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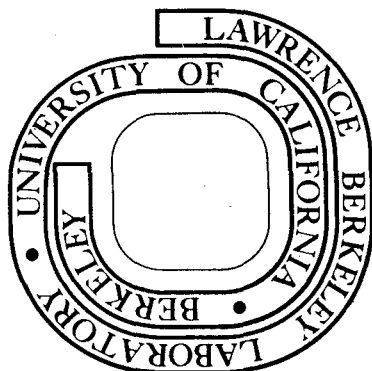
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WAVELENGTH MODULATED SPECTRUM AND ELECTRONIC PROPERTIES OF  $\text{HfS}_2$

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JANUARY 1976

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Wavelength Modulated Spectrum and Electronic Properties of  $\text{HfS}_2$ C. Y. Fong<sup>§</sup>

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## ABSTRACT

We have measured the reflectivity and the wavelength modulated reflectivity of  $\text{HfS}_2$  at room temperature and 5°K. The reflectivity spectrum is compared with that obtained from a band structure calculated by the empirical pseudopotential method. Structures in the spectrum are identified. The volume effect of the optical transitions is shown to be important in this semiconducting layer crystal.

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## I. INTRODUCTION

Among the transition metal dichalcogenides, the group IVB compounds crystallize in the  $CdI_2$  configuration. A typical layer consists of a plane of metal atoms sandwiched between two planes of the chalcogenides. In contrast to the polytypes of the group VB and VIB crystals,<sup>1</sup> there is only one stacking sequence. Within a layer, each metal atom is octahedrally surrounded by six chalcogens as shown in Fig. 1. The saturation of the p-orbitals in one formula unit suggests these compounds should be semiconductors. As expected, most of the Zr and Hf compounds (except the ditellurides) are semiconductors. Conflicting results about the fundamental properties of Ti-dichalcogenides have been found in the literature,<sup>2</sup> but we shall not pursue this subject here.

Experimentally, one of the most extensively studied group IVB semiconducting dichalcogenides is  $HfS_2$  because good quality crystal can easily be obtained. Absorption measurements<sup>4</sup> support an indirect energy gap of value 1.96 eV at room temperature and a temperature coefficient of  $-4.3 \times 10^{-4}$  eV/°K in the range of 77-500°K. An independent electrical determination<sup>5</sup> gives a slightly higher value of 2.1 eV. At liquid helium temperature, transmission measurements performed on thin adhesive cleaved samples<sup>6</sup> have been able to resolve some fine structures in the range 2.5-3.5 eV.

Theoretical band structure calculations on  $HfS_2$  have been performed by Murray, et al (MBY)<sup>1</sup> and by Mattheiss.<sup>3</sup> MBY used a semi-empirical tight-binding scheme with three empirical parameters. These parameters

were used to weigh the calculated overlapping integrals and were determined by assigning a priority: (i) an indirect gap  $\Gamma_2^- \rightarrow L_1^+$  at 2.08 eV; (ii)  $L_1^- \rightarrow L_1^+$  at 2.87 eV; and (iii)  $\Gamma_3^- \rightarrow \Gamma_1^+$  at 3.4 eV.

In an attempt to explain the data of the transmission measurements,<sup>6</sup> they calculated the joint density of states of  $ZrS_2$  and extended it to  $HfS_2$ . On the other hand, the augmented plane-wave method (APW) has been applied by Mattheiss to calculate the band structure of  $HfS_2$  at a few important  $\vec{k}$ -points in the Brillouin zone (BZ). The band structure along symmetry directions was then obtained by Slater-Koster's tight-binding interpolation scheme. The results suggest an indirect gap  $\Gamma_2^- \rightarrow L_1^+$  at 2.77 eV. No serious comparison with the experimental data has been made in this case.

Even in this simple semiconducting transition metal layer compound, comparisons between the experimental and the theoretical results have been previously restricted to a semiquantitative basis because of lack of the dipole transition matrix elements<sup>1,3</sup> and the two-dimensional nature of the theoretical approach.<sup>1</sup> For better understanding of transition-metal dichalogenides a more realistic comparison between theory and experiment is necessary. In this paper, we report our measurements on the reflectivity and wavelength modulated reflectivity of  $HfS_2$  at room temperature and liquid helium temperature in the range of 2-6 eV. We also present a band structure of  $HfS_2$  obtained from the empirical pseudopotential method (EPM). The experimental reflectivity spectrum is then compared with the theoretical reflectivity spectrum deduced from the band structure calculation. We believe that this is the first realistic

comparison ever made on such layer compounds.

We have arranged this paper in the following way: Sections II and III briefly describe the experimental arrangement and theoretical method respectively. Section IV is a discussion and comparison of the present measured and calculated results as well as a comparison with various earlier experimental and theoretical work on the crystal.

