Lawrence Berkeley National Laboratory

Recent Work

Title

Isotopic Tracer Studies of Fischer-Tropsch Synthesis over Ru/TiO{sub 2} Catalysts

Permalink https://escholarship.org/uc/item/505018s7

Author Krishna, K.R.

Publication Date

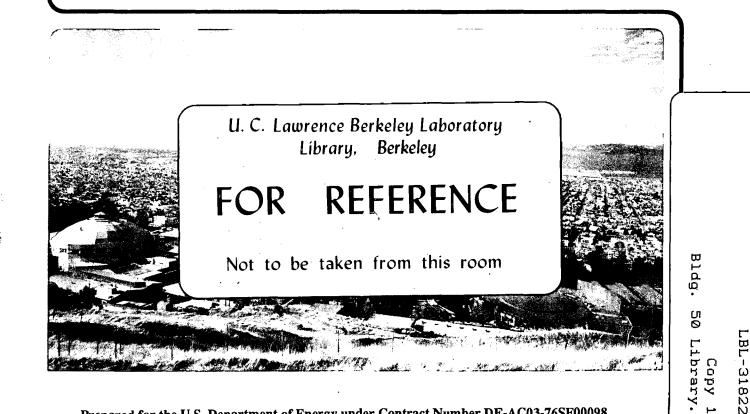
Lawrence Berkeley Laboratory UNIVERSITY OF CALIFORNIA

CHEMICAL SCIENCES DIVISION

Isotopic Tracer Studies of Fischer-Tropsch Synthesis over Ru/TiO2 Catalysts

K.R. Krishna (Ph.D. Thesis)

January 1992



Prepared for the U.S. Department of Energy under Contract Number DE-AC03-76SF00098

DISCLAIMER

This document was prepared as an account of work sponsored by the United States Government. Neither the United States Government nor any agency thereof, nor The Regents of the University of California, nor any of their employees, makes any warranty, express or implied, or assumes any legal liability or responsibility for the accuracy, completeness, or usefulness of any information, apparatus, product, or process disclosed, or represents that its use would not infringe privately owned rights. Reference herein to any specific commercial product, process, or service by its trade name, trademark, manufacturer, or otherwise, does not necessarily constitute or imply its endorsement, recommendation, or favoring by the United States Government or any agency thereof, or The Regents of the University of California. The views and opinions of authors expressed herein do not necessarily state or reflect those of the United States Government or any agency thereof or The Regents of the University of California and shall not be used for advertising or product endorsement purposes.

Lawrence Berkeley Laboratory is an equal opportunity employer.

DISCLAIMER

This document was prepared as an account of work sponsored by the United States Government. While this document is believed to contain correct information, neither the United States Government nor any agency thereof, nor the Regents of the University of California, nor any of their employees, makes any warranty, express or implied, or assumes any legal responsibility for the accuracy, completeness, or usefulness of any information, apparatus, product, or process disclosed, or represents that its use would not infringe privately owned rights. Reference herein to any specific commercial product, process, or service by its trade name, trademark, manufacturer, or otherwise, does not necessarily constitute or imply its endorsement, recommendation, or favoring by the United States Government or any agency thereof, or the Regents of the University of California. The views and opinions of authors expressed herein do not necessarily state or reflect those of the United States Government or any agency thereof or the Regents of the University of California.

Isotopic Tracer Studies of Fischer-Tropsch Synthesis over Ru/TiO₂ Catalysts

Kamala Raghunathan Krishna Ph. D. Thesis

Department of Chemical Engineering University of California

and

Chemical Sciences Division Lawrence Berkeley Laboratory University of California Berkeley, CA 94720

January 1992

This work was supported by the Director, Office of Energy Research, Office of Basic Energy Sciences, Chemical Sciences Division, of the U. S. Department of Energy under Contract No. DE-AC03-76SF00098.

Isotopic Tracer Studies of Fischer-Tropsch Synthesis over Ru/TiO₂ Catalysts

by

Kamala Raghunathan Krishna

ABSTRACT

Fischer-Tropsch synthesis is a process in which CO and H_2 react to give predominantly liquid hydrocarbons. The reaction can be considered a special type of polymerization in which the monomer is produced *in situ*, and chain growth occurs by a sequence of independently repeated additions of the monomer to the growing chain. An investigation has been conducted to study the CO hydrogenation reaction in order to better understand catalyst deactivation and the elementary surface processes involved in chain growth.

Isotopic tracers are used in conjunction with transientresponse techniques in this study of Fischer-Tropsch synthesis over Ru/TiO₂ catalysts. Experiments are conducted at a total pressure of 1 atmosphere, reaction temperatures of 453-498 K and D₂/CO (or H₂/CO) ratios of 2-5. Synthesis products are analyzed by gas chromatography or isotope-ratio gas chromatography-mass spectrometry.

Ru/TiO₂ catalysts deactivate with no change of product selectivity and the rate of deactivation correlates with initial

catalyst activity. Deactivation occurs at an initial rapid rate, followed by a slower activity loss. Deactivation is accompanied by a loss in CO uptake and the accumulation of various types of carbonaceous species. The long-term loss of activity is attributed to the buildup of long chain hydrocarbon product species.

Rate constants for chain initiation, propagation and termination are evaluated under steady-state reaction conditions by using transients in isotopic composition. The activation energy for chain termination is much higher than that for propagation, accounting for the observed decrease in the chain growth parameter with increasing temperature. Coverages by reaction intermediates are also estimated. The dominant reactive surface species are monomeric building units, which occupy 0.2-0.6 ML. Alkyl species that are the direct hydrocarbon product precursors occupy < 0.2 ML. Adsorbed CO covers 0.7 ML.

When small amounts of ${}^{12}C$ -labelled ethylene are added to ${}^{13}CO/H_2$ synthesis gas, ethylene acts as the sole chain initiator. Ethylene-derived carbon also accounts for 45 % of the C₁ monomer pool. То

my parents,

my parents-in-law,

Ashok,

and

Ananth.

ιų.

5° 1

Table of Contents

•

| Ch | apter | 1 | Introduction | 1 |
|----|--------|-----|----------------------------------------------------------------------------------------------------------------------------------------------------------|-----|
| Ch | apter | 81 | An Isotopic Tracer Study of the Deactivation of Ru/TiO ₂ Catalysts during Fischer-Tropsch Synthesis | 5 |
| Ch | apter | 111 | Intrinsic Rate Parameters of the Fischer -Tropsch Synthesis | 50 |
| Ch | apter | IV | Estimates of the Rate Coefficients for Chain Initiation, Propagation, and Termination during Fischer-Tropsch Synthesis over Ru/TiO ₂ | 55 |
| Ch | apter | V | The Effect of Ethylene Addition on Fischer- Tropsch Synthesis | 102 |
| Ap | pendix | I | Data Acquisition and Analysis Programs | 125 |
| Ap | pendix | 11 | Solution of the differential equations describing chain growth during Fischer- Tropsch Synthesis | 173 |
| Ap | pendix | 111 | Chain-growth model parameter estimation | 177 |

List of Figures

Chapter II

| Fig. 1 | CO turnover frequency as a function of reaction time. | |
|--------|-----------------------------------------------------------------------------------------------------------------|----|
| | Reaction Conditions: $P_{D2} = 150$ torr, $P_{CO} = 50$ torr, | |
| | T = 498 K | 16 |
| Fig. 2 | Catalyst activity at 1 min after reaction startup | |
| | versus ruthenium dispersion | 17 |
| Fig. 3 | Correlation of the inverse of the deactivation time | |
| | constant with the CO turnover frequency at $t_r = 0$ | |
| | obtained by extrapolation of the N_{CO} versus t_r curve | |
| | for $t_r \ge 20$ min | 19 |
| Fig. 4 | Effect of reaction time on the ASF plot (log N_{Cn} versus | 5 |
| | C_n) for Ru/TiO ₂ (D). N _{Cn} is the turnover frequency for | |
| | products of carbon number n | 20 |
| Fig. 5 | ¹³ C TPSR spectra to estimate CO uptake as a function | |
| | of t_r . a. Data for Ru/TiO ₂ (D). b. Data for Ru/TiO ₂ (R). | |
| | Reaction Conditions: $P_{D2} = 150$ torr, $P_{CO} = 50$ torr, | |
| | T = 498 K. Gas Introduction sequence: $12CO + D_2$ (t _r) | |
| | \rightarrow He (cool) \rightarrow ¹³ CO (5 min) \rightarrow D ₂ (TPSR). In the TPSR | |
| | spectra, the temperature is raised from room | |
| | temperature to 503 K at 0.17 K/sec and then | |
| | maintained constant at 503 K. | 22 |
| Fig. 6 | CO uptake as a function of reaction time, tr | 23 |
| Fig. 7 | ¹³ C TPSR spectra to estimate carbon accumulation on | |

Ŷ,

ŵ.

¥

¥.

| | | the catalyst at $t_r = 10$ min, standard reaction |
|-----|---------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| | | conditions. a. CO + C_{α} + C_{β} . Gas Introduction sequence: |
| | . · · | ¹³ CO + D ₂ (10 min) \rightarrow He (cool) \rightarrow D ₂ (TPSR). b. C _{α} + C _{β} : |
| | | Gas Introduction sequence: $^{13}CO + D_2$ (10 min) \rightarrow |
| | | ¹² CO + He (30 s) \rightarrow He (cool) D ₂ (TPSR). c. C _{β} ". Gas |
| | | Introduction sequence: $^{13}CO + D_2$ (10 min) $\rightarrow ^{12}CO + D_2$ |
| | | (2 min) \rightarrow He (cool) \rightarrow D ₂ (TPSR). In the TPSR spectra, |
| | | the temperature is raised from room temperature to |
| | | 503 K at 0.17 K/sec and then maintained constant at |
| | | 503 K |
| | Fig.8 | ^{13}C TPSR spectra for $\text{C}_{\beta}^{\text{"}}$ with varying reaction time $t_{r}.$ |
| | | Gas introduction sequence: 13CO + D ₂ (t _r) \rightarrow 12CO + D ₂ |
| | | (2 min) \rightarrow He(cool) \rightarrow D ₂ (TPSR). In the TPSR spectra, |
| | | the temperature is raised from room temperature to |
| | | 503 K at 0.17 K/sec and then maintained constant at |
| | | 503 K |
| | Fig. 9 | Coverages of carbon species obtained from 13C TPSR |
| | | as a function of reaction time. a. $C_{\alpha} + C_{\beta}$. b. C_{β} ". |
| · . | | c. $C_{\alpha} + C_{\beta}'$ |
| | Fig. 10 | Comparison of methane turnover frequency from this |
| | | work over Ru/TiO_2 and Ru/Al_2O_3 (25). All data are |
| | | based on measurements made using a H ₂ /CO feed |
| | | mixture |
| | Fig. 11 | Model curves for N_{CO}/θ_{CO} , θ_{α} , θ_{CO} , and θ_{β} " as a |
| | | |

ł

÷

Ŷ

lation in the second se

V

| | function of reaction time. | 42 |
|---------|-------------------------------------------------------------------|----|
| Chapter | IV | |
| Fig. 1 | Schematic of GC-MS Analytical System. | 63 |
| Fig. 2 | (a) Isotopic Transient Data Sampling. | |
| | (b) Average Rise Curve | 67 |
| Fig. 3 | Chain Growth Model | 69 |
| Fig. 4 | Anderson-Schulz-Flory plot, log N _{Cn} vs Carbon number, | |
| | where N _{Cn} is the turnover frequency for products of | |
| | carbon number n | 73 |
| Fig. 5 | a) CO turnover frequency, N _{CO} , as a function of | |
| | temperature; (b) Chain growth parameter α as a | |
| | function of temperature; $D_2/CO = 3$ | 75 |
| Fig. 6 | (a) CO turnover frequency, N_{CO} , as a function of D_2/CO | |
| | ratio; (b) Chain growth parameter α as a function of | |
| | D ₂ /CO ratio; T = 463 K | 76 |
| Fig. 7 | (a) α -olefin to n-paraffin ratio vs Carbon Number; (b) | |
| | β -olefin fraction in straight-chain olefins vs Carbon | |
| | Number; T = 463 K, D_2/CO = 3. (c) Straight chain | |
| | olefins to n-paraffin ratio as a function of reaction | |
| | temperature; (d) β -olefin fraction in straight-chain | |
| | olefins as a function of reaction temperature; | |
| | $D_2/CO = 3$. (e) Straight chain olefins to n-paraffin | |
| | ratio as a function of D_2/CO ratio; (f) β -olefin | |

vi

| | fraction in straight-chain olefins as a function of D_2/CO ratio; T = 463 K |
|---------|----------------------------------------------------------------------------------------------|
| Fig. 8 | F (13CD ₄) rise after a switch from $12CO/D_2$ to |
| | $^{13}CO/D_2$ at t = 0. T = 463 K, D_2/CO = 3 |
| Fig. 9 | (a) $F(^{13}C)$ rise in the C ₃ -C ₅ products; (b) $F(^{13}C)$ rise in |
| C C | the C_6 - C_8 products; transient response after a switch |
| | from $12CO/D_2$ to $13CO/D_2$ at t = 0. T = 463 K, |
| | D ₂ /CO = 3 |
| Fig. 10 | (a) Propagation rate constant, kp, as a function of |
| | temperature; (b) Inititation rate constant, k _i , and |
| | termination rate constant, kt, as a function of |
| | temperature; $D_2/CO = 3$ |
| Fig. 11 | (a) Coverage by alkyl surface species as a function of |
| | temperature; (b) Coverage by monomeric species as a |
| | function of temperature; $D_2/CO = 3$ |
| Fig 12 | (a) Propagation rate constant, k_p , as a function of D_2/CO |
| | ratio; (b) Inititation rate constant, k _i , and termination |
| | rate constant, k_t , as a function of D_2/CO ratio; |
| | T = 463 K |
| Fig. 13 | (a) Coverage by alkyl surface species as a function of |
| | D_2/CO ratio; (b) Coverage by monomeric species as a |
| | function of D_2/CO ratio; T = 463 K |

2

vii

Chapter V

.

| Fig. 1. | Effect on total carbon in hydrocarbon product when |
|---------|-----------------------------------------------------------------------------------------------------------|
| | ethylene is added to the CO/H ₂ feed; (a) 250 μ pm C ₂ H ₄ . |
| | (b) 1.2 % C_2H_4 . Reaction conditions: T= 463 K; $H_2/CO = 3$. |
| | Ethylene is added from $t = 20$ min to $t = 30$ min 110 |
| Fig. 2. | Anderson-Sculz-Flory plot of N _{Cn} versus carbon |
| | number, C_n , in a) CO/H ₂ ; (b) CO/H ₂ /C ₂ H ₄ . Reaction |
| | conditions: T= 463 K; H ₂ /CO = 3 112 |
| Fig. 3. | Activity increase in rates of formation of |
| | hydrocarbon products as a function of carbon number, |
| | C_n , on addition of 1.2 % C_2H_4 to CO/H ₂ feed 114 |
| Fig. 4. | Olefin/n-paraffin ratio as a function of carbon |
| | number, C_n in (a) CO/H ₂ ; (b) CO/H ₂ /C ₂ H ₄ . Reaction |
| | conditions: T= 463 K; $H_2/CO = 3$ |
| Fig. 5. | $F(^{13}C)$ rise in the C_3 - C_8 products; transient response |
| | after (a) a switch from ${}^{12}CO/H_2$ to ${}^{13}CO/H_2$ at t = 0; |
| | (b) a switch from $12CO/H_2/12C_2H_4$ to $13CO/H_2/12C_2H_4$ |
| | at t = 0. Reaction conditions: T= 463 K; $H_2/CO = 3$ 117 |

viii

*

4

1

- -

List Of Tables

Chapter II

. .

.

| Table 1 | Catalyst Characteristics | 12 |
|---------|--------------------------------------------------------------------------------------|----|
| Table 2 | Comparison of the time constants for the decay in $N_{\mbox{CO}}$ | |
| | with that for the decay in θ_{CO} , for $t_r > 20$ min | 24 |
| Table 3 | Comparison of the Initial Loss in θ_{CO} with that due to | |
| | room temperature disproportionation of CO | 26 |
| Table 4 | Comparison of the time constants for the | |
| | accumulation of $C_{\alpha}\text{+}$ C_{β} with that for the decay in N_{CO} | |
| | during the first 10 min under reaction conditions | 32 |

Chapter IV

| Table1 | τ and τ_m obtained from fitting the chain growth model | |
|---------|------------------------------------------------------------------|----|
| | to the data: D ₂ /CO = 3; T = 463 K | 82 |
| Table 2 | Average τ and τ_m obtained from fitting the chain | |
| | growth model to the data: $D_2/CO = 3$; reaction | |
| | temperature is varied | 84 |
| Table 3 | Average τ and τ_m obtained from fitting the chain | |
| | growth model to the data: Ratio of D ₂ /CO is varied; | |
| | T = 463 K | 84 |
| Table 4 | Transient at standard reaction conditions: Ru/TiO2 | |
| | catalyst | 85 |

~

| Table 5 | The effect of temperature on the coverage by | |
|---------|-----------------------------------------------------------|----|
| | reaction intermediates: D ₂ /CO ratio=3 | 90 |
| Table 6 | The effect of D ₂ /CO ratio on the coverage by | |
| | reaction intermediates: T= 463 K | 96 |

Chapter V

X

.

¥.

List of Symbols

| ASF | Anderson-Schulz-Flory |
|------------------|---------------------------------------------------------------------------|
| C _α | Carbidic carbon (ML) |
| C _β | Alkyl carbon chains (ML) |
| C _β ' | Alkyl carbon chains that are precursors to the C_{2+} |
| | hydrocarbon products (ML) |
| C _β " | Unreactive alkyl chains, of longer chain length than C_{β}^{\prime} |
| | (ML) |
| F ₁ | Fraction of labelled carbon in the surface precursor to |
| | methane |
| F _m | Fraction of labelled carbon in the monomer pool |
| Fn | Fraction of labelled carbon in the pool of carbon chain |
| | length n |
| к | Equilibrium constant for CO adsorption |
| k | Rate parameter |
| k _i | Initiation rate constant (s-1) |
| k _p | Intrinsic Rate constant for propagation (s-1) |
| k _p ' | Apparent rate constant for propagation (s-1) |
| k _t | Rate constant for termination (s-1) |
| k ₁ | Rate constant |
| k ₂ | Rate constant |
| k ₃ | Rate constant |
| ML | Monolayer, unit of coverage based on hydrogen |
| | chemisorption to estimate the number of surface exposed |

| Ru a | toms |
|------|------|
|------|------|

.

| N _{co} | Turnover frequency of CO (s-1) i.e., moles of CO converted |
|-------------------|------------------------------------------------------------|
| | per moles of surface-exposed metal atoms per sec |
| N _{CO} o | Apparent turnover frequency of CO at $t_r = 0$ min |
| N _{C1} | Turnover frequency of methane (s-1) |
| N _{Cn} | Turnover frequency of products of carbon chain length n |
| | (S ⁻¹) |
| n | Carbon number |
| n _{av} | Average carbon number of hydrocarbon products |
| Pco | Partial pressure of CO |
| t _r | Time onstream after reaction startup |
| α | ASF chain growth probability or chain growth parameter |
| θ | Surface coverage |
| θω | CO coverage (ML) |
| θm | Coverage by monomer building block |
| θ1 | Coverage by methane precursor |
| θn | Coverage by precursor to hydrocarbon products of chain |
| | length n |
| θ_{α} | Coverage by $C_{\alpha} + C_{\beta}'$ (ML) |
| θ _β " | Coverage by C _β " (ML) |
| τ | Lifetime of surface alkyl chains |
| τ _m | Lifetime of monomer pool |

¥

Acknowledgements

I would like to thank Dr. Bell for his guidance, interest and constant encouragement throughout the course of my research. I would also like to thank Dr. Theodorou and Dr. Stacy for serving on my dissertation committee.

I am grateful to the members of the Bell group, past and present, for making my stay at Berkeley enjoyable and also for helping me through many crises! A special thanks to Phil, Reha, Rebecca, Gina, Judith, Grant, Rich, Bill, Rick, Mike, Catherine, Narcis, Debbie, Alon, Mark, Larry, Steve, Greg, Kevin, Janet, Ken, Marjorie, Karen, Dean, Bob, Rusty, Nick, Isao, Hiroshi, Takashi, Randy, Craig and Ed.

I would like to thank Wai Ming (Henry) Chan for writing and modifying my GC-MS software and for helping me troubleshoot my electronic equipment woes. Nancy Monroe provided drafting expertise that I am grateful for. Kay and Ferne have helped me with advice and encouragement.

Finally, I am deeply indebted to my parents for their support and encouragement throughout my academic career. My parents-in law have also been a source of strength. Ashok has been a pillar of strength and coped magnificently on the home front. I owe an extra special thank you to Ashok and my son Ananth, who actively kept my spirits up at every stage, and endured my long work hours without (too much) protest.

xiii

Chapter I

Introduction

Fischer-Tropsch synthesis is a route for producing liquid fuels from synthesis gas, a mixture of CO and H₂ (1-3). The most attractive potential sources of synthesis gas are the steam reforming of natural gas (methane) and the gasification of coal. Natural gas is often found in remote locations, and conversion to liquid fuel would facilitate storage, transportation and utilization of this resource. Further, since coal is much more abundant than the natural reserves of liquid hydrocarbons, considerable interest in hydrocarbon synthesis from CO and H₂ has been generated by the need for long-range alternative sources of liquid fuels.

The composition of the products of Fischer-Tropsch synthesis depends on the catalyst employed as well as the reaction conditions, in particular, the pressure, the temperature, and the H_2/CO ratio. The predominant products of Fischer-Tropsch synthesis are linear alkanes and alkenes as well as H_2O or CO_2 . Aldehydes, alcohols, and carboxylic acids are also formed, but in lower concentrations than hydrocarbons.

The group VIII metals Fe, Co and Ru are active for Fischer-Tropsch catalysis. Promoters and supports can also influence the activity and selectivity of a catalyst. Since a broad product distribution of hydrocarbons, ranging from methane to heavy waxes is produced, it is desirable to enhance the selectivity for liquid hydrocarbons. In order to accomplish this goal, research efforts are directed towards a better understanding of the mechanism of the reaction and the elementary surface processes involved in the reaction.

The reaction mechanism can be viewed as a surface polymerization process in which the monomer is produced *in situ* from CO and H₂ on the catalyst surface (2). The products of the reaction often follow an Anderson-Schulz-Flory (ASF) distribution, for which $[C_{n+1}]/[C_n] = \alpha$, where α is independent of chain length, n, and $\alpha < 1$. If it is assumed that polymerization occurs via the addition of a C₁ monomer unit to growing hydrocarbon chains, then α represents the probability of chain growth and is given by $\alpha =$ $r_p/(r_p+r_t)$, where r_p and r_t are the rates of chain propagation and chain termination, respectively. Although the effects of process variables such as reaction temperature and H₂/CO ratio on the product distribution (i. e., α) and overall activity have been wellstudied, the elementary reaction steps that occur during the reaction are not well-understood.

The objective of the present investigation is to better understand the elementary steps that constitute the CO hydrogenation reaction. One goal is to characterize catalyst deactivation and to try and understand the causes of catalyst decay. Isotopic tracers and temperature-programmed surface reaction (4) are used for this purpose. A second goal is to elucidate the mechanism of chain growth during Fischer-Tropsch synthesis. In particular, it is desirable to obtain the rate constants for chain

initiation, propagation and termination and to determine surface coverages by reaction intermediates. Isotopic tracers are combined with transient-response experiments in order to accomplish this aim, since steady-state rate data can only yield product formation rates and distributions (5, 6). Finally, the effect of ethylene addition to the CO/H₂ Fischer-Tropsch synthesis feed on chain initiation and propagation is investigated. Isotopic labelling is used to differentiate between carbon from CO and carbon from ethylene in the product. This further allows the dynamics of ethylene incorporation to be studied.

Ruthenium supported on titania is used in this work for several reasons. Ruthenium has a high specific activity for Fischer-Tropsch synthesis and has high chain growth probabilities at mild reaction conditions (7). A ruthenium catalyst produces mainly straight-chain hydrocarbons, which are believed to be the primary reaction products. Ruthenium does not produce large amounts of oxygenates, thereby simplifying product identification and analysis. Titania is used to support and disperse the ruthenium since titania-supported Group VIII metals are known to be more active than silica- or alumina-supported Group VIII metals (8-11).

This thesis is divided into four parts. Chapter 2 is a study of catalyst deactivation during CO hydrogenation. The dynamics of catalyst deactivation are determined and the role of the build up of carbonaceous species is assessed. The effects of Ru dispersion, TiO_2 phase and TiO_2 surface area on catalyst activity and selectivity are determined. In Chapter 3, expressions are derived for evaluating

the rate coefficients for chain propagation, k_p , and for chain termination, k_t . Chapter 4 describes the use of the isotopic transient technique to evaluate the rate coefficients for chain initiation, propagation, and termination, and the coverages by reaction intermediates. The effects of reaction temperature and the D₂/CO ratio in the feed on rate coefficients and surface coverages are investigated. Chapter 5 describes the effect on chain growth of adding small amounts of ethylene to the CO/H₂ feed.

REFERENCES

- 1. Anderson, R. B., 'The Fischer-Tropsch Synthesis', Academic Press, New York, 1984.
- 2. Biloen, P. and Sachtler, W. M. H., Adv. Catal. 30, 165 (1981).
- 3. Bell, A. T., Catal. Rev.-Sci. Eng. 23, 203 (1981).
- Falconer, J. L. and Schwarz, J. A., *Catal. Rev.-Sci. Eng.* 25, 141 (1983).
- 5. Bennett, C. O., p1, *in* "Catalysis under Transient Conditions", ACS Symposium Series, eds. Bell, A. T. and Hegedus, L. L., 1982.
- 6. Biloen, P., J. Molec. Catal. 21, 17 (1983).
- 7. Vannice, M. A., J. Catal. 37, 449 (1975).
- 8. Vannice, M. A. and Garten, R. L., J. Catal. 56, 236 (1979).
- 9. Vannice, M. A., and Sudhakar, C., J. Phys. Chem. 88, 2429 (1984).
- 10. Reuel, R. C., and Bartholomew, C. H., J. Catal. 85, 78 (1984).
- 11.Rieck, J. S., and Bell, A. T., J. Catal. 99, 262 (1986).
- 12. Jordan, D. S., and Bell, A. T., J. Phys. Chem. 90, 4797 (1986).
- 13.Kellner, C. S., and Bell, A. T., J. Catal. 70, 418 (1971).

Chapter II

An Isotopic Tracer Study of the Deactivation of Ru/TiO₂ Catalysts During Fischer-Tropsch Synthesis

ABSTRACT

An investigation of the causes of catalyst deactivation during Fischer-Tropsch synthesis over Ru/TiO₂ catalysts has been carried out. The effects of Ru dispersion, TiO2 phase, and TiO2 surface area on catalyst activity and selectivity were examined. CO chemisorption capacity and carbon species accumulation were determined as a function of reaction time using isotopic tracer techniques in conjunction with temperature-programmed surface reaction (TPSR). The results of this investigation show that all of the catalysts undergo deactivation with time, with no change in product selectivity. Initially, deactivation is very rapid followed by a slower activity loss. The long-term rate of deactivation is proportional to the initial CO turnover frequency, obtained by extrapolation of the long-term activity data. Deactivation is accompanied by a progressive loss in CO chemisorption capacity as well as an accumulation of various types of carbon species. Carbidic carbon, C_{α} , and alkyl carbon chains, C_{β} , were observed to accumulate as reaction proceeds. C_{β} consists of two species, C_{β} ' which is the precursor to C_{2+} hydrocarbon products and C_{B} " which

consists of longer alkyl chains and does not participate in the production of gas phase products. The rapid initial loss in activity in the first ten minutes correlates with the $C_{\alpha}+C_{\beta}$ accumulation; the long-term loss in CO uptake and catalyst activity are probably due to C_{β} ". The alkyl chains comprising C_{β} " do not undergo hydrogenolysis under reaction conditions, probably due to inaccessibility to hydrogen.

INTRODUCTION

A number of previous investigations have shown that while Ru exhibits a high specific activity for Fischer-Tropsch synthesis, it undergoes a progressive loss in activity that is accompanied by a build-up of carbonaceous species (1-6). Dalla Betta and co-workers (1,2) have ascribed the loss in activity of Ru/Al_2O_3 catalysts to the carbonaceous deposits, and have noted that the original activity of these catalysts could be restored by reduction in H_2 . Similar observations have been reported by Everson et al. (3) and Ekerdt and Bell (4). These authors noted that the rate of deactivation was a function of reaction conditions. Using infrared spectroscopy, Ekerdt and Bell (4) and Yamasaki and co-workers (7) observed the accumulation of hydrocarbon species on the surface under reaction conditions. Ekerdt and Bell (4) concluded that the observed species did not function as reaction intermediates, since these species could only be removed by H_2 reduction in the absence of CO. Reduction of the catalyst following reaction demonstrated that during reaction, the catalyst had accumulated 1-6 Ru ML equivalents of carbon. Based on studies on a Ru/Al₂O₃ catalyst, Bartholomew et al. (6) have proposed a model for the rate of deactivation. According to this model, the rate of deactivation is proportional to the partial pressure of CO and the concentration of active sites. Temperature programmed reaction of the catalyst after reaction produced a spectrum exhibiting two peaks. The first of these peaks occurred at 460 K and corresponded to the removal of 5 ML equivalents of

carbon, whereas the second peak occurred at 685 K and corresponded to the removal of 2.5 ML equivalents of carbon.

Isotopic tracer studies conducted in this laboratory (8-14) have demonstrated that two types of carbon are deposited on the surface of Ru particles supported on SiO₂ and TiO₂. The first is carbidic, or C_{α} , carbon. This species is produced by the dissociation of adsorbed CO and serves as a precursor to methane and C_{2+} hydrocarbons. The second form of carbon consists of short (3-5 carbon atoms) alkyl chains and is designated as C_B. By combining isotopic tracer techniques with temperature programmed reaction, it has been shown that the C_{B} pool of carbon can be divided into two pools. The first of these pools is designated as $C_{\beta}\xspace$, and corresponds to alkyl groups serving as intermediates to the C_{2+} hydrocarbons. The second pool of carbon, designated as C_{B} ", corresponds to longer alkyl chains which are not involved in the formation of reaction products. Under reaction conditions, the coverages of C_{α} and C_{β} ' come to a steady state with time, whereas the accumulation of C_B" increases monotonically. Zhou and Gulari (15) have also found evidence for the presence of C_{α} and C_{β} during CO hydrogenation over $Al_2O_3\text{-supported}$ Ru. The inventory of C_α was observed to go through a maximum with reaction time, whereas the inventory of C_{B} increased monotonically. In a subsequent study (16), the authors speculated that the low activity alkyl species that could be observed by infrared spectroscopy were located on sites surrounded

by adsorbed CO.

The objective of this study was to characterize the deactivation of Ru/TiO_2 catalysts during Fischer-Tropsch synthesis and to identify the causes for the loss in activity. The influence of Ru dispersion, TiO_2 phase, and TiO_2 surface area were considered. The CO chemisorption capacity and the quantity of carbon accumulated were determined as a function of time under reaction conditions. Isotopic tracer techniques were used in conjunction with temperature-programmed surface reaction (TPSR) to study changes in the reactivity of CO and the different forms of carbon accumulated on the catalyst.

EXPERIMENTAL

Four titania supports were used for this study: Degussa P-25 titania, a mixture of 30% rutile and 70% anatase; two anatase supports differing in BET surface area; and rutile. These supports will be referred to as $TiO_2(D)$, $TiO_2(A1)$, $TiO_2(A2)$, and $TiO_2(R)$. TiO₂(A1) is the higher surface area anatase.

 $TiO_2(A1)$ was prepared as follows. Titanium isopropoxide $(Ti(C_3H_7O)_4, Dupont)$ was added dropwise to an excess of isopropyl alcohol at 274 K over a period of 4.5 hours with constant mixing. The resulting slurry was allowed to settle, decanted and washed with distilled water. The decanting and washing was repeated 5-6 times, and the slurry was then filtered and washed several times. The final product was ground and calcined in an O₂ atmosphere. The

preparation of $TiO_2(A2)$ was similar to that of $TiO_2(A1)$, except that the initial step was carried out at 280 K.

 $TiO_2(R)$ was prepared according to the procedure described by Kikuchi *et al.* (16). Titanium tetrachloride (TiCl₄) was added dropwise to hot distilled water at 368K, stirred for 1 hour, and then cooled to ambient temperature. After filtration, precipitated titanium hydroxide was washed with distilled water and filtered again. The washing cycle was repeated several times and finally the precipitate was dried overnight at 383 K. To remove residual chloride impurities, the support was Soxhlet extracted with water and then calcined in pure O₂ at 673 K. Extraction and calcination were repeated three times (18).

The phase structure of each TiO_2 support was confirmed using Raman spectroscopy, since this technique is very sensitive to the phase of TiO_2 and can detect small proportions of anatase in the presence of rutile. By this means, it was established that $TiO_2(R)$ contained no traces of anatase and that $TiO_2(A1)$ and $TiO_2(A2)$ contained no detectable traces of rutile.

Ru was introduced onto each support by incipient wetness impregnation using an aqueous solution of RuCl₃.3H₂O (Strem). The impregnated supports were dried in air at 373 K overnight, and then sieved to -30, +60 mesh. Reduction of the dried products were carried out at 503 K in a flow of pure H₂. The reduction temperature was intentionally kept low to keep the catalyst in its lowtemperature reduced state as much as possible (19). To check for complete conversion of the RuCl₃ to metallic Ru, the chloride

content of each catalyst was determined after reduction. The chloride level in $Ru/TiO_2(D)$ and $Ru/TiO_2(A1)$ was below the detection limit (0.02%). For $Ru/TiO_2(A2)$ and $Ru/TiO_2(R)$, the levels were 0.04% and 0.07% respectively. The weight loading of Ru was determined by X-ray fluorescence.

Table 1 summarizes the physical characteristics of each catalyst. The dispersion of the Ru was determined by H_2 chemisorption at 373 K following a two hour reduction at 473 K. Chemisorption was carried out at 373 K because hydrogen adsorption is known to approach equilibrium slowly at room temperature (20), and equilibrium is attained more rapidly at this temperature (21, 22). A static chemisorption apparatus was used. The isotherms for total and reversible adsorption were determined and the difference between the intercepts at zero pressure was used to estimate hydrogen uptake. The CO chemisorption capacity of Ru was determined by temperature programmed surface reaction in D₂ following reduction at 498 K in pure D₂ for two hours. Further details concerning this procedure are discussed in the Results section. The BET surface area and pore size distribution for each catalyst was determined from N₂ isotherms at 77K.

 H_{2} , CO and He were supplied from a gas flow manifold to a low dead volume quartz microreactor. UHP H_2 (Matheson Gas) or D_2 supplied by U.C.L.B.L. were further purified by passage through a Deoxo unit (Engelhard Industries) and water was removed by a molecular sieve 13X trap. UHP CO (99.999% pure, Matheson Gas) was passed through a glass bead trap at 573 K to remove iron carbonyls,

| ladie |
|-------|
|-------|

| Catalyst | Ru (wt %) | Dispersion (%) | BET (m²/gm) | H uptake (µmoles/gm) | CO/H | pore dia (Å) |
|--------------------------|--------------|-------------------|----------------|-------------------------|------|-----------------|
| Ru/TiO ₂ (D) | 3.3 | 15.5 | 47.5 | 51.1 | 1.3 | 213 |
| Ru/TiO ₂ (A1) | 3.7 | 30.9 | 105.4 | 112.5 | 0.8 | 94 |
| Ru/TiO ₂ (A2) | 3.1 | 40.6 | 76.5 | 125.3 | 0.8 | 120 |
| Ru/TiO ₂ (R) | 6.1 | 30.8 | 46.0 | 186.6 | 2.2 | 167 |

Catalyst characteristics

a

an Ascarite trap to remove CO₂, and finally a molecular sieve trap. UHP He was passed through a molecular sieve trap. 99% ¹³CO (Isotec Inc) was used as supplied.

The products of CO hydrogenation were analysed by gas chromatography using a Perkin Elmer Sigma 3B gas chromatograph equipped with a FID detector. C_1 - C_{14} hydrocarbons were separated on a fused silica capillary column (0.25 mm i.d. x 50m) coated with SE-54 (1 μ m thick). Temperature programming of the column was as follows: 253 K for 5 min, 20 K/min upto 523 K, and then 523K for 10 min. Since the analysis of each loop requires 28.5 min, samples of reaction products were taken as needed, stored at 393 K, and then introduced to the chromatograph after reaction. To accomplish this, the effluent from the reactor was routed through a 10-port, twoposition valve (used either to sample the products or inject the stored sample into the chromatograph) in series with a 16 sampleloop multiposition valve (used to acquire and store the samples). Both valves were contained in heated ovens maintained at 393 K to avoid condensation of products. Operation of both valves was by motor-driven actuators connected to a personal computer (IBM-PC). The microcomputer was programmed to schedule sample acquisition and analysis at desired times. The output from the FID detector was acquired by the computer via an interface and stored at a rate of 2 data points per second.

During a temperature-programmed surface reaction experiment, the reactor effluent was monitored by a mass spectrometer (UTI 100C). The following masses were monitored: 15

(12CH₄), 21 (13CD4), 28 (12CO), 29 (13CO), 44 (12CO₂) and 45 (13 CO₂). Mass spectrometer control and data acquisition were carried out by the personal computer. Using this system each mass intensity could be sampled twice a second.

For each experiment, 0.2 to 0.3 gm of catalyst was loaded in the reactor. The catalyst was then reduced by slowly ramping the temperature in D₂ at 10 K/min to 503 K, and then holding at this temperature for at least two hours. The synthesis of hydrocarbons was carried out at 1 atm using ¹²CO and D₂. All reactions were performed at the following conditions: T = 498K; D₂/CO = 3; P_{CO} = 50 torr; P_{D2} = 150 torr; P_{He} = 560 torr; Q = 150 cc/min. CO conversions on all the catalysts were < 10 %. Activity was followed as a function of reaction time (t_r) by sampling at different times after the start-up of the reaction, and data were collected up to four hours onstream. After reaction, the catalyst was reduced at 503 K overnight.

TPSR experiments were initiated by pretreating the catalyst in one of several ways, as discussed in the Results section. The reactor was flushed with He to remove gas phase reactants and the catalyst was quenched in He to room temperature in under one minute by blowing air over the outside of the reactor. If the uptake of CO was to be determined, the catalyst was exposed to 50 torr of 13 CO in He for 5 min, and then flushed in pure He. The final step in each TPSR experiment was to ramp the catalyst temperature at 0.17 K/s to 503 K in flowing D₂ (50 torr). During this period, the evolution of 13 C labeled products (including 13 CO and 13 CD₄) was

monitored by the mass spectrometer.

RESULTS

Figure 1 shows a plot of the turnover frequency for CO conversion to hydrocarbons, N_{CO} , as a function of time under reaction conditions, for each of the four catalysts. N_{CO} was determined by summing the rate of formation of C₁ through C₁₄ hydrocarbons weighted by the carbon number and dividing this sum by the moles of surface Ru atoms determined by hydrogen chemisorption. Each of the catalysts exhibits a rapid initial loss in activity which is then followed by a much slower decline. The initial activity could be restored by D₂ reduction at 498 K and the plots of N_{CO} versus time could be reproduced over several cycles of reduction and reaction. It was also observed that the room temperature uptake of CO after reduction of the partially deactivated catalysts was identical to that prior to reaction.

The initial activity at $t_r = 1$ min for Ru/TiO₂(D), Ru/TiO₂(A1) and Ru/TiO₂(A2) exhibits an inverse linear correlation with Ru dispersion, as shown in Fig. 2. The point for Ru/TiO₂(R) lies well below the correlation. For $t_r > 20$ min, the loss in activity can be fit by an exponential function, $N_{CO}=N_{CO}\circ\exp(-t_r/\tau)$, where $N_{CO}\circ$ is the apparent initial activity at $t_r = 0$ min and τ is the time constant for deactivation. The values of τ are 310 min for Ru/TiO₂(D), 420 min for Ru/TiO₂(A1), 500 min for Ru/TiO₂(A2) and 714 min for

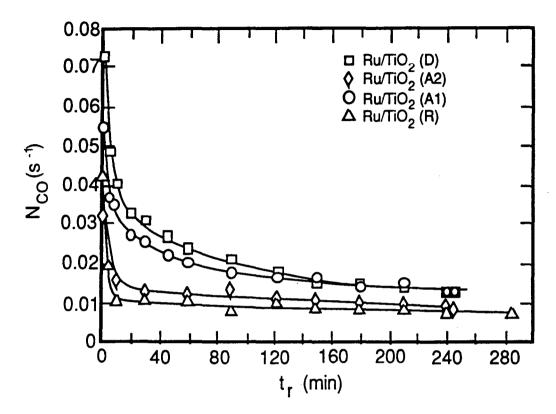


Fig. 1 CO turnover frequency as a function of reaction time. Reaction Conditions: $P_{D2} = 150$ torr, $P_{CO} = 50$ torr, T = 498 K.

