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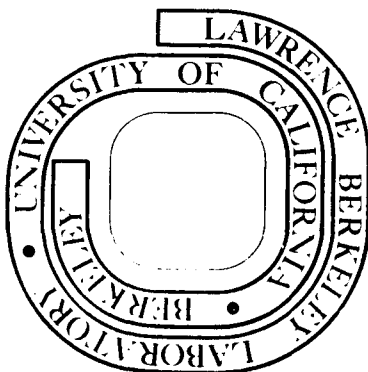
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THE METASTABLE PHASE Ni<sub>2</sub>Mo AND THE INITIAL STAGES

OF ORDERING IN Ni-Mo ALLOYS \*

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The initial stages of ordering in Ni<sub>3</sub>Mo and Ni<sub>4</sub>Mo have been investigated by transmission electron microscopy and diffraction. The development of long-range order in Ni<sub>3</sub>Mo is associated with decomposition into the two metastable phases Ni<sub>2</sub>Mo and Ni<sub>4</sub>Mo, which are eventually replaced by the equilibrium Ni<sub>3</sub>Mo at a later stage of ordering. Evidence for the presence of metastable Ni<sub>2</sub>Mo phase was also found during the early stages of ordering of Ni<sub>4</sub>Mo. The presence of the metastable phase Ni<sub>2</sub>Mo at Ni<sub>4</sub>Mo composition and that of Ni<sub>2</sub>Mo and Ni<sub>4</sub>Mo at Ni<sub>3</sub>Mo composition can be explained in terms of the recent thermodynamic calculations of the ground states of ordered binary alloys by Cahn and his co-workers.

1. Introduction

There have been a number of studies on the ordering of Ni-Mo alloys, particularly on the systems Ni<sub>4</sub>Mo [1—9] and Ni<sub>3</sub>Mo [10—12]. In the long-range-ordered (lro) state, Ni<sub>4</sub>Mo is body-centered

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tetragonal and  $\text{Ni}_3\text{Mo}$  has an orthorhombic structure; and both are disordered fcc at high temperature in the single-phase region. On fast quenching from the single-phase region, the decomposition can be suppressed and both the alloys exhibit diffuse short-range order (sro), scattering peaks at  $\{1\frac{1}{2}0\}$  position of the fcc reciprocal lattice. In a recent study [13] of the sro state of  $\text{Ni}_4\text{Mo}$  and  $\text{Ni}_3\text{Mo}$ , it was found that both of these alloys are similar in the quenched state and contain weak superlattice reflections corresponding to  $\text{Ni}_4\text{Mo}$  and  $\text{Ni}_2\text{Mo}$  superstructures in addition to the  $\{1\frac{1}{2}0\}$  spots. Thus, one may expect these two alloys to behave similarly at the very early stages of the development of lro. Yamamoto et al. [10], who quenched the alloy  $\text{Ni}_3\text{Mo}$  from high temperature single phase region and then allowed it to age, reported that it initially decomposed to  $\text{Ni}_2\text{Mo}$  and then  $\text{Ni}_4\text{Mo}$  precipitated and that these two phases coexist for some time. On prolonged aging these are subsequently replaced by the equilibrium  $\text{Ni}_3\text{Mo}$  phase. In the studies [4—8] on the development of lro in  $\text{Ni}_4\text{Mo}$ , on the other hand, the formation of metastable  $\text{Ni}_2\text{Mo}$  phase has never been reported. Thus, it is not clear why the metastable  $\text{Ni}_2\text{Mo}$  phase is observed in stoichiometric  $\text{Ni}_3\text{Mo}$  but not at  $\text{Ni}_4\text{Mo}$  composition, even though both of them show weak  $\text{Ni}_2\text{Mo}$  superlattice reflections in the as quenched state. The recent calculations of the ground-state structures in ordered binary alloys by Richards [14], by Richards and Cahn [15], and by Allen and Cahn [16] predict that the  $\text{Ni}_2\text{Mo}$  phase may be present in the composition range considered here (20—25 at. % Mo). In view of these results, the initial stages of ordering in both  $\text{Ni}_4\text{Mo}$  and  $\text{Ni}_3\text{Mo}$  were carefully examined by electron microscopy and diffraction, for various isothermal annealing treatments.

The results presented in this paper show that the metastable  $\text{Ni}_2\text{Mo}$  phase can form in very small amounts after appropriate isothermal annealing of the quenched  $\text{Ni}_4\text{Mo}$ . In the alloy  $\text{Ni}_3\text{Mo}$ , both  $\text{Ni}_2\text{Mo}$  and  $\text{Ni}_4\text{Mo}$  phases form simultaneously during the initial stages of ordering. These results provide the experimental evidence for some of the

predictions [14—16] from the calculations of ground-state structures in ordered binary alloys.

## 2. Crystallography of Ni<sub>2</sub>Mo

The crystallographic features of the ordered Ni<sub>4</sub>Mo and Ni<sub>3</sub>Mo structures have been discussed elsewhere [2, 8, 11] and need not be repeated here. Only a few aspects of the ordered Ni<sub>2</sub>Mo structure that are important to this study will be described. The Ni<sub>2</sub>Mo phase does not occur in the Ni-Mo phase diagram [17] at stoichiometric composition and has been observed only as a metastable phase. The atomic arrangement has been found [10] to be isomorphous with ordered Pt<sub>2</sub>Mo, and Fig. 1(a) shows the body-centered orthorhombic unit cell; the dotted line outlines the fcc unit cell. The relationships between the disordered fcc lattice ( $\alpha$ ) and the ordered orthorhombic Ni<sub>2</sub>Mo lattice are

$$\begin{aligned} [100]_{\text{Ni}_2\text{Mo}} & \parallel [110]_{\alpha} , \\ [010]_{\text{Ni}_2\text{Mo}} & \parallel [\bar{1}10]_{\alpha} , \\ [001]_{\text{Ni}_2\text{Mo}} & \parallel [001]_{\alpha} . \end{aligned}$$

Figure 1b shows the projection of atoms on the (001) plane<sup>2</sup>); the dotted line outlines the orthorhombic Ni<sub>2</sub>Mo lattice and the open circles represent the projection of atoms on a/2 layer above. This structure can be described by the stacking of atoms on either {420} or {220} planes where every third plane contains all Mo and in between all Ni atoms. Thus, the reciprocal lattice of the ordered structure can be constructed from the original fcc lattice, where the superlattice reflections will appear at every  $\frac{1}{3} \langle 220 \rangle$  or  $\frac{1}{3} \langle 420 \rangle$  reciprocal lattice vectors. This gives rise to six orientation variants of Ni<sub>2</sub>Mo corresponding to six variants of {220} because of the two-fold degeneracy associated with stacking on {420} planes. The

<sup>2</sup>) Unless otherwise specified, the indices refer to the fcc lattice.

reciprocal lattice of ordered  $\text{Ni}_4\text{Mo}$ (D1a) can be constructed in a similar way where the superlattice reflections appear at every  $\frac{1}{5} \langle 420 \rangle$  fcc reciprocal lattice vector.

### 3. Experimental Procedure

The alloys  $\text{Ni}_4\text{Mo}$  and  $\text{Ni}_3\text{Mo}$  were prepared by melting together the required proportions of high-purity (99.99%) Ni and Mo in an arc furnace, back filled with argon. The alloys were melted at least six times, and after each melt the ingot was cut into small pieces and the pieces were intermixed in order to obtain a homogeneous composition. The ingots were encapsulated in quartz tubes in vacuum and were homogenized at temperatures of  $1200^\circ\text{C}$  and  $1270^\circ\text{C}$  for  $\text{Ni}_4\text{Mo}$  and  $\text{Ni}_3\text{Mo}$ , respectively. The ingots were quenched into water and then cold rolled to 6-mil strips with intermediate anneals. The foils were then finally homogenized in an inert atmosphere and quenched directly into iced brine and subsequently aged. The compositions of the homogenized alloy ingots were 19.7 at %Mo and 25.1 at %Mo for  $\text{Ni}_4\text{Mo}$  and  $\text{Ni}_3\text{Mo}$ , respectively.

The thin foils suitable for transmission electron microscopy were prepared in two stages. The 6-mil foils were first electrolytically thinned to 1–2 mils by the window technique, in which a solution containing 396 cc ethylene glycol, 57 cc perchloric acid, 57 cc hydrofluoric acid, and 27 cc distilled water was used. The temperature of the solution was maintained at  $10^\circ\text{C}$  and the applied voltage was 9–11 V. From these 1–2-mil foils, 2.3-mm disks were punched out and were finally jet polished in an electrolyte containing two parts of sulphuric acid and one part water, with the total current kept below 10 mA. The foils were examined in a Siemens Elmiskop IA operated at 100kV.

## 4. Results

### 4.1 Ni<sub>3</sub>Mo

The isothermal aging studies of Ni<sub>3</sub>Mo were carried out at 650°C and all the results to be described below correspond to various aging times at this temperature. The choice of this temperature is based on previous studies on Ni<sub>4</sub>Mo [8], which indicate that aging at 650°C is associated with some interesting diffraction effects at the initial stages whereas the ordering reaction at high temperatures (~750°C) is extremely fast and these diffraction effects are missed altogether. Yamamoto et al. [10] aged Ni<sub>3</sub>Mo samples at 860°C, which is rather high.