## II. EXPERIMENT

The  $\text{HfS}_2$  crystal we used had a broad face of 1 cm x 0.5 cm and a thickness of about 10  $\mu$ . The latter was deduced from the interference fringes shown in Fig. 2 around 2.2 eV. The C axis of the crystal was perpendicular to the platelet. Because of the small sample thickness, our optical measurements were restricted to the configuration  $\vec{E} \perp \hat{C}$ . The sample was mounted on a sample holder free of strain and an "as grown" natural face of the platelet was used for the optical measurements.

The experimental apparatus for simultaneous measurements of the reflectivity and the logarithmic derivative of the reflectivity has been described elsewhere.<sup>7</sup> In order to facilitate comparison with theory, the data were digitized and converted from wavelength to energy scale on a computer. The results are presented in Fig. 2.

## III. THEORY

The empirical pseudopotential method has been discussed in detail in the literatures.<sup>8</sup> In essence, a nonlocal pseudopotential with



$l = 2$  centered at the Hf-atom in the unit cell was used to account for the strong potential experienced by the partially filled d-electrons. The potentials of the s- and p-electrons and some of the hybridization effects in the crystal are expressed in terms of the form factors of the local pseudopotentials. The starting form factors of the S-atom was scaled from  $\text{SnS}_2$ .<sup>9</sup> As the form factors of Hf have never been reported in the literature, they were initially approximated by the pseudopotential of the Nb-atom<sup>10</sup> with proper scaling. These atomic form factors were cut off at  $|\vec{G}|_{\text{max}}^2 = 15 (\sqrt{2}\pi/a)^2$ , where  $\vec{G}$  is a reciprocal lattice vector and  $a$  is the lattice constant in the X-Y plane. This results in a total of 17 nonvanishing form factors for each atomic species. To secure proper convergence of the band energies with respect to the number of plane waves, we used control energies<sup>8</sup>  $E_1 = 19.5$  and  $E_2 = 37.5$  in units of  $(\sqrt{2}\pi/a)^2$ . Equivalently, there are about 185 plane waves with energies less than  $E_1$  and about 300 plane waves used in the Lowin-Brust perturbation scheme.<sup>11</sup> The convergence of the calculated energies at  $\Gamma$ , K, A and H is within 0.1 eV, whereas at M and L it is only of the order of 0.1 eV. Spin-orbit interaction is neglected in the present calculation.

To calculate the reflectivity from the band structure we calculate first the imaginary part of the dielectric function,  $\epsilon_2(\omega)$ , by the linear interpolation scheme.<sup>12</sup> There are 60  $\vec{k}$ -points in the (1/12)th of the BZ used to set up the mesh. Since we anticipate a comparison of  $R(\omega)$  with  $\vec{E} \cdot \hat{C}$ , only the perpendicular components of the dipole transition

matrix elements of six valence bands<sup>(3-8)</sup> to five conduction bands<sup>(9-13)</sup> were considered at the mesh points. An equivalent of  $2.5 \times 10^4$  points in the BZ were sampled. Then, we used the Kramer-Kronig relation to calculate the real part of the dielectric function,  $\epsilon_1(\omega)$ , and the reflectivity  $R(\omega)$ .

#### IV. RESULTS AND COMPARISONS

In Fig. 2 the reflectivity,  $R(\omega)$ , and its logarithmic derivative were plotted as functions of photon energy,  $\hbar\omega$ . In general, the reflectivity shows prominent structures for  $\hbar\omega \leq 3.5$  eV, a strong drop-off above 4.0 eV and a fairly constant "plateau" observed up to 6 eV. The minimum of the reflectivity at 4.23 eV is only about 2%. The magnitude of the reflectivity of the "plateau" is sensitive to the position of the focused beam on the sample surface. As usual, the derivative spectrum displays many fine structures. We shall compare later the details of other experimental and theoretical results.

The calculated band structure along several symmetry directions is shown in Fig. 3. We have used Slater's notations of the irreducible representations for the  $D_{3d}$  group. The labelings at L are different from those used in Ref. 3, but are equivalent with  $1 \leftrightarrow 1^+$ ,  $2 \leftrightarrow 1^-$ ,  $3 \leftrightarrow 2^-$  and  $4 \leftrightarrow 2^+$ . From now on, we shall use the notations without the "+" and "-" signs at L. In Fig. 4, we compare our experimental and calculated reflectivity spectra.

The calculated indirect fundamental gap is the transition of  $\Gamma_2^- \rightarrow M_1^+$  at 1.8 eV which agrees to  $\sim 0.2$  eV with the experimental value.

