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1 **Tuning of oscillation modes by controlling dimensionality of spin structures**

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19

1 **Abstract**

2 Harmonic oscillation of spin structures is a physical phenomenon that offers great potential  
3 for applications in nanotechnologies such as nano-oscillators and bio-inspired computing.  
4 The effective tuning of oscillations over wide frequency ranges within a single ferromagnetic  
5 nanoelement is a prerequisite to realize oscillation-based nanodevices, but it has not been  
6 addressed experimentally or theoretically. Here, utilizing a vortex core structure, one of spin  
7 structures, we report a drastic change of oscillation modes over the frequency range from  
8 MHz to sub-GHz in a 100 nm-thick permalloy circular disk. Oscillation mode was found to  
9 considerably depend on the shape and dimension of the vortex core structure and various  
10 oscillation modes over a wide range of frequencies appeared with dimensional change in the  
11 vortex core structure. This work demonstrates that oscillation modes of the vortex core  
12 structure can be effectively tuned and opens a way to apply spin structures to oscillation-  
13 based technology.

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21 **Keywords:** Spintronics, Nano-oscillator, Oscillation modes, Spin dynamics, X-ray  
22 microscopy, Magnetic vortex.

## 1 Introduction

2 Harmonic oscillation is an intriguing physical phenomenon that has attracted  
3 significant attentions in various material systems. The fundamental understanding and  
4 manipulation of oscillation properties (e.g., frequency and amplitude) have been extensively  
5 studied in the research fields of two-dimensional (2D) materials<sup>1-3</sup>, quantum materials<sup>4,5</sup>,  
6 lattice distortion<sup>6,7</sup> and magnetic materials<sup>8-10</sup> since it offers a high potential for energy-  
7 efficient technological applications, e.g., nano-oscillators<sup>1,2,11-13</sup>, bio-inspired computing<sup>5,14-18</sup>,  
8 and programmable logic devices<sup>19,20</sup>.

9 Spin structures have been highly regarded in the application to oscillation-based  
10 nanodevices due to its high stability and rich oscillation properties<sup>21-28</sup>. The magnetic vortex,  
11 one of spin structures, is a ground state stabilized in a soft ferromagnetic disk, which is  
12 composed of the in-plane curling magnetization and out-of-plane magnetization at the centre  
13 of the element, referred to as a vortex core. The vortex core structure in typical thin  
14 ferromagnetic disks where the thickness is within the range of the exchange length (thickness  
15 < 50 nm) is considered as a rigid structure and it generally shows the gyrotropic motion of the  
16 MHz-ranged frequency without its deformation along the thickness direction, which is called  
17 the zeroth-order gyrotropic mode<sup>29-32</sup>. The oscillation mode of vortex core structure can be  
18 easily detected through the electrical measurements compared to the oscillation mode of other  
19 spin structures due to its large amplitude and narrow linewidth<sup>11-13</sup>. Recently, it has been

1 revealed that the oscillation mode could significantly change as the thickness of the disk  
2 increases and it leads to the emergence of unique three-dimensional (3D) dynamic  
3 characteristics of magnetic vortex<sup>33-41</sup>. For instance, the higher-order gyrotropic modes with  
4 GHz frequency range accompanying oscillation nodes along the thickness of the disk appear  
5 in addition to zeroth-order gyrotropic modes<sup>38-41</sup>.

6 To realize a versatile nano-oscillator, efficient tuning of harmonic oscillations of  
7 vortex core structure in a wide range of frequencies, especially in a single ferromagnetic  
8 element is highly required<sup>31,42,43</sup>. However, earlier works on the oscillation of vortex core  
9 structure have focused on tuning the eigenfrequency of the zeroth-order gyrotropic mode of  
10 vortex core structure in thin ferromagnetic disks, and thus the reported frequency tuning  
11 range has been limited to MHz range<sup>31,42,43</sup>. In our works, we manipulate oscillation modes of  
12 vortex core structure over from MHz to sub-GHz frequency range within a 100 nm-thick  
13 single permalloy ( $\text{Ni}_{80}\text{Fe}_{20}$ , Py) circular disk utilizing time-resolved magnetic transmission X-  
14 ray microscopy (MTXM) measurement (Figure 1a). We show that the oscillation modes of  
15 the vortex core structure are controllable by manipulating the shape and dimension of the  
16 vortex core structure.