Figure 2A shows a [001] diffraction pattern obtained after aging for 4 h. The pattern consists of fundamental fcc spots and superlattice reflections from both Ni<sub>2</sub>Mo and Ni<sub>4</sub>Mo phases as indexed in Fig. 2C. Some of the fundamental fcc spots in Fig. 2A have also been indexed. The Ni<sub>2</sub>Mo reflections (marked M) appear to be arced towards the neighboring Ni<sub>4</sub>Mo reflections (marked N) the main direction of streaking is  $\langle 110 \rangle$ , whereas the Ni<sub>4</sub>Mo reflections are streaked in  $\langle 210 \rangle$  directions. The streaking of Ni<sub>4</sub>Mo spots after 4 h of aging (Fig. 2A) is similar to that observed by Okamoto and Thomas [8] in Ni<sub>4</sub>Mo after 5–10 min of aging at the same temperature; thus Ni<sub>3</sub>Mo seems to decompose more slowly than Ni<sub>4</sub>Mo at 650°C. There also appears to be some intensity near the  $\{1\frac{1}{2}0\}$  positions (marked by arrows), especially along  $\langle 100 \rangle$  directions. This intensity is not due to the presence of  $\{1\frac{1}{2}0\}$  spots (as is shown by the fact that they do not lie precisely at  $\{1\frac{1}{2}0\}$  positions) but arise from the relrods from the other two Ni<sub>4</sub>Mo spots that are also streaked in  $\langle 210 \rangle$  directions and lie at positions  $\frac{1}{10}[002]$  above and below this [001] reciprocal lattice section. Thus, they extend from the  $\{1\frac{1}{2}0\}$  position to



the projection of the  $\text{Ni}_4\text{Mo}$  spots, along  $\langle 100 \rangle$  directions.

On further aging the  $\text{Ni}_4\text{Mo}$  spots (marked N) become rounded as can be seen in Fig. 2B, whereas the  $\text{Ni}_2\text{Mo}$  spots (marked M) are still spread into arcs. The previous study on  $\text{Ni}_4\text{Mo}$  [8] has shown that the streaking of  $\text{Ni}_4\text{Mo}$  superlattice spots in  $\langle 210 \rangle$  directions is not a shape factor effect because the streaking is asymmetrical and the dark field images show equiaxed domains. This streaking of  $\text{Ni}_4\text{Mo}$  spots in  $\langle 210 \rangle$  directions was explained [8] to be due to the presence of nonconservative APB's on  $\{420\}$  planes. If the APB's are spaced periodically then one would observe satellites; but if the spacing is irregular, these satellites will be broadened into streaks. On aging for longer times, these nonconservative APB's (which have a relatively higher energy than the conservative APB's) are eliminated and the streaks will disappear as seen in Fig. 2B. However, some of them may still remain and it will be seen later that they give rise to very weak streaks. Although the  $\text{Ni}_4\text{Mo}$  spots are not streaked after aging for 49 h (Fig. 2B) the  $\text{Ni}_2\text{Mo}$  spots are still streaked. This makes it doubtful whether an explanation based on APB's, similar to that of  $\text{Ni}_4\text{Mo}$  can be applied to  $\text{Ni}_2\text{Mo}$  or not. A detailed explanation will be given later in this section.

In order to see the actual reason for the arcing of  $\text{Ni}_2\text{Mo}$  spots and to determine their true shape, several other reciprocal lattice sections were examined after various aging treatments. Figures 3 and 4 show  $[\bar{1}20]$  and  $[121]$  reciprocal lattice sections, respectively. It can be seen from Fig 3A that the  $\text{Ni}_2\text{Mo}$  spots (as indexed in Fig. 3C) are streaked along the  $\langle 210 \rangle$  direction and not along  $\langle 110 \rangle$  as was apparent from the  $[001]$  pattern. A dark field micrograph of the  $\text{Ni}_2\text{Mo}$  spot [as shown by the position of the objective aperture in Fig. 3A] reveals that the  $\text{Ni}_2\text{Mo}$  domains have a plate-like shape forming on  $(420)$  planes. Thus, the streaking of  $\text{Ni}_2\text{Mo}$  spots in  $\langle 210 \rangle$  directions is a true shape-factor effect due to plate-like domains. The  $[\bar{1}20]$  diffraction pattern in Fig 3A also contains some

additional reldods from the  $\text{Ni}_4\text{Mo}$  spots whose positions are shown in Fig. 3C by open squares. Their intensities are fairly strong because they lie very close to this section and are still elongated.

The  $[\bar{1}21]$  sections (Fig. 4) further confirm that the  $\text{Ni}_2\text{Mo}$  spots are streaked along  $\langle 210 \rangle$  directions. Figure 4A shows the diffraction pattern after 4 h of aging. Each of the three variants of  $\text{Ni}_2\text{Mo}$  that are present is streaked in a different  $\langle 210 \rangle$  direction. Since the variant marked by open triangles [Fig. 4B] is streaked in a  $\langle 210 \rangle$  direction that intersects the  $[\bar{1}21]$  section at an angle, this spot appears slightly elliptical [Fig. 4A]. In fact, the streaks in the  $\langle 210 \rangle$  directions appear to extend continuously from one reciprocal lattice point to another [Fig. 4A] with maxima at  $\text{Ni}_2\text{Mo}$  and  $\text{Ni}_4\text{Mo}$  positions.

Now after establishing that the  $\text{Ni}_2\text{Mo}$  spots are streaked in  $\langle 210 \rangle$  directions as a result of a shape-factor effect, we can examine why in the  $[001]$  diffraction pattern the streaking appears to be along  $\langle 110 \rangle$ . As described above (Fig. 1), the  $\text{Ni}_2\text{Mo}$  structure, for example, stacking on  $(420)$  and  $(240)$  planes gives rise to the same variant of  $\text{Ni}_2\text{Mo}$  (Spot A in Fig. 2C). Thus if plate-like  $\text{Ni}_2\text{Mo}$  domains form with equal probability on  $(420)$  and  $(240)$  planes, the  $\text{Ni}_2\text{Mo}$  spot at A will be streaked both in  $[420]$  and  $[240]$  directions, as shown by the thick lines (Fig. 2C). Since these two directions are fairly close to each other and the streaks are fairly wide, these two streaks are not discernible from each other in a  $[001]$  orientation and give rise to an apparent streak in the  $\langle 110 \rangle$  direction and an arcing towards the neighboring  $\text{Ni}_4\text{Mo}$  spots. However, the  $[\bar{1}20]$  section contains only one direction of the streak as can be seen from the trace in Fig. 2C and it is possible to see that the  $\text{Ni}_2\text{Mo}$  spots are, in fact, streaked in  $\langle 210 \rangle$  directions. Similar is the case with  $[121]$  orientation whose trace on  $[001]$  section is the same as that of  $[\bar{1}20]$ . These results show that it is the same as that of  $[\bar{1}20]$ . These results show that it is absolutely necessary to examine certain particular reciprocal lattice sections such

as  $[\bar{1}20]$  and  $[121]$  in order to reveal the origin of the diffraction effects associated with  $\text{Ni}_2\text{Mo}$  spots, or else erroneous conclusions may be drawn. It may be mentioned that Yamamoto et al. [10] reported plate-like  $\text{Ni}_2\text{Mo}$  precipitates to form in  $\text{Ni}_3\text{Mo}$  on  $\{110\}$  planes after annealing for 30 min at  $860^\circ\text{C}$ . It is not clear whether there is an error in their analysis, as they did not report any evidence of streaks, or the difference may be due to different isothermal annealing treatments.

The  $\text{Ni}_2\text{Mo}$  and  $\text{Ni}_4\text{Mo}$  phases coexist for a long time (up to about 160 h of aging), but after about 250 h they disappear and the equilibrium  $\text{Ni}_3\text{Mo}$  phase appears [18]. Thus, the stoichiometric  $\text{Ni}_3\text{Mo}$  first decomposes to two metastable phases  $\text{Ni}_2\text{Mo}$  and  $\text{Ni}_4\text{Mo}$ . In the initial stages of decomposition the  $\text{Ni}_2\text{Mo}$  phase forms plate-like domains on  $\{420\}$  planes that give rise to pronounced streaking in the diffraction pattern, whereas the  $\text{Ni}_4\text{Mo}$  phase does not form plate-like domains but still shows streaking in the diffraction patterns in  $\langle 210 \rangle$  directions. At an intermediate stage of aging, the streaking of  $\text{Ni}_4\text{Mo}$  spots disappear whereas those of  $\text{Ni}_2\text{Mo}$  spots remain. On prolonged aging, the metastable phases  $\text{Ni}_2\text{Mo}$  and  $\text{Ni}_4\text{Mo}$  are both replaced by the equilibrium  $\text{Ni}_3\text{Mo}$ .

#### 4.2 $\text{Ni}_4\text{Mo}$

As in the case of  $\text{Ni}_3\text{Mo}$ , the isothermal aging treatments for the  $\text{Ni}_4\text{Mo}$  alloy were carried out at  $650^\circ\text{C}$  for various times from 5 min to 50 h; but only some typical results pertinent to this study will be described. Figure 5 shows a  $[001]$  diffraction pattern obtained after aging for 8 h. This pattern contains two variants of the  $\text{Ni}_4\text{Mo}$  superlattice reflections (which are indexed in Fig. 2C). In addition to the  $\text{Ni}_4\text{Mo}$  superlattice reflections, there are also weak  $\text{Ni}_2\text{Mo}$  superlattice reflections (marked by the single arrows). This pattern is very similar to the pattern obtained from  $\text{Ni}_3\text{Mo}$  (Fig. 2 B), except that  $\text{Ni}_2\text{Mo}$  reflections are very

weak. Much as in the case of  $\text{Ni}_3\text{Mo}$ , the weak  $\text{Ni}_2\text{Mo}$  spots are arced towards the neighboring  $\text{Ni}_4\text{Mo}$  spots. There are also some retrods (marked by double arrows) from the  $\text{Ni}_4\text{Mo}$  spots that lie  $\frac{1}{10}[002]$  above and below this reciprocal lattice section.

