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Department of Statistics Papers

Title

Show Me the Missing Data

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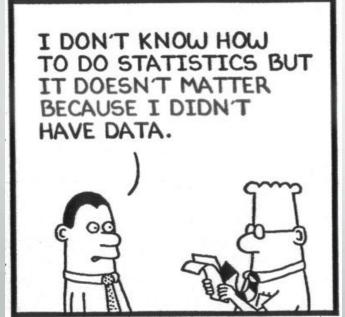
Author

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Publication Date

2017-05-19

Show Me the Missing Data Juana Sanchez (with Dennis Li) UCLA, Department of Statistics (USCOTS 2017, BOS 2H, 5/19/2017)



USCOTS 2017 Breakout Session 2H

Juana Sanchez (UCLA) 5/19/2017

"Well, this certainly explains much company's missing data. Who else the 'DEL' key on their computer was for work?"

Source: https://ducttapefordata.com/category/analysis/

Source: https://www.cartoonstock.com/directory/d/de

u teach intro stats classes for undergraduates students that never took statistics before?

ice in a while, not every year, in college

Every year, college

Never, college

e in a while, not every year, high school

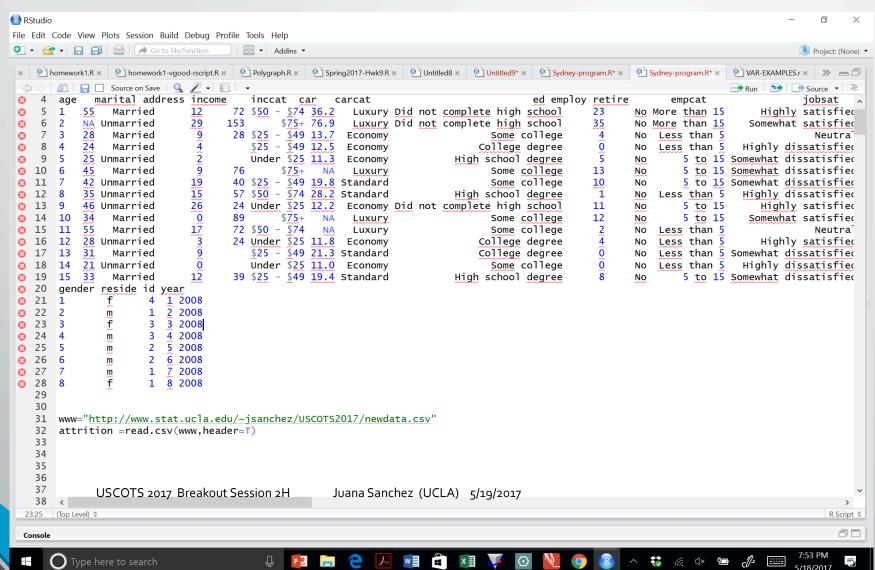
Never, high school

Every year, high school

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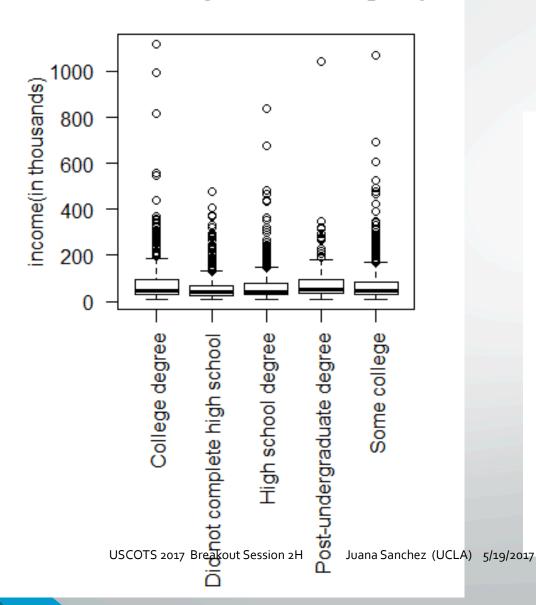
We indulge in data since the first lectures and labs in an intro stats class, e.g., n=3165 and 15 variables



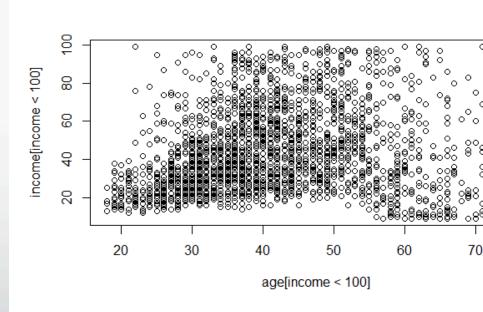
In a decent Stats class we may use that data to achieve, for example, the third of the following learning objectives:

Box Plots Grade A 17/10/2015 Learning Objectives: Know what the quartiles are and able to calculate them Able to draw a box plot Able to interpret a box plot, including the interquartile range