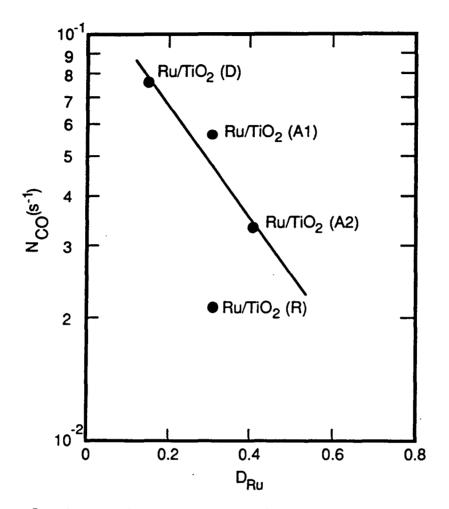


Fig. 2 Catalyst activity at 1 min after reaction start up versus ruthenium dispersion.

Ru/TiO₂(R). Figure 3 shows that a linear correlation exists between τ^{-1} and N_{CO}⁰, which suggests that whetever causes the slow deactivation of the catalyst is produced by the catalyst itself.

Figure 4 shows an Anderson-Schulz-Flory (23) plot of the distribution of C₁ through C₁₄ hydrocarbons for $t_r = 5$ min and $t_r = 120$ min for Ru/TiO₂(D). It is evident that the carbon number distribution of products is not strongly affected by deactivation. Similar observations were also made for the other three catalysts. Moreover, for all four catalysts, the probability of chain growth, α , was found to be 0.7 ± 0.01 , indicating that α is independent of Ru dispersion and support properties (i.e., TiO₂ phase and surface area). The effects of reaction time on the proportions of total olefins, internal olefins, and branched products was examined at each carbon number between 2 and 7. For a given carbon number, the fraction of α -olefins was observed to rise during the first 10 min, at the same time that the fraction of β -olefins declined by an equivalent amount; however, neither the proportion of total olefins nor the proportion of branched products changed significantly with reaction time.

The CO adsorption capacity of each catalyst was measured both prior to the onset of reaction and after progressively longer periods of time under reaction conditions. The CO uptake of a freshly reduced catalyst was determined by exposing it to 13CO at room temperature for 5 min, flushing the catalyst with He for 15 min and then carrying out a temperature-programmed surface reaction in D₂. A peak of 13CD₄ was observed. To estimate the CO

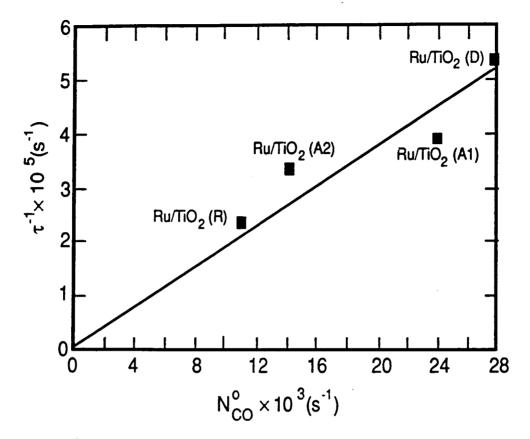


Fig. 3 Correlation of the inverse of the deactivation time constant with the CO turnover frequency at $t_r = 0$ obtained by extrapolation of the N_{CO} versus t_r curve for t_r ≥ 20 min.

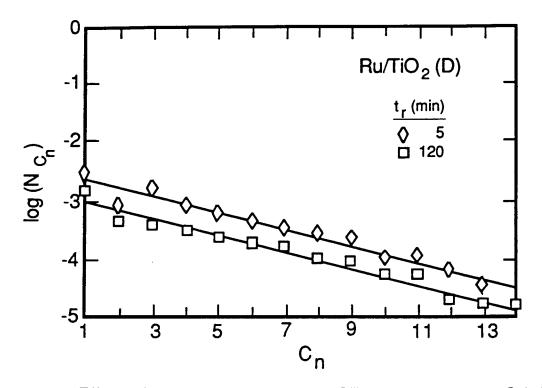
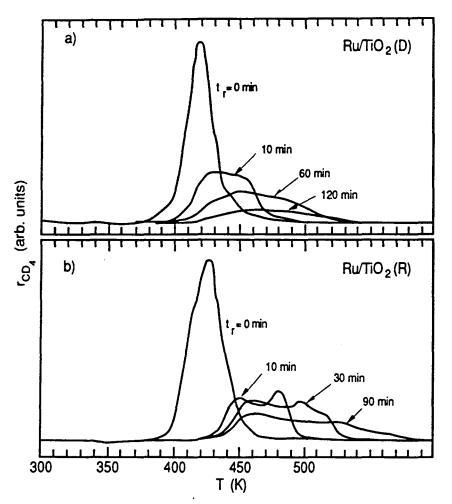


Fig. 4 Effect of reaction time on the ASF plot (log N_{Cn} vs C_n) for Ru/TiO₂(D). N_{Cn} is the turnover frequency for products of carbon number n.

adsorption capacity after reaction, reaction was carried out in a mixture of $12CO/D_2$ for a specified time after which the catalyst was cooled abruptly to room temperature in flowing He. The 12CO remaining on the catalyst surface was displaced by exposing the catalyst to 13CO for 5 min. The catalyst was then flushed in He for 15 min and a temperature-programmed surface reaction was carried out in flowing D₂.

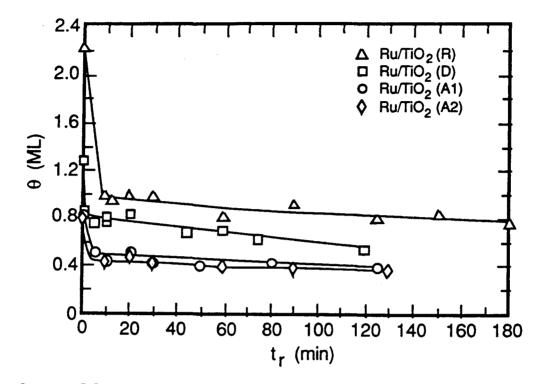
The only 1³C-labeled product observed during the temperatureprogrammed surface reaction of adsorbed 1³CO was 1³CD₄. As can be seen in Fig. 5, the amount of 1³CD₄ formed decreases with increasing t_r. This change is accompanied by a progressive upscale shift in the temperature of the maximum rate of 1³CD₄ formation. It is also apparent, particularly for Ru/TiO₂(R), that the 1³CD₄ spectrum for t_r > 0 consists of two or more overlapping peaks. The apparent activation energy for the reduction of adsorbed 1³CO was estimated from a plot of the log of the initial rate of 1³CD₄ formation versus inverse temperature. A value of 30 ± 2.5 kcal/mol was obtained for all of the catalysts, independent of t_r.

The area under the ${}^{13}CD_4$ peaks obtained during temperatureprogrammed surface reaction of ${}^{13}CO$ is taken as the measure of the CO adsorption capacity of Ru. Figure 6 shows that as t_r increases, the CO adsorption capacity of each of the four catalysts decreases rapidly and then declines more slowly for t_r ≥ 5 min. As can be seen from Table 2, the time constants for the slow loss of CO adsorption capacity are virtually identical to those for the slow loss in CO hydrogenation activity.

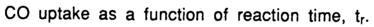




¹³C TPSR spectra to estimate CO uptake as a function of t_r. a. Data for Ru/TiO₂(D). b. Data for Ru/TiO₂(R). Reaction Conditions: P_{D2} = 150 torr, P_{CO} = 50 torr, T = 498 K. Gas Introduction sequence: ¹²CO + D₂ (t_r) \rightarrow He (cool) \rightarrow ¹³CO (5 min) \rightarrow D₂ (TPSR). In the TPSR spectra, the temperature is raised from room temperature to 503 K at 0.17 K/sec and then maintained constant at 503 K.







| Ta | ble | 2 |
|----|-----|---|
|----|-----|---|

Comparison of the time constants for the decay in N_{CO} with that for the decay in $\theta_{CO},$ for t_r > 20 min

| Catalyst | N _{CO} decay (min) | θ _{CO} decay (min) |
|--------------------------|--------------------------------|--------------------------------|
| Ru/TiO ₂ (D) | 310 | 306 |
| Ru/TiO ₂ (A1) | 420 | 476 |
| Ru/TiO ₂ (A2) | 500 | 550 |
| Ru/TiO ₂ (R) | 714 | 715 |

•

.

*

Additional experiments were performed to determine the cause of the immediate loss of CO chemisorption capacity upon initiation of CO hydrogenation. The freshly reduced catalyst was exposed to 13CO at room temperature for 5 min, flushed in He for 5 min, and then contacted with 12CO in He for 5 min to exchange off all the adsorbed ¹³CO. The catalyst was then flushed with He and TPSR in D_2 /He was initiated. A pulse of ${}^{13}CO_2$ was observed when the catalyst contacted with 13CO, and a peak of 13CD₄ was observed during TPSR. Both of these observations suggest that some of the adsorbed ¹³CO disproportionates via the reaction: $2CO_s \rightarrow C_s + CO_2(g)$. As shown in Table 3, the amount of ¹³C_s deposited by CO disproportionation correlates well with the immediate loss of CO chemisorption capacity observed upon initiation of CO hydrogenation over Ru/TiO₂(D), Ru/TiO₂(A1), and Ru/TiO₂(A2). Similar results have been reported by Yamasaki et al. (7) who observed that CO disproportionation caused a reduction in the extent of CO adsorption. For $Ru/TiO_2(R)$, the loss in CO chemisorption capacity is much greater than the amount of carbon deposited by room-temperature disproportionation of CO. It is also observed that the amount of carbon deposited on $Ru/TiO_2(R)$ by CO disproportionation is significantly less than that deposited on the other three catalysts.

The accumulation of carbonaceous species on the catalyst was determined using the following procedure. Reaction was run for a specified duration using a feed mixture of ^{13}CO and D_2 . The catalyst was then exposed for 30 s to ^{12}CO in He, to exchange the adsorbed ^{13}CO for ^{12}CO (13), after which the catalyst was rapidly cooled to

| Та | ble | 3 |
|----|-----|---|
|----|-----|---|

Comparison of the initial Loss in θ_{CO} with that due to room temperature disproportionation of CO

| Catalyst | Loss on running reaction (ML) | Room Temp. disprop. CO (ML) |
|--------------------------|----------------------------------|--------------------------------|
| Ru/TiO ₂ (D) | 0.45 | 0.47 |
| Ru/TiO ₂ (A1) | 0.33 | 0.27 |
| Ru/TiO ₂ (A2) | 0.35 | 0.34 |
| Ru/TiO ₂ (R) | 1.23 | 0.13 |

.

.

room temperature in flowing He. Temperature-programmed surface reaction was then carried out in flowing D₂ and the formation of ${}^{13}CD_4$ was monitored as a function of time. Spectrum b in Fig. 7 shows the rate of ${}^{13}CD_4$ formation versus the temperature for the case of Ru/TiO₂(D). Spectrum a shows the rate of ${}^{13}CD_4$ formation if the exchange of adsorbed ${}^{13}CO$ for ${}^{12}CO$ is eliminated from the procedure. The area under spectrum b corresponds to the total amount of carbonaceous species present on the catalyst, namely, the sum of C_{α} and C_{β}, whereas the area under spectrum a also includes the amount of chemisorbed CO.

*

As discussed by Yokomizo et al. (14), the C_{β} pool of carbon can be subdivided into two pools: a C_{β} ' pool corresponding to alkyl precursors to C_{2+} products and a C_{β} " pool corresponding to alkyl groups produced by reaction, but not associated with the formation of C_{2+} products. The amount of C_{β} " was determined using the following procedure. The reaction was run in a mixture of 1³CO and D_2 for a time t_r . The feed was then switched to a mixture of 1²CO and D_2 for 2 min. Experiments performed to determine the reaction time required for the latter step showed that within 2 min, the adsorbed 1³CO would be displaced by 1²CO and all the 13-labeled carbon in the C_{α} and C_{β} ' pools would be replaced by 1²C, but that the 1³C carbon in the C_{β} " pool would remain. After reaction in the 1²CO/D₂ mixture, the catalyst was rapidly cooled to room temperature in He, and a temperature-programmed surface reaction

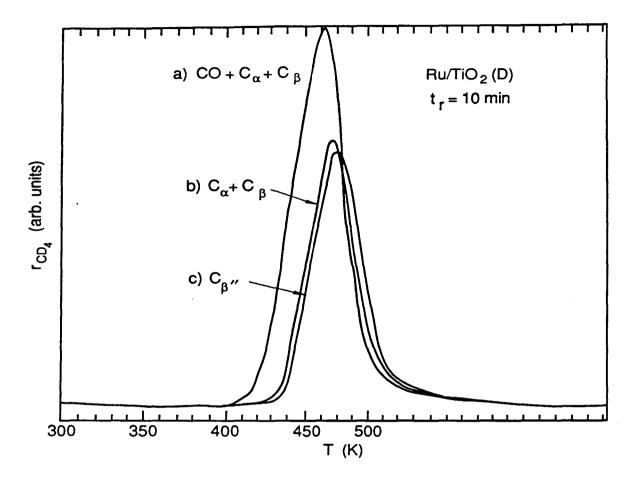


Fig. 7 ¹³C TPSR spectra to estimate carbon accumulation on the catalyst at $t_r = 10$ min, standard reaction conditions. a. $CO + C_{\alpha} + C_{\beta}$. Gas Introduction sequence: ¹³CO + D₂ (10 min) \rightarrow He (cool) \rightarrow D₂ (TPSR). b. $C_{\alpha} + C_{\beta}$: Gas Introduction sequence: ¹³CO + D₂ (10 min) \rightarrow ¹²CO + He (30 s) \rightarrow He (cool) D₂ (TPSR). c. C_{β} ". Gas Introduction sequence: ¹³CO + D₂ (10 min) \rightarrow ¹²CO + D₂ (2 min) \rightarrow He (cool) \rightarrow D₂ (TPSR). In the TPSR spectra, the temperature is raised from room temperature to 503 K at 0.17 K/sec and then maintained constant at 503 K. was then carried out in flowing D₂. Spectrum c in Fig. 7 shows the resulting trace of ${}^{13}CD_4$ formation as a function of temperature. The small difference in the areas under spectra c and b represents the amount of $C_{\alpha}+C_{\beta}$ ' carbon accumulated on the catalyst. Figure 8 shows that the amount of C_{β} " builds up monotonically as t_r increases.

The accumulation of C_{α} , C_{β} ', and C_{β} " during the first 20 min of reaction are shown in Fig. 9. It is evident that the surface concentration of C_{α} and C_{β} ' is less than 1 ML in most cases. For Ru/TiO₂(R), RuTiO₂(A1) and Ru/TiO₂(D), the accumulation of these forms of carbon passes through a maximum as t_r increases. Much larger quantities of C_{β} " are formed on the catalyst surface and these species increase in quantity monotonically, and after 20 min of reaction can be as high as 7 ML equivalents. The time constant for the build up of $C_{\alpha}+C_{\beta}$ during the first 10 min of reaction is listed in Table 4 and is compared with the time constant for the loss in CO hydrogenation activity during the same period. It is apparent that the time constants for the two phenomena are virtually identical, suggesting that the loss in CO hydrogenation activity during the initial stages of reaction can be attributed to the rapid buildup of C_{α} and C_{β} on the catalyst surface.

DISCUSSION

Previous investigations have shown that the specific activity

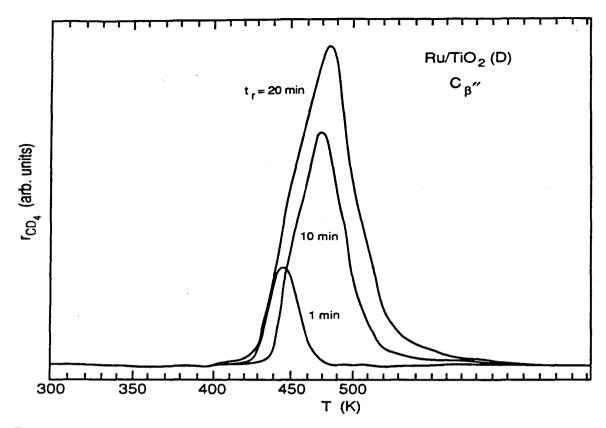


Fig. 8 ¹³C TPSR spectra for C_β^{*} with varying reaction time t_r. Gas introduction sequence: ¹³CO + D₂ (t_r) \rightarrow ¹²CO + D₂ (2 min) \rightarrow He(cool) \rightarrow D₂ (TPSR). In the TPSR spectra, the temperature is raised from room temperature to 503 K at 0.17 K/sec and then maintained constant at 503 K.

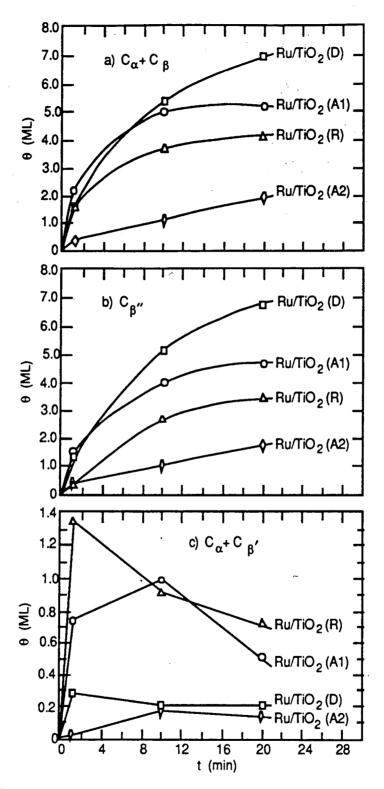


Fig. 9 Coverages of carbon species obtained from 13C TPSR as a function of reaction time. a. $C_{\alpha} + C_{\beta}$. b. C_{β} ". c. $C_{\alpha} + C_{\beta}$ '.

| Tat | le | 4 |
|-----|----|---|
|-----|----|---|

Comparison of the time constants for the accumulation of C_{α} +C_{\beta} with that for the decay in N_{CO} during the first 10 min under reaction conditions

| Catalyst | (Cα+Cβ) (min) | N _{CO} (min) |
|--------------------------|------------------|--------------------------|
| Ru/TiO ₂ (D) | 6.1 | 6.3 |
| Ru/TiO ₂ (A1) | 8.3 | 8.7 |
| Ru/TiO ₂ (A2) | 6.2 | 7.8 |
| Ru/TiO ₂ (R) | 8.3 | 8.3 |
| | | |

of Ru for Fischer-Tropsch synthesis decreases with increasing Ru dispersion (24, 25). A similar trend has been observed in the present study for the CO turnover frequency measured after 1 min and for the turnover frequency determined by extrapolation of the slowly deactivating portion of the activity versus time plots (see Fig. 1). As can be seen in Fig. 2, with the exception of the point for Ru/TiO₂(R), all of the data fall along a single line, suggesting that the surface area of titania does not affect the specific activity of Ru. The deviation of the point for $Ru/TiO_2(R)$ is believed to be due to the higher chloride content of this catalyst relative to the other three. CI impurities can inhibit the catalytic activity of Ru for CO hydrogenation (26). lyagba et al. (26) have shown that for a fixed Ru dispersion, the turnover frequency for CO hydrogenation decreases with increasing initial levels of chloride impurity. Based on their results, it is estimated that the CI impurity in the $Ru/TiO_2(R)$ catalyst could be expected to reduce the activity of this catalyst by about a factor of 2. This is nearly the same as the ratio of turnover frequencies for Ru/TiO₂(A1) and Ru/TiO₂(R), which have identical dispersions.

To determine whether the decrease in turnover frequency with increasing Ru dispersion is dependent on the support composition, a comparison was made between Ru/TiO_2 and Ru/Al_2O_3 catalysts. Figure 10 shows the turnover frequencies for methane obtained in the present study and similar results obtained by Kellner and Bell (25) using Ru/Al_2O_3 catalysts. It is evident that the slopes of the two sets of data are identical, indicating that the decrease in turnover frequency with increasing dispersion is an intrinsic function of the Ru particle size, independent of the support composition. Figure 10 shows as well that at a fixed Ru dispersion, the methane turnover frequency is 2 times higher for titaniasupported Ru than for alumina-supported Ru. Since the weight ratio of C_{2+} products to methane is roughly a factor of five higher for the titania supported catalysts, this means that the CO turnover frequency for the titania-supported catalysts is approximately a factor of ten higher than that for alumina-supported Ru.

The higher activity of TiO₂-supported Ru to Al₂O₃-supported Ru can be attributed to effects of highly active sites located at the boundaries of TiO_x islands located on the Ru metal surface. XPS studies (27) have suggested that the partial reduction of TiO₂ produces Ti³⁺ sites which can then interact with the oxygen of CO adsorbed on metal atoms immediately adjacent to the Ti³⁺ ions. This mode of CO adsorption has been proposed to weaken the C-O bond, and hence facilitate its cleavage, an important first step in CO hydrogenation (28-34). The TiO_x coverage is independent of Ru dispersion.

Kellner and Bell (25) have attributed the decrease in specific activity with increasing Ru dispersion to a geometric effect. They note that an essential step in the hydrogenation of CO to hydrocarbons is the dissociation of adsorbed CO. Indirect evidence suggests that this process occurs preferentially on flat metal surfaces, rather than on low coordination sites occurring at the corners and edges of metal particles (35, 36). Since the proportion

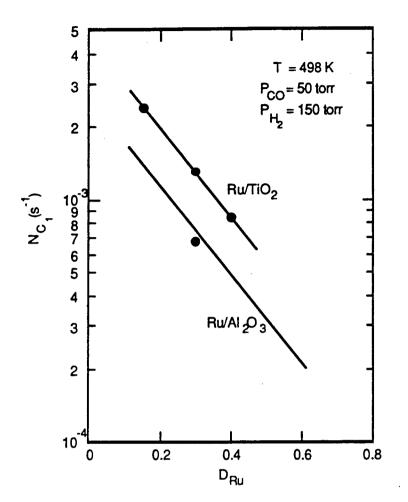


Fig. 10 Comparison of methane turnover frequency from this work over Ru/TiO₂ and Ru/Al₂O₃ (25). All data are based on measurements made using a H₂/CO feed mixture.

of surface metal sites occurring on flat planes decreases with increasing metal dispersion, it is possible to explain the results shown in Fig. 10. The postulation of CO dissociation as a ratedetermining step in CO hydrogenation is also consistent with the observed distribution of products. As noted in the preceding section, the probability of chain growth, α , is independent of Ru dispersion. This together with the absence of any effect of dispersion on the olefin to paraffin ratio or the extent of chain branching suggest that the only step in the reaction sequence affected by Ru particle size is the initial process of CO dissociation.

The importance of CO dissociation in CO hydrogenation is also borne out by the observation that the room-temperature disproportionation of CO is most extensive on the catalyst exhibiting the highest initial activity, Ru/TiO₂(D), and is least extensive on the catalyst with the lowest initial activity, Ru/TiO₂(R) (see Table 3). Furthermore, the observation of roomtemperature CO disproportionation on Ru/TiO₂ indicates a higher activity for these catalysts compared to silica-supported Ni, Co, and Ru, which require temperatures of at least 423 K (37).

All four Ru/TiO_2 catalysts exhibit very similar deactivation behavior with time under reaction conditions. There is a very rapid loss of activity during the first 20 min or so, whereafter the activity declines much more slowly. Deactivation does not change the product carbon number distribution; the product selectivity is independent of the degree of deactivation, the dispersion of Ru, and the phase of the titania support. Comparison of the data in Figs. 1

and 6 shows that the loss in synthesis activity is accompanied by a loss in CO chemisorption capacity. Hydrogen reduction of the catalyst fully restores the initial activity of the catalysts as well as their CO chemisorption capacity. What this indicates is that the loss in activity is reversible and does not appear to be associated with a decrease in metal dispersion.

For very short reaction times ($t_r \leq 1$ min), the loss in Ru activity can be attributed to the accumulation of C_{α} . As noted earlier, this species is a precursor to the formation of hydrocarbons. However, the increase in coverage of C_{α} will result in a loss in CO chemisorption capacity. This is also shown in Table 3. Hoffmann and Robbins (38) have also observed a loss in CO chemisorption capacity during CO hydrogenation over Ru (001) due to the formation of surface carbon. Figure 9c shows, though, that the coverage of C_{α} + C_{B} ' rapidly passes through a maximum with reaction time. For reaction times longer than a few minutes, the coverage by C_B" becomes significant, and it is probably this species which is primarily responsible for the loss in catalytic activity and CO chemisorption capacity at longer reaction times. The TPSR spectra presented in Fig. 8 indicate that C₈ does not undergo hydrogenolysis until much of the chemisorbed CO has been removed from the surface, in agreement with earlier observations by Kobori et al. (39) and Zhou and Gulari (16). It has been proposed (16, 40, 41) that the stability of alkyl groups in the C_{B} " pool is due to the stabilization of CO adsorbed on the same, or nearby, sites. It is interesting to note

in this context that White and coworkers (40) have reported a similar stabilization of ethylidyne by adsorbed CO on a Ni(111) surface.

The loss in catalytic activity for longer reaction times is attributed to the progressive accumulation of C_{α} and C_{β} . This explanation is suggested by the similarity in the time constants for the accumulation of C_{α} and C_{β} , and the time constant for deactivation during the first 10 min of reaction (see Table 4). While the results of the present study do not provide direct evidence of a correlation between activity loss and the accumulation of carbon for reaction times in excess of 20 min, one can infer such a relationship from the observed correlation between the loss in CO chemisorption capacity and activity (see Table 2), since the loss in CO chemisorption capacity is ascribable to the accumulation of carbonaceous species.

Further support for the idea that the slow deactivation is due to species produced by the catalyst can be drawn from Fig. 3. This figure shows that the rate of deactivation for $t_r > 20$ min increases linearly with the turnover frequency of the catalyst. For Ru/TiO₂(D), Ru/TiO₂(A1) and Ru/TiO₂(A2), the differences in the turnover frequency are due to differences in Ru dispersion (see Fig. 2). As discussed above, the lower than anticipated activity of Ru/TiO₂(R) is attributed to the higher initial Cl impurity of this catalyst relative to the other three investigated.

The observed pattern of deactivation and loss in CO chemisorption capacity can be represented qualitatively by the

following sequence of steps.

$$\begin{array}{ccc} \mathsf{K} & \mathsf{k}_1 & \mathsf{k}_2 \\ \mathsf{CO}_{\mathsf{g}} \rightleftharpoons \mathsf{CO}_{\mathsf{s}} \to \mathsf{C}_{\alpha} \to \mathsf{P} \\ & \downarrow \mathsf{k}_3 \\ & \mathsf{C}_{\beta}^{\mathsf{*}} \end{array}$$

The first step is the reversible, nondissociative adsorption of CO. Isotopic tracer studies (8, 13, 42) have shown that this step can be assumed to be at equilibrium under reaction conditions. Dissociation of adsorbed CO produces C_{α} , which is viewed in the above scheme as a precursor to both hydrocarbon products and C_{β} ". The accumulation of C_{β} " is assumed to reduce the fraction of metal sites available for CO adsorption and hence will inhibit the rate at which products are formed.

The general features of the proposed scheme are also supported by isotopic tracer studies conducted using Ru/SiO₂ (9, 11), Ru/Al₂O₃ (15), and Ru/TiO₂ (14). In as much as the work carried out with Ru/TiO₂ (14) has shown the surface coverage by C_{β} ' to be small relative to C_{α} and C_{β} ", the presence of C_{β} ' is not indicated explicitly in the proposed scheme, and in the analysis of the dynamics of carbon accumulation on the catalyst surface presented below, the coverage by C_{β} ' is included implicitly with that by C_{α} . As written, the proposed scheme assumes that the coverage of the catalyst by hydrogen is time independent. In one tracer study, Wislow and Bell (10) observed close to monolayer coverages of both CO and D₂ on an unsupported Ru catalyst under reaction conditions, indicating that CO and D₂ chemisorb on different sites.

Expressions for the rate of product formation and for the coverage of the catalyst surface by CO, C_{α} , and C_{β} " can be derived on the basis of the reaction scheme presented above. The rate of product formation can be expressed as

$$N_{\rm CO} = k_2 \theta_{\alpha} \tag{1}$$

The coverage of the surface by CO, C_{α} , and C_{β} " is governed by the following relationships

$$\theta_{\rm CO} = \frac{{\rm KP}_{\rm CO}(1-\theta_{\alpha}-\theta_{\beta}^{"})}{1+{\rm KP}_{\rm CO}}$$
(2)

$$\frac{d\theta_{\alpha}}{dt} = k_1 \theta_{CO} \cdot (k_2 + k_3) \theta_{\alpha}$$
(3)

$$\frac{d\theta_{\beta}''}{dt} = k_3 \theta_{\alpha}$$
(4)

where θ_{CO} , θ_{α} , and θ_{β} " are the coverages of CO, C_{α} , and C_{β} ", respectively; P_{CO} is the partial pressure of CO; K is the equilibrium constant for CO adsorption; and k_i is the rate coefficient for reaction i. The initial conditions for eqns. 3 and 4 are $\theta_{\alpha} = \theta_{\beta}$ " = 0.

Assuming that KP_{CO} >> 1, the time dependences of θ_{α} and θ_{β} " are given by

$$\theta_{\alpha}(t) = \frac{k_1(\exp(m_1 t) - \exp(m_2 t))}{\sqrt{(k_1 + k_2 + k_3)^2 - 4k_1 k_3}}$$
(5)

and

$$\theta_{\beta}^{"}(t) = 1 + \frac{k_1 k_3 (\frac{\exp(m_1 t)}{m_1} - \frac{\exp(m_2 t)}{m_2})}{\sqrt{(k_1 + k_2 + k_3)^2 - 4k_1 k_3}}$$
(6)

where

$$m_1, m_2 = \frac{-(k_1 + k_2 + k_3) \pm \sqrt{(k_1 + k_2 + k_3)^2 - 4k_1 k_3}}{2} \quad \text{and } m_1 > m_2$$

Substitution of eqns. 5 and 6 into eqn. 2 gives

$$\theta_{CO}(t) = \frac{k_1}{\sqrt{(k_1 + k_2 + k_3)^2 - 4k_1k_3}} \left(\exp(m_2 t) (1 + \frac{k_3}{m_2}) - \exp(m_1 t) (1 + \frac{k_3}{m_1}) \right)$$
(7)

and

$$\frac{N_{CO}(t)}{\theta_{CO}(t)} = \frac{k_2(\exp(m_1 t) - \exp(m_2 t))}{(\exp(m_2 t)(1 + \frac{k_3}{m_2}) - \exp(m_1 t)(1 + \frac{k_3}{m_1}))}$$
(8)

Plots of N_{CO}/θ_{CO} , θ_{CO} , θ_{α} , and θ_{β} " are shown in Fig. 11. The values of the three rate coefficients used to generate these plots were selected to be representative of the dynamics observed in the experiments reported here. Comparison of the curves shown in Fig. 11 with the data shown in Figs. 6 and 9 shows a number of similarities. The coverage of CO decreases very rapidly during the first two to three minutes and then decays more slowly. This

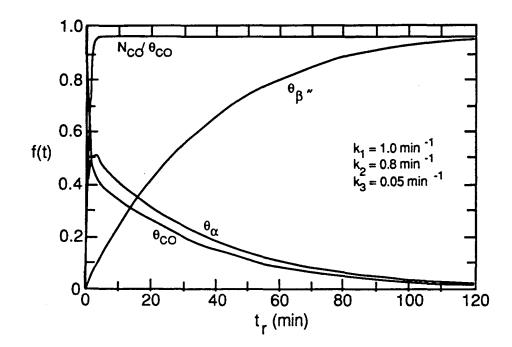


Fig. 11 Model curves for N_{CO}/θ_{CO} , θ_{α} , θ_{CO} , and θ_{β} " as a function of reaction time.

pattern can be attributed to the rapid initial build up of $(C_{\alpha} + C_{\beta})$ and the subsequently slower build up of C_{β} ". In agreement with experimental observation, the coverage by $(C_{\alpha} + C_{\beta})$ passes through a maximum within the first few minutes of reaction, whereas the coverage by C_{β} " rises monotonically. The ratio N_{CO}/θ_{CO} rises rapidly to a fixed value which remains constant thereafter, in agreement with the observation that N_{CO} and θ_{CO} decline concurrently at $t_r \ge 10$ minutes.

The proposed model assumes that hydrogen chemisorption is not affected by the process of reaction and subsequent slow reduction in adsorbed CO on the catalyst surface. There is also an implicit assumption in the model that the chain length of the C_{B} " is time independent. Analysis of our data indicates that the ratio of the average chain length of the accumulated carbon at 10 min of reaction to that at 1 min after the start-up of reaction is 2.8 ± 0.6 , while the ratio estimated between 20 min and 10 min is only 1.3 This indicates that the average chain length rises rapidly and ±0.3. then at a slower rate as reaction proceeds. A similar pattern has also been observed recently by Zhou and Gulari (16) for Ru/Al_2O_3 . One can, therefore, envision a scenario in which the number of Ru surface sites blocked by each unit of \hat{C}_{B} " decreases with time. During a period of rapidly increasing chain length (i. e., shortly after the start-up of reaction) the assumption of a constant chain length would lead to an overestimation of the effects of C_B" accumulation and, hence, to an underestimation in θ_{CO} . Despite these simplifying

assumptions, the model does qualitatively describe experimental observations.

Finally, one might ask whether the observed loss in activity might be due to the progressive accumulation of wax either on the surface of Ru particles or in the catalyst pores. To address this question, estimates were made of the wax accumulation after 2 h of reaction. The carbon number threshold for condensation of wax was determined using an extrapolation of the measured ASF distribution together with the Kelvin equation and known vapor pressures of alkanes. For the conditions of the present experiments, it was found that all products with 28 carbon atoms or more would condense in 10 Å pores, whereas all products with 83 carbon atoms or more would condense in 100 Å pores. The total wax accumulation could then be calculated for each catalyst using the measured pore size distribution. By this means, it was found that the wax could occupy between 0.06-0.55% of the pore volume in the four catalysts studied. If the wax is assumed to cover the Ru particles in a maximal fashion, then it is estimated that between 3% and 7% of the exposed Ru sites would be covered. These figures are to be compared with fractional activity losses of 23-46% over the same period of time. This suggests that wax accumulation cannot account for a significant part of the loss in activity under the conditions used in this study. Of further note is the fact that the estimated amount of wax accumulation is only 1-4% of the amount of carbon removed from the catalyst surface after reaction.

CONCLUSIONS

Titania-supported Ru catalysts undergo deactivation during CO hydrogenation, but exhibit no change in product selectivity with time onstream. The initial activity can be restored by reduction in H_2 or D_2 and there is no evidence of metal sintering due to reaction. The rate of deactivation is most rapid during the first 20 min after the startup of reaction and declines to a much smaller rate for reaction times longer than 20 min. The long-term rate of deactivation is proportional to the activity of the catalyst, obtained by extrapolation of the long-term activity data. The loss in activity is paralleled by a loss in CO chemisorption capacity, and for reaction times longer than 20 min, the ratio of the CO turnover frequency to the CO coverage remains constant. Differences in the initial activity of Ru supported on Degussa P-25 and anatase can be attributed to differences in Ru dispersion, with higher dispersion contributing to a decrease in CO turnover frequency. For the same dispersion, Ru supported on rutile exhibits a two to threefold lower activity than Ru supported on anatase. The lower activity of rutilesupported Ru is attributed to the higher level of chloride impurity on rutile versus anatase. The formation of highly active sites at the boundaries of TiO_x islands located on the metal surface is proposed to be the cause for the higher activity of TiO₂-supported Ru, compared to SiO₂- or Al₂O₃-supported Ru.

Temperature-programmed surface reaction experiments show evidence of the accumulation of carbidic, C_{α} , and alkyl, C_{β} , carbon on

the catalyst surface. The catalyst inventory of $(C_{\alpha} + C_{\beta})$ increases, passes through a maximum, and then decreases as the catalyst loses activity. On the other hand, the inventory of C_{B} " increases monotonically with reaction time. The accumulation of both C_{α} and C_B carbon results in a reduction in the CO chemisorption capacity of the catalyst. The immediate loss in CO uptake after reaction startup is attributed to the buildup of C_{α} . The rapid loss in activity in the first ten minutes correlates with the buildup of C_{α} and C_{β} , whereas the slower loss in activity is ascribed to the accumulation of C_{B} ". The alkyl chains comprising the C_{B} pool of carbon do not undergo extensive hydrogenolysis under reaction conditions, very likely due to inaccessibility of the chains to hydrogen as a result of CO adsorbed on adjacent sites. A model has been proposed that qualitatively agrees with the experimental obseravtions of changes in activity, CO uptake, and the accumulation of reactive and unreactive carbon species on the catalyst surface as reaction proceeds.

REFERENCES

- 1. Dalla Betta, R. A., Piken, A. G., and Shelef, M., *J. Catal.* **35**, 54 (1974).
- 2. Dalla Betta, R. A., Piken, A. G., and Shelef, M., *J. Catal.* **40**, 173 (1975).
- 3. Everson, R. C., Woodburn, E. T., and Kirk, A. R. M., J. Catal. 53,

186 (1978).

- 4. Ekerdt, J. G., and Bell, A. T., *J. Catal.* **58**,170 (1979).
- 5. Moeller, A. D., and Bartholomew, C. H., *Ind. Eng. Chem. Prod. Res. Dev.* **21**, 390 (1982).
- 6. Bowman, R. M., and Bartholomew, C. H., *Appl. Catal.* **7**,179 (1983).
- 7. Yamasaki, H., Kobori, Y., Naito, S., Onishi, T., and Tamaru, K., J. *Chem. Soc., Far. Trans.* **177**, 2913 (1981).
- 8. Cant, N. W., and Bell, A. T., J. Catal. 73, 257 (1982).
- 9. Winslow, P., and Bell, A. T., J. Catal. 86, 158 (1984).
- 10. Winslow, P., and Bell, A. T., J. Catal. 91, 142 (1985).
- 11. Duncan, T. M., Winslow, P., and Bell, A. T., J. Catal. 93, 1 (1985).
- Duncan, T. M., Reimer, J. A., Winslow, P., and Bell, A. T., J. Catal.
 93, 305 (1985).
- 13. Winslow, P., and Bell, A. T., J. Catal. 94, 385 (1985).
- 14. Yokomizo, G. H., and Bell, A. T., J. Catal. 119, 467 (1989).
- 15. Zhou, X., and Gulari, E., J. Catal. 105, 499 (1987).
- 16. Zhou, X., and Gulari, E., Langmuir 4, 1132 (1988).
- 17. Kikuchi, E., Matsumoto, N., Takahashi, T., Machino, A., and Morita, Y., *Appl. Catal.* **10**, 251 (1984).
- 18. Parfitt, G. D., Trans. Far. Soc. 67, 2469 (1971).
- Tauster, S. J., Fung, S. C., and Garten, R. L., *J. Amer. Chem. Soc.* 100, 170 (1978).
- 20. Dalla Betta, R. A., J. Catal. 34, 57 (1974).
- 21. Taylor, K. C., J. Catal. 38, 299 (1975).
- 22. Kubicka, H., React. Kin. Cat. Lett. 5, 223 (1976).
- 23. Anderson, R. B., in "The Fischer-Tropsch Synthesis," Academic

Press, New York, 1984.

- 24. King, D. L., J. Catal. 61, 77 (1980).
- 25. Kellner, C. S., and Bell, A. T., J. Catal. 75, 251 (1982).
- 26. Iyagba, E. J., Hoost, T. E., Nwalor, J. U., and Goodwin, J. G., J. *Catal.* **123**, 1 (1990).
- 27. Levin, M. E., Salmeron, M., Bell, A. T., and Somorjai, G. A., Surf. Sci. 195, 429 (1988).
- 28. Bracey, J. D., and Burch, R., J. Catal. 86, 384 (1984).
- Anderson, J. B. F., Bracey, J. D., Burch, R., and Flambard, A. R., "Proceedings, 8th International Congress on Catalysis," Vol V, p. 111. Berlin, 1984.
- 30. Sachtler, W. M. H., in "Proceedings, 8th International Congress on Catalysis," Vol V, p.151. Berlin, 1984.
- Sachtler, W. M. H., Shriver, D. F., Hollenberg, W. B., and Long, A. F., *J. Catal.* 92, 429 (1985).
- Vannice, M. A., and Sudhakar, C., J. Phys. Chem. 88, 2429 (1984).
- 33. Rieck, J. S., and Bell, A. T., J. Catal. 99 262 (1986).
- Levin, M. E., Salmeron, M., Bell, A. T., and Somorjai, A. T., J. Catal. 106, 401 (1987).
- 35. Boudart, M., and McDonald, M. A., *J. Phys. Chem.* **88**, 2185 (1984).
- 36. Rieck, J. S., and Bell, A. T., *J. Catal.* **103**, 46 (1987).
- Rabo, J. A., Risch, A. P., and Poutsma, M. L., *J. Catal.* 53, 295 (1978).
- 38. Hoffmann, F. M., and Robbins, J. L., in "Proceedings of the 9th International Congress in Catalysis, Calgary, 1989", Vol. 3,

p.1144. Calgary, 1989.

- 39. Kobori, Y., Yamasaki, H., Naito, S., Onishi, T., and Tamaru, K., J. *Chem. Soc., Far. Trans. I* **78**, 1473 (1982).
- 40. Akhter, S., and White, J. M., Surf. Sci. 180, 19 (1987).
- 41. Akhter, S., Henderson., M. A., Mitchell, G. E., and White, J. M., Langmuir 4, 246 (1988).
- 42. Biloen, P., Helle, J.N., van den Berg, F. G. A., and Sachtler, W. M. H., *J. Catal.* **81**, 450 (1983).

