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Constraining axionlike particles from rare pion decays

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Ultraviolet completions for axionlike particles (ALPs) lighter than the neutral pion generically induce ALP-neutral pion mixing and are therefore sensitive to direct constraints on the mixing angle. For ALPs below the pion mass, we demonstrate that strong and novel bounds on the ALP-pion mixing angle can be extracted from existing rare pion decay data, measured by the PIENU and PIBETA experiments.

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I. INTRODUCTION

Searches for axionlike particles (ALPs) provide a powerful probe of various extensions of the Standard Model (SM), including models of dark matter, baryogenesis, and the strong *CP* problem (see, e.g., [1–4]). In the MeV-GeV mass range, the strongest known constraints arise mainly through their coupling to photons. At large couplings, bounds from LEP diphoton searches are applicable. For somewhat smaller couplings, bounds from beam-dump and fixed-target experiments, such as Charm/Nu-Cal, E137, and E141 apply. Current or future experiments, such as NA62, SeaQuest, and Belle II will further probe this masscoupling parameter space.

The phenomenology of an ALP, *a*, in this mass range may, however, be partly reparametrized in terms of its mixing with light unflavored hadrons. The generic nature of this mixing makes it an attractive phenomenological quantity to explore: UV completions for such ALPs will typically generate ALP-pion mixing and are therefore sensitive to mixing constraints. In this paper, we demonstrate how strong bounds on ALP-pion mixing can be extracted from existing rare pion decay data.

In particular, we leverage the high precision measurements of the chirally suppressed decay $\pi^+ \rightarrow e\nu$ (" π_{e2} ") and of the phase-space suppressed $\pi^+ \rightarrow \pi^0 e\nu$ (" π_{β} ") to place strong constraints on $\pi^+ \rightarrow ae\nu$ (" π_{a3} "), as the latter has neither of these suppressions. These constraints can in

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turn be transformed into bounds on ALP-pion mixing because the $\pi^+ \rightarrow ae\nu$ amplitude can be estimated via mixing with the final state π^0 in $\pi^+ \rightarrow \pi^0 e\nu$ (cf. Refs. [5,6]). We derive these bounds for 10 MeV $\leq m_a < m_{\pi}$, extendible down to the massless limit with improved form factor treatments for the π_{β} decay.

The PIENU experiment [7,8] currently provides the highest precision measurement of the $\pi^+ \rightarrow e\nu$ branching ratio from decays of stopped charged pions: the world average $Br[\pi^+ \rightarrow e\nu] = (1.230 \pm 0.004) \times 10^{-4}$ [9]. Multicomponent fits to the measured positron energy spectra have been used in previous studies to tightly constrain contributions from heavy sterile neutrino decays, i.e., $\pi^+ \rightarrow eN$ [7,10] (see also [11]), as well as Majoron-neutrino couplings [12]. In this paper, we derive ALP-pion mixing constraints from PIENU spectra via a similar analysis. (The irreducible background from $Br[\pi^+ \rightarrow \pi^0 e\nu]$ is much smaller than the experimental precision. This is not the case for, e.g., $K \rightarrow \pi e\nu$ vs $K \rightarrow e\nu$, for which reason we do not study bounds from semileptonic kaon decays.)

Further, the PIBETA experiment [13] currently provides the highest precision measurement of the rare $\pi^+ \rightarrow \pi^0 e\nu$ decay, $\text{Br}[\pi^+ \rightarrow \pi^0 e\nu] = (1.036 \pm 0.006) \times 10^{-8}$, including a measurement of the opening angle spectrum of the daughter $\pi^0 \rightarrow \gamma\gamma$ process. This spectrum has a kinematic edge that is highly sensitive to the $\gamma\gamma$ invariant mass. We show that it generates even tighter constraints on $\text{Br}[\pi^+ \rightarrow (a \rightarrow \gamma\gamma)e\nu]$ for a small m_a range.

