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D. J. Gorman and F. Asaro

May 1970

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TABLES OF THE CLEBSCH-GORDAN COEFFICIENTS FOR ODD-
AND EVEN-MASS DEFORMED NUCLEI*

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May 1970

A set of tables has been prepared as a convenient source of the Clebsch-Gordan Coefficients commonly used in the calculation of nuclear transition probabilities for deformed nuclei. Similar, less extensive tables have been prepared by other authors (Si 54, Lu 61, and Ya 66).

The transition probability for a nuclear transition of multipole order L between an initial state I and a final state F is characterized by the reduced transition probability $B(L, II \rightarrow IF)$.

If the nuclear motion is separated into two modes--rotational and intrinsic--the reduced transition probability can be written as a product of a geometrical factor, depending only on the angular momenta, and a factor involving integrations over the intrinsic wave function of the initial and final states.[†]

If one compares the reduced transition probability for the emission of a given multipole radiation from a state I to different members F, F', \dots of a rotational family, the factors involving the intrinsic wave functions are the same. One thus obtains a ratio which depends only on the geometrical factors.

* Available as UCRL-18975 from Lawrence Radiation Laboratory, University of California, Berkeley, California 94720.

[†]This and most of the following discussion is taken from Ref. A1.

$$\frac{B(L, II \rightarrow IF)}{B(L, II \rightarrow IF')} = \frac{|\langle II L KI KF-KI | IF KF \rangle|^2}{|\langle II L KI KF-KI | IF' KF \rangle|^2}, \quad (1)$$

where $\langle II L KI KF-KI | IF KF \rangle$ is the Clebsch-Gordan Coefficient (Co 35).

II = The spin of the initial state.

IF = The spin of the final state.

KI = The K of the initial state, where K is the projection
of the nuclear angular momentum on the nuclear symmetry axis.

KF = The K of the final state

L = The angular momentum carried off by the radiation
emitted during the transition from the initial to the
final state.

The relation (1) holds when the initial and final states belong to
the same or different rotational bands.

In special cases when $L \geq KI + KF$, symmetrization of the wave function
may cause the transition matrix elements to become a sum of two products of
geometrical and intrinsic factors. The ratio of reduced transition probabilities
can then be written in the form.

$$\frac{B(L, II \rightarrow IF)}{B(L, II \rightarrow IF')} = \left[\frac{\langle II L KI KF-KI | IF KF \rangle + b(-)^{IF+KF} \langle II L KI -KF-KI | IF -KF \rangle}{\langle II L KI KF-KI | IF' KF \rangle + b(-)^{IF'+KF} \langle II L KI -KF-KI | IF' -KF \rangle} \right]^2 \quad (2)$$

where b is a parameter depending on the intrinsic wave function.

The reduced transition probabilities are also important in Coulomb exci-
tation experiments. The cross section for Coulomb excitation of particular
states is proportional to $B(L, II \rightarrow IF)$.

THE ARRANGEMENT OF THE TABLES

The compilation is arranged into four tables covering integral and half-integral values of the spin (I) and positive and negative values of KF. The range of the arguments used is shown in the table below.

Table I. Range of Arguments for Clebsch-Gordan Coefficients

Table	KI	KF	II	L	IF
1	$1/2 - 31/2$	$1/2 - 31/2$	$1/2 - 31/2$	$0 - 6$	$1/2 - 43/2$
2	$1/2 - 11/2$	$1/2 - (-11/2)$	$1/2 - 31/2$	$0 - 6$	$1/2 - 43/2$
3	$0 - 16$	$0 - 16$	$0 - 16$	$0 - 6$	$0 - 22$
4	$0 - 5$	$-1 - (-6)$	$0 - 16$	$0 - 6$	$0 - 22$

