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Negative magnetoresistance due to conductivity fluctuations in films of the topological semimetal Cd₃As₂

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Recently discovered Dirac and Weyl semimetals display unusual magnetoresistance phenomena, including a large, nonsaturating, linear transverse magnetoresistance and a negative longitudinal magnetoresistance. The latter is often considered as evidence of fermions that have a defined chirality. Classical mechanisms, due to disorder or nonuniform current injection, can, however, also produce negative longitudinal magnetoresistance. Here, we report on magnetotransport measurements performed on epitaxial thin films of Cd_3As_2 , a three-dimensional Dirac semimetal. Quasilinear positive transverse magnetoresistance and negative longitudinal magnetoresistance are observed. By evaluating films of different thickness and by correlating the temperature dependence of the carrier density and mobility with the magnetoresistance characteristics, we demonstrate that both the quasilinear positive and the negative magnetoresistance are caused by conductivity fluctuations. Chiral anomaly is not needed to explain the observed features.

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Recent experimental realizations of three-dimensional topological semimetals have opened up numerous exciting opportunities to test quasiparticle behavior that mimics massless, relativistic Dirac or Weyl fermions. A signature of Weyl fermions is the "chiral anomaly", when charge flows from one Weyl node to one of opposite chirality under parallel electric and magnetic fields, thereby giving rise to an unusual negative longitudinal magnetoresistance (MR) [1,2]. In Dirac semimetals the Dirac nodes split into Weyl nodes in the magnetic field and similar physics is expected. Recent observations [3–9] of longitudinal negative MR in Dirac and Weyl semimetals have therefore generated significant attention. While most studies consider the negative longitudinal MR to be evidence of the chiral anomaly, current jetting has been proposed as an alternative explanation [10,11]. Current jetting arises under inhomogeneous current injection into high-mobility materials that have a large conductivity anisotropy [12]. It leads to a strong preference of the current to flow in the direction of the magnetic field, resulting in a negative longitudinal MR [12]. Other studies claim to have ruled out current jetting caused by nonuniform current injection [7]. Negative longitudinal MR can also be due to conductivity fluctuations and has been reported for disordered semiconductors [13,14]. A recent study [15] showed that mobility fluctuations are a likely origin of linear, positive transverse MR in Cd₃As₂, a three-dimensional Dirac semimetal [16–20].

Most studies that attribute the negative longitudinal MR to chiral anomaly have been carried out on bulk materials. Thin films offer several important advantages towards resolving the origin of the negative longitudinal MR in Dirac and Weyl semimetals. In particular, thin-film-device geometries are much less susceptible to current jetting. Furthermore, the effects of nonuniformities can be studied by varying the film thickness and growth conditions. In this work, we study the magnetotransport properties of epitaxial Cd_3As_2 thin films.

We show that both the transverse positive MR and the negative longitudinal MR are due to conductivity fluctuations.

Cd₃As₂ films were grown by molecular beam epitaxy on relaxed, 180-nm-thick GaSb buffer layers on GaAs (111)B substrates (1° miscut towards the [112] direction), as described elsewhere [21]. The beam equivalent pressure was 2×10^{-6} Torr, the substrate temperatures ranged between 150 °C and 170 °C, and the growth time was between 5 min and 60 min (see Table I). Surface morphologies were investigated by optical, atomic force, and scanning electron microscopies. The film's structure and alignment with the substrate were probed by x-ray diffraction (XRD) using Cu $K\alpha$ radiation. The films were patterned into Hall bar structures with widths and lengths of 100 μ m using standard optical lithography and Ar⁺ ion milling. The thicknesses of the Cd₃As₂ layers were determined by scanning electron microscopy of the patterned Hall bar structures. Magnetoresistance measurements were carried out in a Quantum Design Dynacool PPMS, at temperatures between 300 K and 2 K and magnetic fields up to 9 T. DC excitation currents of $10 \,\mu\text{A}$ were used in all measurements. Shubnikov-de Haas oscillations were detected in the thinnest films (See Fig. S1 in the Supplemental Material [22]).

