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An optimization algorithm for dose reduction with fluence-modulated proton CT

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Abstract

Purpose: Fluence-modulated proton computed tomography (FMpCT) using pencil
 beam scanning aims at achieving task-specific image noise distributions by modulating
 the imaging proton fluence spot-by-spot based on an object-specific noise model. In
 this work we present a method for fluence field optimization and investigate its performance in dose reduction for various phantoms and image variance targets.

Methods: The proposed method uses Monte Carlo simulations of a proton CT (pCT) 27 prototype scanner to estimate expected variance levels at uniform fluence. Using an 28 iterative approach, we calculate a stack of target variance projections that are required 29 to achieve the prescribed image variance, assuming a reconstruction using filtered back-30 projection. By fitting a pencil beam model to the ratio of uniform fluence variance 31 and target variance, relative weights for each pencil beam can be calculated. The 32 quality of the resulting fluence modulations is evaluated by scoring imaging doses and 33 comparing them to those at uniform fluence, as well as evaluating conformity of the 34 achieved variance with the prescription. For three different phantoms, we prescribed 35 constant image variance as well as two regions-of-interest (ROI) imaging tasks with 36 inhomogeneous image variance. The shape of the ROIs followed typical beam profiles 37 for proton therapy. 38

Results: Prescription of constant image variance resulted in a dose reduction of 8.9 %
 for a homogeneous water phantom compared to a uniform fluence scan at equal peak

variance level. For a more heterogeneous head phantom, dose reduction increased to 41 16.0% for the same task. Prescribing two different ROIs resulted in dose reductions 42 between 25.7% and 40.5% outside of the ROI at equal peak variance levels inside the 43 ROI. Imaging doses inside the ROI were increased by 9.2% to 19.2% compared to the 44 uniform fluence scan, but can be neglected assuming that the ROI agrees with the 45 therapeutic dose region. Agreement of resulting variance maps with the prescriptions 46 was satisfactory. 47 Conclusions: We developed a method for fluence field optimization based on a noise 48

⁴⁸ **Conclusions:** We developed a method for nuelice held optimization based on a holse ⁴⁹ model for a real scanner used in proton computed tomography. We demonstrated that ⁵⁰ it can achieve prescribed image variance targets. A uniform fluence field was shown ⁵¹ not to be dose optimal and dose reductions achievable with the proposed method for ⁵² fluence-modulated proton CT were considerable, opening an interesting perspective

⁵³ for image guidance and adaptive therapy.

Keywords: proton CT, fluence field optimization, proton therapy, dose reduction, fluence modulated proton CT

56 I. Introduction

Cancer treatment using intensity-modulated proton and heavier ion therapy is effective, 57 and comes at a low risk of side-effects for the patient compared to conventional treatment 58 modalities using x-rays. The good tolerance is believed to be linked to the low dose to 59 normal tissue when using protons for treatment.¹⁻⁴ At the same time, low-dose, frequent 60 and accurate imaging, ideally at the treatment site, is required to ensure a safe delivery 61 of the therapeutic doses.^{5,6} Proton therapy treatment planning requires a spatial map of 62 the relative (to water) stopping power (RSP), which in current clinical practice is acquired 63 through a conversion from x-ray CT images.⁷⁻⁹ X-ray CT images are typically not acquired 64 in treatment position and not prior to every treatment fraction, in order to keep treatment 65 time short and imaging dose low enough that they do not compromise the dose benefit of 66 proton therapy.¹⁰ Direct imaging of RSP using proton computed tomography $(pCT)^{11-16}$ 67 has been proposed to increase accuracy and to allow for a frequent, dose efficient acquisition 68 in treatment position. Accuracies achievable with current prototypes are comparable to 69 state-of-the art clinical dual energy x-ray CT.^{7,17-19} 70

A further reduction of imaging dose can be achieved by modulating the imaging fluence 71 field during the acquisition and thereby achieving a task-specific image quality. Fluence-72 modulated scans²⁰ can either aim for homogeneous variance across the whole volume, or for 73 region-of-interest imaging, where only the relevant part of the image is acquired at low noise 74 and imaging dose is reduced elsewhere. Algorithms $^{21-24}$ and experimental prototypes $^{25-29}$ 75 have been developed for fluence modulation in x-ray CT. Recently, fluence-modulated pCT 76 (FMpCT) has also been proposed³⁰ and its initial experimental feasibility using pencil beam 77 scanning was investigated.³¹ The best achievable dose efficiency through fluence modulation 78 or other techniques is a key requirement for x-ray CT³² and most likely will be for pCT as 79 it moves closer to the clinics. Moreover, region-of-interest imaging is of high interest for 80 particle therapy treatment planning and dose verification, where only a fraction of the image 81 volume (the treatment beam path) is of relevance.³⁰ A challenge for FMpCT is that simple 82 Poisson noise modeling is not sufficient, as image variance for pCT depends on the object's 83 heterogeneity, and several contributions, including multiple Coulomb scattering, have to be 84 taken into account for fluence-modulation.^{33,34} 85

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In this work, we present a method for fluence–field optimization in pCT using pencil

beam scanning. We employ a pCT scanner–specific Monte Carlo simulation,³⁵ which was 87 shown to reproduce experimental variance levels for a typical fluence field.³⁴ The problem 88 of finding relative modulation factors for each pencil beam such that the summed fluence 89 pattern results in a prescribed image variance map is a computationally expensive optimiza-90 tion problem which generally requires alternating between the reconstructed image domain 91 (where the variance prescription is defined) and the projection domain (the detector data at 92 each projection angle from which the image is reconstructed, and where the fluence modu-93 lation is defined). Therefore we separated the problem into first solving for the projection 94 domain variance yielding a given prescribed variance in the image domain and subsequently 95 optimizing pencil beam weights leading to this projection domain variance. To realistically 96 describe pencil beams in the optimization and in simulations, we established a pencil beam 97 model based on experimental data. In a simulation study, we estimated dose savings for 98 fluence-modulated pCT using three different phantoms, and compared our proposed solu-99 tion with a straightforward intersection-based fluence modulation.³¹ We also verified that 100 the resulting variance map approaches the target variance. Both a constant variance tar-101 get as well as two regions-of-interest (ROI) following typical treatment beam paths were 102 investigated. 103