17

## 18 **Results**

### 19 **Manipulating the shape and dimension of the vortex core structure**

1           Figure 1b shows three different magnetic structures imaged at the external magnetic  
2 fields of  $H_x = 0$  mT, 12 mT, and 24 mT in permalloy ( $\text{Ni}_{80}\text{Fe}_{20}$ , Py) circular disk of diameter  
3  $D = 3 \mu\text{m}$  and thickness  $h = 100$  nm by utilizing MTXM (See Methods)<sup>44</sup>. Black and white  
4 contrasts in those images indicate downward and upward magnetic components, respectively.  
5 At zero field ( $H_x = 0$  mT), a black spot at the centre of the disk is observed, which  
6 corresponds to the typical dot-shaped vortex core structure with downward magnetization. As  
7  $H_x$  increase to +12 mT, the vortex core structure is shifted in the +y-axis and the vortex core  
8 structure gets slightly enlarged in a horizontal direction. As  $H_x$  increases further, the vortex  
9 core structure gets closer to the edge of the disk and completely deforms into the elongated  
10 structure with curvature (See the magnetic image at  $H_x = +24$  mT in Figure 1b). The magnetic  
11 images in Figure 1b show that the shape and dimension of the vortex core structure  
12 noticeably change as it gets closer to the edge of the disk by increasing the external magnetic  
13 field (See zoomed images). Figure 1c indicates the simulated magnetic structures (See  
14 Methods)<sup>45</sup>, which match well with the experimentally observed structures.

15           The detailed 3D magnetization configurations of vortex core structures (marked by  
16 the yellow dashed box in Figure 1c) are displayed in Figure 1d. The volumes of vortex core  
17 structures with  $m_z \leq -0.8$  are indicated by blue colour. One can see that as the field varies,  
18 the shape of the vortex core structure changes and the vortex core structure is transformed  
19 from a one-dimensional (1D) vortex core structure to a 2D vortex core structure containing a

1 domain wall. At  $H_x = 0$  mT, a typical 1D vortex core structure (hereafter, called VC<sub>1</sub>  
2 structure) is observed; the vortex cores on the top and bottom surfaces are coaxially aligned,  
3 which supports that the VC<sub>1</sub> structure is a 1D vortex core structure (See orange dotted arrow).  
4 In the vortex core structure at  $H_x = 12$  mT (hereafter, called VC<sub>2</sub> structure), the vortex cores  
5 on top and bottom surfaces are still coaxially aligned like VC<sub>1</sub> structure, which supports that  
6 VC<sub>2</sub> structure is also a 1D structure (See orange dotted arrow). However, unlike VC<sub>1</sub>  
7 structure, the shape of VC<sub>2</sub> structure is slightly expanded along the horizontal direction and  
8 the magnetization of the VC<sub>2</sub> structure is not completely uniform along the thickness of the  
9 disk, which might occur to compensate for the demagnetization energy induced by the vortex  
10 core structure shifting toward the edge of the disk. At  $H_x = 24$  mT, the vortex core structure  
11 (hereafter, called VC<sub>3</sub> structure) is largely deformed. The vortex cores located on the top and  
12 bottom surfaces of the disk are no longer coaxial and the two vortex cores on the top and  
13 bottom surfaces of the disk are connected through the domain wall stretched along the  $x$ -axis  
14 (See Supplementary Figure 1 and Supplementary Note 1), which indicates that the VC<sub>3</sub>  
15 structure is clearly a 2D vortex core structure (See orange dotted arrows)<sup>21,40,46-51</sup>. We  
16 confirmed that the dimensional change of the vortex core structure starts occurring at  $H_x = 15$   
17 mT, and the domain wall connecting the vortex cores on the top and bottom surfaces of the  
18 disk gets longer as  $H_x$  increases until the vortex core structure is annihilated at  $H_x = 62$  mT  
19 (See Supplementary Figure 2 and Supplementary Note 2). Additionally, it was confirmed that

1 the dimensional change of vortex core structure by applying magnetic field only occurs when  
2 the disk is thicker than or equal to 70 nm in the Py circular disk of  $D = 3 \mu\text{m}$  (See  
3 Supplementary Figure 2 and Supplementary Note 2). It is noticed that the observed  
4 dimensional change of vortex core structure is analogous to the one achieved by changing the  
5 geometry of the disk from square to the rectangle<sup>51</sup>. The results in Figure 1 demonstrate that  
6 the shape and dimension of vortex core structure in thick ferromagnetic disks can be  
7 controlled simply by applying in-plane magnetic fields.