Representative optical and atomic force micrographs of a Cd₃As₂ film are shown in Figs. 1(a) and 1(b). In most areas, the film is smooth with atomically stepped surfaces [Fig. 1(b)]. The step height (\sim 4 Å) matches the interplanar spacing of the Cd₃As₂ (112) planes, which form the surface [21]. The defects in the optical micrograph [Fig. 1(a)] are likely areas that grew in a three-dimensional (island) growth mode. Their density was about 10^3-10^4 cm⁻². Out-of-plane XRD confirmed single-phase, epitaxial Cd₃As₂ [Fig. 1(c)]. High-resolution XRD showed Laue fringes from the GaSb buffer layer and for the thinnest Cd₃As₂ layers [arrows in Fig. 1(d)]. The three-dimensional carrier densities determined from low-field Hall measurements were similar for all films grown at 150 $^{\circ}$ C (see Table I) and ranged from \sim (0.8–1.8) \times $10^{17} \,\mathrm{cm}^{-3}$ at 2 K to $(5.0-8.0) \times 10^{17} \,\mathrm{cm}^{-3}$ at 300 K. These carrier densities are lower than those of single crystals reported in the literature (typically $> 10^{18}$ cm⁻³ [15,17,23]), indicating

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TABLE I. Sample parameters of the Cd₃As₂ thin films. n_{2D} is the sheet carrier density, n_{3D} the three-dimensional carrier density, and μ is the Hall mobility.

	Growth temperature	Growth time (min)	Film thickness (nm)	$n_{\rm 2D}(10^{12}{\rm cm}^{-2})$		$n_{\rm 3D} (10^{17} {\rm cm}^{-3})$		$\mu (\mathrm{cm^2/V s})$	
				2 K	300 K	2 K	300 K	2 K	300 K
o10	150 °C	5	85	1.46	4.25	1.7	5.0	6700	4550
o12	150 °C	10	120	2.17	7.42	1.8	6.2	7900	6400
o19	150 °C	20	170	1.43	13.6	0.8	8.0	5250	8950
o21	150 °C	40	340	3.76	24.1	1.1	7.1	11250	11950
o22	170°C	60	370	13.0	52.5	3.5	14.2	13650	12050

that the Fermi level is lower (i.e., closer to the Dirac node). The carrier density of the film grown at 170 °C was slightly higher, $\sim 3.5 \times 10^{17} \, \mathrm{cm}^{-3}$ at 2 K (14.2 \times 10¹⁷ cm⁻³ at 300 K). The phase diagram for Cd₃As₂ shows a line compound that opens up to a phase field towards the Cd-rich side, i.e., Cd₃As_{2-\delta}, at higher temperatures [24]. This leads to higher concentrations of As vacancies, which are the source of unintentional *n*-type doping in Cd₃As₂ [25]. The Hall mobility (Table I) increased with film thickness either due to a reduction in scattering from

the interface with the buffer layer or annihilation of extended defects with increasing thickness.

Figure 2 shows the transverse (magnetic field **B** perpendicular to the electric field **E**) and longitudinal (**B** parallel to **E**) MR of the different samples, measured at 2 K. For **B** normal to the film plane [Fig. 2(a)], a positive, quasilinear, nonsaturating MR is observed, similar to many other Dirac and Weyl semimetals. A linear MR in Cd_3As_2 has been attributed to the lifting of the protection from backscattering under an applied magnetic field

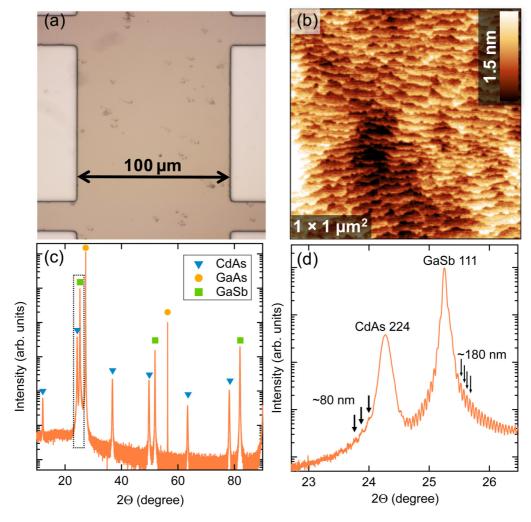


FIG. 1. (a) Optical micrograph of a Cd_3As_2 film patterned into a Hall bar. (b) Atomic force micrograph of the film surface. (c,d) XRD scans of a $Cd_3As_2/GaSb/GaAs$ heterostructure. The arrows in (d) indicate the Laue fringes.

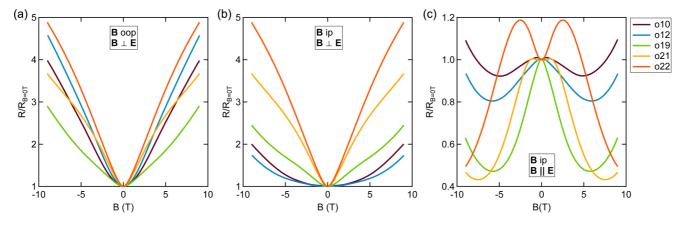


FIG. 2. (a,b) Transverse (**B** perpendicular to **E**) magnetoresistance and (c) longitudinal (**B** in the plane and parallel to **E**) magnetoresistance obtained from different samples and measured at 2 K. The labels in (a,b) indicate the orientation of **B**: oop = out of plane and ip = in plane. The samples are labeled in order of increasing thickness from sample o10 (85 nm) to o22 (370 nm); see Table I.