Chapter III

Intrinsic Rate Parameters of the Fischer-Tropsch Synthesis

ABSTRACT

Fischer-Tropsch synthesis results in a large range of products, from methane to higher hydrocarbons. Steady-state product distributions obtained during the Fischer-Tropsch synthesis can be described by the Anderson-Schulz-Flory (ASF) polymerization model. The product distribution is characterized by a single parameter, α , the probability of chain growth, which is the ratio of the apparent rate constant for propagation (k_p') to the sum of the apparent rate constant for propagation and the rate constant for termination (k_t). Expressions are derived for k_p', k_t, and the average hydrocarbon product carbon number. It is shown that steady state rate data cannot be used to evaluate k_p' and k_t individually. The reaction mechanism of Fischer-Tropsch synthesis is viewed as a surface polymerization in which the monomer is produced *in situ* from CO and H₂ on the catalyst surface (1-3). The experimentally observed product distribution obeys Anderson-Schulz-Flory (ASF) polymerization kinetics: $N_{Cn}/N_{Cn-1} = \alpha$, where N_{Cn} is the turnover frequency of products of carbon number n and α is the chain growth parameter and is independent of chain length n. This is indicative of propagation by a sequence of independently repeated additions of a monomer group to the growing chain, in competition with the termination step.

$$\begin{array}{cccc} k_p' & k_p' \\ C_{n-1}(s) & & \longrightarrow & C_n(s) & \longrightarrow & C_{n+1}(s) \\ & +C_1(s) & \downarrow & +C_1(s) \\ & & & C_n(g) \end{array}$$

The ASF distribution can be expressed by the following two equations:

$$N_{C_n} = k(1-\alpha)^2 \alpha^{n-1}$$
(1)
$$\alpha = \frac{k_p}{k_p + k_1}$$
(2)

where k is a rate parameter and $k_p' = k_p \theta_m$, k_p being the intrinsic propagation rate and θ_m the coverage of the monomer building block. N_{Cn}, α and k can be determined from steady-state data. The objective is to derive individual expressions for k_p' and k_t .

 N_{CO} can be expressed in terms of the turnover frequency for producing a product with n carbon atoms, N_{Cn} , in the following

manner.

$$N_{CO} = \sum_{n=1}^{\infty} n N_{C_n}$$
(3)

Kellner and Bell (4) have shown that N_{Cn} can be expressed as

$$N_{C_n} = k_t \theta_n \tag{4}$$

where θ_n is the surface coverage by chains containing n carbon atoms. If chain growth occurs by the addition of single carbon units, it then follows that

$$\theta_n = \theta_1 \alpha^{n-1} \tag{5}$$

Now, the average product carbon number, n_{av} is given by the following expression:

$$n_{av} = \frac{\sum_{n=1}^{\infty} nN_{C_n}}{\sum_{n=1}^{\infty} N_{C_n}}$$
(6)

Substitution of eqns. 3 and 4 into eqn. 6 results in

$$n_{av} = \frac{N_{CO}}{k_t \sum_{n=1}^{\infty} \theta_n}$$
(7)

By substitution of eqns. 7 and 8 into eqn. 9, it can be shown that

$$n_{av} = \frac{\sum_{n=1}^{\infty} n\alpha^{n-1}}{\sum_{n=1}^{\infty} \alpha^{n-1}}$$
(8)

and for α < 1, this simplifies to

$$n_{av} = \frac{1}{(1-\alpha)}$$
(9)

Using eqns. 7 and 9 in conjunction with eqns. 1 and 2, it can further be shown that

$$k_{1} = \frac{k(1-\alpha)}{\sum_{n=1}^{\infty} \theta_{n}}$$
(10)
$$k_{p}' = \frac{k\alpha}{\sum_{n=1}^{\infty} \theta_{n}}$$
(11)

and

Evaluation of k_p' and k_t requires determination of the sum of the surface coverages of the precursors to the gas-phase hydrocarbon products. It is evident from the above analysis that steady state rate data cannot be used to evaluate k_p' and k_t despite claims to have done so (5,6), since such data do not provide the sum of surface coverages appearing in the denominator of eqns. 10 and 11. As has already been noted by Zhang and Biloen (7), k_p' and k_t can be properly evaluated from transient isotopic tracer experiments.

Acknowledgements

The equations in this chapter were derived jointly with G. H. Yokomizo.

REFERENCES

Bell, A. T., *Catal. Rev.-Sci. Eng.* 23, 203 (1981).
 Biloen, P., and Sachtler, W. M. H., *Adv. Catal.* 30, 165, 1981.

- 3. Anderson, R. B., 'The Fischer-Tropsch Synthesis', Academic Press, New York, 1984.
- 4. Kellner, C. S., and Bell, A. T., J. Catal. 70, 216 (1981).
- 5. Fu, L., Rankin, J. L., and Bartholomew, C. H., C₁ Mol. Chem. 1, 369 (1986).
- 6. Adesina, A. A., J. Catal. 124, 297 (1990).
- 7. Zhang, X. and Biloen, P., J. Catal. 98, 468 (1986).

Chapter IV

Estimates of the Rate Coefficients for Chain Initiation, Propagation, and Termination during Fischer-Tropsch Synthesis over Ru/TiO₂

ABSTRACT

Transient response isotopic tracer experiments have been used to study chain growth during Fischer-Tropsch synthesis over a Ru/TiO₂ catalyst. This involves observation of the incorporation of ¹³C into reaction products after an abrupt switch from $12CO/D_2$ to $13CO/D_2$ in the feed. Values for the rate constants for initiation, propagation and termination are determined by fitting theoretically generated model curves to the observed transient responses. The rate constant for chain initiation is independent of temperature and D_2/CO ratio. The rate constants for propagation and termination increase with temperature. The rate constant for propagation is not affected by the D_2/CO ratio. The rate constant for termination increases linearly with increasing D₂/CO ratio. The activation energy for chain termination is significantly higher than that for chain propagation, explaining the observed decrease in chain growth probability, α , with increasing temperature. Coverages by reaction intermediates are also estimated. The dominant species are monomeric building units which occupy 0.2-0.6 ML. Alkyl species

that are the direct hydrocarbon product precursors occupy < 0.2 ML and adsorbed CO covers 0.7 ML.

1.0 INTRODUCTION

Fischer-Tropsch synthesis (FTS) produces a spectrum of products consisting primarily of linear olefins and alkanes (1). The carbon number distribution of the products containing four or more carbon atoms is often well described by an Anderson-Schulz-Flory (ASF) distribution, which assumes that products containing n carbon atoms are produced by a stepwise polymerization of C₁ species (2). If the probability of chain growth, α , defined as the ratio of the rate of chain propagation to the sum of the rates of chain propagation and termination, is taken to be independent of n, then $[N_{Cn+1}]/[N_{Cn}] = \alpha$, where N_{Cn} and N_{Cn-1} are the turnover frequencies for products containing n and n+1 carbon atoms, respectively. Steady state investigations of FTS have shown that α is a complex function of both temperature and the partial pressures of H₂ and CO (2-5).

Mechanistic studies of hydrocarbon production by FTS over Fe, Co and Ru suggest that the mechanism of FTS might be described by the following reaction sequence (6):

| 1. | CO _g ≓ CO _s |
|----|-----------------------------------------------------------------|
| 2. | H _{2,g} |
| 3. | $CO_s \rightarrow C_s + O_s$ |
| 4. | $O_s + H_s \rightarrow OH_s$ |
| 5. | $H_s + H_s \rightarrow H_2O_s$ |
| 6. | $C_s + H_s \rightleftharpoons CH_s$ |
| 7. | CH _s + H _s _₹ CH _{2,s} |
| 8. | CH _{2,s} + H _s |
| 9. | $CH_{3,s} + H_s \rightarrow CH_{4,g}$ |

Adsorbed CO covers most of the catalyst surface and is in equilibrium with gas-phase CO (6-8). Likewise, dissociatively adsorbed H₂ is found to be in equilibrium with gas-phase H₂ (8). Some of the adsorbed CO dissociates irreversibly (7, 9) to form C_s and O_s. The atomic oxygen produced in this manner reacts rapidly with H_s to form water, whereas the atomic carbon reacts with hydrogen to form CH_x (x = 1-3) species (9, 10). The CH_{3,s} species can react with additional hydrogen to form CH₄ or react with a CH_{2,s} species, thereby initiating the process of chain growth. Chain propagation is sustained by CH_{2,s} addition to adsorbed alkyl species. Chain termination can occur by hydrogen addition to a surface alkyl species to give a paraffin or by hydrogen abstraction to give an olefin.

A number of investigators have used isotopic-tracer techniques to identify the species involved in the chain growth process and to estimate the rate coefficients for chain propagation and termination (7, 11-20). In studies conducted with a Ru/SiO₂ catalyst, Kobori *et al.* (11) concluded that hydrocarbons are formed by the polymerization of CH_x intermediates, and that CO insertion plays no part in the chain growth process leading to hydrocarbons. Work by Biloen *et al.* (12) on unsupported Co, Ni/SiO₂ and Ru/ γ -Al₂O₃ has shown that carbidic intermediates are involved in the reaction and that methane and higher hydrocarbons have a common precursor. Stockwell *et al.* (17) were unable to conclude whether chain growth occurred via a CO or a CH_x insertion mechanism. Studies on an Fe/Al₂O₃ catalyst by Stockwell *et al.* (18) implicated a CH species as responsible for chain growth. They concluded that once chain growth is initiated, methane and higher hydrocarbon production is rapid and hence, coverages by the growing chains is small.

Several attempts to determine the rate coefficients for chain propagation and termination have been reported. Zhang and Biloen (14) have looked at the successive incorporation of ${}^{13}C$ into C₁₋₃ hydrocarbon products over Co and Ru catalysts. For Co, it was estimated that at 483 K, the value of the apparent rate constant for propagation decreased from 0.045 to 0.025 s-1 and the corresponding value of the apparent rate constant for chain termination increased from 0.02-0.04 s-1, as the D₂/CO ratio increased from 1 to 6.55. For the same reaction conditions, the coverage by alkyl chains was estimated to be between 0.19 and 0.25 ML, whereas the coverage by monomeric species was much smaller. For Ru, the apparent rate coefficient for chain propagation was estimated to be \geq 1s-1. Based on similar experiments, Mims *et al.* (15) have estimated the apparent rate coefficient for chain propagation to be 2-4 s-1 for a promoted Fe catalyst at 510 K and a H₂/CO ratio of 1 (15), and 2 s-1 on Co at 475 K and a H₂/CO ratio of 2 (16). Over both Fe and Co, the coverage by the monomeric species exceeded the coverage by hydrocarbon chains. In a recent study using a Ru/TiO₂ catalyst, Yokomizo and Bell (21) observed that 80 % of the carbidic species on the Ru surface served as a monomer building block, and 20 % acted as the precursor to methane. The rate coefficient for chain termination was estimated to be 0.044 s⁻¹ at T = 463 K, $p_{CO} = 50$ torr and a D₂/CO = 3. The total coverage by C₁ species was reported to be 0.25 ML, and the coverage by C₂₊ species leading to hydrocarbon product was estimated at 0.1 ML.

The objective of the present investigation is to estimate the rate coefficients for chain initiation, propagation and termination, and to study their dependence on temperature and D₂/CO ratio. A further aim of this effort is to determine the surface coverages by the various reactive carbonaceous species present on the catalyst. A Ru/TiO₂ catalyst was used for these investigations because of the high specific activity of Ru for FTS and its characteristically high value of α (22). The absence of alcohols from the products of FTS over Ru was a further reason for choosing this metal. Titania was used to support and disperse the ruthenium since titania-supported Group VIII metals are known to be more active than silica-or alumina-supported Group VIII metals (23-26).

2.0 EXPERIMENTAL

2.1 Catalyst Preparation and CharacterizationA 3.3% Ru/TiO₂ catalyst was prepared by incipient wetness

impregnation of Degussa P-25 titania with an aqueous solution of $RuCl_3.H_2O$ (Strem). Details of the preparation are given in ref. (27). The dried catalyst was reduced at 503 K to minimize encapsulation of the Ru crystallites by titania. The metal content of the catalyst was determined by X-ray fluorescence. The chloride level after reduction was below the detection limit (0.02%). The dispersion of Ru was determined by H₂ chemisorption to be 15.5%, while the CO uptake on the freshly reduced catalyst was 1.3 ML (ML based on H₂ chemisorption). The BET surface area, determined from a N₂ isotherm at 77 K, was 47.5 m²/gm.

2.2 Apparatus

 D_2 , 12CO, 13CO and He were supplied from a gas manifold to a low dead volume quartz microreactor. UHP H₂ (Matheson Gas) or D₂ (Union Carbide) were further purified by passage through a Deoxo unit (Engelhard Industries) and water was removed by a molecular sieve 13X trap. UHP CO (99.999% pure, Matheson Gas) was passed through a glass bead trap maintained at 573 K to remove iron carbonyls, an Ascarite trap to remove CO₂, and a molecular sieve trap to remove water. UHP He was passed through a molecular sieve trap to remove water. 13CO (Isotec Inc, 99% 13C) was used as supplied.

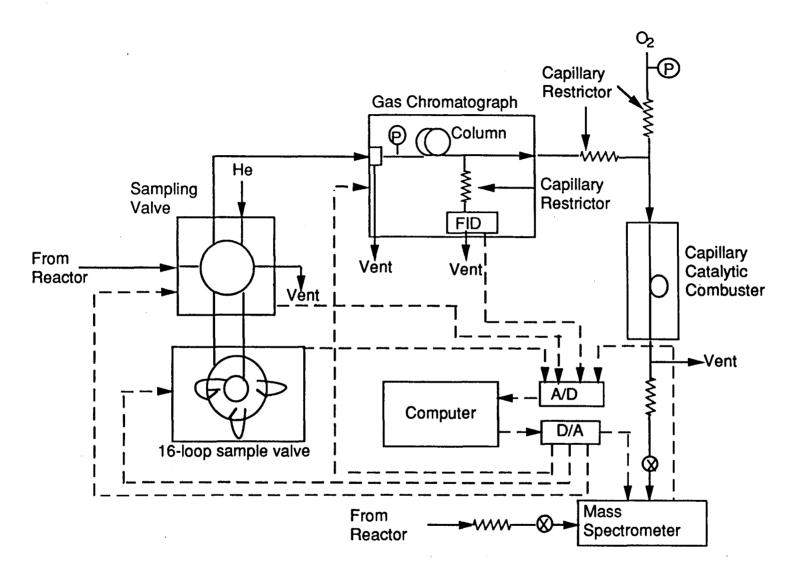
Tylan mass flow controllers were used to regulate the flow of all four gases. The 12CO and 13CO streams flow from the flow controllers into two separate low dead-volume, 2-position, 4-port valves. One stream from each of these valves flows through a

bubblemeter to a vent line, while the other stream flows to a 4-way tee. He and D_2 are mixed and introduced into the third inlet of the 4-way tee, and the outlet from the tee goes to the microreactor. This flow scheme enables establishment of steady-state flow to the vent line in both CO streams and allows switching the reactor feed from one isotopically labeled form of CO to the other without significant flow perturbation. By simultaneous switching of the two 4-port valves, one avoids the elution of a small slug of the first isotope of CO held up in the valve and flow line.

2.3 Product Analysis

The steady-state distribution of reaction products was determined by gas chromatography and the temporal variation in the distribution of 1²C and 1³C in each product was determined by isotopic ratio gas chromatography-mass spectroscopy (28-30). Figure 1 shows a schematic of the analytical system. A 10-port GC sampling valve (Valco E410UWP) and a multiposition 16 sample-loop valve (Valco E6ST16T) were used to acquire and store samples. Both valves are housed in valve ovens and can be actuated electrically. Flow lines downstream of the reactor, the valve ovens and lines to the GC inlet were all maintained at 393 K, to minimize product condensation.

Product analysis is initiated by injecting the contents of one of the sample loops into a Perkin-Elmer Sigma 3B chromatograph containing a fused silica capillary column (0.25mm i.d. x 50 m)



đ

÷

Fig. 1 Schematic of Analytical System

coated with a 1 μ m film of SE-54. To achieve good product resolution, the column is maintained at 233 K for 4 min, then ramped at 20 K/min to 523 K, and finally held at 523 K for 10 min. This sequence results in a total sample analysis time of 28.5 min. C₁₋₂ products elute at the initial temperature, C₃₋₈ products elute during the temperature ramp, and C₉₋₁₈ products elute at the final temperature. Products heavier than C₁₄ hydrocarbons are not detected. The column effluent is split into two streams using a glass-lined capillary union (SGE); one line (0.11 mm i.d.) is sent to an FID detector for quantification, while the other transfer line (0.20 mm I.D.) is routed to a capillary combuster. This latter stream is mixed with O₂ and combusted to CO₂ in a 2 m long capillary (0.2 mm i.d.) containing Pt wire (0.13 mm o.d.) maintained at 873 K. Details of the capillary combuster are given in ref. (30).

The effluent from the combuster is leaked into a vacuum chamber containing the probe of a UTI 100C quadrupole mass spectrometer. The leak is accomplished by coupling the exit of the combuster directly to the inlet capillary restrictor of the mass spectrometer. The flow rate through the combuster is sufficient to preclude the back diffusion of air into the mass spectrometer. Complete combustion of all hydrocarbon products except methane was confirmed by the absence of peaks at masses corresponding to fragments derived from the hydrocarbons. The combustion of methane was found to be inhibited by the presence of a large amount of CO, which elutes at the same time as methane. The masses monitored by the mass spectrometer were amu 4 (He), amu 20 (D₂O

and $12CD_4$), amu 21 ($13CD_4$), amu 44 ($12CO_2$) and amu 45 ($13CO_2$). The distribution of 12C and 13C in methane was determined from the relative intensities of the signals for amu 20 and amu 21. The presence of D_2O in the products, which also produces a signal at amu 20, did not interfere with the detection of $12CD_4$, since CD_4 and D_2O elute at sufficiently different times. The distribution of 12C and 13C in C_{2+} hydrocarbons was obtained from the relative signal intensities at amu 44 and amu 45. The temporal resolution of these products recorded by the mass spectrometer was comparable to that recorded by the FID.

Operation of the sampling valves was controlled by an IBM PC/XT computer programmed to acquire samples at preset times. The output from the FID detector and mass spectrometer were acquired by the computer at the rate of 2 data points a second.

2.4 Procedure

Experiments were carried out at temperatures between 453 K and 483 K. The ratio of D_2/CO was varied between 2 and 5, by holding the CO partial pressure at 0.1 atm, and varying the D_2 partial pressure between 0.2 and 0.5 atm. The total flowrate to the reactor was 100 cm³/min. CO conversions were maintained as low as possible and, in most cases, were below 10%. For each set of conditions, the reaction was allowed to proceed in a mixture of 12CO, D_2 and He for 20 min, to avoid the rapid initial loss in activity after start-up (27). Deactivation after the initial start-up proceeds with a first order decay time constant of 5 h. After each

experiment, the catalyst was reduced in D_2 /He at 523 K for 2 h to ensure that steady-state activity levels were maintained.

Isotopic-tracer, transient response experiments were initiated by switching the feed from a stream containing 12CO to one containing an equivalent concentration of ¹³CO, after steady-state conditions had first been achieved in 12CO. In this fashion, the steady-state activity of the catalyst was not perturbed by the switch in isotopic composition of the CO. To obtain good temporal resolution of the isotopic composition of the products, the following sampling sequence was used. A sample was taken 15 s after the switch in CO isotopic composition, followed by four samples taken at 10 s intervals, followed by a sample taken after an interval of 15 s, one taken after an interval of 20 s, one taken after an interval of 30 s interval, and two taken after intervals of 240 s. In this way, 11 samples are acquired in 10 min. Because the fill-time of the sample loops is 6s, data were not collected at intervals shorter than 10s. Since most changes in product isotopic composition occur in the first 2 min after the switch in feed isotopic composition, it is desirable to acquire data at intervals shorter than 10 s. To do so, the feed composition was changed from $13CO/D_2/He$ to $12CO/D_2/He$ and 5 samples were acquired at 10 s intervals for upto 60 s.

Figure 2 is a schematic of the data acquired during a typical experiment. The curves labelled $F(1^2C)$ and $F(1^3C)$ represent the fractions of the carbon atoms that are 1²C-labelled and 1³C-labelled, respectively. $F(1^2C)$ is calculated by dividing the 1²C concentration observed at a given time by the initial steady-state 1²C

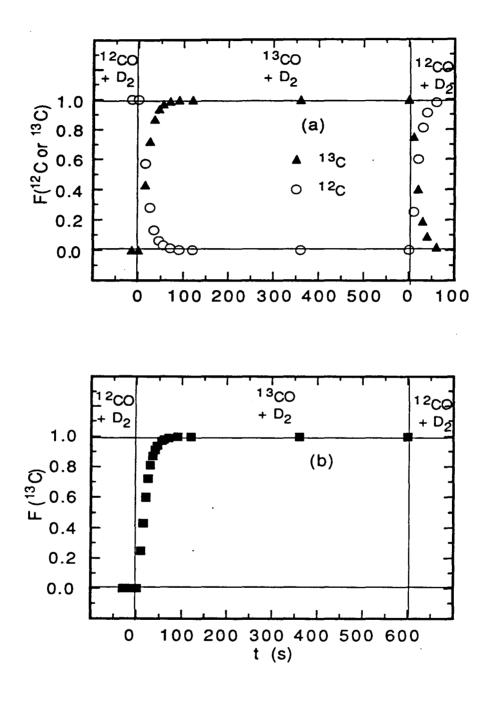


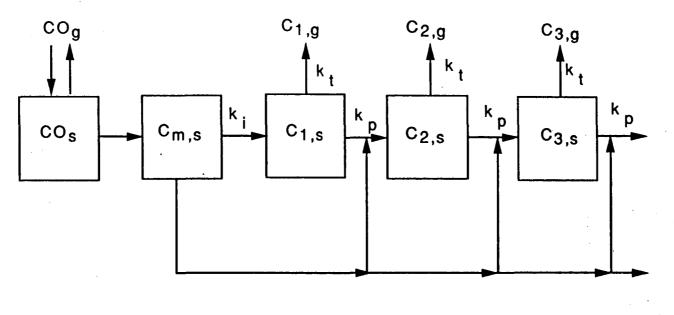
Fig. 2 (a) Isotopic Transient Data Sampling. (b) Average Rise Curve.

concentration measured in $12CO/D_2$; F(13C) is obtained by dividing the observed 13C concentration by the 13C concentration measured after 10 min in 13CO/D₂. [It had previously been determined that the transients are complete in 10 min.] The sum of F(12C) and F(13C) for a given product always equals 1.0. For the first portion of the experiment, the rise curve points for each product were calculated as the average of the values of F(13C) and [1-F(12C)], and in the latter section, as the average of the values of F(12C) and [1-F(13C)]. All the points could then be combined to give a rise curve with 16 points. Sampling times were chosen such that data could effectively be collected at 5 s intervals for the first minute after the switch. Data acquired during the initial part of the experiment, as the 13C content in the product rises, was found to be in agreement with data from the latter part of the transient experiment, when the 13C content in the products declines.

3.0 THEORETICAL MODELLING

3.1 Chain growth model

Simulation of the experimentally observed transients was carried out on the basis of the scheme shown in Fig. 3. This scheme is identical to that used by Zhang and Biloen (14) and by Mims and McCandlish (16). In Fig. 3, CO_g and CO_s refer to gas-phase and adsorbed CO, $C_{m,s}$ refers to adsorbed monomeric building units and $C_{n,s}$ and $C_{n,g}$ refer to adsorbed alkyl chains and gaseous products containing n carbon atoms. Reference to reactions 1-16 in the



e



Introduction show that the scheme in Fig. 3 represents a simplification of the more detailed reaction sequence. First, the species C_s , CH_s and $CH_{2,s}$ are treated as a common species, C_m , on the assumption that the individual species are in equilibrium with each other. Second, no distinction is made between chain termination to olefins and paraffins. The rate coefficient for conversion of $C_{m,s}$ to $C_{1,s}$ is the apparent first-order rate coefficient for chain initiation, k_i . The rate coefficients k_p and k_t , are first-order rate coefficients for chain initiation, equivalent propagation, and termination. The dependence of any process on adsorbed hydrogen is not shown explicitly, since, for a given set of reaction conditions, the surface coverage of hydrogen is time independent.

3.2 Steady-State Rate and Label Balances

The scheme presented in Fig. 3 can be used to derive expressions for F_m and F_n , the fraction of labelled carbon in the monomer pool and in the pool of chains of length n, respectively. Equations for F_m and F_n are obtained in the following manner. A balance on labelled carbon entering and leaving the monomer pool gives

$$\theta_{m} \frac{dF_{m}}{dt} = k_{d} \theta_{CO} F_{CO} - \theta_{m} F_{m} (k_{i} + k_{p} \sum_{n=1}^{\infty} \theta_{n})$$
(1)

[In eqn. 1, θ_{CO} , θ_m , and θ_n are the surface coverages for CO, monomeric building units, $C_{m,s}$, and alkyl chains, $C_{n,s}$, respectively.] At steady state,

$$N_{CO} = k_d \theta_{CO} = k_i \theta_m + k_p \theta_m \sum_{n=1}^{\infty} \theta_n$$
(2)

Combining eqns. (1) and (2), one obtains

$$\frac{dF_{m}}{dt} = \frac{F_{CO} - F_{m}}{\tau_{m}}$$
(3)

where $\tau_m = 1/(k_i + k_p(\Sigma \theta_n))$

The appearance and disappearance of labelled carbon in the methane precursor pool C_1 is governed by

$$\theta_1 \frac{dF_1}{dt} = k_i \theta_m F_m - k_t \theta_1 F_1 - k_p \theta_m \theta_1 F_1$$
(4)

Since at steady state

$$k_{i}\theta_{m} = k_{t} \theta_{1} + k_{p} \theta_{m}\theta_{1}$$
(5)

eqn. (4) can be rewritten as

$$\frac{dF_1}{dt} = \frac{F_m - F_1}{\tau}$$
(6)

where $\tau = 1/(k_p \theta_m + k_t)$. The appropriate balance on labelled carbon in the pool of alkyl species containing n carbon atoms is given by

$$n\theta_n \frac{dF_n}{dt} = k_p \theta_m \theta_{n-1} [(n-1)F_{n-1} + F_m] - k_p \theta_m \theta_n (nF_n) - k_t \theta_n (nF_n)$$
(7)

Once again, at steady state,

$$k_{p}\theta_{m}\theta_{n-1} = k_{p}\theta_{m}\theta_{n} + k_{t}\theta_{n}$$
(8)

so that eqn. 7 can be rewritten as

$$\frac{dF_{n}}{dt} = \frac{\frac{(n-1)F_{n-1} + F_{m}}{n} - F_{n}}{\tau}$$
(9)

The initial conditions for F_m , F_1 , and F_n are $F_m = F_1 = F_n = 0$ at t = 0. Since CO is assumed to equilibrate rapidly with the catalyst

surface, $F_{CO} = 1$ for $t \ge 0$. With these initial conditions, the solution to eqn. 6 is

$$F_{m}(t) = 1 - \exp(-t/\tau_{m}) \tag{10}$$

An analytical solution for $F_n(t)$ can be obtained using Laplace transforms and the convolution theorem (31). The resulting expression is

$$F_{n}(t) = 1.0 + \left(\frac{\exp(-\frac{t}{\tau_{m}})}{n}\right)\sum_{i=1}^{n} (-1)^{i-1} \left(\frac{\tau_{m}}{\tau - \tau_{m}}\right)^{i} + \left(\frac{\exp(-\frac{t}{\tau})}{n}\right)\sum_{i=1}^{n} \frac{1}{\tau^{i}} \sum_{r=0}^{i-1} \frac{t^{i-r-1}}{(i-r-1)!} \tau^{r+1} \left(\left(-\frac{\tau_{m}}{\tau - \tau_{m}}\right)^{r+1}\right)$$
(11)

4.0 RESULTS AND DISCUSSION

4.1 Catalyst Activity and Selectivity

Gas chromatographic analyses of the products taken during the isotopic transient experiments shows that the catalyst activity and selectivity are unchanged over the 11-min duration of the experiment. The main products observed are α -olefins, cis- and trans- β -olefins and n-paraffins. A few branched products are also detected, but these constitute less than 10% of the total product. Alcohols and other oxygenates are not detected. Mass spectometric analysis of the products indicates that no CO₂ is formed and that D₂O is the only oxygenated product.

Figure 4 shows an Anderson-Schulz-Flory (ASF) plot of the turnover frequencies for C_1 - C_{12} at 463K and a $D_2/CO = 3$. As is characteristic of Ru catalysts (3, 30), the points for C_2 and C_3

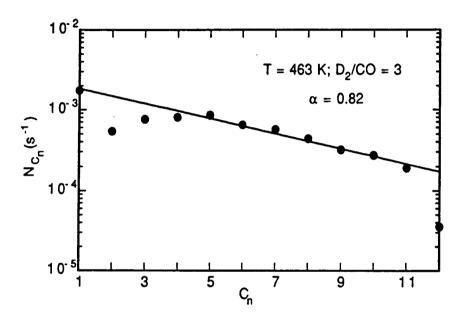


Fig. 4 Anderson-Schulz-Flory plot, log N_{Cn} vs Carbon number, where N_{Cn} is the turnover frequency for products of carbon number n.

products fall below the line passing through the points for the C₄-C₁₁ products. From the slope of this line, α is determined to be 0.82.

Figures 5a and 5b show the dependence of the turnover frequency for CO consumption and α on temperature, respectively. N_{CO} is calculated as Σ nN_{Cn} for values of n between 1 and 13, and α is taken as the slope of the linear portion of the ASF plot. It is seen from Fig. 5a that N_{CO} exhibits an Arrhenius behavior for temperatures below 473 K, and then becomes nearly constant at higher temperatures. Calculations of the Weisz parameter indicate the absence of intraparticle mass transfer limitations, leading to the conclusion that the observed dependence on temperature is a reflection of the intrinsic kinetics. Figure 5b shows that α decreases monotonically from 0.88 to 0.73 as temperature increases from 453K to 498K.

The effects of D₂ partial pressure on N_{CO} and α , for a fixed temperature and CO partial pressure are shown in Figs. 6a and 6b. The value of N_{CO} is seen to increase linearly with increasing D₂ partial pressure, whereas the value of α decreases monotonically. The trends reported in Figs. 5b and 6b are similar to those observed previously for Ru/Al₂O₃ (3) and for supported Fe catalysts (4, 5).

Figure 7 shows a series of product selectivity plots. It is observed that the total straight-chain olefin/n-paraffin ratio rises from C_2 to C_4 and then decreases with increasing carbon number. The fraction of internal olefins in the straight-chain olefin product rises with increasing carbon number. The β -olefin fraction in the

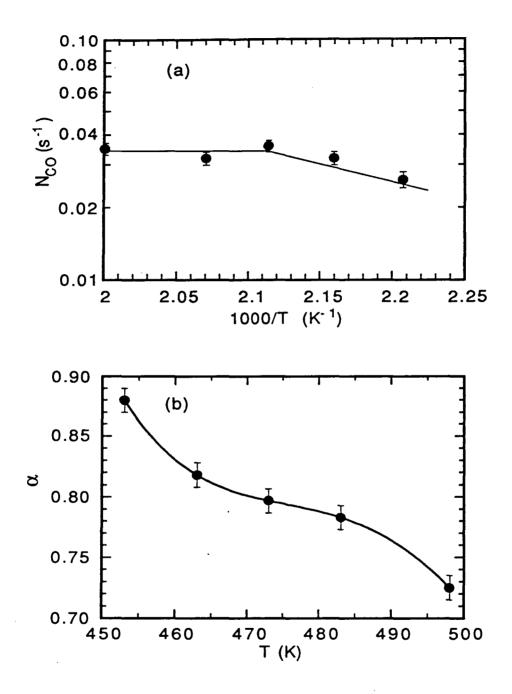


Fig. 5 a) CO turnover frequency, N_{CO} , as a function of temperature; (b) Chain growth parameter α as a function of temperature; $D_2/CO = 3$.

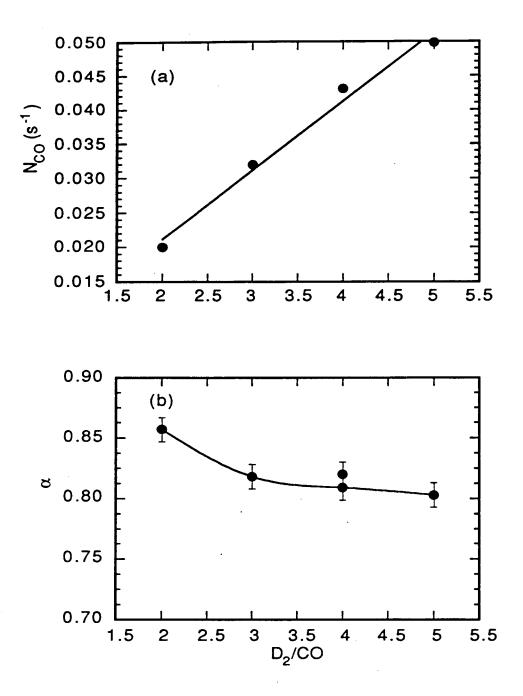
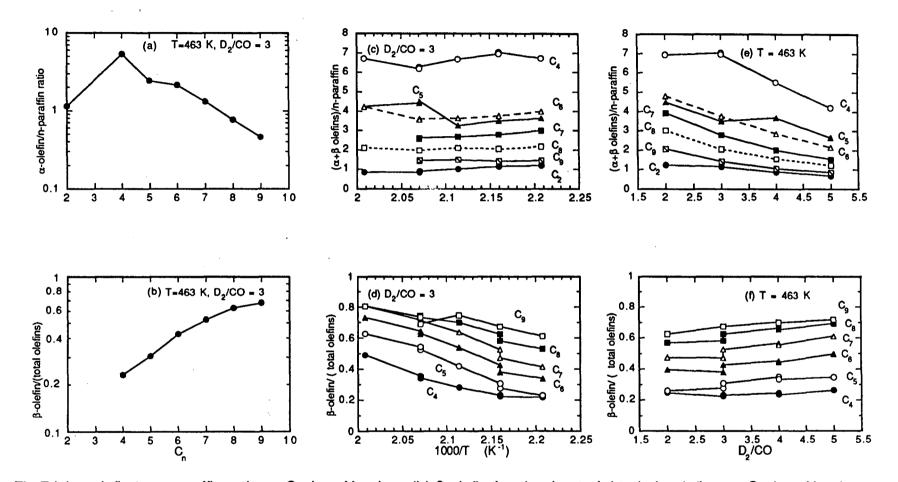


Fig. 6 (a) CO turnover frequency, N_{CO}, as a function of D₂/CO ratio; (b) Chain growth parameter α as a function of D₂/CO ratio; T = 463 K.



•

Fig.7 (a) α -olefin to n-paraffin ratio vs Carbon Number; (b) β -olefin fraction in straight-chain olefins vs Carbon Number; T = 463 K, D₂/CO = 3; (c) Straight chain olefins to n-paraffin ratio as a function of temperature; (d) β -olefin fraction in straight-chain olefins as a function of temperature; D₂/CO = 3; (e) Straight chain olefins to n-paraffin ratio as a function of D₂/CO ratio; (f) β -olefin fraction in straight-chain olefins as a function in straight-chain olefins as a function of D₂/CO ratio; T= 463 K.

ø

olefin product at any carbon number also increases with temperature. The ratio of olefins to paraffins decreases with increasing D_2 /CO ratio. These changes in product selectivity are in agreement with data reported by Dictor and Bell (32) on an Fe catalyst and by Schulz (33) on a Fe/Mn catalyst.

١

4.2 Isotopic Transients

The incorporation of 13C and the concurrent decline in 12C in the C_1 and C_{3-8} products was monitored by isotope-ratio GC-MS, following a switch in the feed from $12CO/D_2$ to $13CO/D_2$. The concentration of the C₂ product was too low for mass spectrometric detection. Figures 8 and 9 show representative plots of $F_1(t)$ and $F_n(t)$ (n = 3-8), respectively. The data points in Fig. 8 are based on the measured isotopic fractions in all olefins and paraffins of a given carbon number, since it was observed that the dynamics for products with a given number of carbon atoms could not be differentiated on the basis of structure (i.e., olefin vs paraffin, α olefin vs β -olefin, n-paraffin vs branched paraffin). Figure 8 shows that the methane transient rises rapidly but on comparison with Figure 9, does not lie before the C_3 data. The transients for C_{3+} are shown in Fig. 8 and are seen to approach 1.0 after 120 s. While there is considerable scatter in the data, it is observed that the appearance of 13C-labelled carbon in the products is progressively slower as the value of n increases from 3 to 8. This trend is particularly evident for the C_{6+} products.

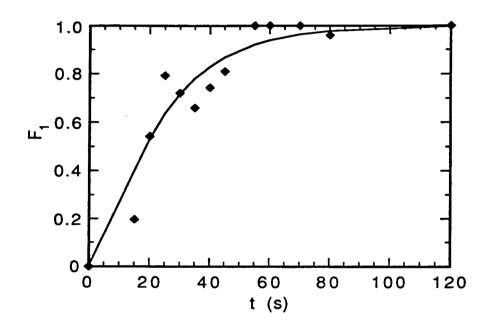


Fig. 8 F (1³CD₄) rise after a switch from 1²CO/D₂ to 1³CO/D₂ at t = 0. T = 463 K, D₂/CO = 3.

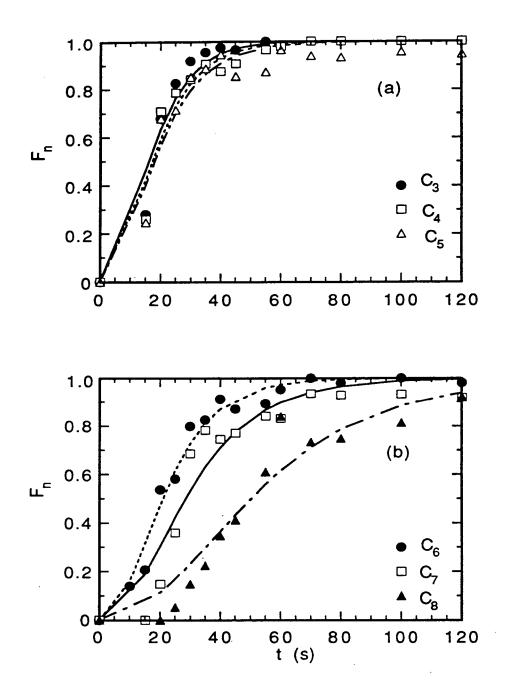


Fig. 9 (a) $F(1^{3}C)$ rise in the C₃-C₅ products; (b) $F(1^{3}C)$ rise in the C₆-C₈ products; transient response after a switch from $1^{2}CO/D_{2}$ to $1^{3}CO/D_{2}$ at t = 0. T = 463 K, D₂/CO = 3.

4.21 Parameter evaluations

Values of the two parameters τ and τ_m were obtained by fitting the analytical expressions for F_n given by eqn. 11 to the experimental data. This was done using a quasi-Newton method (31) to minimize the objective function S_n (τ , τ_m) defined as

$$S_{n}(\tau, \tau_{m}) = \sum_{j=1}^{M} \left[F_{n}^{expt}(t_{j}) - F_{n}(t_{j})\right]^{2}$$
(12)

In eqn. 12, $F_n^{expt}(t_j)$ and $F_n(t_j)$ are the experimental and theoretical values at time t_j and M is the number of experimental points.

Figures 8 and 9 show data and model fits at a temperature of 463 K and a D_2/CO ratio of 3. The F-test was used to assess the statistical adequacy or lack of fit of the model (34, 35). For each value of n, the F-test indicated that the model fit the data at a 95% confidence interval. The parameters τ and τ_m were determined independently for each of the transients from C_1 - C_8 . Table 1 shows values obtained for the data set at 463 K and $D_2/CO = 3$. It is evident that the values of τ and τ_m determined from different transients exhibit a modest spread in values. Of particular note are the large values for τ_m for n = 1 and n = 8. For n = 8, the value of τ_m is directly related to the slow approach of $F_8(t)$ to unity (see Fig. 8), as a consequence of a partial loss of product due to condensation in the transfer-line upstream of the capillary combuster. The large value of τ_m for n =1 also reflects the slow approach of F₁(t) to unity. In part this may be due to the presence of 12C impurity in the 13CO

TABLE 1

| Carbon Number | τ(s) | τ _m (s) |
|---------------|-------------------|--------------------|
| 1 | 4.7 | 19.6 |
| 3 | 5.2 | 7.8 |
| 4 | 3.7 | 10.3 |
| 5 | 2.8 | 12.3 |
| 6 | 3.2 | 12.7 |
| 7 | 3.5 | 16.7 |
| 8 | 5.7 | 31.6 |
| Average | 3.9 ± 0.9^{1} | 11.9 ± 4.0 |

 τ and τ_m obtained from fitting the chain growth model to the data: D_2/CO = 3; T = 463 K.

¹ Average of values for C_1 , $C_{3.7}$. See text for details.

² Average of values for C_{3-7} .

. .

e

feed. For these reasons, it was decided that average values of τ should be based on the individual values obtained for C₁ and C₃₊, and average values of τ_m should be based on individual values obtained for C₃₊. It was found that the F_n predictions based on the average values of τ and τ_m were nearly indistiguishable from those based on the best-fit model values for each n from 3-7. Tables 2 and 3 show the average values of τ and τ_m obtained for the transients when temperature and the D₂/CO ratio were varied.