8

## 9 **Dynamics of 1D vortex core structures**

10 To investigate the oscillation mode of vortex core structures formed with varying  
11 external magnetic fields, we performed time-resolved MTXM measurements<sup>44</sup> (See  
12 Methods). To excite the dynamic motions of the vortex core structures, we injected the  
13 magnetic field pulse with an amplitude of 1 mT and a pulse width of 1.12 ns to the disk along  
14 the  $-x$ -axis. Figures 2a and 2b show the representative snapshots of the dynamic motions of  
15  $\text{VC}_1$  and  $\text{VC}_2$  structures, respectively. To track the position of vortex core structures, we  
16 defined area  $A$  of the vortex core structure with the normalized MTXM contrast less than 0.2  
17 as denoted by the red closed curves (See Figure 2c and Methods). Both vortex core structures  
18 show the clockwise (CW) gyrotropic motion (See Figures 2a, 2b, Supplementary Movies 1,  
19 2, and Supplementary Figure 3). However, the shapes of the two vortex core structures



1 become distinct from each other during their dynamic motions. The shape of the  $VC_2$   
2 structure, indicated by the red closed curves in Figure 2b, is varied from (to) circular to  
3 (from) elliptical shape during its dynamic motion, whereas the shape of the  $VC_1$  structure  
4 stays the same, circular shape over the dynamic process. To quantitatively analyse the change  
5 of shape and size of those vortex core structures, we measured the variation of  $A$  ( $\Delta A$ ) during  
6 their dynamic motions. Figure 2d clearly shows that unlike the case of the  $VC_1$  structure  
7 showing subtle random fluctuations,  $\Delta A$  of the  $VC_2$  structure is largely and periodically  
8 varied during its dynamic motion. It should be noticed that the noticeable changes of shape  
9 and size have never been reported in the dynamic motion of vortex core structures in typical  
10 thin ferromagnetic disks<sup>22,23</sup>.

11 For deeper understanding of the shape and size variation of the  $VC_2$  structure, we  
12 performed micromagnetic simulations for the dynamic motions of both  $VC_1$  and  $VC_2$   
13 structures (See Methods). Figures 2e and 2f illustrate the simulated magnetization images  
14 during the dynamic motions of  $VC_1$  and  $VC_2$  structures, respectively. The shape and size of  
15 the  $VC_2$  structure noticeably change during the dynamic motion as observed in experiments  
16 unlike those of the  $VC_1$  structure (Figures 2e, 2f, Supplementary Movies 3 and 4). Detailed  
17 3D magnetization configurations of  $VC_1$  and  $VC_2$  structures during their dynamic motions  
18 were investigated to clearly interpret the change of shape and size of the  $VC_2$  structure seen in  
19 2D images, respectively (Figures 2e and 2f). The respective trajectory curves of vortex core

1 motions on the top and bottom surfaces of the disk are added. For the  $VC_1$  structure, the  
2 gyrotropic motions with circular trajectories are observed in both vortex cores on the top and  
3 bottom surfaces. In the  $VC_2$  structure, however, vortex cores show the gyrotropic motions  
4 with elliptical trajectories. Interestingly, the major axis of the elliptical trajectories observed  
5 in the  $VC_2$  structure is aligned to the axis rotated by an angle of  $|\theta| \sim 35^\circ$  with respect to the  
6 magnetic field pulse direction ( $x$ -axis,  $|\theta| = 0^\circ$ ), which is in sharp contrast to previous reports  
7 that the major axis of the elliptical trajectory of vortex core gyrotropic motion in off-  
8 resonance is aligned to be parallel ( $x$ -axis,  $|\theta| = 0^\circ$ ) or perpendicular ( $y$ -axis,  $|\theta| = 90^\circ$ ) to the  
9 magnetic field pulse direction ( $x$ -axis,  $|\theta| = 0^\circ$ )<sup>31,32</sup>. More importantly, the directions of major  
10 axes of the elliptical trajectories of vortex core motions on the top and bottom surfaces are  
11 not aligned. The major axis of the elliptical trajectories of the vortex cores of the top and  
12 bottom surfaces are aligned to the axis rotated by  $\theta = -35^\circ$  and  $\theta = +35^\circ$ , respectively.