¹⁰⁴ II. Materials and methods

105 II.A. Simulation framework

The Monte Carlo simulation framework³⁵ used in this study is a detailed model of the phase II 106 pCT prototype scanner.¹³ It is based on the GEANT4 toolkit³⁶ version 10.2.p01. Details 107 about the modeling of physics processes can be found in literature, where the platform was 108 validated for its fidelity in terms of RSP.^{19,35} A previous study³⁴ improved the platform 109 for reproducing variance levels of experimental scans. With respect to that work, the beam 110 model was modified, and is described below. Imaging doses, in the form of absorbed physical 111 dose, were scored on a centered grid of $125 \times 125 \times 35$ voxels with a uniform voxel size of 112 2 mm and summed for all projection angles. 113

The simulation framework outputs data in the same format as the prototype scanner. It records position and direction information of individual protons before and after the object, as well as the proton's residual energy. Using a calibration,³⁷ the residual energy can be mapped to a water-equivalent path length (WEPL), which is the line integral over the RSP of the object along the curved path of the proton. Because measurements are available for every detected proton, these data are referred to as "list-mode."

¹²⁰ II.B. Image reconstruction

To reconstruct RSP images from the list–mode data, a most likely path³⁸ is estimated for 121 every proton from the tracking information. The path information is taken into account by 122 performing distance-driven binning and applying a special cone-beam filtered backprojec-123 tion algorithm.³⁹ In total, 90 projections from rotation angles covering a full rotation were 124 used. This relatively low number of projections was chosen to satisfy experimental timing 125 constraints and to allow for a future experimental validation of this work. Reconstructions 126 were performed on a grid of $250 \times 250 \times 70$ voxels with a uniform size of 1 mm. For performing 127 data cuts, 12,38,39 the grid was 125×125 pixels with a uniform size of 2 mm. Binning of data 128 into distance–driven projections was performed on a grid of $250 \times 250 \times 70$ voxels with a 129 uniform size of 1 mm. All grids were centered on the isocenter. 130

Assume a voxel centered in (u, v, d) in the three-dimensional distance-driven projection, 131 where d is the binning depth and u and v are the coordinates normal to it. We can identify a 132 set of protons such that the most likely path of every proton crosses the voxel volume around 133 (u, v, d). The number of protons in that set is then referred to as the "counts" C(u, v, d). 134 These counts only consider protons used for image reconstruction and therefore are reduced 135 compared to the incident protons due to interactions with the object and cuts on the data. 136 In contrast to that, counts in the absence of interactions and cuts are referred to as F(u, v, d)137 throughout the paper. The point u = v = d = 0 is the location of the isocenter, where the 138 rotation axis is located. 139

¹⁴⁰ II.C. Phantoms

In the simulation study, three different phantoms with a physical counterpart were used. The water phantom is a cylindrical container made from polystyrene (outer diameter 150.5 mm, wall thickness 6.35 mm) and filled with distilled water. The CTP404 phantom (*Phantom* Laboratory, New York, USA) is a commercial sensitometric phantom with a cylindrical shape (diameter 150 mm) and several tissue-equivalent inserts and two cylinders filled with air. Both phantoms were implemented in the simulation as analytical models. The pediatric head phantom (ATOM[®], Model 715 HN, *CIRS Inc.*, Norfolk, USA) models the anatomy of a 5-year-old child and was implemented as a voxelized phantom in the simulation.⁴⁰ Previous publications^{34,35,40} can be consulted for details about the phantoms.

¹⁵⁰ II.D. Gaussian pencil beam model

To allow for the flexible simulation of FMpCT data, an analytical pencil beam model was derived from experimental tracking data acquired at the pencil beam scanning beamline of the Northwestern Medicine Chicago Proton Center without phantom. Using the timing information of the scanner, a count rate was calculated in steps of 0.8 ms, allowing for the separation of individual pencil beams as the count rate dropped in between two spots. The separated data were processed individually by estimating most likely paths and performing distance-driven binning.³⁹

For each pencil beam b, this resulted in a three-dimensional experimental counts map $C_b(u, v, d)$. We fitted the Gaussian model

160
$$G(u, v, d) = \frac{N_0}{2\pi\sigma'_u\sigma'_v} \cdot \exp\left(-\frac{(u - u'_0(d))^2}{2\sigma''_u} - \frac{(v - v'_0(d))^2}{2\sigma''_v}\right)$$
(1)

to each pencil beam's C_b , where N_0 is the total number of protons per pencil beam, and 161 $(u'_0(d), v'_0(d))$ is the pencil beam center at depth d. The pencil beam center is assumed 162 to diverge linearly with the binning depth, such that $u'_0(d) = u_0 \cdot (1 + \delta_u \cdot d)$ and $v'_0(d)$ 163 analogously, where (u_0, v_0) is the pencil beam center at d = 0 and δ_u and δ_v are the linear 164 divergence factors. By construction, the isocenter-beam for $u_0 = v_0 = 0$ is parallel to the 165 *d*-axis. The $\sigma'_u = \sigma_u \cdot \sqrt{1 + \delta_u^2 u_0^2}$ and σ'_v analogously are the beam widths projected to a 166 plane normal to the d-axis while σ_u and σ_v are the actual beam widths. This resulted in 167 a fit with seven open parameters $(N_0, u_0, v_0, \sigma_u, \sigma_v, \delta_u, \delta_v)$, which was performed for each 168 individual pencil beam by minimization of the squared deviation. The parameters $\sigma_u, \sigma_v, \delta_u$ 169 and δ_v were not specific to one pencil beam, and estimates for them were therefore found as 170 the mean value over all pencil beams. N_0 , v_0 and u_0 were open parameters specific to a given 171 pencil beam, but overwritten in subsequent simulations of different pencil beam patterns. 172

II.. MATERIALS AND METHODS

¹⁷³ They are therefore not reported.