In order to confirm the presence of a  $\text{Ni}_2\text{Mo}$  phase, some other reciprocal lattice sections were also examined. Figure 6 shows a  $[121]$  diffraction pattern and the corresponding microstructure obtained after aging for 8 h. In Fig. 6A, the typical tweed contrast can be seen and the direction of the tweed striations coincides with the trace of the  $(10\bar{1})$  plane. Figure 6B is the dark-field micrograph of one variant of the  $\text{Ni}_4\text{Mo}$  superlattice reflection (marked b in Fig. 6C) and shows an alignment of the domains more or less in the direction of the tweed striations. Some typical areas are marked by arrows. These results show that the ordered domains are not in a random array of particles but are arranged in some ordered fashion in three dimensions. At this stage it is not possible to describe further the exact nature of the ordered array.

The  $[121]$  diffraction pattern in Fig. 6C clearly shows the presence of  $\text{Ni}_2\text{Mo}$  superlattice reflections of different variants that are streaked in different  $\langle 210 \rangle$  directions. The indexing of this pattern is identical to that in Fig. 4B and some of the  $\text{Ni}_2\text{Mo}$  spots are marked by single arrows. Here the  $\langle 210 \rangle$  streaks are elongated continuously from one superlattice reflection to another, with maxima at the  $\text{Ni}_2\text{Mo}$  positions (marked by the single arrows), similar to the weak  $\langle 210 \rangle$  streaks observed in  $\text{Ni}_3\text{Mo}$  (Fig. 4). This means that the  $\text{Ni}_2\text{Mo}$  phase exists as very thin platelets whose thickness is of the order of a unit cell. There are also some weak double diffraction spots present (marked by double arrows), from the different variants of the  $\text{Ni}_4\text{Mo}$  reflections. It must be pointed out that the detection of these weak spots depends very much on the exposure time, foil contamination, etc. In relatively thicker foils, these weak spots are difficult to detect at 100 kV because of the presence of the Kikuchi lines or bands. The presence of the  $\text{Ni}_2\text{Mo}$  superlattice reflections was also

detected [18] for aging times up to 24 h but these  $\text{Ni}_2\text{Mo}$  peaks in the  $\langle 210 \rangle$  streaks did not grow into strong superlattice reflections. The fact that these  $\langle 210 \rangle$  streaks through the  $\text{Ni}_2\text{Mo}$  reflections do not vanish even after aging for 24 h implies that the  $\text{Ni}_2\text{Mo}$  phase does not grow beyond a thickness of a few atom layers. It will be shown later in Section 4 that this monolayer of  $\text{Ni}_2\text{Mo}$  phase arises from the presence of nonconservative APB's on  $\{420\}$  planes in  $\text{Ni}_4\text{Mo}$  phase.

For aging treatments beyond 24 h, the structure is dominated by the heterogeneous reaction at the grain boundaries. Figure 7 shows an example. The heterogeneous reaction starts at the grain boundary and advances into the next grain B. The structure inside the heterogeneous component A contains a dense array of dislocations and APB's.

A similar heterogeneous reaction mode has been observed in  $\text{Ni}_2\text{V}$  [19] and it has been found that this heterogeneous reaction at the grain boundary is the predominant decomposition mode at lower temperatures.

The important observation on  $\text{Ni}_4\text{Mo}$  is the presence of weak superlattice reflections corresponding to  $\text{Ni}_2\text{Mo}$  phase. The pronounced streaking of  $\text{Ni}_2\text{Mo}$  reflections in  $\langle 210 \rangle$  directions implies that this phase arises from the presence of nonconservative APB's on  $\{420\}$  planes of  $\text{Ni}_4\text{Mo}$  domains. At a later stage of aging, heterogeneous reaction starts at the grain boundary and this heterogeneously nucleated phase migrates from the grain boundary into the whole grain. No  $\text{Ni}_2\text{Mo}$  phase is present in the final equilibrium  $\text{Ni}_4\text{Mo}$  phase.

## 5. Discussion

The results described above clearly indicate that the  $\text{Ni}_2\text{Mo}$  can form as a metastable phase in the Ni-Mo alloy in the composition range 20—25 at % Mo, although this phase does not appear in the equilibrium phase diagram [17,18]. First we will discuss some thermodynamic reasons

for the formation of the metastable  $\text{Ni}_2\text{Mo}$  and  $\text{Ni}_4\text{Mo}$  phases at stoichiometric  $\text{Ni}_3\text{Mo}$  compositions and then discuss some structural considerations.

Recently Richards [14], Richards and Cahn [15] have outlined a procedure for deriving the ground state of binary ordering alloys as a function of composition and the first and second nearest-neighbor interaction parameters  $V_1$  and  $V_2$ . The ground state for a given basic crystal structure, composition, and  $V_i$  is the state that has lowest configurational energy. If there are total  $N$  atoms arranged on a lattice and  $C$  is the fraction of B atoms (in the present case it is fraction of Mo atoms), the energy of mixing  $E$  can be written [14] as follows:

$$\text{For } \underline{\text{Ni}_4\text{Mo}}, \frac{E}{NV_1} = -\frac{3}{5} - 3C - 2C \left( \frac{V_2}{V_1} \right) \text{ for } 0.2 \leq C \leq 0.3 \quad (1)$$

$$\frac{E}{NV_1} = -\frac{3}{5} - 3C - \frac{3}{5} \left( \frac{V_2}{V_1} \right) \text{ for } 0.3 \leq C \leq 0.4 \quad (2)$$

$$\text{For } \underline{\text{Ni}_2\text{Mo}}, \frac{E}{NV_1} = -\left(3C + \frac{1}{2}\right) - 3C \left( \frac{V_2}{V_1} \right) \text{ for } 0.167 \leq C \leq 0.33 \quad (3)$$

$$\text{For } \underline{\text{DO}_{22}}, \frac{E}{NV_1} = \left(-3C + \frac{3}{4}\right) - \frac{V_2}{V_1} \left(3C - \frac{1}{2}\right) \text{ for } 0.25 \leq C \leq 0.375 \quad (4)$$

By use of these equations, the energy of mixing was calculated for the three structures for different values of the ratios  $V_2/V_1$ . From Fig. 8, which shows the results of such a calculation for  $V_2/V_1 = 0.4$ , it can be seen that the configurational energies of the  $\text{Ni}_4\text{Mo}$ ,  $\text{Ni}_2\text{Mo}$ , and  $\text{DO}_{22}$  structures are nearly equal; and at 25 at % solute those of  $\text{Ni}_2\text{Mo}$  and  $\text{Ni}_4\text{Mo}$  are almost identical. Because of the approximations involved in Richards [14] calculations in arriving at the configurational energies, there may be an error of 10—15% in the estimated values. Hence it is rather

difficult to say which of the three structures  $DO_{22}$ ,  $Ni_2Mo$ , or  $Ni_4Mo$  has the lowest energy. All we can really say is that the energies of the three structures are close to one another. The most recent calculation by Allen and Cahn [16], who used a cluster method, indeed show that for  $V_1 > 0$  and  $0 \leq (V_2/V_1) \leq 0.5$  the ground-state structure is a polyphase mixture of  $A_5B$  (which is same as  $Ni_2Mo$  at a different stoichiometry see Richards [14]),  $Ni_4Mo$ , and  $DO_{22}$  structures. According to them the energy of mixing of the polyphase mixture of the three structures  $Ni_2Mo$ ,  $Ni_4Mo$ , and  $DO_{22}$  can be written as

$$\frac{E}{NV_1} = -6C + 3C\left(\frac{V_2}{V_1}\right) - \left(\frac{V_2}{V_1}\right) \text{ for } 0.167 \leq C \leq 0.25. \quad (5)$$

The configuration energy obtained from this equation is also shown in Fig. 8 for  $V_2/V_1 = 0.4$ . It may be noted that these values are very close to those calculated from Richards' equations. In these calculations, the value of  $V_2/V_1 = 0.4$  has been chosen as an example because in our earlier [13] computation of diffuse sro scattering maps for  $Ni_3Mo$  by use of the Clapp-Moss theory [20] it was seen that the ratio  $V_2/V_1 = 0.4$  gave reasonable agreement with the experimental diffuse-scattering results.