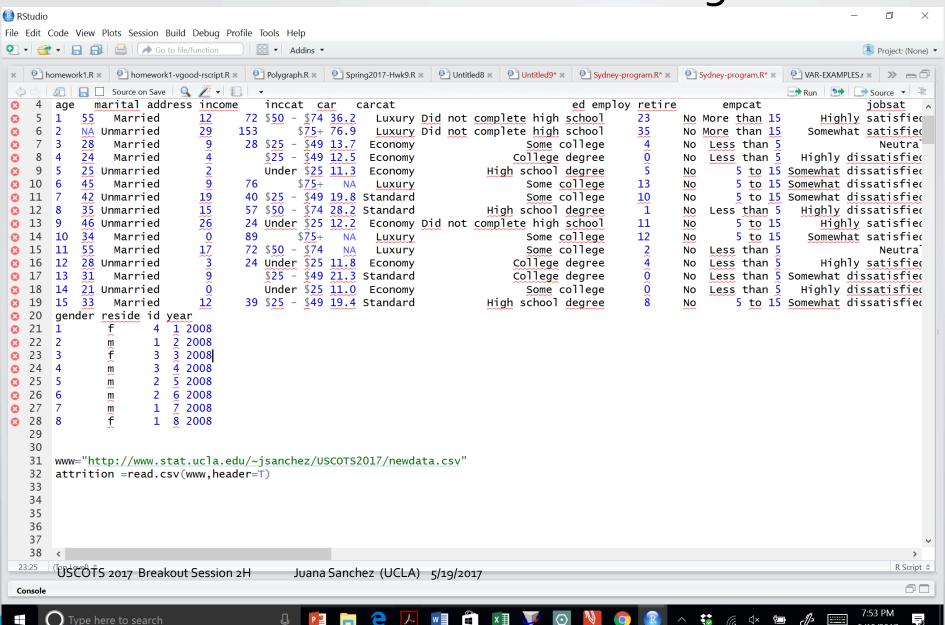
Income by educational group



And we get more multivariate later, using the same data.



What do we do with the missing data?



How do you approach missing data in your intro stats class?

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Why do these things get forgotten so quickly after the intro stats course?



Our students come to our classes with mental model prior knowledge, beliefs and categorizations that mainterfere with the transition from novice to experts it statistics.

Transformed courses have:

- Pre-lecture assignments
- Just-in-time teaching (clickers, in-class polls)
- Socially mediated, collaborative learning, think-pair-share, dialogue.
- In-class tutorials that engage students in coversations between themselves and with the teacher.
- Emphasis on the process by which students learn.

Transform to engage studer

- Cognitively and emotionally
 - In knowledge construction, via
 - Critical thinking skills ,
 - Long term memory retention,
 - conceptual change., awareness of contradiction
 - Thinking like scientists
 - Talking about what they think.

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What about a more investigative rown What can the data tell us about missing da

Hands on acti

Think-pair-share (5 mir

the margin plots from VIM package in R telling us about the missir of income, age, and car value (car)?

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What can the data tell us about to missing da

Hands on acti

Think-pair-share (5 mir

Missing Data Techniques: Mechanisms and Methods

Juana Sanchez

Dennis Li

UCLA, Department of Statistics

Missing Data Mechanisms

Mechanisms describe the assumptions about the nature of the missing data and can be categorized as follows:

- MCAR (Missing Completely at Random)
- 2. MAR (Missing at Random)
- 3. NMAR (Not Missing at Random)

MCAR (Missing Completely at Random)

- Probability of missing values has nothing to do with the observed or missir values
- Example: someone flips a coin to determine if they will fill out a survey, or a researcher is unable to gather data for a day due to an assay failure

MAR (Missing at Random)

- Probability of missing values depends only on the observed values in the dataset (not the missing variable itself)
- Example: women may be more likely to answer or decline to answer certain questions than men. Older subjects may be more likely to drop out of a study (Gender and age are observed here)

NMAR (Not Missing at Random)

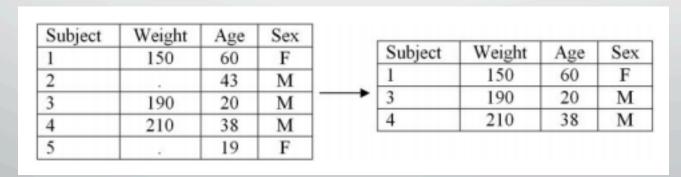
- Probability of missing values depends on the missing values themselves, and can also depend on observed values too
- Example: a study that measures weight has 2 rounds, and people don't should be second round because they've gained weight and believe the studies isn't helping them (missing weight data is due to weight itself)

Some Methods to Handle Missing Data

- Complete Case (CC) Analysis
- Inverse Probability Weighting (IPW)
- 3. Last Observation Carried Forward (LOCF) Imputation
- 4. Unconditional Mean Imputation
- 5. Single/Deterministic/Regression Imputation
- 6. Stochastic Imputation
- 7. Multiple Imputation

