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¹ Impact basin relaxation as a probe for the thermal ² history of Pluto

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3 **Abstract.** We investigate viscoelastic impact basin relaxation on Pluto
4 for a variety of thermal evolution scenarios encompassing both convective
5 and conductive ice shells. Basins smaller than 200 km in diameter do not re-
6 lax appreciably, while relaxation fractions can be up to $\sim 60\%$ for large im-
7 pact basins. The main control on basin relaxation is the amount of radio-
8 genic heat produced in the rocky core; our results are insensitive to the for-
9 mation time of the basin, the ice reference viscosity adopted, and the pres-
10 ence/absence of a subsurface ocean. **Other volatiles, such as CO_2 or NH_3 ,**
11 **if present in the ice shell in sufficient quantities could increase the predicted**
12 **relaxation fraction of basins.** Relaxation causes extensional stresses interior
13 to the basin; the orientation of the resulting tectonic features is controlled
14 by the effective elastic thickness beneath the basin. Future observations of
15 the relaxation states and tectonics of impact basins are therefore likely to
16 provide a key constraint on Pluto's thermal history.

1. Introduction

17 Impact basin topography produces stresses which can potentially drive lateral flow in
18 the subsurface. Depending on the thermal (and thus viscosity) structure, the topography
19 of these basins will therefore relax over time. As a result, impact basins provide a probe
20 of thermal histories of terrestrial planets and icy satellites [e.g., *Parmentier and Head,*
21 *1981; Solomon et al., 1982; Thomas and Squyres, 1988; Dombard and McKinnon, 2006;*
22 *Mohit and Phillips, 2007; Robuchon et al., 2011; Kamata et al., 2013; White et al., 2013*].
23 Pluto, like most other icy planetary bodies, is likely to possess large impact basins. In
24 this study, we carry out an analysis of the likely extent of basin relaxation on Pluto which
25 can be compared with forthcoming *New Horizons* observations [e.g., *Moore et al., 2014*]
26 to provide insight into Pluto's evolution.

27 Our current knowledge of Pluto is mainly from telescopic observations. Its size and
28 mass are constrained with a relatively small error [e.g., *Person et al., 2006*], while spectral
29 information pertaining to composition [*Owen et al., 1993*] and surface colour [*Buie et al.,*
30 *2010*] have also been obtained.

31 These observations, however, are insufficient to determine the interior structure and
32 thermal history of Pluto; numerical studies are **therefore** necessary. Most such studies
33 have either assumed conduction or treated convection using a parameterized approach
34 [*McKinnon et al., 1997; Hussmann et al., 2006; Desch et al., 2009; Barr and Collins, 2014*].
35 One exception is the work of *Robuchon and Nimmo* [2011], in which a 3D convection code
36 was used to investigate the thermal and structural evolution of Pluto. These authors found
37 that the evolution depends mainly on the reference viscosity of ice (i.e., the viscosity at the

38 melting point), and the amount of radiogenic material present. If the reference viscosity
39 is higher than 5×10^{15} Pa s, the icy shell is conductive, and a subsurface ocean develops.
40 On the other hand, if the reference viscosity is lower than that value, the icy shell is
41 convective, and a subsurface ocean does not develop. A typical reference viscosity is
42 $\sim 10^{14}$ Pa s, though it depends on many factors, such as grain size of ice [e.g., *Goldsby*
43 *and Kohlstedt*, 2001] and the temperature of the subsurface ocean, if present. A global
44 pattern of tectonic features, if observed on Pluto's surface, would provide constraints on
45 its evolution: thickening of an ice shell above an ocean would result in recent extension,
46 while cooling of a shell in the absence of a subsurface ocean would generate compression
47 [*Robuchon and Nimmo*, 2011].

48 Another observation that would provide information on the thermal history is basin
49 relaxation. The aim of this study is to investigate which factors control basin relaxation
50 on Pluto. To do so, we first obtain a series of time-dependent viscosity profiles for dif-
51 ferent Pluto evolution scenarios, using the results of *Robuchon and Nimmo* [2011] and
52 additional calculations described below. Using these viscosity profiles, we then calculate
53 the viscoelastic relaxation of impact basins of different sizes. We find that the primary
54 factor that controls basin relaxation is the amount of radiogenic heat produced in the
55 rocky core, and that the present-day relaxation fraction can be up to $\sim 60\%$ for large im-
56 pact basins. These results suggest that basin relaxation can be used as a probe of Pluto's
57 thermal history.

58 The rest of this paper is organized as follows. Section 2.1 describes the thermal evolution
59 models employed, while Section 2.2 explains how the results of these models are then used
60 to calculate impact basin relaxation. Section 3 presents the results of our thermal evolution

61 and basin relaxation calculations, while Section 4 discusses some potential caveats and
62 implications of our work.

2. Method and Model

63 Figure 1 shows our interior structure model of Pluto, which is adopted from *Robuchon*
64 *and Nimmo* [2011] to maintain consistency. **Table 1 lists the parameters adopted.** We
65 assume a differentiated Pluto, consisting of an H₂O layer overlying a silicate core. The
66 radius of the core is assumed to be 850 km [*McKinnon et al.*, 1997]. **Here, the silicate**
67 **mass fraction ~ 0.67 is assumed, though it might range from 0.5–0.7 [*McKinnon et al.*,**
68 **1997]. Since this uncertainty leads to a change in the core radius by only 50 km, different**
69 **core radii would not change our results significantly. The key point is that only cold, near-**
70 **surface ice can support topographic loads for billions of years; thus, the total thickness**
71 **of the ice shell is of only secondary importance.** The thickness of the H₂O layer depends
72 on the thickness of a subsurface ocean. This is because the total mass of Pluto needs to
73 be conserved. Specifically, the thickness of the H₂O layer is assumed to be 330 km when
74 it is completely frozen, and the presence of a subsurface ocean leads to a decrease in the
75 thickness. It should be noted, however, that the change in the planetary radius is <10 km
76 (<1%) under all calculation conditions and has only negligible effects on basin relaxation.
77 **The surface temperature is assumed to be 40 K. The expected spatial variation in surface**
78 **temperature of 10 K [*Stern et al.*, 1993] results in only a <5% change in the final basin**
79 **relaxation fraction for our nominal model.**

80 In the following, we describe details of the calculations and model assumptions for
81 thermal evolution and viscoelastic relaxation separately.

2.1. Thermal evolution

82 In general, convection transports heat produced inside a planet more effectively than
 83 conduction. Thus, whether the ice shell is convective or conductive has a large influence
 84 on the thermal history [e.g., *Robuchon and Nimmo*, 2011]. 3D convection calculations,
 85 however, are much more time-consuming than 1D conduction calculations. Thus, in order
 86 to investigate the thermal evolution under a wide variety of parameter conditions, we
 87 use both the 3D convection results of *Robuchon and Nimmo* [2011] and additional 1D
 88 conduction calculations as described below. The variables explored using these codes are
 89 summarized in Table 2. **In our calculation, the start time of the thermal model is assumed**
 90 **to be 30 Myr after CAI formation [*Robuchon and Nimmo*, 2011]; heating due to the decay**
 91 **of short-lived radioactive nuclides is therefore negligible.**

2.1.1. 3D convection

93 For convection cases, we use results obtained by *Robuchon and Nimmo* [2011]. **Briefly,**
 94 **the thermal evolution of the ice shell is calculated using a finite-volume numerical code**
 95 **“CEDIPUS” [*Choblet et al.*, 2007].** This code assumes an incompressible spherical body
 96 and a Newtonian rheology and solves the heat transfer and momentum equations with a
 97 prescribed top and bottom temperature.

98 The viscosity of ice is calculated using the following equation:

$$\eta = \eta_0 \xi_m \exp \left[\frac{E_a}{R_g} \left(\frac{1}{T} - \frac{1}{T_m} \right) \right], \quad (1)$$

99 where η is the viscosity, η_0 is the reference viscosity, $E_a = 60 \text{ kJ mol}^{-1}$ is the activation
 100 energy, R_g is the gas constant, T is temperature, and $T_m = 273 \text{ K}$ is the reference
 101 temperature, set equal to the melting temperature of pure ice, respectively. For numerical
 102 reasons, the viscosity is not allowed to exceed 10^{30} Pa s . The dimensionless constant ξ_m

103 represents a reduction in viscosity due to partial melting and takes a value between 0
 104 and 1. The melt fraction for each cell is calculated from the balance of input and output
 105 of heat flux. If an ice cell is completely melted, the shell thickness is reduced, and the
 106 grid structure is refined keeping the total number of grids points constant. The freezing
 107 of water is also considered. The temperature of a subsurface ocean, if exists, is assumed
 108 to be constant (i.e., 273 K). Note that although we are keeping T_m fixed (in accordance
 109 with *Robuchon and Nimmo* [2011]), the potential effect on the viscosity structure of a
 110 reduction in subsurface-ocean temperature due to the presence of impurities such as NH_3
 111 is accounted for by allowing the reference viscosity at T_m to vary very widely.

112 The rocky core is assumed to be rigid and conductive, and to contain heat-producing
 113 elements. In the core, the 1D thermal conduction equation,

$$\rho C_p \frac{dT}{dt} = \frac{1}{r^2} \frac{d}{dr} \left(r^2 k \frac{dT}{dr} \right) + H, \quad (2)$$

114 is solved where ρ is density, C_p is specific heat, t is time, r is radial distance from the
 115 center of the planet, H is heat production rate, and k is thermal conductivity, respectively.

116 Two heat sources were considered: despinning due to Charon formation and radiogenic
 117 heat produced in the rocky core. The former heat source is concentrated in the ice shell,
 118 but it has only a very limited duration, of order 10^5 years [*Hussmann et al.*, 2010], and
 119 no significant effects on long-term thermal evolution [*Robuchon and Nimmo*, 2011]. A
 120 higher ice viscosity leads to a longer timescale of orbital evolution, though it also leads to
 121 a smaller heat production rate [*Barr and Collins*, 2014]. Thus, Pluto's major long-term
 122 heat source is radiogenic heating (unless the rocky core is highly depleted in radioactive
 123 elements). The conductive heat flow out of the core is compared with the heat transferred
 124 across the base of the ice shell to determine whether melting or freezing takes place.

125 The initial temperature condition assumed in the 3D models was isothermal, with a
126 value of $T_{\text{ini}} = 150, 200$ or 250 K. The long-term evolution was found to be very insensitive
127 to the initial value adopted [*Robuchon and Nimmo, 2011*].

128 For shell reference viscosities higher than 5×10^{15} Pa s, heat transfer occurs entirely
129 via conduction [*Robuchon and Nimmo, 2011*] and is thus amenable to a 1D treatment.
130 As described below, we benchmarked our 1D conduction calculations by comparing the
131 output with these 3D conductive cases.