13         It is worth noting that the vortex core on the top surface is slightly lagging behind  
14 that on the bottom surface in both  $VC_1$  and  $VC_2$  structure, which indicates that there is a  
15 phase difference in the gyrotropic motions of the vortex cores of the top and bottom surfaces  
16 (Figure 2g). The non-zero phase difference of the gyrotropic motions of vortex cores on the  
17 top and bottom surfaces causes structural strain of the vortex core structure and is reflected as  
18 a slightly inclined structure in the thickness direction.<sup>34</sup> We estimated the phase differences of  
19 the gyrotropic motions of vortex cores on the top and bottom surfaces  $\Delta\delta$  during the dynamic

1 motion of  $VC_1$  and  $VC_2$  structures (Figure 2h). In the  $VC_1$  structure, the  $\Delta\delta$  occurred between  
2 the two vortex cores on the top and bottom surfaces remains the same over the dynamic  
3 motion (blue line in Figure 2h). Surprisingly,  $\Delta\delta$  in  $VC_2$  structure is periodically varied  
4 during the dynamic motion of the  $VC_2$  structure (red line in Figure 2h), which is probably due  
5 to the different directions of major axes of the elliptical trajectories of the vortex cores on the  
6 top and bottom surfaces (See Supplementary Movie 5). Based on the simulations results  
7 (Figures 2e-2h), it can be understood that the shape and size of  $VC_1$  structure rarely varied  
8 (Figures 2a and 2d) due to the  $\Delta\delta$  remaining constant in the structure (Figure 2h). On the  
9 other hand, the variation of the  $\Delta\delta$  of the  $VC_2$  structure (Figure 2h) causes the periodic shape  
10 change of the  $VC_2$  structure from (to) circular to (from) elliptical shape as shown in Figures  
11 2b and 2d.

12

### 13 **Dynamics of the 2D vortex core structure**

14 Figure 3 shows the dynamic motion of the  $VC_3$  structure, which is significantly  
15 different from those of  $VC_1$  and  $VC_2$  structures (See Figure 3a and Supplementary Movie 6).  
16 The flexure oscillation of the  $VC_3$  structure with the lateral motion and severe shape  
17 deformation is witnessed as shown in Figure 3a. The position and shape changes of the  $VC_3$   
18 structure during its dynamic motion are clearly observed as seen in green areas (right panel of  
19 Figure 3a). In Figure 3, the black and red curves represent the initial position of the  $VC_3$

1 structure at  $t = 0$  ns and its perturbed position triggered by the same magnetic field pulse  
2 applied to VC<sub>1</sub> and VC<sub>2</sub> structures.

3 Figure 3b displays the simulated magnetization image of the VC<sub>3</sub> structure and 3D  
4 magnetization configurations during the dynamic motion. It is noticed that the domain wall  
5 portion of the VC<sub>3</sub> structure shows the flexure oscillation as well as the lateral motion clearly  
6 visualized in experimental results (Figure 3a). It expands and shrinks repetitively in the  
7 horizontal direction (See Supplementary Movie 7). We traced the change of green areas in  
8 Figure 3a and 3b to quantitatively estimate the position change of the VC<sub>3</sub> structure (Figure  
9 3c) and found that the position of the VC<sub>3</sub> structure was largely fluctuated (Figure 3c) after  
10 the initial lateral motions triggered by magnetic field pulse injected.

11 Our micromagnetic simulation verified that while the domain wall portion of the VC<sub>3</sub>  
12 structure experiences the flexure oscillation with the rigorous lateral motion (Figure 3b), the  
13 vortex cores on the top and bottom surfaces of the disk still show gyrotropic motions similar  
14 to those of VC<sub>1</sub> and VC<sub>2</sub> structures (Figure 3d). Figure 3d exhibits that the trajectory of the  
15 vortex core motions on the top and bottom surfaces (VC<sup>Top</sup> and VC<sup>Bot</sup>) are elliptical as  
16 observed in the dynamic motion of the VC<sub>2</sub> structure. However, vortex cores on the top and  
17 bottom surfaces of the VC<sub>3</sub> structure show not only the phase difference but also considerably  
18 different gyrotropic radius. Those differences of phase and gyrotropic radius of vortex cores  
19 on the top and bottom surfaces that occurred during the dynamic motion of the VC<sub>3</sub> structure

1 might be responsible for the flexure oscillation and shape deformation of the domain wall  
2 connecting the two cores on surfaces. As the dimension of the vortex core structure changes  
3 from 1D to 2D, the dynamic motion of the vortex core structure becomes more complex with  
4 the oscillation of the domain wall in addition to the gyrotropic motions of vortex cores on  
5 surfaces.