[23,26] or due to the quantum magnetoresistance [27]. The latter condition (all electrons in the lowest Landau level) is not fulfilled here. Charge density and/or mobility fluctuations can also cause linear, nonsaturating MR [14,28-31]. In an inhomogeneous material, the direction of travel of the charge carriers deviates from the direction of the applied field, leading to a velocity component perpendicular to both **B** and **E**. A Hall signal is superimposed, leading to a contribution linear in **B**. Measurements with **B** in the film plane and perpendicular to the current are shown in Fig. 2(b). For thicker films, a positive, quasilinear MR is observed. In contrast, for the thinner samples (<170 nm), the magnitude of the positive MR is reduced and resembles classical, $\sim B^2$ behavior. With **B** in the film plane, carriers would need to travel along the film normal to generate a Hall contribution. In thin films, confinement makes this path unavailable and the linear contribution to the MR vanishes. Thus the film thickness dependence is a clear indication that the quasilinear, positive transverse MR arises from a classical mechanism, in accordance with the conclusions in Ref. [15], and is not a phenomenon reflecting the peculiar properties of Dirac fermions.

Negative longitudinal MR is observed in all samples [Fig. 2(c)], followed by a positive MR at high **B**. Additionally, positive MR is observed in thicker films at low B. These features are strikingly similar to those reported for bulk, thin-film, and nanowire Cd₃As₂ [6,32-34], as well as other Dirac and Weyl semimetals [4,5,7,8]. We also measured much thicker films, which have higher mobilities (see Ref. [21]) and which also showed qualitatively similar behavior. We first discuss the positive longitudinal MR component. While a weak positive low-field MR in Cd₃As₂ can be attributed to weak antilocalization [8,32,35], the correction to the conductance is too strong and the temperature dependence too weak for weak localization (see [22]). A longitudinal positive MR of Cd₃As₂ has previously been observed and attributed to the two elliptical Fermi surfaces centered at the Dirac nodes, which are displaced away from the zone center [36]. This seems a reasonable explanation for the positive MR component observed here, which is varies as B^2 (see below).

We next address the strong negative component of the longitudinal MR. In thin film experiments the current is

injected by large-area ohmic contacts away from the measured Hall bar structures (>200 μ m; see Fig. S4 in the Supplemental Material [22]), so geometric current jetting, see Ref. [10], is likely not the origin of the negative longitudinal MR. To further exclude geometrical current jetting, additional measurements with completely straight Hall bars were conducted, which show similar behavior (see Fig. S5 [22]). To gain further insights, we use the following generic equation to describe the longitudinal conductivity at different temperatures:

$$\sigma(B) = \sigma_0 + S_p B^2 + \frac{1}{R_n + A_n B^2}.$$
 (1)

Equation (1) contains two terms that are quadratic in B, with one leading to a negative MR or positive magnetoconductance (S_p) and the other to a positive MR (consistent with prior observations [36], see above) or negative magnetoconductance $(R_n \text{ and } A_n)$. Similar equations have been used to describe Dirac and Weyl semimetals in the literature [4,5,35], because theory predicts that the magnetoconductance due to the chiral anomaly in the classical (not quantum) regime is $\sim B^2$ [2]. Here, we use Eq. (1) because it adequately describes the magnetoconductance between 2 and 300 K [see Fig. 3(a)] with a minimum number of terms. This allows us to evaluate the relative strengths of the positive and negative contributions as a function of temperature. Figures 3(c) and 3(d) show the extracted fit parameters as a function of temperature. S_p increases with temperature, reaching a peak value at \sim 100 K, and subsequently decreases. In contrast, R_n and A_n first decrease with increasing temperature, reaching a minimum at \sim 100 K, and then increase.

Crucially, the MR behavior can be compared with the temperature behavior of charge carrier densities and mobilities [Fig. 3(b)]. The results in Fig. 3(b) were obtained by fitting the Hall resistance, $R_{xy}(B)$, which was nonlinear at high **B**, to the standard two-carrier Drude equation [22,37]. The zero-field longitudinal resistance was set to $R_{xx}(0-T) = (n_1e)^{-1} + (n_2e)^{-1}$, where n_1 and n_2 are the carrier densities and e the elementary charge. The transverse magnetoresistance with **B** out of plane cannot be fit to the standard two-carrier model as the linear component (discussed above) is not described