From Tables 2 and 3, it is seen that the modelling leads to the result that $\tau < \tau_m$ and that the ratio τ_m/τ lies between 3 and 13. This is similar to the findings of Mims *et al.* (16) on Co/SiO₂ and promoted Fe and is in disagreement with the results of Zhang and Biloen (14) on Co. This modelling result implies that active species on the surface spend a larger portion of their residence time in the monomer pool than in alkyl chains and further translates to higher coverages by the monomer pool than by the hydrocarbon precursors.

4.22 Intrinsic Rate Parameters and Surface Coverages

The values of k_i , k_p , and k_t , and θ_m and $\Sigma \theta_n$, can be determined from the values of τ and τ_m , obtained through the fitting procedure described above, and the values of N_{CO}, N_{Cn} and α , obtained from steady-state rate data. The approach used to calculate the rate coefficients and the surface coverages is described in the Appendix. Table 4 gives a complete summary of all the results at 463 K and D₂/CO = 3.

TABLE 2

Average τ and τ_m obtained from fitting the chain growth model to the data:

| Т (К) | $\tau_{av}(s)$ | $\tau_{m,av}(s)$ |
|-------|----------------|------------------|
| 453 | 3.5 | 13.5 |
| 463 | 3.9 | 11.9 |
| 463 | 3.9 | 15.0 |
| 473 | 1.8 | 18.1 |
| 483 | 2.1 | 18.8 |
| 483 | 1.6 | 19.1 |
| | | |

 $D_2/CO = 3$; temperature is varied.

TABLE 3

Average τ and τ_m obtained from fitting the chain growth model to the data:

| D ₂ /CO ratio | is | varied; | Т | = | 463 | Κ |
|--------------------------|----|---------|---|---|-----|---|
|--------------------------|----|---------|---|---|-----|---|

| D ₂ /CO | $\tau_{av}(s)$ | $\tau_{m,av}(s)$ |
|--------------------|----------------|------------------|
| 2 | 3.3 | 14.0 |
| 3 | 3.9 | 11.9 |
| 4 | 1.5 | 16.7 |
| 4 | 2.5 | 15.2 |
| 5 | 2.5 | 13.1 |

æ

TABLE 4

Transient at standard reaction conditions: Ru/TiO2 catalyst.

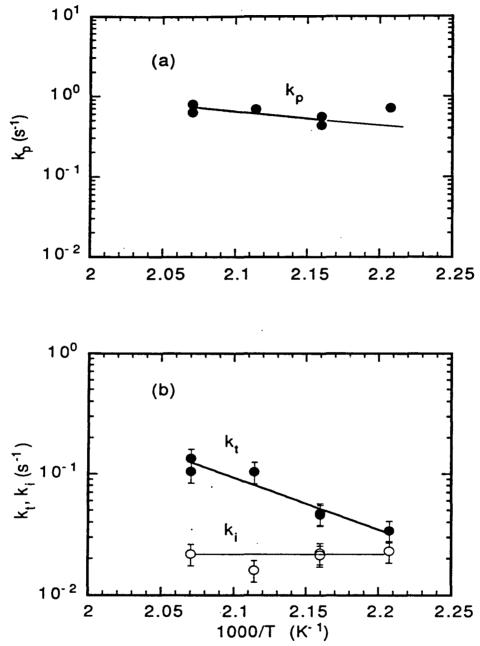
Reaction T= 463 K; $D_2/CO = 3$ $N_{CO} = 0.032 \text{ s}^{-1}$; $\alpha = 0.82$ $\tau = 3.9 \text{ s}$ $k_p^{app} = 0.212 \text{ s}^{-1}$, 0.208 s $^{-1}$ $k_1 = 0.047 \text{ s}^{-1}$, 0.046 s $^{-1}$ $k_i = 0.022 \text{ s}^{-1}$, 0.021 s $^{-1}$ $\Sigma \theta_n = 0.14 \text{ ML}$, 0.17 ML $\theta_m = 0.38 \text{ ML}$, 0.48 ML $\theta_{CO} = 0.67 \text{ ML}$

(Two values indicate results of separate experiments.)

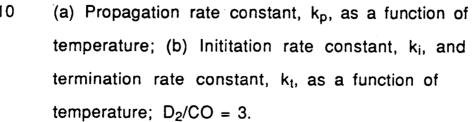
Figure 10 shows the variation of rate coefficients k_i, k_p, and k_t with T-1. The value of the initiation rate coefficient k_i appears to be independent of temperature. This trend can be rationalized if the initiation of chain growth is assumed to proceed via the process $CH_{2,s} + H_s \rightarrow CH_{3,s}$. In such a case, k_i is an apparent rate coefficient, representing the product of the true rate coefficient, k'_i, and the coverage of adsorbed hydrogen, θ_H . Since k'_i is expected to increase with increasing temperature but θ_H is expected to decrease, the product of k'_i and θ_H should be less sensitive to temperature than either of the two factors making up the product. The plots of k_p and k_t versus T-1 both have negative slopes, from which it is determined that the activation energy for chain propagation, E_p, is 8 kcal/mol and the activation energy for chain termination, E_t, is 20 kcal/mol.

The present evaluation of k_p can be compared to the estimated apparent rate of propagation reported by Zhang and Biloen (14). To do so, k_p is multipled by θ_m (see below) to obtain $k_p^{app} = k_p \theta_m$. For the data presented in Fig. 10, k_p^{app} lies between 0.25 and 0.5 s⁻¹. This range lies somewhat below Zhang and Biloen's estimate of >1 s⁻¹. There is close agreement between the values of k_t reported here and in the work of Yokomizo *et al.* (21). Using a Ru/TiO₂ catalyst similar to that described here, Yokomizo *et al.* determined a value of $k_t =$ 0.044s⁻¹ at T = 463 K, from modelling of temperature programmed surface reaction (TPSR) data. For the same reaction conditions, we obtain a value of $k_t = 0.047$ s⁻¹.

The activation energy for chain termination (20 kcal/mol) is

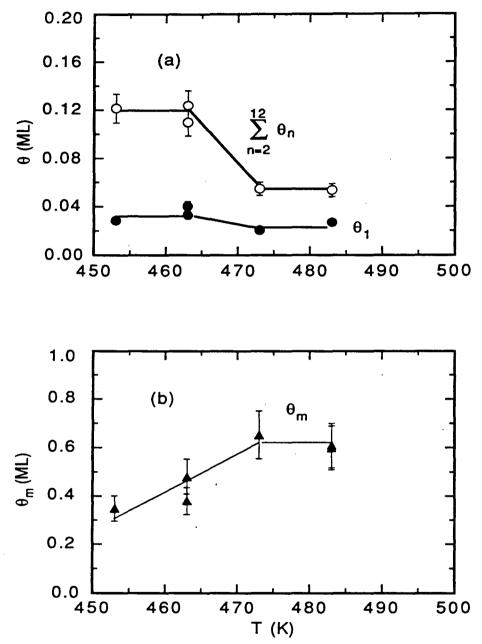






significantly higher than that for chain propagation (8 kcal/mol). This explains why the value of α decreases with increasing temperature (see Fig. 5b). While experimental values of E_t and E_p have not been reported in the literature previously, Shustorovich and Bell (36) have shown using the Bond-Order-Conservation-Morse-Potential (BOC-MP) approach, that E_t should be larger than E_p for Ni and Fe. Thus, for Ni(111), E_p for the chain growth step to form a C₂ species is estimated to be 6 kcal/mol, whereas E_t is estimated to be 11 kcal/mol for chain termination to ethylene and 19 kcal/mol for chain termination to ethane. For Fe(110), E_p for the formation of C₂ species is estimated to be 20 kcal/mol, whereas E_t is estimated to be 16 kcal/mol for chain termination to ethylene and 32 kcal/mol for chain termination to ethane.

The effects of temperature on the calculated values of surface coverage by carbonaceous species is given in Fig. 11 and Table 5. The values of θ_m lies between 0.3 and 0.6 ML, while the value of $\Sigma \theta_n$ lies between 0.12 and 0.05 ML. It is observed that with increasing temperature, θ_m increases, but θ_1 and $\Sigma \theta_n$ decrease. These trends are consistent with the observed temperature dependences for chain initiation, propagation, and termination. As seen in Fig. 10, increasing temperature has virtually no effect on k_i , but increases both k_p and k_t . Since E_t is larger than E_p , the rate of chain termination increases more rapidly than the rate of chain propagation, with the result that the surface coverage by growing alkyl chains decreases, whereas the coverage by monomeric building units increases. The total coverage by reaction intermediates is





(a) Coverage by alkyl surface species as a function of temperature; (b) Coverage by monomeric species as a function of temperature; D₂/CO = 3.

TABLE 5

| $D_2/CO = 3$, reaction temperature is varied. | | | | | | | | |
|------------------------------------------------|---------------------|---------------------------------|---------------------|-------------------------------|----------------------|--|--|--|
| Т (К) | θ ₁ (ML) | $\sum_{n=2}^{12} \theta_n (ML)$ | θ _m (ML) | Total θ _(n+m) (ML) | θ _{CO} (ML) | | | |
| 453 | 0.03 | 0.12 | 0.35 | 0.5 | - | | | |
| 463 | 0.03 | 0.11 | 0.38 | 0.52 | 0.67 | | | |
| 463 | 0.04 | 0.12 | 0.48 | 0.64 | 0.67 | | | |
| 473 | 0.02 | 0.05 | 0.62 | 0.69 | - | | | |
| 483 | 0.03 | 0.05 | 0.61 | 0.69 | 0.65 | | | |
| 483 | 0.03 | 0.61 | 0.60 | 0.68 | 0.65 | | | |

.

Coverage by reaction intermediates:

seen to be between 0.5 and 0.7 of a monolayer.

To determine whether or not the surface coverages estimated from the model are representative of actual coverages by carbonaceous species, a series of temperature-programmed surface Using the techniques described in ref. reactions were carried out. (27), measurements were made of the CO uptake capacity of the freshly reduced catalyst, the CO uptake of the catalyst after 20 min under reaction conditions, and the total carbon inventrory on the catalyst surface, exclusive of CO, after 20 min under reaction conditions. The room-temperature uptake of CO on the freshly reduced catalyst is 1.3 ML. After 20 min of reaction at 463 K and a D₂/CO ratio of 3, the CO coverage decreases to 0.67 ML and the total amount of carbon exclusive of CO is 1.08 ML. The last of these figures compares very favorably with the value of $\Sigma n\theta_n = 1.03$ obtained from the simulation of the transient response experiments. Moreover, the sum of θ_{CO} plus $\Sigma \theta_n$ for n=1-13 is equal to 1.19-1.31 ML (see Table 5), in good agreement with the initial CO uptake capacity of the catalyst, 1.3 ML. A similar level of agreement is observed when the reaction is carried out at 483 K.

The close correspondence between the predicted and experimentally observed coverages by carbon indicates that the dynamics of the transient response experiments are governed primarily by the α (carbidic) and β ' (growing alkyl chains) forms of surface carbon (21). As noted by Krishna and Bell (27), these forms of carbon exhibit time constants that are much shorter than that associated with the build up and consumption of β " carbon, which

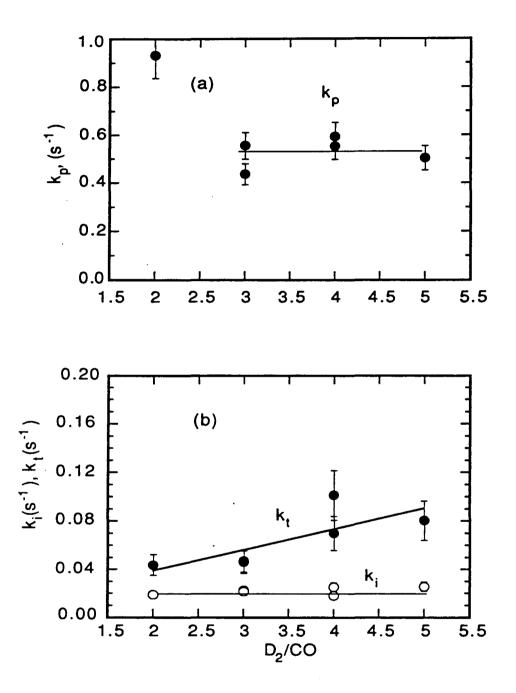
contribute to the slow deactivation of Ru.

The observation of a higher surface coverage by monomeric units than by growing chains is qualitatively consistent with the findings of Yokomizo *et al.* (21) for Ru/TiO₂ and Mims *et al.* (16) for Co/Al₂O₃. Yokomizo *et al.* (21) estimate the surface coverage by all C₁ species to be 0.25 ML, and the coverage by C₂₊ chains to be about 0.10 ML. This compares favorably with the present results which indicate a surface coverage of 0.12 ML by C₂₊ species and a coverage of 0.4 by all C₁ species. Since the estimates of surface coverages reported here and by Yokomizo *et al.* (21) are based on completely different methods, the degree of agreement is all the more remarkable.

Figure 12 indicates the effects of D_2 partial pressure on k_i , k_p , and k_t . The value of k_p is essentially independent of the partial pressure of D_2 , consistent with what would be expected, since chain growth does not involve adsorbed D atoms. By contrast, the value of k_t rises linearly with increasing D_2 partial pressure. This trend can be explained in the following manner. As defined, k_t is an apparent rate coefficient representing termination to olefinic and paraffinic products. Expressing k_t in terms of its component parts gives

$$k_{t} = k_{t}^{-} \theta_{v} + k_{t} \theta_{D}$$
(13)

where $k_t^{=}$ and k_t are the rate coefficients for termination to olefins and paraffins, respectively, and θ_v and θ_D are the vacancy and D atoms surface coverages, respectively. The increase in k_t with D₂ partial pressure can, therefore, be attributed to the increase in θ_D .





(a) Propagation rate constant, k_p , as a function of D_2/CO ratio; (b) Inititation rate constant, k_i , and termination rate constant, k_t , as a function of D_2/CO ratio

In agreement with this, the product distribution shifts to more paraffinic products as the D_2 partial pressure rises (see Fig. 7e). Equation 13 also helps explain the weak dependence of the olefin to paraffin ratio on temperature, seen in Fig. 7c. Since θ_D decreases and k_1 increases with temperature, the product of θ_D and k_1 should show a weaker temperature dependence.

The independence of k_i on D_2 partial pressure is puzzling, since as discussed above, this rate coefficient is, in fact, the product of an intrinsic rate coefficient and θ_D . No explanation can be given for why k_i does not behave in the same manner as k_t .

The dependence of the surface coverages of carbonaceous species calculated from the model is given in Fig. 13 and Table 6. The coverage by monomeric building units and C₁ chain initiators increases with D₂ partial pressure and approaches a constant value, whereas the surface coverage by C₂₋₁₂ chains appears to pass through a maximum. The trends in θ_m and θ_1 indicate that with decreasing D₂ partial pressure, the rate of conversion of nascent carbon atoms to CH_x species is somewhat faster than the consumption of these species to form reaction products. The total coverage by reactive species is seen to increase from 0.4 to 0.8 ML as the D₂/CO ratio is changed.

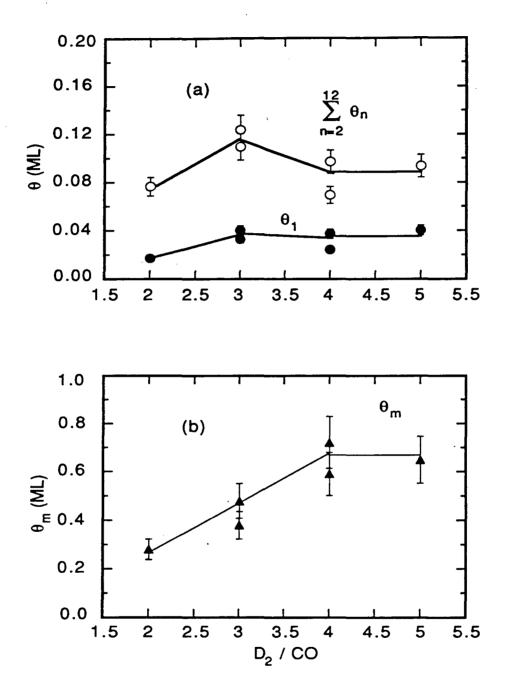


Fig. 13(a) Coverage by alkyl surface species as a function of D_2/CO ratio; (b) Coverage by monomeric species as a function of D_2/CO ratio; T = 463 K.

TABLE 6

| D ₂ /CO | θ ₁ (ML) | $\sum_{n=2}^{12} \theta_n (ML)$ | θ _m (ML) | Total θ _(n+m) (ML) |
|--------------------|---------------------|---------------------------------|---------------------|-------------------------------|
| 2 | 0.03 | 0.12 | 0.28 | 0.43 |
| 3 | 0.03 | 0.11 | 0.38 | 0.52 |
| 3 | 0.04 | 0.12 | 0.48 | 0.64 |
| 4 | 0.02 | 0.07 | 0.72 | 0.81 |
| 4 | 0.04 | 0.10 | 0.59 | 0.73 |
| 5 | 0.04 | 0.10 | 0.65 | 0.79 |

Coverage by reaction intermediates:

*

CONCLUSIONS

Isotopic tracer methods have been used to determine the dynamics of chain initiation, propagation and termination for Fischer-Tropsch synthesis over Ru/TiO₂. Values for the rate coefficients k_i , k_p and k_t were determined by fitting theoretically generated transient response curves to those obtained experimentally. The rate coefficient for chain initiation, k_i , is independent of both temperature and D₂/CO ratio. The rate coefficient for chain propagation, k_p , has an activation energy of 8 kcal/mol, but is independent of the D₂/CO ratio. The rate coefficient for chain termination, k_t , has an activation energy of 20 kcal/mol and increases linearly with D₂/CO ratio. The higher activation energy for chain termination than that for chain propagation explains the observed decrease in probability of chain growth, α , with increasing temperature.

The surface coverages by various carbonaceous species have also been determined from an analysis of the fitted transient response curves. It is concluded that the dominant species are monomeric building units, which occupy 0.2 to 0.6 ML. Growing alkyl chains, the direct precursors to hydrocarbon products occupy ≤ 0.2 ML. Adsorbed CO occupies an additional ≈ 0.7 ML. These estimates are found to be in good agreement with independent measurements made by temperature-programmed reaction spectroscopy.

APPENDIX

The apparent rate constant for propagation, $k_p \theta_m$, and the rate constant for termination, k_t , are calculated from α and τ using the following equations:

$$\alpha = \frac{k_p \,\theta_m}{k_p \,\theta_m + k_t} \tag{A1}$$

and

$$\tau = \frac{1}{k_p \theta_m + k_t}$$
(A2)

The value of τ is determined from a fit of eqn. 12 to the observed curves of $F_n(t)$.

The monomer coverage, θ_m , is calculated as follows. At steadystate, the rate of CO consumption must equal the rate at which monomeric species are consumed. This equality can be written as:

$$N_{\rm CO} = \frac{\theta_{\rm m}}{\tau_{\rm m}} \tag{A3}$$

Since N_{CO} is known from steady-state rate measurements and τ_m is known from the fit of eqn. 12 to the observed curves F_n(t), θ_m can be evaluated. The value of k_p can be determined from eqn. A2.

The value of k_i can be calculated by recognizing that the rate at which carbon atoms are consumed from the C₁ pool is equal to the rate at which carbon atoms enter this pool. This leads to eqn. A4.

$$\frac{\theta_1}{\tau} = k_i \theta_m \tag{A4}$$

Since

$$\frac{\theta_1}{\tau} = \frac{\frac{N_{C_1}}{k_1}}{\frac{1}{k_p \theta_m + k_1}} = \frac{N_{C_1}}{1 - \alpha}, \qquad (A5)$$

 k_i can be calculated from eqns. A4 and A5, using the measured values of N_{C1} and α , and the previously determined value of θ_m .

The coverages by alkyl species can be calculated from the hydrocarbon turnover frequencies and the value of k_t . Since

$$N_{Cn} = k_t \theta_n \tag{A6}$$

then

$$\sum_{n=1}^{n_1} \theta_n = \frac{1}{k_1} \sum_{n=1}^{n_1} N_{C_n}$$
(A7)

REFERENCES

- 1. Anderson, R. B., 'The Fischer-Tropsch Synthesis', Academic Press, New York, 1984.
- 2. Biloen, P. and Sachtler, W. M. H., Adv. Catal. 30, 165 (1981).
- 3. Kellner, C. S., and Bell, A. T., J. Catal. 70, 418 (1981).
- 4. Dry, M. E., Catal.-Sci. and Tech. 1, 150 (1981).
- 5. Dry, M. E., Catal. Today 6, 183 (1990).
- 6. Bell, A. T., Catal. Rev.-Sci. Eng. 23, 203 (1981).
- 7. Winslow, P., and Bell, A. T., J. Catal. 86, 158 (1984).
- 8. Winslow, P., and Bell, A. T., J. Catal. 91, 142 (19845).
- 9. Biloen, P., Helle, J. N., and Sachtler, W. M. H., J. Catal. 58, 95

(1979).

- 10.Bonzel, H. P., and Krebs, H. J., Surf. Sci. 91, 499 (1980).
- 11.Kobori, Y., Yamasaki, H., Naito, S., Onishi, T., and Tamaru, K., J. Chem. Soc., Far. Trans. i78, 1473 (1982).
- 12.Biloen, P., Helle, J. N., van den Berg, F. G. A., and Sachtler, W. M. H., J. Catal. 81, 450 (1983).
- 13.Orita, H., Naito, S., and Tamaru, K., J. Catal. 90, 183 (1984).

14.Zhang, X., and Biloen, P., J. Catal. 98, 468 (1986).

- 15.Mims, C. A., and McCandlish, L. E., *J. Am. Chem. Soc* **107**, 696 (1985).
- 16.Mims, C. A., and McCandlish, L. E., J. Phys. Chem. 91, 929 (1987).
- 17.Stockwell, D. M., and Bennett, C. O., J. Catal. 110, 354 (1988).
- 18.Stockwell, D. M., Bianchi, D., and Bennett, C. O., *J. Catal.* **113**, 13 (1988).
- 19.Biloen, P., J. Molec. Catal. 21, 17 (1983).
- 20.Bennett, C. O., in "Catalysis under Transient Conditions", eds: A. T. Bell and L. L. Hegedus, ACS Symposium Series **178**, 1 (1982).
- 21. Yokomizo, G. H., and Bell, A. T., J. Catal. 119, 467 (1989).
- 22.Vannice, M. A., J. Catal. 37, 449 (1975).
- 23. Vannice, M. A., and Garten, R. L., J. Catal. 56, 236 (1979).
- 24. Vannice, M. A., and Sudhakar, C., J. Phys. Chem. 88, 2429 (1984).
- 25. Reuel, R. C., and Bartholomew, C. H., J. Catal. 85, 78 (1984).
- 26. Rieck, J. S., and Bell, A. T., J. Catal. 99, 262 (1986).
- 27.Krishna, K. R. and Bell, A. T., J. Catal. 130, 597 (1991).
- 28.Sano, M., Yotsui, Y., Abe, H., and Sasaki, S., J. Biomed. Mass Spec.
 3, 1 (1976).
- 29. Matthews, D. E., and Hayes, J. M., Analyt. Chem. 50, 1465 (1978).

- 30. Jordan, D. S., and Bell, A. T., J. Phys. Chem. 90, 4797 (1986).
- 31.Jenson, V. G., and Jeffreys, G. V., "Mathematical Methods in Chemical Engineering", Second Edition, Academic Press, 1977.

32. Dictor, R. A., and Bell, A. T., Appl. Catal. 20, 145 (1986).

- 33.Schulz, H., C₁ Molec. Chem. 1, 231 (1985).
- 34. Froment, G. F., and Hosten, L. H., *Catal.-Sci. and Tech.* 2, 97 (1981).
- 35.Box, G. E. P., Hunter, W. G., and Hunter, J. S., "Statistics for Experimenters", John Wiley and Sons, 1978.
- 36. Shustorovich, E. and Bell, A. T., Surf. Sci. 248, 359 (1991).

Chapter V

The Effect of Ethylene Addition on Fischer-Tropsch Synthesis

ABSTRACT

The C₂ products formed over Ru catalysts during Fischer-Tropsch synthesis often lie well below the Anderson-Schulz-Flory line describing the C₄₊ products. This has lead to speculation that either the surface precursor to these products plays a special role in chain growth, or that the ethylene formed re-adsorbs and re-enters the chain growth process. In this study, the effect of adding small amounts of ethylene to the CO/H₂ feed is investigated, using 1³CO/H₂ and 1²C₂H₄ to differentiate between the carbon sources. Ethylene addition suppresses methanation and results in an increase in the C₃₊ hydrocarbon formation rates. Isotopic tracer studies show that ethylene-derived carbon is present in the C₃₋₈ product. Ethylene acts as an effective chain initiator, and ethylene-derived carbon accounts for 45% of a C₁ monomer species.

INTRODUCTION

The C_{3+} products observed during Fischer-Tropsch synthesis (FTS) are often characterized by an Anderson-Schulz-Flory (ASF) distribution. The concentration of methane usually lies above an extrapolation of the plot to lower carbon numbers, and the concentrations of C_2 and C_3 often lie below this line. The deviation of C_2 products from the ASF distributuion is particularly noticeable for FTS over Ru catalysts (1, 2). Two possible explanations have been proposed. The first is that the precursor to C_2 products may be characterized by a longer average lifetime than the precursors to higher molecular products (3, 4). The second possible explanation is that the ethylene, once formed, is readsorbed and reenters into the chain growth process (5, 6).

The first of these possibilities, the presence of a long lived C₂ intermediate during CO hydrogenation over Ru, has been suggested by Mims and co-workers (3, 4). Mims *et al.* (3) performed isotopic tracer experiments in which an abrupt switch was made from ${}^{12}CO/H_2$ to ${}^{13}CO/H_2$ in the reactor feed. NMR analysis of C₂ to C₅ olefin products allowed the determination of the fraction of ${}^{13}C$ at each position in these products. These studies showed that there are two distinct isotope replacement rates, with the two carbons at the aliphatic end having a distinctly longer average residence time than those in the remaining positions. Based on this evidence, the authors suggested the presence of two-carbon surface species that has a comparitively long residence time relative to higher molecular

weight surface species. The authors further proposed that these two-carbon species play the role of chain initiators. In a subsequent study, Mims *et al.* (4) proposed that these results could be explained by a model based on the assumption that initiators for chain growth spent over half their surface residence time as C_2 groups.

In situ addition of 1.2 % $C_2H_5NO_2$ to the CO/H₂ feed over a Ru/SiO₂ catalyst by Cavalcanti *et al.* (7) was performed to understand the role of the C₂ intermediate during FTS. The rate and selectivity for the C₃ through C₆ hydrocarbon products increased by 25% or more, while methane formation was reduced. An order of magnitude increase was seen in the C₂ and C₃ olefin to paraffin ratios. The addition of 1.2 % nitroethane did not alter the chain growth probability, which led the authors to speculate that the rates of chain initiation and propagation were both increased by comparable amounts when C₂H₅NO₂ was added. The authors concluded that both one-carbon and two-carbon units were formed, and that C₂H_x groups derived from C₂H₅NO₂ play an important role in enhancing chain initiation, while CH_x groups formed by hydrogenolysis participate in chain growth.

The effect of ethylene addition to CO/H₂ during FTS has been examined by a large number of investigators. Many of the older studies were conducted on Co and Fe catalysts and are reviewed by Eidus (8) and by Jordan and Bell (2). Over Co catalysts, added olefins readily incorporate into the FTS products and cause an increase in higher hydrocarbon production. Olefin readsorption is found to initiate hydrocarbon chains, the effectiveness of this process decreasing rapidly with increasing chain length. Olefins also decompose to one-carbon fragments which then serve as monomer for chain growth. Over Fe catalysts, most researchers reported an increase in the production of higher molecular weight hydrocarbon products when olefins were added to the feed. Ethylene was also reported to act as a chain initiator.

Several recent studies of the effects of ethylene addition have been carried out over Fe and Co catalysts and these are briefly detailed here. Snel and Espinoza (9) have carried out ethylene addition experiments using an Fe catalyst. Their results indicated that the addition of 5 to 10 % ethylene to the feed readily initiates chain growth without altering the chain growth probability. The olefin selectivity increases, while the rate of hydrocarbon synthesis virtually doubles. A substantial fraction of the ethylene was incorporated into the C_3 products, whereas the amount of methane formed decreased. The authors also concluded that propagation by ethylene was unlikely. The incorporation of a small amount of 14Clabelled ethylene during FTS over a doubly-promoted Fe catalyst was investigated by Tau et al. (10). 40% of the labelled ethylene was converted to ethane. The C₅₊ products contained \approx 10% of the ethylene. With increasing carbon number, a decrease in radioactivity/mole was observed. The authors concluded that 85 % of the incorporated ethylene initiates chain growth.

Percy and Walter (11) used isotopic labelling and NMR spectroscopy to study the effects of adding 2 % ethylene to the synthesis feed passed over a Co/Al catalyst. From an analysis of the

propene, it was concluded that some ethylene dissociated to C₁ fragments. Ethylene incorporation as a C₂ unit was also observed. Adesina and co-workers (12) studied the effect of adding 1-2 % ethylene to different feed CO/H₂ mixtures over a commercial Co catalyst. The rates of formations of C₃-C₇ hydrocarbons increased from 50 to 100 %. The rate of methane formation and the probability of chain growth, α , remained unchanged. The effect of C₂H₄ addition was largest for the C₃ products, and decreased progressively for the higher hydrocarbons. The conclusion was that ethylene acted as a chain initiator.

In the case of FTS over Ru catalysts, it has been postulated that the low yields of C_2 and C_3 olefins may be due to the reincorporation of these products into growing chains (1). **Studies** by Kellner and Bell (1) showed that at concentrations above 1 %, ethylene addition enhanced the C_3 and C_4 product formation but suppressed the synthesis of C_{6+} hydrocarbons. Kobori *et al.* (13) have examined the effect of adding 12C-labelled olefins to 13CO/H2 mixtures, using GC-MS product analysis. The addition of ethylene in a 1:1 ratio to the CO resulted in an increase in the C_3 and C_4 products, with C₃ showing the larger increase. The methanation rate decreased. Propylene addition caused an increase in the C_2 and C_4 product, with a concurrent drastic reduction in methane formation. Isotopic distributions for C1, C3-C5 alkanes indicate extensive 12C incorporation. When ${}^{12}C_2H_4$ was added, 59 % of the methane was ${}^{12}C_2$ labelled. More than 50 % of the C3-C5 alkanes consisted of only 12C-

labelled molecules, whereas the percentage of products that were all 13C-labelled was 4, 2 and 7 for C₃, C₄ and C₅ alkanes, respectively. 12C-labelled propylene and octene addition also resulted in a large fraction of the C₁-C₅ alkanes containing 12C. The authors concluded that carbon from the olefins can randomly incorporate into the reaction products. Morris *et al.* (14) studied the effects of ethylene and propylene addition on FTS over Ru supported on silica, 13x zeolite, titania and magnesia. For the silica and zeolite supported Ru, ethylene addition markedly enhanced the higher hydrocarbon formation rates without greatly influencing the mehanation rate, whereas for Ru/TiO₂ and Ru/MgO₂, the rate of higher hydrocarbons was enhanced by a factor of less than two and the methanation rate was reduced.

Jordan and Bell (2) have studied the interactions of ethylene with H₂ and CO over a Ru/SiO₂ catalyst, using isotopic labelling of the CO to differentiate carbon sources. These authors concluded that CO hydrogenation was strongly influenced by the presence of ethylene. The rates of C₃-C₆ hydrocarbon products increased, revealing maxima as the partial pressure of ethylene was increased. The methanation rate decreased when ethylene was added. With increasing partial pressure of ethylene, CO hydrogenation to hydrocarbons was progressively suppressed, while the hydroformylation of ethylene to propanal was enhanced. The product distribution could be described in terms of C₁ and C₂ monomer units that participate in chain propagation. The authors conclude that C₂H₄ is a more efficient source of intermediates for chain initiation and chain growth than CO.

Mims and coworkers (15) have investigated the effects of adding ethylene, 1-hexene and 1-octene on FTS over Ru/ γ -Al₂O₃. Concentrations of upto 5 % 12C- labelled olefin were added to H₂-13CO mixtures. From an analysis of the products by GC-MS and NMR spectroscopy, it was established that alkenes could initiate the growth of higher molecular weight hydrocarbons, and with a lower probability, depolymerize to form lower molecular weight hydrocarbons. With added alkene concentrations of less than 1 %, the product distribution was substantially altered. The production of all hydrocarbon products except methane was increased. The increase in rates was highest for carbon numbers adjacent to the added alkene, and decreased for progressively higher and lower carbon numbers. NMR analysis of the products showed the presence of a C_2 initiator at the alkyl end of the 1-alkene products when ethylene was co-fed. The fractional 12C-labelling of the last two positions of the 1-alkenes was \approx 75%. These results were attributed to chain initiation from adsorbed ethylene and further growth from a common C_1 pool. About 54 % of the carbon in the methane formed when ethylene was added to the feed derived from the ethylene.

The objective of this study was to investigate the effect of adding small amounts of ethylene to the CO/H_2 feed mixture, using labelled ¹³CO and ¹²C₂H₄ in order to differentiate between the carbon sources. Of particular interest was the determination of the extent to which chain initiation and propagation are affected by the added ethylene.

EXPERIMENTAL

A 3.3% Ru/TiO₂ (Degussa P25) catalyst was used. Catalyst preparation and characterization have been described in Chapter 4. 1.35 gm of catalyst was loaded into a quartz microreactor. The product sampling and analysis system used were also identical to that described in Chapter 4.

Addition of ethylene to the feed were accomplished by using mixtures of 420 ppm ethylene in He (Matheson Gas) or 2 % ethylene in He (Matheson Gas). All experiments were conducted at 1 atm, 463 K and a H₂/CO ratio of 3. Total flow rate to the reactor was 100 cm³/min comprised of 30 cm³/min of H₂, 10 cm³/min of CO and He or (He+ethylene) making up the remaining 60 cm³/min.

RESULTS

After 20 min of reaction in 10:30:60 mixture of CO:H₂:He, the He in the feed was abruptly replaced by a He/420 ppm ethylene mixture. This resulted in the effective addition of 252 ppm of ethylene to the reactor feed. This concentration is similar to the amount predicted for C₂ by an ASF line based on the C₄₊ products. This small amount of ethylene caused almost no change in the rate of hydrocarbon production, as seen in Figure 1. There was also no

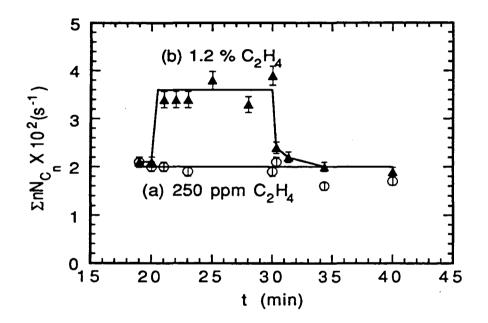


Fig. 1. Effect on total carbon in hydrocarbon product when ethylene is added to the CO/H₂ feed; (a) 250 ppm C_2H_4 . (b) 1.2 % C_2H_4 . Reaction conditions: T= 463 K; $H_2/CO = 3$. Ethylene is added from t = 20 min to t = 30 min.

change in the chain growth probability, α , which remained at 0.80 ± .02. Product analysis indicates that the C_2 product rose by a level equal to 32 % of the added ethylene. 68% of the added ethylene incorporated into products other than ethane, accounting for 2 % of these products. The rates of formation of the C_1 and C_{3+} products were unchanged. When 1.2 % ethylene was similarly introduced after 20 min of reaction, an immediate effect was seen (Fig. 1). The total rate of hydrocarbon production rose by a factor of 1.5. This rate is calculated as $\Sigma n N_{Cn}$, where N_{Cn} is the turnover frequency of the total hydrocarbon product of carbon number n. Figure 2 shows that the addition of 1.2 % C₂H₄ caused a small decrease in α to of 0.75 ± 0.2. After 30 min, a switch was made in the He stream back to pure He, and the activity dropped to the initial level in $CO/H_2/He$ and α rose to 0.8. Some deactivation was seen after 40 min on-stream consistent with the deactivation rate estimated for this catalyst in Chapter 2.

Experiments were also conducted in which reaction was started up in CO/H₂/He/1.2 % C₂H₄ and samples were taken between 20 and 40 min of reaction; these were then compared with reaction in the absence of ethylene. The results obtained confirmed the activity and α changes observed in the step change experiments shown in Fig. 1.

Of the ethylene fed, 12 % was converted to ethane and 82 % to other products. From these figures, it is determined that 68 % of the total hydrocarbon product, exclusive of C₂ products, derives from C₂H₄. The addition of 1.2 % C₂H₄ to the feed caused the CO

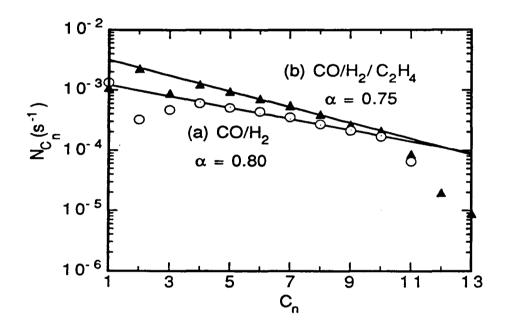


Fig. 2. Anderson-Schulz-Flory plot of N_{Cn} versus carbon number, C_n, in a) CO/H₂; (b) CO/H₂/C₂H₄. Reaction conditions: T= 463 K; H₂/CO = 3.

conversion to decrease from 20 % to 9 %.

The methanation rate decreased by 30 % upon C_2H_4 addition. Activity increases were observed for other products also, as can be seen from Figs. 2 and 3. Ethylene addition also resulted in an increase in the olefin content of the products. Figure 4 shows the olefin/paraffin ratio in the absence and presence of ethylene. There was no change in the identity of the reaction products formed when ethylene was added to the feed.

1

Experiments were also conducted in which 1.4 % C_2H_4 was reacted with 30 % H_2 in the absence of CO. The ethylene was completely converted since no ethylene was detected by gas chromatographic analysis of the reactor effluent. 54% of the ethylene was converted to methane, 43 % to ethane and 3 % to higher hydrocarbons upto C_{14} , which were detected in trace amounts.

To determine the extent to which the carbon derived from ethylene enters into the formation of hydrocarbon products, isotopic labelling was used. Reaction was initiated in $12CO/H_2/He/1.2 \% C_2H_4$ and after 20 min, the CO in the feed was replaced by 13CO. After 10 min in labelled CO, the CO in the feed was switched back to 12CO. Isotope-ratio gas chromatography (16, 17, 2) was used to study the incorporation of the 13C from the CO into the hydrocarbon products from C₃-C₈. In order to assess the effect of the added ethylene, this experiment was repeated in the absence of ethylene in the He diluent stream.

Figure 5a shows the the transient response of the fraction of each product that is 1^{3} C- labelled, F_n (n=3-8), when the feed is

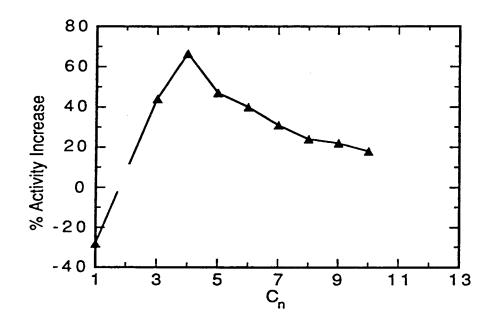


Fig. 3. Activity increase in rates of formation of hydrocarbon products as a function of carbon number, C_n , on addition of 1.2 % C_2H_4 to CO/H₂ feed.

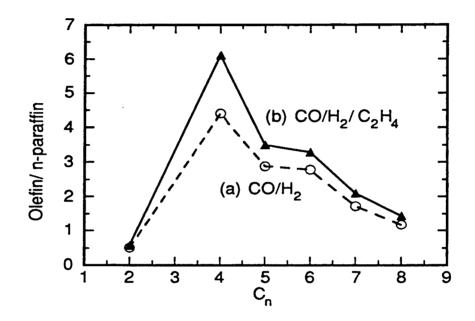


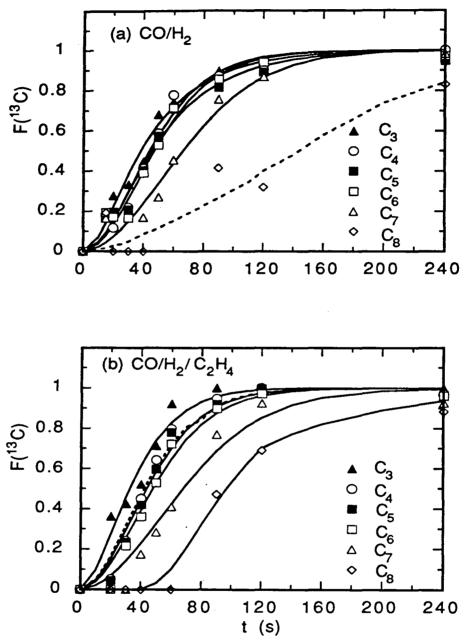
Fig. 4. Olefin/n-paraffin ratio as a function of carbon number, C_n in (a) CO/H₂; (b) CO/H₂/C₂H₄. Reaction conditions: T= 463 K; H₂/CO = 3.

changed from $12CO/H_2/He$ to $13CO/H_2/He$. These traces are similar to those presented in Chapter 4 and are representative of a sequential incorporation of 13C into the products. Figure 5b shows the corresponding transient responses when 1.2% ethylene is present in the feed. Due to the presence of the $12C_2H_4$, the products are never completely 13C labelled, and consequently, the steady-state value of the 13C fraction after 10 min in $13CO/H_2/He/12C_2H_4$ is used to normalize the fractions.