6

### 7 **Oscillation modes of vortex core structures with different dimensions.**

8 To investigate oscillation modes of 1D and 2D vortex core structures, we obtained  
9 the fast Fourier transformation (FFT) power spectra for the VC<sub>1</sub> and VC<sub>3</sub> structures taken  
10 from MTXM measurements (Figure 4a and Methods). The peak in FFT power spectra  
11 indicates an individual oscillation mode of vortex core structures. The blue and red lines in  
12 Figure 4a indicate the FFT power spectrum for the VC<sub>1</sub> and VC<sub>3</sub> structures. It clearly  
13 indicates the frequency of oscillation modes of 1D vortex core structures is different from  
14 those of 2D vortex core structures. Moreover, the number of peak increases in the frequency  
15 range from MHz to sub-GHz as the dimension of the vortex core structure changes from 1D  
16 to 2D indicating that the dimensional change of the vortex core structures leads to the  
17 emergence of the oscillation modes with sub-GHz frequency. To corroborate the  
18 experimental observation, we performed micromagnetic simulation (Figure 4b and Methods).  
19 Figure 4b shows FFT power spectra for the vortex core structures with varying  $H_x$ , obtained

1 from the micromagnetic simulation. Each branch in FFT power spectra indicates an  
 2 individual oscillation mode of vortex core structures. The frequencies of two oscillation  
 3 modes in the low field region ( $H_x < 12$  mT) where VC<sub>1</sub> structure is stabilized, are rarely  
 4 changed. However, at  $12 \text{ mT} \leq H_x < 15$  mT where VC<sub>2</sub> structure is formed, the frequencies  
 5 of both oscillation modes alter, which suggests that the shape change of the vortex core  
 6 structure such as the expansion of the core observed in VC<sub>2</sub> structure results in the change of  
 7 oscillation frequency. More importantly, the drastic change of the FFT power spectra is  
 8 witnessed around  $H_x = 15$  mT where the dimensional change of the vortex core structure  
 9 occurs. For 1D vortex core structures, VC<sub>1</sub> and VC<sub>2</sub> structures ( $H_x < 15$  mT), there are only  
 10 two distinct modes denoted by  $F_0^{1D}$  and  $F_1^{1D}$  with large and small powers. When the 1D vortex  
 11 core structure is transformed into the 2D vortex core structure ( $H_x > 15$  mT) and the VC<sub>3</sub>  
 12 structure is established, various oscillation modes over a wide range of frequencies from  
 13 MHz to sub-GHz appear. The  $F_0^{1D}$  and  $F_1^{1D}$  modes are split into five modes, denoted by  $F_0^{2D}$ ,  
 14  $F_1^{2D}$ ,  $F_2^{2D}$ ,  $F_3^{2D}$ , and  $F_4^{2D}$  (Figure 4b). It is noted that intensities of  $F_2^{2D}$ ,  $F_3^{2D}$ , and  $F_4^{2D}$  are  
 15 relatively small compared to those of  $F_0^{2D}$ , and  $F_1^{2D}$ .

16 The modes of 1D and 2D vortex core structures are schematically illustrated in

1 Figures 4c-4e, which were confirmed by calculating inverse FFT corresponding to each  
 2 oscillation mode (See Supplementary Figures 4, 5, Supplementary Notes 3 and 4). For the 1D  
 3 vortex core structure (Figure 4c, Supplementary Figure 4 and Supplementary Note 3), mode  
 4  $F_0^{1D}$  corresponds to the gyrotropic motion of the vortex core structure, which is uniformly  
 5 excited in the thickness direction without any node. Mode  $F_1^{1D}$  still corresponds to the  
 6 gyrotropic motion of the vortex core structure, but in this case, at the centre of the vortex core  
 7 structure in the thickness direction, the gyrotropic motion is not excited due to the node  
 8 formed at the centre of the vortex core structure. That is, modes  $F_0^{1D}$  and  $F_1^{1D}$  are the zeroth-  
 9 and first-order gyrotropic modes of vortex core structures, respectively. The modes  $F_0^{2D}$ ,  
 10  $F_1^{2D}$ , and  $F_2^{2D}$  of 2D vortex core structures (Figures 4d, Supplementary Figure 5, and  
 11 Supplementary Note 4) correspond to the gyrotropic motions of vortex cores on the top and  
 12 bottom surfaces as well as the lateral motion of the domain wall. Similar to the modes of the  
 13 1D vortex core structure, mode  $F_0^{2D}$  corresponds to dynamic motion without a node, and  
 14 mode  $F_1^{2D}$  represents dynamic motion including a node at the centre of the domain wall.

