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### Permalink

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### Journal

Solid State Communications, 32(4)

### ISSN

0038-1098

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### Publication Date

1979-10-01

### DOI

10.1016/0038-1098(79)90949-9

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Peer reviewed

COEXISTENCE OF SUPERCONDUCTIVITY AND ANTIFERRO-  
MAGNETIC ORDER IN  $\text{SmRh}_4\text{B}_4$

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(Received 26 June 1979 by H. Suhl)

The ternary rare earth compound  $\text{SmRh}_4\text{B}_4$  has been studied by means of upper critical field, low temperature specific heat, and static magnetic susceptibility measurements. A lambda-type specific heat anomaly, a discontinuity in the slope of the upper critical field versus temperature curve, and a cusp-like feature in the magnetic susceptibility suggest that superconductivity and long-range antiferromagnetic order coexist in  $\text{SmRh}_4\text{B}_4$  below 0.87 K. Machida's theory for antiferromagnetic superconductors provides a good description of the upper critical field data, while the magnetic susceptibility data can be represented as the sum of a Curie-Weiss term with  $\mu_{\text{eff}} = 0.632 \mu_B$  and  $\theta_p = -1.93$  K and a temperature independent Van Vleck contribution.

The class of ternary rare earth (RE) compounds  $\text{RERh}_4\text{B}_4$  has recently been investigated in order to study the interaction between superconductivity and long-range magnetic order. The compounds are ferromagnetic for RE = Gd, Tb, Dy and Ho and superconducting for RE = Sm, Nd, Er, Tm, and Lu.<sup>1,2</sup> Furthermore,  $\text{ErRh}_4\text{B}_4$  exhibits re-entrant superconductivity, wherein the superconductivity is destroyed by the onset of long-range ferromagnetic ordering of the  $\text{Er}^{3+}$  magnetic moments at a temperature  $T_{C2}$  below the superconducting transition temperature  $T_{C1}$ .<sup>3,4</sup> Recently we reported the results of an investigation of  $\text{NdRh}_4\text{B}_4$  which revealed two lambda-type anomalies in the heat capacity data, indicative of two phase transitions below the superconducting transition temperature.<sup>5</sup> Features in the upper critical field vs. temperature curve and the static magnetic susceptibility data suggest that the phase transitions are magnetic, and therefore that superconductivity and long-range magnetic order coexist in this compound. However, the presence of impurity phases prevented an unambiguous determination of the exact nature of the magnetic ordering.

The observation of superconductivity and magnetism in both  $\text{ErRh}_4\text{B}_4$  and  $\text{NdRh}_4\text{B}_4$  sug-

gests that the other superconducting  $\text{RERh}_4\text{B}_4$  compounds containing localized magnetic moments might also order magnetically. In this communication we report upper critical field, specific heat, and static magnetic susceptibility data for  $\text{SmRh}_4\text{B}_4$ . The results indicate that long-range antiferromagnetic order and superconductivity coexist in this material below 0.87 K.

Two samples of  $\text{SmRh}_4\text{B}_4$  were synthesized by arc melting the high purity elements under argon. The samples were annealed at 1200°C for more than a week, followed by an additional week at 800°C. The first sample was used for four-probe ac electrical resistance and static magnetic susceptibility measurements. In the former experiment a long parallelepiped-shaped sample aligned parallel to various applied magnetic fields was cooled using a  $\text{He}^3$ - $\text{He}^4$  dilution refrigerator to obtain temperatures from below 0.07 to 10 K. The magnetic susceptibility data were taken between 0.7 and 294 K using a Faraday magnetometer. Heat capacity data for the second sample were obtained between 0.5 and 36 K with a  $\text{He}^3$  semi-adiabatic calorimeter using a standard heat-pulse technique.

Figure 1 shows the electrical resistance

\* Research supported by the U. S. Department of Energy under Contract Number EY-76-S-03-0034-PA227-3.

† Research supported by the National Science Foundation under Grant Number NSF/DMR77-08469.