¹⁷⁴ II.D.1. Simulation of pencil beams

All datasets were generated by shooting a regular grid of simulated proton pencil beams. 175 At d = 0, neighboring pencil beams were interspaced by $\Delta_{\text{PB},u} = 12 \text{ mm}$ along u and 176 $\Delta_{\text{PB},v} = 8 \,\text{mm}$ along v. The pencil beam grid was offset in u by $\Delta_{\text{PB},u}/4 = 3 \,\text{mm}$ so that 177 the summed fluence from two opposing angles was homogeneous. This helped to reduce the 178 total number of pencil beams and thereby reduce the complexity of the optimization. In 179 the simulation platform, protons were emitted from a point $(u_0 \cdot (1 + \delta_u \cdot d_0), v_0 \cdot (1 + \delta_v \cdot d_0))$ 180 $(d_0), d_0) + (r_u, r_v, 0)$, where $d_0 = -400 \,\mathrm{mm}$ and r_u and r_v are normally distributed random 181 numbers with a standard deviation of σ_u and σ_v respectively. The point d_0 is just before 182 the front tracker and was chosen in agreement to previous investigations.³⁴ Protons were 183 assumed to have an initial direction vector of $(u_0\delta_u, v_0\delta_v, 1)$. The beam centers (u_0, v_0) were 184 chosen according the pencil beam grid defined above. For non-modulated scans, N_0 was set 185 to a default value $N_0 = N$ for all pencil beams. For modulated scans it was $N_0 = m_b^{\alpha} N$ 186 for a pencil beam modulated with a factor m_h^{α} . The proton's initial energy was set to 187 (200.00 ± 0.66) MeV, which is the standard mean energy used experimentally. The energy 188 spread was determined in a previous study³⁴ and agrees with experimental data acquired 189 at the beamline at Northwestern Medicine Chicago Proton Center, albeit with a wider spot 190 size setting. 191

¹⁹² II.D.2. Pencil beam reference counts

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To optimize pencil beam weights, a reference of the proton counts for every pencil beam is needed. This reference serves as a basis function for the fluence modulation and should not take into account interactions with the object. It can be generated for every pencil beam busing the Gaussian model

$$F_b(u, v, d) = G(u, v, d) \Big|_{N_0 = N, u_0 = u_b, v_0 = v_b}$$
(2)

assuming a pencil beam center (u_b, v_b) according to the regular grid and a constant number of protons N which is equal for all pencil beams.

²⁰⁰ II.D.3. Optimization of pencil beam weights

Using the F_b as basis functions, it is possible to generate an arbitrary counts field C^{α} for rotation angle α by finding weights w_b^{α} , such that C^{α} is expressed as a linear combination of the reference counts F_b from equation (2). Weights were found by minimizing the squared deviation, and therefore

$$w_b^{\alpha}(C^{\alpha}) = \arg\min_{w_b^{\alpha}} \iint du \, dv \, \left(C^{\alpha}(u,v,0) - \sum_b w_b^{\alpha} F_b(u,v,0) \right)^2.$$
(3)

Integration was performed over u and v, but only the isocenter binning depth d = 0 was considered. Optimization was performed using the method of Nelder and Mead.⁴¹

²⁰⁸ II.E. Proposed algorithm for fluence field optimization

Fluence field optimization requires finding a set of fluence modulation factors $m_b^{\alpha} \in [0, 1]$ for pencil beam b at rotation angle α , such that the resulting pCT reconstruction best achieves a given image variance target $V_{\text{target}}(x, y, z)$. The proposed method for fluence field optimization is performed in the projection domain (denoted by coordinates (u, v, d) and the rotation angle α) instead of the image domain (denoted by coordinates (x, y, z)). The method is sketched in figure 1 and consists of the following three steps, which will be detailed in sections II.E.1. to II.E.3.:

- 1. For a given phantom, find the resulting variance $V_{\text{unit}}^{\alpha}(u, v, d)$ in the projection domain for a unit fluence simulation with $m_b^{\alpha} = 1$ for all pencil beams.
- 218 2. For a given image variance target $V_{\text{target}}(x, y, z)$, find a stack of variance levels in the 219 projection domain $V_{\text{target}}^{\alpha}(u, v, d)$ that yields the image variance target.
- 220 3. Calculate the pixel-wise counts target $C^{\alpha}_{\text{target}}(u, v, d)$. Then, optimize weights that 221 yield the counts target according to equation (3).

The algorithm extends ideas from literature for x-ray CT^{21,22} to requirements of pCT such as the three-dimensional projections due to distance-driven binning³⁹ and a more complex noise model.^{33,34} It is, to our knowledge, not equivalent to any existing approach as it is performed in projection domain and computationally feasible without simplification to a parallel-beam geometry.

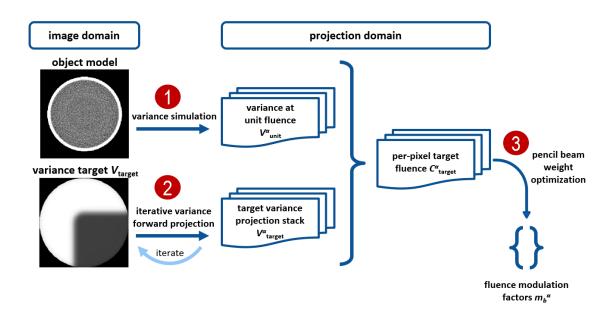


Figure 1: Workflow for optimization of fluence modulation factors m_b^{α} , given an object model and a variance target V_{target} .