1 Additionally, it is found that the mode  $F_2^{2D}$  includes two nodes. Namely, the modes  $F_0^{2D}$ ,  
2  $F_1^{2D}$ , and  $F_2^{2D}$  are the zeroth-, first-, and second-order oscillation modes of the 2D vortex  
3 core structure, respectively. The modes  $F_3^{2D}$ , and  $F_4^{2D}$  correspond to the modes where the  
4 spin-wave propagates along the domain wall while the gyrotropic motions of vortex cores  
5 occur on the top and bottom surfaces. The spin-waves in modes  $F_3^{2D}$  and  $F_4^{2D}$  have different  
6 oscillation phases from each other. In mode  $F_3^{2D}$ , the vortex cores on the top surface shows  
7 the counter-clockwise (CCW) gyrotropic motion while the vortex cores on the bottom surface  
8 shows CW gyrotropic motion. In contrast, in mode  $F_4^{2D}$ , both vortex cores on the top and  
9 bottom surfaces show CW gyrotropic motion (See Figure 4e and Supplementary Note 4). The  
10 superposition of multiple oscillation modes is reflected by the flexure oscillation of the VC<sub>3</sub>  
11 structure including noticeable motion change observed in the experiment. The results in  
12 Figure 4 support that the oscillation properties of vortex core structures such as  
13 eigenfrequency, the number of oscillation modes, and the range of oscillation frequency,  
14 which are important features for developing vortex-based nano-oscillator, can be easily tuned  
15 by manipulating the shape and dimension of vortex core structure within a single magnetic



1 disk.

2           In summary, we demonstrate that the oscillation modes of vortex core structures can  
3 be controlled over the wide range of frequencies from MHz to sub-GHz by manipulating the  
4 shape and dimension of the vortex core structure within a single ferromagnetic disk. The  
5 observed various oscillation modes of the vortex core structure can be electrically excited by  
6 spin-transfer torque<sup>13,52</sup> and detected by magnetoresistance effects<sup>13</sup>. Moreover, the oscillation  
7 modes with sub-GHz frequency can be selectively excited based on the  
8 constructive/destructive interference phenomena, and therefore can be implemented into  
9 nano-devices. Our findings provide a fundamental understanding of the oscillation nature of  
10 spin structures and its dependency on the shape and dimension of spin structures, which  
11 would be essential information for the development of nano-oscillator and also bio-inspired  
12 devices utilizing the oscillation.

13

## 1 **Methods**

### 2 **Sample fabrication.**

3           The electrode of Ti (5 nm)/Au (50 nm) was fabricated on a 100 nm thick X-ray  
4 transparent silicon-nitride ( $\text{Si}_3\text{N}_4$ ) membrane to apply an oersted field. On the electrode, Py  
5 circular disk was deposited using the dc sputtering. The circular disk of a diameter  $D = 3 \mu\text{m}$ ,  
6 and a thickness  $h = 100 \text{ nm}$  was patterned by electron-beam lithography and lift-off  
7 processing.

8

### 9 **X-ray imaging and time-resolved measurement.**

10           The magnetization components in a Py circular disk were directly observed by  
11 utilizing full-field magnetic transmission X-ray microscopy (MTXM) at XM-1 beamline  
12 6.1.2 the Advanced Light Source (ALS).<sup>1</sup> Out-of-plane magnetic components were imaged at  
13 the Fe  $L_3$  X-ray absorption edge (708 eV). To image out-of-plane magnetic components,  
14 samples mounted with respect to the X-ray propagation direction. The MTXM contrasts  
15 represent a projection of out-of-plane magnetic components along the thickness direction.  
16 The images were normalized by an image with opposite photon helicity to enhance the  
17 MTXM contrasts.