The experimental results presented in the present paper are in qualitative agreement with the above thermodynamic predictions. At the same time, the thermodynamic calculations plausibly explain why  $Ni_2Mo$  and  $Ni_4Mo$  phases form during the decomposition of  $Ni_3Mo$  and also explain the presence of  $Ni_2Mo$  phase at  $Ni_4Mo$  composition. Now since thermodynamic calculations predict that the configurational energy for the  $DO_{22}$  structure should be similar to those for  $Ni_2Mo$  and  $Ni_4Mo$  (Fig. 8), one may question why this structure is not observed as a metastable phase. It has been shown earlier [8, 13] that the presence of  $\{1\frac{1}{2}0\}$  sro spots in Ni-Mo

alloys can be interpreted as due to imperfectly ordered microdomains based on  $DO_{22}$  structure. The microdomains observed in the dark-field micrographs of  $\{1\frac{1}{2}0\}$  spots in  $Ni_4Mo$  [2, 8] and in  $Ni_3Mo$  [13] at the very early stages of ordering predominantly consist of imperfectly ordered regions of  $DO_{22}$ . The presence of weak  $Ni_2Mo$  and  $Ni_4Mo$  superlattice reflection shows that some microdomains with these structures also coexist [13]. Thus these experimental results are in agreement with the thermodynamic predictions [14-16]. On further aging of the quenched Ni-Mo alloys, local composition fluctuations may continuously transform the  $DO_{22}$  regions to  $Ni_2Mo$  and  $Ni_4Mo$  that have similar energies. In the case of  $Ni_3Mo$ , the stoichiometry is easily balanced if both  $Ni_2Mo$  and  $Ni_4Mo$  form simultaneously side by side.

Apart from the thermodynamic reasoning, a close examination of the  $Ni_2Mo$  and  $Ni_4Mo$  structures shows why  $Ni_2Mo$  can be present in  $Ni_4Mo$ . It has been shown earlier [8] that the  $DO_{22}$  structure can be formed from  $D1a$  by introducing APBs of the nonconservative type. In a similar manner,  $Ni_2Mo$  structure can also be created from  $Ni_4Mo$  and vice versa. Figure 9 shows an example in which an APB of the type  $(420)\frac{1}{2}[\bar{1}01]$  has been introduced on the (420) plane in the fully ordered  $D1a$  structure. The notations used are the same as those in Fig. 1. The introduction of such an APB is equivalent to removing two layers of {420} planes containing Ni atoms exclusively. A comparison of the area in the vicinity of the APB with Fig. 1 shows that the structure locally transforms to  $Ni_2Mo$  type, as if a platelet of thickness  $3d_{420}$  is formed on the (420) plane. Some of these local regions may act as nuclei for  $Ni_2Mo$  phase; some may grow and some may stay as platelets. The observation of the weak  $\langle 210 \rangle$  streaks extending from one superlattice reflection to another with a maximum at the  $Ni_2Mo$  position in Fig. 4A for  $Ni_3Mo$  and in Figs. 5 and 6C for  $Ni_4Mo$  can now be explained as being due to these thin plate-like  $Ni_2Mo$  regions formed on {420} planes.



## 6. Conclusions

- 1) During the initial stages of ordering of  $\text{Ni}_3\text{Mo}$ , both  $\text{Ni}_2\text{Mo}$  and  $\text{Ni}_4\text{Mo}$  occur as metastable phases. The  $\text{Ni}_2\text{Mo}$  phase forms as plate-like particles on {420} planes but  $\text{Ni}_4\text{Mo}$  phase is more or less equiaxed.
- 2) The  $\text{Ni}_2\text{Mo}$  phase also occurs as a metastable phase during ordering of  $\text{Ni}_4\text{Mo}$ , but its volume fraction is restricted.
- 3) The experimental results support the thermodynamic predictions that the ground-state structures in Ni-Mo alloys in the composition range 16—25 at % Mo is a polyphase mixture. The thermodynamic calculations explain why  $\text{Ni}_2\text{Mo}$  occurs as a metastable phase during the ordering of Ni-Mo alloys.
- 4) A structural model based on the presence of nonconservative APBs shows that such APBs are nuclei for  $\text{Ni}_2\text{Mo}$  phase in stoichiometric  $\text{Ni}_4\text{Mo}$ .

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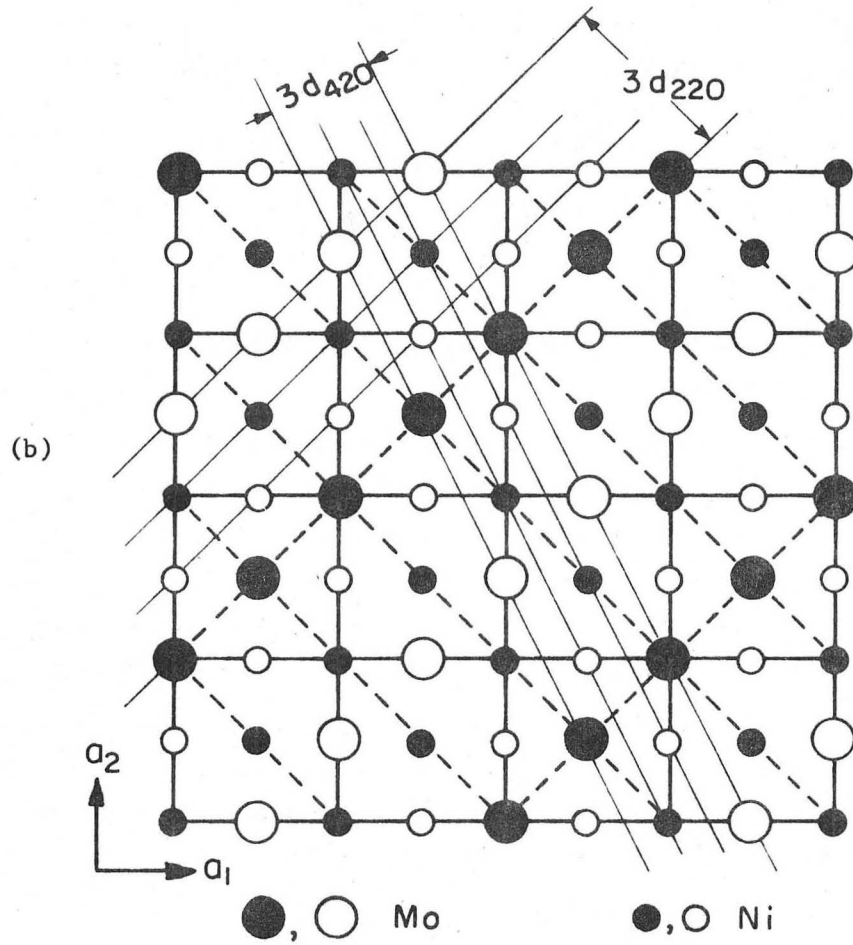
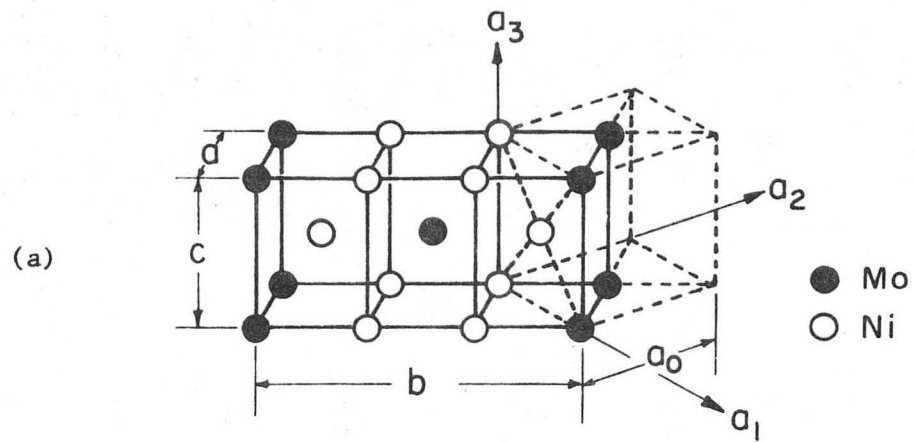
FIGURE CAPTIONS

- Fig. 1. The crystal structure of ordered  $\text{Ni}_2\text{Mo}$ : (a) the orthorhombic unit cell as derived from the original fcc lattice and (b) the atomic packing on the (001) plane.
- Fig. 2. The [001] diffraction patterns from a  $\text{Ni}_3\text{Mo}$  sample. Photographs (A) and (B) were obtained after aging at  $650^\circ\text{C}$  for 4 h and 49 h, respectively. The diagram (C) is the indexed pattern. The arrows in (A) point to the relrods corresponding to  $\text{Ni}_4\text{Mo}$  reflections.
- Fig. 3. (A) The  $[\bar{1}20]$  diffraction pattern of a  $\text{Ni}_3\text{Mo}$  sample after aging for 49 h at  $650^\circ\text{C}$ . (B) Dark field micrograph of  $\text{Ni}_2\text{Mo}$  spot whose position is shown in (A) by the superimposed image of the objective aperture, (C) the indexed  $[\bar{1}20]$  pattern.
- Fig. 4. (A) The [121] diffraction pattern of  $\text{Ni}_3\text{Mo}$  sample after aging at  $650^\circ\text{C}$  for 4 h. (B) The indexed pattern corresponding to one quadrant of the diffraction pattern in (A).
- Fig. 5. The [001] diffraction pattern of  $\text{Ni}_4\text{Mo}$  sample after aging at  $650^\circ\text{C}$  for 8 h. The single black-white arrows point to the weak  $\text{Ni}_2\text{Mo}$  superlattice reflections and the small double arrows point to the relrods from  $\text{Ni}_4\text{Mo}$  reflections.
- Fig. 6. Micrographs of  $\text{Ni}_4\text{Mo}$  sample after aging for 8 h at  $650^\circ$ : (A) bright-field micrograph, (B) dark-field micrograph of  $\text{Ni}_4\text{Mo}$  superlattice spot marked b in the [121] diffraction pattern shown in (C), which corresponds to the area in Fig. 6(A). In (C) the foil has been tilted from that in (A) to obtain a symmetrical diffraction pattern. The single large black-white arrows in (C) point to weak  $\text{Ni}_2\text{Mo}$  superlattice reflections and the small double arrows are double diffraction spots from  $\text{Ni}_4\text{Mo}$ .