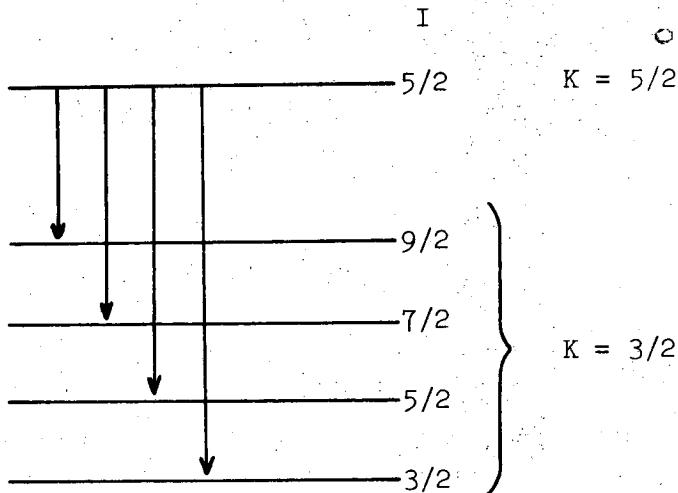
Some sample pages from the tables are reproduced below. The tables are arranged such that the right hand argument IF varies the fastest, followed by L, II, KF, and KI.

KI	KF	II	L	IF	(CLER)***2	CLER
1/2	1/2	5/2	0	5/2	1.0000000	1.0000000
1/2	1/2	5/2	1	3/2	.40000000	-.63245553
				5/2	.02657143	-.16903085
				7/2	.57142857	-.75592895
1/2	1/2	5/2	2	1/2	.20000000	.44721360
				3/2	.05714286	-.23904572
				5/2	.22857143	-.47809164
				7/2	.03409524	.19518001
				9/2	.47619048	.69006556
1/2	1/2	5/2	3	1/2	.14285714	.37796447
				3/2	.11424571	.33806170
				5/2	.07619068	-.27602622
				7/2	.19047619	-.43643578
				9/2	.04329004	.20806259
				11/2	.43290043	.65795169
1/2	1/2	5/2	4	3/2	.19047619	.41643578
				5/2	.09523810	.30860670
				7/2	.08658009	-.29424494
				9/2	.17316017	-.41612519
				11/2	.04662005	.21591676
				13/2	.40792541	.63869039
•	•	•	•	•	•	•
•	•	•	•	•	•	•
•	•	•	•	•	•	•
•	•	•	•	•	•	•
•	•	•	•	•	•	•
5/2	3/2	5/2	1	3/2	.66666667	.81649658
				5/2	.28571429	.53452248
				7/2	.04761905	.21821789
5/2	3/2	5/2	2	3/2	.28571429	.53452248
				5/2	.42857143	.65465367
				7/2	.23809524	.48795004
				9/2	.04761905	.21821789
5/2	3/2	5/2	3	3/2	.07142857	.26726124
				5/2	.28571429	.53452248
				7/2	.38095238	.61721340
				9/2	.21645022	.46524211
				11/2	.04545455	.21320072
5/2	3/2	5/2	4	3/2	.00793651	.08908708
				5/2	.09523810	.30860670
				7/2	.28860029	.53721531
				9/2	.36075036	.60062498
				11/2	.20396270	.45162230
				13/2	.04351204	.20859541
•	•	•	•	•	•	•
•	•	•	•	•	•	•
•	•	•	•	•	•	•
•	•	•	•	•	•	•
•	•	•	•	•	•	•
1/2	-1/2	3/2	5	7/2	.36363636	-.60302269
				9/2	.04545455	-.21320072
				11/2	.22377622	.47304992
				13/2	.36713287	.60591490
1/2	-1/2	3/2	6	9/2	.36713287	-.60591490
				11/2	.05594466	-.21652496
				13/2	.20769231	.45573272
				15/2	.4923077	.60766362
1/2	-1/2	3/2	1	3/2	.20000000	.44721360
				5/2	.51424571	.71713717
				7/2	.28571429	.53452248
1/2	-1/2	3/2	2	1/2	.13333333	-.36514837
				3/2	.73809524	-.48795004
				5/2	.00600000	.00000000
				7/2	.31111111	.55777335
				9/2	.31746032	.56347617
1/2	-1/2	3/2	3	1/2	.19047619	.43643579
				3/2	.00952381	-.09759001
				5/2	.22857143	-.47809144
				7/2	.01587302	-.12598816
				9/2	.23046023	.48049998
				11/2	.32467532	.56980288

Fig. 1

EXAMPLES OF THE USE OF THE TABLES

A. An E2 transition from a $K = 5/2$ to a $K = 3/2$ rotational band.



We can obtain the relative transition probabilities from the spin $5/2$ member of the $K = 5/2$ rotational band to the different rotational members of the $K = 3/2$ band using formula 1. In this case $II = 5/2$, $KI = 5/2$, $KF = 3/2$, $L = 2$, and $IF = 9/2, 7/2, 5/2$ and $3/2$.