Complete Case Analysis (CC)

- Default method in statistical software packages such as R, Stata, SAS
- Delete whole row which contains missing data on any variable
- Advantages: easiest, default, unbiased with MCAR
- Disadvantages: loss of valuable data, mostly biased (MCAR is rarest)



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Inverse Probability Weighting (IPW)

- Look for similarities between subjects who are missing the outcome of interest vs those who are not
- Find pairings where similarities exist, and calculate the probability of missing the outcome of interest based on pairings
- Assumes MAR data (allows calculation to be based on observed info)
- Advantages: results are unbiased under MAR and MCAR
- Disadvantages: reduced sample size, skewed if small predicted probability of complete data

Example of IPW

Table 1. Data used to explain IPW.									
Subject	Age	Sex	Year in College						
1		F	Graduated						
2		F	Junior						
3	20	M	Junior						
4	24	F	Graduated						
5	21	F	Senior						
6	19	F	Junior						

Estimated Mean Age =
$$\frac{1}{6}$$
 (Subject3' sage + 2 * Subject4' sage + Subject5' sage + 2 * Subject6' sage)
$$= \frac{1}{6} \left(\frac{Y_{\text{Subject3}}}{1} + \frac{Y_{\text{Subject4}}}{\frac{1}{2}} + \frac{Y_{\text{Subject5}}}{1} + \frac{Y_{\text{Subject6}}}{\frac{1}{2}} \right)$$
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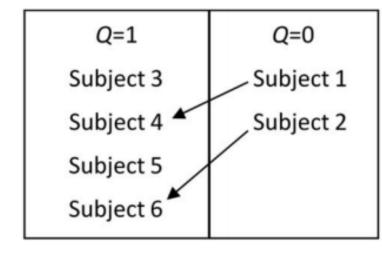


Figure 2. Grouping subjects based on having complete or missing data.

Megan M. Marron & Abdus S. Wahed (2016) Teaching Missing Data Undergraduates Using a Group-Based Project Within a Six-Week S Journal of Statistics Education, 24:1, 8-15

Last Observed Carried Forward (LOCF) Imputation

- Plug in last available measurement in place of the missing values
- Advantages: very simple
- Disadvantages: decreased sample variance (replacement with identical values)
- It is the least preferred method because of large bias

Subject	Age	Cau	Week			Subject	Age	Sex	Week			
		Sex	1	2	3		Subject	Age	Sex	1	2	3
1	60	F	20.1	20.9			1	60	F	20.1	20.9	20.9
2	43	M	13.7		15.3	_	2	43	M	13.7	13.7	15.3
3	20	M	18.0	19.1	20.2		3	20	M	18.0	19.1	20.2
4	38	M	19.3	20.0			4	38	M	19.3	20.0	20.0

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Unconditional Mean Imputation

- Method is to replace missing values with the mean of the available values
- Advantages: easy to implement
- Disadvantages: leads to a reduction in variability because you are imputin based on the mean. It also changes the correlation between the imputed variable vs. other variables.

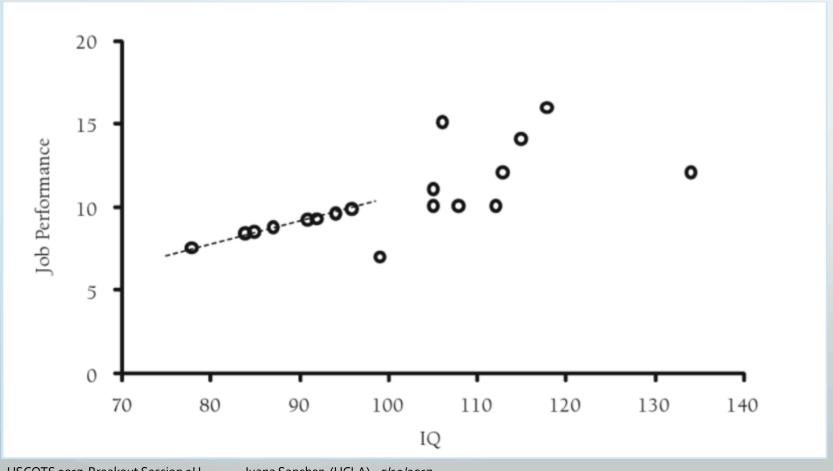
*since mean imputation is based on the values of that variable itself, there is no relationship between the imputed variable and other observed variables

Single/Deterministic/Regression Imputation

- also known as regression/conditional mean imputation: where missing values are imputed with predicted values from a regression equation
- Advantages: usage of complete information to impute
- Disadvantages: imputed values are directly from the regression line, decreasing variability. Also inflates correlations because it is using values that are already perfectly correlated with one another to impute. There is no residual variance because the imputed points fit perfectly onto the regression line. It does not refle the full uncertainty of the missing data.

