{PGH_3}^{pd}$, respectively. It is important to note that $v_{PGH_2}^{simp} = v_{PGH_2}$ and $v_{PGH_3}^{simp} = v_{PGH_3}$. The simulation results from Section 3.1 provide k_{PGH_2} and k_{PGH_3} , which are utilized in this analysis. **Figure 5** shows the variation of $v_{PGH_3}^{simp}$ and $v_{PGH_2}^{simp}$ (Equation 26) with AA and EPA concentrations. As expected, $v_{PGH_2}^{simp}$ reaches a maximum value of 1 for higher concentrations of AA, whereas $v_{PGH_3}^{simp}$ is maximized for higher EPA levels. Equation 27 analytically describes the ratio of $[EPA]_{switch}$ to $[AA]_{switch}$, which causes the transition from the dominance of $v_{PGH_3}^{simp}$ prevails over a broader range of AA and EPA levels (Fig. 5).

$$v_{PGH_2}^{simp} = \frac{k_{PGH_2}[AA]}{\max(k_{PGH_2}[AA], k_{PGH_3}[EPA])};$$

$$v_{PGH_3}^{simp} = \frac{k_{PGH_3}[EPA]}{\max(k_{PGH_3}[AA], k_{PGH_3}[EPA])}$$
(26)

$$[AA]_{swtich}k_{PGH_2} = [EPA]_{switch}k_{PGH_3}; \quad \frac{[AA]_{swtich}}{[EPA]_{switch}} = \frac{k_{PGH_3}}{k_{PGH_2}}$$
(27)

Cybernetic model prediction: enzyme dynamics

A notable aspect of the cybernetic model is that it can predict enzyme profiles. The enzyme e_{Ptgds} , which is depicted in **Fig.** 6A, is responsible for catalyzing the production of PGD₂ and PGD₃. In comparison to other enzymes, e_{Ptgds} shows higher levels. This trend is primarily because the levels of PGD₂ and PGD₃ are higher among the 2-series (as shown in Fig. 3C) and 3-series PGs (as shown in Fig. 3I), respectively. e_{Ptgds} increases and eventually saturates, reflecting the similar trends observed for prominent PGD₂ and PGD₃. Similarly, e_{Ptges} (Fig. 6B) also increases because of rising PGE₂ and PGE₃ levels. The enzyme e_{COX} (Fig. 6C) also follows a similar pattern, which depends on AA and EPA levels.

Model validation results

F-test. The F-test for all metabolites show that the fit error is less than the experimental error as all F-test values are less than $F_{0.05}$ (16, 32) = 0.46. The 2-series metabolites, including PGD₂, PGJ₂, and dPGD₂, exhibit a better fit compared to PGE₂ and dhkPGD₂, and all 3-series PGs demonstrate a satisfactory fit.

Leave-one-out-metabolite PGD_2 cross-validation method. The model demonstrates a good fit to the data when using the leave-one-out-metabolite PGD_2 cross-validation method. (Fig. 7A–F). The results align closely with the original AA and EPA-supplemented conditions, validating the cybernetic formulation. Removing PGD_2 from the cost function (Equation 13) does not significantly degrade the quality of the fit results as PGD_2 is included in the reaction kinetics and satisfies flux balances for all metabolites. The goodness of fits indicates that our cybernetic model accurately captured the mechanistic details, even without considering PGD_2 in the cost function. The rationales for the trends observed remain the same for metabolites and enzymes (Fig. 7A–F).

Validation of the model by the application of the cybernetic model developed to a new scenario: DHA supplementation. We simulated the control and DHA-supplemented model, presented in the Materials and methods section. As discussed, measurements are unavailable for metabolites formed due to DHA metabolism, so we assumed that P_D (an EFOX) is the only downstream product. The results are shown in Fig. 8. The fits are reasonable, increasing our confidence in the cybernetic model. Similar to EPA, DHA is also antiinflammatory. In these supplementations, we observed a decline in 2-series PGs levels due to DHA addition (pink curve, Fig. 8B-F). PGH_2 and P_D competition is also intact: PGH_2 decreases (Fig. 8A), and P_D increases (Fig. 8G) with DHA addition. The reasoning behind the dynamics of metabolites and enzymes aligns with the AA and EPA supplementation, except for downstream P_D due to the absence of its downstream metabolites. For AA and DHA experiments, $u_{PGH_2} > u_{P_D}$ (Fig. 9A) and $v_{PGH_2} > v_{P_D}$ (Fig. 9C) indicates the prominence of PGH2 in the control condition. Whereas, for DHA supplementation case (Fig. 9B, D), P_D is the dominant metabolite, promoting the antiinflammatory behavior. The observed result is consistent with the EPA supplementation scenario, where a similar pattern was observed. In the control condition, PGH2 emerged as the prominent metabolite, whereas in the EPA supplemented scenario, PGH3 dominated.