132 **2.1.2. 1D conduction**

133 To model purely conductive cases, we used the numerical code described in *Nimmo and*
134 *Spencer* [2014]. In this approach, equation (2) is solved both for a rocky core and for
135 an H₂O layer, and 1D temperature profiles are obtained. **A node in the ice shell with a**
136 **temperature higher than the melting point is treated as liquid, and heat is instantaneously**
137 **transferred across the subsurface ocean. Further details of the melting and freezing for**
138 **the H₂O layer incorporated are described in Appendix A of *Nimmo and Spencer* [2014].**
139 Parameter values adopted are again as for *Robuchon and Nimmo* [2011], except as noted
140 otherwise.

141 For the 1D cases, we assumed different concentrations of radioactive isotopes in the
142 core: 50, 200, 400, and 738 ppm for ⁴⁰K concentration (C_K). The highest (nominal)
143 concentration is that for carbonaceous (CI) chondrites [*Lodders, 2003*], and was assumed
144 in the 3D convection calculations analyzed here. For all C_K , we assume that the ratios
145 U/K and Th/K are the same as those for carbonaceous chondrites. **Although these ratios**
146 **vary across the solar system [e.g., *McCubbin et al., 2012*], this simplification should work**
147 **since we adopt a wide range of C_K .** Heat sources other than long-term radiogenic heating,

148 such as tidal heating, were not considered (and for Pluto are unlikely to be important,
149 except early in its history [*Barr and Collins, 2014*]).

2.2. Viscoelastic deformation

150 For our viscoelastic deformation calculations, we used horizontally-averaged (thus 1D)
151 temperature profiles. This is because our deformation code assumes a spherically-
152 symmetric interior profile.

153 We first calculate a time-dependent 1D viscosity profile from the 1D temperature profiles
154 for the ice shell. Here, we use the same rheology (i.e., equation (1)), assuming $\xi_m = 1$. A
155 significant change in viscosity due to partial melting arises only near the base of the ice
156 shell. Since the viscosity in this region is already much smaller than that for near-surface,
157 this simplification will not significantly affect our results. We assume a Newtonian (stress-
158 independent) viscosity, and discuss the validity of this assumption further in Section 4.

159 Our viscoelastic relaxation code is described in *Kamata et al. [2012]*. Briefly, the
160 spheroidal deformation of a compressible Maxwell viscoelastic body induced by a sur-
161 face load is calculated. The governing equations are as follows [e.g., *Takeuchi and Saito,*
162 *1972; Peltier, 1974*]:

$$\frac{d\sigma_{ji}}{dt} + \frac{\mu}{\eta} \left(\sigma_{ji} - \frac{\sigma_{kk}}{3} \delta_{ji} \right) = \left(\kappa - \frac{2\mu}{3} \right) \frac{de_{kk}}{dt} \delta_{ji} + 2\mu \frac{de_{ji}}{dt}, \quad (3)$$

$$0 = \nabla_j \cdot (\sigma_{ji} - P \delta_{ji}) + \rho \nabla_i \phi, \quad (4)$$

$$\nabla^2 \phi = -4\pi G \rho, \quad (5)$$

163 where ∇_i is a spatial differentiation in direction of $i (= x, y, z)$, σ is stress tensor, e is strain
164 tensor, ϕ is gravitational potential, P is hydrostatic pressure, κ is bulk modulus, μ is
165 shear modulus, δ is the Kronecker delta, and G is the gravitational constant, respectively.

166 A finite difference is applied to the time differentials in the constitutive equation (i.e.,
 167 equation (3)), and a spherical harmonic expansion is applied to the three equations. This
 168 formulation leads to a six-component, time-dependent, inhomogeneous first-order ordinary
 169 differential equation system [*Kamata et al.*, 2012]. Then, time-marching calculations are
 170 carried out for each harmonic degree. The highest degree we calculate is 30 because we
 171 found there is no significant deformation for higher degrees. We checked that different
 172 values for the time-step did not change our results.

173 For this study, we had to modify our code in order to incorporate the changing thickness
 174 of the ice layer due to melting and freezing. Boundary conditions at liquid-solid interfaces
 175 and the governing equations in a liquid layer are given by *Saito* [1974]; our implementation
 176 of melting/freezing is described in Appendix A.

177 A shear modulus of 3.33 GPa is assumed for ice to maintain consistency with *Robuchon*
 178 *and Nimmo* [2011]. For simplicity, the rocky core is assumed to be an elastic body (i.e.,
 179 infinite viscosity) with a shear modulus of 50 GPa. The constitutive equation is given by

$$\sigma_{ji} = \left(\kappa - \frac{2\mu}{3} \right) e_{kk} \delta_{ji} + 2\mu e_{ji}. \quad (6)$$

180 This results in a simpler differential equation system; an inhomogeneous term is no longer
 181 needed. The use of a finite viscosity for the core would lead to a larger deformation.
 182 Nevertheless, in our models the temperature at the top of the core does not exceed 273 K,
 183 so the outermost region of the core would not deform significantly. Consequently, although
 184 the deep interior of the core may be hot and soft, our model gives a good first-order
 185 estimate on relaxation of impact basins.

186 We assume that Pluto is an incompressible body, appropriate for a relatively small body.
 187 Thus the dilatation $e_{kk} = 0$ at any time; the terms with bulk modulus κ in equations (3)

188 and (6) disappear. In addition, we ignore the density change due to thermal expansion.
189 Although this is not consistent with our thermal evolution calculations, this simplification
190 does not significantly affect our results, because the density changes are much smaller than
191 the unperturbed densities.

192 Since the start time of viscoelastic deformation is set to the basin formation age, it can
193 be different from the start time of the thermal evolution calculation. In this study, we
194 assumed five different basin formation times (t_{form}): 50, 100, 200, 400 and 1000 Myr after
195 the start of the thermal evolution model.

196 It is noted that lateral variations of mechanical properties are neglected because we use a
197 1D interior model. A basin-forming impact may cause significant transient heating around
198 the impact site and may contribute to form small-scale topography, such as a central peak.
199 Nevertheless, numerical studies suggest that impact heating should not affect the long-
200 term relaxation fraction of a basin [e.g., *Balcerski et al.*, 2010; *Melosh et al.*, 2013], and
201 this is particularly likely to be true for Pluto, where the expected impact velocities and
202 consequent heating are very modest.

3. Results

203 For a body like Pluto with a relatively low heat flow, the thickness of the lithosphere is
204 comparable to the scale of basins, and as a result the viscosity structure of the lithosphere
205 largely controls the rate of basin relaxation. Below, we first investigate the lithospheric
206 structure, before going on to calculate the present-day relaxation fraction of impact basins
207 for different parameter choices.

3.1. Thermal lithosphere

208 For illustrative purposes, we define the thermal lithosphere as the near-surface top layer
209 with viscosity higher than 10^{27} Pa s (Maxwell time comparable to the age of the solar
210 system). The equivalent temperature is 128 K for a reference viscosity $\eta_0 = 10^{14}$ Pa s. Fig-
211 ure 2 shows the time evolution of the thermal lithospheric thickness for different thermal
212 evolution cases.

213 In most cases, the thermal lithosphere grows rapidly for $t \leq 200$ Myr. This initial
214 rapid change is a result of the initial thermal state assumed. With a homogeneous initial
215 temperature of 150 K and $\eta_0 \leq 10^{17}$ Pa s, the viscosity is less than 10^{27} Pa s for the
216 whole H₂O layer, and thus there is no lithosphere initially. On the other hand, when $\eta_0 >$
217 10^{17} Pa s, the ice viscosity is higher than 10^{27} Pa s everywhere, so the initial lithospheric
218 thickness is 330 km. The lithospheric thickness at early times is, therefore, highly model
219 dependent. Nevertheless, since we mostly consider impact basins formed several hundred
220 Myr after the formation of Pluto, this early rapid change does not generally contribute to
221 their relaxation.

222 Following the initial transient, the lithospheric thickness decreases slowly and then
223 increases much more slowly. These longer-term effects are the result of the build-up,
224 release and decay of radiogenic heat from the core. Figure 2 (a) illustrates that a decrease
225 in radiogenic heating rate leads to a thicker thermal lithosphere at the present day, as one
226 would expect. On the other hand, as illustrated in Figure 2 (b), a significant thickening
227 cannot be achieved even by using a 10^5 times larger reference viscosity. This is because the
228 viscosity of ice is such a strong function of temperature that large changes in η_0 result in
229 only small changes in the temperature (and thus depth) at which a viscosity of 10^{27} Pa s
230 is achieved. This result holds for different C_K values. These results indicate that the

231 thermal lithospheric thickness is mainly controlled by the radiogenic heating rate in the
232 rocky core. As we will show below, for Pluto, basin relaxation is controlled mainly by the
233 thickness of the lithosphere, and thus relaxation is much more sensitive to the radiogenic
234 heating rate than to the reference viscosity assumed.

235 Figure 2 (a) shows that the 1D and 3D model results do not exactly coincide early in
236 the simulation. This is because the 3D results include an early transient heating term
237 from despinning caused by Charon (see *Robuchon and Nimmo* [2011]); this effect was not
238 included in the 1D model. As a result, initial lithospheric thinning occurs more rapidly
239 in the 3D case than in the equivalent 1D case. However, the long-term evolution in these
240 two cases is almost indistinguishable, as expected, since it is controlled primarily by long-
241 term radioactive decay. In particular, the minimum lithospheric thickness—which we will
242 argue below provides the primary control on basin relaxation—is almost identical in the
243 1D and 3D cases.

244 The effect of thermal convection is also illustrated in Figure 2 (b). Convection trans-
245 ports heat produced in the core more rapidly to the near surface, and thus the epoch of
246 lithospheric thinning happens earlier. Nevertheless, the minimum lithospheric thickness
247 obtained is not significantly different to conductive cases with the same C_K values. This
248 is because a specific heat flux implies a specific conductive boundary layer thickness in
249 the near-surface, irrespective of whether the material below that region is convective or
250 conductive. Again, because the main control on basin relaxation is lithospheric thickness,
251 whether the ice shell is convective or conductive turns out not to be a major factor in
252 controlling basin relaxation.

3.2. Basin relaxation

Figure 3 (a) shows the time evolution of normalized topography as a function of spherical harmonic degree for our nominal thermal evolution model. For each degree, the topographic amplitude is normalized by its initial value, because the fractional relaxation rate is independent of the initial topography for Newtonian fluids. In general, there is some degree of initial (instantaneous) elastic rebound, with less rebound happening at higher degrees. The rate of subsequent viscoelastic relaxation slows down (because of progressive cooling and stiffening of the lithosphere), and relaxation is mostly complete within 2 Gyr after formation. At this point, any remaining topography is effectively completely elastically supported. The result that low-degree (i.e., long-wavelength) topographies relax faster than high-degree (i.e., short-wavelength) topographies is consistent with previous studies [e.g., *Solomon et al.*, 1982; *Kamata et al.*, 2012] and is a consequence of two effects. First, and more important, a small basin is only sensitive to the shallow viscosity structure, which results in it experiencing a higher mean viscosity, and thus a longer relaxation time. Second, for all except the largest basins, flow is primarily vertical and not lateral. Under these circumstances, relaxation time decreases with increasing basin diameter; conversely, when flow is predominantly lateral, relaxation time is longer at longer wavelengths [e.g., *McKenzie et al.*, 2000; *Zhong and Zuber*, 2000]. Figure 3 (a) also illustrates that the normalized topography is ~ 1 for degree ~ 30 , indicating that almost no deformation occurs for these degrees. Considering the fact that a higher degree leads to smaller deformation, we assume the final/initial ratio of topography is 1 for degrees higher than 30.