*impute observed values of a variable based on values of other variables

Example of Regression Imputation



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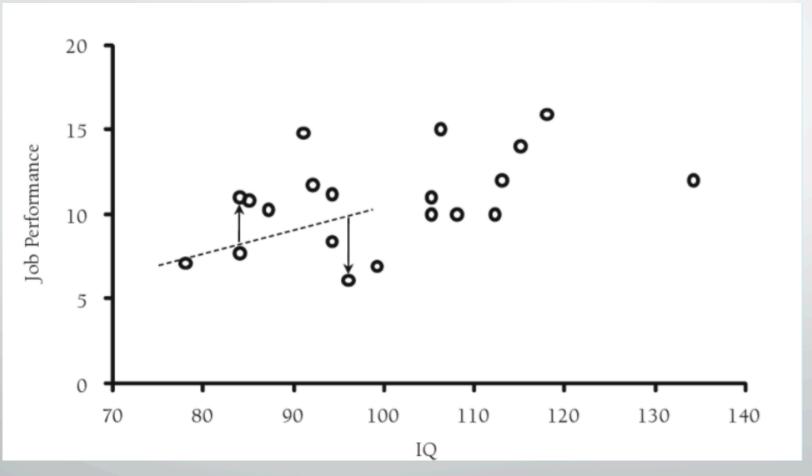
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Megan M. Marron & Abdus S. Wahed (2016) Teaching M Methodology to Undergraduates Using a Group-Based F Six-Week Summer Program, Journal of Statistics Educat

Stochastic Imputation

- Addresses problems with regression imputation (lost variability) with the attempt to add back this lost variability
- Done by adding randomly drawn residuals from regression imputation, based on residual variance from regression model
- Advantages: "adds back" lost variability from regression imputation and produce unbiased correlation estimates under MAR
- Disadvantages: standard errors are less biased than in regression imputation but still weakened

Example of Stochastic Imputation



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Megan M. Marron & Abdus S. Wahed (2016) Teaching Mis Methodology to Undergraduates Using a Group-Based Pi Week Summer Program, Journal of Statistics Education,

Multiple Imputation

- Obtain several estimates of the missing value using draws from the multivariate distribution of all variables.
- Or, at an intro level, obtain several estimates of the missing value using regression of the variable on all other variables.
- Either way, take the average of all the estimates.

Mean Imputation Example w/R code

- Convert Stata file of missing data into R
- 2. Perform mean imputation on the missing values dataset (becomes new dataset
- Compare correlation tables of the missing values dataset and the imputed dataset
- 4. Compare summary statistics of the missing values dataset and the imputed dataset and observe the variability
- 5. Perform linear regression and observe differences

Set-up

Use the haven package to convert the Stata file into R.

```
#convert hsb2.dta and hsb2_mar.dta from Stata to R. Replicate missing dataset so we can impute.
fullData <- read_dta("~/Downloads/hsb2.dta")
View(fullData)
missingData <- read_dta("~/Downloads/hsb2_mar.dta")
View(missingData)
meanImputedData <- missingData
View(meanImputedData)</pre>
```

Preview of the full dataset:

	id	female	race	\$es \$	schtyp type of school	prog [‡] type of program	read [‡] reading score	write [‡] writing score	math \$\pi\$ math score	science core	socst $^{\scriptsize \scriptsize $
1	70	male	white	low	public	general	57	52	41	47	57
2	121	female	white	middle	public	vocation	68	59	53	63	61
3	86	male	white	high	public	general	44	33	54	58	31
4	141	male	white	high	public	vocation	63	44	47	53	56
5	172	male	white	middle	public	academic	47	52	57	53	61
6	113	male	white	middle	public	academic	44	52	51	63	61
7	50 U:	male SCOTS 201	african-amer 17 Breakout Ses		public Juana Sanc	<mark>general</mark> hez (UCLA) 5/19/	2017	59	42	53	61

Set-up (continued)

Preview of the missing values dataset:

	id [‡]	female ‡	race	ses [‡]	schtyp type of school	prog [‡] type of program	read † reading score	write writing score	math \$\pi\$ math score	science score	socst \$\phi\$ social studies score
1	116	female	white	middle	public	NA	57	59	54	50	56
2	170	male	white	high	public	NA	47	62	61	69	66
3	97	male	white	high	public	NA	60	54	58	58	61
4	104	male	white	high	public	NA	54	63	57	55	46
5	121	female	white	middle	public	NA	68	59	53	63	61
6	94	male	white	high	public	NA	55	49	61	NA	56
7	65	female	white	middle	public	NA	55	NA	66	42	56