²²⁷ II.E.1. Step 1: Variance at unit fluence prediction

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To find variance levels at unit fluence for a given phantom, we employed a Monte Carlo 228 simulation using the beam model described in section II.D. and $m_b^{\alpha} = 1$ for all pencil beams 229 and rotation angles. This step requires an object model according to section II.C. and resulted 230 in counts $C_{\text{unit}}^{\alpha}(u, v, d)$, which were reduced compared to the reference counts $F_{\text{unit}}(u, v, d) =$ 231 $\sum_{b} F_{b}(u, v, d)$ due to interactions with the object. For every point (u, v, d) in the projection, 232 a set of $n = C_{\text{unit}}^{\alpha}(u, v, d)$ WEPLs, $\{p\}$, was found such that the voxel around (u, v, d) was 233 crossed by the most likely path of each of the selected protons.³⁹ The unit fluence variance 234 was then the squared error of the mean 235

$$V_{\text{unit}}^{\alpha}(u, v, d) = \operatorname{Var}[\{p\}] / C_{\text{unit}}^{\alpha}(u, v, d).$$
(4)

Given a variance projection stack $V_{unit}^{\alpha}(u, v, d)$ the corresponding image variance $V_{unit}(x, y, z)$ can be calculated analytically as reconstruction was performed using filtered backprojection. Please refer to previous publications^{33,34} for details about variance calculations for pCT and for variance reconstruction in general.⁴²

²⁴¹ II.E.2. Step 2: Iterative variance forward projection

Finding a stack of variance projections $V_{\text{target}}^{\alpha}(u, v, d)$ whose variance reconstruction³³ yields 242 a given image variance target $V_{\text{target}}(x, y, z)$ is a problem with a large set of solutions. We 243 therefore aimed to find the inverse operation of variance reconstruction,⁴² i.e. a "variance 244 forward projection." An initial guess $V_0^{\alpha}(u, v, d)$ could be obtained by performing ray-245 tracing⁴³ through the image variance target $V_{\text{target}}(x, y, z)$ followed by a ramp-filtration. 246 The additional filtration was motivated by the fact that variance reconstruction is very 247 close to a simple unfiltered backprojection.⁴² Since ray-tracing is the inverse operation to 248 filtered backprojection, an additional ramp-filtration was required. While such forward- and 249 backprojection yield V_{target} again, this often yields unphysical negative variance projection 250 values and amplifies noise. Therefore, a median filter was applied to the ramp-filtered 251 projections followed by thresholding to positive values. 252

To minimize the error introduced by thresholding, we employed an iterative approach by applying variance reconstruction to the *i*-th set of variance projections $V_i^{\alpha}(u, v, d)$ yielding a variance volume $V_i(x, y, z)$. Again, using ray-tracing, the difference volume $V_{\text{target}}(x, y, z) V_i(x, y, z)$ was forward-projected and added to the current stack of variance projections. In every iteration, variance projection values were forced to be positive. This will converge to a set of physical (i.e. strictly positive) variance projections that yield an image variance approaching $V_{\text{target}}(x, y, z)$.

²⁶⁰ II.E.3. Step 3: Fluence optimization

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By definition, the variance projection values in equation (4) are inversely proportional to the number of contributing protons C. Therefore, the pixel-wise counts required to achieve the variance target could be calculated as $(V_{\text{unit}}^{\alpha}/V_{\text{target}}^{\alpha}) \cdot C_{\text{unit}}^{\alpha}$. However, for low counts, we need to consider that C follows a Poisson distribution (contrary to a normal distribution at sufficiently high counts) and therefore an additional correction function

$$k(C) = C \cdot \sum_{n'=1}^{\infty} P_C(n') \cdot \beta_{n',C} = C^2 \sum_{n'=1}^{\infty} \frac{P_C(n')}{n'}$$
(5)

needs to be introduced, where $P_C(n') = C^{n'} \exp(-C)/n'!$ is the Poisson probability of detecting n' protons instead of the expectation value of C and $\beta_{n',C} = C/n'$ is the relative change in variance if n' instead of C protons were detected. The function k(C) was stored in a lookup table for all relevant integer values of C up to 300 by numerically calculating the infinite sum for 1000 summands. Since $\lim_{C \to \infty} k(C)/C = 1$ and k(300)/300 = 1.0033 we assumed k(C) = C for all C > 300. Furthermore, k(C) was thresholded to return at least $C_{\min} = 8$ protons to avoid detector elements with missing information.

We used an optimization according to equation (3) to find pencil beam weights $w_b^{\alpha}(C_{\text{target}}^{\alpha})$ which achieve the pixel-wise projection counts target of

$$C^{\alpha}_{\text{target}}(u,v,d) = k \left[\frac{V^{\alpha}_{\text{unit}}(u,v,d)}{V^{\alpha}_{\text{target}}(u,v,d)} \cdot C^{\alpha}_{\text{unit}}(u,v,d) \right].$$
(6)

²⁷⁷ Due to the fact that C_{unit}^{α} and $C_{\text{target}}^{\alpha}$ are both affected by interactions with the object, the ²⁷⁸ optimization also needed to be performed for unit fluence allowing for an elimination of the ²⁷⁹ effect of attenuation and scattering. This resulted in fluence modulation factors

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$$m_b^{\alpha} = \frac{w_b^{\alpha}(C_{\text{target}}^{\alpha})}{w_b^{\alpha}(C_{\text{unit}}^{\alpha})}$$
(7)

with numerator and denominator as defined in equation (3). Due to the normalization, these factors were corrected for interactions with the object and thus could be used to simulate an FMpCT scan according to section II.D.1..

²⁸⁴ II.E.4. Reference approach

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A simpler approach for fluence field optimization, which was used in previous works,³¹ is to perform a binary modulation with two fluence levels. In image domain, a ROI is defined as a set of voxels that should be imaged with high fluence. A pencil beam is assigned a high imaging fluence if its central axis intersects the ROI, and a low imaging fluence otherwise. The fluence modulation factors were

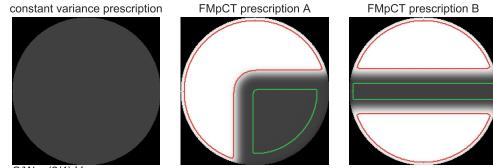
$$m_b^{\alpha} = \begin{cases} 1 & \text{if intersecting} \\ \gamma & \text{otherwise} \end{cases}$$
(8)

where $0 < \gamma < 1$ is the modulation strength, which was chosen to be equal to the contrast of the variance prescription of the proposed method.

