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# Evidence for even parity unconventional superconductivity in Sr<sub>2</sub>RuO<sub>4</sub>

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**Unambiguous identification of the superconducting order parameter symmetry in Sr<sub>2</sub>RuO<sub>4</sub> has remained elusive for more than a quarter century. While a chiral *p*-wave ground state analogue to superfluid <sup>3</sup>He-A was ruled out only very recently, other proposed triplet-pairing scenarios are still viable. Establishing the condensate magnetic susceptibility reveals a sharp distinction between even-parity (singlet) and odd-parity (triplet) pairing since the superconducting condensate is magnetically polarizable only in the latter case. Here field-dependent <sup>17</sup>O Knight shift measurements, being sensitive to the spin polarization, are compared to previously reported specific heat measurements for the purpose of distinguishing the condensate contribution from that due to quasiparticles. We conclude that the shift results can be accounted for entirely by the expected field-induced quasiparticle response. An upper bound for the condensate magnetic response of < 10% of the normal state susceptibility is sufficient to exclude all purely odd-parity candidates.**

unconventional superconductivity | triplet pairing | Knight shift | nuclear magnetic resonance | order parameter

Unraveling the secrets of the superconducting state in Sr<sub>2</sub>RuO<sub>4</sub> (1–3) has been a priority for unconventional superconductivity research since its discovery in 1994, by Maeno et al. (4). Among several reasons for broad interest in Sr<sub>2</sub>RuO<sub>4</sub> was the particularly notable suggestion of a *p*-wave triplet pairing state (5). One of the symmetry-allowed triplet states is the chiral state  $\mathbf{z}(p_x \pm ip_y)$ , which breaks time reversal symmetry and therefore requires two components. Soon after, the combination of results from NMR Knight shift (6) and  $\mu^+$ SR (7) measurements lent support to the chiral *p*-wave description. Further evidence was inferred from the observed onset of a nonzero Kerr rotation at  $T_c$  (8). Unresolved issues remained, however. For example, thermal conductivity (9) and specific heat (10) experiments were both interpreted as evidence for a nodal gap structure (3). Furthermore, the field-driven first-order phase transition observed at low temperatures (11, 12) is a natural consequence of the Zeeman coupling to quasiparticles (1), but this mechanism is inoperative for any fully gapped state. In a step toward clarification, recent <sup>17</sup>O NMR measurements exclude candidate *p*-wave states with **k**-independent **d**-vector aligned parallel to the *c* axis (13, 14). Left open is the possibility for an odd-parity triplet-pairing state with an in-plane **d**, as explicitly discussed in recent theoretical works (15, 16).

With these developments in mind, we recall other distinctive properties of superconductivity in Sr<sub>2</sub>RuO<sub>4</sub>. Among unconventional superconductors, Sr<sub>2</sub>RuO<sub>4</sub> is not just stoichiometric but possibly also the cleanest (1). Unlike the cuprates (17) and Fe-based superconductors, the superconductivity emerges from a well-understood Fermi liquid normal state (18), and for which the fermiology is precisely characterized (19, 20). Thus, Sr<sub>2</sub>RuO<sub>4</sub>

constitutes an ideal platform for achieving a level of understanding for an unconventional superconductor rivaling what is routinely expected for conventional superconductors. In general, identifying the order parameter symmetry is an essential step toward that goal. Moreover, there is a broader motivation to make connections from a system so well characterized, to other unresolved questions in unconventional superconductivity. As described above, Sr<sub>2</sub>RuO<sub>4</sub> was reasonably proposed as analogous to <sup>3</sup>He, for which ferromagnetic (FM) fluctuations are key to the superfluid triplet pairing. Indeed, the presence of FM correlations was inferred early on (4, 5). In an alternative proposal, the system is a more weakly coupled analog of the cuprate and Fe-based superconductors, in which antiferromagnetic fluctuations most naturally mediate singlet pairing (21). Thus, associating the superconducting state with AF fluctuations would more directly relate the physics of Sr<sub>2</sub>RuO<sub>4</sub> to the much broader class of unconventional superconductors.