Previous analyses have considered bounds on ALP-pion mixing using constraints on $K^+ \rightarrow \pi^+ +$ invisible and estimating the $K^+ \rightarrow \pi^+ a$ amplitude from mixing with $K^+ \rightarrow \pi^+ \pi^0$ (see, e.g., Ref. [14]). While powerful, these bounds implicitly require suppression of the ALP-top quark coupling, which can otherwise generate large shortdistance $s \rightarrow d$ penguin contributions. E.g., in the case of universal ALP-quark coupling, the penguins are

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enhanced by $\frac{m_t^4}{32\pi^4 f_\pi^4} \frac{m_\pi^4}{m_a^4} \frac{|V_{ts}V_{td}|^2}{|V_{us}V_{ud}|^2} \log^2[\frac{m_W^2}{m_t^2}]$ compared to the mixing amplitudes [6,15–17] and naively dominate the $K^+ \rightarrow \pi^+ a$ amplitudes. By contrast, the semileptonic processes we consider arise from tree-level charged-current amplitudes. Short-distance contributions are expected to enter only at higher loop and electroweak order, far smaller than the hadron mixing contributions we probe. In the context of UV completions, the bounds we derive are therefore independent from kaon bounds.

II. ALP-PION MIXING

We consider an ALP, *a*, coupled to SM quarks or gauge bosons, with mass $m_a < m_{\pi}$. We assume no tree-level ALP-lepton couplings, and consider only the case that the diphoton branching ratio is dominant.

The low-energy effective field theory of ALP-SM interactions may be matched onto the chiral Lagrangian of the light hadrons, such that the ALP-SM interactions involve either mixings with SM hadrons or higher-dimension derivatively coupled interactions to hadrons or gauge bosons (see, e.g., Ref. [18]). In the regime that the ALP-SM effective couplings are perturbative, the physical ALP state

$$|a\rangle = (\cos\vartheta + \dots)|a_0\rangle + \sin\vartheta|\pi^0\rangle + \dots \tag{1}$$

in which the angle ϑ encodes the mixing of the ALP and QCD neutral pion eigenstates, and the ellipsis indicates mixings with other hadrons as allowed by parity and angular momentum conservation. An amplitude involving a π^0 generates a contribution to an associated ALP amplitude, via mixing with an off shell π^0 ,

$$\langle \dots | a \dots \rangle = \sin \vartheta \langle \dots | \pi^{*0} \dots \rangle + \dots$$
 (2)

Other contributions may involve mixing with other hadrons, or other UV operators.

ALP- π^0 mixing may arise in the chiral Lagrangian at leading order via a mixed kinetic term $\varepsilon \partial_{\mu} a \partial^{\mu} \pi^{0}$, or via a mass mixing term $\mu^2 a \pi^0$. In UV-complete models, ε can be generated either through an ALP-gluon coupling or through an ALP coupling to light quarks (see, e.g., Ref. [18]). Typically $\varepsilon \sim f_{\pi}/f_a$, where $f_{\pi}(f_a)$ is the pion (ALP) decay constant, and in the limit $\varepsilon \ll 1$, $\sin \vartheta \simeq m_a^2 \varepsilon / (m_\pi^2 - m_a^2)$. A large mixing, $\sin \vartheta \lesssim 1$, with $m_a \ll m_{\pi}$ requires $f_a \lesssim f_{\pi}$, for which it may be difficult to construct a UV completion. By contrast, a Higgs Yukawa-like term $y(a/f_a)\bar{Q}_L H\gamma^5 D_R$ may generate a mass mixing term $\mu^2 \sim y v_{\rm EW} 4\pi f_{\pi}^2/f_a$. In the limit, $\mu^2 \ll m_{\pi}^2$, $\sin \vartheta \simeq \mu^2 / (m_{\pi}^2 - m_a^2)$. In this case, even for large mixing $\sin \vartheta \lesssim 1$, one may have $f_a \gg v_{\rm EW}$, with m_a remaining arbitrarily small, and corrections to m_{π} negligible. Thus plausible UV completions may exist that cover the entire $m_a - \sin \vartheta$ plane that we consider in this work. Other sources of isospin breaking may generate additional mass mixing terms that further modify $\sin \vartheta$. Hereafter, we shall treat $\sin \vartheta$ as a purely phenomenological mixing parameter—keeping in mind that it may be reexpressed in terms of UV quantities in a model-dependent way—and seek to develop direct $\sin \vartheta$ constraints.