DISCUSSION

This study presents a mathematical model that aims to capture the dynamics of enzyme competition in the



Fig. 5. The surface plot depicts the relationship between simplified control variables for enzyme activity $(v_{PCH_2}^{simp}, v_{PCH_3}^{simp})$, and AA and EPA concentrations. $v_{PCH_2}^{simp}$ dominates for higher AA and $v_{PCH_3}^{simp}$ takes precedence for higher EPA levels. Consequently, the system switches from $v_{PCH_2}^{simp} = 1$ to $v_{PCH_3}^{simp} = 1$ as EPA increases. The ratio of switch levels, $[AA]_{switch}$ to $[EPA]_{switch}$, follows (Equation 27). Therefore, AA and EPA levels are responsible for the transition in dominance of proinflammatory PGH₂ in the Ctrl scenario to antiinflammatory PGH₃ in the EPA-supplemented case (Fig. 4). AA, arachidonic acid; EPA, eicosapentaenoic acid; PG, prostaglandin.

metabolism of AA and EPA/DHA. We used the cybernetic model, which inherently incorporates the enzyme competition mechanism by optimizing the cybernetic goal. Within this framework, AA and EPA share the enzyme COX (e_{COX}). AA and its downstream 2-series PGs demonstrate proinflammatory characteristics, while EPA and the 3-series PGs are associated with antiinflammatory behavior (35, 53). A recent study by Zaid et al. observed high levels of both series PGs in intubated COVID-19 patients (60). This finding emphasizes the critical roles of both proinflammatory and antiinflammatory stages in the inflammatory response observed in these individuals. Considering the important opposing functionality of AA and EPA, we hypothesized that during the inflammatory response in RAW 264.7 cells, the biological objective is to maximize both the proinflammatory and antiinflammatory phases. Consequently, we proposed the cybernetic goal: maximizing the combined consumption rates of AA (representing proinflammatory action) and EPA (representing antiinflammatory activity). This goal formulation is equivalent to maximizing the production rates of PGH₂ and PGH₃ since they are the primary products of AA and EPA through *e*_{COX} activation, respectively. The model fitted the experimental data reasonably, supporting our hypothesis regarding the biological goal and cybernetic goal formulation. The success of the model underscores the goal-oriented behavior of the system, where the levels and activities of relevant enzymes are modulated to achieve the formulated goal (27). The quantitative results of this study emphasize the significance of both pro inflammatory and antiinflammatory phases during the inflammatory response in RAW 264.7 macrophages.

The cybernetic control variables are introduced for the enzyme COX (e_{COX}), involved in forming PGH₂ and PGH₃ from AA and EPA, respectively. It should be noted that the cybernetic variables are the ratios of fluxes and do not represent fluxes themselves. They are lumped variables that capture the complex biological regulation mathematically. The single enzyme e_{COX} concerned with the production of PGH₂ and PGH₃ is assigned different variables for enzyme activity (v_{PGH_2} , v_{PGH_3}) and synthesis (u_{PGH_3} , u_{PGH_3}). This formulation accounts for the potentially distinct processes governing the activity and synthesis process with which e_{COX} interacts with AA and EPA. Two experimental conditions of control and EPA supplementation are explored. The enzyme competition is depicted by the dynamics of the cybernetic control variables for enzyme activity (v_{PGH_2} ,



Fig. 6. The cybernetic model provides predictions for the enzyme profiles. Among these enzymes, e_{Pigds} (A) stands out with higher levels compared to the others. Its levels increase and reach saturation following the profiles of PGD₂ (Fig. 3C) and PGD₃ (Fig. 3I), respectively. Similarly, the enzymes e_{Piges} (B) and e_{COX} (C) show an increase in levels due to the corresponding trends observed in their substrates PGE₂, PGE₃, and AA, EPA, respectively. These patterns hold for both experimental conditions of Ctrl and EPA supplementation. AA, arachidonic acid; EPA, eicosapentaenoic acid; PG, prostaglandin.