Although our identification differs from the one ( $\Gamma_2^- \rightarrow L_1$ ) given by Refs. 1 and 3, it may not be incompatible. As shown in Fig. 3, the energy of the lowest conduction band (the 9th band) at  $L(L_1)$  is 0.1 eV about  $M_1+$  while the convergence of energy at both L and M points, as we discussed in previous section, is only of the order of 0.1 eV. It is quite possible that with finer matrices, the relative ordering of  $L_1$  and  $M_1+$  is reversed. As a comparison, we note that the indirect gap calculated by MBY is 2.7 eV (as deduced from the band structure of  $\text{HfS}_2$  in Ref. 1). Similar discrepancy appears in the other identified structures.

The first prominent structure in our experimental reflectivity spectrum is a 2.83 eV. Compared to the value reported by Greenaway and Nitche<sup>4</sup> (2.9 eV) and the one given by Beal et al<sup>6</sup> (2.88 eV), our peak is about 60 meV lower. This difference may be due (a) to the increased accuracy achieved in the modulation spectroscopy, and (b) to the shift of peak energies between absorption and reflectivity spectra<sup>13,14</sup>. The theoretical spectrum in this range shows a weak shoulder at 2.7 eV and a peak at 2.9 eV. We assign the peak to the observed structure at 2.83 eV. Both theoretical structures come from regions near  $\Delta$  (line  $\Gamma \rightarrow A$ ) from transitions of the upper most valence band to the lowest conduction band (8  $\rightarrow$  9 transitions) except that the 2.7 eV contour does not enclose the point A. We find no correlation of this structure with the point L in the BZ as suggested by MBY.<sup>1</sup> Their calculated energies of transitions  $L_2 \rightarrow L_1$  and  $L_3 \rightarrow L_1$  (assigned by MBY as the direct gap) are at 3.47 and 3.6 eV respectively. Hence, it will be impossible to account for the 2.83 eV experimental

structure in a spectrum deduced from their band structure. The result of the APW calculation<sup>3</sup> suffers the same shortcoming, since the calculated minimum direct gap at 3.43 eV is also at L. From our calculation, we suggest that the fundamental direct gap of HfS<sub>2</sub> is at  $\Gamma(\Gamma_2^- \rightarrow \Gamma_3^+)$  with a gap energy of 2.4 eV and rather weak dipole transition matrix elements, and the contribution to the 2.83 eV structure is due to the volume effect.<sup>8</sup>

The two next structures around 2.94 and 2.99 eV in the derivative reflectivity spectrum agree with the ones at 3.03 and 3.07 eV in the transmission data<sup>6</sup>. The splitting in our case is 50 meV, and agrees with the value (~65 meV) calculated by MBY for the spin-orbit splitting of the  $\Gamma_3^-$ <sup>(6,7)</sup> band. However, the interband energy of  $\Gamma_3^- \rightarrow \Gamma_1^+$  given by MBY is 4.08 eV which is about 1 eV higher than the measured value of the structure. Beal et al<sup>6</sup> identified the 3.07 eV shoulder as the transitions associated with  $M_1^- \rightarrow M_1^+$ , i.e.,  $8 \rightarrow 9$  at M. Our theoretical result shows a shoulder at 3.1 eV. It is not resolved into two structures since the resolution of the calculation is only 0.1 eV. The contributions to this structure are from  $8 \rightarrow 9$  transitions near the L point and  $7, 8 \rightarrow 11$  transitions around the A point. Both regions have strong dipole matrix elements. Since part of the contributions associated with the degenerate valence bands at the point A ( $A_3^- \rightarrow A_1^+$ ), it is possible that the 50 meV splitting is due to spin-orbit splitting of these degenerate bands.

The 3.2 eV structure in Refs. 4 and 6 is seen in our experimental spectrum (Fig. 2) as a shoulder at 3.17 eV with no splitting resolved. The transition possibly responsible for the structure is  $L_2 \rightarrow L_1$  ( $7 \rightarrow 9$ )

but its contribution is not visible in our calculated spectrum as it is masked by the strong peak at 3.3 eV.

Both our experimental and theoretical spectra show a strong peak at 3.3 eV, which presumably corresponds to the 3.23 eV peak in the absorption spectrum. This peak was identified in Ref. 1 as due to  $\Gamma_3^- \rightarrow \Gamma_1^+$  transitions. Their calculated energy of this peak was however, at 4.08 eV. We find from our calculation that the peak comes from  $8 \rightarrow 9$  transitions in an extended region very near the  $\Gamma$ ALM plane in the BZ. A nearby critical point with  $M_1$  symmetry is found along R  $[(\frac{1}{3}, 0; \frac{1}{2}) \frac{\sqrt{2}\pi}{a}]$  at 3.25 eV. The strong dipole transition matrix elements near the plane enhance the intensity of the peak.