274 We note that the deformation timescale for degree 1 is much faster than those for
 275 higher degrees. Since the center of mass does not change with time, the degree-1 potential
 276 perturbation is zero at any time [e.g., *Saito*, 1974]. Because of this, degree-1 deformation
 277 excites only “transition modes”; the “mantle mode” is not excited [*Greff-Lefftz and Legros*,
 278 1997]. The timescales of transition modes are much shorter than that of the mantle mode
 279 [e.g., *Han and Wahr*, 1995], resulting in a rapid deformation only for degree 1.

280 Using these results, we can obtain the time evolution of topography for an arbitrary
 281 initial topography. Figure 3 (b) shows the time evolution of topography of an impact basin
 282 1000 km in diameter. Here we use the same paraboloid initial shape as *Robuchon et al.*
 283 [2011] and an initial depth of 1 km. We note that many impact basins on icy satellites
 284 are deeper than 1 km [e.g., *Giese et al.*, 2008; *White et al.*, 2013]. Nevertheless, the initial
 285 topography assumed is irrelevant for a Newtonian (stress-independent) rheology. The
 286 present-day relaxation fraction f_{rel} is given as follows;

$$f_{\text{rel}} = 1 - \frac{d_{\text{fin}}}{d_{\text{ini}}}, \quad (7)$$

287 where d_{ini} and d_{fin} are initial and final basin depths, respectively. The “basin depth” is
 288 defined as the difference in altitude at the rim and that at the basin center. For the
 289 particular case of Figure 3 (b), $f_{\text{rel}} \sim 31.5\%$.

290 Figure 4 summarizes the present-day relaxation fraction (f_{rel}) as a function of basin
 291 diameter for a suite of different evolution scenarios. The value of f_{rel} decreases with
 292 decreasing basin diameter because short-wavelength components relax less than long-
 293 wavelength components (see above). In particular, impact basins smaller than ~ 200 km
 294 in diameter do not exhibit significant relaxation under any circumstances: they are entirely

295 elastically supported. This result indicates that such small impact basins are unlikely to
296 provide information on the thermal state of Pluto.

297 In contrast, impact basins larger than ~ 200 km in diameter can relax depending on the
298 interior viscosity structure. Figure 4 clearly illustrates that the dominant factor controlling
299 basin relaxation is radiogenic heat produced in the rocky core. For example, f_{rel} can be
300 $>60\%$ for impact basins 1000 km in diameter when $C_K = 738$ ppm while $f_{\text{rel}} < 20\%$ when
301 $C_K \leq 50$ ppm. Such a large difference in f_{rel} cannot be achieved by a change in reference
302 viscosity even by a factor of 10^4 . *As discussed above, this is because the lithospheric*
303 *thickness is mainly controlled by the radiogenic heating rate.*

304 The fact that basin relaxation is so insensitive to reference viscosity is in some ways an
305 advantage, because it means that our ignorance about ice grain size and the temperature
306 at the base of the ice shell do not matter. On the other hand, this result also means that
307 we cannot use basin relaxation as a probe of whether or not a deep subsurface ocean exists.
308 *Robuchon and Nimmo [2011]* showed that the reference viscosity controlled whether or
309 not a *subsurface* ocean would form: high viscosities result in inefficient (conductive) heat
310 transfer and ocean formation, while low viscosities result in efficient (convective) heat
311 transfer and no *subsurface* ocean forming. However, the near-surface viscosity structure
312 is the same in either case (see above), and it is this structure that is mainly being probed
313 by relaxation. As a result, basin relaxation is not sensitive to the presence or absence
314 of a *subsurface* ocean. This is an important result; it arises because at sufficiently long
315 timescales both water and ice near the melting point have sufficiently low viscosities that
316 they provide no topographic support. In Appendix B, we show the insensitivity of basin

317 relaxation to the presence of a subsurface ocean more clearly by using simpler viscosity
318 models.

319 Figure 4 further illustrates that the timing of basin formation has almost no effect
320 on the final basin topography. On the other hand, as shown in Figure 2, the thermal
321 lithospheric thickness changes significantly during the epoch of basin formation (i.e., 50–
322 1000 Myr). These results indicate that the final (present-day) basin topography does
323 not reflect the lithospheric thickness immediately after the impact. This is because the
324 lithosphere generally becomes thinner after basin formation (Figure 2). For example, when
325 $C_K = 738$ ppm, the thickness of the lithosphere at $t \sim 1$ Gyr (during basin formation)
326 is ~ 100 km, while at $t \sim 2$ Gyr it is ~ 40 km. Because of this lithospheric thinning,
327 relaxation is more pronounced than would be expected based on the initial lithospheric
328 thickness. As a consequence, the final basin topography reflects the minimum lithospheric
329 thickness, as we will show in Section 3.4.

3.3. Stress and faulting patterns

330 Displacements due to basin relaxation introduce stresses may lead to faulting. Faulting
331 patterns can be predicted from the stress differences [e.g., *Anderson, 1951*]. For example,
332 if the radial stress exceeds the hoop (or tangential) stress, and both are extensional,
333 concentric normal faults are expected. In contrast, if hoop stress exceeds radial stress,
334 and both are extensional, radial normal faults are expected.

335 Faulting patterns due to loads on the surface have been investigated in previous studies
336 [e.g., *Golombek, 1985; Janes and Melosh, 1990; Freed et al., 2001*]. *Janes and Melosh*
337 [1990] show that on a spherical body interior concentric faults are dominant for the case
338 of a broad load on a thin lithosphere, and interior radial faults are dominant for the

339 case of a narrow load on a thick lithosphere. In other words, faults due to relaxation
340 inside a large basin would be concentric while those inside a small basin would be radial,
341 and the transition diameter depends on the lithospheric thickness. This transition is
342 due to the effect of planetary curvature; membrane stresses support a broad load on
343 a thin lithosphere while bending stresses dominate for the case of a narrow load on a
344 thick lithosphere [*Turcotte et al.*, 1981; *Janes and Melosh*, 1990]. This fact suggests that
345 fault directions inside impact basins could provide a constraint on the thickness of the
346 lithosphere. To investigate the sensitivity of faulting patterns on the thermal properties,
347 we calculate radial and hoop stresses and fault directions. We use analytical expressions
348 of stresses and displacements given by *Takeuchi and Saito* [1972], and we assume a zero
349 stress state prior to the onset of relaxation.

350 Figure 5 shows radial and hoop stresses at the surface as a function of horizontal distance
351 from the basin center. A basin diameter of 800 km is assumed here, and predicted faulting
352 patterns are also shown. For the case of $C_K = 738$ ppm, concentric normal faults are
353 dominant. In contrast, for the case of $C_K = 200$ ppm, radial normal faults are dominant.
354 The stresses are lower in this case because less rebound has occurred. This relation
355 between fault directions and the lithospheric thickness is consistent with previous studies
356 [*Janes and Melosh*, 1990].

357 Figure 6 show the basin diameter at which the transition of fault directions occurs.
358 Results for $T_{\text{ini}} = 150$ K, $\eta_0 = 10^{16}$ Pa s, and $t_{\text{form}} = 1$ Gyr are shown here. Differ-
359 ent parameter values do not change the results much because basin relaxation is mainly
360 controlled by C_K . As discussed above, a small transition diameter is found for a high
361 radiogenic heating rate (which results in a thin lithosphere). Figure 6 indicates that, in

362 order to constrain the thermal evolution of Pluto based on fault directions, impact basins
363 700–1200 km in diameter would be of most use.

3.4. Elastic and Viscoelastic Comparison

364 Because of the strong temperature dependence of ice, viscosity near the surface is very
365 high and decreases with depth. Such a viscosity profile can be approximated as an elastic
366 shell overlying an inviscid fluid: an elastic thin shell model [e.g., *Turcotte et al.*, 1981]. We
367 have argued above that it is Pluto’s relatively thick lithosphere that exerts the primary
368 control on basin relaxation; if this is correct, the elastic shell model should approximately
369 predict the final relaxation state.

370 Figure 7 plots the degree-dependent normalized final topography obtained by using the
371 time-dependent viscoelastic relaxation model and compares it with results obtained by
372 using a time-independent elastic thin shell approach. The latter is also obtained by using
373 our viscoelastic code; we assume a three layer Pluto which consists of an outer elastic
374 (not viscoelastic) layer, an intermediate inviscid fluid layer, and an elastic core. As seen
375 in Figure 7, the shapes of the two sets of curves are very similar, indicating that the purely
376 elastic approach provides a reasonable approximation as long as the appropriate effective
377 elastic thickness T_e is used.

378 The purely elastic solution has been compared with the analytical solution by *Turcotte*
379 *et al.* [1981] (not shown in Figure 7); small differences arise because the analytical solu-
380 tion is obtained assuming a fixed (i.e., radially-independent) gravity acceleration. Both
381 solutions, however, are identical when the shell is very thin, confirming the validity of our
382 code.

383 As a rough guide to deriving the appropriate T_e , we note that $T_e = 40$ km provides a
 384 good fit to the baseline ($C_K = 738$ ppm) case. We find that this effective elastic thickness
 385 is close to the minimum thickness of the thermal lithosphere (see Figure 2 (b)). The
 386 highest heat flux in this case is 5.0 mW m^{-2} at $t \sim 2.0$ Gyr and the thermal conductivity
 387 is $2.25 \text{ W m}^{-1} \text{ K}^{-1}$. The isotherm defining the base of the (40 km-thick) effective elastic
 388 layer is then at 129 K. This temperature is in good agreement with that used to define
 389 the base of the thermal lithosphere (see Section 3.1). For the $C_K = 200$ ppm case, we
 390 would then predict $T_e \approx 110$ km at $t \sim 3.5$ Gyr, in reasonable agreement with the model
 391 results.

392 Figure 8 more clearly illustrates the correspondence of the effective elastic thickness
 393 derived from the final basin topography and the minimum thermal lithospheric thickness.
 394 Here, we fit the model relaxation fraction for degrees 2–30 with our purely elastic model to
 395 obtain a least-squares estimate of the effective elastic thickness. The degree-1 component
 396 is excluded because of its poor dependence on the interior structure [e.g., *Métivier et al.*,
 397 2008]. This figure indicates that, based on the degree-dependent relaxation fraction, we
 398 can estimate the effective elastic thickness, which corresponds closely to the minimum
 399 thermal lithospheric thickness.