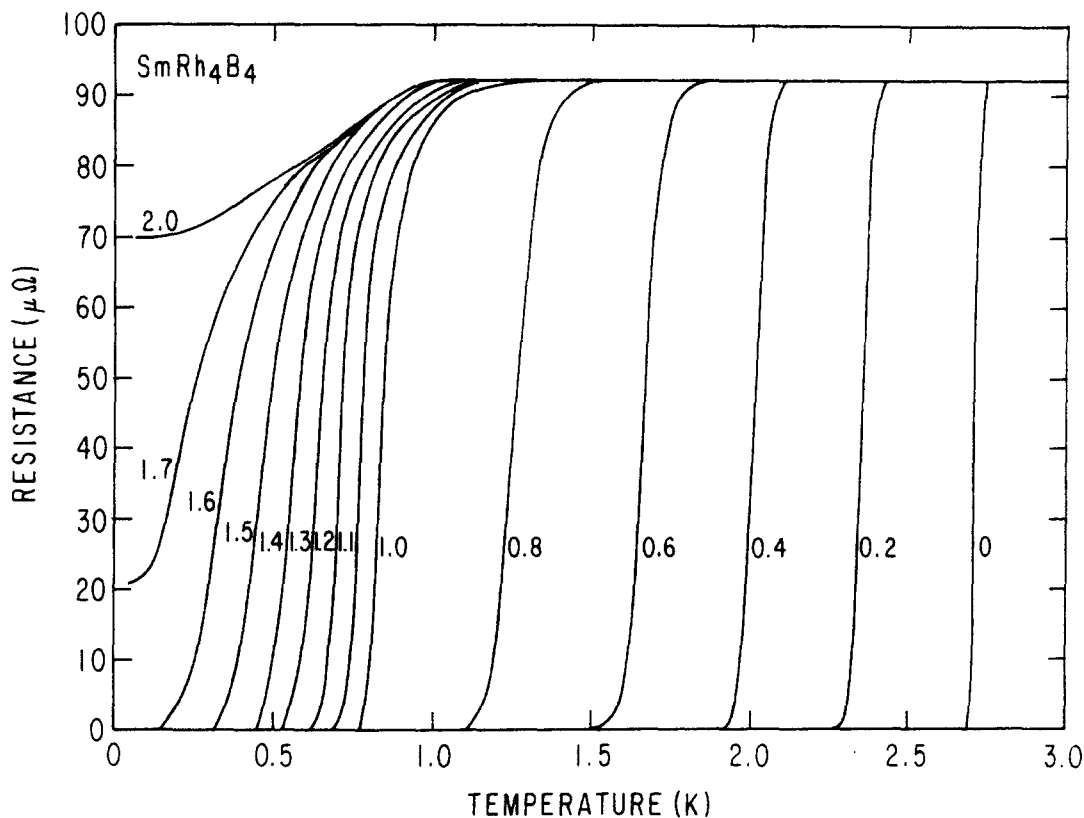


Fig. 1 ac electrical resistance versus temperature for  $\text{SmRh}_4\text{B}_4$  in applied magnetic fields between 0 and 2 kOe.

vs temperature in various applied magnetic fields for  $\text{SmRh}_4\text{B}_4$ . In all fields measured below its zero-temperature upper critical field  $H_{c2}(0) \sim 1.85$  kOe, the sample exhibits only a single normal to superconducting state transition. The normal state resistance, however, markedly decreases below 0.9 K, indicative of some type of phase transition below the zero field superconducting transition temperature  $T_c = 2.72$  K. The upper critical field  $H_{c2}$  vs temperature data shown in Fig. 2 seem to support this hypothesis. The transition temperatures were defined as the temperatures at which the sample resistance became fifty percent of the normal state value. The  $H_{c2}$  vs temperature curve shows a sharp discontinuity in its slope at approximately 0.85 K; below this temperature  $H_{c2}$  is considerably larger than would be expected from the high temperature portion of the curve.

Shown in Fig. 3 is the heat capacity  $C$  vs temperature data for  $\text{SmRh}_4\text{B}_4$  between 0.5 and 9 K in zero applied magnetic field. The data reveal a small jump in the heat capacity at the superconducting transition temperature ( $T_c = 2.72$  K) and a pronounced lambda-type anomaly which peaks at a temperature  $T_\lambda \approx 0.87$  K.