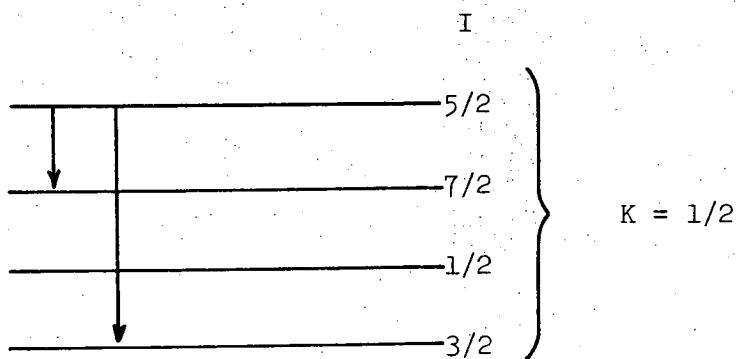
$$B(2, 5/2 \rightarrow 3/2) \propto | \langle 5/2 \ 2 \ 5/2 \ -1 | 3/2 \ 3/2 \rangle |^2 = 0.28571429$$

$$B(2, 5/2 \rightarrow 5/2) \propto | \langle 5/2 \ 2 \ 5/2 \ -1 | 5/2 \ 3/2 \rangle |^2 = 0.42857143$$

$$B(2, 5/2 \rightarrow 7/2) \propto | \langle 5/2 \ 2 \ 5/2 \ -1 | 7/2 \ 3/2 \rangle |^2 = 0.23809524$$

$$B(2, 5/2 \rightarrow 9/2) \propto | \langle 5/2 \ 2 \ 5/2 \ -1 | 9/2 \ 3/2 \rangle |^2 = 0.04761905$$

B. An M1 transition within a $K = 1/2$ rotational band with a decoupling constant (a) of -1.5.



In this case, to find the relative transition probabilities for the transitions from the $5/2$ to the $7/2$ and $3/2$ members of the $K = 1/2$ band we must use formula 2. Here we have $II = 5/2$, $KI = KF = 1/2$, $L = 1$, and $IF = 7/2$ and $3/2$.

$$B(1, 5/2 \rightarrow 7/2) \propto [\langle 5/2 \ 1 \ 1/2 \ 0 | 7/2 \ 1/2 \rangle + b \langle 5/2 \ 1 \ 1/2 \ 0 | 7/2 \ -1/2 \rangle]^2$$

$$= [0.75592895 + b (0.53452248)]^2$$

$$B(1, 5/2 \rightarrow 3/2) \propto [\langle 5/2 \ 1 \ 1/2 \ 0 | 3/2 \ 1/2 \rangle + b \langle 5/2 \ 1 \ 1/2 \ 0 | 3/2 \ -1/2 \rangle]^2$$

$$= [-0.63245553 + b (0.44721360)]^2$$

THE COMPUTER PROGRAM

The computer program consists of a main program, which is slightly different for each of the four tables, and a subroutine CLEB which remains the same. The program is written in Chippewa Fortran for the CDC 6600.

