Lawrence Berkeley National Laboratory

Recent Work

Title

TEMPERATURE DEPENDENCE OF DAMPING OF LATTICE RESONANCE IN ALKALI HALIDES

Permalink

https://escholarship.org/uc/item/5k52m9xr

Author

Harper, Charlie.

Publication Date

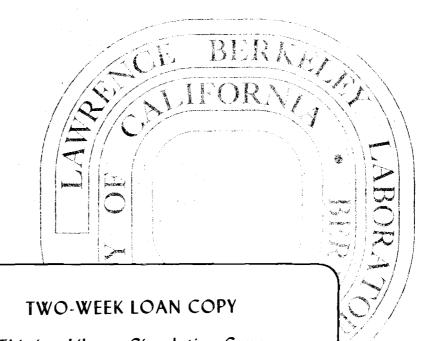
1971-07-01

TEMPERATURE DEPENDENCE OF DAMPING OF LATTICE RESONANCE IN ALKALI HALIDES

Charlie Harper

July 22, 1971

AEC Contract No. W-7405-eng-48



This is a Library Circulating Copy which may be borrowed for two weeks. For a personal retention copy, call Tech. Info. Division, Ext. 5545

() ()

DISCLAIMER

This document was prepared as an account of work sponsored by the United States Government. While this document is believed to contain correct information, neither the United States Government nor any agency thereof, nor the Regents of the University of California, nor any of their employees, makes any warranty, express or implied, or assumes any legal responsibility for the accuracy, completeness, or usefulness of any information, apparatus, product, or process disclosed, or represents that its use would not infringe privately owned rights. Reference herein to any specific commercial product, process, or service by its trade name, trademark, manufacturer, or otherwise, does not necessarily constitute or imply its endorsement, recommendation, or favoring by the United States Government or any agency thereof, or the Regents of the University of California. The views and opinions of authors expressed herein do not necessarily state or reflect those of the United States Government or any agency thereof or the Regents of the University of California.

TEMPERATURE DEPENDENCE OF DAMPING OF LATTICE RESONANCE IN ALKALI HALIDES*

Charlie Harper**

Lawrence Berkeley Laboratory University of California Berkeley, California 94720

July 22, 1971

ABSTRACT

It is shown that the explicit T^2 dependence of damping due to quartic contributions is small in comparison with the T dependence from cubic anharmonicity. A two-time Green's function method is used.

This work was supported in part by the U. S. Atomic Energy Commission.

Permanent address: California State College, Hayward - Hayward,
California 94542

The problem of explaining the temperature dependence of the damping for lattice resonance of alkali halides has received considerable attention [1]. Recently, Mooij [2] pointed out that (1) previous theoretical considerations neglected the implicit temperature dependence of thermal expansion and (2) the quartic anharmonic contributions to the damping are negligible if thermal expansion is considered.

We have derived a general expression for the complex susceptibility tensor by use of two-time Green's functions. The susceptibility is a function of the frequency shifts $\Delta(\alpha)$ and corresponding damping constant $\Gamma(\alpha)$. The usual absorption coefficient is proportional to the imaginary part of the susceptibility tensor.

It is found that the cubic anharmonic contributions give rise to T $(n \to kT)$ dependence for the damping in the classical limit, and the quartic contributions introduce an additive T^2 dependence to the damping. However, the quartic contributions are of the order $O(1/N^2)$ compared to O(1/N) for the cubic contributions.

The two-time retarded Green's functions used are defined by [3]

$$G(t,t') = -i\theta(t - t')\langle [A(t),B(t')]\rangle,$$

$$= \langle \langle A; B \rangle \rangle = G(A; B), \qquad (1)$$

where

$$\Theta(t - t') = \begin{cases} 1, t - t' > 0 \\ 0, t - t' < 0 \end{cases}$$
 (2)

and the canonical ensemble average is denoted by

$$\langle \cdots \rangle = \frac{\text{Tr}(e^{-\beta H} \cdots)}{\text{Tr}(e^{-\beta H})}; \quad \beta = \frac{1}{kT}.$$
 (3)

The operators A and B are second quantized phonon operators in the Heisenberg representation. The Hamiltonian of the isolated system is denoted by H. The equation of motion of G(t,t') is obtained by differentiating eq. (1) with respect to time. On taking the Fourier transform of this equation of motion, we obtain (in the energy representation)

$$EG(A; B)_{E} = \frac{1}{2\pi} \langle [A,B] \rangle_{E} + G([A,H]; B)_{E},$$
 (4)

where $E = \omega + i\varepsilon$ and n = 1. The frequency of the applied field is given by ω .