The temperature and field dependences of the NMR Knight shifts  $K_s(T < T_c, \mathbf{B})$  are recognized as a crucial probe of the order-parameter symmetry. In the normal state,  $K_s \sim \chi_n$ , with

## Significance

**Sr<sub>2</sub>RuO<sub>4</sub> is distinctive among unconventional superconductors, in that in addition to exhibiting evidence for strong correlations, it is stoichiometric and extremely clean. As a result, its electronic structure is unusually well characterized, rendering it an ideal platform for developing a deep understanding of the mechanism behind the emergence of the superconducting state from a Fermi liquid. Toward that end, an unambiguous determination of the pairing symmetry is an essential step. For more than 2 decades, the preponderance of evidence pointed to a triplet spin pairing state and only recently has this interpretation been challenged. By field-dependent NMR Knight shift measurements, we eliminate from further consideration all candidate purely odd-parity triplet pairing states.**

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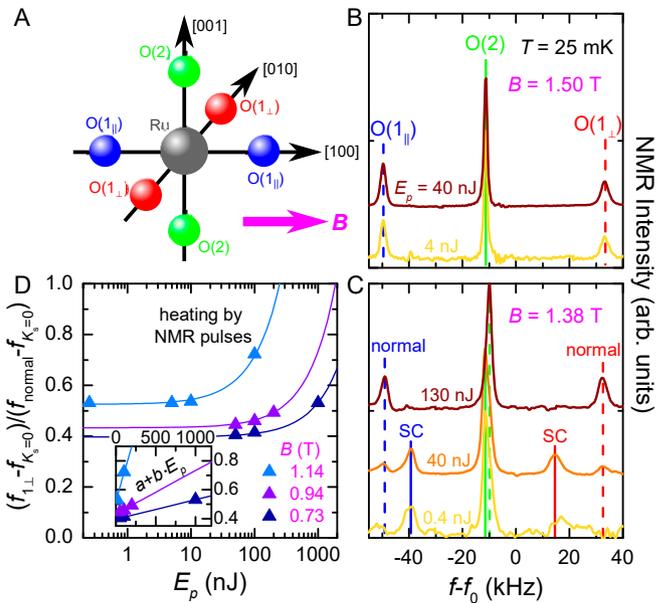
$\chi_n$  the susceptibility. In the superconducting phase, a nonzero susceptibility  $\chi_{sc}$  associated with condensate polarization is expected generally for triplet-paired,  $p$ -wave states. The response ranges from vanishingly small to that of the normal state,  $\chi_n$ , with the limiting cases corresponding to  $\mathbf{d} \parallel \mathbf{B}$ ,  $\mathbf{d} \perp \mathbf{B}$ , respectively. Hence, the observed reduction of the Knight shift for an applied in-plane field excludes the chiral state (13), for which  $\mathbf{d} \parallel \mathbf{c}$ . Crucially, states characterized by  $\mathbf{d} \perp \mathbf{c}$  are not eliminated by the prior work. Among such states allowed by the crystal symmetry is the so-called “helical” state,  $\mathbf{d} = p_x \mathbf{x} + p_y \mathbf{y}$ , for which  $\chi_{sc}/\chi_n = 1/2$  [in the absence of Fermi-liquid corrections (13, 14)].

The most direct way to test for symmetry-allowed states with  $\mathbf{d} \perp \mathbf{c}$  is to perform measurements with  $\mathbf{B} \parallel \mathbf{c}$ , since for this orientation the response of the helical state is  $\chi_{sc} = \chi_n$ . However, the relevant upper critical field  $B_{c2,[001]} < 100$  mT is very small\* making such experiments particularly challenging because signal strength and spectral resolution are reduced for very weak applied fields. Here we take another approach, discussed previously in refs. 14, 23: the field orientation is fixed in-plane, and the  $^{17}\text{O}$  shifts  $K_s$  are evaluated at low temperature (25 mK) while varying  $B$  as much as experimentally feasible. Quasiparticle creation is controlled by the field strength and also contributes to the magnetic response. At issue is the fractional magnetic response arising from quasiparticles, which must be separated from the condensate contribution. The relative contributions are determined by way of comparing to previously reported specific heat results  $C_e(B)/T$  (24), which is sensitive to field-induced quasiparticles only. We estimate that the upper bound for the condensate portion is  $\chi_{sc}/\chi_n < 10\%^\dagger$ , a value that contradicts the expectation for any of the proposed purely odd-parity order parameters relevant to  $\text{Sr}_2\text{RuO}_4$ .