In the higher energy region, both spectra in Fig. 4 show a structure at 3.5 eV which can be attributed to the  $M_1^- \rightarrow M_1^+$  ( $8 \rightarrow 9$ ) transitions. The theoretical spectrum has a structure at 3.9 eV which differs from the experimental structure at 3.8 eV by 0.1 eV and is due to the volume effect in two extended regions: (a)  $8 \rightarrow 9$  transitions with cylindrical contour surface intersecting the midpoints of the S and T lines and the zone boundaries near L and M since the dipole matrix elements of  $8 \rightarrow 9$  transitions decrease sharply as the  $\bar{k}$ -points move away from the  $\Gamma$ ALM plane, the strength of the structure is weaker than the 3.3 eV peak; (b)  $7 \rightarrow 9$  transitions with contour surface almost parallel to the  $\Gamma$ LM plane. The dipole matrix elements associated with these transitions are weak. The peak at 4.4 eV is mainly due to the  $7 \rightarrow 9$  transitions with contours similar to the one given in (b) except it is farther away from  $\Gamma$ LM planes.

A fast drop in the reflectivity around 4.1 eV is exhibited in both spectra, although the one in the theoretical spectrum appears to be less drastic. A similar dip has been observed in Refs. 4 and 6. Our calculation shows that this is due to exhaustion of oscillator strength of the  $8 \rightarrow 9$  and  $7 \rightarrow 9$  transitions. The experimental reflectivity starts arising gradually after 4.2 eV and reaches a weak maximum at 4.9 eV. This is in good agreement with the result of Greenaway and Nitché.<sup>6</sup> The corresponding structure in the theoretical spectrum is 0.3 eV lower and the magnitude is about seven times higher. The main contribution to this peak comes from  $7 \rightarrow 10$  transitions in the region near  $\Delta$  but above the  $\Gamma$ MK plane. The discrepancy in the higher region has been found in most pseudopotential calculations of semiconductors<sup>8</sup>. We have summarized the above discussion in Table I.

Compared with other theoretical calculations, the band ordering near the gap shown in Fig. 3 agrees well with the APW results<sup>3</sup> but differs from the tight-binding calculation which shows  $\Gamma_1+$  being the lowest conduction band. A detailed comparison of the band energies at  $\Gamma$  and L with respect to  $\Gamma_2-$  and the ordering of the bands near the gap is given in Table II. Our  $\Gamma_3+$  (3rd and 4th bands) and  $\Gamma_1+$  (5th band) are reversed with respect to the other two calculations. This can be an artifact due to imposition of smoothness for the pseudopotential form factors. The (3s)-bands of the S-atoms are about 15. eV below the top of the valence band. The accuracy of these bands may be tested in the future by the soft x-ray photoemission (XPS) measurements. It is

interesting to compare the widths of the nonbonding d bands and the uppermost p bands obtained in different calculations as listed in Table I. We take the maximum separation of the energies between the 9th and 11th bands for the width of the d-states and that between the 7-th and 8-th bands of the width of the p-states. The bandwidths of the present calculation in both cases are wider than those of Ref. 1 and 3.

In conclusion, we have measured the reflectivity and the first-order derivative reflectivity spectra of  $\text{HfS}_2$  at room temperature and at  $5^\circ\text{K}$ . The structures agree well with earlier experimental results and are in reasonable agreement with those derived from the band structure calculation using the empirical pseudopotential method. Structures below  $\hbar\omega = 5.0$  eV have been identified. Prominent peaks at  $\hbar\omega \leq 3.5$  eV come from transitions from two uppermost valence bands (p-states) to the lowest nonbanding d states in a large region of the BZ. This is contrary to the earlier identifications<sup>1</sup> which associate strong peaks with only a few critical points in the BZ. Comparison of the present calculation tight-binding and APW calculations shows that: (1) The band ordering near the gap agrees with the APW results but differs from the tight-binding results; (2) the two uppermost p and the nonbonding d conduction bands are wider by a factor of 2 in empirical pseudopotential calculation than those in the other calculations.

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## FIGURE CAPTIONS

- Fig. 1      a. Hexagonal unit cell of  $\text{HfS}_2$ .  
            b. Octohedral continuation within one layer.
- Fig. 2      The wavelength modulated reflectivity at  $5^\circ\text{K}$  and the  
            reflectivity at  $5^\circ\text{K}$  (—) and at  $300^\circ\text{K}$ (--).
- Fig. 3      The band structure of  $\text{HfS}_2$ .
- Fig. 4      The experimental and theoretical spectra of  $\text{HfS}_2$ .

TABLE CAPTIONS

Table I Comparison of experimental and theoretical critical point energies and their assignments. All energies are in eV.

Table II Comparison of the band ordering and eigenvalues at  $\Gamma$  and L in different band structure calculations. (All energies are in eV).