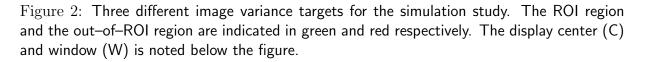
²⁹³ II.F. Simulation study

In a simulation study we prescribed three different image variance targets, which can be appreciated in figure 2: (1) constant variance V_{ROI} throughout the imaged object; (2) FMpCT prescription A (variance V_{ROI} inside one quadrant of the imaged object and $4 \cdot V_{\text{ROI}}$ elsewhere); and (3) FMpCT prescription B (V_{ROI} inside a central rectangular region and $4 \cdot V_{\text{ROI}}$ elsewhere). Variance targets are used in step 2 of the proposed algorithm, and therefore independent of the imaged object. In agreement to previous investigations³¹ the prescription contrast of 4 was chosen such that it is higher than the variance dynamic range of a unit fluence scan,³⁴ but reasonably achievable without expecting regions with vanishing counts or distortions of RSP accuracy.

Previous investigations³⁴ have shown that a uniform fluence does not yield a constant 303 variance for pCT. Therefore, the constant variance prescription is the most dose-efficient 304 image, if the complete image is required for diagnosis. Prescriptions A and B model two 305 treatment scenarios, where the treatment beam path is coming from 0 and 90 degrees in 306 A and from 90 and 180 degrees in B. Prescriptions were slightly blurred as sharp gradients 307 in image variance cannot be achieved due to the ramp filtration involved in reconstruction. 308 Throughout this work we use the nomenclature "constant", "A" and "B" to refer to the 309 three prescriptions. 310



 $\overline{C/W} = (2/4) V_{ROI}$



For all phantoms we first simulated a high dose unit fluence dataset with $m_i^{\alpha} = 1$. The mean incident proton fluence was chosen to be $133 \,\mathrm{mm}^{-2}$ such that it yielded a typical imaging dose for pCT of about $1.4 \,\mathrm{mGy}$,¹² when summed over all projections. We then chose the value of $V_{\rm ROI}$ for each phantom as the 95–th–percentile value of the variance in the unit fluence scan. For the water phantom this was $V_{\rm ROI} = 4.61 \times 10^{-4}$, for the CTP404 phantom $V_{\rm ROI} = 5.89 \times 10^{-4}$, and for the head phantom $V_{\rm ROI} = 11.96 \times 10^{-4}$. These values ³¹⁷ are consistent with previous studies.³⁴

For the CTP404 phantom RSP values of the phantom body and of two inserts inside the ROI were evaluated and compared to the unit fluence scenario. The body consisted of epoxy (RSP = 1.144), and inserts were made from Teflon (RSP = 1.791) and polymethylpentene (RSP = 0.883). RSP values were calculated with GEANT4 at a proton energy of 150 MeV and agreed with previous experiments.³⁵

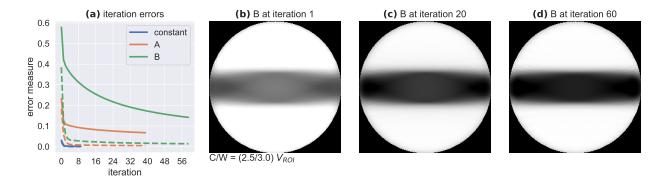
For a fair comparison of imaging doses, we computed the 95-th-percentile variance value 323 $v_{95}^{\rm ROI}$ inside the ROI (inside the whole phantom for unit fluence) and calculated a linear 324 correction factor $\eta = v_{95}^{\text{ROI}}/V_{\text{ROI}}$. Doses and counts were multiplied by η , variances were 325 multiplied by $1/\eta$. The choice of the 95-th-percentile value over the mean or the maximum 326 value is a compromise between the requirement that variances should be at $V_{\rm ROI}$ or lower, 327 and tolerating outliers. As the water and the CTP404 phantom were thin, the percentile 328 value was calculated only within the displayed central slice. For the head phantom, which 329 covered the entire height of the detector aperture, it was calculated over the full volume. To 330 avoid the variance evaluation being dominated by increased noise at the hull of the phantom 331 as discussed in previous works,^{33,34} we determined the shape of the hull by setting an RSP 332 threshold of 0.5 and eroding the hull by 7 mm. Values outside this region were disregarded. 333 The ROI region and the out-of-ROI region are indicated in figure 2 for fluence modulations 334 A and B. 335

336 III. Results

³³⁷ III.A. Gaussian pencil beam model

In an experimental dataset without phantom we determined the beam spreads of the Gaus-338 sian beam model to be $\sigma_u = (4.04 \pm 0.08) \text{ mm}$ and $\sigma_v = (5.24 \pm 0.09) \text{ mm}$. The divergence 339 was $\delta_u = (5.2 \pm 0.6) \, 10^{-4} \text{mm}^{-1}$ and $\delta_u = (5.8 \pm 1.4) \, 10^{-4} \text{mm}^{-1}$. The beam spread in the u 340 direction was significantly smaller compared to the beam spread in v direction. Divergence 341 in the u and v direction did not differ outside of the uncertainty bounds. The distances from 342 the isocenter to a virtual source were $1/\delta_u = (1.9 \pm 0.2)$ m and $1/\delta_v = (1.7 \pm 0.4)$ m, which 343 agrees with the position of the scanning magnets, which is 1.8 m from the isocenter. The 344 stated parameters were used in all following evaluations. 345

³⁴⁶ III.B. Variance optimization



³⁴⁷ III.B.1. Iterative variance forward projection

Figure 3: (a) Root-mean-square error (solid) and mean error (dashed) as a function of the iteration number of the three image variance targets. (b) – (d) Reconstructed variance volumes for prescription B for different iterations. The display center (C) and window (W) is noted below the figure.