## Results

**Pulse-Heating Control by Low-Power NMR Experiments.** The recent studies (13, 14) identified radio frequency (RF) heating by the NMR pulses as a possible impediment to accurate measurements in the superconducting state. The issue is illustrated in the results of Fig. 1. So as to enhance sensitivity to this potential artifact, we examined the transients with the field set to 1.38 T, a value very close to but smaller than  $B_{c2}$ . Clear evidence for warming by the RF pulsing is inferred from a transient response corresponding to that of the normal state (instead of the sought-after superconducting state). Shown in Fig. 1 B and C are  $^{17}\text{O}$  spectra corresponding to central transitions for the three oxygen sites,  $\text{O}(1_{\parallel}, 2, 1_{\perp})$ , at applied magnetic fields slightly above and below  $B_{c2}$ . With  $B = 1.5 \text{ T} > B_{c2}$ , the line shape remains unaffected by changing the pulse energy, and a normal state spectrum is also produced for  $B = 1.38 \text{ T} < B_{c2}$  when using a pulse energy  $E_p = 130 \text{ nJ}$ . Decreasing  $E_p$  to 40 nJ leads to a response where a new spectral line appears for each site, indicating the coexistence of normal and superconducting phases. This dataset is particularly useful since the macroscopic phase segregation provides a quantitative measure of the magnetization jump  $\Delta M$  at the discontinuous (first-order) transition (11, 12). Note that these data are recorded following a single-pulse excitation. That is, the transient NMR response corresponds to a free induction decay (FID). All shift results of the present work were obtained from FID measurements carried out with RF pulse energies sufficiently small to avoid heating, as illustrated in Fig. 1D.

**Field-Dependent Knight Shifts in the Superconducting State.** Having established a threshold for heating effects, we now inspect the



**Fig. 1.** (A)  $\text{Sr}_2\text{RuO}_4$  involves three distinct oxygen sites for field direction  $\mathbf{B} \parallel [100]$ . (B) The three associated  $^{17}\text{O}$  NMR central transitions [ $\text{O}(1_{\parallel})$ ,  $\text{O}(2)$ , and  $\text{O}(1_{\perp})$ , from left to right] are independent of pulse energy  $E_p$  at  $1.50 \text{ T} > B_{c2} \approx 1.45 \text{ T}$ . (C) Also at  $B = 1.38 \text{ T} \lesssim B_{c2}$  the normal-state spectrum is observed for  $E_p \geq 10^{-7} \text{ J}$ . Reducing to  $E_p = 40 \text{ nJ}$  leads to doubled spectral features, most pronounced for  $\text{O}(1_{\parallel, \perp})$ , which we assign to coexisting normal (dashed vertical lines) and superconducting (solid) contributions around the first-order transition. Further reduction of  $E_p$  reveals the pure superconducting-state spectrum. (D)  $\text{O}(1_{\perp})$  frequencies normalized to normal-state ( $f_{\text{normal}}$ ) and zero-shift ( $f_{K_s=0}$ ; Fig. 2) positions at  $B < B_{c2}$  for variable  $E_p$ . Linear fits (solid lines; Inset) indicate that heating is less problematic at lower field due to larger  $T_c(B)$ . Knight shifts  $K_s$  were determined using the frequency values leveling off at  $E_p \rightarrow 0$ .