400 We note that there is one exceptional case: a basin formed at an extremely old age (i.e.,
 401 50 Myr) on an extremely soft (i.e., $\eta_0 = 10^{13}$ Pa s), heat-depleted (i.e., $C_K = 50$ ppm)
 402 Pluto. In our model, the lithosphere at such an early age is very thin (see Section 3.1; this
 403 is highly model dependent). Because of the very small reference viscosity, a basin formed
 404 on an extremely thin lithosphere can relax within a short time after its formation. On
 405 the other hand, the lithosphere grows rapidly and then remains very thick (i.e., ~ 200 km)

406 because of the small heat production rate (Figure 2). As a result, in this case the effective
407 elastic thickness estimated from the final topography is somewhat less than than the
408 minimum lithospheric thickness subsequent to basin formation.

409 Finally, we show the present-day relaxation fraction as a function of the minimum
410 lithospheric thickness in Figure 9. The minimum lithospheric thickness is obtained from
411 thermal evolution calculations (Figure 2). As discussed above, for a given basin size, the
412 lithospheric thickness is the main control on basin relaxation, and this thickness is mainly
413 controlled by the amount of heat production in the core.

4. Discussion

414 Figure 4 summarizes our main results. Impact basins on Pluto in excess of 200 km
415 diameter are expected to show some degree of relaxation, up to 60%; the main control
416 on the degree of relaxation is the radiogenic content of the silicate interior. We antic-
417 ipate that, as at Iapetus [e.g., *Robuchon et al.*, 2011; *White et al.*, 2013], measurement
418 by *New Horizons* of impact basin shapes will therefore provide constraints on the long-
419 term thermal evolution of Pluto. A second important result is that stresses arising from
420 progressive relaxation may lead to tectonic features at the surface (Figure 5), and if so,
421 then the orientation of these features places constraints on Pluto's lithospheric thickness
422 (Figure 6).

423 When considering these results, however, there are several caveats and consequences
424 which should be borne in mind.

425 An important potential practical limitation is that it may not be straightforward to
426 estimate the relaxation fraction of basins on Pluto. Impactors on Pluto are expected to
427 have relatively modest impact velocities, because of Pluto's modest (heliocentric) orbital

428 velocity of 4.7 km s^{-1} : *Zahnle et al.* [2003] give a mean impact velocity of 1.9 km s^{-1}
429 (barely supersonic). As a result, the **depth-diameter** ratios observed for unrelaxed basins
430 on other icy bodies may not provide a good indication of unrelaxed basin morphologies
431 on Pluto [*Bray and Schenk*, 2014]. Iapetus, with a mean impact velocity of 6.1 km s^{-1}
432 and plentiful unrelaxed basins, may provide the best, if imperfect, analogue available. **In**
433 **addition, further studies to estimate the depth-diameter ratio of unrelaxed large impact**
434 **basins using hydrocode simulations [e.g., *Senft and Stewart*, 2011; *Bray and Schenk*, 2014]**
435 **would be very important.**

436 From a theoretical point of view, the main simplifications we have adopted are a Newto-
437 nian viscosity, neglect of yielding in the near-surface [cf. *Dombard and McKinnon*, 2006],
438 **and the presence of volatiles other than H_2O** . The first issue was examined by *Robuchon*
439 *et al.* [2011] who concluded that non-Newtonian effects are relatively small as long as basin
440 relaxation is not too extreme. The main difficulty with ice is not its non-Newtonian rheol-
441 ogy, per se, but the fact that the reference viscosity is so poorly constrained. Fortunately,
442 as we have shown above, our results are very insensitive to the value of η_0 adopted.

443 We examined the second issue (i.e., neglect of yielding) by additional calculations. **To**
444 **permit near-surface deformation**, we reduced the viscosity of the top 10 km-thick layer
445 and calculated the resulting deformation. Results are shown in Figure 10. If the surface
446 viscosity $\geq 10^{27} \text{ Pa s}$, the effect of a surface weak layer is very small. In contrast, if
447 the surface viscosity $< 10^{27} \text{ Pa s}$, final topographic amplitudes become smaller than for
448 the nominal case. These smaller final topographic amplitudes lead to a 10 km smaller
449 inferred effective elastic thickness (Figure 7). Since this change is small compared to the
450 likely range of elastic thicknesses, we regard the effect of near-surface yielding as unlikely

451 to significantly alter our conclusions. Finally, if the surface viscosity $\leq 10^{23}$ Pa s, lateral
452 flow can occur, resulting in a larger relaxation fraction. However, this effect arises only for
453 degrees higher than ~ 20 (i.e., small craters). We note that this simple calculation (i.e.,
454 reducing the near-surface viscosity) provides only a crude representation of the effect
455 of surface yielding. Nevertheless, a more realistic calculation that limits the strength
456 depending on the depth using a finite-element method also found that yielding does not
457 play a major role in surface deformation [*Dombard and McKinnon, 2006*].

458 In Section 3.3, we discuss the relation between basin relaxation and resulting faulting
459 patterns. The faulting patterns shown in Figure 5 and Figure 6, however, are calculated as-
460 suming that the stress profile is determined purely by relaxation. Stresses associated with
461 the impact and its immediate aftermath may complicate the tectonic patterns produced,
462 although the long duration associated with relaxation means that relaxation-related tec-
463 tonic features should overprint other impact-related features. In addition, the magnitude
464 of the predicted stress difference needs to be compared with the strength of ice in order
465 to assess whether faults can develop or not. Since the magnitude of the stress depends
466 on the magnitude of displacement, the depth-diameter ratio of unrelaxed basin must be
467 known in order to calculate the stress.

468 An advantage of our treatment is its use of a spherical geometry, which is required
469 when the basin diameter is comparable to the satellite radius. Satellites in the outer solar
470 system frequently exhibit impact basins having this kind of relative scale. While we do
471 not yet know how large impact basins will be on Pluto, our spherical geometry means
472 that effects of curvature are not being inappropriately neglected.

473 The thermal conductivity assumed ($2.25 \text{ W m}^{-1} \text{ K}^{-1}$) is conservatively low, which
474 promotes a relatively thin lithosphere. Such a low value is appropriate for a body with
475 a relatively thick insulating regolith, which Pluto may well have. Higher conductivities
476 would result in a thicker lithosphere and less relaxation.

477 On the other hand, we have neglected the role of secondary volatiles, which might change
478 the lithospheric rheology or (if present as clathrates) alter its thermal conductivity. For
479 instance, CO_2 ice has an activation energy of $\sim 33 \text{ kJ mol}^{-1}$ and is significantly weaker than
480 water ice under the same conditions [Durham *et al.*, 1999]. An inclusion of NH_3 also results
481 in a weak rheology; an activation energy $\sim 34 \text{ kJ mol}^{-1}$ is found for ammonia-water ice
482 with 4–8% of NH_3 [Arakawa and Maeno, 1994]. Thus, volatiles might reduce the effective
483 lithospheric thickness if present in the ice shell in sufficient quantities. To investigate
484 such an effect, we further calculate basin relaxation using a very small activation energy
485 of 30 kJ mol^{-1} , which is half of our nominal case. Results are shown in Figure 11. Since
486 a decrease in activation energy leads to a decrease in viscosity for a given temperature
487 and a given reference viscosity, it results in a thinner lithosphere and a larger deformation
488 for a given heat flux. Nevertheless, the effective elastic thickness inferred from the final
489 basin state corresponds well with the minimum lithospheric thickness. Thus, basin final
490 states can be used as a good index for the lithospheric thickness even if the rheology of
491 the upper part of Pluto is much weaker than that of pure water ice.

492 It is clear, both from this work and from Robuchon and Nimmo [2011], that the ra-
493 diogenic abundance in Pluto is the single most important factor controlling its long-term
494 evolution. This factor, here expressed as potassium concentration C_K , is currently highly
495 uncertain, because of our lack of knowledge concerning compositions in the outer solar

496 system [e.g. *Ciesla*, 2010]. Our baseline value of 738 ppb is derived from carbonaceous
497 chondrites [*Lodders*, 2003], but ordinary chondrites can have significantly higher values
498 [*Castillo-Rogez et al.*, 2007]. On the other hand, if Pluto experienced a giant Charon-
499 forming impact [*Canup*, 2005], some loss of volatile materials (including K) may have
500 occurred. Leaching of K from the silicates into any subsurface ocean will not change the
501 details of our relaxation calculations significantly, unless there is some way of advecting
502 this K-enriched material into the near-surface of the ice shell. Further consideration of
503 the abundance and (re)distribution of radiogenic elements in outer solar system objects
504 will hopefully be facilitated by the forthcoming *New Horizons* observations.

505 An interesting consequence of basin relaxation on Pluto is that it generally occurs on
506 billion-year timescales (Figure 3). As noted by *Nimmo and Matsuyama* [2007], Pluto's
507 slow rotation rate makes it rotationally unstable. Thus, formation of a large impact basin
508 could cause significant prompt reorientation (true polar wander), potentially generating
509 global tectonic stress patterns. Subsequent slow basin relaxation would result in a slow
510 reversal of the initial true polar wander path. Further tectonic features, both from this
511 reorientation and the relaxation itself (see above) would likely result. Thus, the tectonic
512 consequences of large impact basins on Pluto are likely to prove interesting.

513 Lastly, it is of interest to consider how our results might apply to Charon. Because of its
514 smaller size, radiogenic heat flows will have been lower on Charon. This effect, together
515 with the lower gravity, is likely to result in less-relaxed basins. The main caveat to this
516 conclusion is that Charon is more likely to have experienced significant tidal heating early
517 in its history than Pluto. Thus, in the event that Charon's basins are more relaxed than
518 those of Pluto, tidal heating is the likeliest explanation.

5. Conclusions

519 We investigated the thermal evolution and viscoelastic deformation of impact basins
520 on Pluto assuming a wide range of parameter values: the amount of radiogenic heat,
521 the reference viscosity of the ice shell, the time of basin formation, and the diameter of
522 the basin. Our results indicate that for a **water-ice shell** basins smaller than 200 km in
523 diameter would not experience viscous relaxation and would be supported elastically since
524 formation. In contrast, basins larger than 200 km in diameter would experience relaxation
525 depending on the interior thermal state; the amount of radiogenic heat in the rocky core
526 is the main controlling factor. Other factors, such as the reference viscosity and the time
527 of basin formation, which are poorly known, do not affect basin relaxation significantly.
528 These results arise from the fact that the relaxation of a basin is mainly controlled by
529 the lithospheric thickness, and this thickness is mainly controlled by radiogenic heating
530 for the case of Pluto. As expected from this fact, the presence of a subsurface ocean
531 has little effect on basin relaxation; neither an inviscid liquid water layer nor a low-
532 viscosity ice layer can support basin topography on billion-year timescales. **Other volatiles,**
533 **such as CO₂ or NH₃, if present in the ice shell in sufficient quantities could increase the**
534 **predicted relaxation fraction of basins.** We also show that the tectonic pattern inside
535 basins ~ 1000 km in diameter can be used to bound the lithospheric thickness and thus
536 the amount of radiogenic heat in the core. Our results therefore suggest that future
537 observations of basin structures will provide key information on the thermal evolution of
538 Pluto.