For step 2 of the proposed method, figure 3 (a) shows error measures as a function of 348 the iteration number. The root-mean-square (RMS) error as well as the mean error between 349 the current variance volume $V_i(x, y, z)$ and the variance target $V_{\text{target}}(x, y, z)$ are calculated 350 within the field-of-view. The fastest convergence is observed for the constant variance 351 prescription, while both FMpCT prescriptions A and B show a remaining RMS error that 352 only reduces slowly in every iteration. The mean error quickly drops to zero within the 353 first iterations. The relative change in RMS error for all prescriptions was below 1% per 354 iteration when they were stopped. Figure 3 (b) to (d) show $V_i(x, y, z)$ for prescription B at 355 three different iterations. At iteration 20, the high-variance region has reached the correct 356 value, while in the low-variance region artifacts remain, but decrease up to the last iteration. 357

358 III.B.2. Fluence optimization

To validate the use of the correction function k(C), figure 4 shows k(C)/C together with the relative increase of the image variance V_C at mean counts C. The relative increase is calculated as $(V_C \cdot C)/(V_{C_{\infty}} \cdot C_{\infty})$ for $C_{\infty} = 310$ for simulated pCT data. Both curves agree, which shows that variance increases overproportionally for low counts and that the correction function k(C) describes this well.

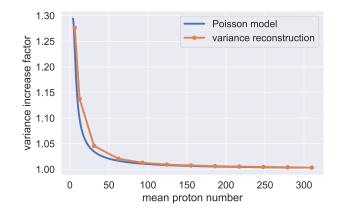


Figure 4: Overproportional increase of image variance with decreasing counts in a simulation with varying mean proton number C and agreement with the fluence correction function k(C)/C.

Figure 5 shows intermediate steps of the fluence optimization for the pediatric head 364 phantom and variance prescription A. All projection data are shown as sinograms plotted 365 as a function of the detector position in u direction and the rotation angle. Only data for 366 v = d = 0 are shown. In figure 5 (a), variance at unit fluence $V_{\text{unit}}^{\alpha}(u, 0, 0)$ is shown (step 1) 367 of the algorithm), which is high at the periphery of the object and around heterogeneities, 368 as discussed in previous works.³⁴ Figure 5 (b) shows the variance target $V^{\alpha}_{\text{target}}(u, 0, 0)$ as a 369 result of the iterative optimization (step 2). Figure 5 (c) shows the pixel-wise counts target 370 for fluence modulation $C^{\alpha}_{\text{target}}(u, 0, 0)$ (step 3) as given by equation (6). Parts of the variance 371 target in (b) are assigned a value of 0, and receive the unit fluence in (c). In figure 5 (d), 372 the counts target is fitted by the pencil beam model to get the weights required for fluence 373 modulation (also step 3). This can be calculated as $\sum_{b} w_{b}^{\alpha} F_{b}(u, v, d)$. Some small features 374 of (c) are not present in (d) if they are smaller than the extension of a pencil beam. 375

376 III.C. Simulation study

Figures 6 and 7 show simulated fluence modulations for all phantoms. RSP, variance and dose maps are shown together with the counts sinograms. For the water phantom imaged with unit fluence (figure 6 (a)), counts and dose were homogeneous throughout the phantom, variance was reduced in the center. This reduction was compensated in figure 6 (b) for the constant variance target, where instead counts and imaging dose were reduced in the center and variance was homogeneous across the phantom, except for a steep increase at the hull.

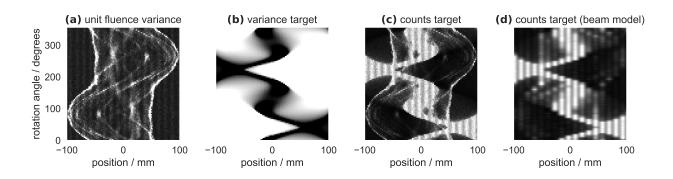


Figure 5: Intermediate results of the fluence optimization process for the pediatric head phantom and the orthogonal beams variance target: (a) unit fluence variance $V_{unit}^{\alpha}(u, 0, 0)$, (b) variance target $V_{target}^{\alpha}(u, 0, 0)$, (c) pixel-wise target counts $C_{target}^{\alpha}(u, 0, 0)$, and (d) target counts as fitted by the beam model. Data are shown as a function of the rotation angle α and the detector coordinate u. For display a center of 0.4 mm^2 and a window of 0.8 mm^2 has been applied for variances, and a center of 80 and a window of 160 for counts.

The fluence modulations in figure 6 (c) and (e) for variance targets A and B can already 383 be appreciated in the RSP maps. Variance levels followed the prescription with a sharp 384 gradient. For prescription A some streaks of high variance were observed within the ROI. 385 Using the reference approach in figure 6 (d) and (f), conformity of variance and dose maps 386 with the ROI was degraded, in particular for prescription B, where variance and dose are 387 at the same level as in the unit fluence scan for most of the phantom and the change in 388 variance cannot be seen in the RSP maps. In the counts sinograms, regions of increased 389 counts roughly agreed with those using the optimization, but were uniform, as required. 390 Instead, using the optimization, a heterogeneous counts pattern was observed. 391

For the CTP404 phantom (figure 7 (a,b)) and the head phantom (figure 7 (c,d)), variance increased around heterogeneities both in unit fluence and fluence-modulated scans. For the head phantom in particular the palate exhibited locally elevated variance levels. The fluence modulation with prescription A was less conformal, compared to those of the water phantom. In particular for the CTP404 phantom variance contrast was impaired. Counts sinograms for prescription A in figure 6 (c) and figure 7 (b,d) are similar, but phantom-specific differences are noticeable.