spectra recorded at variable field strength. In Fig. 2, we show the NMR intensity as a function of  $f - f_0$ , where  $f_0 \equiv \frac{1}{2} \gamma B$ . The central transitions ( $-1/2 \leftrightarrow 1/2$ ) for the  $\text{O}(1_{\parallel}, 2, 1_{\perp})$  sites (left to right in the spectrum) exhibit pronounced variations with changing  $B$ . The shifts of the planar sites  $\text{O}(1_{\parallel})$  and  $\text{O}(1_{\perp})$  have opposite sign; this is a consequence of the applied field direction relative to the local environment.  $\text{O}(2)$  is the apical site (Fig. 1A). The dotted curves include only the quadrupolar and orbital contributions for each site, while omitting the Knight shift contribution; more information on these corrections appears below.<sup>†</sup> Crucially, simultaneous scrutiny of the field-dependent quadrupolar effects at both in-plane O sites leads to a quantitative upper bound on the condensate contribution. Open symbols line up with these spectral baselines at each field at which data were recorded. Also shown, using the dashed lines and closed symbols, are transition frequencies at each field, generated using the known normal state NMR parameters.<sup>†</sup> Then, the frequency differences between closed and open symbols are proportional to the hyperfine fields and constitute the product of (normal-state) Knight shifts with applied field,  $K_{s,\text{normal}} \frac{1}{2} \gamma B$ , for  $\text{O}(1_{\parallel})$ ,  $\text{O}(2)$ , and  $\text{O}(1_{\perp})$ . When decreasing the field  $B < B_{c2}$ , the NMR lines in Fig. 2 are displaced from the normal-state positions, toward the frequency corresponding to  $K_s = 0$ , due to the drop of  $K_s$  in the superconducting state. Below, we compare and contrast the measured shifts  $K_s$  with results of field-dependent specific heat experiments, which are sensitive to the field-induced quasiparticles.

The parameters needed for the quadrupolar corrections were determined previously (6, 25, 26) and confirmed here in field-dependent measurements.<sup>†</sup> In particular, we determined the field orientation as deviating  $\approx 3.0^\circ \pm 0.4^\circ$  from the

\* a-axis stress increases  $B_{c2}$  significantly by this measure (22).

<sup>†</sup> See SI Appendix for details on the discontinuous transition at  $B_{c2}$ , the different contributions to  $^{17}\text{O}$  NMR shifts, and sample alignment with respect to the external magnetic field.

[100] direction and otherwise aligned orthogonal to the  $c$  axis,  $\theta = 90^\circ \pm 0.2^\circ$ . Due to several factors, including reduced signal strength and resolution, as well as the strong increase of the  $O(1_{\parallel})$  quadrupolar component at low fields, we limited the measurements to  $B \geq 0.24$  T. In addition to the well-known quadrupolar effects, one has to include purely orbital contributions. These were evaluated in ref. 6, yielding  $K_o = +0.18\%$  for the  $O(1_{\parallel})$  site and a value indistinguishable from zero for  $O(1_{\perp})$  and  $O(2)$ .<sup>†</sup>

The shifts  $K_{1_{\parallel},2,1_{\perp}}$  are plotted as a function of  $B$  in Fig. 3. Results are shown in Fig. 3A as total shift,  $K = K_s + K_o$ . In the normal state,  $K_{1_{\parallel}} < 0$ , while  $K_{2,1_{\perp}} > 0$ ; each exhibits a reduction in the superconducting state.  $B_{c2}$  is marked by the discontinuous change of each of the three sites, accompanied by a coexistence regime (cf. Fig. 1 B and C). Consistent with expectations ( $B \gg B_{c1}$ ) (27), the results indicate that diamagnetic shielding is a small effect. Otherwise, the discontinuous drop  $\Delta M$  (Figs. 1 and 2) would be similar for all three sites. Instead, only the hyperfine field, which is much greater for the planar sites than it is for the apical site, and opposite in sign for  $O(1_{\parallel})$  relative to  $O(2)$  and  $O(1_{\perp})$ , decreases on entering the superconducting state.