III. ALP LIFETIME

The amplitude for the diphoton mode $a \rightarrow \gamma\gamma$ —the dominant decay mode for $m_a < m_{\pi}$ —presents a simple manifestation of Eq. (2): it always receives a contribution from ALP-pion mixing $\langle \gamma\gamma | a \rangle = \langle \gamma\gamma | \pi^{*0} \rangle \langle \pi^{*0} | a \rangle + ... = \langle \gamma\gamma | \pi^{*0} \rangle \sin \vartheta + \cdots$, with possibly additional model-dependent UV contributions from a direct coupling to photons, $g_{a\gamma} a F_{\mu\nu} \tilde{F}^{\mu\nu}$ ($\tilde{F}_{\mu\nu} = \varepsilon_{\mu\nu\rho\sigma} F^{\rho\sigma}$). The diphoton width is then (choosing $f_{\pi} = 130$ MeV)

$$\Gamma_{a\gamma\gamma} = (g_{a\gamma}^{\text{eff}})^2 m_a^3 / \pi, \qquad g_{a\gamma}^{\text{eff}} = \sin \vartheta g_{\pi\gamma} + g_{a\gamma}, \quad (3)$$

with an effective coupling, $g_{a\gamma}^{\text{eff}}$, and the coupling of the pion to photons is $g_{\pi\gamma} = \sqrt{2}\alpha/8\pi f_{\pi} \simeq 3.2 \times 10^{-3}/\text{GeV}$.

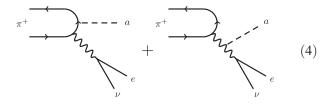
The limits we explore from PIENU and PIBETA data are sensitive to the ALP lifetime, as it determines whether the ALP is prompt or invisible at detector scales. Since the lifetime (3) is in general independent from $\sin \vartheta$, for the purposes of setting $\sin \vartheta$ limits we shall explore two lifetime regimes:

- (i) The *prompt* regime, i.e., $g_{a\gamma}^{\text{eff}}$ is sufficiently large for the ALP to decay within the timing/displacement resolution of the detector, possibly via a large $g_{a\gamma}$,
- (ii) The *invisible* regime, i.e., $g_{a\gamma}^{\text{eff}}$ is sufficiently small for the ALP to be long-lived enough to escape the detector, possibly via tuning of $g_{a\gamma}$ against the mixing contribution.

In this context, we will also consider a pure *mixing* scenario, arising from particularly predictive models that do not contain a UV contribution to the ALP-photon coupling, such that $g_{a\gamma}^{\text{eff}} \simeq \sin \vartheta g_{\pi\gamma}$.

IV. PION SEMILEPTONIC DECAYS TO ALPS

At tree level, the $\pi^+ \rightarrow ae\nu$ parton-level amplitude



The second term is electroweak suppressed compared to the first and can be neglected. The first term contains the ALP-hadron matrix element of the form

$$\mathcal{A}^{\mu} \simeq \sum_{M^{0}} \langle a | M^{0} \rangle \langle M^{0} | \bar{d} \gamma^{\mu} u | \pi^{+} \rangle + \sum_{M^{+}} \langle 0 | \bar{d} \gamma^{\mu} u | M^{+} \rangle \langle M^{+} a | \bar{q} \not p_{a} \gamma^{5} q | \pi^{+} \rangle, \quad (5)$$

where M^0 and M^+ span complete sets of (multi)hadronic states, with appropriate quantum numbers. The axial vector matrix element $\langle M^0 | \bar{d} \gamma^{\mu} \gamma^5 u | \pi^+ \rangle$ vanishes by parity and angular momentum conservation.

The leading chirally unsuppressed contribution to the second term of Eq. (5) arises from virtual ρ^* exchange and is therefore suppressed by $m_a^2/m_{\rho^*}^2$. The dominant contribution to the matrix element is then generated via off shell π^{*0} "insertion" in the first term, as in Eq. (2), so that the $\pi^+ \rightarrow a$ amplitude

$$\mathcal{A}^{\mu} \simeq \langle a | \pi^{*0} \rangle \langle \pi^{*0} | \bar{d} \gamma^{\mu} u | \pi^{+} \rangle \equiv \sin \vartheta \langle \pi^{*0} | \bar{d} \gamma^{\mu} u | \pi^{+} \rangle.$$
 (6)

The $\pi^+ \to \pi^0 e\nu$ decay is conventionally computed by applying the conserved vector current hypothesis and by mapping to the $\mu \to e\nu\nu$ process; see, e.g., Ref. [19]. Our estimates for $\pi^+ \to \pi^{*0}e\nu$ will instead be informed by the similar $K^+ \to \pi^0 e\nu$ process, using the language of form factors. This is a similar, but more general, approach to that of Refs. [5,6], that studied $\pi^+ \to (a \to ee)e\nu$ in the context of the long-defunct 1.8 MeV axion anomaly [20].