Comparison of the heat capacity data with the upper critical field data shows that  $T_\lambda$  corresponds closely with the temperature at which the discontinuity in the slope of the  $H_{c2}$  vs temperature curve occurs. Subtracting the electronic and lattice contributions to the specific heat of the isostructural nonmagnetic compound  $\text{LuRh}_4\text{B}_4$  results in a magnetic entropy between 0 and 16 K of  $S_{\text{mag}} \approx R \ln 2$ , which suggests that the crystal field ground state of the  $\text{Sm}^{3+}$  ions is a doublet.

A plot of the reciprocal molar magnetic susceptibility  $\chi_M^{-1}$  vs temperature for  $\text{SmRh}_4\text{B}_4$  is shown in Fig. 4. The data cannot be described by a simple Curie-Weiss law, which is consistent with the  $\text{Sm}^{3+}$  ions having relatively low-energy angular momentum states above the Hund's rule ground state. Therefore, a least squares fit of the data above 0.87 K was made to the function

$$\chi_M^{-1} = \frac{N_A}{k_B} \left[ \frac{u_{\text{eff}}^2}{3(T - \theta_p)} + \frac{u_B^2}{\delta} \right], \quad (1)$$

where  $N_A$  is Avogadro's number,  $k_B$  is Boltz-

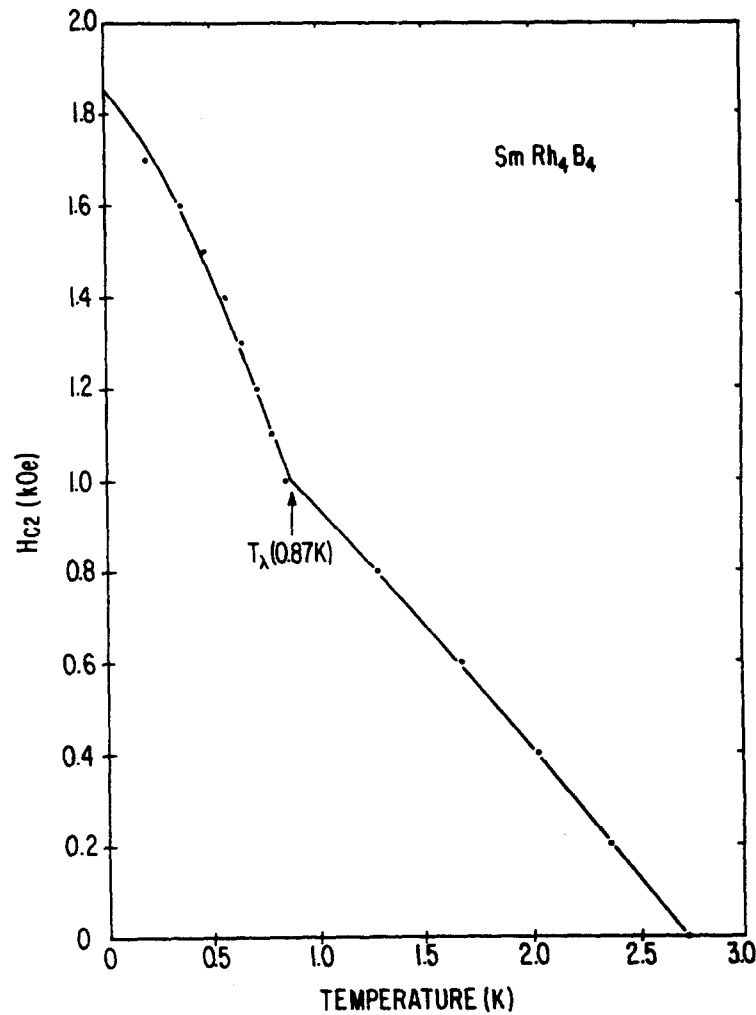


Fig. 2 Upper critical field  $H_{c2}$  versus temperature for  $\text{SmRh}_4\text{B}_4$ . The arrow represents the transition temperature defined by the lambda-type anomaly observed in the heat capacity data. The curve represents a fit of the data to Machida's theory<sup>8</sup> for antiferromagnetic superconductors.