**Comparison to Specific Heat: Condensate Polarization vs. Field-Induced Quasiparticles.** The main results of this work are displayed in Fig. 3B, where the Knight shifts are compared to previous heat capacity results (24),  $C_e(B)/T$  ( $C_e$  is the electronic contribution), both normalized to the normal state. As shown, the field-induced trends are similar and particularly relevant to the open question of order-parameter symmetry. Simply put, at nonzero field, an NMR shift can originate from quasiparticles and, in the case of triplet pairing, also from the condensate. In contrast, the specific heat is sensitive only to the quasiparticle

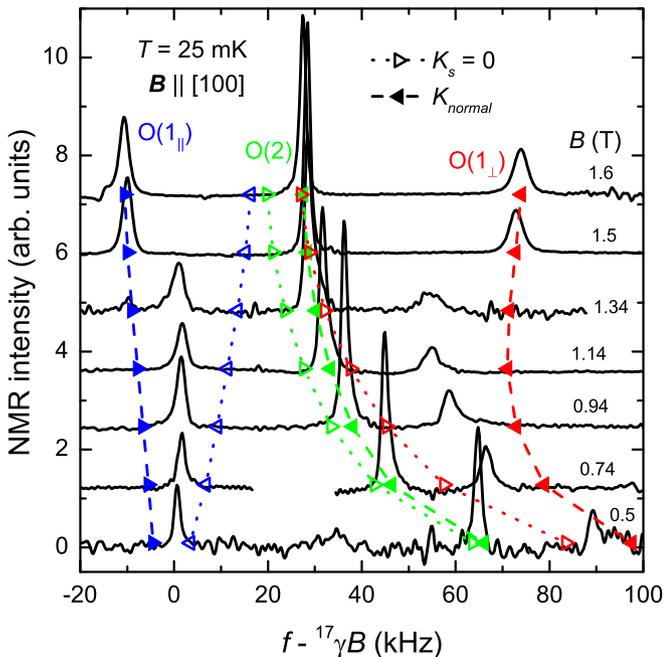


Fig. 2. Spectra for central  $^{17}\text{O}$  NMR transitions at different field strengths, for  $O(1_{\parallel})$ ,  $O(2)$ , and  $O(1_{\perp})$  sites, from left to right, plotted as intensity vs.  $f - ^{17}\gamma B$ . The dotted curves running vertically through the spectra follow the expected field dependence after taking into account quadrupolar and orbital couplings; the dashed curves also include the normal-state hyperfine fields. We provide details of quadrupolar and orbital contributions to the transition frequencies, as well as an analysis of the sample orientation relative to  $\mathbf{B}$ .<sup>†</sup>