Fig. 7. Microstructure of  $\text{Ni}_4\text{Mo}$  after aging for 24 h at  $650^\circ\text{C}$ . Note the heterogeneous reaction at the grain boundary.

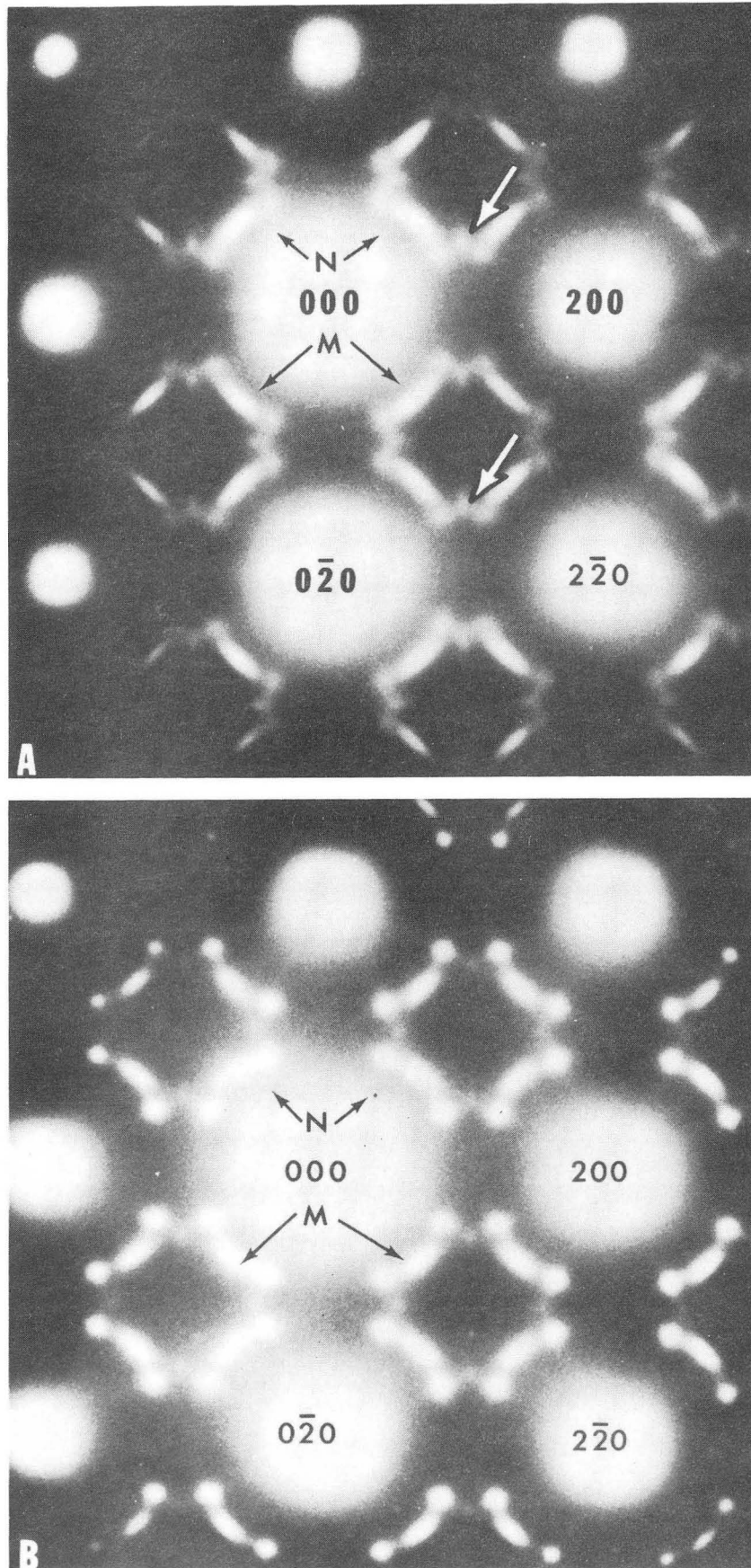
Fig. 8. The theoretical curves for energy of mixing versus composition for  $\text{DO}_{22}$ ,  $\text{Ni}_4\text{Mo}$  and  $\text{Ni}_2\text{Mo}$  structures calculated using  $\frac{V_2}{V_1} = 0.4$ .

Fig. 9. An APB model showing how the  $\text{Ni}_2\text{Mo}$  structure can be derived from  $\text{Ni}_4\text{Mo}$  structure by introducing a non-conservative APB of the type  $(420)\frac{1}{2}[\bar{1}01]$ .



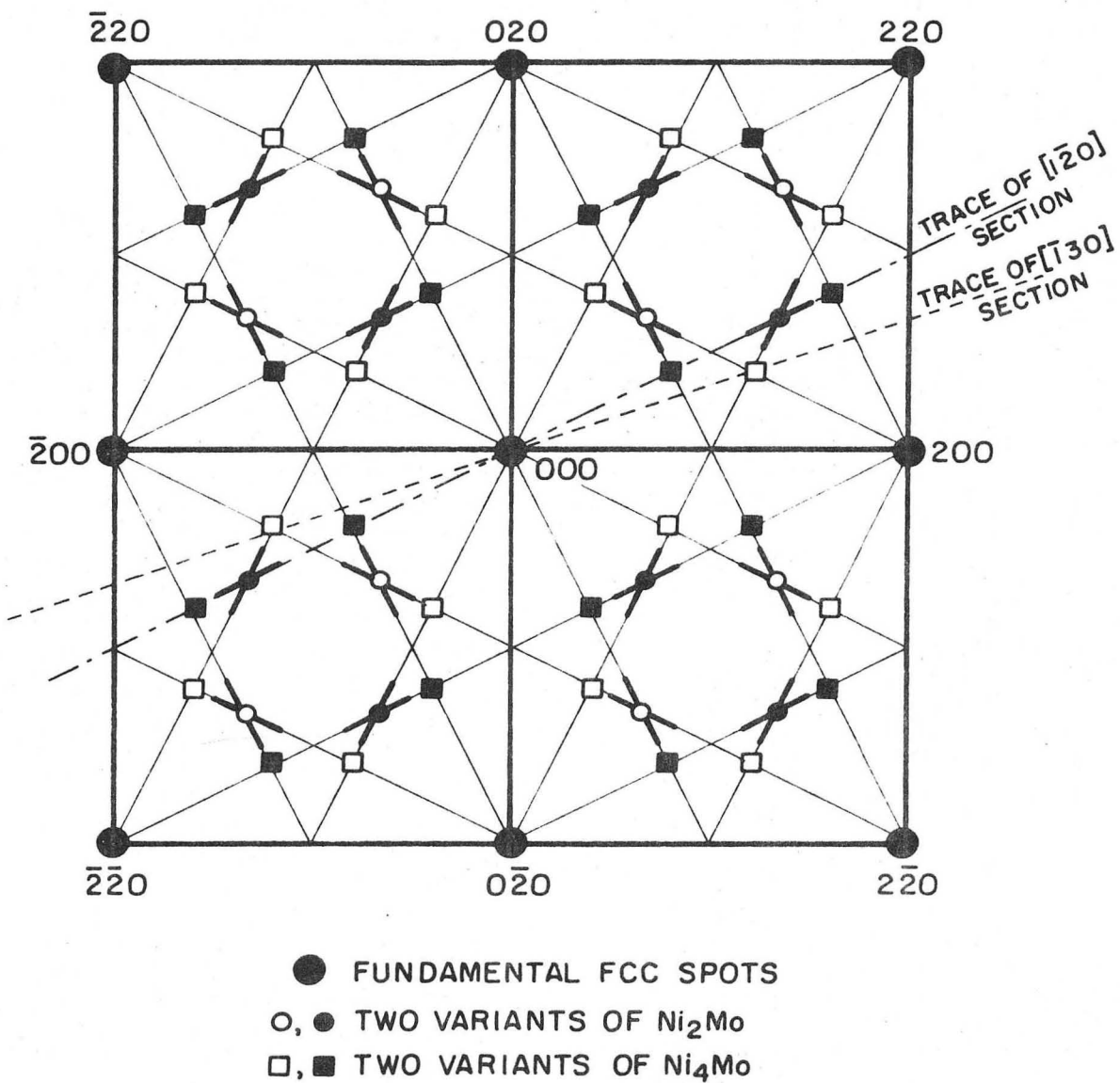
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Fig. 1