It is well known that the linear complex susceptibility is given by [3]

$$\chi_{uv}(\omega) = -2\pi G(M_u; M_v)_E, \qquad (5)$$

where M is the electric moment of the crystal. The directions of the applied electric field and the response are ν and μ respectively. The Hamiltonian and electric moment in terms of phonon creation and annihilation operators are [4]

$$H = H^{+} = H_{0} + H_{3} + H_{4},$$

$$= \sum_{\alpha} \omega_{\alpha} a_{\alpha}^{+} a_{\alpha} + \sum_{\alpha,\beta,\gamma} v_{\alpha,\beta,\gamma}^{(3)} A_{\alpha} A_{\beta} A_{\gamma}$$

$$+ \sum_{\alpha,\beta,\gamma,\rho} v_{\alpha,\beta,\gamma,\rho}^{(4)} A_{\alpha} A_{\beta} A_{\gamma} A_{\rho} A_{\rho},$$

$$(6)$$

and

$$M_{\mu} = N^{\frac{1}{2}} \sum_{\substack{o \ (2\omega_{o})^{\frac{1}{2}}}} M_{\mu} (0), \qquad (7)$$

where $A_{\alpha} = a_{-\alpha}^{+} + a_{\alpha}$ and $A_{0} = a_{0}^{+} + a_{0}$. The indices α , β , γ , and β represent both the wave vector k and polarization index j. For example, $\alpha = kj$ and $\beta = k'j'$. The expansion coefficients in eqs. (6) and (7) are discussed by Born and Huang [5].

On substituting eq. (7) into eq. (5), we obtain

$$\chi_{\mu\nu}^{(\omega)} = -2\pi \frac{N}{2} \sum_{\substack{0,0' \\ 0 \neq 0}} \frac{M_{\mu}(0) M_{\nu}(0')}{(\omega_{0}\omega_{0}')^{\frac{1}{2}}} [G^{\perp} + G^{2}], \qquad (8)$$

where

$$G^{1} = G(a_{\underline{O}}^{+}; A_{\underline{O}}^{\prime})_{\underline{E}}$$
 (9)

and

$$G^2 = G(a_0; A_0')_E. \qquad (10)$$

The scheme for solving the system of dependent equations is

$$G(1; \cdots) \rightarrow (constant)_1 + f_1(\omega) G(1; \cdots) + g_2(2; \cdots) + g_3(3; \cdots),$$

$$(11)$$

$$g_2(2; \cdots) \rightarrow (constant)_2 + f_2(\omega) g_2(2; \cdots)$$

$$\begin{array}{ccc}
+ \Gamma_{3}(3; \cdots) + \Gamma_{4}(4; \cdots), & (12) \\
\downarrow \leftarrow \text{decoupling} \rightarrow \downarrow \\
\gamma^{(3)}(E,n) G(1; \cdots) + \xi^{(1)}(n) g_{2}(2; \cdots)
\end{array}$$

$$g_3(3; \cdots) \rightarrow (constant)_3 + f_3(\omega) g_3(3; \cdots)$$

where $g_2(2; \cdots)$ and $g_3(3; \cdots)$ are higher-order Green's functions[2]. The numbers on the left of the semicolons in the Green's functions indicate the number of phonon operators present. The second, third, and fourth terms in each of the equations represent contributions from H_0 , H_3 , and H_4 respectively. The functions $\gamma^{(3)}(E,n)$ and $\gamma^{(4)}(E,n^2)$ are the cubic and quartic contributions to the damping; they give rise to T and T^2 dependence of the damping constant. However, the T dependence is O(1/N) and the T^2 dependence is $O(1/N^2)$. The decoupling scheme is as follows

$$g_{3}^{1}(a_{-\alpha}^{+} a_{\beta}^{+} a_{-\gamma}^{+}; A_{0}^{+}) \approx [n_{\beta}^{+} \delta_{-\alpha}, \beta_{\beta}^{+} \delta_{-\gamma}, 0] + (n_{\beta}^{+} + 1) \delta_{\beta}^{+}, -\gamma \delta_{-\alpha}, 0] G^{1},$$

$$(14)$$

where off-diagonal terms are neglected and n... is the usual average boson occupation number. A similar procedure is used to decouple the $\Gamma_5(5;\cdots)$ Green's functions giving rise to n^2 (or T^2) dependence in the classical limit.

The details of this work will be presented elsewhere.

REFERENCES

- For example, see I. P. Ipatova, A. A. Maradudin, and R. F. Wallis, Phys. Rev. 155 (1967) 882.
- 2. J. E. Mooij, Phys. Letters 29A (1969) 111.
- D. N. Zubarev, Usp. Fiz. Nauk. 71 (1960) 71 [translation, Soviet Phys. - Usp. 3 (1960) 320].
- V. N. Kashcheev, Fiz. Tverd. Tela 5 (1963) 2339 [translation Soviet Phys. -Solid State 5 (1963) 1700].
- 5. M. Born and K. Huang, <u>Dynamical Theory of Crystal Lattices</u> (Oxford University Press, New York, 1954).

LEGAL NOTICE

This report was prepared as an account of work sponsored by the United States Government. Neither the United States nor the United States Atomic Energy Commission, nor any of their employees, nor any of their contractors, subcontractors, or their employees, makes any warranty, express or implied, or assumes any legal liability or responsibility for the accuracy, completeness or usefulness of any information, apparatus, product or process disclosed, or represents that its use would not infringe privately owned rights.

TECHNICAL INFORMATION DIVISION LAWRENCE BERKELEY LABORATORY UNIVERSITY OF CALIFORNIA BERKELEY, CALIFORNIA 94720