Table 1 lists the fraction of 1²C-labelled carbon in the C₃-C₇ products at steady-state reaction in $^{13}CO/H_2/He/^{12}C_2H_4$ (i.e., after 10 min of reaction). 1²C-labelled ethylene and ethane were also detected. These products were virtually 100% 1²C labelled because of the high concentrations of $^{12}C_2H_4$ in the feed.

DISCUSSION

Ethylene added to the CO/H₂ feed can facilely incorporate into the chain growth process; 68 % of the ethylene was incorporated into the non-C₂ hydrocarbon product when 250 ppm of ethylene was added to the CO/H₂ feed, and 82 % of the added ethylene was incorporated into C₁ and C₃₊ products when 1.2% ethylene was added. At the lower concentration, ethylene does not affect the rates of C₁ and C₃₊ product formation, but only displaces 2 % of the ¹³CO. At a level of 1.2 % C₂H₄, the overall rate of hydrocarbon product formation rose by 50 % (Fig. 1). This increase is similar to that



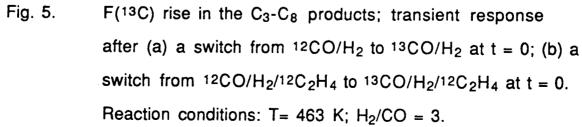


TABLE 1

Fraction ¹²C in product at steady state in a 1.2 % ${}^{12}C_{2}H_{4}/10$ % ${}^{13}CO/30$ % H₂/He mixture

| Carbon Number | F ¹² C (expt) | F ¹² C (C ₂ initiator) | F ¹² C (C ₂ initiator + 0.45 ¹² C ₁) |
|---------------|-----------------------------|-------------------------------------------------|--------------------------------------------------------------------------------------|
| 3 | 0.79 | 0.66 | 0.82 |
| 4 | 0.77 | 0.50 | 0.73 |
| 5 | 0.68 | 0.40 | 0.67 |
| 6 | 0.65 | 0.33 | 0.63 |
| 7 | 0.64 | 0.29 | 0.61 |
| 8 | 0.57 | 0.25 | 0.53 |

observed by other researchers upon ethylene addition (1, 2, 8, 9, 12-15). Conversion of CO to products is reduced from 20 % to 9 % in the presence of 1.2% ethylene (i.e., ethylene displaces 55 % of the ¹³CO) in a manner similar to that observed by Jordan and Bell (2), and CO accounts for only 32 % of the hydrocarbon product. The α value fell slightly on ethylene addition, (Fig. 2), in contrast to other reports (2, 9, 15). As can be seen from Figs. 2 and 3, this is due to the activity increase on ethylene addition being most pronounced for the C₃ and C₄ products and progressively decreasing for longer chains. This progressive decline in enhancement for the higher hydrocarbons was also noted by Mims *et al.* (15).

An increase in olefin to paraffin ratio (shown in Fig. 4) on 1.2 % C_2H_4 addition is also in agreement with observations made by Snel and Espinoza (9). A concurrent decrease in methanation is seen here and has also been reported by other researchers (2, 9, 13-15). A probable cause is a lower hydrogen coverage on the surface that results in a reduced hydrogenation capability of the catalyst in the presence of ethylene, which would account for both these changes in product selectivity.

The isotopic transients presented in Fig. 5 show that the dynamics of 1³C incorporation into the products is not altered by the presence of ethylene. This indicates that the added ethylene does not alter the mechanism of chain propagation and termination.

The results shown in Table 1 indicate that in the presence of 1.2% C_2H_4 , a large fraction of the products are ¹²C-labelled. If the added ethylene only contributes ¹²C₁ units to the monomer pool, the

fraction of 12C in all the products should be the same, at a level that reflects the fraction in this pool. The progressive decrease in the fraction of 12C carbon suggests that adsorbed ethylene acts primarily as a chain initiator. If this were the only role of the added $12C_2H_4$, then the fraction of 12C would be 66 % in the C₃ products and the 12C fraction would decrease rapidly in the higher molecular weight products with increasing number of carbon atoms. Table 1 shows the results of this calculation. Comparison with the experimental results reveals that the observed fractions are higher than these estimates and decrease much more gradually.

A slower decrease in the fraction of ¹²C-labelled products would occur, if, in addition to acting as a chain initiator, ¹²C₂H₄ contributes to the pool of C₁ monomer units (e. g., CH_{2,s}). It can be assumed that a fraction of the C₁ monomer pool is ¹²C-labelled, f_m, and further, that there is a constant fraction of C₂ initiators in the C₃₊ products, f_i. This would lead to the overall fraction of ¹²C in a product of carbon number n, F_n(¹²C) to be:

 $F_n(^{12}C) = \frac{1}{n} [2f_i + (n-2)f_m]$

A multiple-regression of this equation in two variables over the data for F_n (n = 3-8) yields values of $f_i = 1.03$ and $f_m = 0.45$. This indicates that the experimental results are consistent with every product molecule containing a ${}^{12}C_2$ initiator unit, and furthermore, that 45 % of the monomer is ${}^{12}C$ -labelled. Fixing this as the isotopic composition of the monomer pool, one can calculate the isotopic composition of the C_3 - C_8 products. The results shown in Table 1

indicate that the calculated isotopic compositions agree reasonably well with those observed.

The results in Table 1 can be compared with those of Kobori et al. (13) and Mims et al. (15). Kobori and co-workers (13) report that when ${}^{12}C_2H_4$ was added to ${}^{13}CO/H_2$ at a level of 0.79:1:2, 59 % of the methane was 12C-labelled. 13C_i fractions (fraction of molecules containing i 13C atoms) are reported for C3-C5 alkanes. These data show that 81 % or more of the $C_{3.5}$ molecules contain a ${}^{12}C_2$ unit. Calculations from Kobori et al.'s data show that the total fraction of 12C-labelled carbon is 85 % in the C₃ product, 88 % in the C₄ product and 69 % in the C_5 product. These data are also consistent with a model assuming extensive ${}^{12}C_2$ initiation and a monomer pool that contains 50-60 % 12C. The 59 % fraction of this pool that is indicated by the isotopic composition of the methane is probably higher than that of 45 % indicated by our study due to the higher ratio of ethylene to CO used here. Mims et al. (15) report that when less than 5 % ethylene was added to the CO/H₂ feed, the methane contained \approx 55 % ¹²C, and that the fractional ¹²C-labelling of the last two positions in the C_3 and C_4 1-olefins was 75%. These results can be compared to the 45 % 12C-labelled monomer pool, and the 100 % 12C2 initiation estimated here.

Jordan and Bell (2) have proposed that C_2 species can participate in chain propagation. If C_2 species were more efficient chain propagation units than C_1 species, the products with an even number of carbon units would probably contain more ${}^{12}C$ than the adjacent odd number products. Also, the incorporation of the ${}^{13}C$ from CO would be slower in the even number products. The data presented in Table 1 indicates that the fraction of 12C falls off with increasing carbon number, and the data shown in Fig. 5 show that 13C incorporates successively into each carbon number product from C_3 upwards. This leads to the conclusion that C_2 species are not more effective chain propagation units that C_1 species.

The data in Fig. 3 indicate that the maximum activity increase is seen for the C₄ product, in contrast to the results of Adesina *et al.* (12) and Mims *et al.* (15) who reported a maximum increase in the C₃ product. Data by Jordan and Bell (2) indicate that the rate of production of the C₄ hydrocarbons can exceed that of the C₃ hydrocarbons for a range of reaction conditions used. Also, C₄ is the dominant product when ethylene is present in the feed (see Fig. 2), as has also been noted by Jordan and Bell (2). This could be due in part to ethylene homologation; calculations based on the observed isotopic composition, a 1^2C_2 initiator, a 45 % 1^2C monomer pool and allowing for homologation indicate that roughly a fifth of the C₄ product may be formed by this process.

CONCLUSIONS

The effect of adding small amounts of ethylene to the CO/H_2 feed show that ethylene addition results in a substantial rate increase in hydrocarbon production, with the exception of methane. At an ethylene/CO ratio of 0.12, the ethylene accounts for 68 % of the hydrocarbon product. Isotopic tracer studies show that the ethylene-derived carbon is present in the C_3 - C_8 product, the fraction of such carbon decreasing as the hydrocarbon chain length increases. These observations lead to the conclusion that ethylene acts as an effective chain initiator, and as a source of carbon for C_1 monomer units. For the conditions of the present experiment, 100 % of the chain initiator and 45 % of C_1 species for chain propagation are derived from ethylene.

REFERENCES

- 1. Kellner, C. S., and Bell, A. T., J. Catal. 70, 418 (1981).
- 2. Jordan, D. S., and Bell, A. T., J. Phys. Chem. 90, 4797 (1986).
- 3. Mims, C. A., McCandlish, L. E., and Melchior, M. T., *Catal. Lett.* 1, 121 (1988).
- Mims, C. A., McCandlish, L. E., and Melchior, M. T., "Proceedings of the 9th International Congress of Catalysis", Vol IV, p1992 (1988).
- Iglesia, E., Reyes, S. C., and Madon, R. J., *J. Catal.* 129, 238 (1991).
- Madon, R. J., Reyes, S. C., and Iglesia, E., J. Phys. Chem. 95, 7795 (1991).
- 7. Cavalcanti, F. A. P., Oukaci, R., Wender, I., and Blackmond, D. G., J. *Catal.* **123**, 270 (1990).
- 8. Eidus, Ya. T., Russ. Chem. Rev. (Engl. Transl.) 36, 338 (1967).
- 9. Snel, R., and Espinoza, R. L., J. Molec. Catal. 43, 237 (1987).
- 10. Tau, L-M., Dabbagh, H. A., Chawla, B., and Davis, B. H., Catal. Lett.

7, 141 (1990).

- 11. Percy, L. T., and Walter, R. I., J. Catal. 121, 228 (1990).
- 12. Adesina, A. A., Hudgins, R. R., and Silveston, P. L., *App. Catal.* **62**, 295 (1990).
- 13. Kobori, Y., Yamasaki, H., Naito, S., Onishi, T., Tamaru, K., *J. Chem.* Soc, Faraday Trans. 178, 1473 (1982).
- 14. Morris, S. R., Hayes, R. B., Wells, P. B., Whyman, R., J. Catal. 96, 23 (1985).
- 15. Mims, C. A., Krajewski, J. J., Rose, K. D., and Melchior, M. T., *Catal. Lett.* 7, 119 (1990).
- 16. Sano, M., Yotsui, Y., Abe, H., and Sasaki, S., J. Biomed. Mass Spec.
 3, 1 (1976).
- 17. Matthews, D. E., and Hayes, J. M., Analyt. Chem. 50, 1465 (1978).

Appendix I

Data Acquisition and Reduction

This appendix describes data acquisition and reduction for the different types of experiments used to generate data presented in this thesis. Listings of computer programs that have been used for this purpose are provided at the end of this Appendix. Primary gas chromatography (GC) and mass spectrometry (MS) data acquisition and reduction programs are written in 'Turbobasic' (Borland International Inc., Scotts Valley, CA). Lotus 123 (Lotus Development Corporation, Cambridge, MA) has been used for further data reduction. These have been used on an IBM-PC (XT) microcomputer.

1. Data Acquisition

Data can be recorded from the MS or from the GC alone; also, GC-MS data where both data are followed (and are linked) can be followed. Three main data acquisition programs are used. The first, called "LOCTMS", is used to locate digital/analog (D/A) mass spectrometric peak locations; these are then used in the other two programs. The second, called "MSONLY", records MS data continuously for a user-programmed duration. Up to 5 masses can be monitored; data is collected at 2 readings/s for each mass programmed. The third program is called "TSNEWGC" and records GC-MS data; due to the lengthy nature of these experiments, data is stored only if a GC or MS peak is found. Peak-sensing criteria are built-in for the GC and MS separately and can be user-modified. This program is used for either GC data alone or GC-MS data. Data is collected on a GC channel and up to 5 MS channels at 2 readings/s. Detailed descriptions of these programs follow. All the programs are user-friendly and will prompt the operator to perform the next step at each stage.

1.1 LOCTMS

This program is used to search the mass spectrum for peak locations. The MS is first set up for computer control: 'Program' EXTernal, 'Function' MULTiplier and 'Gain' 6. The cursor keys now controls the external D/A location that sets the amu being scanned on the MS. The '6' key is coarse up, the '4' key is coarse down, the '8' key is fine up and the '2' key is fine down. An input of 'G' prompts the user to input the desired gain. Finally, the computer provides the desired D/A location after a peak is found.

1.2 MSONLY

MSONLY is used to generate on-line MS data. Initial input consists of a filename to save to on the 'B' drive, and the number of masses that are of interest, as well as the total length of the experiment (which is limited by the number of masses followed). Then on further prompting, the masses desired are programmed. A D/A location and external gain factor for each mass are required, and can be searched for, since 'LOCTMS' is built in to this program, or keyed in if already known. At this point, the input parameters are saved, and the computer display indicates its readiness to record data after a keystroke input prompt from the operator. This program is used for experiments such as temperature programmed surface reaction (TPSR; see Chapter 2 or 4) or on-line isotopic transients

(Chapter 4).

1.3 TSNEWGC

This program is used to acquire GC and GC-MS data. It is used for computer control of the 10-port GC 'load/inject' valve and the 16sample loop Multiposition GC valve(MPV) and also to externally start up the Perkin-Elmer Sigma 3B GC and subsequently the MS in order to analyze all the samples stored in the MPV.

The first part of the input consists of MS parameters, which are entered in a manner identical to that used in 'MSONLY'. Then GC loop data is entered; the user keys in the number of loops to be filled, the load time for each of these loops and the total time required for a sample to elute through the GC column. (This depends on the GC temperature program used.) Also programmed is the delay to start recording MS data after GC start-up; this allows the big injection air wave to elute through the MS without being recorded or changing the He carrier baseline. At this point, the computer waits for a user keypad prompt to begin the experiment.

The GC-MS temperature program takes \approx 30 min for each loop; there are a possible maximum of 16 such loops. So a large amount of data is generated as GC and MS readings versus time. Therefore, to simplify and limit data acquisition, the computer only stores data if a peak is detected in the GC or on any of the MS traces. Peak retention times and GC or MS reading vs. time data for 20 s around a peak are recorded. This is sufficient as each peak lasts about 6s. GC or MS peak criteria can be altered by the user in the program. MS criteria, which are more critical (since MS data is in general more noisy than the GC) can be changed by changing the input text file, 'mspkpar.txt'. This has 4 parameters, $\{n_1, n_2, n_3 \text{ and } n_4\}$; n_1 is the minimum step size in numbers from 0-4096. A number 1 corresponds to a 2.44 mV change in the 0-10V MS output to the A/D converter. The value used here is 2. n_2 is the minimum number of consecutive rising steps, each equal to or greater than n_1 . A value of 3 is used here. n_3 is the absolute peak height above the baseline and a value of 15 is used. Finally, n_4 sets the MS delay time between sampling to allow the MS readings to settle. This is currently set at 3000. Optimization of these parameters allows picking up almost all peaks that are visible on the screen, while minimizing the pick-up of random noise.

When the operator starts up the computer to begin the experiment, the computer initially 'homes' the 16-loop MPV and sets the 10-port valve to the LOAD position. It then switches the MPV to loop 2 and proceeds to fill loop 2 for the programmed loading time. Before it switches to loop 3, the computer beeps and awaits a userprompt. This is to allow the operator to do the isotopic transient switching. After the loading has re-commenced, the computer loads the required number of loops for the programmed loading times. The last loop to be filled is always loop 1. After all loop-loading is complete, the computer awaits a user-prompt to commence sampleinjection and GC-MS data acquisition. After this, it also waits for a GC-Ready signal from the GC. (Usually, it is ensured that when loading is complete, the GC is also ready for injection.)

When the GC is ready, the computer externally starts up the GC temperature program and immediately switches the 10-port GC

valve to the 'INJECT' position. Loop1 is the first loop to elute through the column. GC-MS data is now acquired for the input time/loop. After the sample has eluted, the IBM-PC writes the peak information to disk and again waits for the GC to get ready before switching the MPV to the next loop for injection. When saving the data for loop n, the computer also checks that there is sufficient space for the next loop data, and if found to be insufficient, a message appears on the screen, prompting the user to insert another disk and hit enter, before the next loop is injected. After all the loaded loops are eluted, the computer stops data acquisition. There is an error-handling Turbobasic subroutine built into TSNEWGC that writes into an error file if the program is abruptly terminated in the middle of an experiment. This aids trouble-shooting if the program fails.

2.0 Data Reduction

There are two programs which read data acquired by 'MSONLY' and 'TSNEWGC'. This data is then stored in files that are imported into LOTUS 123 worksheets, which are used for the next step in data analysis. Finally, if model fitting is required, a FORTRAN program, 'MINIMUM' is used.

2.1 Reading MS or GC-MS data

'MSONLY' data is read by a program called 'READMS'. This program will display on the screen the mass spectrum of any of the masses recorded; these can also be plotted on a Hewlett Packard plotter to provide a hard copy. There are two little cursors that appear on the screen that can be moved using the right and left arrow cursor keys. These can be positioned where desired and if 'B' is entered, a new baseline will be drawn between them. If they are positioned and 'return' is entered, the area between the two cursors will be integrated and printed out on the screen. The average carrier He signal is also computed. The data for any mass can also be saved to disk as time-reading x-y pairs for further analysis by LOTUS. Calibrations are then used to convert the MS areas to actual amounts of products. MS data is usually normalized to the He signal to account for changes in the MS electron multiplier gain.

'TSNEWGC' data is read by a program called 'READTS'. This allows us to look at any loop. GC or MS data can be separately scanned, peak by peak, and peak areas can be integrated using the two screen cursors. This takes a lot of time when many peaks are present and so in both cases, the data can be automatically integrated using the 'Autointegrate' option. The most used feature of this program is the 'Autoalign' option; this will autointegrate the GC and every MS spectrum recorded for a given loop, then align the GC peaks to a library of known compound based on GC peak retention times, and finally align the MS peaks to the corresponding GC peak based on input GC-MS time delay for each known GC peak. The final step is a printout of all the data; integrated GC peaks and each MS channel and finally the aligned, integrated GC/MS data. The GC-MS data is saved to disk.

The GC- MS data is first examined for accurate peak identification and GC-MS peak line-up. (Since retention times are very sensitive to GC carrier flow rate and temperature program, there can be some variations.) Also, at low concentrations,

especially in the MS, peaks are not well-separated and require manual integration using the cursors. Any such corrections are noted on the GC-MS data hard copy. The next step in data reduction uses a LOTUS 123 spread sheet. Usually there may be up to 60-70 GC peaks and MS peaks corresponding to these on 4 masses for each sample loop, and a possible 16 such samples.

2.2 LOTUS 123 Data Analysis

The large quantity of data necessitates the use of three worksheets for data analysis. First, the GC-MS data are imported, loop by loop, into a LOTUS worksheet. This is the 'raw' data, and in this worksheet, blanks are inserted for missing peaks and any corrections in peak identification or areas is incorporated. Data for each loop consists of 5 columns; peak ID, peak number, GC area, and MS areas normalized by the He signal for ¹² and ¹³ labelled compounds.

Once the 'GCMS.RAW' spreadsheet is created, GC data is analyzed in a separate spreadsheet. Here, GC areas are copied from the .RAW worksheet for each loop; calibrations for C_{1-14} species are used to convert these areas to concentrations. For each loop, the sum of all the concentrations for each carbon number is calculated; these sums are further used to obtain an ASF chain growth parameter for each loop. Finally, a calculation is made of the ΣnN_{Cn} product to calculate overall CO conversion for each loop.

The final worksheet is used for GC-MS data analysis. Here, for each loop, GC concentrations are imported from the GC worksheet;

MS data is copied from the .RAW worksheet. Here, MS calibrations are used to obtain 12 and 13C MS peak concentrations. These are then divided by the corresponding GC peak concentration to obtain fractional isotopic concentrations. At a given carbon number, the MS concentrations of all detected peaks are added together and divided by the total concentrations of those peaks (obtained from GC data) for 12C-labelled and 13-C labelled isotopic fractions. MS data is often noisy, and there is also a 1% 12CO impurity in the feed 13CO; hence, further normalization is necessary. The steady state loop data in either isotope is used for this purpose. (Typically, loop 2 is the steady-state in $12CO/H_2$ and loop 10 the steady-state in ¹³CO/H2.) All data is converted to isotopic rise data, by using the fact that $F^{rise}+F^{fall} = 1.0$ at any time; for each time, the average of the ¹²C and ¹³C rise curve for each product is calculated. Finally, 16 points of t, Frise(t) are obtained. This data is now fitted to the chain growth model using a FORTRAN program, 'Minimum'. This is described in Appendix 3.

MSONLY.TXT

1 REM Turbo Basic program to run MS for Kamala ver 1.0 04-26-88 10 KEY OFF:CLS:REM turn off key line 12 PRINT "Switch valve interface to manual" 14 PRINT "Type any key to continue" 16 IF INKEY\$="" THEN 16 20 PRINT "Place DATA disk into drive B:" 40 INPUT "Enter file name you want to save on ";FLNAME\$ 60 OPEN "b:"+FLNAME\$+".cmy" FOR OUTPUT AS #2 70 PRINT "Enter comments, terminate with a blank line" 80 INPUT COMMENT\$: IF COMMENT\$="" THEN 92 90 PRINT#2,COMMENT\$:GOTO 80 92 CLOSE 2 100 BASE1=&H300 110 HEXTABLE\$="0123456789ABCDEF" 120 OUT BASE1+3,&H90:REM init Metrabyte PIO12 130 INJECTOR=BASE1+1:LOOPVALVE=BASE1+2:STATES=BASE1 140 LD=2:INJECT=4:FIDSTART=1:INJNORM=&H6 150 STP=&H80:HOME=&H40:SELPOS=&H20:LOOPNORM=&HFF **160 OUT INJECTOR.INJNORM** 170 OUT LOOPVALVE.LOOPNORM 180 OPEN "com1:1200,n,7,1,rs,cs,ds,cd"AS 1:REM open channel of Omega 200 BASE2=&HE6A0 210 ATOD=BASE2:DTOA=BASE2+4:COUNTER=BASE2+8:PLOTTER=BASE2+12 220 ADSTART=BASE2+&H1C:CTRESET=BASE2+&H1D:RDYCLR=BASE2+&H1E: SCAN1=BASE2+&H1F 230 REM program 8255s of the GCMS interface 240 OUT ATOD+3,&H92:OUT DTOA+3,&H89:OUT COUNTER+3,&H92:OUT PLOTTER+3.&H80 250 REM define dafault I/O condition 260 OUT COUNTER+2,16+4+1:REM select time-base 2 Hz 270 OUT DTOA+1,0:OUT DTOA,0:REM set mass program to 0 280 OUT PLOTTER+2,255:OUT PLOTTER+1,255:OUT PLOTTER,255:REM zero plotter

290 OUT ATOD+2,0+6*32:gain%=6:REM select ch.0 and gain factor 6 370 DEF FNFREESPACE(DRIVE%) 'find free space on drive 380 REG 4, DRIVE% '0=default.1=A:.2=B:.etc. 'AH=function number 390 REG 1.&H3600 'DOS function call 400 CALL INTERRUPT & H21 410 FNFREESPACE=CSNG(REG(2))*REG(3)*REG(1) **420 END DEF** 490 REM 510 GOSUB 5000:REM get MS parameters 520 numm=nummass% 550 NEED=(NUMM*5000+1000) 552 IF NEED>FNFREESPACE(2) THEN PRINT "Not enough disk space **562 PRINT** 570 PRINT "Turn damping control of UTI to min." 580 PRINT "Select gain control of UTI to (-11)" 600 PRINT "Type any key when ready" 610 IF INKEY\$="" THEN 610 620 REM DATA ACQ. START HERE------622 MASSPG=MASSLOC(0):GOSUB 1000:REM move mass program to 1st mass 624 OUT ATOD+2,0+MASSGAIN%(0)*32:REM select 1st mass gain and ch. 0 630 STARTDATE\$=DATE\$:STARTTIME\$=TIME\$:IF STARTDATE\$<>DATE\$ **THEN 630** 632 GOSUB 4000:REM save parameters 644 SCREEN 2:CLS:REM graphics screen 680 GOSUB 3000:REM data acquisition procedure 682 out atod+2,0+6*32:rem switch to ch.0 and gain 6 690 GOSUB 4200:REM data saving procedure 702 SCREEN 0:REM text screen again 710 FINISHDATE\$=DATE\$:FINISHTIME\$=TIME\$:IF FINISHDATE\$<>DATE\$ **THEN 710** 720 PRINT "experiment starts at ";STARTDATE\$;" ";STARTTIME\$ 730 PRINT " finishes at ";FINISHDATE\$;" ";FINISHTIME\$ 740 OUT ATOD+2,0+6*32:gain%=6:REM select ch.0 and gain factor 6

```
990 END:REM end of main
program-----
            output dtoa data------
      REM
1000
1010 IF MASSPG<0 THEN MASSPG=0
1020 IF MASSPG>65535! THEN MASSPG=65535!
1030 MVAL=INT(MASSPG/256):LVAL=MASSPG-MVAL*256
1040 OUT DTOA+1.MVAL:OUT DTOA,LVAL
1050 RETURN
3000 REM data acquisition
procedure-----
3030 element%=0:x1=0:y1=199
3010 rdyfg=(INP(ATOD+1) AND &H20):REM WAIT UTIL COUNTER IS
READY
3013 if rdyfg=0 then goto 3010
3014 OUT RDYCLR,0:REM clear counter ready flag
3200
      REM
            read
                  masses-----
3202 if nummass%=0 then 3400:rem no mass
3210 FOR I=0 TO NUMMASS%-1
3220 REM mass is selected in previous loop
3260 OUT ADSTART, 0:REM strobe A to D
3270 MASSREAD%=(INP(ATOD+1) AND 15)*256+INP(ATOD):REM read
mass intensity
3280 MASSINT%(element%,I)=MASSREAD%:REM put reading into
buffer
3290 IF I=(NUMMASS%-1) THEN NEXTMASS%=0 ELSE NEXTMASS%=I+1
3300 out atod+2,0+massgain%(nextmass%)*32:rem select new gain
3310 MASSPG=MASSLOC(NEXTMASS%):GOSUB 1000:REM program
nextmass
3320 for xxx=0 to 20:next:rem delay gen
3380 NEXT I:REM NEXT MASS------
3390 v2=199-massread%/22:x2=x1+1
3400 line (x1,y1)-(x2,y2)
3402 x1=x2:y1=y2
3404 if x1>600 then x1=0:y1=199:cls
3410 ELEMENT%=ELEMENT%+1
3412 LOCATE 23,1:PRINT "At point ";ELEMENT%
```

3430 if element% < numpoint% then 3010 3470 RETURN: REM data acq proedure return-----REM Saving parameters routine-----4000 4010 PRINT "Saving parameters; please wait" 4020 OPEN "b:"+FLNAME\$+".paz" FOR OUTPUT AS #2 4040 PRINT#2,NUMMASS% 4042 print#2,numpoint% 4050 FOR I=0 TO NUMMASS%-1 4060 PRINT#2, MASSNUM%(I), MASSGAIN%(I) 4070 NEXT I 4140 CLOSE 2:RETURN:REM ------4200 REM saving data -----4202 LOCATE 1,1 4204 PRINT "Saving data, please wait" 4340 DEF SEG=VARSEG(MASSINT%(0,0)) 4350 LENGTH=VARPTR(MASSINT%(numpoint%,NUMMASS%-1)) 4360 BSAVE "b:"+FLNAME\$+".mas",0,LENGTH 4590 RETURN:REM======= 5000 REM get MS parameters ------5010 INPUT "Enter number of masses interested ";NUMMASS% 5011 maxpoint%=int(16000/nummass%):print "Max. # of points ";maxpoint% 5012 input "Enter number of data points per mass ";numpoint% 5013 if numpoint%>maxpoint% then print "out of range":goto 5012 5014 if nummass%=0 then 5300 5016 dim massint%(numpoint%,nummass%) 5017 dim massnum%(nummass%),massloc(nummass%),massgain%(nummass%) 5020 PRINT "Locate mass :" to the prompt of 'LOCATE' use keypad key" 5030 PRINT " 5040 PRINT " '8' for fine up" 5050 PRINT " '2' for fine down" 5060 PRINT " '6' for coarse up" 5070 PRINT " '4' for coarse down" 5080 PRINT " to move mass around " 5082 PRINT " 'K' to use key entry" 'G' 5084 PRINT " to select gain"

```
5090 PRINT and 'ENTER' to select location":PRINT
5100 MASSPG=0:GOSUB 1000:REM preset to mass 0
5110 FOR I=0 TO NUMMASS%-1
5120 PRINT I+1;" ";
5130 INPUT "enter mass number ";MASSNUM%(I)
5140 PRINT "LOCATE
5150 TEMP$=INKEY$:IF TEMP$="" THEN 5150
5160 IF ASC(TEMP$)=13 THEN 5250:REM select location of mass
5162 if temp$="K" then 5242
5164 if temp$="G" then gosub 5400:rem change gain%
5170 IF LEN(TEMP$)<>2 THEN 5150
5180 TEMP=ASC(RIGHT$(TEMP$,1))
5190 IF TEMP=72 THEN MASSPG=MASSPG+1
5200 IF TEMP=80 THEN MASSPG=MASSPG-1
5210 IF TEMP=77 THEN MASSPG=MASSPG+100
5220 IF TEMP=75 THEN MASSPG=MASSPG-100
5230 GOSUB 1000:REM program D to A
5240 GOTO 5150
5242 input "Enter D to A setting ";MASSPG:gosub 1000
5250 PRINT "at D to A setting of ";MASSPG
5260 MASSLOC(I)=MASSPG
5270 MASSGAIN%(I)=gain%
5272 print "gain control for mass";massnum%(i);" is";massgain%(i)
5280 PRINT
5290 NEXT I
5300
RETURN:REM------
5400 rem change gain% ------
5410 input "enter mass gain (0 to 7) ";gain%
5420 if (gain%<0) or (gain%>7) then 5410:rem out of range
5450 out atod+2,gain%*32:rem switch gain
5460
       return:rem -----
```

100 REM loading data from MSONLY program ver 1.0 5-27-88 by Henry Chan 110 base2=&he6a0 120 plotter=base2+12 130 out plotter+3,&h80 140 xplot%=0:yplot%=0:gosub 4200:rem zero plotter 310 PRINT "Place data disk in drive B:, type any key to continue" 312 IF INKEY\$="" THEN 312 314 FILES "b:*.paz" 320 INPUT "Enter file name ";FLNAME\$ 330 OPEN "b:"+FLNAME\$+".cmy" FOR INPUT AS #2 340 WHILE NOT EOF(2) 350 LINE INPUT#2, COMMENT\$ **360 PRINT COMMENT\$ 370 WEND** 380 CLOSE 2 390 INPUT "Is this the right one (y/n) ";YES\$ 400 IF YES\$="y" THEN 430 410 IF YES\$="n" THEN 310 420 GOTO 390 **430 PRINT** 500 REM Loading parameters-----510 PRINT "Loading parameters, please wait" 520 OPEN "b:"+FLNAME\$+".paz" FOR INPUT AS #2 540 INPUT#2.NUMMASS%:PRINT "Number of masses observed =":NUMMASS% 542 input#2,numpoint% 544 dim massint%(numpoint%,nummass%),massnum%(nummass%),massgain%(nummass%) 546 dim ydel%(10) 550 FOR I=0 TO NUMMASS%-1 560 INPUT#2, MASSNUM%(I), MASSGAIN%(I) 570 PRINT "MASS";I+1;"is";MASSNUM%(I),"Gain factor";MASSGAIN%(I) 580 NEXT I 660 CLOSE 2:REM parametes loaded------

1000 REM read data-----1100 print "reading data; please wait" 1110 def seg=varseg(massint%(0,0)) 1120 bload "b:"+flname\$+".mas",0 1180 screen 2 1190 rem data loaded------1200 rem display data 1210 for i=0 to nummass%-1 1220 print "mass";massnum%(i);" used gain factor";massgain%(i) 1230 next i 1240 input "Which mass (0 to exit)";massdisp% 1241 if massdisp%=0 then 2990 1250 msptr%=-1 1252 for i=0 to nummass%-1 1260 if massnum%(i)=massdisp% then msptr%=i 1262 if massnum%(i)=4 then refptr%=i 1270 next i 1280 if msptr%=-1 then print "mass not found; try again":goto 1200 1281 input "Save in x,y pair (y/n) ";an\$ 1282 if an\$<>"y" then 1284 else gosub 4400 1283 input "Do you want to continue to plot (y/n) ";an\$:if an\$<>"y" then 2980 1284 input "Plotter output (y/n) ";an\$ 1285 if an\$="y" then plotyes=1 else if an\$="n" then plotyes=0 else goto 1282 1286 if plotyes then print "Plotting is selected" 1290 print "Calculating scale; please wait" 1300 ymax%=-1:ymin%=4096 1310 for i=0 to numpoint%-1 step int(1+numpoint%/600) 1320 y%=massint%(i,msptr%) 1330 if y%>ymax% then ymax%=y%:xmax%=i 1340 if y%<ymin% then ymin%=y%:xmin%=i 1350 next i 1352 print ymax%, xmax%, ymin%, xmin% 1360 yscale%=(ymax%-ymin%)/170+1 1362 print yscale% 1370 yoffset%=ymin%

```
1380 print yoffset%
1390 print "Resetting plotter, lift pen and type any key to continue"
1400 if inkey$="" then 1400
1410 xplot%=0:yplot%=0:gosub 4200:rem zero plotter
2000 print "Type any key to start plotting routine"
2004 if inkey$="" then 2004
2006 base1%=0:base2%=numpoint%-1:head%=base1%:tail%=base2%
2010 cls:gosub 3000:xplot=0
2090 xscale%=numpoint%/600+1
2094 intsts=0:integral=0:flag%=0
2096 x1=0:y1=190-(massint%(0,msptr%)-yoffset%)/yscale%
2098 if plotyes then inc=1 else inc=int(1+numpoint%/600)
2100 for i=0 to numpoint%-1 step inc
2110 x2=i/xscale%:y%=massint%(i,msptr%):yplot%=y%
2120 y2=190-(y%-yoffset%)/yscale%
2140 line (x1,y1)-(x2,y2)
2141 if plotyes then gosub 4200
2142 y1=y2:x1=x2:xplot=xplot+0.90:xplot%=int(xplot)
2290 if inkey$=chr$(27) then i=numpoint%:flag%=1
2300 next i
2302 if flag%=1 then 2980
2304 plotyes=0
2310 locate 2,1:print "Integration routine; use 'ESC' to return to
main menu "
2330 y1=190-(massint%(base1%,msptr%)-yoffset%)/yscale%
2340 y2=190-(massint%(base2%,msptr%)-yoffset%)/yscale%
2350 line (base1%/xscale%,y1)-(base2%/xscale%,y2):rem line base
line
2352 locate 4,1:print "BASE LINE " massint%(base1%,msptr%);" at
";base1%;" ";
                                                               ۳.
2354 print massint%(base2%,msptr%);" at ";base2%;"
2360 y1=190-(massint%(head%,msptr%)-yoffset%)/yscale%
2370 y2=190-(massint%(tail%,msptr%)-yoffset%)/yscale%
2380 line (head%/xscale%,y1-10)-(head%/xscale%,y1-20)
2390 line (tail%/xscale%,y2-10)-(tail%/xscale%,y2-20)
                                                           н.
2392 locate 5,1:print massint%(head%,msptr%); " at ";head%;"
2394 print massint%(tail%,msptr%);" at ";tail%;
۳.
```

```
2400 ky$=inkey$:if ky$="" then 2400
2410 ky%=asc(ky$)
2420 if ky%=27 then 2980
2430 if ky%=13 then 2600
2440 if ky$="B" then gosub 2800:base1%=head%:base2%=tail%:goto
2330
2442 if ky$="R" then goto 2010:rem redraw
2445 if ky$="8" then if head%<numpoint%-21 then
nhead%=head%+20:goto 2510
2446 if ky$="2" then if head%>20 then nhead%=head%-20:goto 2510
2447 if ky$="6" then if tail%<numpoint%-21 then
ntail%=tail%+20:goto 2510
2448 if ky$="4" then if tail%>20 then ntail%=tail%-20:goto 2510
2450 if len(ky$)<2 then 2400
2460 temp=asc(right$(ky$,1))
2470 if temp=72 then if head%<numpoint%-1 then nhead%=head%+1
2480 if temp=80 then if head%>0 then nhead%=head%-1
2490 if temp=77 then if tail%<numpoint%-1 then ntail%=tail%+1
2500 if temp=75 then if tail%>0 then ntail%=tail%-1
2510 line (head%/xscale%,y1-10)-(head%/xscale%,y1-20),0
2520 line (tail%/xscale%,y2-10)-(tail%/xscale%,y2-20),0
2530 head%=nhead%:tail%=ntail%
2540 aoto 2360
2600 rem integrate
2610 locate 5,40:print "Integrating; please wait
2620 sum=0:sum1=0:offs=0
2622
slope=(massint%(base2%,msptr%)-massint%(base1%,msptr%))/(base
2%-base1%)
2624 yx0=massint%(base2%,msptr%)-slope*base2%
2630 offs=((tail%+head%)/2*slope+yx0)*(tail%-head%+1)
2640 for ji=head% to tail%
2650 sum=sum+cdbl(massint%(ji,msptr%))
2652 sum1=sum1+cdbl(massint%(ji,refptr%))
2660 next ji
2670 sum=sum-abs(offs)
2680 locate 6,40:print "Mass 4 average
";int(abs(sum1/(tail%-head%+1)));
```

```
۳.
2682 locate 5,40:print "Integral= ";int(sum);"
```

```
2690 goto 2400
2800 rem clear base line
2810 y1=190-(massint%(base1%,msptr%)-yoffset%)/yscale%
2820 v2=190-(massint%(base2%,msptr%)-yoffset%)/yscale%
2830 line (base1%/xscale%,y1)-(base2%/xscale%,y2),0:rem line base
line
2840 return
2980 cls:goto 1200
2990 end
3000 rem ymax% subroutine
3020 locate 1,1:print flname$;" MASS"massdisp%;"
YMAX";ymax%;"at";xmax%;
3022 print " YMIN"; ymin%; "at"; xmin%
3030 print "use 'ESC' key to abort display";
3031 if plotyes then print "; Plotting is selected";
3032 locate 24,1:print i;:locate 25,73:print numpoint%;
3040 return
4200 rem output to plotter
                              -----
4210 if xplot%<0 then xplot%=0
4220 if xplot%>4095 then xplot%=4095
4230 if yplot%<0 then yplot%=0
4240 if yplot%>4095 then yplot%=4095
4250 plot0%=255-yplot% and 255
4260 plot2%=255-xplot% and 255
4270 plot1%=255-(int(xplot%/256)*16+int(yplot%/256))
4280 out plotter+2,plot2%:out plotter+1,plot1%:out plotter,plot0%
4290
        return:rem -----
4400 rem saving x,y pair------
4405 print "Make sure you have enough disk space in drive B:"
4410 input "Please enter new filename for X.Y pair ";flname1$
4412 open "b:"+flname1$ for output as #2
4420 for i=0 to numpoint%-1
4430 print#2, i/2,massint%(i,msptr%)
4440 next i
4450 close 2
```