mann's constant,  $\mu_B$  is the Bohr magneton,  $\mu_{\text{eff}}$  is the effective magnetic moment, and  $\theta_p$  is the Curie-Weiss temperature.<sup>6</sup> The first term represents a Curie-Weiss contribution from the  $J=5/2$  ground state, while the second term is the temperature independent Van Vleck correction arising from the accessible first excited angular momentum  $J=7/2$  state. In the absence of crystal field effects,  $\mu_{\text{eff}} = g_J \sqrt{J(J+1)} \mu_B = 0.845 \mu_B$ , where  $g_J$  is the Landé g-factor, and  $\delta = 7 \Delta E / 20$ , where  $\Delta E$  is the difference in energy between the  $J=5/2$  and  $J=7/2$  angular momentum states. Using

the best fit parameters of  $\mu_{\text{eff}} = 0.632 \mu_B$ ,  $\theta_p = -1.93$  K, and  $\delta = 377$  K, Eq. (1) describes the data reasonably well, as shown in Fig. 4. However, the effective magnetic moment  $\mu_{\text{eff}} = 0.632 \mu_B$  is considerably less than the  $0.845 \mu_B$  free ion value for the  $J=5/2$  Hund's rule ground state of  $\text{Sm}^{3+}$ , while  $\delta = 377$  K corresponds to  $\Delta E = 1080$  K, a value somewhat less than but comparable to the  $\sim 1500$  K value estimated for free  $\text{Sm}^{3+}$  ions.<sup>7</sup> In contrast, the magnetic susceptibilities of  $\text{ErRh}_4\text{B}_4$ <sup>3</sup> and  $\text{NdRh}_4\text{B}_4$ <sup>5</sup> yielded effective magnetic moments nearly equal to their free ion values. The re-

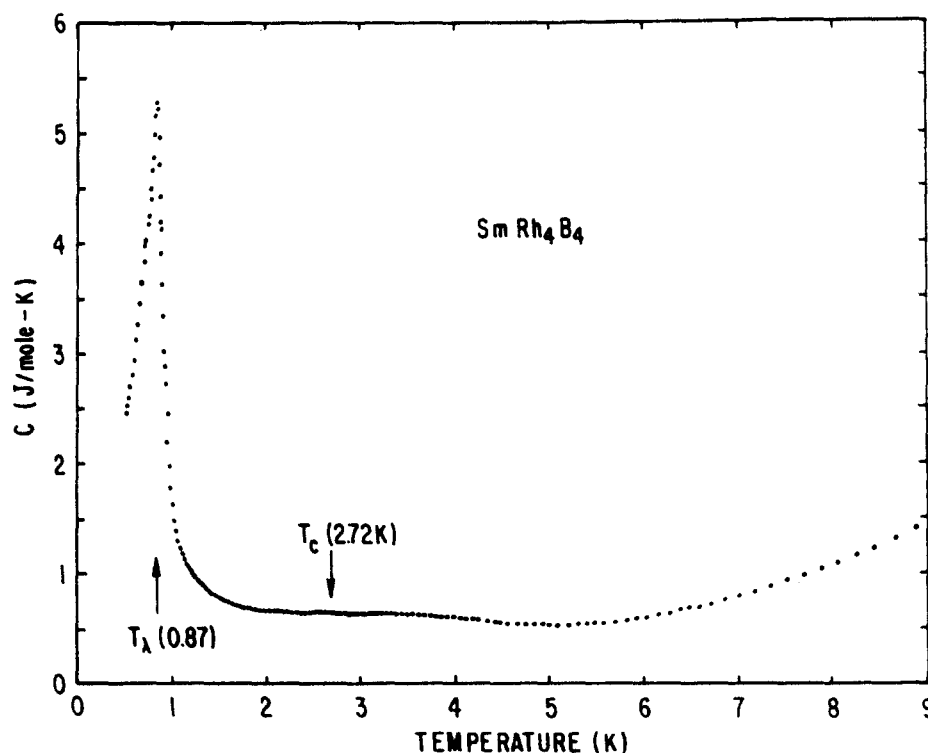


Fig. 3 Specific heat  $C$  versus temperature for  $\text{SmRh}_4\text{B}_4$  in zero applied magnetic field.

duced value of  $\mu_{\text{eff}}$  for  $\text{SmRh}_4\text{B}_4$  is consistent with the specific heat data which revealed crystal field splitting of the Hund's rule ground state energy levels. The magnetic susceptibility curve also exhibits a cusp-like feature near  $T_\lambda$ , indicative of an antiferromagnetic transition at this temperature.