TABLE I

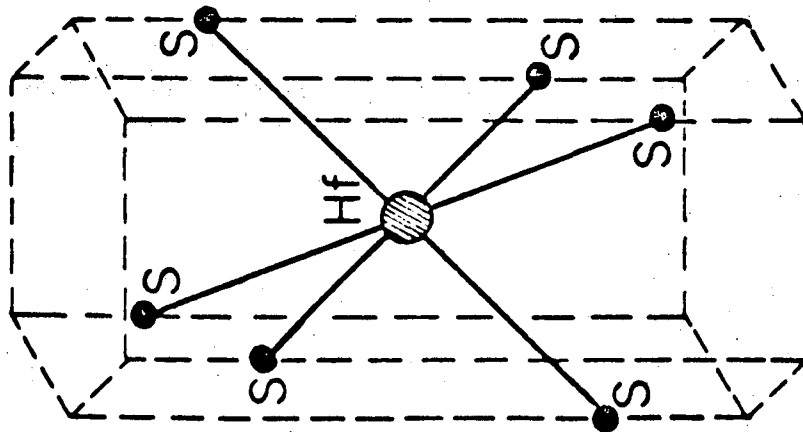
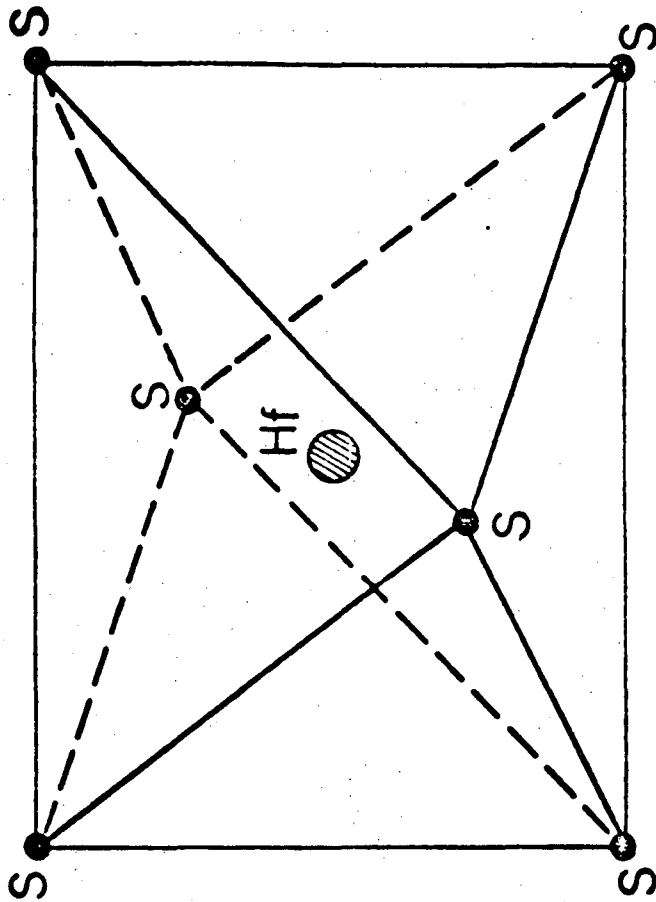
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Authors Feature	THEORY				EXPERIMENT		
	Wilson Yoffe	Present Work	Murray <sup>1</sup> Brumley Yoffe <sup>†</sup>	Mattheiss <sup>3</sup>	Greenaway <sup>4</sup> Nitsche	Beal <sup>6</sup> Knight Liang	Present Work
Indirect Gap	1.98	1.8 ( $\Gamma_2 \rightarrow M_1+$ )	(2.7) ( $\Gamma_2 \rightarrow L_1+$ )	2.77 ( $\Gamma_2 \rightarrow L_1$ )	1.96		
Direct Gap		2.4 ( $\Gamma_2 \rightarrow \Gamma_3+$ )	3.47 ( $L_3 \rightarrow L_1$ )	3.43 ( $L_3 \rightarrow L_1$ )			
Optical		2.9 { 8 + 9 } near $\Delta$	3.6 ( $L_2 \rightarrow L_1$ )		2.9	2.88	2.83
Structure		3.1 { $L_3 \rightarrow L_1,$ $A_3 \rightarrow A_1+$ }				3.03, 3.07 ( $M_1 \rightarrow M_1+$ )	2.94 2.99
		3.16 ( $L_2 \rightarrow L_1$ )			3.2	3.2	3.17
		3.3 { 8 + 9 } ( $\frac{1}{3}, 0, \frac{1}{2}$ ) $\sqrt{2}\pi$ and a near $\Gamma_{ALM}$ plane	4.08 <sup>*</sup> ( $\Gamma_3^- \rightarrow \Gamma_1+$ )			3.23	3.3
		3.5 ( $M_1 \rightarrow M_1+$ )					3.5
		3.9 { 8+9, 7+9 } Volume effect					3.8
		4.4 { 7+9 } Volume effect					
		4.6 { 7 + 10 } Volume effect				5.0	4.9
	Width of the nonboundary d-bands	1.98	4.0 ( $L_1 \rightarrow L_1$ )	3.14 ( $M_1+ \rightarrow M_1+$ )	3.31 ( $M_1+ \rightarrow M_1+$ )		
Width of the uppermost p-band	0.87	3.1 ( $H_1 \rightarrow \Gamma_2-$ )	1.56 ( $M_2- \rightarrow \Gamma_2-$ )	1.54 ( $M_2- \rightarrow \Gamma_2-$ )			