TSNEWGC.TXT

1 REM Turbo Basic program to run GCMS for Kamala ver 3.10 04-29-90 2 on error goto 9000 4 open "mspkpar.txt" for input as 2 5 input#2,mspkstp%:input#2,mspkre%:input#2,mspkht%:input#2,msdel av% 6 close 2 10 KEY OFF:CLS:REM turn off key line 12 PRINT "Switch valve interface to manual" 14 PRINT "Type any key to continue" 16 IF INKEY\$="" THEN 16 20 PRINT "Place DATA disk into drive B:" 40 INPUT "Enter file name you want to save on ";FLNAME\$ 50 mkdir "b:\"+flname\$:flnamed\$=flname\$:flname\$="b:\"+flname\$+"\"+flname\$: drive%=1 60 OPEN FLNAME\$+".cmm" FOR OUTPUT AS #2 70 PRINT "Enter comments, terminate with a blank line" 80 INPUT COMMENTS: IF COMMENTS="" THEN 92 90 PRINT#2,COMMENT\$:GOTO 80 92 CLOSE 2 100 BASE1=&H300 110 HEXTABLE\$="0123456789ABCDEF" 120 OUT BASE1+3,&H90:REM init Metrabyte PIO12 130 INJECTOR=BASE1+1:LOOPVALVE=BASE1+2:STATES=BASE1 140 LD=2:INJECT=4:FIDSTART=1:INJNORM=&H6 150 STP=&H80:HOME=&H40:SELPOS=&H20:LOOPNORM=&HFF **160 OUT INJECTOR, INJNORM** 170 OUT LOOPVALVE, LOOPNORM 180 OPEN "com1:1200,n,7,1,rs,cs,ds,cd"AS 1:REM open channel of Omega 200 BASE2=&HE6A0 210 ATOD=BASE2:DTOA=BASE2+4:COUNTER=BASE2+8:PLOTTER=BASE2+12 220

```
ADSTART=BASE2+&H1C:CTRESET=BASE2+&H1D:RDYCLR=BASE2+&H1E:
SCAN=BASE2+&H1F
230 REM program 8255s of the GCMS interface
240 OUT ATOD+3,&H92:OUT DTOA+3,&H89:OUT COUNTER+3,&H92:OUT
PLOTTER+3.&H80
250 REM define dafault I/O condition
260 OUT COUNTER+2,16+4+1:REM select time-base 2 Hz
270 OUT DTOA+1,0:OUT DTOA,0:REM set mass program to 0
280 OUT PLOTTER+2,255:OUT PLOTTER+1,255:OUT PLOTTER,255:REM
zero plotter
290 OUT ATOD+2,0+6*32:gain%=6:REM select ch.0 and gain factor 6
300 DIM MASSINT%(103,200),GC%(60,80)
310 DIM GCPKST%(1,80),gcpara%(585)
320 DIM MASSNUM%(7), MASSLOC%(1,7), LOADTIME%(15)
340 DIM GC$(2)
350 GC$(1)="FID":GC$(2)="TCD"
370 DEF FNFREESPACE(DRIVE%) 'find free space on drive
                         '0=default,1=A:,2=B:,etc.
380 REG 4, DRIVE%
390 REG 1,&H3600
                         'AH=function number
400 CALL INTERRUPT & H21
                           'DOS function call
410 FNFREESPACE=CSNG(REG(2))*REG(3)*REG(1)
420 END DEF
490 REM
500 INPUT "Please choose which GC 1. FID, 2. TCD ";GCTYPE%
502 IF (GCTYPE%<1) OR (GCTYPE%>2) THEN PRINT "WRONG TYPE":GOTO
500
510 GOSUB 5000:REM get MS parameters
520 GOSUB 5400:REM get loop loading parameters
530 INPUT "Select GC recording loop (0 to select all loops)
":GCRECORD%
540 IF (GCRECORD%<0) OR (GCRECORD%>NUMLOOP%) THEN PRINT "OUT
OF RANGE":GOTO 530
560 INPUT "Enter time (sec.) for each loop "; DUETIME%
562 PRINT
570 PRINT "Turn damping control of UTI to min."
580 PRINT "Select gain control of UTI to (-11)"
```

590 PRINT "Program the Omega for ramp and soak cycle" 592 PRINT "Put Omega to remote control" 594 PRINT "Switch valve interface to computer" 596 print "Turn gas valve for loading" 600 PRINT "Type any key when ready" 610 IF INKEY\$="" THEN 610 620 REM DATA ACO. START HERE------622 MASSPG=massloc%(0,0):GOSUB 1000:REM move mass program to 1st mass 624 OUT ATOD+2.0+MASSloc%(1.0)*32:REM select 1st mass gain and ch. 0 630 STARTDATE\$=DATE\$:STARTTIME\$=TIME\$:IF STARTDATE\$<>DATE\$ **THEN 630** 632 GOSUB 4000:REM save parameters 640 GOSUB 4600:REM do gas loop loading 642 GOSUB 1110:REM home loop valves 644 SCREEN 2:CLS:REM graphics screen 646 Print:print "Turn manual gas valve for inject" 647 print "Type any key to continue" 648 if inkey\$="" then 648 649 gcpkptr%=80:mspkptr%=200:rem init. for storage need 650 FOR II=0 TO NUMLOOP%-1 :REM do gc loop one at time 654 LOCATE 20,1:PRINT "Waiting for GC loop ";II+1 656 PRINT "Last loop data:" 657 gosub 1600:rem check storage and wait if not enough 658 GCPKPTR%=0:REM reset GC peak count 660 GOSUB 2000:REM wait until gc is ready 662 open flname\$+".cmm" for append as #2 664 print#2,time\$,; 666 close 2 668 LOOPDATE\$=DATE\$:LOOPTIME=TIMER:IF LOOPDATE\$<>DATE\$ THEN 668 670 GOSUB 2400:REM start gc temp ramp 671 GOSUB 1360:REM switch injector valve to inject 673 for ji=0 to 500:next ji:rem delay for valve to switch 674 if II=0 then 676:rem if 1st loop skip next step 675 GOSUB 1150:REM step to next loop 676 GOSUB 2900:REM renew screen

680 GOSUB 3000:REM data acquisition procedure 682 open finame\$+".cmm" for append as #2 684 print#2,time\$,gcstop\$ 686 close 2 690 GOSUB 4200:REM data saving procedure 700 NEXT II:REM do next ac loop 702 SCREEN 0:REM text screen again 710 FINISHDATE\$=DATE\$:FINISHTIME\$=TIME\$:IF FINISHDATE\$<>DATE\$ **THEN 710** 720 PRINT "experiment starts at ";STARTDATE\$;" ";STARTTIME\$ finishes at ":FINISHDATE\$:" ":FINISHTIME\$ 730 PRINT " 980 out atod+2,6*32:rem switch UTI gain back to 6 990 END:REM end of main program-----1000 REM output dtoa data-----1010 IF MASSPG<0 THEN MASSPG=0 1020 IF MASSPG>65535! THEN MASSPG=65535! 1030 MVAL=INT(MASSPG/256):LVAL=MASSPG-MVAL*256 1040 OUT DTOA+1, MVAL: OUT DTOA, LVAL 1042 if masspg>32767 then massprog%=32767-65536 else massprog%=masspg **1050 RETURN** 1100 REM 16 loop valves control------1110 REM home loop valves-----1120 OUT LOOPVALVE, LOOPNORM XOR HOME 1122 FOR JI=0 TO 300:NEXT JI 1130 OUT LOOPVALVE.LOOPNORM 1132 FOR JI=0 TO 2000:NEXT JI **1140 RETURN** 1150 REM step loop valve-----1160 OUT LOOPVALVE LOOPNORM XOR STP 1162 FOR JI=0 TO 300:NEXT JI 1170 OUT LOOPVALVE, LOOPNORM **1180 RETURN** 1200 REM position loop valve-----1210 POX=INT(LOOPPOS/10) 1220 POX=POX*16+INT(LOOPPOS-POX*10+.2)

1230 OUT LOOPVALVE.LOOPNORM XOR POX 1240 OUT LOOPVALVE, LOOPNORM XOR (POX OR SELPOS) 1250 OUT LOOPVALVE LOOPNORM XOR POX 1260 OUT LOOPVALVE, LOOPNORM RETURN:REM-----_____ 1270 injector valve control-----1300 REM 1310 REM load injector------**1320 OUT INJECTOR, INJNORM XOR LD** 1330 FOR JI=0 TO 1500:NEXT JI:REM delay **1340 OUT INJECTOR, INJNORM 1350 RETURN** 1360 REM iniect-----**1370 OUT INJECTOR.INJNORM XOR INJECT** 1380 FOR JI=0 TO 1500:NEXT JI:REM delay **1390 OUT INJECTOR, INJNORM 1400 RETURN** 1410 REM _____ 1500 REM wait fid ready-----1502 FOR JI=0 TO 20 1510 IF INP(STATES) AND 1 THEN JI=0:REM test until FID is ready 1512 NEXT JI **1520 RETURN** 1530 REM FID remote start------**1540 OUT INJECTOR, INJNORM XOR FIDSTART** 1550 FOR JI=0 TO 300:NEXT JI:REM delay **1560 OUT INJECTOR, INJNORM 1570 RETURN** 1580 REM------1600 rem check drive B: storage and wait if not enough--1610 mspkneed%=mspkptr%+10:if mspkneed%>200 then mspkneed%=200 1620 IF (GCRECORD%=0) OR (GCRECORD%=II+1) then gcpkneed%=gcpkptr%+5 else gcpkneed%=0 1622 if gcpkneed%>80 then gcpkneed%=80 1630 need1=104*cdbl(mspkneed%)*2 1640 need2=61*cdbl(gcpkneed%)*2 1650 need=need1+need2 1660 if need < fnfreespace(2) then 1690

1670 print "Not enough disk space; put another formated disk in B:" 1680 print "Type 'return' key to continue" 1682 if inkey\$<> chr\$(13) then 1682 1684 if need >= fnfreespace(2) then 1670 1686 mkdir "b:\"+flnamed\$ _____ 1690 return:rem-----2000 REM wait for gc to be ready -----2010 PRINT "CHECKING " GC\$(GCTYPE%) 2020 ON GCTYPE% GOSUB 1500,2100:REM fid or tcd 2030 PRINT "GC IS READY" 2040 RETURN:REM appropriate gc is ready------2100 REM wait until TCD is ready------2110 GOSUB 2200:REM read Omega PSW 2120 IF (OMEPSW AND 128) THEN 2110:REM test Omega stop flag 2130 RETURN: REM TCD is ready ------2200 REM read Omega PSW ------2210 PRINT#1,"*00:RPSW:":REM command Omega to read 2220 INPUT#1,OME\$:IF MID\$(OME\$,2,2)<>"00" THEN PRINT "error":OME\$:STOP 2230 PSW\$=MID\$(OME\$,5,2) 2240 OMEPSW=(INSTR(LEFT\$(PSW\$,1),HEXTABLE\$)-1)*16+INSTR(RIGHT\$(P SW\$,1),HEXTABLE\$)-1 2250 RETURN:REM------2400 REM start GC temp ramp-----2410 PRINT:PRINT "STARTING ";GC\$(GCTYPE%) 2420 ON GCTYPE% GOSUB 1530,2500:REM fid or tcd start 2430 PRINT GC\$(GCTYPE%);" IS STARTED" 2440 PRINT 2450 RETURN:REM------TCD-----2500 REM START 2510 GOSUB 2200:REM read Omega PSW 2520 NEWPSW=PSW OR 128:REM set start bit for Omega 2530 PRINT #1,"00:wpsw/";HEX\$(NEWPSW);":" 2540 INPUT#1,OME\$:REM get reponse 2550 IF MID\$(OME\$,2,2)<>"00" THEN PRINT "error";OME\$:STOP RETURN:REM------2560 2600 REM check if gc is running return with gcstop% -------

2610 ON GCTYPE% GOSUB 2700,2800:REM fid.tcd stop ? 2612 if gcstop%=1 then sense%=sense%+1 else sense%=0 2614 if sense%<9 then acstop%=0 else acstop\$="Stop by GC" 2620 LASPDATE\$=DATE\$:LASPTIME=TIMER:IF LASPDATE\$<>DATE\$ **THEN 2620** 2630 IF LASPDATE\$<>LOOPDATE\$ THEN LASPTIME=LASPTIME+86400! 2640 IF (LASPTIME-LOOPTIME)>DUETIME% THEN GCSTOP%=1:acstop\$="Timer Stop" 2690 RETURN:REM------2700 REM check if fid stop 2710 IF INP(STATES) AND 1 THEN GCSTOP%=0 ELSE GCSTOP%=1 2720 RETURN:REM------2800 REM check if tcd stop 2810 GOSUB 2200:REM read Omega PSW 2820 IF (OMEPSW AND 128) THEN GCSTOP%=0 ELSE GCSTOP%=1 2830 RETURN: REM------2900 REM init screen------2910 CLS:SCRNX%=0 2912 LOCATE 20,1:PRINT "GC loop ";II+1 2920 LOCATE 21.1 2930 PRINT "GC peak found = ";GCPKPTR% 2940 print "MS peak found = ";mspkptr% 2990 RETURN:REM------3000 REM data acquisition procedure-----3002 PASSFLAG=0:OLDCOUNT=0:ELEMENT%=0:GCPKPTR%=0:REM init. counts & ptrs 3003 LASTCOUNT%=0:KNEE%=1:TAIL%=1:GCPKST%=0 3004 INDPTR%=0:GCSTOP%=0:SCRNX%=0:REM init. massbuf% index and stop flag 3006 ERASE MASSINT%, GC%, GCPKST%, gcpara% 3007 gcpara%(6)=mspkstp%:gcpara%(7)=mspkre%:gcpara%(9)=mspkht% 3008 gcpara%(8)=ms4%:gcpara%(20)=100:gcpara%(26)=msdelay% 3009 gcpara%(2)=gctype%:gcpara%(5)=element:gcpara%(12)=gcpkptr% 3010 IF (INP(ATOD+1) AND &H20) =0 THEN 3010:REM WAIT UTIL COUNTER IS READY

```
3012 OUT RDYCLR,0:REM clear counter ready flag
3016 if element%< (mslag%*2) then gcpara%(19)=0 else
gcpara%(19)=nummass%
3020 call readgc
(massint%(0,0),massloc%(0,0),gc%(0,0),gcpkst%(0,0),gcpara%(0))
3060 gccount%=gcpara%(3):ms%=gcpara%(156+(dispmass%-1)*61)
3062 if mspkptr% <> gcpara%(24) then mspkptr%=gcpara%(24):gosub
2920
3070 if gcpkptr% <> gcpara%(12) then gcpkptr%=gcpara%(12):gosub
2920
3075 IF SCRNX%>639 THEN GOSUB 2900:REM clear screen if full
3076 if element%=0 then 3190 :rem no display
3077 print ms%,gcpara%(27);
3080 gcscrny%=199-(gccount%-gcpara%(6))/20
3082 if acscrny% <100 then acscrny%=100
3084 msscrny%=99-ms%/20
3086 if msscrny% < 0 then msscrny%=0
3100 IF SCRNX%=0 THEN LINE
(0,gcscrny%)-(0,gcscrny%):oldgcy%=gcscrny%
3102 if scrnx%=0 then line
(0,msscrny%)-(0,msscrny%):oldmsy%=msscrny%:goto 3180
3104 line (scrnx%-1,oldgcy%)-(scrnx%,gcscrny%):oldgcy%=gcscrny%
3106 line
(scrnx%-1,oldmsy%)-(scrnx%,msscrny%):oldmsy%=msscrny%
3180 SCRNX%=SCRNX%+1:REM prepare for next dot
3190 REM end of gc peak------
3200 REM read masses------
```

```
3410 ELEMENT%=ELEMENT%+1
3412 LOCATE 23,1:PRINT "At point ";ELEMENT%
3420 IF GCSTOP%=0 THEN REFDATE$=DATE$:REFTIME=TIMER
3430 IF GCSTOP%=0 THEN GOSUB 2600:REM check if gc is still
running
3450 NOWTIME=TIMER:IF REFDATE$<>DATE$ THEN
```

NOWTIME=NOWTIME+86400! 3460 IF NOWTIME-REFTIME<240 THEN 3010:REM continue data acq. for 4 min. 3470 RETURN: REM data acq proedure return-----4000 REM Saving parameters routine------4010 PRINT "Saving parameters; please wait" 4020 OPEN FLNAME\$+".par" FOR OUTPUT AS #2 4030 PRINT#2,GC\$(GCTYPE%) 4040 PRINT#2,NUMMASS% 4050 FOR I=0 TO NUMMASS%-1 4060 PRINT#2,MASSnum%(I),MASSloc%(1,I) :rem save massnum and gain 4070 NEXT I 4080 PRINT#2.NUMLOOP% 4090 FOR I=0 TO NUMLOOP%-1 4100 PRINT#2,LOADTIME%(I) 4110 NEXT I 4120 PRINT#2,GCRECORD% 4130 PRINT#2, DUETIME% 4140 CLOSE 2:RETURN:REM ------4200 REM saving data ------4202 LOCATE 1.1 4204 PRINT "Saving data, please wait" 4206 IF (GCRECORD%=0) OR (GCRECORD%=II+1) THEN 4210 ELSE 4290 4210 OPEN FLNAME\$+".a"+MID\$(STR\$(II),2) FOR OUTPUT AS #2 4212 gcpkptr%=gcpara%(12):print#2,gcpkptr% 4220 for i=0 to gcpkptr%-1 4230 print#2,gcpkst%(0,i),gcpkst%(1,i):rem save peak elem & count 4240 next i 4250 CLOSE 2 4252 if gcpkptr%=0 then 4290 4260 DEF SEG=VARSEG(GC%(0,0)):REM get seg for BASVE 4270 LENGTH=VARPTR(GC%(60,GCPKPTR%-1))+2:REM get length for BASVE 4280 BSAVE FLNAME\$+".g"+MID\$(STR\$(II),2),0,LENGTH 4290 if mspkptr%=0 then 4590 4310 OPEN FLNAME\$+".b"+MID\$(STR\$(II),2) FOR OUTPUT AS #2

```
4320 print#2,mspkptr%:rem save # of mass peaks
4330 CLOSE 2
4340 DEF SEG=VARSEG(MASSINT%(0,0))
4350 LENGTH=VARPTR(MASSINT%(103,mspkptr%-1))+2
4360 BSAVE FLNAME$+".m"+MID$(STR$(II),2),0,LENGTH
4590 RETURN:REM=======
4600 REM GC gas loading
4602 PRINT: PRINT "LOADING LOOP VALVES"
4610 GOSUB 1100:REM home loop valves
4620 GOSUB 1310:REM put injector valve to load
4622 if numloop%=1 then 4700:rem 1st loop only
4630 FOR I=1 TO NUMLOOP%-1:REM do every loop
4632 GOSUB 1150:REM step loop valve to next loop
4633 if i <> 2 then 4636 else beep:print "Type any key to continue
LOOP 3"
4634 if inkey$="" then 4634
4636 PRINT "LOADING LOOP";I+1;" FOR";LOADTIME%(I);" SEC."
4640 REFDATE$=DATE$:REFTIME=TIMER:IF REFDATE$<>DATE$ THEN
4640:REM get ref time
4650 IF REFDATE$<>DATE$ THEN DAY=1 ELSE DAY=0
4660 PASSTIME=TIMER+DAY*86400!:REM account for day boundary
4670 IF (PASSTIME-REFTIME)<LOADTIME%(I) THEN 4650:REM wait for
full load time
4690 NEXT I:REM fill all gas loops
4700 print "LOADING LOOP 1 FOR";LOADTIME%(0);" SEC."
4702 gosub 1100:rem home loop valve
4710 REFDATE$=DATE$:REFTIME=TIMER:IF REFDATE$<>DATE$ THEN
4710
4720 IF REFDATE$<>DATE$ THEN DAY=1 ELSE DAY=0
4730 PASSTIME=TIMER+DAY*86400
4740 IF (PASSTIME-REFTIME)<LOADTIME%(0) THEN 4720
4800
PRINT:RETURN:REM------
----
5000 REM get MS parameters -----
5010 INPUT "Enter number of masses interested ";NUMMASS%
5012 PRINT
```

```
5014 if nummass%=0 then 5300
5020 PRINT "Locate mass :"
5030 PRINT "
                to the prompt of 'LOCATE' use keypad key"
                 '8' for fine up"
5040 PRINT "
                  '2' for fine down"
5050 PRINT "
                 '6' for coarse up"
5060 PRINT "
                  '4' for coarse down"
5070 PRINT "
5080 PRINT "
                to move mass around "
                  'K'
                        to use key entry
5082 PRINT "
5084 print "
                 'G'
                       to select gain"
                and 'ENTER' to select location":PRINT
5090 PRINT "
5100 MASSPG=0:GOSUB 1000:REM preset to mass 0
5110 FOR I=0 TO NUMMASS%-1
5120 PRINT I+1;" ";
5130 INPUT "enter mass number ":MASSNUM%(I)
5132 if massnum%(i)=4 then ms4\%=i+1
5140 PRINT "LOCATE
5150 TEMP$=INKEY$:IF TEMP$="" THEN 5150
5160 IF ASC(TEMP$)=13 THEN 5250:REM select location of mass
5162 if temp$="K" then 5242
5164 if temp$="G" then gosub 5500:rem change gain%
5170 IF LEN(TEMP$)<>2 THEN 5150
5180 TEMP=ASC(RIGHT$(TEMP$,1))
5190 IF TEMP=72 THEN MASSPG=MASSPG+1
5200 IF TEMP=80 THEN MASSPG=MASSPG-1
5210 IF TEMP=77 THEN MASSPG=MASSPG+100
5220 IF TEMP=75 THEN MASSPG=MASSPG-100
5230 GOSUB 1000:REM program D to A
5240 GOTO 5150
5242 input "Enter D to A setting ";MASSPG
5244 goto 5230
5250 PRINT "at D to A setting of ";MASSPG
5260 MASSLOC%(0,I)=MASSProG%
5270 MASSloc%(1,I)=gain%
5272 print "gain control for mass";massnum%(i);" is";gain%
5280 PRINT
5290 NEXT I
5291 if ms4%=0 then beep:print "Mass 4 not selected" else
```

ms4%=ms4%-1 5292 print "Display which mass (1 to";nummass%;") "; 5294 input dispmass% 5296 input "MS delay after GC (sec.) ";mslag% 5300 RETURN:REM------5400 REM get loop valve load data -----5410 PRINT "GETTING LOOP VALVE LOAD DATA" 5412 print "LOOP 1 WILL BE YOUR 1ST LOOP WITH STEADY LOADING" 5414 PRINT "Load-Time for loop 1 is the min. load-time for it" 5420 INPUT "Enter number of loops (1 to 16)"; NUMLOOP% 5430 IF (NUMLOOP%<1) OR (NUMLOOP%>16) THEN 5420 5440 FOR I=0 TO NUMLOOP%-1 5450 PRINT "enter load-time (in sec.) for loop":1+1; 5460 INPUT LOADTIME%(I) 5470 NEXT I 5480 RETURN: REM ------------5500 rem change gain%------5510 input "enter mass gain (0 to 7) ";gain% 5520 if $(gain \ll 0)$ or $(gain \gg 7)$ then 5510:rem out of range 5550 out atod+2,gain%*32:rem switch gain 5560 return:rem-----9000 error handle routine----rem 9010 open "tberr1.txt" for output as 10 9020 print#10,erl,err 9030 close 10 9032 print "ERR";err;"AT line";erl 9040 end:rem-----**10000 SUB READGC INLINE** 10010 \$inline "gcms.bin"

10020 end sub

READTS.TXT

100 REM loading data from TSNEWGC program ver 3.10 4-27-90 by Henry Chan 110 on error acto 9000 120 base2=&he6a0:plotter=base2+12 130 out plotter+3,&h80 140 xplot%=0:yplot%=0:gosub 6400:rem zero plotter 200 DIM GCELEM%(80) 210 DIM MASSPEAK%(7),GCPEAK%(80),pkbg%(200),pkend%(200),pkbase%(200) 220 DIM MASSNUM%(7), MASSGAIN%(7), LOADTIME%(15) 230 dim gcret%(100),msdel%(100) 232 cls:print "Loading reference data" 240 open "readts1.par" for input as 1 250 for i=0 to 93 260 input#1,gcret%(i),msdel%(i) 270 next i 280 close 1 310 PRINT "Place data disk in drive B:, type any key to continue" 312 IF INKEY\$="" THEN 312 314 chdir "b:\" 316 files "b:*." 320 INPUT "Enter file name ";FLNAME\$ 322 chdir "b:"+flname\$ 330 OPEN "b:"+FLNAME\$+".cmm" FOR INPUT AS #2 340 WHILE NOT EOF(2) 350 LINE INPUT#2, COMMENT\$ 360 PRINT COMMENT\$ **370 WEND** 380 CLOSE 2 390 INPUT "Is this the right one (y/n) ";YES\$ 400 IF YES\$="y" THEN 430 410 IF YES\$="n" THEN 310 420 GOTO 390 **430 PRINT** 500 REM Loading parameters-----

510 PRINT "Loading parameters, please wait" 520 OPEN "b:"+FLNAME\$+".par" FOR INPUT AS #2 530 INPUT#2.GC\$:PRINT "GC type was ";GC\$ 540 INPUT#2,NUMMASS%:PRINT "Number of masses observed =":NUMMASS% 550 FOR I=0 TO NUMMASS%-1 560 INPUT#2, MASSNUM%(I), MASSGAIN%(I) 570 PRINT "MASS";I+1;"is";MASSNUM%(I),"Gain factor";MASSGAIN%(I) 580 NEXT I 590 INPUT#2, NUMLOOP%: PRINT "Number of GC loop is "NUMLOOP% 600 FOR I=0 TO NUMLOOP%-1 610 INPUT#2,LOADTIME%(I) 620 PRINT "Loop";I+1;" load time is ";LOADTIME%(I);" sec." 630 NEXT I 640 INPUT#2,GCRECORD%:PRINT "GC recording loop is (0 for all)";GCRECORD% 650 INPUT#2, DUETIME%: PRINT "Max. time for GC loop is"; DUETIME%;" sec." 660 CLOSE 2:REM parametes loaded-----700 REM display parameters-----710 CLS 720 GOSUB 1700:REM display parameters------1000 REM read data-----1010 PRINT: 1020 INPUT "Enter which GC loop (0 to exit) ";II 1022 if ii=0 then 9900:rem exit program 1030 IF (II<1) OR (II>NUMLOOP%) THEN PRINT "Out of range":GOTO 1020 1050 IF (GCRECORD%=0) OR (GCRECORD%=II) THEN 1060 ELSE GOTO 1200 1060 REM load gc data-----1070 OPEN "b:"+FLNAME\$+".a"+MID\$(STR\$(II-1),2) FOR INPUT AS#2 1080 INPUT#2,GCPKPTR%:PRINT "number of GC peak located is":GCPKPTR% 1082 if gcpkptr%=0 then close 2:dim gc%(60,gcpkptr%+1):goto 1200

```
1090 FOR I=0 TO gcpkptr%-1
1100 INPUT#2.GCELEM%(I).GCPEAK%(I)
1110 NEXT |
1112 CLOSE 2
1150 PRINT "Loading GC data, please wait"
1152 gcname$="b:"+flname$+".g"+mid$(str$(ii-1),2)
1158 dim gc%(60,gcpkptr%+1)
1160 DEF SEG=VARSEG(GC%(0,0))
1170 BLOAD gcname$
1180 PRINT "Done loading GC data"
1200 REM read MS data-----
1202 if nummass%=0 then dim massint%(103,mspkptr%+1):goto
1400
1210 OPEN "b:"+FLNAME$+".b"+MID$(STR$(II-1),2) FOR INPUT AS #2
1230 INPUT#2,mspkptr%: rem get # of mass peak%
1260 CLOSE 2
1262 PRINT
1264 dim massint%(103,mspkptr%+1)
1270 DEF SEG=VARSEG(MASSINT%(0,0))
1280 PRINT "Loading MS data, please wait"
1290 BLOAD "b:"+FLNAME$+".m"+MID$(STR$(II-1),2)
1300 PRINT "Done loading MS data"
1400
        REM
               Data
                       view-----
1402 CLS:GOSUB 1700:GOSUB 1900:REM print peaks data
1410 PRINT "To view 1. GC peak, 2. MS peak, 3. another loop, 4. Auto
align"
1420 INPUT "Enter choice by number ";CHOICE
1430 ON CHOICE GOTO 1450,1460,1470,1462
1440 GOTO 1410:REM no choice
1450 GOSUB 2000:GOTO 1400 :REM view GC peak
1460 GOSUB 3000:GOTO 1400 :REM view MS peak
1462 gosub 7000:goto 1400 :rem auto align GC & MS data
1470 erase gc%:erase massint%:goto 700:rem clear gc% array and
repeat
1480 gosub 4000:goto 1400:rem auto-integrate GC peaks
1700 REM print parameters
1720 PRINT "GC type used was ";GC$
1730 PRINT "Number of masses observed ="NUMMASS%
```

```
1740 FOR I=0 TO NUMMASS%-1
1750 PRINT "mass";MASSNUM%(I)" gain";MASSGAIN%(I),;
1760 NEXT I
1770 PRINT
1780 PRINT "Number of GC loop is";NUMLOOP%
1790 PRINT "Load time in sec. for each loop"
1800 FOR I=0 TO NUMLOOP%-1
1810 PRINT I+1;" is";LOADTIME%(I),;
1820 NEXT I
1830 PRINT
1840 PRINT "GC recording loop (0 for all) is";GCRECORD%
1850 PRINT "Max. time for each GC loop is";DUETIME%;"sec."
        RETURN:REM------
1860
1900 REM print GC & MS data------
1910 PRINT "LOOP #";ii;" GC peaks located =";GCPKPTR%
1912 print "GC peak#, at element ,intensity"
1920 FOR I=0 TO GCPKPTR%-1
1930 PRINT I+1;GCELEM%(I)/2;GCPEAK%(I);
1932 tabcount=(i+1)-int((i+1)/4+.1)*4:print tab(tabcount*20);
1940 NEXT I
1950 print:PRINT "Total mass peak ";mspkptr%
1990 RETURN:REM ------
2000 REM view GC peak
2002 GCMAX=0:if gcpkptr%=0 then print "no GC peak":return
2003 FOR I=0 TO GCPKPTR%-1
2004 IF GCPEAK%(I) > GCMAX THEN GCMAX=GCPEAK%(I)
2005 next i:print:gosub 1900
2006 INPUT "Which gc peak (e to exit,p to plot,a to
autointegrate)";GCPOINT$
2007 gcpoint=val(gcpoint$):if gcpoint$="e" then return
2008 if gcpoint$="a" then gosub 4000:goto 2000
2009 if gcpoint$="p" then gosub 6000:goto 2000
2010 if ((gcpoint=0) or (gcpoint>gcpkptr%)) then 2000
2011 SCREEN 2:YSCALE=GCMAX/180:gosub 4500
2012 nhead=head:ntail=tail
2013 cls:line (30,0)-(30,10):rem tack peak
2014 SCRNY=199-(GC%(0,GCPOINT-1)-baseline+10)/YSCALE
2016 IF SCRNY < 0 THEN SCRNY=0
```

```
2020 LINE (0.SCRNY)-(0,SCRNY):rem 1st point
2021 locate 1,40:print "Loop #";ii
2022 locate 2,40:print "GC peak";gcpoint;"
at";gcelem%(gcpoint-1)/2;"sec."
2024 locate 3,40:print gcpeak%(gcpoint-1)
2030 FOR I=1 TO 60
2032 SCRNY=199-(GC%(I,GCPOINT-1)-baseline+10)/YSCALE
2034 IF SCRNY < 0 THEN SCRNY=0
2040 LINE -(I.SCRNY)
2050 NEXT I
2200 y1=199-(baseline-baseline+10)/yscale
2216 line (0,y1)-(60,y1)
2222 y1=199-(gc%(head,gcpoint-1)-baseline+10)/yscale
2224 y2=199-(gc%(tail,gcpoint-1)-baseline+10)/yscale
2226 line (head, y1)-(head, y1-5)
2228 line (tail, y2)-(tail, y2-5)
2230 ky$=inkey$:if ky$="" then 2230
2240 if asc(ky$)=13 then 2500:rem CR
2250 if asc(ky$)=27 then 2950:rem ESC
2251 if ky$="R" then goto 2013
2252 if ky$="E" then yscale=yscale/2:goto 2013
2253 if ky$="S" then yscale=yscale*2:goto 2013
2254 if ky$="<" then baseline=baseline-1:goto 2013
2255 if ky$=">" then baseline=baseline+1:goto 2013
2258 if ky$="^" then gosub 2700:goto 2230:rem display array
2260 if len(ky$)<2 then 2230
2262 locate 5.40
2264 print "
2270 temp=asc(right$(ky$,1))
2280 if temp=72 then if head<59 then nhead=head+1:gosub 2800
2290 if temp=80 then if head>0 then nhead=head-1:gosub 2800
2300 if temp=77 then if tail<59 then ntail=tail+1:gosub 2850
2310 if temp=75 then if tail>0 then ntail=tail-1:gosub 2850
2340 head=nhead:tail=ntail:goto 2230
2500 rem integrate----
2510 sum=0:if head=tail then 2600
2530 for ji=head to tail
2550 sum=sum+gc%(ji,gcpoint-1)-baseline
```

159

14

i.

en. Sta

```
2560 next ji
2600 locate 5,40
2610 print "INTEGRAL =";sum;"
2620 goto 2200
2700 rem display array------
2710 for i=0 to 60
2715 if i=30 then print "*";
2720 print gc%(i,gcpoint-1);
2730 next i
2740 print
2750 return:rem------
2800 rem tack header------
2805 if nhead>ntail then nhead=ntail
2810 line(head,y1-1)-(head,y1-5),0:rem erase old tack
2815 y1=199-(gc%(nhead,gcpoint-1)-baseline+10)/yscale:rem
calculate new y1
2820 line(nhead,y1)-(nhead,y1-5):rem tack new leader
        return:rem------
2830
2850 rem tack tail
2855 if ntail<nhead then ntail=nhead
2860 line(tail,y2-1)-(tail,y2-5),0:rem erase old tack
2865 y2=199-(gc%(ntail,gcpoint-1)-baseline+10)/yscale:rem
calculate new y2
2870 line(ntail,y2)-(ntail,y2-5):rem tack new tail
2880
        return:rem-----
2950 LOCATE 22.1
2960 PRINT "Type any key to exit"
2970 IF INKEY$="" THEN 2970
2980 SCREEN 0
2990 goto 2000:rem -----
3000 rem view MS data------
3002 if mspkptr%=0 then print "no mass peak":return
3006 print "View mass peaks"
3010 for i=0 to nummass%-1
3020 print "Mass";massnum%(i);" gain";massgain%(i),;
3030 next i
3040 print
3070 input "Which Mass (e to exit)";mass$
```

```
3072 mass=val(mass$):if mass$="e" then return
3080 mspoint=0
3090 for i=0 to nummass%-1
3100 if mass=massnum%(i) then mspoint=i+1
3110 next i
3120 if mspoint=0 then print "Mass not found":goto 3070
3122 mpmax%=0:mspk%=0:for i=0 to mspkptr%-1
3123 if massint%(0,i) <>(mspoint-1) then 3127
3124 if massint%(2,i) > mpmax% then mpmax%=massint%(2,i)
3126 mspk%=mspk%+1:print mspk%;massint%(1,i)/2;massint%(2,i),;
3127 next i:print
3128 print mspk%;"peaks for mass";massnum%(mspoint-1)
3129 input "Which one (e to exit,p to plot, a to autointegrate)";mk$
3130 if mk$="e" then 3000
3131 if mk$="a" then gosub 5000:goto 3120:rem autointegrate
3132 if mk$="p" then gosub 6500:goto 3120:rem plot
3133 mk%=val(mk$):if mk%>mspk% then print "out of range":goto
3129
3134 dim vmloc%(mspk%):mspk%=0:for i=0 to mspkptr%-1
3135 if massint%(0,i)<>(mspoint-1) then 3137
3136 vmloc%(mspk%)=massint%(1,i):mspk%=mspk%+1:if mspk%=mk%
then vmspk%=i
3137 next i
3138 yscale=mpmax%/180:gosub 4700:erase vmloc%:rem find
baseline
3139 scrny1=199-(massint%(3,vmspk%)-baseline+10)/yscale
3142 scrny2=199-(massint%(54,vmspk%)-baseline+10)/vscale
3145 nhead=head:ntail=tail
3150 screen 2:cls
3152 line (25,0)-(25,10):rem tack peak
3160 line (0,scrny1)-(0,scrny1):rem point 1st pt.
3162 locate 1,40:print "Loop #";ii
3170 locate 2,40:print "Mass";mass;" peaks
at";massint%(1,vmspk%)/2;"sec."
3190 locate 3,40:print massint%(2,vmspk%)
3200 for i=4 to 53
3202 oscrny1=scrny1
3210 scrny1=199-(massint%(i,vmspk%)-baseline+10)/yscale
```

```
3220 if scrny1 < 0 then scrny1=0
3230 line (i-4,oscrny1)-(i-3,scrny1)
3232 oscrny2=scrny2
3233 scrny2=199-(massint%(i+50,vmspk%)-baseline+10)/yscale
3234 if scrny2 < 0 then scrny2=0
3235 line (i+100,oscrny2)-(i+101,scrny2)
3240 next i
3300 y1=199-(baseline-baseline+10)/yscale
3320 LINE (0,Y1)-(50,Y1):REM draw base line
3330 Y1=199-(massint%(HEAD,vmspk%)-baseline+10)/YSCALE
3340 Y2=199-(massint%(TAIL,vmspk%)-baseline+10)/YSCALE
3350 LINE (HEAD-3,Y1)-(HEAD-3,Y1-5)
3360 LINE (TAIL-3,Y2)-(TAIL-3,Y2-5)
3370 KY$=INKEY$:IF KY$="" THEN 3370
3380 IF ASC(KY$)=13 THEN 3520:REM CR
3390 IF ASC(KY$)=27 THEN 3820:REM ESC
3400 IF KY$="R" THEN GOTO 3150
3410 if ky$="E" then yscale=yscale/2:goto 3150
3412 if ky$="S" then yscale=yscale*2:goto 3150
3413 if ky$="<" then baseline=baseline-1:goto 3150
3414 if ky$=">" then baseline=baseline+1:goto 3150
3420 IF KY$="^" THEN GOSUB 3630:GOTO 3370:REM display array
3430 IF LEN(KY$)<2 THEN 3370
3440 LOCATE 5.40
3450 PRINT "
3460 TEMP=ASC(RIGHT$(KY$,1))
3470 IF TEMP=72 THEN IF HEAD<53 THEN NHEAD=HEAD+1:GOSUB 3700
3480 IF TEMP=80 THEN IF HEAD>3 THEN NHEAD=HEAD-1:GOSUB 3700
3490 IF TEMP=77 THEN IF TAIL<53 THEN NTAIL=TAIL+1:GOSUB 3760
3500 IF TEMP=75 THEN IF TAIL>3 THEN NTAIL=TAIL-1:GOSUB 3760
3510 HEAD=NHEAD:TAIL=NTAIL:GOTO 3370
3520 REM integrate----
3530 SUM=0:sum4=0:IF HEAD=TAIL THEN 3600
3560 FOR JI=HEAD TO TAIL
3580 SUM=SUM+massint%(JI,vmspk%)-BASELINE
3582 sum4=sum4+massint%(ji+50,vmspk%)
3590 NEXT JI
3600 LOCATE 5.40
```