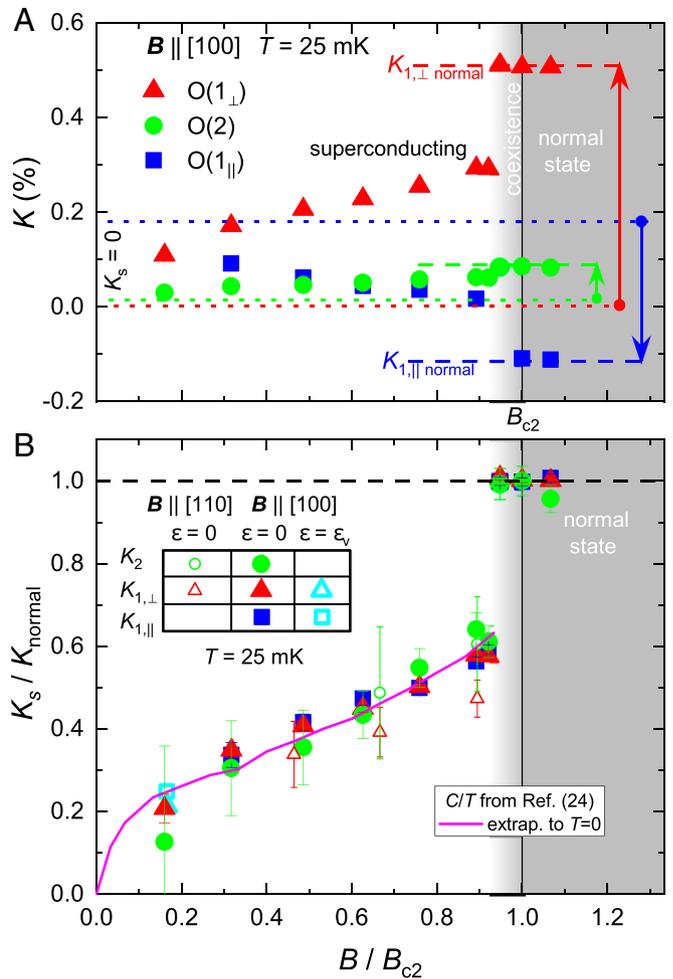


Fig. 3. (A) NMR shifts  $K = K_s + K_o$  determined from the spectra in Fig. 2. While the shifts are positive and the assigned  $K_o \approx 0.0\%$  for  $O(2)$  and  $O(1_{\perp})$ , the  $O(1_{\parallel})$  line occurs at a positive value  $K_o = 0.18\%$  at  $B = 0$  and  $K_{1_{\parallel}} < 0$  (6, 25). (B) The field-dependent drop of NMR Knight shift determined in the present work at  $T = 25$  mK is compared to specific heat  $C/T$  (24) extrapolated to  $T = 0^{\ddagger}$ , all normalized to the normal state value. The values of  $K_s$  coincide with the zero-temperature extrapolations of  $C/T$ , providing compelling evidence that this is the contribution of unpaired quasiparticles in the superconducting state. Measurements along  $[110]$  (small open symbols) reveal a similar jump at the transition, and also uniaxial strain results (open cyan symbols,  $\mathbf{B} \parallel [100]$ ,  $\epsilon_{aa} = \epsilon_v$ ) from ref. 13 coincide at low  $B/B_{c2}$ .

response with no contribution from the condensate. Note that in a fully gapped superconductor, gapless excitations are created in vortex cores, where the order parameter is suppressed. Whereas, in the case of a nodal state, the quasiparticle perturbations arising from both Zeeman and orbital coupling lead to additional contributions to the density of states (DOS) at  $E_F$ . [The latter is widely referred to as the Volovik effect (28).]

As can be seen by inspection of Fig. 3B, we observe no systematic difference between the  $T \rightarrow 0$  extrapolation of the heat capacity data of ref. 24 and the spin susceptibility deduced from our measurements. Taking into account systematic uncertainties we estimate an upper limit for the condensate response of

<sup>†</sup>We also note that recent specific heat measurements (10, 20) differ from those of ref. 24 by finding a larger residual electronic specific heat at low temperatures. While sample quality is the most obvious source of such a discrepancy, it merits further experimental attention. However, since those results indicate a larger quasiparticle contribution (than that of ref. 24), the central conclusion of the present work is not invalidated: we find no evidence for a condensate contribution to the spin susceptibility.

< 10% of that of the normal state, for fields applied both along [100] and [110].<sup>†</sup> Similar  $K_{1||,\perp}$  are found at  $B/B_{c2} = 0.17$  under strained conditions (13). These observations place such strong constraints on the magnetic polarizability of the condensate that we believe they rule out any pure  $p$ -wave order parameter for the superconducting state of  $\text{Sr}_2\text{RuO}_4$ , as we now discuss.

The  $p$ -wave order parameters most commonly discussed in the context of  $\text{Sr}_2\text{RuO}_4$  are the so-called chiral  $[\hat{z}(p_x \pm ip_y)]$  and helical  $(p_x\hat{x} + p_y\hat{y})$  states. Assuming that the unit vectors encoding spin directions are pinned to the lattice, they are predicted in the simplest models to result in condensate polarizabilities of 100% (chiral) and 50% (helical) of the normal state value. The chiral state was ruled out by our previous work (13), but the helical state and certain others were not. The data presented in Fig. 3 allow us to go much further; it is unclear how to reconcile an upper bound of 10% of the normal state susceptibility with any  $p$ -wave state. While Fermi liquid corrections may reduce the condensate response to  $\sim 30\%$  of the normal state value (14), this still far exceeds our observations. Spin-orbit coupling (SOC) effects tend to weaken the distinction between spin-singlet and spin-triplet states (29), in that a nonzero magnetic response survives in the limit  $T, B \rightarrow 0$  (16). Thus, we conclude that SOC effects are not significantly impacting our results, an outcome we tentatively attribute to the dominant normal state DOS (and magnetic response) arising from those states at  $E_F$  proximate to a van Hove singularity, where the SOC is relatively weak (26). One could also postulate extreme situations such as a momentum-independent  $\mathbf{d}$  aligned along either [100] or [110] or an unpinned  $\mathbf{d}$  free to rotate in response to the applied field. None result in a spin susceptibility suppression compatible with our results; a few remaining possibilities are eliminated by our use of both [100] and [110] fields in the current experiments. We therefore assert that our measurements have ruled out any  $p$ -wave order parameter candidate for the superconducting state of  $\text{Sr}_2\text{RuO}_4$ .