Preview of the imputed dataset:

	id	female	race [‡]	\$es \$	schtyp type of school	prog \$ type of program	read [‡] reading score	write [‡] writing score	math † math score	science science score	socst \$\phi\$ social studies score
1	116	female	white	middle	public	academic	57.00000	59.00000	54.0000	50.00000	56
2	170	male	white	high	public	general	47.00000	62.00000	61.0000	69.00000	66
3	97	male	white	high	public	academic	60.00000	54.00000	58.0000	58.00000	61
4	104	male	white	high	public	vocation	54.00000	63.00000	57.0000	55.00000	46
5	121	female	white	middle	public	general	68.00000	59.00000	53.0000	63.00000	61
6	94	male	white	high	public	academic	55.00000	49.00000	61.0000	51.30978	56
7	JSCOT	S 2017 Br	eakout Session white	2H middle	Juana Sanchez public	(UCLA) 5/19/201	7 55.00000	52.95082	66.0000	42.00000	56

Perform Mean Imputation

- For each column (variable), use a for loop and iterate through each observation. If an observation matches as missing (NA), we set it equal to the mean of the whole column.
- Example:

```
#for read variable
for(i in meanImputedData$id){
   if(is.na(meanImputedData[i,7]) == TRUE){
      meanImputedData[i,7] = mean(meanImputedData$read, na.rm = TRUE)
   }
}
#for math variable
for(i in meanImputedData$id){
   if(is.na(meanImputedData[i,9]) == TRUE){
      meanImputedData[i,9] = mean(meanImputedData$math, na.rm = TRUE)
   }
}
```

Repeat for each variable with missing values

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Analyze Correlation Tables

 Using the cor() function and selecting the columns that we want to analyze, we compare the correlation tables for the missing values dataset and the imputed dataset. We can observe altered correlation

Correlation table for full dataset:

Correlation table for missing values dat

	read	write	math	science	socst		read	write	math	science
read	1.0000000	0.5967765	0.6622801	0.6301579	0.6214843	read	1.0000000	0.5807117	0.6478505	0.6232614 (
write	0.5967765	1.0000000	0.6174493	0.5704416	0.6047932	write	0.5807117	1.0000000	0.6175467	0.5734457 (
math	0.6622801	0.6174493	1.0000000	0.6307332	0.5444803	math	0.6478505	0.6175467	1.0000000	0.6409446 (
science	0.6301579	0.5704416	0.6307332	1.0000000	0.4651060	science	0.6232614	0.5734457	0.6409446	1.00000000
socst	0.6214843	0.6047932	0.5444803	0.4651060	1.0000000	socst	0.5740294	0.5744264	0.5200243	0.4218290

Correlation table for the imputed dataset:

```
read write math science socst read 1.0000000 0.5480112 0.6158825 0.6076032 0.6028521 write 0.5480112 1.0000000 0.5491474 0.4955650 0.5707113 math 0.6158825 0.5491474 1.0000000 0.5576771 0.5106852 science 0.6076032 0.4955650 0.5576771 1.0000000 0.4306481 USCOTS 2017 Breakout Sessist2H 0.602865231ch0x, 50707113/39/8015106852 0.4306481 1.0000000
```

Summary Statistics for Mean Imputation

Here, we compare the summary statistics with a focus on mean and standard deviation

		For full	dataset:			For missing values dataset:					
	read	write	math	science	socst		read	write	math	science	
mean	52.23000	52.775000	52.645000	51.850000	52.40500	mean	52.28796	52.950820	52.897297	51.309783	
sd	10.25294	9.478586	9.368448	9.900891	10.73579	sd	10.21072	9.257773	9.360837	9.817833	
min	28.00000	31.000000	33.000000	26.000000	26.00000	min	28.00000	31.000000	33.000000	26.000000	
max	76.00000	67.000000	75.000000	74.000000	71.00000	max	76.00000	67.000000	75.000000	74.000000	

For mean imputed data:

```
read write math science socst
mean 52.28796 52.950820 52.89730 51.309783 52.40500
sd 9.97715 8.853514 9.00113 9.414877 10.73579
min 28.00000 31.000000 33.00000 26.000000 26.000000
max 76.00000 67.000000 75.00000 74.000000 71.00000
```

Question: What do we notice about the summary statistics for the mean imputed data when conto the other datasets? Specifically the standard deviation?

Summary Statistics for Mean Imputation

Here, we compare the summary statistics with a focus on mean and standard deviation

		For full	dataset:			For missing values dataset:					
	read	write	math	science	socst		read	write	math	science	
mean	52.23000	52.775000	52.645000	51.850000	52.40500	mean	52.28796	52.950820	52.897297	51.309783	
sd	10.25294	9.478586	9.368448	9.900891	10.73579	sd	10.21072	9.257773	9.360837	9.817833	
min	28.00000	31.000000	33.000000	26.000000	26.00000	min	28.00000	31.000000	33.000000	26.000000	
max	76.00000	67.000000	75.000000	74.000000	71.00000	max	76.00000	67.000000	75.000000	74.000000	

For mean imputed data:

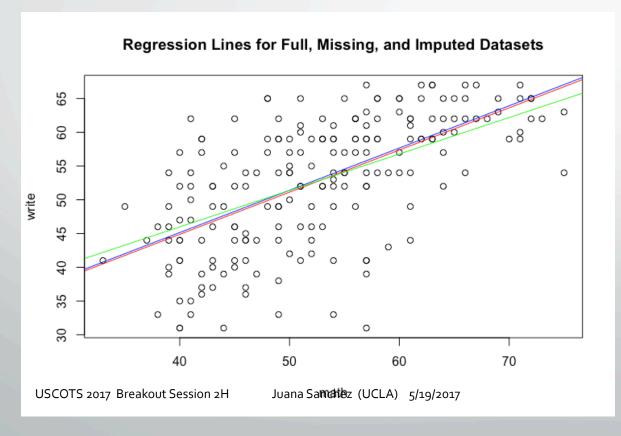
```
read write math science socst
mean 52.28796 52.950820 52.89730 51.309783 52.40500
sd 9.97715 8.853514 9.00113 9.414877 10.73579
min 28.00000 31.000000 33.00000 26.000000 26.00000
max 76.00000 67.000000 75.00000 74.000000 71.00000
```

Answer: We see that the mean stays the same because we imputed based on the mean of the o values. More interestingly, we see that the standard deviation is less for each variable in the important the important of the distribution, decreasing the variability.

Linear Regression for Mean Imputation

- Perform bivariate regression analysis using the lm() and summary() functions

Graph of the relationship between math and write (dependent) with regression lines for all 3 datasets



Full data= RED
Missing values data = BLUE
Mean Imputed values data =

Regression Results for Imputation Methods

	Full Data	CCA	Mean Imputation	Mean Imputation w/ Cat.	Multiple Imputation
Intercept	9.62**	13.03**	13.94***	9.11*	10.11**
write	0.37***	0.44***	0.38***	0.33***	0.38***
math	0.44***	0.32***	0.34***	0.46***	0.42***
female	-2.70*	-2.71*	-2.17(.)	-0.59	-2.67*
prog general	0.23	0.52	1.72	1.51	0.63
prog academic	1.88	1.81	2.95(.)	2.35(.)	2.42
R-squared	0.5045	0.4679	0.4257	0.4449	0.5147
# of missing observations	0	70	35	0	0

Standard Deviations/Means/Proportions for Imputation Meth

				<u> </u>	
	Full Data	CCA	Mean Imputation	Mean Imputation w/ Cat.	Multiple Imputar
	mean: 52.23	mean: 52.288	mean: 52.288	mean: 52.288	mean:
read	sd: 10.253	sd: 10.211	sd: 9.977	sd: 9.977	sd:
	mean: 52.775	mean: 52.951	mean: 52.951	mean: 52.951	mean:
write	sd: 9.479	sd: 9.258	sd: 8.854	sd: 8.854	sd:
	mean: 52.645	mean: 52.897	mean: 52.897	mean: 52.897	mean:
math	sd: 9.368	sd: 9.361	sd: 9.001	sd: 9.001	sd:
	mean: 51.85	mean: 51.310	mean: 51.310	mean: 51.310	mean:
science	sd: 9.901	sd: 9.818	sd: 9.415	sd: 9.415	sd:
	male: 91/200 = 0.455	male: 81/182 = 0.445	male: 81/182 = 0.445	male: 91/200 = 0.455	male:
female	female: 109/200 = 0.545	female: 101/182 = 0.555	female: 101/182 = 0.555	female: 109/200 = 0.545	female:
	vocation: 50/200 = 0.25	vocation: 46/182 = 0.253	vocation: 46/182 = 0.253	vocation: 50/200 = 0.25	vocation:
	general: 45/200 = 0.225	general: 41/182 = 0.225	general: 41/182 = 0.225	general: 42/200 = 0.21	general:
prog	academic: 105/200 = 0.525	academic: 95/182 = 0.522	academic: 95/182 = 0.522	academic: 108/200 = 0.54	academic:
# of missing observations	0	70	35	0	0

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*Notice again how the standard deviations for the variables in the mean imputed dataset are