Mean imaging doses are summarized in figure 8, where for fluence modulations the mean dose over the whole phantom as well as mean doses in the ROI region and the out-of-ROI region are reported. For the water phantom, prescribing constant variance resulted in a dose reduction of 8.9% compared to the unit fluence dose. For the region-of-interest fluence

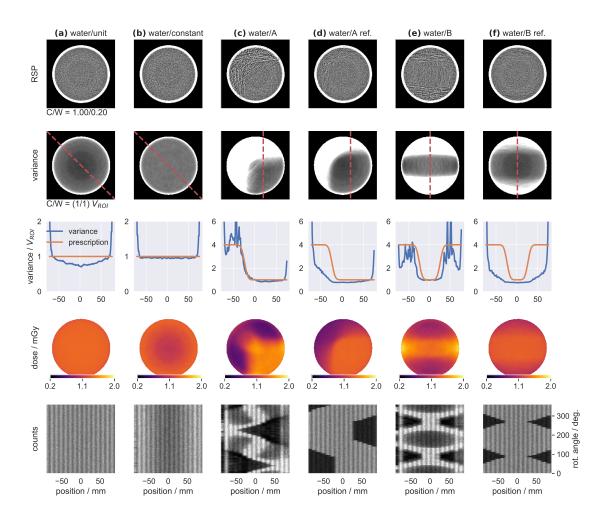


Figure 6: Simulation study for the water phantom and variance targets as indicated in the titles. Sinograms are shown for v = d = 0. Center (C) and window (W) settings for display of RSP and variance values are given.

modulations, dose saving outside the ROI was 40.5% for prescription A and 25.7% for 403 prescription B. Using the simple reference approach, dose reductions were less pronounced 404 and dropped to 29.2% and 13.2% respectively. For the FMpCT prescription A and the 405 CTP404 phantom as well as the head phantom, dose savings outside the ROI were slightly 406 lower compared to the 40.5% of the water phantom (35.4% and 38.9% respectively). For 407 all phantoms, fluence modulations A and B achieved a lower dose outside the ROI compared 408 to the unit fluence, but after normalization with η required a higher dose inside the ROI 409 by 9.2% to 19.2%. Doses inside the ROI were approximately constant for the reference 410 approach. Mean doses over the whole phantom were reduced by 7.2% to 13.1% using the 411 reference approach and by 9.8% to 18.6% for the FMpCT optimizations. 412

For the CTP404 phantom, the two inserts and the body inside the ROI had an RSP value of 1.776, 0.881, and 1.143, compared to 1.776, 0.879, and 1.143 for the unit fluence case.

Figure 9 shows the head phantom with unit fluence (a,b) and for the constant variance 416 target (c,d) both in a sagittal view (a,c) and a coronal view (b,d). Dose is homogeneous 417 for the unit fluence imaging, but the variance is notably lower in the back of the head and 418 around the spinal cord compared to regions around the palate and the nasal cavities. These 419 variations were compensated for in the fluence modulations achieving more homogeneous 420 variance levels at reduced doses in regions where variance was low for unit fluence. Mean 421 dose over the whole phantom was 1.15 mGy compared to 1.37 mGy in the unit fluence case 422 (16.0% reduction). Around the palate and the nasal cavities, dose is increased in the fluence-423 modulated scan, which is not expected and may be due to the normalization by η . 424

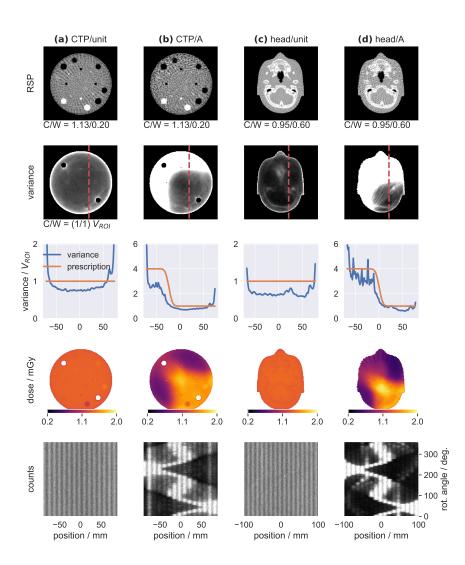


Figure 7: Simulation study for the CTP404 and the head phantom, and variance targets as indicated in the titles. Sinograms are shown for v = d = 0. Center (C) and window (W) settings for display of RSP and variance values are given.

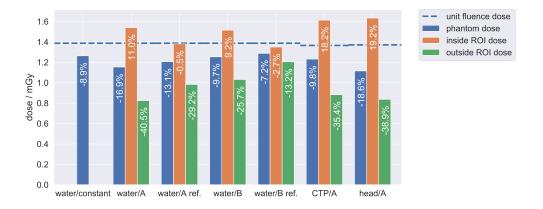


Figure 8: Mean imaging doses for the simulation study. The dashed line indicates the unit fluence dose while bars show the average phantom dose and doses inside and outside the ROI. The relative dose change compared to unit fluence dose is given inside the bars. Unit fluences were equal for all phantoms, but unit fluence doses differed slightly.

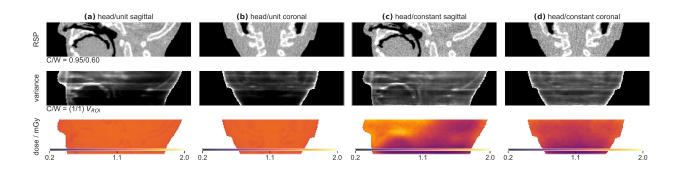


Figure 9: Simulation study for the pediatric head phantom with unit fluence (a), (b) and the constant variance target (c), (d). Row by row, the RSP, variance, and imaging dose are shown. Sagittal and coronal views are shown. Center (C) and window (W) settings for display of RSP and variance values are given.