## Summary and Outlook

Given this input, we close with an evaluation of the current understanding of superconductivity in  $\text{Sr}_2\text{RuO}_4$ . In isolation, our NMR findings are consistent with even-parity states (30), such as  $d_{x^2-y^2}$  ( $B_{1g}$ ),  $d_{xy}$  ( $B_{2g}$ ) or  $\{d_{xz}; d_{yz}\}$  ( $E_{1g}$ ), or  $g_{xy(x^2-y^2)}$  ( $A_{2g}$ ). Indeed, scanning tunneling microscopy measurements are interpreted as most consistent with the  $B_{1g}$  state (31), similar to thermal transport experiments (9). Further emphasizing the constraints imposed by the present work, the viability of proposed even-parity states based on interorbital pairing (32–34), and that of a mixed-parity order parameter of the form  $d \pm ip$  (35) necessarily depends on a sufficiently small condensate response to in-plane fields.

In considering other recent experimental developments, we would like to note in particular reports of a discontinuity in the shear elastic constant  $c_{66}$  (corresponding to  $B_{2g}$  deformations) (36, 37) but not in  $(c_{11} - c_{12})/2$  ( $B_{1g}$ ) (36). This is the expected outcome for a coupling of nearly degenerate even-parity states such as  $\{d_{x^2-y^2}; g_{xy(x^2-y^2)}\}$  (21, 38) or  $\{s'; d_{xy}\}$  (39) but not for the degenerate combination  $\{d_{xz}; d_{yz}\}$ , for which a discontinuity in  $(c_{11} - c_{12})/2$  is also expected. On the other hand,  $\mu^+$ SR measurements have confirmed the early results and observed transition splitting between the TRSB signature and the onset of SC under uniaxial pressure (40). It will be intriguing to see how the quest to finalize identification of the order parameter of  $\text{Sr}_2\text{RuO}_4$  develops.

## Materials and Methods

**Sample Preparation.** As in previous NMR studies on  $\text{Sr}_2\text{RuO}_4$  (6), the labeled  $^{17}\text{O}$  [ $^{17}I = 5/2$ ,  $^{17}\gamma = -5.772$  MHz/T (41)] is introduced by high-temperature annealing (6), here in 90%  $^{17}\text{O}_2$  atmosphere at 1,050 °C. Single-crystal dimensions were (3.5 mm  $\times$  1 mm  $\times$  0.2 mm), with the shortest dimension corresponding to the out-of-plane [001] direction and the longest dimension parallel to [100] (Fig. 1A).

**NMR Experiments.** To facilitate access to relatively low frequencies covering several octaves, we adopted a top tuning/matching configuration. The NMR coil containing the crystal under study was mounted on a single-axis piezorotator inside the mixing chamber of a bottom-loading dilution refrigerator. Sample alignment enabled in-plane orientation to within  $\pm 0.2^\circ$ , based on RF susceptibility measurements sensitive to  $B_{c2}$ , described in ref. 13 and discussed in *SI Appendix*.<sup>†</sup>  $^{63}\text{Cu}$  NMR relaxation rate measurements were used to determine the equilibrium bath temperature  $T = 25$  mK. As in our previous work (13), low-power RF experiments were carried out to make sure the results were not measurably altered by RF pulse heating effects. The applied field strength  $B$  was determined to within uncertainties less than tens of  $\mu\text{T}$  from the NMR resonance of  $^3\text{He}$  in the  $^3\text{He}/^4\text{He}$  mixture of the dilution refrigerator.

**Data Availability.** Excel data have been deposited in <https://www.pa.ucla.edu/content/sr2ruo4-knightshift-vs-field/>.

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