XBB 738-4980

Fig. 2



XBL 717-1217

Fig. 2c



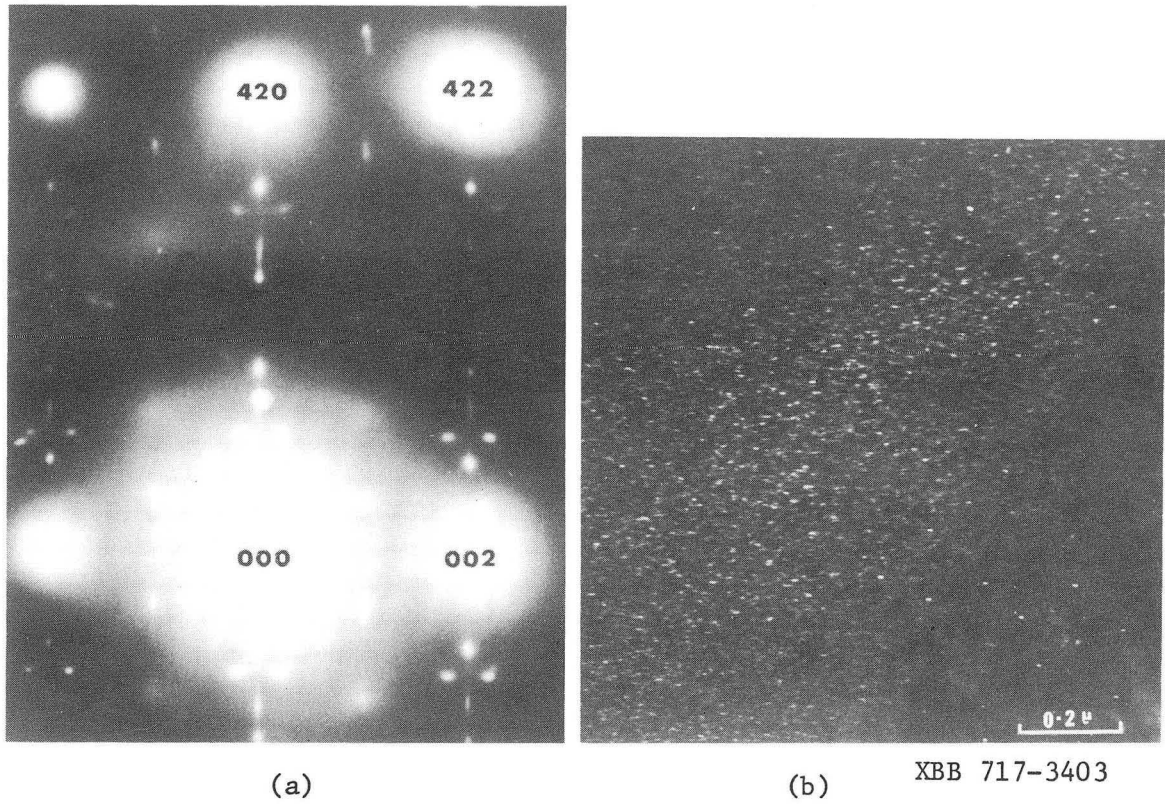
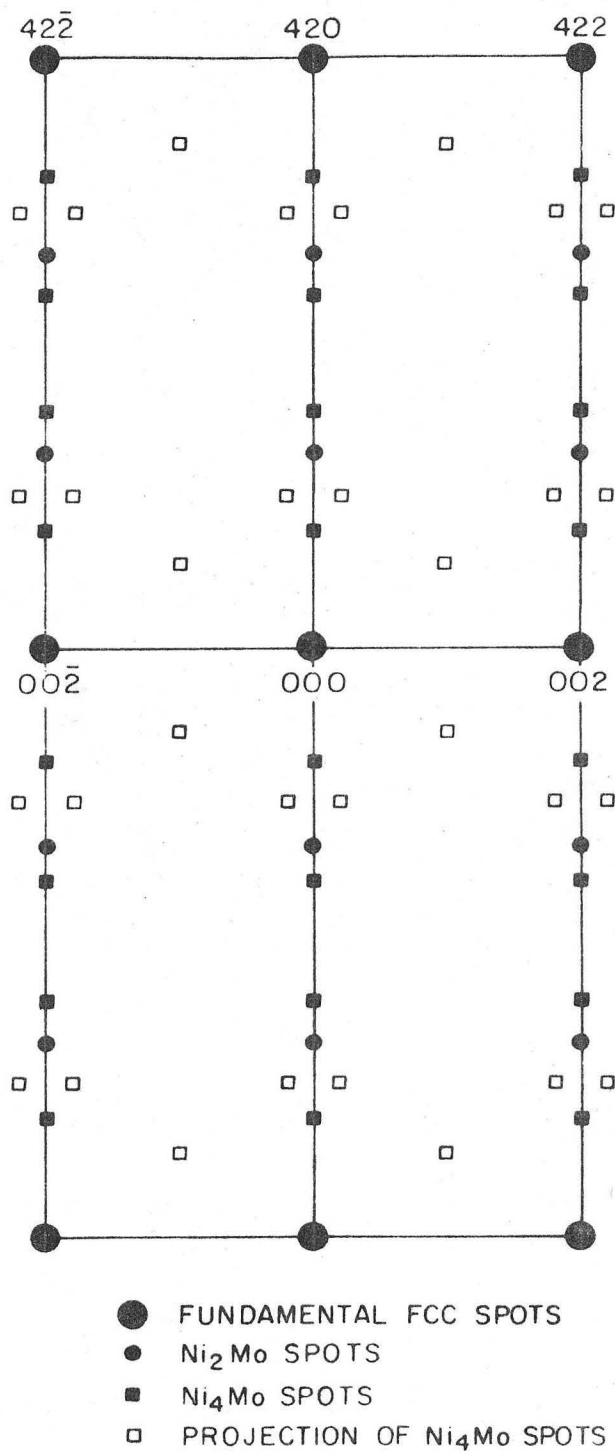
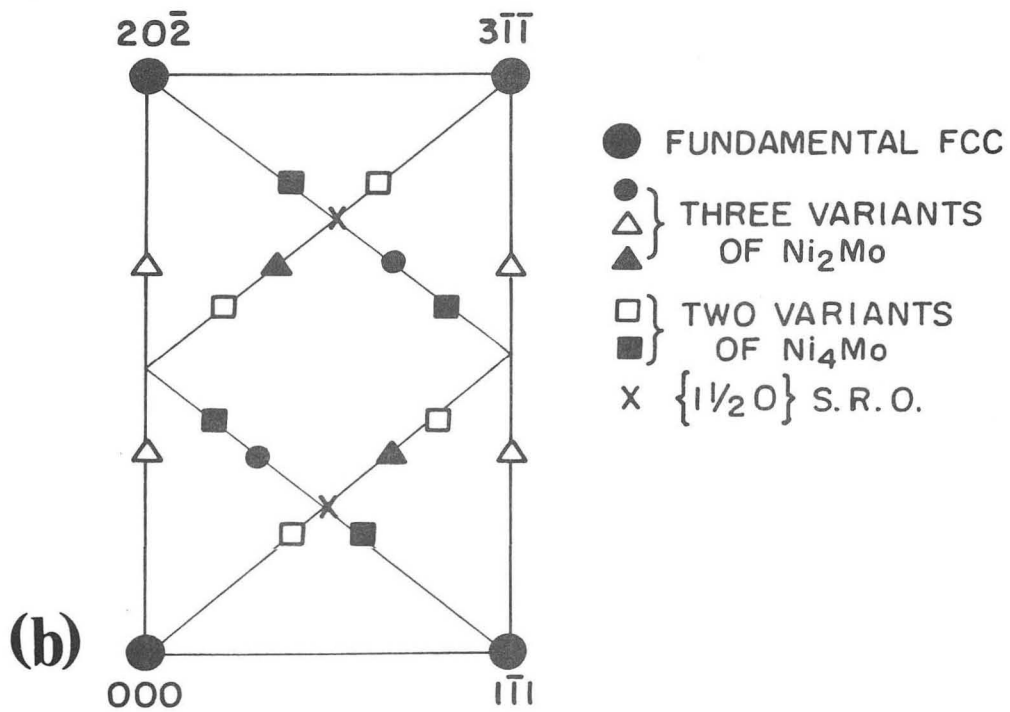
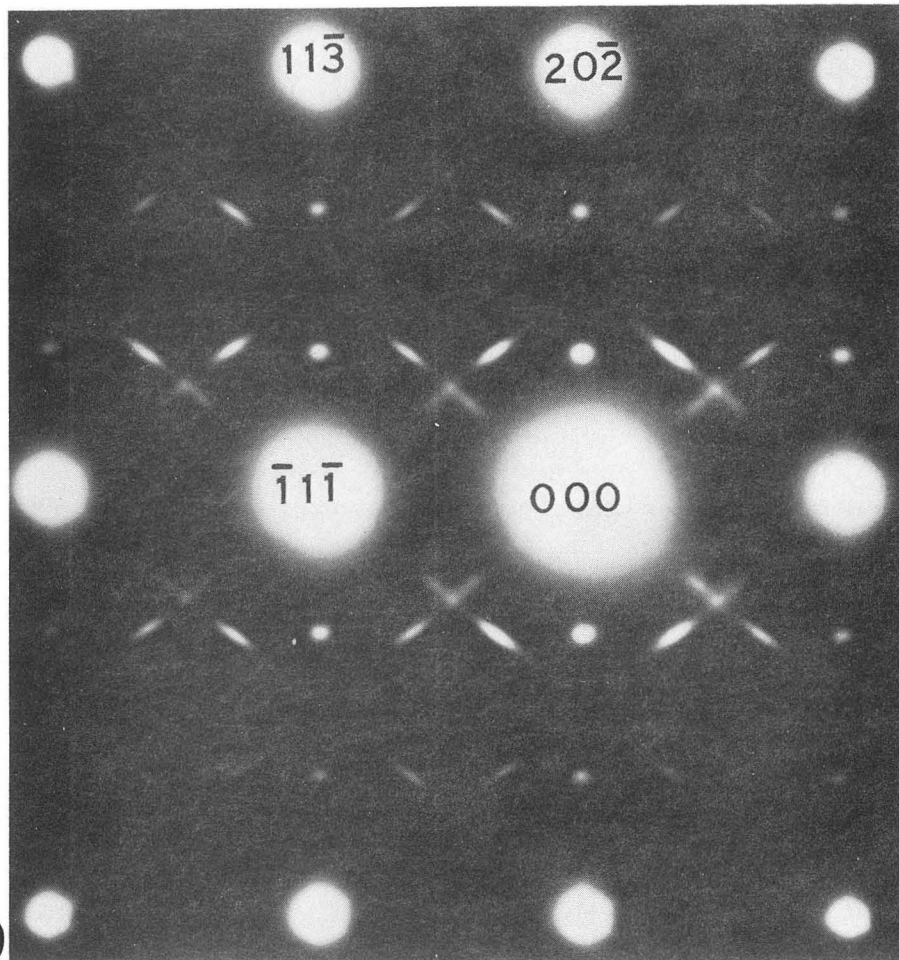