The hadronic $\pi^+ \rightarrow \pi^{*0}$ SM matrix element may be represented by form factors, defined via

$$\langle \pi^{*0} | \bar{d} \gamma^{\mu} u | \pi^{+} \rangle = c_{\pi} \left[f_{+} (p_{+}^{\mu} + p_{0}^{\mu}) + (f_{0} - f_{+}) \frac{m_{+}^{2} - m_{0}^{2}}{q^{2}} q^{\mu} \right]$$

in which $q = p_+ - p_0$, the difference of the charged and neutral pseudoscalar momenta, with masses m_+ and m_0 , respectively. We have defined dimensionless form factors $f_{+,0} = f_{+,0}(q^2)$, such that f_0 couples only to the lepton mass. Here $c_{\pi} = 2 \times 1/\sqrt{2}$ is a coupling combinatoric factor multiplied by a Clebsch-Gordan coefficient. (For $K^+ \to \pi^0 e\nu$, $c_K = 1/\sqrt{2}$.) In the regime $m_+ - m_0 \gg m_e$, the electron mass terms may be neglected, so that the $\pi^+ \to \pi^{*0} e\nu$ rate

$$\frac{d\Gamma}{dq^2} = \frac{G_F^2 |V_{ud}|^2}{24\pi^3} f_+^2 c_\pi^2 m_+^3 r^3 (w^2 - 1)^{3/2} + \mathcal{O}(m_e^2/q^2), \quad (7)$$

in which $r = m_0/m_+$, the recoil parameter $w = (m_+^2 + m_0^2 - q^2)/(2m_+m_0)$, with range $1 \le w \le (1 + r^2)/(2r)$, and we neglect small electroweak corrections [19].

Following from the Ademollo-Gatto theorem [21–23], one expects $f_+(q^2 = 0) \simeq 1$ up to corrections that are expected to scale as $\sim (m_+^2 - m_0^2)^2 / \Lambda_{\rm QCD}^4$. The matrix element may be expressed as an analytic function of a conformal expansion parameter $z = (\sqrt{w+1} - \sqrt{2})/(\sqrt{w+1} + \sqrt{2})$ [24], so that provided $|z| \ll 1$, the form factor should be approximately linear in *w* or q^2 . In the analogous $K^+ \rightarrow \pi^0 e\nu$ system, $f^K_+(q^2)$ is well approximated by a linear function from $f(q^2 = 0) \simeq 1$ to $f(q^2 = q^2_{\max}) \sim 1.2$ and $|z|_{\max} \simeq 0.098$. Thus, requiring a sufficiently small *z*, say $|z|_{\max} \lesssim 0.3$ —equivalent to $r \gtrsim 0.1$ or $m_0 \gtrsim 10$ MeV—and approximating

$$f_+(q^2) \simeq 1 \tag{8}$$

should provide a lower bound on f_+ , yielding a conservative estimate for the $\pi^+ \rightarrow ae\nu$ rate up to $\mathcal{O}(10\%)$ uncertainties. (In the massless positron limit, applying the approximation (8) to Eq. (7) yields a partial width in agreement with, e.g., Eq. (1) of Ref. [13] or Eq. (7.12) of Ref. [19] to $\mathcal{O}[(1-r)^8]$.)

Combining Eqs. (6)–(8) with the $\pi^+ \rightarrow \ell \nu$ partial width, one obtains the ratio of branching ratios,

$$\frac{\operatorname{Br}[\pi_{a3}]}{\operatorname{Br}[\pi_{\ell^2}]} \simeq \frac{2}{3\pi^2} \frac{c_{\pi}^2 m_{\pi}^4 \sin^2 \vartheta}{f_{\pi}^2 m_{\ell^2}^2 (1 - m_{\ell^2}^2 / m_{+}^2)^2} \int_1^{(1 + r^2)/2r} r^4 (w^2 - 1)^{3/2} dw.$$
(9)

Using Eq. (9), we proceed to set bounds on $\sin \vartheta$ from rare pion decay data. These bounds rely, in part, on fits to the positron energy spectrum in the parent rest frame. At truth level, the positron energy is bounded by $0 \le E_e \le m_+(1-r^2)/2$ and

$$\frac{d\Gamma[\pi_{a3}]}{dE_e} = \frac{c_\pi^2 G_F^2 m_+ E_e^2}{8\pi^3} \frac{((1-r^2)m_+ - 2E_e)^2}{m_+ - 2E_e}.$$
 (10)