3610 PRINT "INTEGRAL =":SUM:" 3612 locate 6,40 :print "Average mass 4 intensity" :sum4/(tail-head+1) 3620 GOTO 3300 3630 REM display array------3640 FOR I=0 TO 103 3650 IF I=28 THEN PRINT "*"; 3652 if i=base1 then print "<"; 3654 if i=base2 then print ">"; 3660 PRINT massint%(I,vmspk%),; 3670 NEXT I 3680 PRINT RETURN:REM------3690 3700 REM tack header-----3710 IF NHEAD>NTAIL THEN NHEAD=NTAIL 3720 LINE(HEAD-3, Y1-1)-(HEAD-3, Y1-5), 0: REM erase old tack 3730 Y1=199-(massint%(NHEAD,vmspk%)-baseline+10)/YSCALE:REM calculate new v1 3740 LINE(NHEAD-3,Y1)-(NHEAD-3,Y1-5):REM tack new leader 3750 RETURN:REM------3760 REM tack tail 3770 IF NTAIL<NHEAD THEN NTAIL=NHEAD 3780 LINE(TAIL-3, Y2-1)-(TAIL-3, Y2-5), 0: REM erase old tack 3790 Y2=199-(massint%(NTAIL,vmspk%)-baseline+10)/YSCALE:REM calculate new v2 3800 LINE(NTAIL-3,Y2)-(NTAIL-3,Y2-5):REM tack new tail RETURN:REM-----3810 3820 LOCATE 22.1 3830 PRINT "Type any key to exit" 3840 IF INKEY\$="" THEN 3840 3850 SCREEN 0 3860 goto 3120:REM ------4000 rem auto-integrate 4002 print "GC auto-integrate loop #";ii 4010 dim area(gcpkptr%):rem clear array 4020 gosub 4200:rem auto routine 4030 print 4040 input "Do you want to save integrals (y/n)"; yes\$

```
4050 if yes$="y" then gosub 4300:goto 4080
4060 if yes$="n" then 4080
4070 goto 4040
4080 input "Do you want to print integrals (y/n)"; yes$
4090 if yes$="y" then gosub 4400:goto 4120
4100 if yes$="n" then 4120
4110 goto 4080
4120
                area:return:rem-----
       erase
4200 for gcpk%=0 to gcpkptr%-1:rem do it for every GC peak
4210 gcpoint=gcpk%+1:gosub 4500:rem look baseline & define peak
4220 sum=0:sum4=0: if head=tail then 4290
4230 pkbase%(gcpk%)=baseline
4240 for ji=head to tail
4250 sum=sum+gc%(ji,gcpk%)-baseline
4260 next ji
4270 area(gcpk%)=fix(sum)
4280 print gcpk%+1;" ";area(gcpk%),;
4290 next gcpk%
4299
         return:rem-----
4300 rem saving integrals
4302 sname$=left$(flname$,4)+"gc"+mid$(str$(ii),2)+".prn"
4310 open "b:"+sname$ for output as # 2
4312 print#2,"peak","at (sec.)","height","area","baseline"
4330 for acpk%=0 to acpkptr%-1
4340 print#2, gcpk%+1,gcelem%(gcpk%)/2,gcpeak%(gcpk%),;
4342 print#2, area(gcpk%),pkbase%(gcpk%)
4350 next gcpk%
4360 print#2.
4370 close 2
4390
        return:rem-----
4400
             print integral-----
       rem
4410 lprint flname$;"GC peaks for Loop #";ii
4420 Iprint
4428 lprint "peak","at (sec.)","height","area","baseline"
4430 NL%=0:for gcpk%=0 to gcpkptr%-1
4440 lprint
gcpk%+1,gcelem%(gcpk%)/2,gcpeak%(gcpk%),area(gcpk%),pkbase%(gc
pk%)
```

```
4450 NL%=NL%+1:IF NL%=5 THEN NL%=0:LPRINT
4480 next gcpk%
4482 lprint:lprint
4490
         return:rem-----
4500 rem find base1 & base2
4501 gp=gcpoint
4502 if gp=1 then head=0 else
head=30-(gcelem%(gp-1)-gcelem%(gp-2))
4504 if gp=gcpkptr% then tail=60 else
tail=(acelem%(ap)-acelem%(ap-1))+30
4506 if head < 0 then head=0
4508 if tail >60 then tail=60
4582 a%=4:dim a(a%):for i=0 to 4:a(i)=4096:next i
4583 for i=5 to 60:if gc\%(i,gcpoint-1) > a(0) then 4588
4584 a(0) = gc\%(i,gcpoint-1)
4585 for i1=0 to 3
4586 if a(i1) < a(i1+1) then a1=a(i1):a(i1)=a(i1+1):a(i1+1)=a1
4587 next i1
4588 next i
4589 sum=0:for i=0 to 4:sum=sum+a(i):next i:baseline=sum/5:erase a
4590 basemin%=gc%(head,gcpoint-1):nhead=head
4600 for i=head to 30
4610 if gc\%(i,gcpoint-1) < basemin\% then
nhead=i:basemin%=gc%(i,gcpoint-1)
4620 next i
4630 basemin%=gc%(31,gcpoint-1):ntail=31
4640 for i=31 to tail
4650 if gc%(i,gcpoint-1) <= basemin% then
ntail=i:basemin%=gc%(i,gcpoint-1)
4660 next i
4670 head=nhead:tail=ntail
4680 if head < 15 then head=15
4682 if tail > 52 then tail=52
4690
        return:rem-----
4700 rem find ms baseline
4710 if mk%=1 then head=0 else
head=27-(vmloc%(mk%-1)-vmloc%(mk%-2))
4720 if mk%=mspk% then tail=53 else
```

```
tail=(vmloc%(mk%)-vmloc%(mk%-1))+27
4730 if head < 2 then head=2
4732 if tail > 53 then tail=53
4740 a%=4:dim a(a%):for i=0 to 4:a(i)=4096:next i
4745 for i=2 to 53:if massint%(i,vmspk%) > a(0) then 4770
4750 a(0)=massint%(i,vmspk%)
4755 for i1=0 to 3
4760 if a(i1) < a(i1+1) then a1=a(i1):a(i1)=a(i1+1):a(i1+1)=a1
4765 next i1
4770 next i
4775 sum=0:for i=0 to 4:sum=sum+a(i):next i:baseline=sum/5:erase a
4780 basemin%=massint%(head,vmspk%):nhead=head
4785 for i=head to 27
4790 if massint%(i,vmspk%)< basemin% then
nhead=i:basemin%=massint%(i,vmspk%)
4795 next i
4800 basemin%=massint%(28,vmspk%):ntail=28
4805 for i=28 to tail
4810 if massint%(i,vmspk%)<= basemin% then
ntail=i:basemin%=massint%(i,vmspk%)
4815 next i
4820 head=nhead:tail=ntail
4830 if head < 12 then head=12
4840 if tail > 50 then tail=50
4850
         return:rem-----
5000 REM auto-integrate ms
5010 PRINT "MS auto-integrate loop #":II:" for
mass":massnum%(mspoint-1)
5020 DIM
AREA1(msPKPTR%),height%(mspkptr%),area4(mspkptr%),mselem%(m
spkptr%)
5022 dim vmloc%(mspk%),msbase%(mspkptr%)
5024 gosub 5200
5026 print
5030 if pkcount%=0 then print "no peak":goto 5120
5040 INPUT "Do you want to save integrals (y/n)"; YES$
5050 IF YES$="y" THEN GOSUB 5510:GOTO 5080
5060 IF YES$="n" THEN 5080
```

```
5070 GOTO 5040
5080 INPUT "Do you want to print integrals (y/n)"; YES$
5090 IF YES$="y" THEN GOSUB 5610:GOTO 5120
5100 IF YES$="n" THEN 5120
5110 GOTO 5080
5120 ERASE
AREA1, height%, area4, mselem%, vmloc%, msbase%: RETURN: REM------
. . . . .
5200 rem ms auto-integrate
5210 mspk%=0:for i=0 to mspkptr%-1
5220 if massint%(0,i) <> (mspoint-1) then 5240
5230 vmloc%(mspk%)=massint%(1,i):mspk%=mspk%+1
5240 next i
5250 mk%=1:pkcount%=0
5260 FOR msPKi%=0 TO msPKPTR%-1:REM do it for every peak of this
mass
5270 if massint%(0,mspki%) <> (mspoint-1) then 5430
5280 mselem%(pkcount%)=massint%(1,mspki%)
5290 height%(pkcount%)=massint%(2,mspki%)
5300 vmspk%=mspki%
5310 gosub 4700
5320 mk%=mk%+1
5330 sum=0:sum4=0:area1(pkcount%)=0:area4(pkcount%)=0
5340 for i=head to tail
5350
AREA1(pkcount%)=AREA1(pkcount%)+(massint%(I,msPKi%)-baseline)
5360 area4(pkcount%)=area4(pkcount%)+(massint%(I+50,mspki%))
5370 NEXT I
5380 area4(pkcount%)=area4(pkcount%)/(tail-head+1)
5390 msBASE%(pkcount%)=baseline
5400 AREA1(pkcount%)=FIX(AREA1(pkcount%))
5410 PRINT pkcount%+1;" ";int
(AREA1(pkcount%)),int(area4(pkcount%))
5420 pkcount%=pkcount%+1
5430 NEXT msPKi%
5440
        return:rem-----
5510 REM saving integrals
```

```
5512
```

5. 1

```
sname$=left$(fIname$,4)+mid$(str$(massnum%(mspoint-1)+100),3)
5514 sname$=sname$+mid$(str$(ii),2)+".prn"
5520 OPEN "b:"+sname$ FOR OUTPUT AS # 2
5540 FOR msPKi%=0 TO pkcount%-1
5550 PRINT#2, msPKi%+1,mselem%(mspki%)/2,height%(mspki%),;
5560 print#2,
int(AREA1(msPKi%)),msbase%(mspki%),int(area4(mspki%))
5570 NEXT msPKi%
5580 PRINT#2.
5590 CLOSE 2
        RETURN:REM-----
5600
5610
       REM
              print integral-----
5620 LPRINT FLNAMES:"
                        Loop #";II ;"autointegrate
mass";massnum%(mspoint-1)
5630 LPRINT
5640 LPRINT "peak": TAB(12):"at (sec.)":TAB(24):"height":
5642 LPRINT TAB(36);"area";TAB(48);"baseline"TAB(58);"mass 4
avg.";
5643 lprint tab(70);"pk. ht."
5650 NL%=0:FOR msPK%=0 TO pkcount%-1
5660 LPRINT
msPK%+1;TAB(12);msELEM%(msPK%)/2;TAB(24);height%(mspk%);
5670 LPRINT
TAB(36);int(AREA1(msPK%));TAB(48);msBASE%(msPK%);
5671 lprint TAB(58);int(area4(mspk%));
5672 lprint tab(70);height%(mspk%)-msbase%(mspk%)
5674 NL%=NL%+1:IF NL%=5 THEN NL%=0:LPRINT
5680 NEXT msPK%
5682 lprint:lprint
5690
        RETURN:REM------
                   plot-----
6000
       rem
             GC
6002 print "Plot GC; Pen up ; type any key to continue"
6004 if inkey$="" then 6004
6010 xplot%=0:pbase%=qc%(0,0):yplot%=pbase%:gosub 6400
6012 print "Pen down ;type any key to continue"
6014 if inkey$="" then 6014
6020 for i=0 to gcpkptr%-1 :rem for every gcpeaks
6030 if xplot% >= (gcelem%(i)-30) then 6100
```

```
6040 vplot%=pbase%:gosub 6400
6050 xplot%=xplot%+1
6060 goto 6030
6100 selem%=xplot%-gcelem%(i)+30
6110 if selem% > 60 then 6200
6120 for i1=selem% to 60
6130 yplot%=gc%(i1,i):gosub 6400
6140 xplot%=xplot%+1
6150 next i1
6160 pbase%=gc%(0,i)
6170 for i1=0 to 60
6180 if pbase% > gc%(i1,i) then pbase%=gc%(i1,i)
6190 next i1
6200 next i
6390
         return:rem-----
6400 rem plot-----
6410 if xplot%<0 then xplot%=0
6420 if xplot%>4095 then xplot%=4095
6430 if yplot%<0 then yplot%=0
6440 if yplot%>4095 then yplot%=4095
6450 plot0%=255-yplot% and 255
6460 plot2%=255-xplot% and 255
6470 plot1%=255-(int(xplot%/256)*16+int(yplot%/256))
6480 out plotter+2,plot2%:out plotter+1,plot1%:out plotter,plot0%
6490 return:rem ----
                    plot-----
6500
       rem
              MS
6502 print "Plot MS"massnum%(mspoint-1);" Pen up ; type any key to
continue"
6504 if inkey$="" then 6504
6510 xplot%=0:pbase%=0:yplot%=pbase%:gosub 6400
6512 print "Pen down ;type any key to continue"
6514 if inkey$="" then 6514
6520 for i=0 to mspkptr%-1 :rem for every mspeaks
6522 if massint%(0,i) <> (mspoint-1) then 6700
6524 if xplot%=0 then pbase%=massint%(3,i)
6530 if xplot% >= (massint%(1,i)-28+3) then 6600
6540 yplot%=pbase%:gosub 6400
6550 xplot%=xplot%+1
```

```
6560 goto 6530
6600 selem%=xplot%-massint%(1,i)+28
6610 if selem% > 52 then 6700
6620 for i1=selem% to 52
6630 yplot%=MASSINT%(i1,i):gosub 6400
6640 xplot%=xplot%+1
6650 next i1
6660 pbase%=massint%(3,i)
6670 for i1=3 to 52
6680 if pbase% > massint%(i1,i) then pbase%=massint%(i1,i)
6690 next i1
6700 next i
6990
         return:rem-----
7000 rem auto align GC & MS data
7002 print "Check printer is ready, and there is enough paper"
7004 print "Type any key to continue"
7006 if inkey$="" then 7006
7008 Lprint "Auto align Loop"; ii; of file "; flname$: lprint
7010 dim
area(gcpkptr%), area1(mspkptr%), height%(mspkptr%), area4(mspkptr-
%)
7012 dim
mselem%(mspkptr%),vmloc%(mspkptr%),msbase%(mspkptr%),pkid%(g
cpkptr%)
7014 dim form(gcpkptr%-1,nummass%+1)
7022 print:print:print "Auto align routine"
7024 print "Now doing auto integrating GC"
7030 gosub 4200:rem auto gc integrate
7032 gosub 4400:rem print gc integrals
7040 print "Now aligning GC data with peak ID"
7050 idptr%=0
7060 for igc%=0 to gcpkptr%-1
7070 oskew%=30000
7072 if idptr%=94 then 7094
7080 skew%=abs(gcret%(idptr%)-gcelem%(igc%)/2)
7090 if skew% < oskew% then oskew%=skew%:idptr%=idptr%+1:goto
7072
7094 pkid%(igc%)=idptr%
```

```
7096 form(igc%,0)=idptr%:form(igc%,1)=area(igc%)
7098 rem idptr%=idptr%-1
7110 next jac%
7120 for ims%=0 to nummass%-1
7130 mspoint=ims%+1
7140 print "auto integrating mass";massnum%(ims%)
7150 gosub 5200:rem ms integrate
7152 gosub 5610:rem print ms integrate
7160 if pkcount%=0 then print "no peak for this mass":goto 7700
7170 print "Aligning MS with GC data"
7180 igc%=0:for imspk%=0 to pkcount%-1
7190 oskew%=30000
7192 if igc\% = gcpkptr\% then 7240
7200
skew%=abs((mselem%(imspk%)-gcelem%(igc%))/2-msdel%(pkid%(igc
%)-1))
7210 if skew% < oskew% then oskew%=skew%:igc%=igc%+1:goto
7192
7220 form(igc%-1,ims%+2)=area1(imspk%)/area4(imspk%)
7230 iqc%=iqc%-1
7240 next imspk%
7700 next ims%
7701 lprint chr$(12);"Align Data for Loop";ii;" of file
";flname$:lprint
7702 lprint "pkid";tab(15);"gcarea";
7703 for i=0 to nummass%-1
7704 lprint using "########;massnum%(i);
7705 next i:lprint
7706 for i=0 to gcpkptr%-1
7707 lprint form(i,0);tab(5);gcelem%(i)/2;tab(15);form(i,1);tab(25)
7708 for iform=2 to nummass%+1:lprint using
"###.####";form(i,iform);:next
7709 lprint:next i:lprint chr$(12);
7710 sname$=left$(flname$,4)+"ag"+mid$(str$(ii),2)+".prn"
7720 open "b:"+sname$ for output as #2
7730 print#2,"pkid","gcarea",;
7740 for i=0 to nummass%-1
7750 print#2, using "########; massnum%(i);
```

```
7760 next i
7762 print#2,
7770 for i=0 to gcpkptr%-1
7772 print#2,form(i,0),form(i,1),;
7780 for iform=2 to nummass%+1
7800 print#2, using "###.####"; form (i, iform);
7810 next iform
7820 print#2,
7830 next i
7840 close 2
7990 erase
area,area1,height%,area4,mselem%,vmloc%,msbase%,pkid%,form
         return:rem-----
7992
9000 rem error handling routine-----
9010 if (err=76) and (erl=322) then resume next:rem not a dir
9020 if (err=53) and (erl=314) then resume next:rem no *.par
9030 if (err=53) and (erl=316) then resume next:rem no <DIR>
9040 if (err=53) and (erl=1210) then nummass%=0:goto 1200:rem no
"*.b"files
9090 open "tberr.txt" for output as 10
9100 print#10,erl,err
9110 close 10
9200 end:rem error end
9900 chdir "b:\":rem reset B drive working dir
9910 END:rem end program
```

Appendix II

Solution of the differential equations describing chain growth during Fischer-Tropsch Synthesis

The solutions for the differential equations that describe the chain growth model used in Chapter IV are derived in this Appendix. The starting point is the equations (eqn.1 and 3 in Chapter IV) for the fractional label incorporation in the monomer pool and in each of the C_n pools that are the precursors to the hydrocarbon products of chain length n. F_i is the fractional label content of pool i on the surface; τ_m is the lifetime of the monomer pool and τ is the lifetime of each of the C_n surface pools.

$$\frac{d F_{m}(t)}{dt} = \frac{1 - F_{m}(t)}{\tau_{m}} \qquad(1)$$

$$\frac{d F_{n}(t)}{dt} = \frac{\frac{(n-1)F_{n-1}(t) + F_{m}(t)}{n} - F_{n}(t)}{\tau} \qquad \text{for } n = 1, n \dots (2)$$

Initial and Boundary conditions:

- 1. The F curves for the monomer and all the C_n pools start at 0 at t =0; i. e., $F_m(t=0) = F_i(t=0) = 0$, where i = 1, n.
- 2. At t = ∞ , all F curves have reached steady state and are equal to 1.0

Laplace transforms of the first-order differential equations 1 and 2 are used to obtain solutions for $F_n(t)$. The Laplace transform (L.T.) of $F_i(t)$ will be represented as $f_i(s)$.

Taking the L.T. of equation 1 gives:

$$sf_{m}(s) - F_{m}(0) = \frac{(\frac{1}{s} - f_{m}(s))}{\tau_{m}}$$
 (3)

From the initial condition for F_m , $F_m(0) = 0$; so this can be simplified to give

$$f_{m}(s) = \frac{1}{s \tau_{m} (s + \frac{1}{\tau_{m}})}$$
 (3')

This expression now yields the solution that

$$F_{m}(t) = 1.0 - \exp\left(\frac{-t}{\tau_{m}}\right)$$
 (4)

Taking the L.T. of equation 2, we get:

$$sf_{n}(s) - F_{n}(0) = \frac{(n-1)}{n\tau} f_{n-1}(s) + \frac{1}{n\tau} f_{b}(s) - \frac{f_{n}(s)}{\tau}$$
 (5)

Again, using the initial condition that $F_n(0) = 0$, this yields:

$$f_{n}(s) = \frac{1}{n\tau(s+\frac{1}{\tau})} [f_{b}(s) + (n-1) f_{n-1}(s)] \qquad (5')$$

The L.T. of each pool depends on the L.T. of the previous pool in this set of recurring relationships as well as $f_b(s)$, except for the expression for $f_1(s)$ which only involves $f_b(s)$. From equation 5',

$$f_1(s) = \frac{1}{\tau(s+\frac{1}{\tau})} [f_b(s)]$$
 (6)

Now, this expression for $f_1(s)$ can be used with equation 5' to yield an expression for $f_2(s)$ and so on; ultimately, this results in the following expression for $f_n(s)$:

$$f_{n}(s) = \frac{f_{b}(s)}{n} \left[\frac{1}{\tau(s+\frac{1}{\tau})} + \frac{1}{\tau^{2}(s+\frac{1}{\tau})^{2}} + \dots \frac{1}{\tau^{n}(s+\frac{1}{\tau})^{n}} \right] \dots \dots (7)$$

The inverse transform of this expression will give the solution $F_n(t)$. Since all the terms can be expressed by a general expression for the ith term, the ith term of the above expression is inverted; the summation of this for all terms from i=1 to i=n then yields $F_n(t)$. The ith term in the expansion is:

$$f_{i}(s) = \frac{f_{b}(s)}{n} \left[\frac{1}{\tau^{i}(s+\frac{1}{\tau})^{i}} \right]$$

To get the L-1 or inverse L.T. of this term, use is made of the convolution theorem (1), which states:

If
$$f(s) = g(s)h(s)$$
, and $L^{-1}[g(s)] = G(t)$ and $L^{-1}[h(s)] = H(t)$,

$$F(t) = \int_{0}^{t} G(u)H(t-u)du \qquad(8)$$

(where $F(t) = L^{-1}[f(s)]$)

Also, from L.T. tables, the following inverse transform is obtained:

$$L^{-1}\left[\frac{1}{(s-a)^{i}}\right] = \frac{1}{(i-1)!} t^{i-1} \exp(at)$$
 (9)

Using eqns. 4, 8 and 9,

$$L^{-1}[ith \ term] = \frac{1}{n\tau^{i}(i-1)!} \int_{0}^{t} u^{i-1} exp(\frac{-u}{\tau})(1 - exp(\frac{-(t-u)}{\tau_{m}})) du \qquad (10)$$

The expression can be evaluated using integral tables (2) to give:

From eqn. 11, $F_n(t)$ can be evaluated:

$$F_{n}(t) = \sum_{i=1}^{n} [L^{-1}(ith \ term)]$$

$$F_{n}(t) = 1.0 + \left(\frac{\exp(-\frac{t}{\tau_{m}})}{n}\right) \sum_{i=1}^{n} (-1)^{i-1} \left(\frac{\tau_{m}}{\tau - \tau_{m}}\right)^{i}$$

$$+ \left(\frac{\exp(-\frac{t}{\tau})}{n}\right) \sum_{i=1}^{n} \frac{1}{\tau^{i}} \sum_{r=0}^{i-1} \frac{t^{i-r-1}}{(i-r-1)!} \tau^{r+1} \left((-\frac{\tau_{m}}{\tau - \tau_{m}}\right)^{r+1} - 1) \qquad (12)$$

Equation 12 can now be used to generate expressions for any desired value of the carbon number, n.

REFERENCES

- 1. Jenson, V. G., and Jeffreys, G. V., "Mathematical Methods in Chemical Engineering", Second Edition, Academic Press, 1977.
- 2. "CRC Handbook of Chemistry and Physics", R. C. Weast (ed.), 63rd edition, CRC Press Inc., Boca Raton, Florida, 1982.

Appendix III

Chain-growth model parameter estimation

This Appendix describes the chain growth model fitting program used for parameter estimation from the model presented in Chapter 4. The program is written in FORTRAN and has been run on the Main Frame IBM 3081.

3.1 Program Minimum

This is a program that can provide parameter estimates for a function of several variables, by minimizing the function using a quasi-Newton method. The user must provide a subroutine to calculate the function and its gradient (first partial derivatives with respect to the variables of interest.) This function is the objective function, which consists of the summation of the square of the difference of the experimental data points and the function evaluated at these points using the current estimates of the solution vector. The user initially inputs the number of variables (2) in our case) and an estimate or initial guess of the solution vector for these variables, and the original experimental data points. The program iteratively searches for the parameter values that minimize the provided objective function. Finally, the program output gives the final solution vector, and the function values that correspond to the experimental data points, as well as a termination indicator that indicates whether convergence occurred.

'MINIMUM' is the name of the FORTRAN main program used here; it is a general error minimization routine that can be used for any user-supplied function. The Subroutine 'SUMDATA' provides the chain growth model objective function and its partial derivatives with respect to the two parameters, τ and τ_m . The Subroutine 'FUNC' that is called by subroutine 'SUMDATA' actually evaluates the F_n(t, n, τ , τ_m) that is obtained as a solution for the chain growth model presented in Chapter 4 at input values of these four parameters. If a different solution function needs to be used, it can be modified in this subroutine. The user also inputs as data the F (rise) curves obtained from the transient response isotopic tracer experiments described in Chapter 4. The input requires the carbon number of the F curve, initial guesses of τ and τ_m and finally, t_i , $F^{expt}(t_i)$ pairs. A listing of the program follows.

```
MIN00020
                                                                    MIN00030
        Program Minimum
                                                                    MIN00040
                                                                    MIN00050
        implicit none
                                                                    MIN00060
        INTEGER
                INPUTUNIT, MAXDATA, N
                                                                    MIN00070
                                                                    MINOOOBO
                 nvar, ihess, maxf, irhess, iwhess, iprint
        integer
                                                                    MIN00090
        INTEGER IERR, ISWTCH, ITER, NFCALL, I
                                                                    MIN00100
        parameter (nvar=2, ihess=.5*nvar*(nvar+1))
                 tolx,tolg,sprec,extbnd,rfn,objf,histry,
                                                                    MIN00110
        real*8
                 x(nvar),g(nvar),solvec(nvar),srhvec(nvar),grdvec(nvar)MIN00120
     2
        REAL*8
                 HESS (IHESS), SCRVEC (NVAR), NORM, T (100), FEXP (100)
                                                                   MIN00130
                                                                    MIN00140
        real*8
                 fn,deltau,deltaub
        LOGICAL ALWAYSTRUE
                                                                    MIN00150
c external function calls for psi and phi
                                                                    MIN00160
                                                                    MIN00170
                                                                    MIN00180
        external sumdata
                                                                    MTN00190
c initialize input parameters for the minimization routine
                                                                    MIN00200
                                                                    MIN00210
        data maxf,tolx,tolq,sprec,extbnd,irhess,iwhess,iprint,ierr,
                                                                    MIN00220
     2
            iswtch,rfn/500,1d-6,1d-10,.1,2.,0,0,0,0,2,1d-6/
                                                                    MTN00230
                                                                    MIN00240
        data AlwaysTrue/.true./
                                                                    MIN00250
        data inputunit/20/
                                                                    MIN00260
        DATA OBJF/0.0D0/
                                                                    MIN00270
                                                                    MIN00280
       COMMON /EXPTDATAR/T, FEXP
                                                                    MIN00290
        common /exptdataI/MaxData
                                                                    MIN00300
       COMMON /CARBON/N
                                                                    MIN00310
MIN00330
C
       OPEN (UNIT=INPUTUNIT, FILE='INPUT.DAT', STATUS='UNKNOWN')
                                                                    MIN00340
С
       OPEN (UNIT=INPUTUNIT)
                                                                    MIN00350
c initial guess on parameters
                                                                    MIN00360
                                                                    MIN00370
С
       READ(INPUTUNIT, *) X
                                                                    MIN00380
C
       WRITE(6,*)X
                                                                    MTN00390
       DO 1 I=1,NVAR
                                                                    MIN00400
       READ(20, *)X(I)
                                                                    MIN00410
 1
       CONTINUE
                                                                    MIN00420
c data points used in fitting function
                                                                    MIN00430
                                                                    MIN00440
с
       T=0
                                                                    MIN00450
                                                                    MIN00460
С
       DO WHILE (ALWAYSTRUE)
                                                                    MIN00470
С
          I = I + 1
                                                                    MIN00480
С
          READ (INPUTUNIT, *, END=999, ERR=999) T(I), FEXP(I)
                                                                    MIN00490
C
                                                                    MIN00500
С
       ENDDO
                                                                    MIN00510
С
                                                                    MIN00520
C99
       CLOSE (UNIT=INPUTUNIT)
                                                                    MIN00530
```

PROGRAM MINIMUM

```
MIN00540
С
        MAXDATA = I-1
                                                                        MIN00550
        MAXDATA IS THE # OF DATA POINTS; N IS THE CARBON # OF DATA
С
                                                                        MIN00560
        READ (20, *) N, MAXDATA
                                                                        MIN00570
        DO 2 I=1, MAXDATA
                                                                        MIN00580
        READ(20, *) T(I), FEXP(I)
                                                                        MIN00590
        WRITE(6, *) 'T=', T(I), 'FEXP', FEXP(I)
С
                                                                        MIN00600
 2
        CONTINUE
                                                                        MIN00610
        do i=1, ihess
                                                                        MIN00620
           hess(i)=0.0d0
                                                                        MIN00630
        enddo
                                                                        MIN00640
        call ggbfgs(nvar, x, iswtch, maxf, iter, iprint, tolx, tolg, rfn,
                                                                        MIN00650
     2
             sprec, extbnd, objf, ihess, hess, g, ierr, nfcall, srhvec,
                                                                        MIN00660
             solvec,grdvec,scrvec,histry,irhess,iwhess,sumdata)
     3
                                                                        MIN00670
                                                                        MIN00680
                                                                        MTN00690
        WRITE(22,*)'OBJF: ',OBJF
                                                                        MIN00700
                                                                        MIN00710
        NORM = 0.0D0
                                                                        MIN00720
        do i = l,nvar
                                                                        MIN00730
           norm = norm + q(i) * * 2
                                                                        MIN00740
        enddo
        NORM =DSQRT (NORM)
                                                                        MIN00750
                                                                        MIN00760
                                                                        MIN00770
        WRITE(22,*)'FINAL X: ', SOLVEC
                                                                        MIN00780
        WRITE (22, *) 'GRADIENT: '
        WRITE(22,*)(G(I),I=1,NVAR)
                                                                        MIN00790
                                                                        MIN00800
        WRITE (22, *) 'NORM: ', NORM
        WRITE(22,*) 'CARBON#',N
                                                                        MIN00810
        WRITE(22,*)'ITER: ', ITER
                                                                        MIN00820
                                                                        MIN00830
        WRITE(22,*)'IERR: ', IERR
        WRITE(22,*)'NFCALL: ',NFCALL
                                                                        MIN00840
                                                                        MIN00850
        WRITE(22,*)
                                                                        MIN00860
        WRITE(23,*) '"MODEL',N,'".'
                                                                        MIN00870
                                                                        MIN00880
        do i = 1, MaxData
                                                                        MIN00890
           call FUNC(T(i),FN,DELTAU,DELTAUB,X,MaxData)
                                                                        MIN00900
           WRITE(23,*) T(I),FN
                                                                        MIN00910
        enddo
        WRITE(23,*)
                                                                        MIN00920
        WRITE(23,*) '"EXP',N,'".'
                                                                        MIN00930
        DO I = 1, MAXDATA
                                                                        MIN00940
                                                                        MIN00950
           WRITE(23,*) T(I), FEXP(I)
        ENDDO
                                                                        MIN00960
                                                                        MIN00970
                                                                        MIN00980
        stop
                                                                        MIN00990
        end
                                                                        MIN01000
                                                                        MIN01010
c note: all real variables in this routine are double precision
                                                                        MIN01030
c so make sure that any variable transfered into the routine is
                                                                        MIN01040
c double precision (64 bit)
                                                                        MIN01050
                                                                        MTN01060
      subroutine gqbfgs(nvar,x,iswtch,maxf,iter,iprint,tolx,tolg,
                                                                        MIN01070
     1
                 rfn, sprec, extbnd, objf, ihess, hess, g, ierr, nfcall, srhvec, MIN01080
     2
                 solvec,grdvec,scrvec,histry,irhess,iwhess,funct)
                                                                        MIN01090
```

d.

| _ | | MIN01100 |
|-----|---------------------------------------------------------------------------------------------------------------|----------------------|
| с | i=1 $i=1$ $i=1$ $(1-1)$ $(1-1)$ $(1-1)$ | MIN01110 |
| | <pre>implicit_real*8 (a-h,o-z)</pre> | MIN01120 |
| с | dimension x(nvar),hess(ihess),g(nvar),srhvec(nvar), | MIN01130 |
| | 1 solvec(nvar), grdvec(nvar), scrvec(nvar) | MIN01140 |
| | i Solvec (nvar), gravec (nvar), scrvec (nvar) | MIN01150 |
| с | external funct | MINO1150 |
| - | external funct | MINO1170 |
| c | this subroutine minimizes a function of several variables | MINO1180 |
| c | | MINO1180 MINO1190 |
| c | objf(x(1),x(2),,x(nvar)) using a quasi-newton method optionally employing the dfp and bfgs updating formulas. | MIN01200 |
| с | | MIN01200 MIN01210 |
| с | the user must provide a subroutine to calculate objf(x) and | |
| с | its gradient (first partial derivative) vector g(x). | MIN01220 |
| с | ****** | MIN01230 |
| с | | MIN01240 |
| с | this routine invokes the package modules search and uphess | MIN01250 |
| с | and the user supplied subroutine funct. | MIN01260 |
| с | ************************ | MIN01270 |
| С | | MIN01280 |
| с | on input: | MIN01290 |
| с | | MIN01300 |
| с | nvar is the number of variables. it is also the dimension of | MIN01310 |
| с | the vectors x, g, srhvec, solvec, grdvec and scrvec. | MIN01320 |
| с | | MIN01330 |
| с | x contains an estimate of the solution vector | MIN01340 |
| с | (x(1),x(2),,x(nvar)). | MIN01350 |
| с | | MIN01360 |
| с | iswtch is a parameter set equal to k which selects the | MIN01370 |
| с | formula used to update the approximation to the hessian | MIN01380 |
| с | inverse. for | MIN01390 |
| с | | MIN01400 |
| С | k = 1 - the dfp update, | MIN01410 |
| с | k = 2 - the bfgs update. | MIN01420 |
| c · | | MIN01430 |
| с | the bfgs update is recommended. | MIN01440 |
| с | · | MIN01450 |
| с | maxf is the limit on the number of calls to the function | MIN01460 |
| С | evaluation routine funct. | MIN01470 |
| с | · | MIN01480 |
| с | funct is a user supplied subroutine to evaluate objf(x) | MIN01490 |
| с | and the components of the gradient $g(x)$ at the estimate | MIN01500 |
| с | | OMINO1510 |
| с | routine. | MIN01520 |
| с | o | MIN01530 |
| с | tolx,tolg are the accuracies required in the solution, i.e. a | MIN01540 |
| с | normal return from the routine occurs if the difference | MIN01550 |
| с | between the components of two successive estimates of the | MIN01560 |
| c | solution are not greater than max(tolx*abs(x(i)),tolx) | MIN01570 |
| с | for all i, and the 12 norm of the gradient is not greater | MIN01580 |
| c | than tolg. | MIN01590 |
| c | ······································ | MIN01600 |
| c | rfn is an estimate of the expected reduction in $objf(x)$. | MIN01610 |
| c | this estimate is used only on the first iteration so an | MIN01620 |
| c | order of magnitude estimate will suffice. the information | MIN01620 |
| c | can be provided in the following ways depending upon the | MIN01630 |
| c | value of rfn. for | MIN01650 |
| ÷ | | |

MIN01660 С rfn .gt. 0.0 - the setting of rfn itself will be taken MIN01670 с as the expected reduction in objf(x), MIN01680 С MIN01690 с - it is assumed that an estimate of the MIN01700 с rfn = 0.0minimum value of objf(x) has been set MIN01710 с in the argument objf, and the expected MIN01720 с reduction in objf(x) will be computed MIN01730 с MIN01740 с as (initial function value) minus objf, MIN01750 С rfn .lt. 0.0 - a multiple abs(rfn) of the modulus of MIN01760 С MIN01770 the initial function value will be taken с as the expected reduction. MIN01780 с MIN01790 с sprec is the accuracy required in the linear search technique MIN01800 С invoked by gqbfgs, i.e. a point xm is accepted as the MIN01810 с minimum along the search direction if the ratio of the MIN01820 с с directional derivative at xm over the directional MIN01830 с derivative at the initial point is not greater than sprec. MIN01840 С MTN01850 the setting 0.100 is recommended. MTN01860 С С MIN01870 С extbnd is the upper bound on the multiplicative increase in MIN01880 с the search scang the extrapolation phase of the MIN01890 С linear search technique. MIN01900 с MIN01910 с the setting 2.000 is recommended. MIN01920 с MIN01930 objf contains an estimate of the minimum value of objf(x) с MIN01940 if rfn = 0.0. otherwise it is only an output parameter. MIN01950 с С MIN01960 с ihess is a parameter set equal to the dimension of hess MIN01970 с which is at least nvar*(nvar+1)/2. MIN01980 с MTN01990 ¢ histry is a dummy parameter. MIN02000 с MIN02010 С on output MIN02020 С MTN02030 С MIN02040 с x contains the best available estimate of the solution vector.MIN02050 с MIN02060 с objf contains the function value at x. MTN02070 с MIN02080 с MIN02090 с hess is an array of dimension ihess which contains the MIN02100 upper triangle of the most recent approximation to the с MTN02110 hessian inverse stored row-wise. с MIN02120 с MIN02130 с g contains the components of the gradient at x. MIN02140 с MIN02150 ierr is a parameter set equal to k which gives the followingMIN02160 с с termination indications MIN02170 с MIN02180 с normal termination, MIN02190 k = 0, с MIN02200 с intermediate termination, MIN02210

| c | | MIN02220 |
|---|---------------------------------------------------------------------|-----------|
| c | | MIN02230 |
| c | | MIN02240 |
| c | likely that no minimum exists, | MIN02250 |
| с | | MIN02260 |
| c | nfcall is the number of calls to funct. | MIN02270 |
| С | | MIN02280 |
| c | srhvec contains the current search direction vector. | MIN02290 |
| c | | MIN02300 |
| С | solvec contains the current solution vector. | MIN02310 |
| С | | MIN02320 |
| С | grdvec contains the current gradient vector. | MIN02330 |
| С | | MIN02340 |
| С | scrvec is a scratch vector. | MIN02350 |
| С | | MIN02360 |
| С | written by k. e. hillstrom, march, 1976. | MIN02370 |
| с | | MIN02380 |
| С | | MIN02390 |
| с | initialize the following parameters | MINO2400 |
| с | | MINO2410 |
| с | ierr - the termination indicator | MINO2420 |
| с | nfcall - the number of calls to funct | MIN02430 |
| с | redfcn - the initial predicted reduction in objf | MINO2440 |
| с | iter - the current iteration number | MIN02450 |
| с | | MIN02460 |
| | ierr ≃ 0 | MINO2470 |
| | iter=0 | MIN02480 |
| | nfcall = 1 | MIN02490 |
| | temp = objf | MIN02500 |
| с | | MIN02510 |
| с | ************************ | MIN02520 |
| | call funct(nvar,x,objf,g) | MIN02530 |
| с | *************************************** | MIN02540 |
| с | | MIN02550 |
| | sqgrad=0.0 | MIN02560 |
| | do 220 iii=1,nvar | MIN02570 |
| | <pre>220 sqgrad=sqgrad+g(iii)**2</pre> | MIN02580 |
| с | | MIN02590 |
| | if (ierr .lt. 0) go to 410 | MIN02600 |
| | redfcn = rfn | MIN02610 |
| | if (rfn .eq. 0.0) redfcn = objf - temp | MIN02620 |
| | if (rfn .lt. 0.0) redfcn = abs(redfcn * objf) | MIN02630 |
| | if (redfcn .le. 0.0) redfcn = 1.0 | MIN02640 |
| с | | MIN02650 |
| с | read initial estimate of hessian inverse, if desired | MIN02660 |
| | if(irhess.eq.0) go to 200 | MIN02670 |
| | read(11,202) (hess(ii),ii=1,ihess) | MIN02680 |
| | 202 format (5e16.9) | MI N02690 |
| | go to 300 | MIN02700 |
| с | | MIN02710 |
| с | begin the quasi-newton process by initializing the approximation | MIN02720 |
| с | to the hessian inverse to unity | MIN02730 |
| с | | MIN02740 |
| | 200 if(iprint.ne.0) write(10,201) | MIN02750 |
| | 201 format(//2x,'>>>> quasi-newton procedure started, with search', | MIN02760 |
| | <pre>1 ' direction set to -g')</pre> | MIN02770 |
| | | |

_t ai

i di i Ali

1.2

1.5

```
MIN02780
      k = 1 + nvar * (nvar+1) / 2
                                                                          MTN02790
 с
                                                                          MIN02800
      do 210 i = 1, nvar
                                                                          MIN02810
С
                                                                          MIN02820
         do 205 j = 1, i
                                                                          MIN02830
             k = k - 1
                                                                          MIN02840
             hess(k) = 0.0
  205
         continue
                                                                          MIN02850
                                                                          MIN02860
С
         hess(k) = 1.0
                                                                          MIN02870
                                                                          MIN02880
  210 continue
                                                                          MIN02890
С
  300 if (iprint.eq.0) go to 301
                                                                          MIN02900
      euclid=sqrt(sqgrad)
                                                                          MIN02910
                                                                          MIN02920
      if(iprint.ge.20.and.mod(iter,10).ne.0) go to 308
                                                                          MIN02930
      write(6,307) iter, nfcall, objf, euclid
  307 format(1x, 'iteration:', i5, 26x, 'function evaluation:', i6,
                                                                          MIN02940
            /lx, 'objective function:',e20.13,2x, 'gradient norme:',
                                                                          MIN02950
     1
             e20.13)
                                                                          MIN02960
     2
  308 if(mod(iter,iprint).ne.0) go to 301
                                                                          MIN02970
                                                                          MIN02980
      write(10,302) iter,nfcall
  302 format(////2x,'iteration no ',i5//2x,'number of function and ',
                                                                          MIN02990
              'gradient evaluations = ', i5//2x, 'parameter values')
                                                                          MIN03000
     1
                                                                          MIN03010
      write(10,303) (j,x(j), j=1,nvar)
  303 format(/3(2x, 'x(',i4,') = ',el6.8))
                                                                          MIN03020
      write(10,304) objf
                                                                          MIN03030
  304 format(//2x, 'function value objf = ',el6.8///2x, 'gradient')
                                                                          MIN03040
      write(10,306) (j,g(j),j=1,nvar)
                                                                          MIN03050
  306 format(/3(2x, 'g(', i4, ') = ', e16.8))
                                                                          MIN03060
  301 iter=iter+1
                                                                          MIN03070
¢
                                                                          MIN03080
с
      begin an iteration by saving the current best estimate of the
                                                                          MIN03090
        function and the solution and gradient vectors.
с
                                                                          MIN03100
с
                                                                          MIN03110
      do 310 i = 1, nvar
                                                                          MIN03120
         solvec(i) = x(i)
                                                                          MIN03130
         grdvec(i) = g(i)
                                                                          MIN03140
  310 continue
                                                                          MIN03150
с
                                                                          MIN03160
      tobjf = objf
                                                                          MIN03170
С
                                                                          MIN03180
      calculate the search direction vector in srhvec and the
С
                                                                          MIN03190
с
        directional derivative in dirdev
                                                                          MIN03200
с
                                                                          MIN03210
      do 340 i = 1, nvar
                                                                          MIN03220
         ij = i
                                                                          MIN03230
         z = 0.0
                                                                          MIN03240
                                                                          MIN03250
С
         do 330 j = 1, nvar
                                                                          MIN03260
            z = z - g(j) * hess(ij)
                                                                          MIN03270
            if (j.ge. i) go to 325
                                                                          MIN03280
            ij ≃ ij + nvar - j
                                                                          MIN03290
            go to 330
                                                                          MIN03300
  325
            ij = ij + 1
                                                                          MIN03310
  330
         continue
                                                                          MIN03320
с
                                                                          MIN03330
```

```
184
```

V.

```
MIN03340
         srhvec(i) = z
                                                                   MIN03350
  340 continue
                                                                   MIN03360
c
                                                                   MIN03370
      dirdev = 0.0
                                                                   MIN03380
С
                                                                   MIN03390
      do 350 i = 1, nvar
                                                                   MIN03400
        dirdev = dirdev + srhvec(i) * g(i)
                                                                   MIN03410
  350 continue
                                                                   MIN03420
с
     if the directional derivative dirdev is .gt. 0, there is no
                                                                  MIN03430
с
       guarantee that a search in the w direction will result in a MIN03440
с
       smaller objf. therefore, the quasi-newton process is
                                                                   MIN03450
С
       restarted at the current estimate of the solution with srhvec MIN03460
С
                                                                   MTN03470
с
       set to -q.
с
                                                                   MIN03480
                                                                   MIN03490
      if (dirdev .gt. 0.0) go to 200
                                                                   MIN03500
      if (dirdev .eq. 0.0) go to 500
                                                                   MIN03510
с
     compute the initial search scaha and conduct the
                                                                   MIN03520
с
                                                                   MIN03530
с
       linear search by means of a call to search
                                                                   MIN03540
С
      alpha = -2.0 * redfcn / dirdev
                                                                   MIN03550
      if (alpha .gt. 1.0) alpha = 1.0
                                                                   MIN03560
                                                                   MIN03570
      redfcn = objf
                                                                   MIN03580
С
      MIN03590
С
                                                                   MIN03600
     call search(nvar, x, g, srhvec, objf, alpha, dirdev, sprec,
     1
        extbnd, nfcall, scrvec, ierr, funct, maxf)
                                                                   MIN03610
     ***********
                                                                   MIN03620
С
с
                                                                   MTN03630
с
     test for abnormal termination
                                                                   MIN03640
С
                                                                   MIN03650
      if (ierr .lt. 0) go to 500
                                                                   MIN03660
     if (nfcall .ge. maxf) go to 400
                                                                   MIN03670
     if ((alpha .lt. 1.0e-20) .or.
                                                                   MIN03680
     1 (alpha .gt. 1.0e20)) go to 410
                                                                   MIN03690
                                                                   MIN03700
с
    test for convergence
                                                                   MIN03710
с
                                                                   MIN03720
с
     sqgrad = 0.0
                                                                   MIN03730
     iconv = 0
                                                                   MIN03740
с
                                                                   MIN03750
     do 360 i = 1, nvar
                                                                   MIN03760
        temp = alpha * srhvec(i)
                                                                   MIN03770
        sqgrad = sqgrad + g(i) * g(i)
                                                                   MIN03780
        t = tolx * abs(x(i))
                                                                   MIN03790
        if (t .le. tolx) t = tolx
                                                                   MIN03800
        if (abs(temp) .gt. t) iconv = 1
                                                                   MIN03810
 360 continue
                                                                   MIN03820
с
                                                                   MIN03830
     if (sqgrad .gt. tolg*tolg) iconv = 1
                                                                   MIN03840
     if (sqgrad .eq. 0.0) iconv = 0
                                                                   MIN03850
     if (iconv .eq. 0) go to 500
                                                                   MIN03860
с
                                                                   MIN03870
с
     the linear search technique has located a minimum. call uphess MIN03880
       to update the approximation to the hessian inverse using the
                                                                   MIN03890
С
```

: 20

....