Appendix A: Relaxation incorporating the freezing and melting of an ice shell

539 Here we first briefly discuss the equation systems we solved in this study. Six-component
 540 and two-component equation systems are used for solid (both elastic and viscoelastic
 541 bodies) and liquid phases, respectively. More specifically, equation systems written as

$$\frac{dy_i^n(r, l)}{dr} = A_{ij}^n(r, l)y_j(r, l) + B_i^n(r, l) \quad (\text{A1})$$

542 are solved. Here, n is time step, r is radial distance from the center of the planet, and l
 543 is harmonic degree, respectively. The subscript $i(j) = 1-6$ for the solid parts and $i(j) =$
 544 $5, 7$ for the liquid parts. $y_1, y_2, y_3, y_4,$ and y_5 are vertical displacement, vertical stress,
 545 horizontal displacement, horizontal stress, and potential perturbation, respectively. Both
 546 y_6 and y_7 are functions of dy_5/dr . B^n are inhomogeneous terms required only for the
 547 viscoelastic parts and depend on y^{n-1} . See *Kamata et al.* [2012] and *Saito* [1974] for
 548 further detailed discussion and boundary conditions. At each time step and each depth,
 549 we check the phase (i.e., solid or liquid), and an appropriate equation system is chosen.

550 Consider a case in which solidification occurs in the interval between n ($t = t^n$) and $n+1$
 551 ($t = t^{n+1}$) at a radial distance r . For a solid, six-component y_i^n are required to calculate
 552 six-component y_i^{n+1} (and B_i^{n+1}) since we assume that ice is a Maxwell body. However,
 553 since the region is liquid at t^n , we only have two-component y^n ; we cannot calculate y^{n+1}
 554 simply from y^n . To resolve this issue, we solve the equation system for a solid elastic
 555 body at t^n ; equation (A1) is solved with $B^n = 0$ and $i = 1-6$. We do so based on the
 556 assumption that ice (a Maxwell body) behaves initially as an elastic body. This equation
 557 system requires six boundary conditions. Because the solidified portion is continuously
 558 connected to the pre-existing ice above, $y_1, y_2, y_4, y_5,$ and y_6 need to be continuous at the
 559 top of the solidified part; only y_3 (i.e., horizontal displacement) need not be continuous.
 560 The last boundary condition is that $y_4 = 0$ at the bottom of the solidified part; it is in

561 contact with the liquid layer below, and thus the horizontal stress needs to be zero. We
 562 can thus obtain the six-component y_i^n , and six-component y_i^{n+1} can then be calculated.

563 We examine the validity of the implementation of freezing to our code as follows. Be-
 564 cause freezing cases (i.e. time-variable shell thickness) do not have analytical solutions,
 565 we compare our results for a freezing case with those for a completely solid case in which
 566 we approximate the (time-varying) liquid layer as a solid layer with a much lower viscos-
 567 ity. Figure A1 (a) shows the interior model we use here. We assume an incompressible,
 568 constant-density three-layer body, which consists of a top viscoelastic layer and an invis-
 569 cid fluid core. The planetary radius is 1180 km, the density is 1850 kg m^{-3} , the shear
 570 modulus is 1 GPa, and the viscosity of the top layer is $5 \times 10^{23} \text{ Pa s}$, respectively. The
 571 depth of the core is 100 km. The depth of the base of the top layer, on the other hand,
 572 depends on time; the thickness of the top layer H is given as

$$H(t) = H_1 + (H_2 - H_1) \exp(-t/\tau) \quad (\text{A2})$$

573 where t is time, $H_1 = 100 \text{ km}$, $H_2 = 10 \text{ km}$, and $\tau = 1 \text{ Gyr}$, respectively. The layer in
 574 between has a thickness of $(100 - H(t)) \text{ km}$ and is either an inviscid fluid (i.e., liquid)
 575 layer or a viscoelastic (i.e., solid) layer with a low viscosity η_{weak} . In the following, we
 576 refer the former and latter cases as the “liquid” case and “solid” cases, respectively. We
 577 expect that the liquid case should coincide with a solid case with a small η_{weak} .

578 Figure A1 (b) compares the time evolution of normalized topography for liquid and solid
 579 cases. As expected, the solid case with a small viscosity (i.e., $\eta_{\text{weak}} = 10^{21} \text{ Pa s}$) leads to
 580 almost the same results as the liquid case. **We found that this result is not specific to the**
 581 **time evolution model adopted for $H(t)$, or the harmonic degree assumed,** and conclude
 582 that our implementation of shell freezing is adequate.

583 In contrast to freezing, melting does not require any additional calculation between t^n
 584 and t^{n+1} because y_5^{n+1} and y_7^{n+1} are independent of y^n . We checked the validity of our
 585 code for a melting case by considering a two-layer incompressible planet consisting of
 586 a solid layer overlying an inviscid fluid. Here we compare the results of our numerical
 587 code and those of a semi-analytical solution for a viscous fluid model. Figure A2 (a)
 588 shows the interior model for this validation; the thickness of the solid layer H is given by
 589 equation (A2) using $H_1 = 10$ km, $H_2 = 100$ km, and $\tau = 100$ Myr. As before, we assume
 590 that the planetary radius is 1180 km, the density is 1850 kg m^{-3} , and the viscosity of
 591 the solid layer is 5×10^{23} Pa s, respectively. For the viscoelastic model, we adopted a
 592 shear modulus of 100 GPa, implying a Maxwell time of 0.16 Myr. This means that for
 593 timescales significantly longer than 0.16 Myr, a viscous solution should provide a very
 594 good approximation to the full viscoelastic calculation.

595 A semi-analytical solution for a viscous fluid model is given by *Solomon et al.* [1982].
 596 When the density is uniform, the surface topographic amplitude F of a viscous fluid layer
 597 overlying an inviscid fluid is given as

$$\frac{dF}{dt} = \frac{\rho g}{2\eta k} \frac{e^{-2kH} - 4kH - e^{2kH}}{e^{-2kH} + e^{2kH} - 4k^2H^2 - 2} F \quad (\text{A3})$$

598 where ρ is density, g is gravitational acceleration, η is viscosity, k is wavenumber of topog-
 599 raphy, and H is the thickness of the viscous fluid layer, respectively. Here, wavenumber
 600 k is used because a Cartesian coordinate system is used by *Solomon et al.* [1982]. Since
 601 $H = H(t)$, a numerical integration of equation (A3) is required to obtain $F(t)$.

602 Figure A2 (b) shows a comparison between the viscoelastic and viscous fluid models. For
 603 the viscoelastic model, we use harmonic degree $l = 70$. This degree gives a wavelength
 604 $\lambda = 2\pi R / \sqrt{l(l+1)} \sim 105$ km, which is much smaller than the planetary radius $R =$

605 1180 km; so the Cartesian assumption is appropriate. For the viscous fluid model, we use
 606 wavenumber $k = 2\pi/\lambda \sim 6.0 \times 10^{-5} \text{ m}^{-1}$. As illustrated in Figure A2 (b), the models
 607 show a good agreement, indicating the validity of our implementation of melting.

608 We did not conduct a comparison with a viscous fluid model for the freezing case. This
 609 is because the frozen layer shows an elastic response immediately after the freezing, and
 610 thus a viscous fluid model might not be appropriate.

Appendix B: Effect of a subsurface ocean on relaxation

611 Here we examine the sensitivity of basin relaxation to the presence of a subsurface ocean.
 612 Figure A3 (a) shows the time-independent viscosity structures used for this examination.
 613 The viscosity deeper than 100 km is assumed to be 0 for the “liquid” case and $4.16 \times$
 614 10^{15} Pa s for the “solid” case. The viscosity structures shallower than 100 km are assumed
 615 to be the same. The viscosity profile for the liquid case is given by that at $t = 2.0 \text{ Gyr}$
 616 obtained by using the 3D convection model assuming the initial temperature 150 K and
 617 the reference viscosity $4.16 \times 10^{15} \text{ Pa s}$. Since the purpose of this calculation is to examine
 618 the effect of the viscosity of deep interior, we ignore the density difference between ice and
 619 water. Because of this, the same thickness for the H_2O layer (i.e., 330 km) is assumed for
 620 both viscosity model. We use densities and shear moduli used in our main calculation.

621 Figure A3 (b) shows the time evolution of normalized topographies for two different
 622 degrees. The instantaneous elastic response differs between the liquid and solid cases.
 623 However, the differences between the models decrease with time and are negligible for $t >$
 624 100 yr for all harmonic degrees. This timescale depends on the reference viscosity assumed;
 625 if we use a 10 times higher reference viscosity, the timescale for agreement becomes \sim
 626 10^3 yr . Nevertheless, this timescale would still be much smaller than basin formation

627 ages even if the reference viscosity is very high. Thus, the presence of a subsurface ocean
628 itself does not change the final basin topography. The physical explanation for this effect
629 is that the Maxwell times of (effectively inviscid) water and ice near the melting point
630 are both so low compared to the age of the basin that neither material can provide any
631 topographic support.

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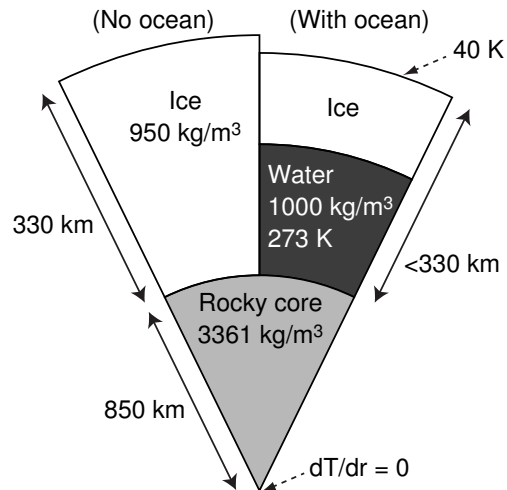


Figure 1. Interior structure model of Pluto, after *Robuchon and Nimmo* [2011]. The radius of the rocky core is fixed to 850 km [*McKinnon et al., 1997*]. The thickness of the H₂O layer depends on the thickness of a subsurface ocean. When there is no liquid water layer, the thickness of the H₂O layer is 330 km. A development of a subsurface ocean reduces the thickness of the H₂O layer to conserve the total mass.