Standard Errors of Coefficients

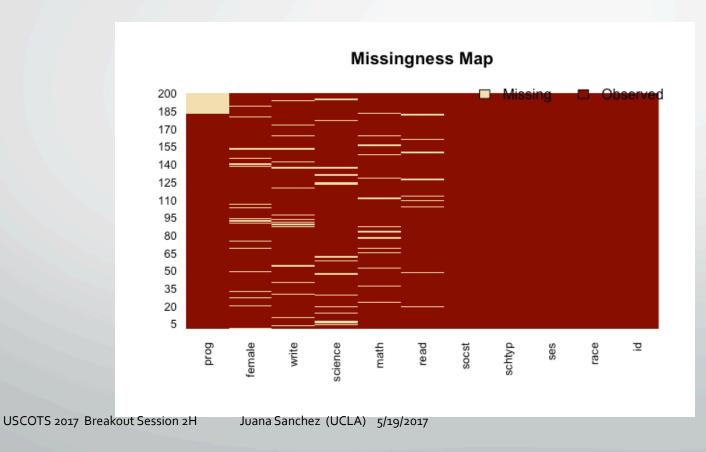
	Full Data	CCA	Mean Imputation	Mean Imputation w/ Cat.	Multiple Imputati
Intercept	3.40980	4.12355	3.94658	3.78154	3.49099
write	0.07463	0.09265	0.08193	0.07492	0.08237
math	0.07500	0.09514	0.07986	0.07503	0.08270
female	1.09541	1.36519	1.18717	1.10094	1.23014
prog general	1.51219	1.88083	1.66568	1.53230	1.62628
prog academic	1.42307	1.65486	1.50343	1.41087	1.52243

Visualization in R

- Packages that can be used to visualize the missing data through plots include VIM and Amelia
- VIM
 - spineMiss
 - aggr
 - matrixplot
 - marginplot
- Amelia
 - missmap

missmap

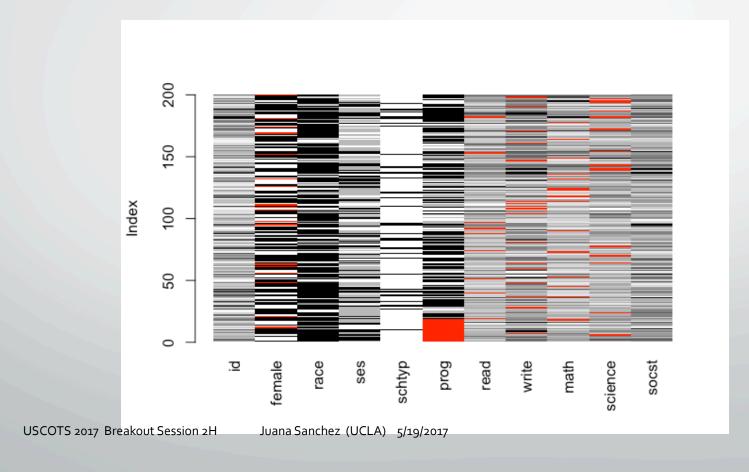
missmap \rightarrow creates a simple plot showing where the missing data occurs in the dataset. Can be used to observe patterns



matrixplot

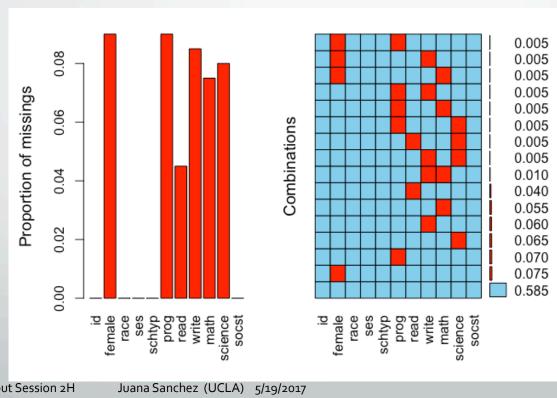
matrixplot

 available data is coded according to a continuous color scheme, while missi
 data is visualized with a distinguishable color (red)



aggr

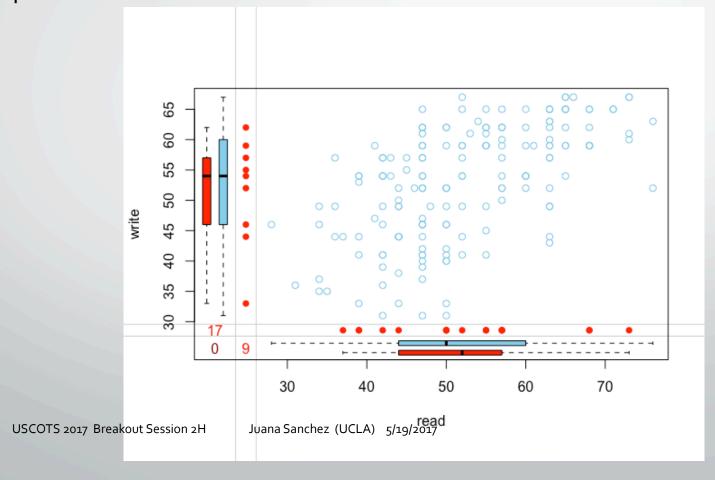
 aggr → shows patterns of missingness through a combinations graph, with red representing missing data. For example, 0.585 of the observations are not missing any and 0.075 are missing just female.



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marginplot

marginplot → enhanced scatterplot which also shows boxplots for each variable, observand imputed





"Well, no, I don't see any patterns in this data, but I did see Elvis in my oatmeal this morning!"