Fig. 3 a,b



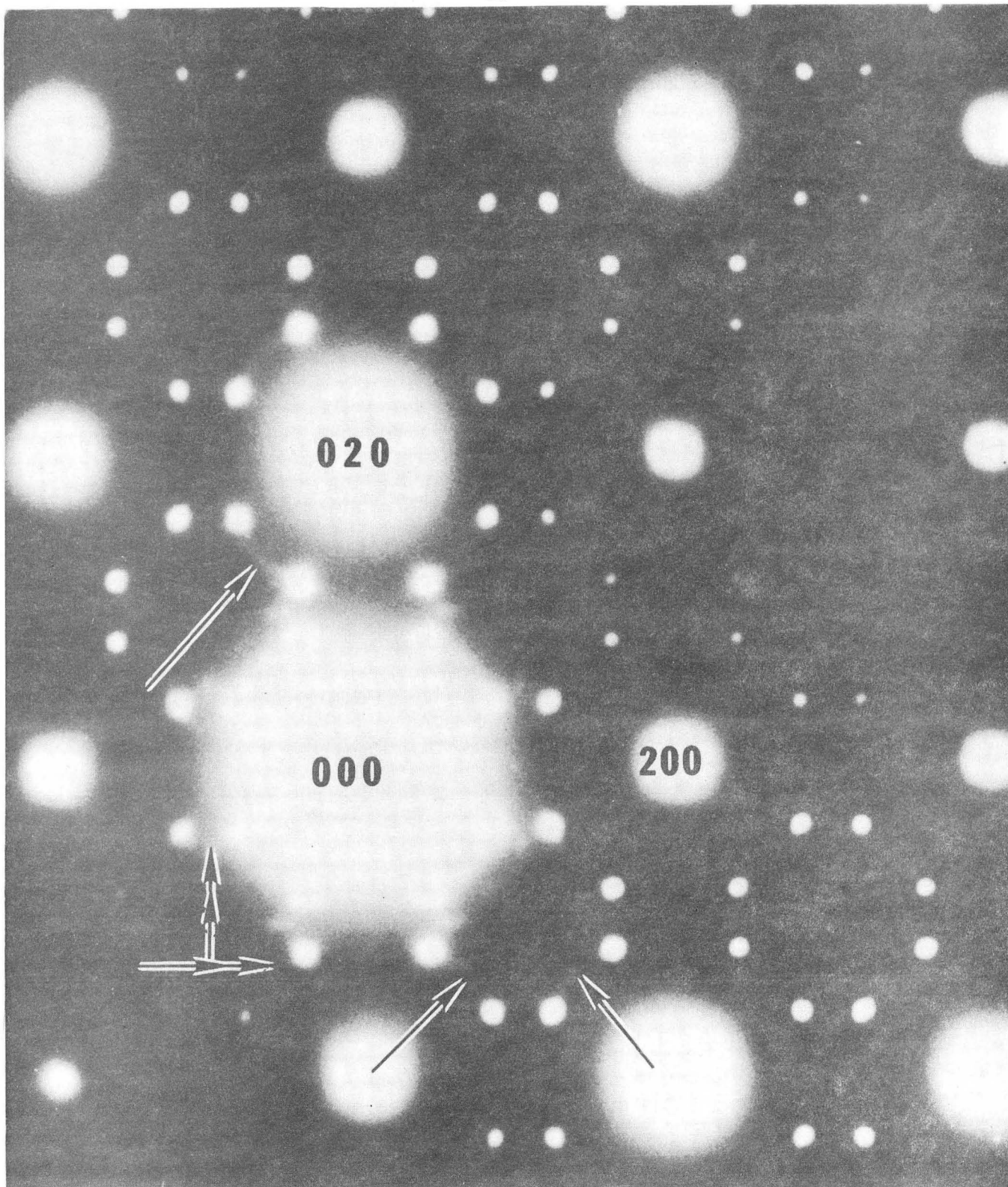
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Fig. 3c