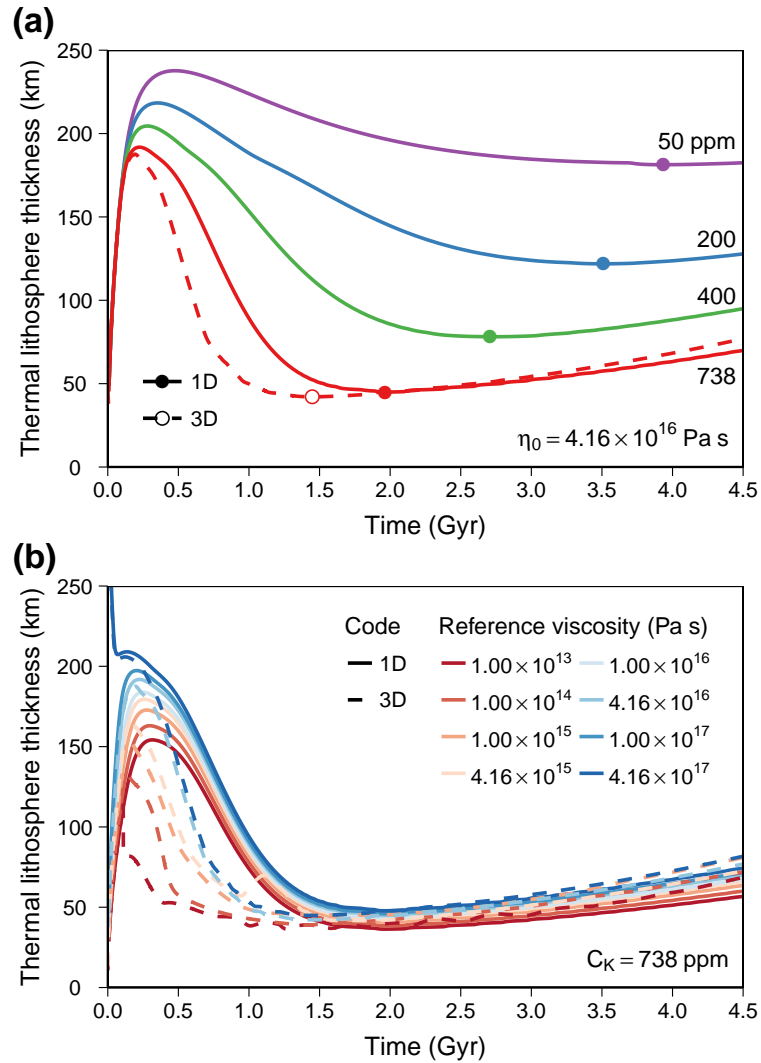


Figure 2. The time evolution of the thermal lithospheric thickness. The lithosphere is defined as the near-surface region in which viscosity exceeds 10^{27} Pa s. Results for $T_{\text{ini}} = 150$ K are shown. The solid and dashed line show results for 1D and 3D calculations, respectively. (a) Dependence on the radiogenic heating rate. Results for $\eta_0 = 4.16 \times 10^{16}$ Pa s are shown. Circles indicate minimum values. The values of C_K are shown. All cases are conductive for these parameters. (b) Dependence on the reference viscosity. Results for $C_K = 738$ ppm are shown. The thermal lithospheric thickness is mainly controlled by the radiogenic heating rate.

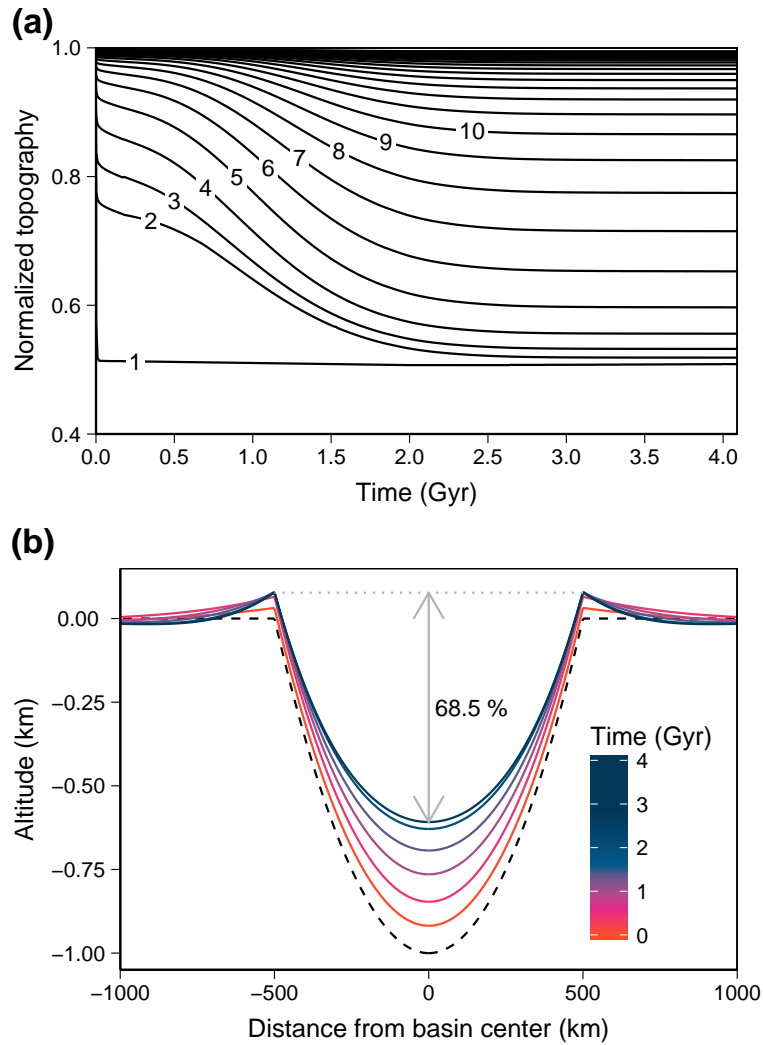


Figure 3. (a) The time evolution of normalized topography for each harmonic degree. Results for $T_{\text{ini}} = 150$ K, $C_K = 400$ ppm, $\eta_0 = 10^{15}$ Pa s, and $t_{\text{form}} = 400$ Myr are shown. Numbers indicate harmonic degrees. The amplitude of topography is normalized by its initial value. (b) The time evolution of topography for an initially paraboloid basin 1000 km in diameter. The initial depth is assumed to be 1 km. Calculation conditions are the same for (a). The dashed line shows the initial condition. The present-day relaxation fraction is $\sim 31.5\%$.

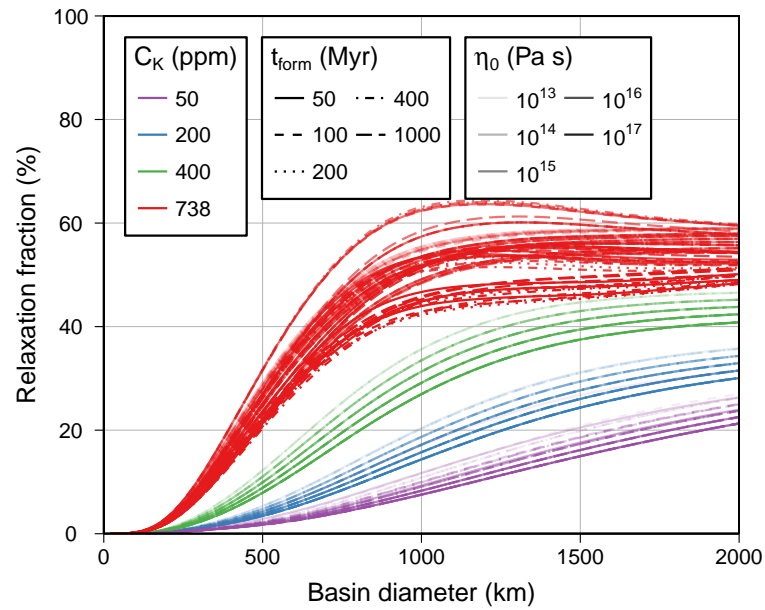


Figure 4. Present-day relaxation fraction for an initially paraboloid basin. Results under all thermal, rheological, and basin formation age conditions are shown. Both 1D and 3D calculation results are shown. Relaxation fractions strongly depend on radiogenic heating in the core.

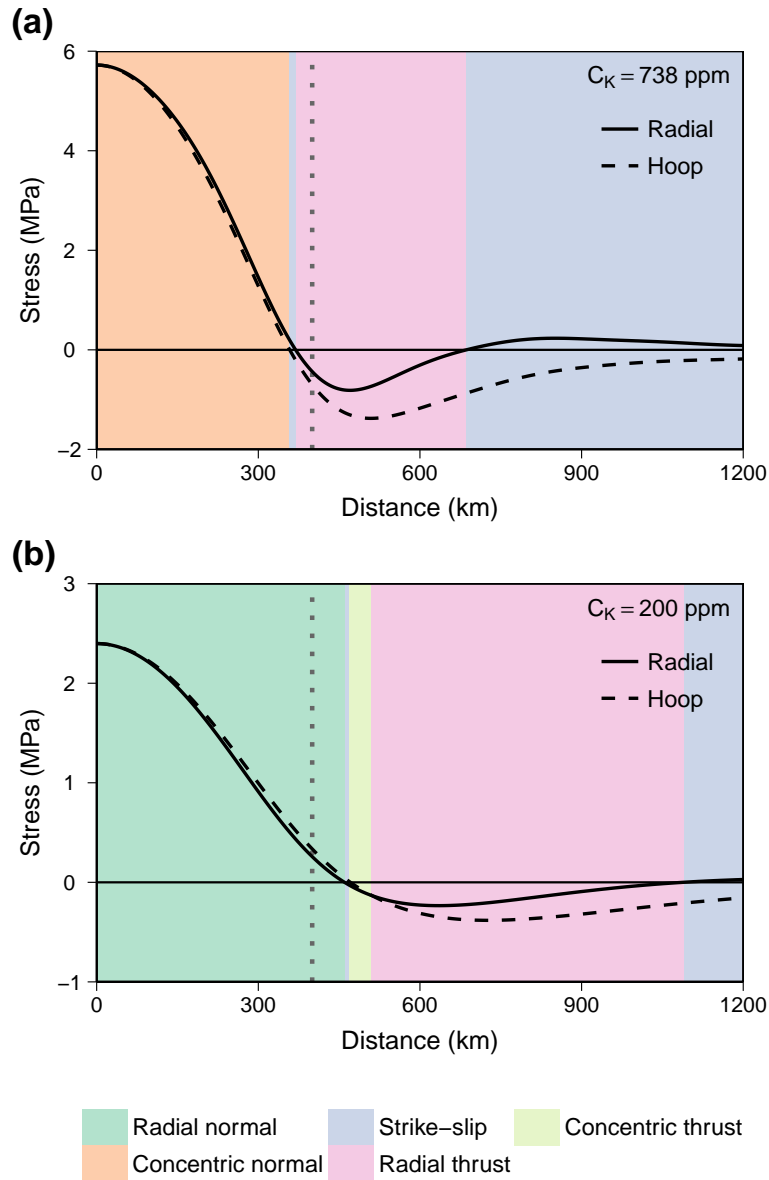


Figure 5. Surface stress profiles and faulting patterns expected from the final state of a basin with diameter 800 km. Results using a 1D thermal evolution code and assuming $T_{\text{ini}} = 150$ K, $\eta_0 = 10^{16}$ Pa s, and $t_{\text{form}} = 1$ Gyr are shown. Positive and negative stresses are extensional and compressional, respectively. Vertical dotted lines indicate the basin main rim. (a) $C_K = 738$ ppm and (b) $C_K = 200$ ppm, respectively. Faults inside the basin are predicted to be concentric and radial for $C_K = 738$ ppm and 200 ppm, respectively. Present-day relaxation fractions for (a) and (b) are $\sim 44.3\%$ and $\sim 10.6\%$, respectively.