V. PIENU RESIDUALS BOUND

The PIENU experiment [8] measures the $\pi^+ \rightarrow e\nu$ branching ratio from a sample of stopped pions, by determining the positron yield in the electromagnetic (EM) inclusive decay $\pi^+ \rightarrow e\nu(\gamma)$ compared to the cascade $\pi^+ \rightarrow (\mu \rightarrow e\nu\nu)\nu(\gamma)$. The main experimental components comprise a target, silicon strips, and wire chambers for high precision tracking, a positron calorimeter to reconstruct the positron energy, and a semihermetic calorimeter array to capture EM showers. The combined calorimeter energy is given by the sum of positron energy and EM showers, $E_{cal} = E_e + E_{EM}$. A sketch of the PIENU detector is shown on the left in Fig. 1.

The relevant backgrounds include not only the $\pi^+ \rightarrow \mu \rightarrow e$ cascade, but also contributions from pion decays-inflight, stopped muon decays, and radiative μ decays to energetic photons. Their branching ratios overwhelmingly dominate the signal mode. Timing cuts are used to suppress these large backgrounds compared to the prompt $\pi \rightarrow e\nu(\gamma)$ modes. A simultaneous fit of the timing distributions for both signal and backgrounds then permits measurement of the ratio, $R_{e/\mu} = \Gamma[\pi \rightarrow e\nu(\gamma)]/\Gamma[\pi \rightarrow \mu\nu(\gamma)]$, at the

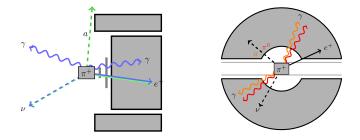


FIG. 1. Left: schematic PIENU detector configuration of the target, tracking, and calorimeter elements (gray). Overlaid are typical event topologies for the prompt (blue) and invisible (green) ALP scenarios. Right: schematic cross section of the PIBETA detector configuration including the target, tracking, and calorimeter elements (gray). Overlaid are typical event topologies at the minimum truth-level opening angle configuration of a π^0 (red) and lighter prompt ALP (orange) diphoton decay.

 10^{-3} level, from which the $\pi^+ \rightarrow e\nu$ branching ratio is inferred.

The $E_{\rm cal}$ distribution for the $\pi^+ \rightarrow e\nu$ mode is sharply peaked at $(m_+^2 + m_e^2)/2m_+ \simeq 69.8 \,{\rm MeV}$, with a low-energy tail arising from EM shower losses. The (timing-cutsuppressed) backgrounds from the $\pi^+ \rightarrow \mu \rightarrow e$ cascade or muon decays-in-flight are, by contrast, smoothly distributed in the low-energy region $E_{\rm cal} < E_0 \simeq 52$ MeV, the endpoint.

References [7,10] perform a precision fit of the measured $E_{\rm cal}$ distribution in the low-energy region to the combination of the (simulated) $\pi^+ \rightarrow e\nu(\gamma)$ low-energy tail and the background distributions. The bin residuals of this fit can be used to place strong constraints on additional prompt contributions from exotic $\pi^+ \rightarrow eX$, where X has sufficient invariant mass to push the signal E_{cal} distribution into the low-energy fit region. References [7,10] consider the case that X = N, a heavy sterile neutrino. In Fig. 2, we show the residuals of Ref. [10] used for such an analysis, normalized against the $\pi^+ \rightarrow e\nu$ branching ratio. In this work, we consider $X = a\nu$, making use of Eq. (9) to convert the bound on branching ratios to a bound on $\sin \vartheta$. (More precise limits will require a dedicated analysis fitting the $X = a\nu$ signal template simultaneously with the background components.)

We characterize whether the ALP is prompt or invisible by considering whether the mean characteristic ALP displacement from decay-in-flight, $\langle \beta \gamma \rangle c \tau$, is inside the target or outside the calorimeter radius, respectively: we treat the PIENU target size as ~1 cm and the calorimeter size as ~1 m. (A full study of regimes outside the prompt or invisible limits requires simulation of the PIENU response when the EM shower is somewhat spatially or time displaced from the prompt decays, but still within the detector acceptance.)