XBB 717-3398

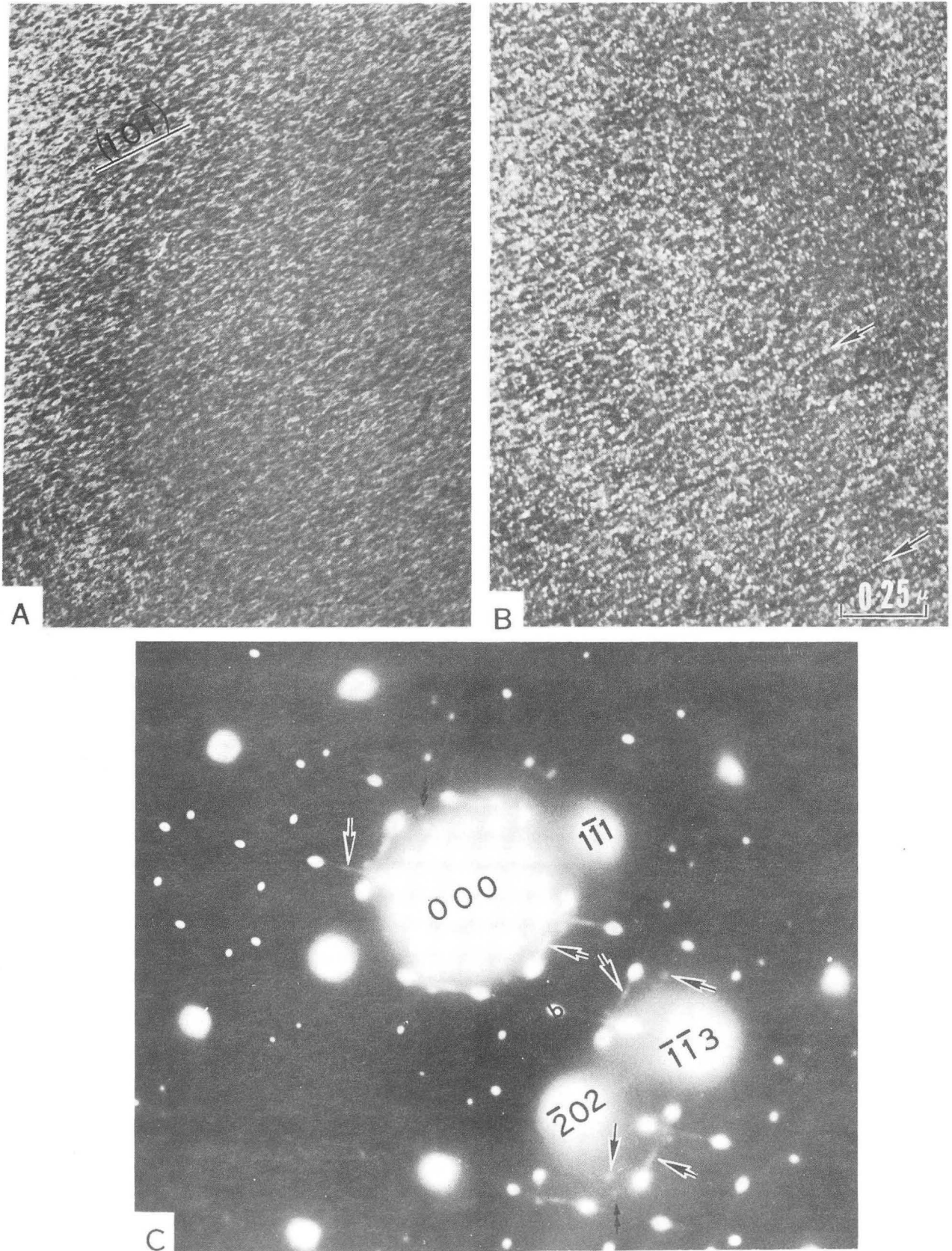
Fig. 4



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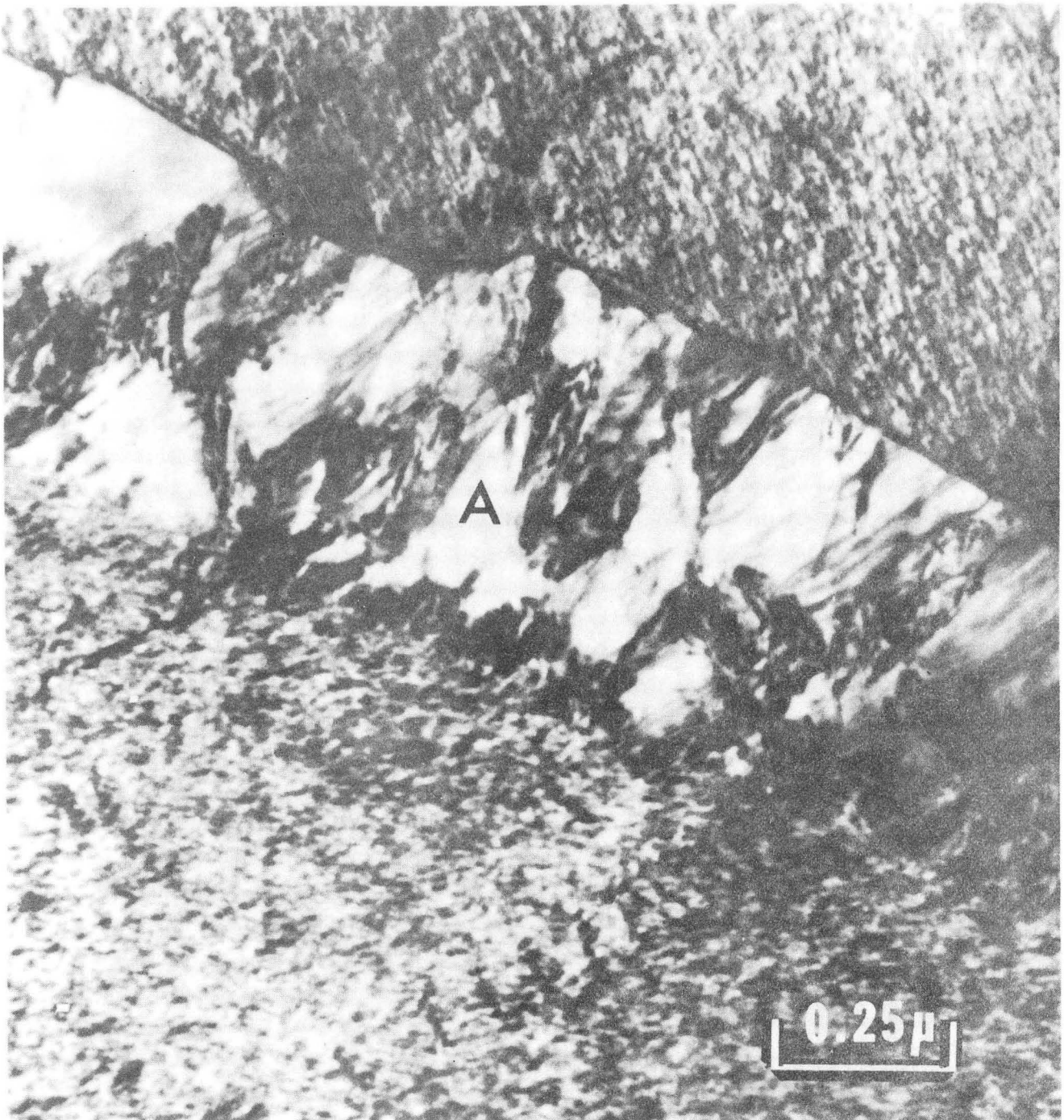
Fig. 5





XBB 738-4981

Fig. 6



XBB 738-4982

Fig. 7

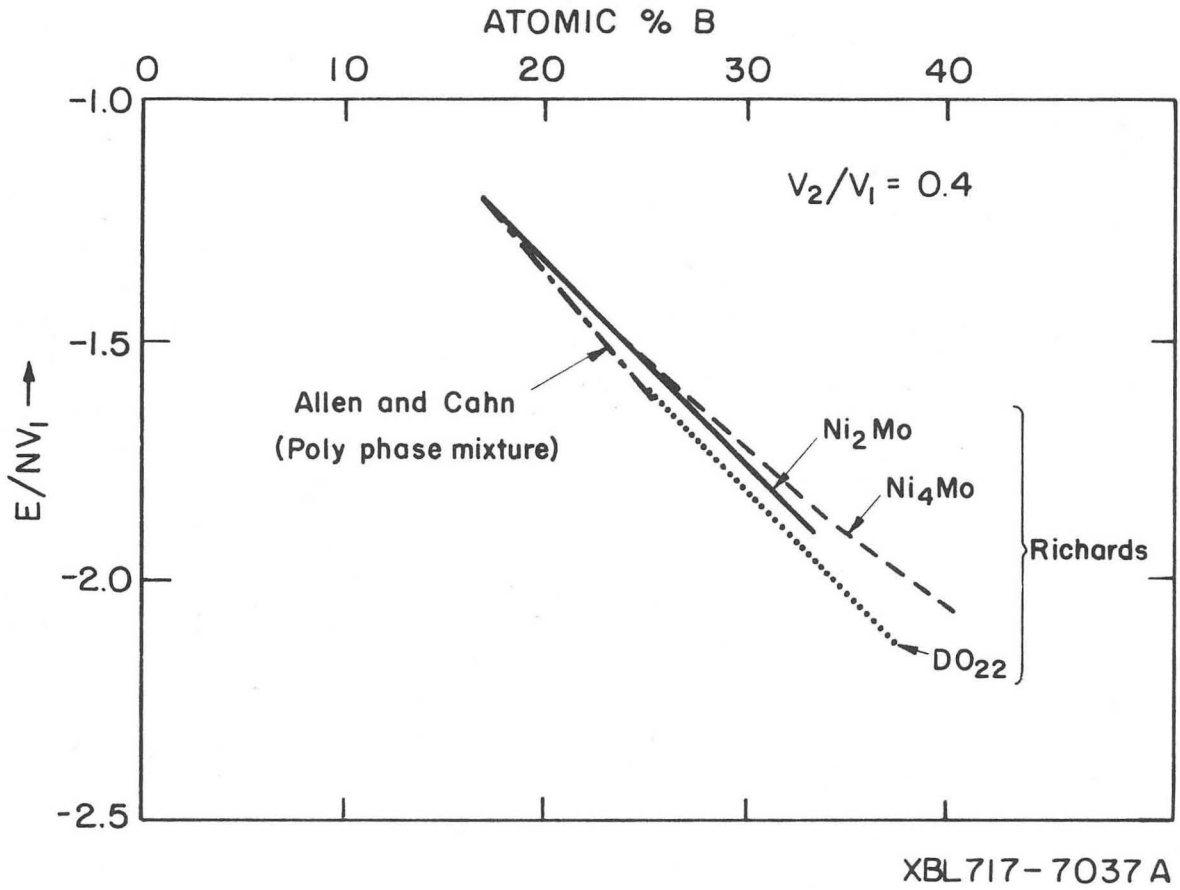
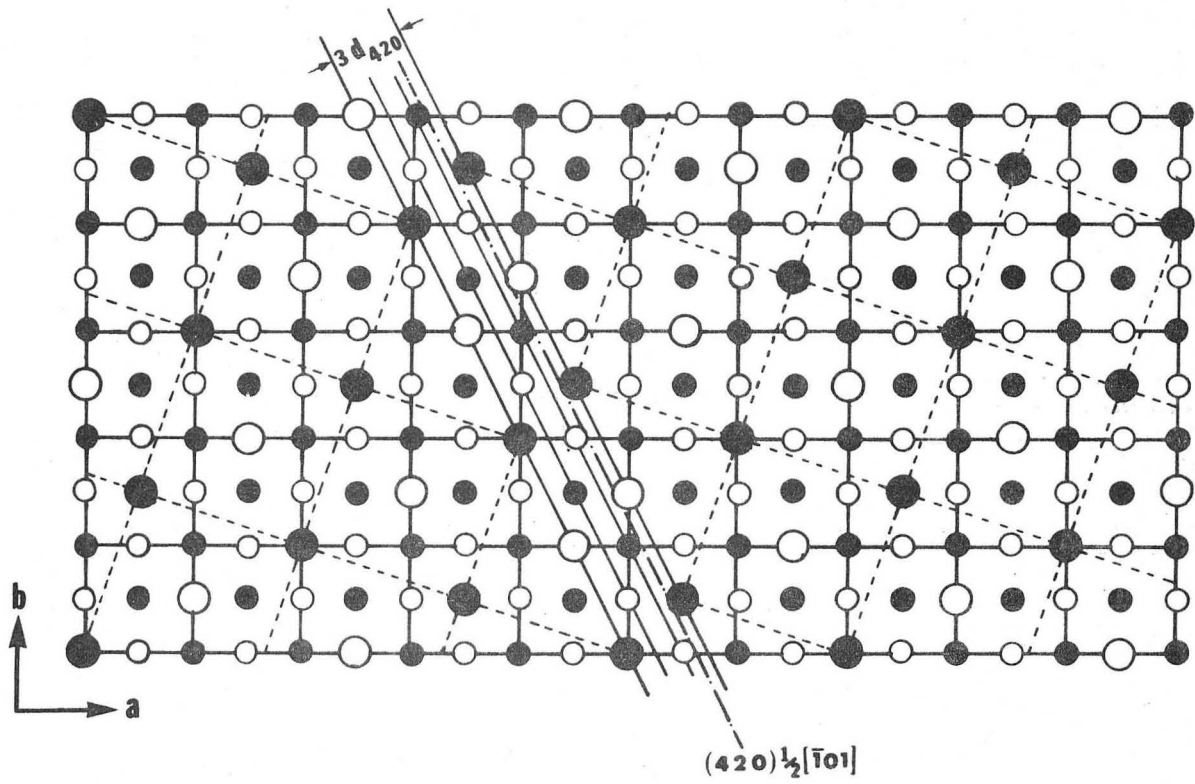


Fig. 8



XBL 717-1216

Fig. 9



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