<sup>†</sup> Values deduced from the band structure.

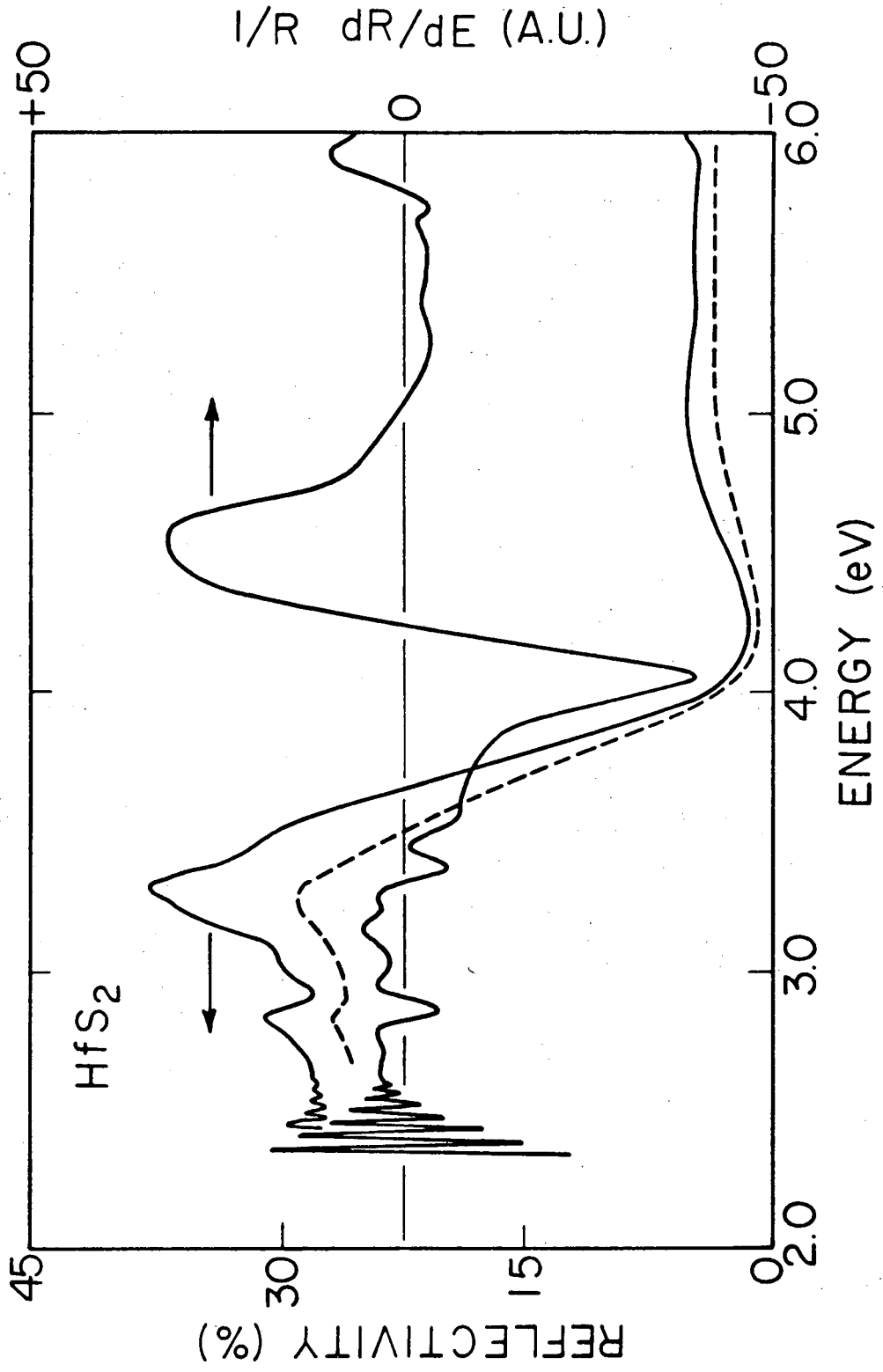
TABLE II

Feature	Ordering of levels at $\Gamma$ , neglecting S.O. interaction.			Ordering of levels at L, neglecting S.O. interaction.		
	<u>Present work</u>	<u>MBY</u>	<u>Mattheiss</u>	<u>Present work</u>	<u>MBY</u>	<u>Mattheiss</u>
Minimum of the C.B.	$\Gamma_1^+$ (2.7 eV)	$\Gamma_3^+$ (4.8 eV)	$\Gamma_1^+$ (4.2 eV)			