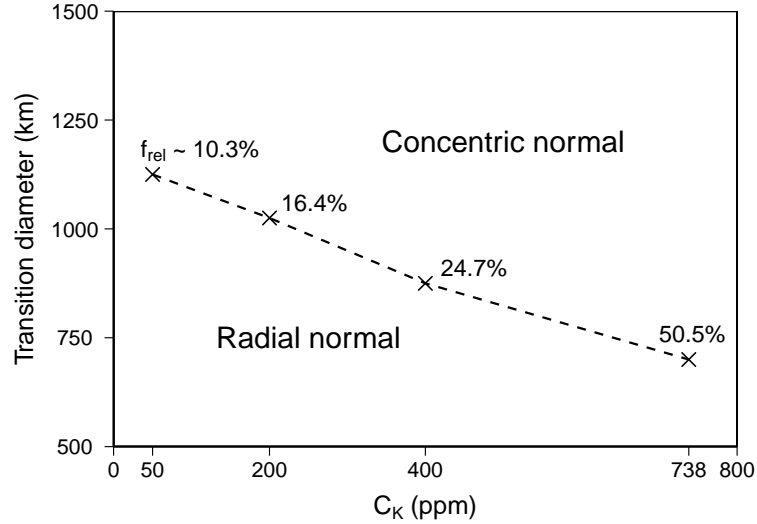


Figure 6. Radial to concentric transition diameter as a function of the concentration of ^{40}K in the silicate core. Results using a 1D thermal evolution code and assuming $T_{\text{ini}} = 150$ K, $\eta_0 = 10^{16}$ Pa s, and $t_{\text{form}} = 1$ Gyr are shown. The values of f_{rel} for each point are also shown.

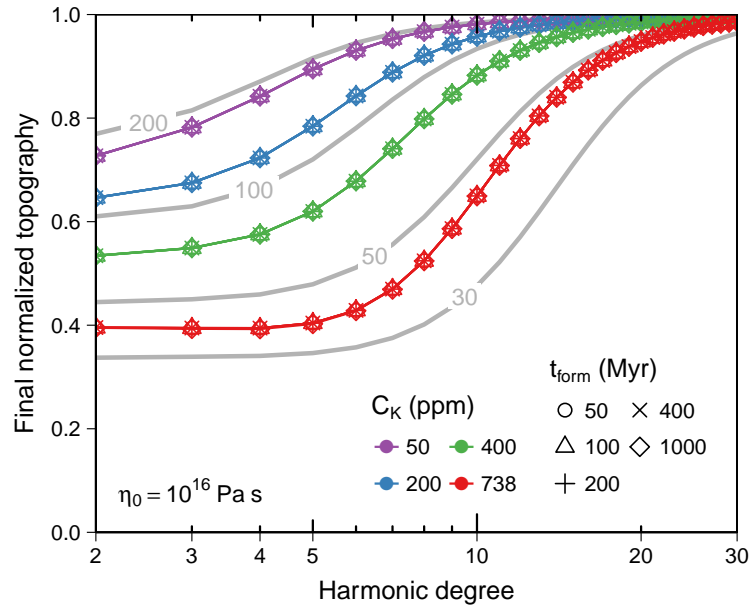


Figure 7. The normalized topography at the final state as a function of harmonic degree. Results obtained by using our 1D conduction code assuming $T_{\text{ini}} = 150$ K and $\eta_0 = 10^{16}$ Pa s are shown. Gray curves show instantaneous elastic responses assuming an elastic shell model. Numbers indicate elastic shell thicknesses (in km).

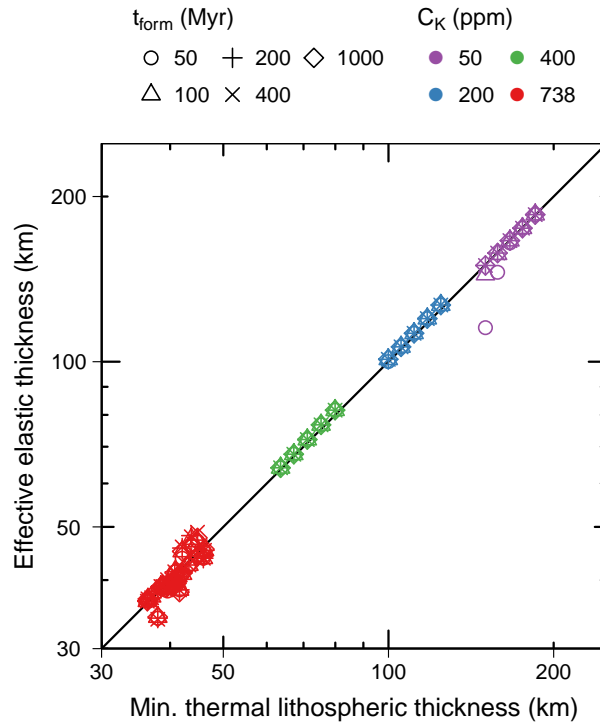


Figure 8. Effective elastic thickness as a function of the minimum thermal lithospheric thickness. The minimum thermal lithospheric thickness is obtained from thermal evolution calculations (Figure 2). The effective elastic thickness is calculated by finding the value which best matches the degree-dependent relaxation fraction (Figure 7). Results for all thermal, rheological, and basin formation age conditions are shown. Both 1D and 3D calculation results are shown. The $y = x$ line is also shown.

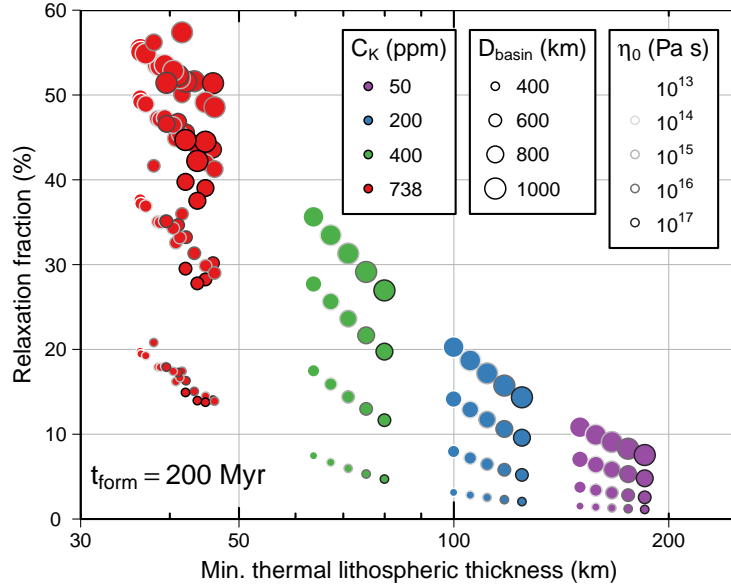


Figure 9. Present-day relaxation fraction as a function of the minimum thermal lithospheric thickness for basin diameters (D_{basin}) 400, 600, 800, and 1000 km. Results for $t_{\text{form}} = 200$ Myr are shown. Both 1D and 3D calculation results are shown.

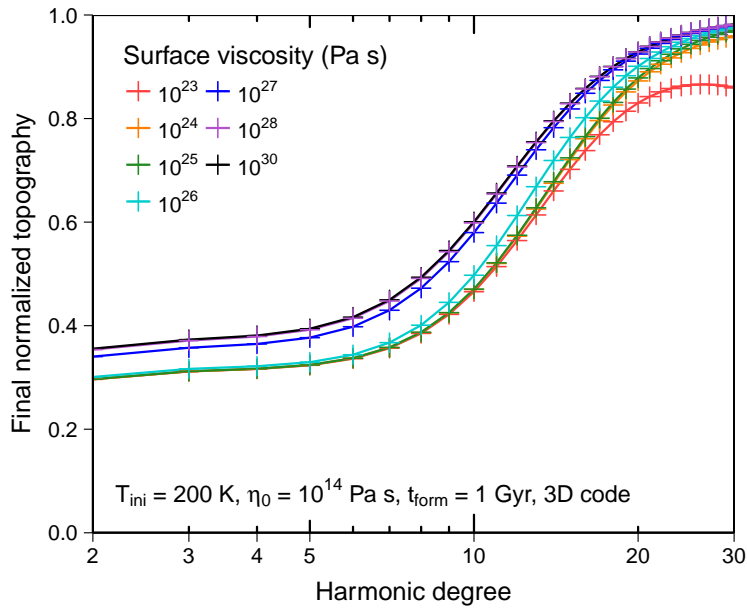


Figure 10. The effect of a weak surface layer. The viscosity of the top 10 km is fixed to 10^{23} – 10^{28} Pa s compared to the nominal surface value of 10^{30} Pa s. Calculation conditions are shown.

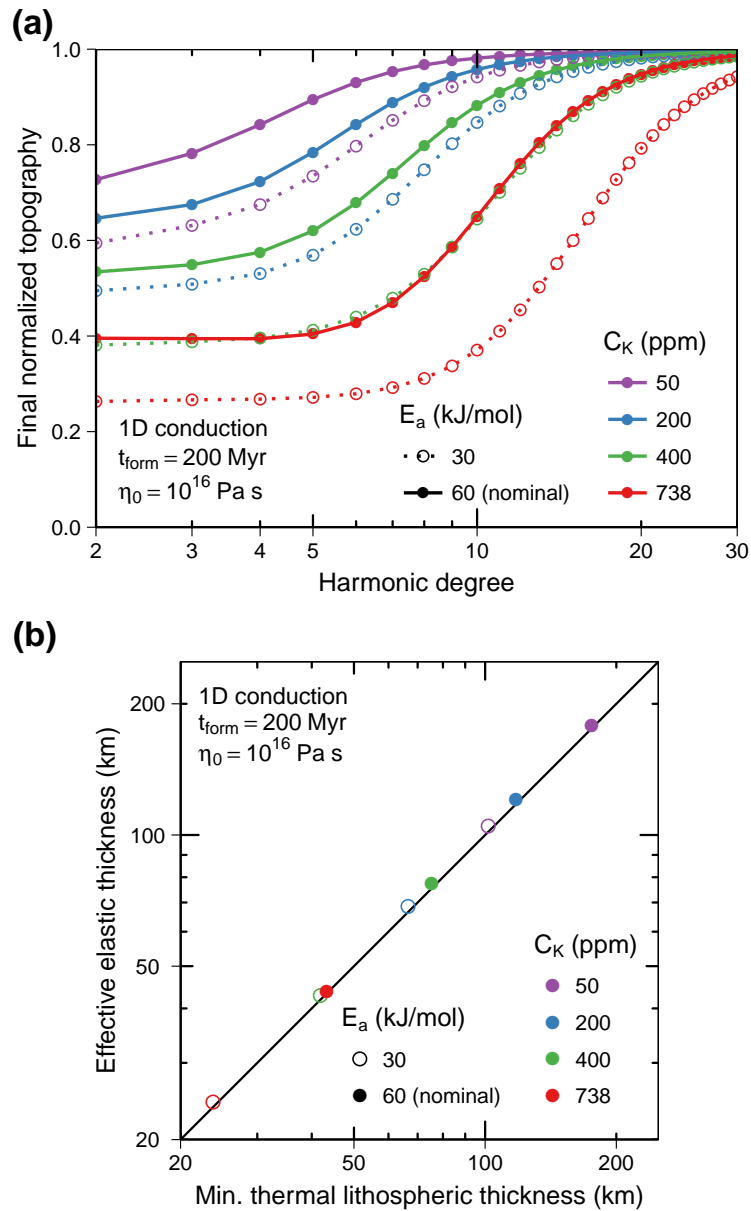


Figure 11. Effects of a weak rheology (i.e., small activation energy). Calculation conditions are shown. (a) The normalized topography at the final state as a function of harmonic degree. (b) Effective elastic thickness as a function of the minimum thermal lithospheric thickness. Although a weak rheology leads to a larger deformation for a given heat flux, the effective elastic thickness inferred from the final basin shape still corresponds well with the minimum lithospheric thickness.