The ac electrical resistance, upper critical field, specific heat, and magnetic susceptibility data all indicate that  $\text{SmRh}_4\text{B}_4$  orders antiferromagnetically in the superconducting state at  $T_\lambda = 0.87$  K. This immediately suggests that the  $H_{c2}$  vs temperature data for  $\text{SmRh}_4\text{B}_4$  may provide a useful test of theories of antiferromagnetic superconductors, such as the one recently developed by Machida.<sup>8</sup> In Machida's model, which is an extension of the Abrikosov-Gor'kov theory,<sup>9</sup> the equation relating the upper critical field and the temperature is given by

$$\ln \frac{T}{T_{c0}} + \frac{1}{2} \left[ \left( 1 + \frac{b}{\sqrt{b^2 + h^2}} \right) \psi \left( \frac{1}{2} + \rho_- \right) + \left( 1 - \frac{b}{\sqrt{b^2 + h^2}} \right) \psi \left( \frac{1}{2} + \rho_+ \right) \right] - \psi \left( \frac{1}{2} \right) = 0, \quad (2)$$

where

$$\rho_\pm = \frac{1}{2\pi T} \left( \frac{1}{\tau(T)} + b + DeB \pm \sqrt{b^2 - h^2} \right) \quad (3)$$

and

$$h = \frac{g_{\text{J}} \mu_{\text{B}} I S_0(T)}{3k_{\text{B}} T} H + \mu_{\text{B}} B. \quad (4)$$

Here  $\psi$  is the digamma function,  $T_{c0}$  is the critical temperature in the absence of ions that carry magnetic moments,  $b = 1/\tau_{\text{so}}$  where  $\tau_{\text{so}}$  is the spin-orbit relaxation time,  $D = \tau_0 v_f^2/3$  is a diffusion constant where  $v_f$  is the Fermi velocity and  $\tau_0$  is the relaxation time associated with scattering of the conduction electrons by nonmagnetic impurities,  $e$  is electronic charge,  $I$  is the exchange integral characterizing the strength of the interaction between the local moments and the conduction electrons,  $\tau(T)$  is the temperature dependent relaxation time of the conduction electron system, and  $S_0$  is the  $q=0$  value for the spin-spin correlation function  $S_q = \langle \vec{J}_q \cdot \vec{J}_{-q} \rangle$ . The relation between  $S_0$  and  $\tau$  is given by