Fig. 7. The simulation results for the model with the leave-one-out-metabolite PGD_2 cross-validation method. The plots (A–F) resemble the original AA and EPA addition instances (Figs. 3A–F and 7A–C). Despite removing PGD_2 (Equation 13) from the cost function, the results remain unaffected due to the adherence of all metabolites to the kinetic rate balance. The similarity of results to the original ones implies that our cybernetic model suitably incorporated mechanistic details. AA, arachidonic acid; EPA, eicosapentaenoic acid; PG, prostaglandin.

 v_{PGH_3}), where upon EPA supplementation, the activity of PGH₃ increases and is higher than PGH₂. The simplified $v_{PGH_2}^{sim}$ and $v_{PGH_3}^{sim}$ also demonstrate similar trend. Consequently, the addition of EPA shifts the system from the dominance of the proinflammatory 2series PGs to antiinflammatory 3-series PGs. The surface plot of simplified control variables ($v_{PGH_2}^{sim}$, $v_{PGH_3}^{sim}$) further illustrates that the levels of AA and EPA play a vital role in the shift from the dominance of proinflammatory PGH₂ in the Ctrl scenario to the prevalence of antiinflammatory PGH₃ in the EPA-supplemented case. The ratio of levels of $[AA]_{switch}$ to $[EPA]_{switch}$ where switch occurs is 3.75, indicating that $v_{PGH_3}^{simp}$ starts to prevail for smaller EPA levels; hence, $v_{PGH_3}^{simp}$ is dominant over a wider range of AA and EPA levels. The cybernetic model adequately described the experimental data, demonstrating that incorporating regulatory variables for e_{COX} is sufficient for studying AA and EPA metabolism. Moreover, it illustrates that an appropriate control mechanism for e_{COX} effectively explains the subsequent conversion of PGH₂ and PGH₃ to downstream 2-series and 3-series PGs, respectively. The outcome of the model, with an $[AA]_{switch}$ to $[EPA]_{switch}$ ratio of 2.65, falls within the desirable range for promoting an antiinflammatory response and thereby reducing the risk of diseases. Recent studies have shown



Fig. 8. The AA and DHA supplementation case simulation results demonstrate similar trends to the AA and EPA addition scenarios. Specifically, there is a decrease in the levels of 2-series PGs (B–F) due to increased DHA levels. The competition between PGH₂ and PGH₃ is maintained, as evidenced by the decline in PGH₂ (A) and the increase in P_D (G) in the DHA addition condition. The e_{COX} levels are shown in the subplot (H). AA, arachidonic acid; DHA, docosahexaenoic acid; EPA, eicosapentaenoic acid; PG, prostaglandin.



Fig. 9. The cybernetic control variables for PGH₂ and P_D for control condition and with DHA supplementation. In the control condition, PGH₂ emerges as the primary metabolite, characterized by higher levels of u_{PGH_2} (A) compared to u_{P_D} (B), and higher levels of v_{PGH_2} (C) compared to v_{P_D} (D). This indicates a prevailing proinflammatory action in this condition. In contrast, in the DHA-supplemented scenario, similar to the case of EPA supplementation, the downstream metabolite of DHA, P_D , becomes the dominant metabolite. This is evident from higher levels of u_{P_D} (B) compared to u_{PGH_2} , (A), and higher levels of v_{P_D} (D) compared to v_{PGH_2} . (C) Consequently, an antiinflammatory role is prevalent in this scenario. DHA, docosahexaenoic acid; EPA, eicosapentaenoic acid; PG, prostaglandin.

that populations in regions with an AA to EPA fatty acid ratio ranging from 1 to 5 experience fewer chronic diseases compared to those in areas where n-6 fatty acids dominate, such as in Western diets with ratios as high as 17 (53, 63).

The cybernetic model formulated for enzyme competition fitted the experimental data well. Our model successfully fitted the data points that were not captured by the Michaelis-Menten dynamics, compared to the previous study by Gupta et al. (21) based on Michaelis-Menten kinetics. For instance, the model predictions were far off the initial peak observed for PGD₃ and PGE₃ in the case of EPA supplementation. In contrast, our model successfully fitted these data points, as supported by the F-test values. The improved performance can be attributed to the incorporation of known and unknown regulatory processes through cybernetic control variables. Notably, the cybernetic model also offered the added advantage of including and predicting enzyme dynamics, overcoming the limitation of unavailable enzyme measurements. The model formulation included the kinetic rate balances for enzymes *e*_{Ptgds}, *e*_{Ptges}, and *e*_{COX}, and their dynamics are shown in Fig. 6: e_{Ptgds} (Fig. 6A), e_{Ptges} (Fig. 6B), and e_{COX} (Fig. 6C). The rationale behind the model effectively capturing the initial peak of PGH₂/PGH₃, PGD₂/PGD₃, and PGE_2/PGE_3 is as follows. For Ctrl, PGH_2 increased for t < 2.5 minutes because the influx of PGH₂ $(v_{PGH_2}k_{PGH_2}[AA]e_{COX}(1+k_{ATP}[ATP]))$, first term in Equation 11) is higher due to the presence of enzyme e_{COX} (Fig. outflux PGH₉ 6C), and of $(g_{PGH_2}[PGH_2] + k_{PGD_2}[PGH_2]e_{Ptgds} + k_{PGE_2}[PGH_2]e_{Ptges}$, last three terms in Equation 11) is lower due to smaller