	$\Gamma_3^+$ (2.4 eV)	$\Gamma_1^+$ (3.7 eV)	$\Gamma_3^+$ (3.9 eV)	$L_1 (L_1^+)$ (1.9 eV)	$L_1^+$ (2.7 eV)	$L_1^+$ (2.7 eV)
Top V.B.	$\Gamma_2^-$	$\Gamma_2^-$	$\Gamma_2^-$	$L_3 (L_2^-)$ (-1.15 eV)	$L_2^-$ (-0.7 eV)	$L_2^-$ (-0.7 eV)
Second V.B.	$\Gamma_3^-$ (-0.1 eV)	$\Gamma_3^-$ (-0.4 eV)	$\Gamma_3^-$ (-0.2 eV)	$L_2 (L_1^-)$ (-0.1 eV from $L_3$ )	$L_1^-$ (-0.14 eV from $L_2^-$ )	$L_1^-$ (-0.1 eV from $L_2^-$ )



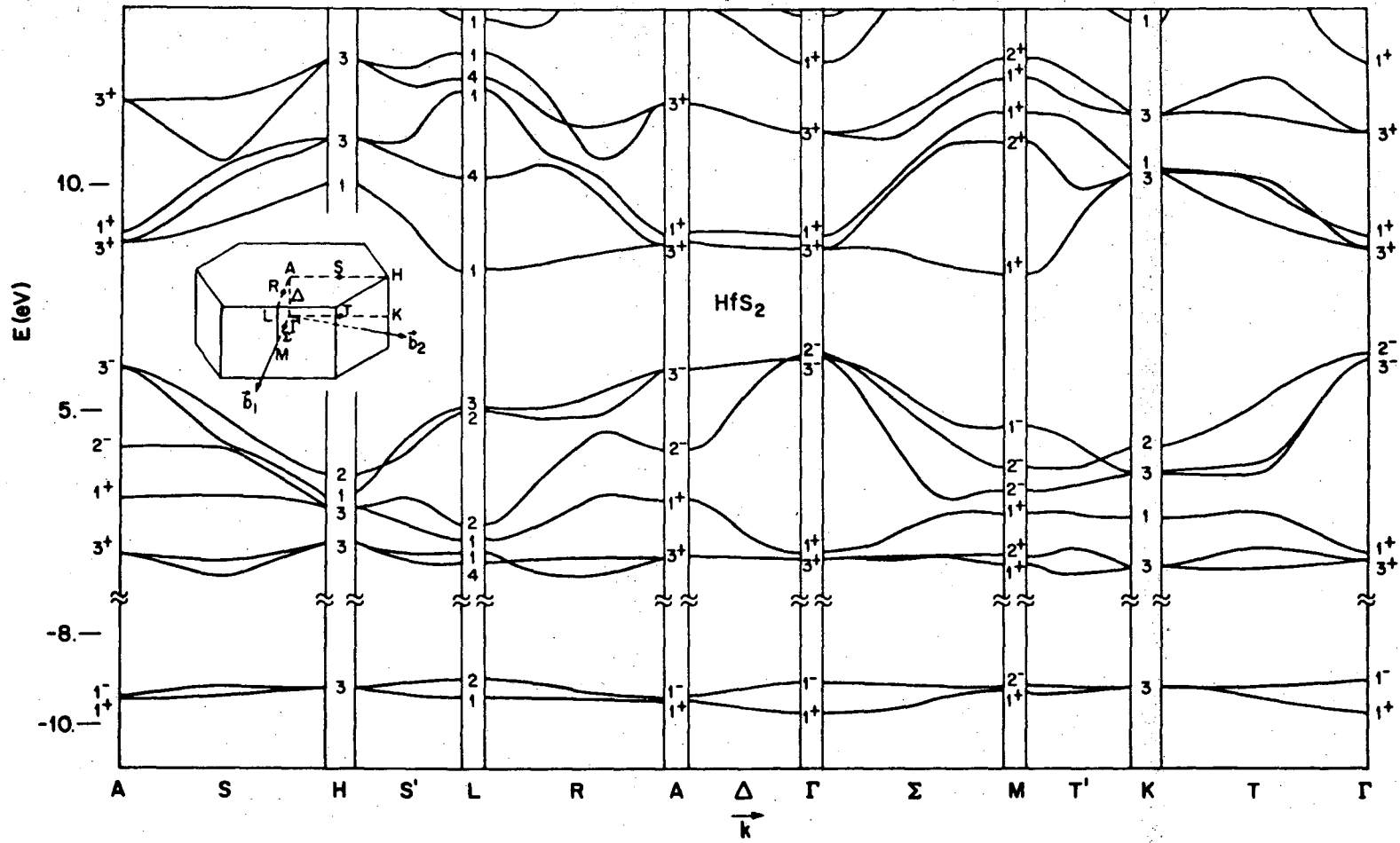
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Fig. 1