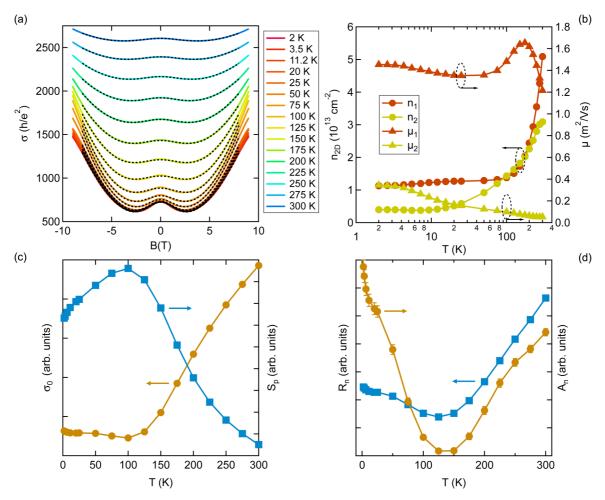


FIG. 3. (a) Longitudinal conductivity for the Cd_3As_2 film grown at $170\,^{\circ}C$ for 60 min (sample number o22) as a function of temperature. The dotted lines are fits to the data, using Eq. (1), with the results shown in (c,d). (b) Carrier density and mobility extracted by fitting the Hall data to 9 T to a standard two-carrier equation.

by it. Both carriers are n-type. Carrier 1 has higher mobility ($\sim 1.2 \,\mathrm{m^2/V}\,\mathrm{s}$ at 300 K and $\sim 1.45 \,\mathrm{m^2/V}\,\mathrm{s}$ at 2 K) and densities ($5 \times 10^{13} \,\mathrm{cm^{-2}}$ at 300 K and $1.1 \times 10^{13} \,\mathrm{cm^{-2}}$ at 2 K) than carrier 2. The presence of two carrier types is consistent with the electronic structure of $\mathrm{Cd_3As_2}$, which exhibits a conduction band valley at the zone center that is only slightly higher in energy than the Dirac nodes [16,19].

Most importantly, the temperature dependence of the carrier densities exhibits a crossover behavior. The carrier densities are nearly independent of temperature at low temperatures but increase with temperature above $\sim 100 \, \text{K}$. The density of carrier 1 in particular shows a steep increase. The crossover coincides with the maximum of S_p . This correlation supports the notion that the negative longitudinal MR is caused by conductivity fluctuations. In particular, spatial fluctuations in the carrier density and/or mobility can lead to inhomogeneous equipotential lines and a negative longitudinal MR [13,38]. Conductivity fluctuations result in current paths that are not parallel to the applied electric field and thus are similar to current jetting. The effects of conductivity fluctuations are strongest in crossover regimes, such as around 100 K, where inhomogeneities lead to large relative mobility/charge carrier density differences [13]. At lower temperatures, as well as at higher temperatures, carrier 1 dominates the transport, leading to reduced relative conductivity fluctuations and therefore reduced positive magnetoconductance (negative MR). The films contain twin defects [21] and likely also As vacancies, which may form clusters [20]. The importance of the latter is corroborated by the fact that the negative longitudinal MR is strongest in the film grown at higher temperatures, which possesses the highest carrier density and hence As vacancy concentration. Simulations of the longitudinal MR due to conductivity fluctuations have been carried out for simple model geometries in the literature [31,38], confirming that they are a cause of negative longitudinal MR. They lead to results that are remarkably similar to those observed here [38]. Quantitative simulation of the MR for the films would require a detailed model of the spatial distribution and nature of the inhomogeneities. Interestingly, other topological Dirac materials for which the negative longitudinal MR has been observed also show a strongly temperature-dependent Hall coefficient (carrier density) [5]. Further studies are clearly needed to understand the temperature-dependent carrier densities and mobilities in all of these materials. The thickness dependence of the longitudinal negative MR further corroborates the interpretation that it is due to conductivity fluctuations. Like the positive linear transverse magnetoresistance, it is less pronounced in thinner films [see Fig. 2(c)]. Current distortions require a path normal to the film thickness, which gets increasingly cut off in thinner films [38].

To summarize, the magnetotransport properties of Cd_3As_2 thin films are remarkably similar to those found in other Dirac and Weyl semimetals, exhibiting both a positive linear transverse MR and the negative longitudinal MR. The film thickness dependence and the correlation with a crossover in the temperature dependence of the carrier density establish that the negative longitudinal MR is due to charge carrier density and/or mobility fluctuations causing distortions in the current paths. Although the results do not rule out the possibility of observing the chiral anomaly in magnetoresistance

measurements, they clearly show that the chiral anomaly does not need to be invoked to explain any of the observed features. Geometrical avoidance of current jetting is not sufficient evidence that the negative longitudinal MR is due to the chiral anomaly, if the material contains disorder.

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