4

â

. anto

```
MIN03900
        dfp or bfgs updating formulas
С
                                                                  MTN03910
С
      ******
                                                                  MIN03920
С
      call uphess(nvar, x, q, ihess, hess, solvec, grdvec, scrvec, iswtch, iexit)MIN03930
      ******
                                                                  MIN03940
с
                                                                  MIN03950
С
                                                                  MIN03960
с
     if the update is not successful the quasi-newton process is
                                                                  MIN03970
с
       restarted with a descent step at the current estimate of the
                                                                  MIN03980
с
       solution
                                                                  MIN03990
С
                                                                  MIN04000
     redfcn = redfcn - objf
                                                                  MIN04010
     if (iexit .ne. 0) go to 200
                                                                  MTN04020
с
                                                                  MIN04030
     now start a new iteration
С
                                                                  MIN04040
С
c write the current estimate of the hessian inverse, if desired.
                                                                  MIN04050
                                                                  MIN04060
     if (iwhess.eq.0) go to 300
                                                                  MIN04070
      write(12,202) (hess(ii),ii=1,ihess)
                                                                  MIN04080
С
     go to 300
                                                                  MTN04090
с
                                                                  MIN04100
     error return because there have been at least maxf calls of
с
                                                                  MIN04110
с
       funct
                                                                  MIN04120
С
                                                                  MIN04130
  400 ierr = 1
                                                                  MIN04140
     go to 450
                                                                  MTN04150
с
                                                                  MIN04160
     error return because linear search technique indicates that it is MIN04170
С
      likely that no minimum exists
                                                                  MIN04180
с
                                                                  MIN04190
с
  410 ierr = 2
                                                                  MIN04200
                                                                  MIN04210
с
  450 \text{ do } 455 \text{ i} = 1, \text{ nvar}
                                                                  MIN04220
        x(i) = solvec(i)
                                                                  MIN04230
        g(i) = grdvec(i)
                                                                  MIN04240
  455 continue
                                                                  MIN04250
                                                                  MIN04260
С
     objf = tobjf
                                                                  MIN04270
  500 return
                                                                  MTN04280
С
                                                                  MIN04290
     end
                                                                  MIN04300
                                                                  MIN04310
subroutine uphess(n,x,g,ih,h,solvec,grdvec,scrvec,iswtch,iexit)
                                                                 MIN04330
С
                                                                  MIN04340
     implicit real*8 (a-h,o-z)
                                                                  MIN04350
с
                                                                  MIN04360
     dimension x(n),g(n),h(ih),solvec(n),
                                                                  MIN04370
    1
               grdvec(n), scrvec(n)
                                                                  MIN04380
С
                                                                  MIN04390
     this subroutine updates an approximation to the hessian inverse
С
                                                                 MTN04400
      using the dfp or bfgs formula
С
                                                                  MIN04410
с
                                                                  MIN04420
С
    on input
                                                                  MIN04430
```

n is the dimension of the vectors x, g, solvec, grdvec and MIN04450

с

С

U.

÷

MIN04440

1.25

```
MIN04460
             scrvec.
 С
                                                                         MIN04470
 С
                                                                         MIN04480
         x contains an estimate of the solution vector.
 С
                                                                         MIN04490
 С
         g contains the components of the gradient corresponding to
                                                                         MIN04500
 с
                                                                          MIN04510
 С
             the x vector.
                                                                          MTN04520
 с
         ih is a parameter set equal to the dimension of h which is MIN04530
 с
                                                                          MIN04540
            at least n*(n+1)/2.
 С
                                                                         MIN04550
 С
         h is an array of dimension ih which contains the upper
                                                                          MIN04560
 с
            triangle of an approximation to the hessian inverse stored MIN04570
 с
                                                                          MIN04580
             by rows.
 С
                                                                          MIN04590
 С
         solvec contains the current solution vector.
                                                                         MIN04600
 c
                                                                         MIN04610
 С
 с
         grdvec contains the current gradient vector.
                                                                          MIN04620
                                                                          MIN04630
 С
                                                                          MIN04640
         iswtch is a parameter set equal to k which selects the
 С
                                                                          MIN04650
 с
            updating formula. for
                                                                          MIN04660
 с
                                                                         MIN04670
             k = 1 - the dfp formula is used,
 с
             k = 2 - the bfgs formula is used.
                                                                         MIN04680
 с
                                                                         MIN04690
 C
                                                                         MIN04700
      on output
 с
                                                                          MTN04710
 с
         iexit is a parameter set equal to k which indicates the
                                                                          MIN04720
С
                                                                          MIN04730
С
            following. for
                                                                          MIN04740
c
                                                                          MIN04750
            k = 0 - the update was successful,
С
                                                                         MIN04760
            k = 1 - the update failed due to zero divisors.
с
                                                                         MIN04770
с
         h contains the updated approximation to the hessian inverse
                                                                         MIN04780
С
                                                                          MIN04790
c
            if iexit = 0.
                                                                         MIN04800
С
         scrvec is a scratch vector.
                                                                         MIN04810
с
                                                                          MIN04820
C
                                                                         MIN04830
     written by k. e. hillstrom, march, 1976.
с
                                                                         MIN04840
с
                                                                         MIN04850
с
      initialize the exit indicator iexit
                                                                          MIN04860
с
                                                                          MIN04870
с
                                                                         MIN04880
      iexit = 0
с
                                                                          MIN04890
      calculate the solution and gradient difference vectors from two · MIN04900
с
        consecutive iterations. from this section on
                                                                         MIN04910
С
                                                                         MIN04920
с
        solvec - contains delta, the solution difference vector
                                                                         MIN04930
с
с
        grdvec - contains gamma, the gradient difference vector
                                                                         MIN04940
                                                                          MTN04950
. с
  100 \text{ do } 110 \text{ i} = 1, \text{ n}
                                                                          MIN04960
         solvec(i) = x(i) - solvec(i)
                                                                          MIN04970
         grdvec(i) = g(i) - grdvec(i)
                                                                          MIN04980
  110 continue
                                                                          MIN04990
с
                                                                         MIN05000
                                                                         MIN05010
с
   calculate z = (gamma transpose) * delta and alpha =
```

```
(gamma transpose) * (hessian inverse) * gamma occuring as
                                                                         MIN05020
с
        denominators in the dfp formula. from this section on
                                                                         MIN05030
с
                                                                         MIN05040
с
               - contains the approximation to the hessian inverse
                                                                         MIN05050
С
        h
        scrvec - contains the successive elements of (gamma transpose) MIN05060
с
                                                                         MIN05070
                 * (hessian inverse)
с
                                                                         MIN05080
С
                                                                         MIN05090
      z = 0.0
                                                                         MIN05100
      alpha = 0.0
                                                                         MIN05110
с
                                                                         MIN05120
      do 130 i = 1, n
                                                                         MIN05130
         wt = grdvec(i)
                                                                         MIN05140
         z = z + wt + solvec(i)
                                                                         MIN05150
         k = i
                                                                         MIN05160
         wt = 0.0
                                                                         MIN05170
с
                                                                         MIN05180
         do 120 j = 1, n
            wt = wt + grdvec(j) * h(k)
                                                                         MIN05190
            if (j .ge. i) go to 115
                                                                         MIN05200
                                                                         MIN05210
            k = k + n - j
                                                                         MIN05220
            go to 120
  115
            k = k + 1
                                                                         MIN05230
  120
         continue
                                                                         MIN05240
                                                                         MIN05250
С
         alpha = alpha + wt * grdvec(i)
                                                                         MIN05260
         scrvec(i) = wt
                                                                         MIN05270
                                                                         MIN05280
  130 continue
                                                                         MIN05290
с
      error exit if the dfp or bfgs formula breaks down due to zero MIN05300
С
С
       divisors z and/or alpha
                                                                         MIN05310
с
                                                                         MIN05320
      if ((z .eq. 0.0) .or.
                                                                         MIN05330
                                                                         MIN05340
     1 (alpha .eq. 0.0 .and. iswtch .eq. 1)) go to 200
                                                                         MIN05350
С
     update the approximation to the hessian inverse using the dfp
                                                                         MIN05360
С
       or bfgs updating formula
                                                                         MIN05370
С
                                                                         MIN05380
С
      k = 1
                                                                         MTN05390
с
                                                                         MIN05400
     do 160 i = 1, n
                                                                         MIN05410
                                                                         MIN05420
с
         do 150 j = i, n
                                                                         MIN05430
            if (iswtch .eq. 1) go to 135
                                                                         MIN05440
            h(k) = h(k) - (solvec(i) * scrvec(j) + scrvec(i) *
                                                                         MIN05450
    1
                   solvec(j)) / z + (1.0 + alpha / z) * (solvec(i) *
                                                                         MIN05460
     2
                                                                         MIN05470
                   solvec(j) / z)
            go to 140
                                                                         MIN05480
  135
            h(k) = h(k) + solvec(i) * solvec(j) / z - scrvec(i) *
                                                                         MIN05490
    1
                   scrvec(j) / alpha
                                                                         MIN05500
  140
            k = k + 1
                                                                         MIN05510
  150
         continue
                                                                         MIN05520
                                                                         MIN05530
с
 160 continue
                                                                         MIN05540
                                                                         MIN05550
С
                                                                         MIN05560
      go to 300
С
                                                                         MIN05570
```

Ŷ

```
MIN05580
     error return due to zero divisors in the updating formula
c
                                                                      MTN05590
c
                                                                      MIN05600
  200 iexit = 1
                                                                      MIN05610
  300 return
                                                                      MIN05620
с
                                                                      MTN05630
      end
                                                                      MIN05640
MIN05660
      subroutine search(n,x,g,s,f,alpha,dirdev,sprec,extbnd,
                                                                      MTN05670
     1
                       nfcall,w,ierr,funct,maxf)
                                                                      MTN05680
С
                                                                      MIN05690
      implicit real*8 (a-h,o-z)
                                                                      MIN05700
С
                                                                      MIN05710
      dimension x(n), g(n), s(n), w(n)
                                                                      MIN05720
с
       this subroutine obtains an estimate of the solution
                                                                      MIN05730
с
      xm = x0 + alpha + s which minimizes f by means of a linear
                                                                      MIN05740
С
      search in the s direction.
                                                                      MIN05750
С
C
                                                                      MTN05760
с
      on input
                                                                      MIN05770
                                                                      MIN05780
с
с
         n is the number of variables. it is also the dimension of the MIN05790
с
            vectors x, q and s.
                                                                      MIN05800
                                                                      MTN05810
С
с
        x contains an estimate of the solution vector
                                                                      MIN05820
С
            (x0(1), x0(2), \dots, x0(n)).
                                                                      MTN05830
с
                                                                      MIN05840
с
         s contains the search direction vector.
                                                                      MIN05850
С
                                                                      MIN05860
с
        f contains the objective function f(x).
                                                                      MIN05870
с
                                                                      MIN05880
с
        funct is a user supplied routine to evaluate f(x) and the
                                                                      MTN05890
           components of the gradient g(x) at the estimate in x.
                                                                      MIN05900
С
с
                                                                      MIN05910
        alpha is the initial step sca
                                                             LAR05800MIN05920
С
с
                                                                      MIN05930
        dirdev is the directional derivative at x.
с
                                                                      MIN05940
с
                                                                      MIN05950
        sprec is the accuracy required in the search, i.e. a point xmMIN05960
с
           is accepted as the minimum along direction s if the ratio MIN05970
С
C
            of the directional derivative at xm over the directional MIN05980
С
           derivative at x0 is not greater than sprec.
                                                                      MIN05990
с
                                                                      MIN06000
        extbnd is the upper bound on the multiplicative increase in
с
                                                                      MIN06010
С
           alpha during extrapolation.
                                                                      MIN06020
с
                                                                      MIN06030
        nfcall is the number of calls to the function evaluation
С
                                                                      MIN06040
с
           subroutine fcn.
                                                                      MIN06050
с
                                                                      MIN06060
с
        w is a scratch vector.
                                                                      MIN06070
с
                                                                      MIN06080
с
     on output
                                                                      MIN06090
с
                                                                      MIN06100
        x contains the estimate of the minimum
С
                                                                      MIN06110
с
            (xm(1), xm(2),..., xm(n))
                                                                      MIN06120
c
                                                                      MIN06130
```

```
ierr is a parameter set to a negative integer if the user
                                                                    MIN06140
с
           wishes to force an exit from search. otherwise it is
                                                                    MIN06150
с
                                                                    MIN06160
           unaltered.
с
                                                                    MTN06170
с
        g contains the components of the gradient at x.
                                                                    MIN06180
С
                                                                    MIN06190
с
                                                                    MIN06200
        f contains the function value f(x).
С
                                                                    MIN06210
с
                                                                    MIN06220
с
        alpha is the final step sca
с
                                                                    MIN06230
                                                                    MIN06240
С
        dirdev is the directional derivative at x.
                                                                    MIN06250
С
        nfcall is the number of calls to the function evaluation
                                                                    MTN06260
с
           subroutine funct.
                                                                    MTN06270
с
                                                                    MIN06280
с
                                                                    MIN06290
с
      initialize the following parameters and indicators
                                                                    MIN06300
С
                                                                    MIN06310
с
                                                                    MIN06320
с
       tot
                 - the sum of the extrapolation steps
                 - the current directional derivative
                                                                    MIN06330
С
       cdirev
       pdirev - the previous directional derivative
                                                                    MIN06340
с
с
       ierr

    the error indicator

                                                                    MIN06350
                                                                    MTN06360
с
     tot = 0.0d0
                                                                    MIN06370
      cdirev = dirdev
                                                                    MIN06380
     pdirev = dirdev
                                                                    MIN06390
c
                                                                    MIN06400
     test whether alpha is too small
                                                                    MTN06410
С
                                                                    MIN06420
С
 105 if (alpha .le. 1.0d-20) go to 150
                                                                    MIN06430
с
                                                                    MIN06440
с
     begin the linear search by incrementing the solution vector x
                                                                    MIN06450
       and calculating the function and gradient at the incremented x.MIN06460
с
С
                                                                    MIN06470
      do 108 i = 1, n
                                                                    MIN06480
        w(i) = x(i)
                                                                    MIN06490
        x(i) = x(i) + alpha * s(i)
                                                                    MIN06500
 108 continue
                                                                    MIN06510
с
                                                                    MIN06520
      *****
с
                                                                    MIN06530
     call funct(n,x,ftest,g)
                                                                    MIN06540
     *****
С
                                                                    MIN06550
с
                                                                    MIN06560
     nfcall = nfcall + 1
                                                                    MIN06570
     if (maxf.lt.nfcall) go to 160
                                                                    MTN06580
     if (ierr .lt. 0) go to 150
                                                                    MIN06590
С
                                                                    MIN06600
c   compute the directional derivative dirdev at  x + alpha * s 
                                                                    MIN06610
с
                                                                    MIN06620
     dirdev = 0.0d0
                                                                    MIN06630
с
                                                                    MIN06640
     do 110 i = 1, n
                                                                    MIN06650
        dirdev = dirdev + g(i) * s(i)
                                                                    MIN06660
 110 continue
                                                                    MIN06670
С
                                                                    MIN06680
С
    test whether f(x + alpha + s) is less than f(x).
                                                                   MTN06690
```

.

```
MIN06700
с
                                                                          MIN06710
       if (ftest .ge. f) go to 120
                                                                          MIN06720
с
       if (dirdev / pdirev) is less than the search precision . sprec,
                                                                          MIN06730
с
                                                                          MIN06740
        alpha is accepted. otherwise alpha is modified
С
                                                                          MIN06750
С
       if (abs(dirdev / pdirev) .le. sprec) go to 140
                                                                          MIN06760
                                                                          MIN06770
с
       alpha is modified. test whether alpha is to be revised by
                                                                          MIN06780
С
        extrapolation or interpolation
                                                                          MIN06790
С
                                                                          MTN06800
с
       if (dirdev .gt. 0.0d0) go to 120
                                                                          MIN06810
с
                                                                          MIN06820
       alpha is revised using an extrapolation formula and a new step
                                                                          MIN06830
С
        is taken if the sum of the steps already made is not too
с
                                                                          MIN06840
с
        the input parameter extbnd limits the multiplicative change
                                                                          MIN06850
с
        in alpha
                                                                          MIN06860
с
                                                                          MIN06870
      tot = tot + alpha
                                                                          MIN06880
      if (tot .gt. 1.0d10) go to 145
                                                                          MTN06890
      temp = extbnd
                                                                          MIN06900
      if (cdirev .lt. dirdev) temp = dirdev / (cdirev - dirdev)
                                                                          MIN06910
      if (temp .gt. extbnd) temp = extbnd
                                                                          MIN06920
      f = ftest
                                                                          MIN06930
      cdirev = dirdev
                                                                          MIN06940
      alpha = alpha * temp
                                                                          MIN06950
      go to 105
                                                                          MIN06960
с
                                                                          MTN06970
с
      x is reset to the current estimate, alpha is revised using the MIN06980
        cubic interpolation formula and a new step is taken if the
С
                                                                          MIN06990
        convergence criteria have not been satisfied.
С
                                                                          MIN07000
                                                                          MIN07010
с
  120 do 130 i = 1, n
                                                                          MIN07020
         x(i) = w(i)
                                                                          MTN07030
  130 continue
                                                                          MIN07040
с
                                                                          MIN07050
      temp = 3.0d0 * (f - ftest) / alpha + dirdev + cdirev
                                                                          MIN07060
      wt = abs(temp)
                                                                         MIN07070
      if(wt.lt.abs(dirdev)) wt=abs(dirdev)
                                                                          MIN07080
                                                                         MIN07090
      if(wt.lt.abs(cdirev)) wt=abs(cdirev)
      ww = temp / wt
                                                                          MIN07100
      ww = ww * ww - cdirev / wt * dirdev / wt
                                                                         MIN07110
      if (ww .lt. 0.0d0) ww = 0.0d0
                                                                         MIN07120
      ww = dsqrt(ww) * wt
                                                                          MIN07130
      temp = 1.0d0 - (dirdev + ww - temp) / (2.0d0 * ww + dirdev -
                                                                         MIN07140
     1
            cdirev)
                                                                         MIN07150
      alpha = alpha * temp
                                                                          MIN07160
      go to 105
                                                                          MIN07170
с
                                                                          MIN07180
с
      alpha is accepted
                                                                         MIN07190
С
                                                                         MIN07200
 140 f = ftest
                                                                         MIN07210
  145 alpha = tot + alpha
                                                                          MIN07220
  150 return
                                                                         MIN07230
с
                                                                         MIN07240
 160 \text{ do } 170 \text{ i} = 1, \text{ n}
                                                                         MIN07250
```

Ð

| 170 continue return c end SUBROUTINE SUMDATA(NVAR,X,OBJF,G) C FILE TO GENERATE FN(T) FOR FISCHER-TROPSCH MODELLING AND FIT DAT C N IS CARBON NUMBER,NO IS THE NO OF DATA POINTS C TAU AND TAUB ARE GUESSES IMPLICIT REAL*8(A-H,O-2) COMMON /EXPTDATAR/T,FEXP COMMON /EXPTDATAI/NO COMMON /CARBON/N | MIN07270 MIN07280 MIN07290 MIN07300 MIN07310 MIN07320 TA MIN07330 MIN07350 MIN07350 MIN07360 MIN07370 MIN07380 |
|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------------------|
| <pre>return c end SUBROUTINE SUMDATA(NVAR, X, OBJF, G) C FILE TO GENERATE FN(T) FOR FISCHER-TROPSCH MODELLING AND FIT DAT C N IS CARBON NUMBER, NO IS THE NO OF DATA POINTS C TAU AND TAUB ARE GUESSES IMPLICIT REAL*8(A-H, O-2) COMMON /EXPTDATAR/T, FEXP COMMON /EXPTDATAI/N0</pre> | MIN07290 MIN07300 MIN07310 MIN07320 FA MIN07330 MIN07340 MIN07350 MIN07360 MIN07370 |
| end SUBROUTINE SUMDATA (NVAR, X, OBJF, G) C FILE TO GENERATE FN(T) FOR FISCHER-TROPSCH MODELLING AND FIT DAT C N IS CARBON NUMBER, NO IS THE NO OF DATA POINTS C TAU AND TAUB ARE GUESSES IMPLICIT REAL*8(A-H, O-2) COMMON /EXPTDATAR/T, FEXP COMMON /EXPTDATAI/NO | MIN07300 MIN07310 MIN07320 FA MIN07330 MIN07340 MIN07350 MIN07360 MIN07370 |
| SUBROUTINE SUMDATA (NVAR, X, OBJF, G) C FILE TO GENERATE FN(T) FOR FISCHER-TROPSCH MODELLING AND FIT DAT C N IS CARBON NUMBER, NO IS THE NO OF DATA POINTS C TAU AND TAUB ARE GUESSES IMPLICIT REAL*8(A-H, O-2) COMMON /EXPTDATAR/T, FEXP COMMON /EXPTDATAI/NO | MIN07310 MIN07320 FA MIN07330 MIN07340 MIN07350 MIN07360 MIN07370 |
| C FILE TO GENERATE FN(T) FOR FISCHER-TROPSCH MODELLING AND FIT DAT C N IS CARBON NUMBER, NO IS THE NO OF DATA POINTS C TAU AND TAUB ARE GUESSES IMPLICIT REAL*8(A-H, O-2) COMMON /EXPTDATAR/T, FEXP COMMON /EXPTDATAI/NO | MIN07320 FA MIN07330 MIN07340 MIN07350 MIN07360 MIN07370 |
| C FILE TO GENERATE FN(T) FOR FISCHER-TROPSCH MODELLING AND FIT DAT C N IS CARBON NUMBER, NO IS THE NO OF DATA POINTS C TAU AND TAUB ARE GUESSES IMPLICIT REAL*8(A-H, O-2) COMMON /EXPTDATAR/T, FEXP COMMON /EXPTDATAI/NO | FA MIN07330 MIN07340 MIN07350 MIN07360 MIN07370 |
| C N IS CARBON NUMBER, NO IS THE NO OF DATA POINTS C TAU AND TAUB ARE GUESSES IMPLICIT REAL*8(A-H, O-Z) COMMON /EXPTDATAR/T, FEXP COMMON /EXPTDATAI/NO | MIN07340 MIN07350 MIN07360 MIN07370 |
| C TAU AND TAUB ARE GUESSES IMPLICIT REAL*8 (A-H, O-Z) COMMON /EXPTDATAR/T, FEXP COMMON /EXPTDATAI/NO | MIN07350 MIN07360 MIN07370 |
| IMPLICIT REAL*8(A-H,O-Z) COMMON /EXPTDATAR/T,FEXP COMMON /EXPTDATAI/NO | MIN07360 MIN07370 |
| COMMON /EXPTDATAR/T,FEXP COMMON /EXPTDATAI/NO | MIN07370 |
| COMMON /EXPTDATAR/T,FEXP COMMON /EXPTDATAI/NO | |
| COMMON /EXPTDATAI/NO | MTN07380 |
| | CITICO DOO |
| COMMON /CARBON/N | MIN07390 |
| | MIN07400 |
| DIMENSION T(100), FEXP(100), X(NVAR), G(NVAR), Y(2) | MIN07410 |
| C************************************* | ** MIN07420 |
| <pre>C OBJF IS SUM OF{F(EXPT)-F(T)}**2;DOFTAU IS D/DTAU OF OBJF;</pre> | MIN07430 |
| C DOFTAUB IS D/DTAUB OF OBJF | MIN07440 |
| C************************************* | ** MIN07450 |
| | MIN07460 |
| OBJF=0.0D0 | MIN07470 |
| DOFTAU=0.0D0 | MIN07480 |
| DOFTAUB=0.0D0 | MIN07490 |
| DTAU=0.0D0 | MIN07500 |
| DTAUB=0.0D0 | MIN07510 |
| DELT=1.0D-5 | MIN07520 |
| | MIN07530 |
| DO 2 I=1, NO | MIN07540 |
| Y(1)=X(1) | MIN07550 |
| Y (2) = X (2) | MIN07560 |
| TIME=T(I) | MIN07570 |
| CALL FUNC (TIME, FN, DELTAU, DELTAUB, X, NVAR) | MIN07580 |
| OBJF=OBJF+(FEXP(I)-FN)**2 | MIN07590 |
| DOFTAU=DOFTAU+ (-2.0D0*(FEXP(I)-FN)*DELTAU) | MIN07600 |
| DOFTAUB=DOFTAUB+ (-2.00* (FEXP (I) -FN) *DELTAUB) | MIN07610 |
| Y(1) = X(1) * (1.0 + DELT/2.) | MIN07620 |
| CALL FUNC (TIME, FNT, DELTA, DELTAB, Y, NVAR) | MIN07630 |
| Y(1) = X(1) * (1.0 - DELT/2.) | MIN07640 |
| | MIN07650 |
| CALL FUNC (TIME, FNT1, DELTA, DELTAB, Y, NVAR) | MIN07660 |
| CALL FUNC(TIME,FNTI,DELTA,DELTAB,Y,NVAR) DTAU=DTAU+(-2.0D0*(FEXP(I)-FN)*(FNT-FNT1)/(X(1)*DELT)) | |
| | MIN07670 |
| | |
| DTAU=DTAU+ (-2.0D0*(FEXP(I)-FN)*(FNT-FNT1)/(X(1)*DELT)) | MIN07670 |
| DTAU=DTAU+ (-2.0D0*(FEXP(I)-FN)*(FNT-FNT1)/(X(1)*DELT)) Y(1)=X(1) | MIN07670 MIN07680 |
| DTAU=DTAU+(-2.0D0*(FEXP(I)-FN)*(FNT-FNT1)/(X(1)*DELT)) Y(1)=X(1) Y(2)=X(2)*(1.0 + DELT/2.0D0) | MIN07670 MIN07680 MIN07690 |
| DTAU=DTAU+(-2.0D0*(FEXP(I)-FN)*(FNT-FNT1)/(X(1)*DELT)) Y(1)=X(1) Y(2)=X(2)*(1.0 + DELT/2.0D0) CALL FUNC(TIME,FNTB,DELTA,DELTAB,Y,NVAR) | MIN07670 MIN07680 MIN07690 MIN07700 |
| DTAU=DTAU+(-2.0D0*(FEXP(I)-FN)*(FNT-FNT1)/(X(1)*DELT)) Y(1)=X(1) Y(2)=X(2)*(1.0 + DELT/2.0D0) CALL FUNC(TIME,FNTB,DELTA,DELTAB,Y,NVAR) Y(2)=X(2)*(1.0 - DELT/2.0D0) | MIN07670 MIN07680 MIN07690 MIN07700 MIN07710 |
| DTAU=DTAU+ (-2.0D0* (FEXP(I)-FN)* (FNT-FNT1) / (X(1)*DELT)) Y(1)=X(1) Y(2)=X(2)*(1.0 + DELT/2.0D0) CALL FUNC(TIME,FNTB,DELTA,DELTAB,Y,NVAR) Y(2)=X(2)*(1.0 - DELT/2.0D0) CALL FUNC(TIME,FNTB1,DELTA,DELTAB,Y,NVAR) | MIN07670 MIN07680 MIN07690 MIN07700 MIN07710 MIN07720 |
| DTAU=DTAU+ (-2.0D0* (FEXP(I)-FN)* (FNT-FNT1) / (X(1)*DELT)) Y(1)=X(1) Y(2)=X(2)*(1.0 + DELT/2.0D0) CALL FUNC(TIME,FNTB,DELTA,DELTAB,Y,NVAR) Y(2)=X(2)*(1.0 - DELT/2.0D0) CALL FUNC(TIME,FNTB1,DELTA,DELTAB,Y,NVAR) | MIN07670 MIN07680 MIN07690 MIN07700 MIN07710 MIN07720 MIN07730 |
| DTAU=DTAU+ (-2.0D0* (FEXP (I) -FN)* (FNT-FNT1) / (X (1)*DELT)) Y (1) =X (1) Y (2) =X (2)*(1.0 + DELT/2.0D0) CALL FUNC (TIME, FNTB, DELTA, DELTAB, Y, NVAR) Y (2) =X (2)*(1.0 - DELT/2.0D0) CALL FUNC (TIME, FNTB1, DELTA, DELTAB, Y, NVAR) DTAUB=DTAUB+ (-2.0D0* (FEXP (I) -FN)* (FNTB-FNTB1) / (X (2)*DELT)) | MIN07670 MIN07680 MIN07690 MIN07700 MIN07710 MIN07720 MIN07730 MIN07740 |
| DTAU=DTAU+ (-2.0D0* (FEXP (I) -FN)* (FNT-FNT1) / (X (1)*DELT)) Y (1) =X (1) Y (2) =X (2)*(1.0 + DELT/2.0D0) CALL FUNC (TIME, FNTB, DELTA, DELTAB, Y, NVAR) Y (2) =X (2)*(1.0 - DELT/2.0D0) CALL FUNC (TIME, FNTB1, DELTA, DELTAB, Y, NVAR) DTAUB=DTAUB+ (-2.0D0* (FEXP (I) -FN)* (FNTB-FNTB1) / (X (2)*DELT)) | MIN07670 MIN07680 MIN07690 MIN07700 MIN07710 MIN07720 MIN07730 MIN07740 MIN07750 |
| DTAU=DTAU+ (-2.0D0* (FEXP (I) -FN)* (FNT-FNT1) / (X (1)*DELT)) Y (1) =X (1) Y (2) =X (2)*(1.0 + DELT/2.0D0) CALL FUNC (TIME, FNTB, DELTA, DELTAB, Y, NVAR) Y (2) =X (2)*(1.0 - DELT/2.0D0) CALL FUNC (TIME, FNTB1, DELTA, DELTAB, Y, NVAR) DTAUB=DTAUB+ (-2.0D0* (FEXP (I) -FN)* (FNTB-FNTB1) / (X (2)*DELT)) 2 CONTINUE | MIN07670 MIN07680 MIN07690 MIN07700 MIN07710 MIN07720 MIN07730 MIN07740 MIN07750 MIN07760 |
| DTAU=DTAU+ (-2.0D0* (FEXP (I) -FN)* (FNT-FNT1) / (X (1)*DELT)) Y (1) =X (1) Y (2) =X (2)*(1.0 + DELT/2.0D0) CALL FUNC (TIME, FNTB, DELTA, DELTAB, Y, NVAR) Y (2) =X (2)*(1.0 - DELT/2.0D0) CALL FUNC (TIME, FNTB1, DELTA, DELTAB, Y, NVAR) DTAUB=DTAUB+ (-2.0D0* (FEXP (I) -FN)* (FNTB-FNTB1) / (X (2)*DELT)) 2 CONTINUE WRITE (6, *) '0.F', OBJF, DTAU, DTAUB | MIN07670 MIN07680 MIN07690 MIN07700 MIN07710 MIN07720 MIN07730 MIN07740 MIN07750 MIN07760 MIN07770 |
| DTAU=DTAU+ (-2.0D0* (FEXP (I) -FN)* (FNT-FNT1) / (X (1)*DELT)) Y (1) =X (1) Y (2) =X (2)*(1.0 + DELT/2.0D0) CALL FUNC (TIME, FNTB, DELTA, DELTAB, Y, NVAR) Y (2) =X (2)*(1.0 - DELT/2.0D0) CALL FUNC (TIME, FNTB1, DELTA, DELTAB, Y, NVAR) DTAUB=DTAUB+ (-2.0D0* (FEXP (I) -FN)* (FNTB-FNTB1) / (X (2)*DELT)) 2 CONTINUE WRITE (6,*) '0.F', OBJF, DTAU, DTAUB WRITE (6,*) 'TAU=', X (1), 'TAUB', X (2) | MIN07670 MIN07680 MIN07690 MIN07700 MIN07710 MIN07720 MIN07730 MIN07750 MIN07750 MIN07760 MIN07770 MIN07780 |

.

×

Ċ)

Ð

ê

MIN07820 G(2) = DTAUBMTN07830 MIN07840 RETURN MIN07850 END MIN07860 MIN07870 SUBROUTINE FACT (M, J) MTN07880 J=1 MIN07890 IF (M.EQ.0) GOTO 4 MIN07900 DO 1 I=1,M MIN07910 J=J*I MIN07920 CONTINUE 1 MIN07930 RETURN 4 MIN07940 END MIN07950 FUNC EVALUATES FN(TIME), AND PARTIAL DERIVATIVES WRT TAU AND TAUB MIN07970 С DELTAU AND DELTAUB MIN07980 С SUBROUTINE FUNC (TIME, FN, DELTAU, DELTAUB, X, NVAR) MTN08000 MIN08010 IMPLICIT REAL*8(A-H,O-Z) COMMON /CARBON/N MIN08020 MIN08030 DIMENSION X(NVAR) MIN08040 TAU = X(1)MIN08050 TAUB=X(2) MIN08060 A1=TAUB/(TAU-TAUB) AK1=0.0D0 MIN08070 MIN08080 AK2=0.0D0 DO 1 I=1,N MIN08090 MIN08100 AK1=AK1+(A1**I)*((-1)**(I+1)) 1 CONTINUE MIN08110 MIN08120 AK2 = AK2 + ((-A1) - 1)DO 2 I=2.N MIN08130 С WRITE(22,*)TIME,NI MTN08140 DO 3 IR1=1,I-1 MIN08150 IR=IR1-1 MIN08160 MIN08170 CALL FACT (I-IR-1, IRR) С WRITE(22, *)TIME, IRR MIN08180 IF(IRR.LE.0)GOTO 200 MIN08190 AK2=AK2+(1.000/(TAU**I))*(TAU**(IR+1)*TIME**(I-IR-1)*(-1+(-A1)**(IMIN08200 1R+1))/IRR) MIN08210 3 CONTINUE MIN08220 AK2=AK2+(1.000)*((-A1)**(I)-1.) MIN08230 2 CONTINUE MIN08240 T1=TIME/TAU MIN08250 T2=TIME/TAUB MIN08260 IF (T1.LT.75.D0.AND.T2.LT.75.D0) GO TO 20 MIN08270 MIN08280 FN=1.0D0 IF (T1.LT.75.D0) FN=1.0D0+AK2*DEXP (-TIME/TAU) /N MIN08290 IF (T2.LT.75.D0) FN=1.0D0+AK1/N*DEXP(-TIME/TAUB) MIN08300 GO TO 21 MIN08310 20 FN=1.0+(AK1/N)*DEXP(-TIME/TAUB)+AK2*DEXP(-TIME/TAU)/N MIN08320 21 AL1=0.0D0 MIN08330 AL2=AK2 MIN08340 AL3=0.0D0 MIN08350 AL4=0.0D0 MINOB360 DO 4 I=1, N MIN08370

Ð

Ð

| | AL1=AL1+(-TAUB)**I*I/((TAU-TAUB)**(I+1)) | MIN08380 |
|-----|-------------------------------------------------------------------|-------------|
| 4 | CONTINUE | MIN08390 |
| | AL3=AL3+1.0*((-A1)-1.0D0)/TAU | MIN08400 |
| | AL4=AL4+1.0D0/TAU*((-A1-1.0D0)-TAU*(-A1)/(TAU-TAUB)) | MIN08410 |
| | DO 5 I=2,N | MIN08420 |
| | DO 6 IR1=1, I-1 | MINO8430 |
| | IR=IR1-1 | MINO8440 |
| | CALL FACT(I-IR-1, IRR) | MINO8450 |
| | IF(IRR.LE.0)GO TO 200 | MIN08460 |
| | AL3=AL3+1.00/TAU**(I+1)*I*(TAU)**(IR+1)*TIME**(I-IR-1)/IRR*(-1+(- | -AMIN08470 |
| | 11)**(IR+1)) | MIN08480 |
| | AL4=AL4+1.0/TAU**I*TIME**(I-IR-1)/IRR*((IR+1)*TAU**IR*(-1+(-A1)* | * (MIN08490 |
| | 1IR+1))-(TAU**(IR+1)*((IR+1)*(-A1)**(IR+1)/(TAU-TAUB)))) | MIN08500 |
| 6 | CONTINUE | MIN08510 |
| | AL3=AL3+I/TAU*((-A1)**I-1.0D0) | MIN08520 |
| | AL4=AL4+I/TAU*((-A1)**I-1.0D0-TAU*(-A1)**I/(TAU-TAUB)) | MIN08530 |
| 5 | CONTINUE | MIN08540 |
| | IF(T1.LT.75.D0.AND.T2.LT.75.D0)GO TO 22 | MIN08550 |
| | DELTAU=0.0D0 | MIN08560 |
| | IF (T1.LT.75.D0) DELTAU=DEXP (-T1) /N* (TIME/TAU**2*AL2-AL3+AL4) | MIN08570 |
| | IF(T2.LT.75.D0)DELTAU=AL1/N*DEXP(-TIME/TAUB) | MIN08580 |
| | GO TO 23 | MIN08590 |
| 22 | DELTAU=AL1/N*DEXP(-TIME/TAUB)+DEXP(-TIME/TAU)/N*(TIME/TAU**2*AL2 | -AMIN08600 |
| | 1L3+AL4) | MIN08610 |
| С | WRITE(6,*)'TIME',TIME,'DELTAU',DELTAU,X(1),X(2) | MIN08620 |
| 2.3 | AM2=0.0 | MIN08630 |
| | AM3=0.0 | MINO8640 |
| | DO 7 I=1,N | MIN08650 |
| 7 | AM2=AM2+(-1)**(I+1)*I*TAU*TAUB**(I-1)/(TAU-TAUB)**(I+1) | MIN08660 |
| | AM3=AM3-TAU/(TAU-TAUB) **2 | MIN08670 |
| | DO 8 I=2, N | MIN08680 |
| • | DO 9 IR1=1, I-1 | MIN08690 |
| | IR=IR1-1 | MIN08700 |
| | AM3=AM3-1./TAU**I*(TAU**(IR+2)*TIME**(I-IR-1)*(IR+1)*(-TAUB)**IR | /IMIN08710 |
| | 1RR/(TAU-TAUB)**(IR+2)) | MIN08720 |
| 9 | CONTINUE | MIN08730 |
| | AM3=AM3-TAU*I*(-A1)**(I-1)/(TAU-TAUB)**2 | MIN08740 |
| 8 | CONTINUE | MIN08750 |
| | IF(T1.LT.75.D0.AND.T2.LT.75.D0)GO TO 24 | MIN08760 |
| | DELTAUB=0.0D0 | MINO8770 |
| | IF(T2.LT.75.D0)DELTAUB=EXP(-T2)/N*(TIME/TAUB**2*AK1+AM2) | MIN08780 |
| | IF(T1.LT.75.D0)DELTAUB=AM3/N*DEXP(-T1) | MIN08790 |
| | RETURN | MIN08800 |
| 24 | DELTAUB=EXP(-TIME/TAUB)/N*(TIME/TAUB**2*AK1+AM2)+EXP(-TIME/TAU)/ | N*MIN08810 |
| | 1AM3 | MIN08820 |
| | RETURN | MIN08830 |
| 200 | WRITE(6,201) | MIN08840 |
| 201 | FORMAT(1X, 'FACTORIAL RETURNED NEGATIVE') | MIN08850 |
| | END | MIN08860 |
| | | MIN08870 |
| | | MIN08880 |
| | | |

-

-

· _

-

ŝ

Ċ

¥Э

ì



Autor pr

•

.

LAWRENCE BERKELEY LABORATORY UNIVERSITY OF CALIFORNIA TECHNICAL INFORMATION DEPARTMENT BERKELEY, CALIFORNIA 94720