The main program for calculating the coefficients for half-integral values of I and negative KF is reproduced below.

```

C PROGRAM TDAL INPUT, OUTPUT, TAPE2=INPUT, TAPE3=OUTPUT
C
C THIS PROGRAM CALCULATES CLEBSCH GORDON COEFFICIENTS FOR
C HALF-INTEGRAL ARGUMENTS
C AND NEGATIVE VALUES OF KF
C
C X(1) = 11
C X(2) = L
C X(3) = TF
C X(4) = KI
C X(5) = KF - KI
C X(6) = KF
C
000063 DATA LINE /0/
000063 DATA CUT/C00000000001/
000043 DIMNSTIN X(6),N161
000043 DIMNSTIN FMT161
000043 DATA NPAGE/1/
000043 FMT(1) = 10H(1H1,5X,0-
000043 FMT(3) = 10H0X,0UCP1-1
000046 FMT(4) = 10H87591
000050 DIGIT1 = 10H+11,0-9,5
000051 DIGIT2 = 10H+12,0-9,5
000051 DIGIT3 = 10H+13,0-9,5
000056 DIGIT4 = 10H+14,0-9,5
000056 PRINT 1
000041 L FORMAT(6H1*CVF*)
000061 ICOUNT = 0
000062 IF(INPAGE.LE.9999) FMT(2) = DIGIT4
000067 IF(INPAGE.LE.999) FMT(2) = DIGIT3
000073 IF(INPAGE.LE.99) FMT(2) = DIGIT2
000077 IF(INPAGE.LE.9) FMT(2) = DIGIT1
000103 WRITE(3,FMT) NPAGE
000111 NPAGE = NPAGE + 1
000113 WRITE(3,3003)
000116 WRITE(3,30001)
000121 WRITE(3,30101)
000126 ICOUNT = ICOUNT + 5
000126 DO 50 I4 = 1,1L,2
000127 X(4) = FLOAT(I4)/2.
000131 PMAX = I6. - X(4)*I2.
000133 KMAX = TFI(X(PMAX))
000135 DO 60 I6 = 1,KMAX,2
000136 X(6) = -FCAT(I6)/2.
000140 X(5) = X(6) - X(4)
000142 DO 50 I1 = I4,31,2
000144 X(1) = FCAT(I1)/2.
000146 DO 40 I2 = 1,7
000147 LINP = 0
000150 X(2) = FLOAT(I2) - 1.
000152 IF(ABS(X(1)).GT.X(2)) GO TO 40
000157 JMIN = ABS(X(1)) - X(2)*2
000163 JMAX = ABS(X(1)) + X(2)*2
000167 KMIN = ABS(X(6)) + 2
000172 IF(JMIN.LT.KMIN) JMIN = KMIN
000174 DO 30 I3 = JMIN,JMAX,2
000176 X(3) = FDAT(I3)/2.
000200 Y = CLE(RX)
000202 IF(ABS(Y).LT.0) Y=CUT
000205 Z = Y**2
000207 LINP = LINE + 1
000210 M(1) = 2 * X(1)
000213 M(2) = X(2)
000215 M(3) = 2 * X(3)
000220 M(4) = 2 * X(4)
000223 M(5) = X(5)
000224 M(6) = 2 * X(6)
000227 IF(LINP.GT.11) GO TO 20
000232 WRITE(3,3002) M(6),M(1),M(2),M(3),Z,Y
000235 ICOUNT = ICOUNT + 2
000257 IF(ICOUNT.GE.60) GO TO 100
000257 GO TO 30
000257 20 WRITE(3,3002) M(3),Z,Y
000270 ICOUNT = ICOUNT + 1
000272 IF(ICOUNT.GE.60) GO TO 100
000274 30 CONTINUE
000277 40 CONTINUE
000301 50 CONTINUE
000303 60 CONTINUE
000306 80 CONTINUE
000310 CALL EXIT
000311 100 ICOUNT = 0
000312 IF(INPAGE.LE.9999) FMT(2) = DIGIT4
000317 IF(INPAGE.LE.999) FMT(2) = DIGIT3
000323 IF(INPAGE.LE.99) FMT(2) = DIGIT2
000327 IF(INPAGE.LE.9) FMT(2) = DIGIT1
000333 WRITE(3,FMT) NPAGE
000341 NPAGE = NPAGE + 1
000343 WRITE(3,3003)
000346 WRITE(3,30001)
000351 WRITE(3,30101)
000356 ICOUNT = ICOUNT + 5
000356 LINP = 0
000357 GO TO 30
000357 3010 FORMAT(1H0)
000357 3000 FORMAT(1H,7X,2HK1,6X,2HKF,6X,2HT1,6X,IHL,6X,2HIC,7X,9H(CLES)002,
000357 1D0,4HCLER)
000357 3011 FORMAT(1H,0,5X,13,2H/2,3X,13,2H/2,3X,13,2H/7,3X,13,4X,13,2H/2,3X,
000357 1F12,8,X,12,8)
000357 3002 FORMAT(1H ,36X,13,2H/2,3X,F12,8,5X,F12,8)
000357 3003 FORMAT(1H )
000357 END