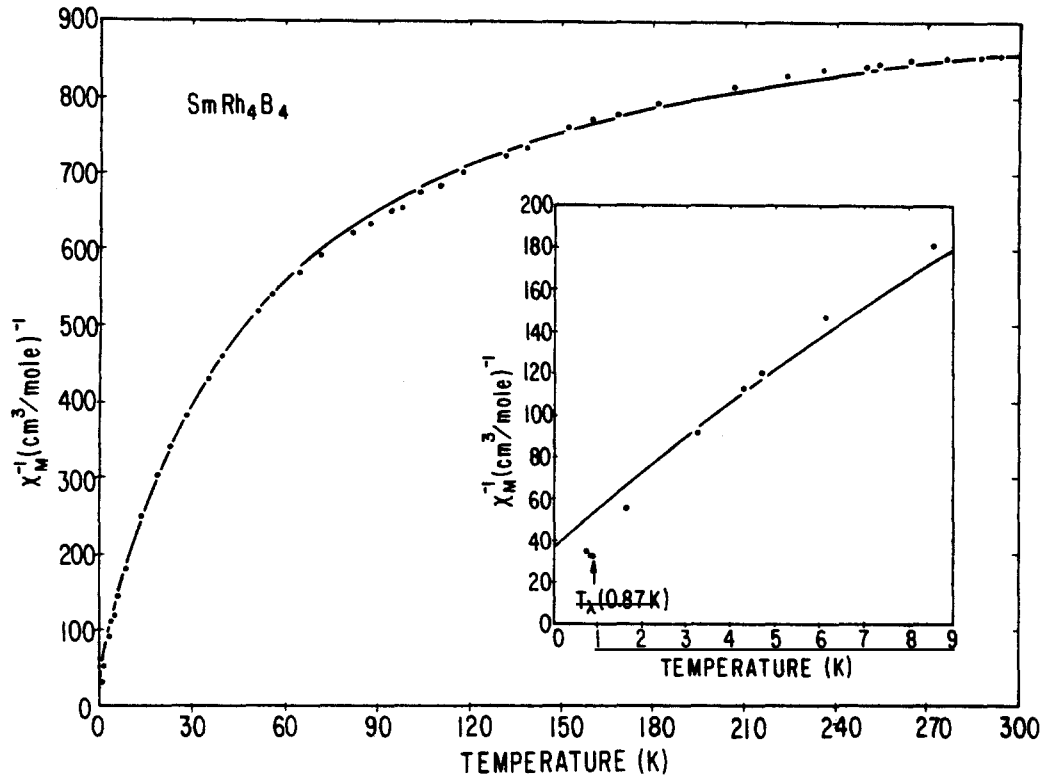


Fig. 4 Inverse magnetic susceptibility per mole  $\chi_M^{-1}$  versus temperature for  $\text{SmRh}_4\text{B}_4$ . The arrow represents the transition temperature defined by the lambda-type anomaly observed in the heat capacity data. The curve represents the sum of a Curie-Weiss law with  $\mu_{\text{eff}} = 0.632$  and  $\theta_p = -1.93$  K and a temperature independent Van Vleck term.

$$\frac{1}{\tau(T)} = 2\pi N(E_F) \left(\frac{I}{2}\right)^2 (g_J - 1)^2 S_0(T), \quad (5)$$

where  $N(E_F)$  is the density of states at the Fermi level, while  $S_0(T)$  is related to the magnetic susceptibility  $\chi$  by the expression

$$\chi = N \frac{g_J^2 \mu_B^2}{3k_B T} S_0, \quad (6)$$

where  $N$  is the number of magnetic moments per unit volume. For  $\chi$  the standard mean field theory expression<sup>10</sup> for an isotropic, polycrystalline antiferromagnetic material was adopted using the Hund's rule free ion values for  $g_J$  and  $J$  and assuming that both the Néel temperature and the magnitude of the Curie-

Weiss temperature were equal to  $T_\lambda$ . Although the magnetic susceptibility data seem to contradict these assumptions, this simplified model provides a qualitative description of the behavior of  $\chi$  at the temperatures  $T \leq 2.7$  K of interest here. The value used for  $N(E_F)$  was 0.57 states/eV-atom-spin direction, the density of states at the Fermi level for the isostructural nonmagnetic compound  $\text{LuRh}_4\text{B}_4$ ,<sup>11</sup> while  $N$  was calculated from the crystallographic data.<sup>2</sup>

The results of the numerical fit are shown in Fig. 2, with the optimum value of the parameters being  $1/\tau_{S_0} = 20.15$  K,  $De/\mu_B = 32.33$ ,  $T_{CO} = 4.95$  K, and  $I = 8.58 \times 10^{-3}$  eV-atom. The agreement between experiment and theory is excellent, especially in view of the simplifications discussed above. The enhancement of the upper critical field at low temperatures

therefore appears to be the result of the reduction of the net magnetization below  $T_\lambda$ . The value for  $I$  obtained here is roughly comparable to the value  $4 \times 10^{-2}$  eV-atom that was previously inferred from the rate of the depression of  $T_c$  with  $x$  in the pseudoternary system  $(\text{Lu}_{1-x}\text{Ho}_x)\text{Rh}_4\text{B}_4$ .<sup>12</sup> Also of interest is the small value of  $T_{c0}$  in comparison to the critical temperature of 11.6 K for  $\text{LuRh}_4\text{B}_4$ . If reliable, this significantly reduced value of  $T_c$  in the absence of magnetic pairbreaking interac-

tions suggests that the superconducting transition temperature of the tetragonal  $\text{RRh}_4\text{B}_4$  compounds depends sensitively on the lattice parameters.

#### Acknowledgment

The authors would like to thank Professor Kazushige Machida for discussions concerning his theory.

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