In the invisible ALP regime, the E_{cal} distribution receives no additional contributions from $a \rightarrow \gamma\gamma$. In Fig. 2, we show the corresponding binned positron energy spectra

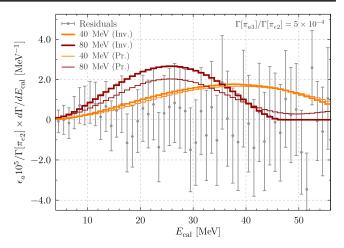


FIG. 2. PIENU fit bin residuals (gray) for the E_{cal} distribution in the low-energy regime, normalized against the $\pi^+ \rightarrow e\nu$ (" π_{e2} ") rate. Overlaid are $\pi^+ \rightarrow ae\nu$ (" π_{a3} ") binned spectra for the prompt (thin solid) and invisible (thick solid) regimes, with $m_a =$ 40 MeV (orange) and 80 MeV (red). The spectra include acceptance corrections, with total acceptance ϵ_a , but are normalized such that $\Gamma[\pi_{a3}]/\Gamma[\pi_{e2}] = 5 \times 10^{-4}$.

(thick lines) from $\pi^+ \rightarrow ae\nu$ decays for $m_a = 40$ and 80 MeV, including quoted acceptance corrections [10].

In the prompt ALP regime, however, daughter photons of the ALP may contribute to the measured E_{cal} in the event. For $m_a \sim m_{\pi}$, the ALP is slow enough that one photon may hit the PIENU positron calorimeter within the ~20% positron acceptance [10], as sketched in Fig. 1 (deposition in the outer calorimeters is required to be <2 MeV [10], thereby excluding hard photon contributions in those). But for $m_a \ll m_{\pi}$, the ALP momentum may backreact against the lepton system, such that the daughter photons, which decay in a narrow cone around the ALP momentum, miss the acceptance. In Fig. 2, we show the corresponding binned positron spectra (thin lines) for the same two mass benchmarks. The heavier 80 MeV benchmark is slightly altered by a longer tail.

While Ref. [10] does not quote the bin residual correlations, one may reproduce quoted $\pi^+ \rightarrow eN$ bounds assuming nearby bins are uncorrelated. We therefore extend this assumption to treat all bins as uncorrelated over the measured energy range. Under this assumption, in the left of Fig. 3, we show the corresponding 95% CL exclusion regions in the $\sin^2 \vartheta - m_a$ parameter space, for both the invisible (green) and prompt (blue) regimes. The excluded regions in $\sin^2 \vartheta$ for the prompt and invisible cases differ at most by $\mathcal{O}(1)$ and extend down to $\sin^2 \vartheta \gtrsim 10^{-5}$. This corresponds to branching ratios as small as $\mathcal{O}(10^{-8})$.

Independent of the relationship between sin ϑ and the lifetime [cf. Eq. (3)], requiring a prompt ALP— $\langle \beta \gamma \rangle c\tau < 1 \text{ cm}$ —directly implies a lower bound on $g_{a\gamma}^{\text{eff}}$. Over the ALP mass ranges considered in this paper, we have checked that this bound is far smaller than the direct

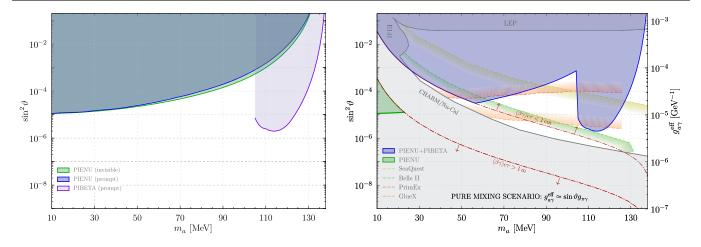


FIG. 3. Left: 95% CL exclusion regions from the PIENU fit residuals for the prompt (blue) and invisible (green) ALP regimes. Also shown is the PIBETA exclusion from the $\theta_{\gamma\gamma}$ spectrum for prompt ALPs (purple). Right: combined PIENU and PIBETA exclusion regions for the models with $g_{a\gamma}^{\text{eff}} \simeq \sin \vartheta g_{\pi\gamma}$ ("pure mixing scenario"). In this case, the mean characteristic decay length regions $\langle \beta\gamma \rangle c\tau < 1 \text{ cm}$ (dot-dashed red line and above) and $\langle \beta\gamma \rangle c\tau > 1 \text{ m}$ (dot-dashed red line and below) approximately delineate where the prompt and invisible regime exclusions apply, respectively. Also shown are exclusions from CHARM/Nu-Cal, E137, E141, and LEP (gray), and projected reaches for SeaQuest (yellow line and below) [25], Belle II (green line and below) [26], PrimEx (red line and above), and GlueX (orange line and above) [27].