425 IV. Discussion

⁴²⁶ IV.A. Gaussian pencil beam model

We found parameters of a Gaussian pencil beam model that allowed us to describe pencil 427 beams at arbitrary fluences and positions. This is a key component of the fluence modulation 428 scheme, as it allows to find a linear combination of a regular grid of pencil beams that achieves 429 the required counts as calculated by our algorithm. Uncertainty bounds for fits in v direction 430 were consistently larger than those in u direction, in particular for the divergence parameter 431 δ . This was because the detector aperture is smaller in u direction and less datapoints were 432 available. The beam spread σ_v was significantly larger than σ_u . While this anisotropy is 433 not expected for clinical operation, it may have been caused by operating the beam line in 434 research mode and modifying beam optics settings to keep proton fluence low and viable for 435 the scanner. For future experimental studies, certain model parameters, such as the beam 436 energy spread, may require adjustment to exactly match experimental variance levels. 437

⁴³⁸ IV.B. Variance optimization

⁴³⁹ IV.B.1. Iterative variance forward projection

Using an iterative approach, we calculated stacks of variance projections that yield a desired 440 variance map in image space. Depending on the complexity of the variance prescription, this 441 required a different amount of iterations and a non-zero RMS error remained. The easiest 442 case (constant variance target), did not require negative variance values (a constant stack of 443 variance projections would yield a constant image variance) and therefore converged quickly. 444 The two inhomogeneous variance targets A and B did suffer from the positivity requirement 445 and therefore only slowly converged towards a reduced RMS error. While with negative 446 variance values, a (close to) zero RMS error would be possible, this was not the case when 447 requiring physical variance values. The variance target stacks therefore already contained an 448 inherent error, which impacted the achievable variance contrast. However, it did not impact 449 fluence modulation in general, as the prescribed fluences could be rescaled, such that $V_{\rm ROI}$ 450 was achieved inside the ROI. 451

452 IV.B.2. Fluence optimization

We calculated the counts target according to equation (6), which could run into a lower and 453 an upper limit. Firstly, to ensure that that data was available throughout the projection, 454 we required at least C_{\min} protons in every pixel. Secondly, to avoid unreasonably high 455 imaging doses, only fluence modulation factors $m_b^{\alpha} \leq 1$ were allowed, even if the variance 456 target from the previous step (iterative variance forward projection) was zero. This was 457 relevant in particular at the hull of the object, which is also a limited area to be traversed by 458 a therapeutic proton beam. Again, both limits impacted achievable variance contrast, but 459 $V_{\rm ROI}$ could be achieved in the ROI by rescaling with η . Due to the limitation to pencil beams 460 with a finite size, small variance features were averaged out, which may impact homogeneity 461 of the achieved variance, in particular for phantoms with strong heterogeneities. 462

⁴⁶³ IV.C. Simulation study

We simulated FMpCT scans for different phantoms and variance targets demonstrating two possible applications for dose reduction using fluence modulation: (1) for achieving constant variance throughout the object and (2) concentrating imaging dose in a high image quality ROI and reducing it elsewhere.

The dose reduction for constant variance with the homogeneous water phantom was 468 8.9%, which already is considerable. As shown in previous investigations,³⁴ variance for 469 hetereogeneous phantoms is dominated by mutiple Coulomb scattering, which depends on 470 the local heterogeneity of the phantom. Therefore, variance maps of the head phantom in 471 coronal and sagittal views were varying greatly. Assuming that good image quality is required 472 in the complete field-of-view, a fluence-modulated scan can reduce the imaging dose by 473 16.0% compared to a unit fluence scan, without any loss of diagnostic value. Equivalently, 474 the signal-to-noise ratio could have been improved by 35% at equal dose. 475

For all phantoms and two different image variance targets we could demonstrate considerable dose savings of 25.7 % to 40.5 % outside of the ROI. At the same time, the imaging dose inside the ROI increased compared to the unit fluence acquisition. Assuming that the ROI agrees with the treatment beam path and that treatment doses are several orders of magnitude higher than imaging doses, this increase is probably not relevant. At the same time, proton therapy allows for minimal doses outside the treatment beam path, requiring that this advantage is not compromised by frequent imaging. Mean imaging doses over the whole phantom were reduced for all combinations of phantoms and variance targets. Using a sensitometric phantom we showed that RSP accuracy is not compromised by fluence modulation. RSP errors were comparable for modulated and un-modulated scans, and all below 1 %, which is within the magnitude expected from literature.^{12,19,35}

Imaging doses in fluence-modulated scans showed local increases and doses partially spilled out of the ROI. This may have impaired results in this study and could be caused by the fact that optimization was exclusively performed with a variance objective. Future studies should therefore include a dose objective outside of the ROI while keeping the variance objective inside the ROI, further developing ideas from studies for x-ray CT.²¹ Moreover, the optimal choice of the contrast in the image variance prescription should be studied in the future, but is out of scope for this work.

⁴⁹⁴ Using a simple intersection-based approach also showed dose savings compared to unit ⁴⁹⁵ fluence acquisitions. However, dose savings were considerably less compared to the opti-⁴⁹⁶ mized FMpCT scans and conformity of variance with the prescription was degraded. By ⁴⁹⁷ construction, a prescription of constant variance is not possible with this approach.

Future work should also address the impact of iterative image reconstruction, which is 498 frequently used for pCT imaging.^{44–48} In contrast to the direct filtered backprojection algo-499 rithm used in this study, iterative reconstruction employs a regularization method (typically 500 total variation), which reduces noise and whose optimal weight depends on the object and 501 the fluence level.⁴⁹ While most fluence modulation studies for x-ray CT have been performed 502 using filtered backprojection,^{20,21} a first study²³ investigated a joint optimization of the flu-503 ence field and a spatially varying regularization parameter in the iterative reconstruction. 504 For pCT, a comparison of iterative and direct reconstruction⁴⁷ showed comparable image 505 quality. Preliminary work of the authors using an iterative reconstruction algorithm⁴⁶ and 506 fluence modulation suggests feasibility of combining the two methods for pCT. 507

508 V. Conclusion

We developed a novel method for fluence-modulated proton computed tomography using 509 pencil beam scanning and demonstrated its feasibility in a simulation study. Dose reductions 510 achieved by prescribing uniform variance were considerable, in particular for an anthropo-511 morphic head phantom. This suggests the need for employing non–uniform fluence patterns 512 in future pCT studies, whenever dose efficiency is a key requirement. Furthermore, the pro-513 posed method allows us to prescribe arbitrary image variance targets, which were shown to 514 further reduce imaging dose outside of a given region-of-interest. This can be of particular 515 interest in the context of particle therapy and allow for daily imaging at a reduced imaging 516 dose to healthy tissue outside of the treatment beam path. 517

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