UC San Diego International Symposium on Stratified Flows

Title

Ageostrophic instability and mixing in a dense overflow

Permalink

<https://escholarship.org/uc/item/4z52f26k>

Journal

International Symposium on Stratified Flows, 8(1)

Authors

Pratt, Larry Llewellyn Smith, Stefan Helfrich, Karl

Publication Date

2016-08-29

Ageostrophic Instability and Mixing in a Dense Overflow

Larry Pratt¹, Presenting Author and Stefan G. Llewellyn Smith² and Karl Helfrich¹

¹ Woods Hole Oceanographic Institution, Woods Hole, MA 02543, lpratt@whoi.edu and khelfrich@whoi.edu

2 Dept. of Mechanical and Aerospace Engineering, UCSD, 9500 Gillman Dr., La Jolla, 92093-0411, sgls@ucsd.edu

Abstract

We will discuss a number of aspects of ageostrophic instability in two-layer systems, with specific applications to deep channel flows such as that of the Denmark Strait. The work touches on the extension to two layers of Ripa's Theorem, including a geometric interpretation, linear stability analysis and finite amplitude simulations using a numerical model. Among other things, we attempt to explain the $2-4$ day oscillations detected in the approach flow to the Denmark Strait sill.

1. Introduction

The Griffiths-Killworth-Stern instability (Griffiths, et. al. 1982) acts in a 1.5-layer layer system in which the thickness of the active layer vanishes at the edges. The instability, which was explored in the context of an eddy or gyre, can be attributed to resonance between different edge modes arising on the frontal boundaries (Paldor, 1983). Pratt et al. (2008) hereafter PHL, and Simeonov and Stern (2008) examined a similar linear instability in a parallel flow confined to a parabolic channel, where the topography potentially has a stabilizing influence. The growing modes are particularly intriguing in that they have zero wave energy and therefore do not formally extract energy from the background flow, a possibility first point out by Hayashi and Young (1987). Although such instabilities alter the mean flow, they cannot easily be classified as barotropic or baroclinic.

The parabolic-channel configuration is often used to explore the rotating hydraulics of deep overflows (Borenäs and Lundberg, 1986 and 1988 and Pratt and Whitehead, 2006). PHL also considered the finite amplitude growth of the unstable edge waves, using a numerical model to track growth and equilibration. Some success in predicting the equilibrated states was enabled by reference to Ripa's Theorem (Ripa, 1983), a sufficient condition for ageostrophic stability that involves conditions on both the potential vorticity gradient and the layer Froude number, thus combining elements of classical quasigeographic instability theory with hydraulics. To make a connection with deep overflows PHL also considered channels that begin in a deep, broad basin and narrow to a sill section where the active layer spills (Figure 1).

Figure 1: From numerical simulation by Pratt et al. (2008) showing finite amplitude state achieved as the result of unstable growth of instabilities in a single-layer, ageostrophic flow in a deep channel with a parabolic cross section. The contours represent the elevation of the interface. The mean flow is from left to right and the channel contains a sill at $y=0$. To the right of the sill, the dense layer spills and becomes banked on the right side (facing downstream) of the channel.

2. Results

Among the climate-relevant deep ocean overflows, that of the Denmark Strait is particularly complex because of its extreme variability on short time scales, even well upstream of the sill (Harden, et al. 2016). It is further complicated by a strong barotropic component, introduced by the influence of the East Greenland Current. This factor makes it difficult to apply the 1.5-layer results mentioned above. For one thing, it is nearly impossible to configure such a model so that it looks anything like the mean flow in the Denmark Strait, as documented by Harden et al. (2016). For this reason we have extended our analysis to include two-active layers, still in a channel with a parabolic cross-section. This extension is nontrivial since the central part of the channel is covered by both layers, while the outside flange regions are covered only by the upper layer. In addition, the upper layer may now contain a potential vorticity gradient, a factor that enlarges the zoological range of possible unstable modes. Ripa's theorem can be extended, but the required bounds are more difficult to derive.

Our presentation will include a discussion of the linear stability problem, growth rates, conditions for the dominance of zero-energy waves, and the derivation, implications and geometric interpretation of Ripa's Theorem in two layers. We will also show numerical simulations (an example of which appears in Figure 2) in both strait channels and channels with sills and width contractions. We will discuss the possible use of Ripa's Theorem to predict equilibrated states. We will also compare findings with recent observations of time-variability (Harden et al., 2016) in the Denmark Strait.

Figure 2: Plan view showing lower layer thickness during the development of an instability in a parabolic channel. The channel is aligned in the x-direction.

Acknowledgements

Partial funding for Pratt and Llewellyn Smith was provided under DOD (MURI) grant N000141110087, administered by the Office of Naval Research

References

Borenäs, K. M. and P. A. Lundberg, 1986. Rotating hydraulics of flow in a parabolic channel*. J. Fluid Mech*. **167**, 309-26.

Borenäs, K. M. and P. A. Lundberg 1988. On the deep-water flow through the Faroe Bank Channel*. J. Geophys. Res*. **93**(C2), 1281-92.

Harden, B. E., R. S. Pickart, H. Valdimarsson, K. Vage, L. de Steur, C. Richards, F. Bahr, D. Torres, E. Borve, S. Jonsson, A. Macrander, S. Osterhus, L. Havik and T. Hattermann 2016. Upstream sources of the Denmark Strait Overflow: Observations from a high-resolution mooring array. *Deep-Sea Res. I*, **112**, 94-96.

Hayashi, Y.-Y. and W. R. Young 1987. Stable and unstable shear modes of rotating parallel flows in shallow water. *J. Fluid Mech.* **184**, 477-504.

Paldor, N. 1983 Stability and Stable Modes of Coastal Fronts. *Geophys. Astrophys. Fluid Dyn.* **27**, 217-218.

Pratt, L. J. and J. A. Whitehead 2008. *Rotating Hydraulics*. Springer, New York. 589 pp.

Pratt, L. J., K. R. Helfrich, and D. Leen, 2008. On the stability of deep overflows. *J. Fluid Mech.*, **602**, 241-266.

Ripa, P. 1983. General stability conditions for zonal flows in a one layer model on a betaplane or the sphere. *J. Fluid Mech.* **126**, 463-487.