 $g_{a\gamma}^{\text{eff}}$ bounds from LEP triphoton searches [28,29]. Electron fixed-target experiments such as NA64 [30] and LDMX [31], as well as Belle (II) [26] and *BABAR* [32], also have invisible ALP searches. However, for these experiments, the ALP production and lifetime is controlled by $g_{a\gamma}^{\text{eff}}$, independent of sin ϑ . Hence, these constraints do not appear in the left panel of Fig. 3.

The pure mixing scenario $[g_{a\gamma} = 0$ in Eq. (3)] fixes the relationship between the $\pi^+ \rightarrow ae\nu$ branching ratio and the ALP lifetime and may therefore interpolate between the prompt and invisible regimes in different parts of the $\sin^2 \vartheta - m_a$ space. For this scenario, in the right side of Fig. 3, the region $\langle \beta \gamma \rangle c\tau < 1$ cm (>1 m) is above (below) the red dot-dashed contours. Above (below) the 1 cm (1 m) contour, the prompt (invisible) exclusion should be a good proxy for the pure mixing scenario.

Further, in the pure mixing scenario, the relation $g_{a\gamma}^{\text{eff}} \simeq \sin \vartheta g_{\pi\gamma}$ enables recasting of beam-dump, collider, and fixed-target experiment bounds on $g_{a\gamma}^{\text{eff}}$ onto the $\sin^2 \vartheta - m_a$ space. For $m_a < m_{\pi}$, the relevant bounds are set by the CHARM/Nu-Cal [33–36], E137 [37], E141 [38], and LEP [28,29] experiments, corresponding in the right panel of Fig. 3 to the gray regions. (Roughly scaling the pion interaction length with $\sin^2 \vartheta \lesssim 10^{-3}$, the ALP interaction length in matter is naively $\gtrsim 10^3$ m, far larger than the typical path length in beam dump experiments, so that their constraints continue to apply in the pure mixing scenario.) We see in Fig. 3 that the PIENU data places powerful new constraints on ALPs in the pure mixing scenario for $m_a \gtrsim 25$ MeV.

These constraints will be complemented in the future by proton fixed-target beam-dump experiments, such as SeaQuest [25] searching for 3γ signatures, or Belle II monophoton searches [26]. In the right panel of Fig. 3, we show the SeaQuest (yellow, 10^{20} protons on target) and Belle II (green) reaches as representatives of experiments capable of setting limits in the $\sin^2 \vartheta - m_a$ space in the pure mixing scenario. Part of the $\sin^2 \vartheta - m_a$ space may also be tested by NA62 running in beam-dump mode [39] and FASER [40]. A slightly larger region of parameter space could be probed by SHiP [41], as well as by PrimEx and GlueX (region above the red and orange lines, respectively) [27].

VI. PIBETA DIPHOTON BOUND

The PIBETA experiment [13,42] measures the rare $\pi^+ \rightarrow (\pi^0 \rightarrow \gamma \gamma) e\nu$ branching ratio from a sample of stopped pions, by triggering on the prompt $\pi^0 \rightarrow \gamma \gamma$ decay in coincidence with a positron track. The main detector elements relevant here are a near-spherical electromagnetic calorimeter and cylindrical multiwire proportional tracking chambers surrounded by plastic scintillator. A schematic of the experiment is shown on the right in Fig. 1.

The photon showers are required to each have energy $E_{\gamma} > m_{\mu}/2$, beyond the kinematic endpoint of stopped $\mu \rightarrow e\nu\nu$ background decays. The normalization of the $\pi^+ \rightarrow \pi^0 e\nu$ rate is obtained via comparison with a large prescaled sample of nonprompt single positron track events, including both $\pi^+ \rightarrow e\nu$ and in-flight $\mu \rightarrow e\nu\nu$ backgrounds. This entails a simultaneous fit of signal and background kinematic and timing distributions.

Reconstruction of the diphoton pair includes measurement of the diphoton opening angle in the lab frame. At truth level, this angle is bounded via

$$-1 \le \cos \theta_{\gamma \gamma} \le -1 + 2[(1 - r^2)/(1 + r^2)]^2.$$
(11)

The maximum (minimum) cosine corresponds to diphoton emission perpendicular (parallel) to the π^+ direction of flight in the π^0 rest frame, generating a sharp kinematic edge (smooth kinematic endpoint) in the $\theta_{\gamma\gamma}$ spectrum. Because the upper bound increases as m_a decreases, the *prompt* diphoton decay of an ALP in $\pi^+ \rightarrow (a \rightarrow \gamma\gamma)e\nu$ with $m_a < m_{\pi}$ may produce diphoton showers with truthlevel opening angles beyond the π^0 edge at ~176°. In Fig. 1, we show schematically the maximum truth-level $\cos \theta_{\gamma\gamma}$ configuration for a π^0 compared to a lighter ALP.