```

Fig. 2

```

FUNCTION C1(F1,X)
DIMENSION X(6)
DIMENSION F(FACT(10))
DATA EPS/1D-15/
DATA FFACT(11),I=1,10/
  X 1.00000000000000E+00, 1.00000000000000E+00,
  X 1.142135621731E+00, 2.4494974278171E+00,
  X 4.4987794556850E+00, 1.0956451150100E+01,
  X 2.6832819730005E+01, 7.09929573972260E+01,
  X 2.007980636831E+02, 6.02195219106488E+02,
  X 1.90946094396762E+03, 6.31797415892595E+03,
  X 2.18861051911534E+04, 7.8911474650057E+04,
  X 2.9525970120214E+05, 1.14353590586437E+05,
  X 6.576146362165827E+06, 1.88596773067634E+06,
  X 8.00168347854957E+07, 3.48776576634565E+08,
  X 1.55977426d62895E+09, 7.14779291818756E+09,
  X 3.15261200821767E+10, 1.60785623545420E+11,
  X 7.87685471322957E+11, 3.9384273561453E+12,
  X 2.0042117944249E+13, 1.04339745809042E+14,
  X 5.52166953567054E+14, 2.97351004601142E+15/
DATA FFACT(11),I=1,1,601/
  X 1.62685352716863E+16, 9.0679869067864E+16,
  X 5.12962802680119E+17, 2.9667669531933E+18,
  X 1.71823397428617E+19, 1.0165292779088E+20,
  X 6.0991255667351E+20, 3.70995124649591E+21,
  X 2.28696477436115E+22, 1.428211156179182E+23,
  X 4.01280290521680E+23, 5.74381592143564E+24,
  X 1.74414112341403E+25, 2.65795164840047E+26,
  X 1.63042067417555E+27, 1.093719437H1310E+28,
  X 7.41176613620652E+28, 5.08550116672975E+29,
  X 3.52333869965390E+30, 2.46633708975722E+31,
  X 1.74393368085876E+32, 1.24533918088317E+33,
  X 8.9098965429102E+33, 6.53827591597705E+34,
  X 4.90461967425191E+35, 3.56320127846641E+36,
  X 2.66645567711136E+37, 2.01312989511718E+38,
  X 1.53315046814452E+39, 1.17763796575137E+40/
DATA FFACT(11),I=1,1,901/
  X 9.12194448166793E+40, 7.12446639315476E+41,
  X 5.609810447778243E+42, 3.65766900411166E+43,
  X 3.562119420328933E+44, 2.87187231470840E+45,
  X 2.331120097790116E+46, 1.40974110595541E+47,
  X 1.576817850987115E+48, 1.10813740782409E+49,
  X 1.09446661300462E+50, 9.22213960291451E+50,
  X 7.82524494032643F+51, 6.68589270780914E+52,
  X 5.75142194719355E+53, 4.94087751415082E+54,
  X 4.36227834686521E+55, 3.81028991056721E+56,
  X 3.36515693214947E+57, 2.99101690577017E+58,
  X 2.675264484926725E+59, 2.40772216433614E+60,
  X 2.18028515016688E+61, 1.98633410460097E+62,
  X 1.82350546126182E+63, 1.67842310368487E+64,
  X 1.55650555157413E+65, 1.45191172964034E+66,
  X 1.36192012340039E+67, 1.28483287475282E+68/
DATA FFACT(11),I=91,101/
  X 1.2189994996304E+69, 1.16275600520414E+70,
  X 1.11527638073502E+71, 1.07553359177801E+72,
  X 1.04276850576775E+73, 1.01636501749511E+74,
  X 9.95830274110833E+74, 9.80779076443175E+75,
  X 9.70921750116777E+76, 9.66054943780904E+77,
  X 9.6605494377946E+78/
CLER=0.
NA=2.*X(1)+EPS
NR=2.*X(2)+EPS
NC=2.*X(3)+EPS
ND=SIGN(ARS(2,*X(4))+EPS,X(4))
NE=SIGN(ARS(2,*X(5))+EPS,X(5))
NF=SIGN(ARS(2,*X(6))+EPS,X(6))
IF(XRS(X(4))-X(5)-X(6)) .GT. EPSI RETURN
L3=X(2)*X(5)+EPS
L8=X(1)+X(4)+EPS
L10=X(3)-X(6)+EPS
IF(XRS(X(2)+X(5))-FLOAT(L3)) .GT. EPSI RETURN
IF(XRS(X(1)+X(4))-FLOAT(L8)) .GT. EPSI RETURN
IF(XRS(X(3))-X(6))-FLOAT(L10)) .GT. EPSI RETURN
L0=L3*L8*L10
IF(L0 .GT. 99) GO TO 2
IF(XRS(ND) .GT. NA .OR.
  X (XRS(NE) .GT. NB .OR.
  X (XRS(NF) .GT. NC) RETURN
L1=L0-NC
L2=L8-NF
L9=L3-NF
L11=L0-NF
L6=L0-NR
L7=L0-N4
L8=L6-L2
L5=L7-L3
L20=NC+1
KMAX=MAX(10,-L4,-L5)
KMAX=MIN(L1,L2,L3)
IF(KMAX .LT. KMINT) RETURN
COL=FACT(L1+1)*FACT(L6+1)*FACT(L7+1)*FACT(L8+1)
X *FACT(L2+1)*FACT(L3+1)
X *FACT(L9+1)*FACT(L10+1)*FACT(L11+1)/FACT(L0+2)
X *FACT(L20+1)/FACT(L20)
SGN=1.
DO 1 K=KMIN,KMAX
  L12=L1-K+1
  L13=L2-K+1
  L14=L3-K+1
  L15=L4-K+1
  L16=L5-K+1
  DEN=FACT(K+1)*FACT(L12)*FACT(L13)*FACT(L14)*FACT(L15)*FACT(L16)
  CLR=CLR+SGN*COL/DEN*#
  SGN=-SGN
1 CONTINUE
IF(MOD(KMIN,2) .NE. 0) CLR=-CLR
RETURN
2 CLR=0./0.
RETURN
END