degradation rate and negligible levels of e_{Ptgds} (Fig. 6A) and e_{Ptges} (Fig. 6B). However, for 2.5 < t < 10, PGH₂ decreased because the influx of PGH₂ reduced due to decreasing ATP and outflux of PGH₂ increased as a result of rising e_{Ptgds} (Fig. 6A) and e_{Ptges} (Fig. 6B). For t > 10minutes, AA governed the temporal profile of PGH₉. Similar arguments followed for the dynamics of EPA supplemented experiments for PGH₂ and PGH₃. The temporal evolution of PGD₂/PGE₂ and PGD₃/PGE₃ followed PGH₂ and PGH₃ dynamics, respectively. The present model adopts nonlinear kinetics for the metabolite rate balance, including control variables (u, v), nonlinearly modulate the rates. In contrast, the rate balances in Gupta et al. study were nonlinear due to the Michaelis-Menten form to model enzyme competition. Both models focus on mechanism; however, the conceptual difference lies in our model adopting the goalseeking behavior of the system. The success of this model supported the notion of a goal-seeking nature during the inflammatory response.

CONCLUSION

Our model provides insights into the overall behavior of cells, particularly their drive to achieve the biological goal of maximizing proinflammatory and antiinflammatory responses. It elucidates the underlying mechanism by formulating the cybernetic goal and enables the system to decide the best trajectory for accomplishing the defined biological and cybernetic goals. The trends for the control variables offered valuable insights into the dominance of metabolites, guiding the system to follow the appropriate underlying

TABLE 1. The F-test results for all metabolites. For a significance value of 0.05, $F_{0.05}$ (16, 32) = 0.46

Metabolite	F-test Value	Metabolite	F-test Value	Metabolite	F-test Value	Metabolite	F-test Value
PGE ₂ PGD ₂	$0.1105 \\ 0.0202$	$dPGD_2$ $dhkPGD_2$	$0.0764 \\ 0.299$	PGJ ₂ PGE ₃	$0.0618 \\ 0.0294$	PGD_3	0.0713

mechanism. In contrast, the previous study formulated the mechanistic form mathematically, directing the system to adopt an informed approach. Our model formulation was supported by the results of the F-test conducted during the model validation process (Table 1). The successful prediction of profiles for the leaveone-out-metabolite PGD₂ cross-validation method, further affirmed accurate incorporation of mechanism within the cybernetic model. Furthermore, the cybernetic model developed can be adapted to study the unseen scenarios involving DHA supplementation. The reasonable fit observed for these cases further substantiates the efficacy of applying the cybernetic model with variations to novel datasets that adhere to similar underlying mechanisms. Future research directions could involve the formulation of a model that integrates AA and EPA/DHA metabolism with the dynamics of cytokines/chemokines, small signaling proteins that play a vital role in recruiting immune cells to specific tissues and are proinflammatory or antiinflammatory in nature. Their interactions and correlations with 2-series and 3-series PGs in disease contexts are well-established. Therefore, developing an integrated model could offer valuable insights into the mutual regulation of PGs and cytokines.

Data availability

The experimental data are available in the publication by Norris and Dennis (59).

Supplemental data

This article contains supplemental data.

Author contributions

S. K., S. G., M. R. M., R. R., L. A., S. S., and D. R. methodology; S. K., S. G., M. R. M., R. R., L. A., S. S., and D. R. visualization; S. K., S. G., M. R. M., S. S., and D. R. visualization; S. K., S. G., M. R. M., S. S., and D. R. writingreview and editing; S. K., S. G., M. R. M., S. S., and D. R. supervision; S. K., S. G., M. R. M., and D. R. investigation; S. K., S. G., R. R., L. A., S. S., and D. R. validation; S. K. data curation; S. K. formal analysis; S. K. writing-original draft; S. S. and D. R. funding acquisition.

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Conflict of interest

The authors declare that they have no conflicts of interest with the contents of this article.

Abbreviations

AA, arachidonic acid; COVID-19, coronavirus disease 2019; COX, cyclooxygenase; DHA, docosahexaenoic acid; EFOX, electrophile oxo-derivative; EPA, eicosapentaenoic acid; ODE, ordinary differential equation; PG, prostaglandin.

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