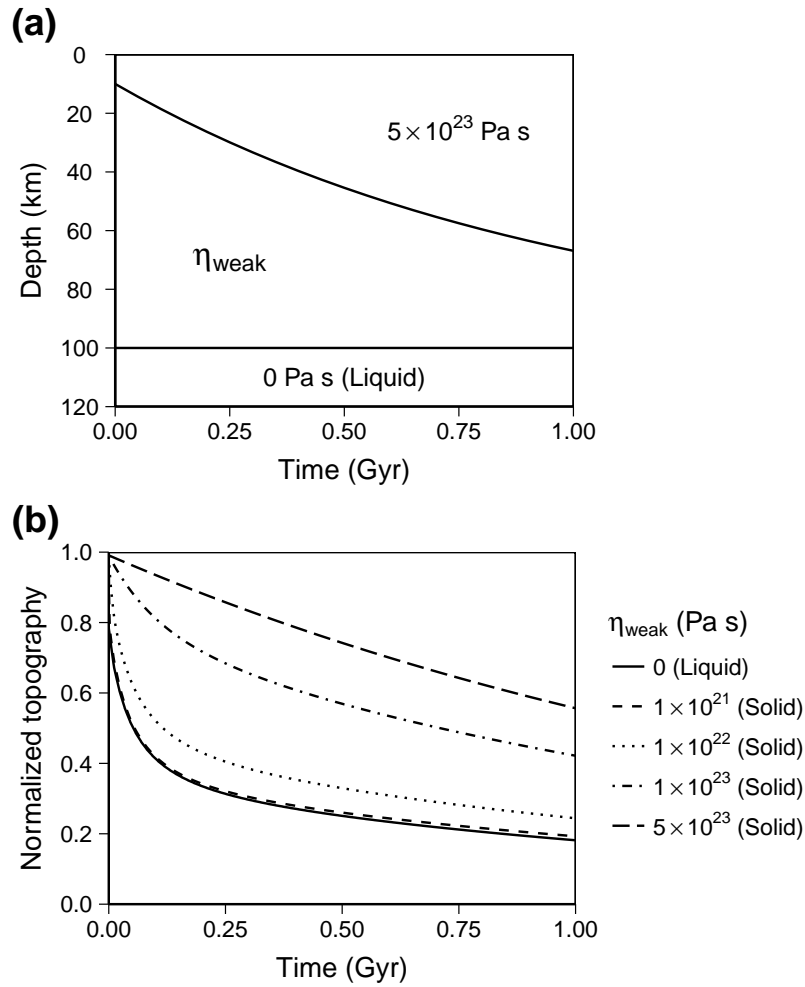


Figure A1. Validation of our code for a freezing case. (a) The viscosity profile for this examination. Only top 120 km is shown. (b) The time evolution of topography for degree 70. The “liquid” case corresponds to a situation with an inviscid layer of time-varying thickness. This freezing case coincides with a “solid” case in which the inviscid layer is approximated as a solid layer with a low viscosity η_{weak} .

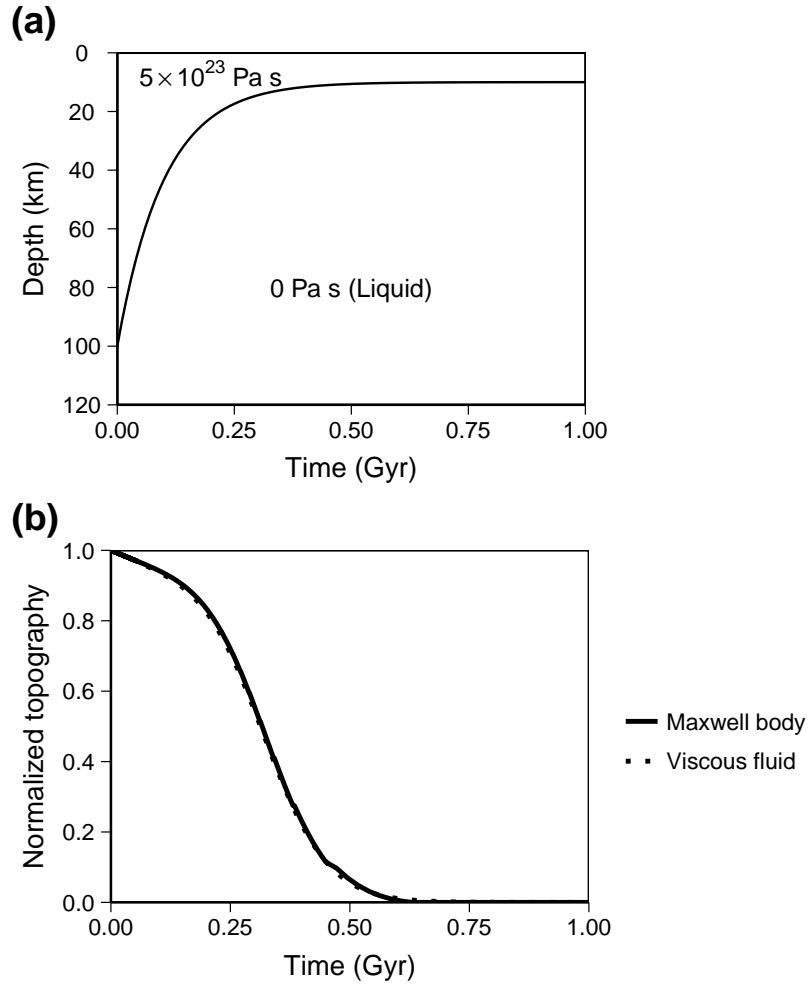


Figure A2. Validation of our code for a melting case. (a) The viscosity profile for this examination. Only top 120 km is shown. (b) The time evolution of topography. Results of our code and of a semi-analytical solution for a viscous fluid model (equation (A3)) show a good agreement.

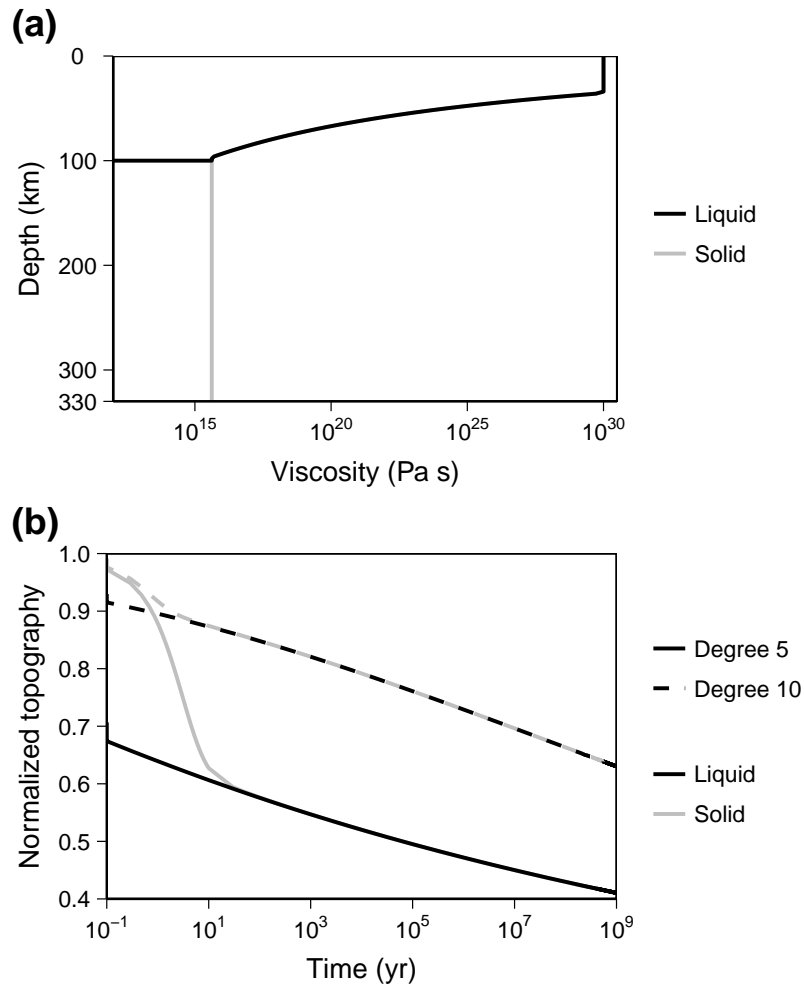


Figure A3. (a) Viscosity profiles to examine the effect of a subsurface ocean on basin relaxation. (b) The time evolution of normalized topography for different harmonic degrees. There are no significant differences in the final states between the liquid and solid cases.

Table 1. Parameters Used for Numerical Calculations

Symbol	Quantity	Value	Unit
R_p	Radius of Pluto	1180	km
R_c	Core radius	850	km
ρ_i	Density of ice	950	kg m ⁻³
ρ_w	Density of water	1000	kg m ⁻³
ρ_s	Density of silicate	3361	kg m ⁻³
μ_i	Shear modulus of ice	3.33	GPa
μ_s	Shear modulus of silicate	50	GPa
E_a	Activation energy	60	kJ mol ⁻¹
T_s	Surface temperature	40	K
T_m	Melting temperature of ice	273	K
L	Latent heat of ice	333	kJ kg ⁻¹
κ	Thermal diffusivity	1.2×10^{-6}	m ² s ⁻¹
k_i	Thermal conductivity of ice	2.25	W m ⁻¹ K ⁻¹
k_s	Thermal conductivity of silicate	4.2	W m ⁻¹ K ⁻¹
α_i	Thermal expansivity of ice	5.6×10^{-5}	K ⁻¹
α_s	Thermal expansivity of silicate	2.4×10^{-5}	K ⁻¹

Table 2. Variables Used for Numerical Calculations

Symbol	Quantity	3D	1D	Unit
η_0	Reference viscosity	10^{13} – 4.16×10^{17}	10^{13} – 10^{17}	Pa s
C_K	⁴⁰ K concentration	738	50, 200, 400, 738	ppm
T_{ini}	Initial temperature	150, 200, 250	150	K