Multiple Imputation in Cancer Research

- Citation: Royston P (2004). "Multiple Imputation of Missing Values." The Stata Journal, 4, 227—241.
- Dataset: http://www.stata-press.com/data/r13/brcancer.dta
- Research Interest: Recurrence-free survival time (duration in years from entry into study t time of death or disease recurrence)
- Total observations: 686
- Author created a new dataset from brcancer.dta (full) called brcaex.dta with missing valu
 (20% of observations were completely at random missing)
- Standard errors were larger with imputed data, and parameter estimates are similar

Multiple Imputation in Sociology Research

- Citation: Finke R, Adamczyk A (2008). "Cross-National Moral Beliefs: The Influence of National Religious Context." Sociological Quarterly, 49(4), 617–652.
- Dataset: One from ISSP (https://dbk.gesis.org/dbksearch/sdesc2.asp?no=3190) and one from WVS (can't access)
- Research Interest: How does religion relate to morality on a micro to macro level? (state vs. national)
- For the ISSP dataset, there were 39034 observations with 35356 after excluding ones with missing info on key variables
- "Approximately twenty percent of respondents in each dataset were missing information on variables needed in the analysis. In a preliminary analysis we ran all models with listwise deleted data, pairwise deleted data, and multiply imputed data, and found that our results were minimally affected by these different techniques for handling missing da Since multiple imputation takes full advantage of the available data and avoids some of the bias in standard errors and test statistics that can accompany pairwise deletion, we chose to present our results using multiple imputation"

Multiple Imputation in Occupational Health

- Citation: Chamberlain LJ, Crowley M, Tope D, Hodson R (2008). "Sexual Harassment in Organizational Context." Work and Occupations, 35(3), 262–295.
- Dataset: available on http://www.icpsr.umich.edu/icpsrweb/ICPSR/studies/3979
- 204 observations; 51 with missing variables
- Research Interest: How does workplace dignity affect employee work behaviors and organizational performance?
- Did not explicitly state how results changed after MICE

Multiple Imputation in Obesity/Physical Activity Research

- Citation: Wiles NJ, Jones GT, Haase AM, Lawlor DA, Macfarlane GJ, Lewis G (2008). "Physical Activity and Emotional Problems Amongst Adolescents." Social Psychiatry and Psychiatric Epidemiology, 43(10), 765–772.
- Dataset: ?
- Research Interest: Relationship between physical activity and emotional problems in children aged 11-14 in England
- Total observations: 1424 children, with 206 missing at 1 year follow-up
- "Imputing missing data using MICE suggested that those imputed were more likely to have higher scores at follow-up. Sensitivity analyses including imputed data were consistent with the results of the complete-case analyses suggesting that missing data had not biased the results?

Multiple Imputation in Behavior Research

- Citation: Melhem NM, Brent DA, Ziegler M, Iyengar S, Kolko D, Oquendo M, Birmaher B, Burke A, Zelazno Stanley B, Mann, J J (2007). "Familial Pathways to Early-Onset Suicidal Behavior: Familial and Individual Antecedents of Suicidal Behavior." American Journal of Psychiatry, 164(9), 1364–1370.
- Dataset: ?
- Research Interest: identify clinical predictors of new-onset suicidal behavior in children of parents with a history of mood disorder and suicidal behavior
- 17% of the sample had no missing data for any variable, 31% had missing data for one or two variables, 43 had missing data for three or four variables, and 9% had missing data for more than four variables
- Results?

Multiple Imputation in Health Economics Research

- Citation: Burton A, Billingham LJ, Bryan S (2007). "Cost-Effectiveness in Clinical Trials: Using Multiple Imputation to Deal with Incomplete Cost Data." Clinical Trials, 4(2), 154–161.
- Dataset: ?
- Research Interest: The objective of this article is to investigate the appropriateness and practicalities of using MI to handle missing cost component data as an alternative to the standard complete case analysis, when one of the aims of the trial is to assess cost effectivene
- 115 observations, 82 with complete data
- The complete case analysis resulted in a higher mean cost for those patients randomized to M
 + PC of £2804 (95% CI £1236 to £4290) compared to PC. When MI was used, a smaller differen
 between treatments in terms of the mean cost of £2384 was seen (95% CI £833 to £3954).

Summary

- There are several imputation methods to replace missing data with substituted data, as well as several mechanisms that govern which imputation methods we should use
- We investigated CCA (complete case analysis), mean imputation, and multiple imputation in depth and how each method affected results
- We can visualize missing data using packages in R that produce visually appealing plots and graphs

Citations

- Megan M. Marron & Abdus S. Wahed (2016) Teaching Missing Data Methodology to Undergraduates Using a Group-Based Project Within a Six-Week Summer Program, Journal of Statistics Education, 24:1, 8-15
- http://www.ats.ucla.edu/stat/stata/seminars/missing_data/Multiple_imputation/mi_in_stata_pt1_new.htm