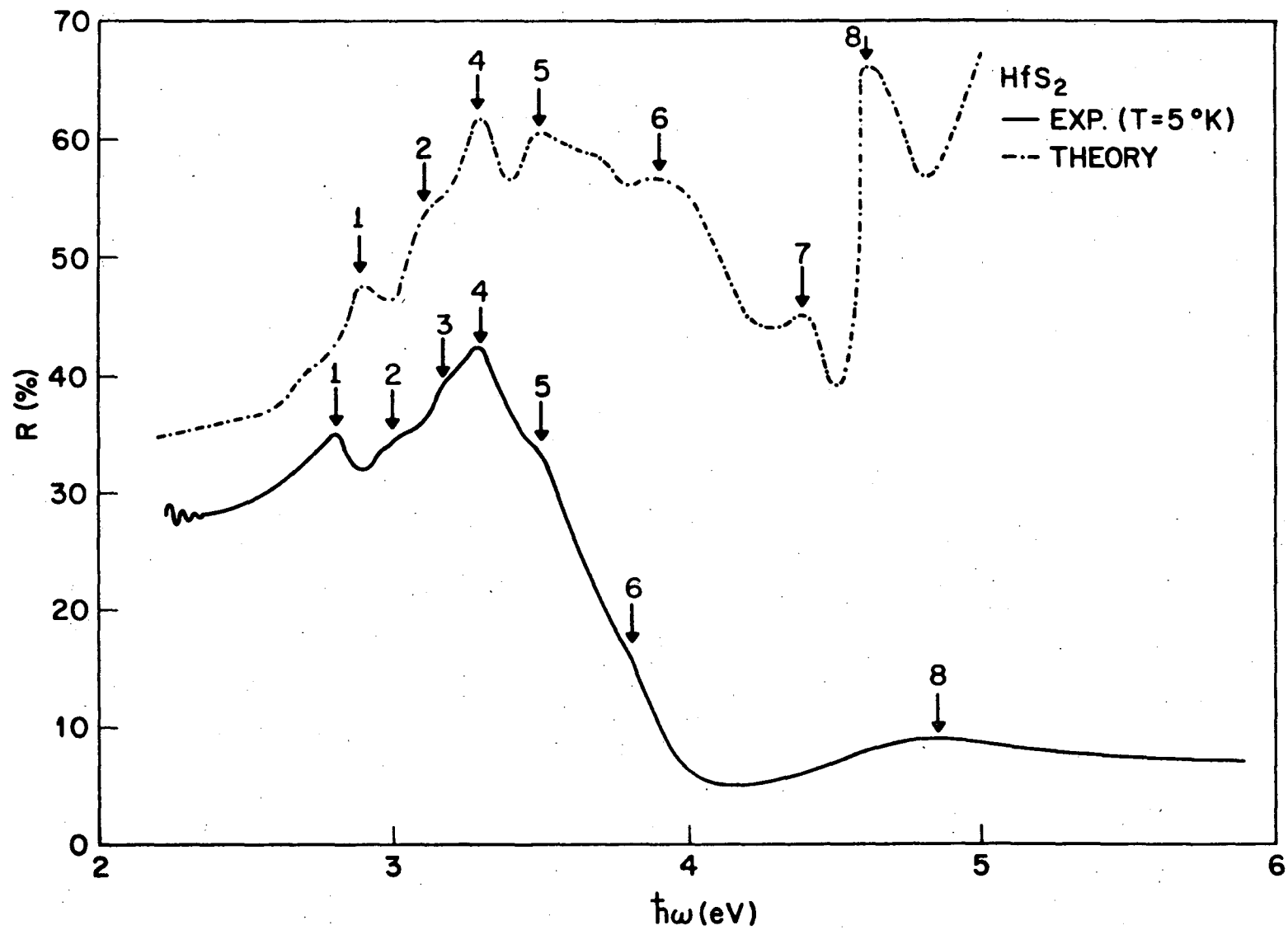


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