```

Fig. 2

To calculate the coefficients for positive values of KF, the following changes should be made.

DO 80 I4 = 1,11,2

becomes

DO 80 I4 = 1,31,2

PMAX = (6. - X(4))* 2.

becomes

PMAX = (X(4) + 6.)* 2.

X(6) = -FLOAT(I6)/2.

becomes

X(6) = FLOAT(I6)/2.

The variable NPAGE which is set in a data statement gives the initial page number. This enables one to calculate the four tables successively and keep consecutive page numbers.

The statements [PRINT 1
1 FORMAT(6H1*OVF*)] suppress the automatic skip to a new page on the printer.

For calculating the coefficients with integral arguments and negative KF, the lines from 000126 through 000224 should be replaced by the following sequence.

```
000126      DD 80 I4 = 0,6
000127      X(4) = FLOAT(14)
000130      PMAX = 16. - X(4)
000132      KMAX = IFIX(PMAX)
000133      DD 60 I6 = 1,KMAX
000135      X(6) = -FLOAT(16)
000136      X(5) = X(6) - X(4)
000140      DD 50 I1 = 1,16
000142      X(1) = FLOAT(11)
000143      DD 40 I2 = 0,6
000145      LINF = 0
000146      X(2) = FLCAT(12)
000147      IF(ASS(X(5))-G,X(2)) GO TO 40
000154      JMIN = ABS(X(1) - X(2))
000157      JMAX = ABS(X(1) + X(2))
000162      KMIN = ABS(X(6))
000164      IF(JMIN.LT.KMIN) JMIN = KMIN
000166      DD 30 I3 = JMIN,JMAX
000170      X(3) = FLOAT(13)
000171      Y = CLEN(X)
000174      IF(ANS(Y).EQ.0) Y = CUT
000177      Z = Y**2
000201      LINE = LINE + 1
000202      DD 10 J = 1,6
000207      10 M(J) = X(J)
```

Fig. 3

For positive KF and integral arguments make the following substitutions:

DO 80 I4 = 0,6	becomes	DO 80 I4 = 0,16
PMAX = 6. - X(4)	becomes	PMAX = X(4) + 6.
DO 60 I6 = 1,KMAX	becomes	DO 60 I6 = 0,KMAX
X(6) = -FLOAT(I6)	becomes	X(6) = FLOAT(I6)

The subroutine CLEB was written by Marjory Simmons of the Math and Computing division at LRL Berkeley.

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