In practice, the finite detector-level angular resolution smears out the reconstructed $\theta_{\gamma\gamma}$ distribution and thus the $\theta_{\gamma\gamma}$ edge. For an angular smearing $\sigma_{\theta_{\gamma\gamma}} \simeq 2.25^{\circ}$ and requiring both photons' energy $E_{\gamma} > 53$ MeV [42], we show in Fig. 4 the expected $\theta_{\gamma\gamma}$ distributions for several m_a benchmarks, as well as for π^0 , compared to the measured $\theta_{\gamma\gamma}$ spectrum for $160^{\circ} \le \theta_{\gamma\gamma} \le 180^{\circ}$ [13]. The π^0 spectrum (gray) agrees well with the data. For $m_a \lesssim 110$ MeV, the photon energy cut significantly suppresses the $\theta_{\gamma\gamma}$ spectrum in the 160–180° range.

The PIBETA experiment does not provide residuals for the fit of the simulated $\pi^+ \rightarrow \pi^0 e\nu$ opening angle spectrum to the data. We extract an approximate, estimated bound on $\sin^2 \vartheta$, by conservatively requiring that the integrated contribution to the $\theta_{\gamma\gamma}$ spectrum in the 160–180° range from $\pi^+ \rightarrow ae\nu$ does not exceed the quoted 0.6% uncertainty for the $\pi^+ \rightarrow \pi^0 e\nu$ branching ratio. In Fig. 3, we show the corresponding exclusion (purple region in the left panel). This exclusion will likely be much stronger if the full differential information shown in Fig. 4 can be incorporated. This approximate bound from PIBETA data

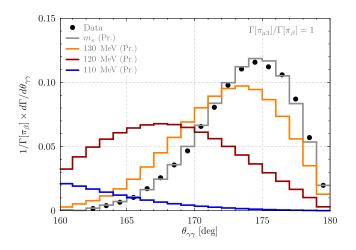


FIG. 4. PIBETA reconstructed diphoton opening angle distribution (black) for $\pi^+ \to (\pi^0 \to \gamma\gamma)e\nu$, normalized to unity. Also shown are $\pi^+ \to ae\nu$ binned spectra for the prompt regime, with $m_a = 110, 120, 130$ MeV and m_{π} . The spectra are normalized such that $\Gamma[\pi^+ \to ae\nu]/\Gamma[\pi^+ \to \pi^0 e\nu] = 1$.

sets the most stringent bound on the mixing angle sin ϑ for prompt regime ALPs with masses above ~100 MeV. A future data analysis for $\theta_{\gamma\gamma} < 160^\circ$ could lead to stringent constraints also for $m_a < 100$ MeV.

VII. CONCLUSIONS AND OUTLOOK

Models for ALPs generically predict mixing between the ALP and the SM neutral pion. We have derived strong new constraints on ALP-pion mixing, by extracting constraints on the $\pi^+ \rightarrow ae\nu$ branching ratio from the rare pion decay data measured by the PIENU and PIBETA experiments.

In the pure mixing scenario, these constraints complement existing exclusions as well as the reaches of planned experiments, leading to near complete coverage of the $\sin^2 \vartheta - m_a$ space over many decades of the mixing angle for 10 MeV $\lesssim m_a \lesssim m_\pi$. Beyond the pure mixing scenario, the constraints provide exclusions for a wide range of UV ALP models that generate ALP-pion mixing. Because they arise from charged current tree-level processes, these exclusions can probe UV models that are characteristically different from those probed by similar bounds extracted from $K^+ \to \pi^+ +$ invisible decays.

Our approximate treatments of the detector responses can be improved by dedicated ALP analyses in future $\pi^+ \rightarrow e\nu$ or $\pi^+ \rightarrow \pi^0 e\nu$ measurements, that account for, e.g., bin correlations, effects of displaced ALP decays, and/or make use of other differential information. Our results rely on theoretical approximations, expected to introduce no more than $\mathcal{O}(10\%)$ uncertainties, that may be improved with more detailed treatments of the $\pi^+ \rightarrow \pi^{*0}$ form factors. This in turn would permit extension of these bounds to lower ALP masses, below ~10 MeV.

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