18           The time-resolved measurement for X-ray imaging of dynamic behaviour of vortex  
19 core structures was performed by utilizing the stroboscopic pump-probe technique at two-  
20 bunch mode of the ALS where X-ray is injected with the frequency of 3.33MHz. We injected  
21 the Gaussian pulse of the amplitude  $V_{pp} = 2\text{V}$  and pulse width of 1.12 ns in Au electrodes.  
22 The injected pulse generates an oersted field pulse of the amplitude of 1 mT and a pulse  
23 width of 1.12 ns along  $-x$ -axis to excite the dynamic motion of vortex core structures in a Py

1 circular disk. By tuning the delay time between pump (field pulse) and probe (X-ray pulse),  
2 the time-resolved MTXM images are measured.

3

#### 4 **Micromagnetic simulation.**

5 To specify the detailed magnetization configurations of spin structures and its  
6 dynamics, we carried out the micromagnetic simulation by using mumax<sup>3</sup> code<sup>45</sup> that can  
7 solve numerically the Landau-Lifshitz-Gilbert (LLG) equation:

8  $\partial \mathbf{M} / \partial t = -\gamma_0 (\mathbf{M} \times \mathbf{H}_{\text{eff}}) + (\alpha / |\mathbf{M}|) (\mathbf{M} \times \partial \mathbf{M} / \partial t)$  with the local magnetization vector  $\mathbf{M}$ , the

9 gyromagnetic ratio  $\gamma_0$ , the effective field  $\mathbf{H}_{\text{eff}}$ , and the phenomenological damping constant

10  $\alpha$ .<sup>53,54</sup> We employed a Py circular disk of a diameter  $D = 3 \mu\text{m}$  and a thickness  $h = 100 \text{ nm}$

11 with the mesh size of  $4 \times 4 \times 4 \text{ nm}^3$ , which has exactly same dimension with the disk

12 measured in our experiments. We used the typical material parameters of Py, i.e., saturation

13 magnetization  $M_s = 800 \text{ kA/m}$ , exchange stiffness  $A_{\text{ex}} = 13 \text{ pJ/m}$ , and damping constant  $\alpha =$

14 0.01. To excite the dynamic motion of vortex core structure, we applied Gaussian field pulses

15 with the amplitude of 1 mT and the pulse width of 1.12 ns in  $-x$ -axis.

16

#### 17 **Capturing position and area of vortex core structures in MTXM images.**

18 To analyse the dynamics of spin structures quantitatively, MTXM contrasts were  
19 processed by Gaussian fitting. After Gaussian fitting, we normalized the MTXM contrasts.

20 For the 1D vortex core structures ( $H_x = 0$ , and 12 mT), the area of the vortex core structure

21 was defined as the area where the normalized MTXM contrast is smaller than 0.2. The

22 position of the vortex core structure was determined as the centre of mass of the area of the

1 vortex core structure. For the 2D vortex core structure ( $H_x = 24$  mT), we captured the position  
2 of the 2D vortex core structure, the minimum value of MTXM contrasts.

3

#### 4 **Fast Fourier Transformation (FFT).**

5 In experiments, we obtained frequency spectra for the 1D and 2D vortex core  
6 structures by performing fast Fourier transformation (FFT) of  $x$ -position of the VC<sub>1</sub>  
7 (Supplementary Figure 3), and the shifted area of VC<sub>3</sub> structures (Figure 3c). To specify the  
8 oscillation mode of vortex core structures depending on the shape and dimension, by utilizing  
9 micromagnetic simulation, we applied the additional in-plane magnetic field with an  
10 amplitude of 1 mT to shift the vortex core structures from the initial position under static in-  
11 plane field  $H_x$  in the  $x$ -axis and turned off the additional magnetic field. We obtained  
12 frequency spectra with the frequency resolution of 10 MHz by performing FFT of the  
13 oscillation of magnetization vector at each discrete cell with varying  $H_x$ .

14

15 **Data availability.** The data that support the findings of this study are available from the  
16 corresponding author upon reasonable request.

17

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10

11 **Author Contributions**

12 H.-S. H., M.-Y. I., K.-S. L. designed and planned the research. H.-S. H., S. L., M.-S. J., N.  
13 K., M. K., H.-J. O., Y.-S. Y., M.-Y. I., K.-S. L performed the experiments. S. L., M.-S.J., Y.-  
14 S. Y., W. C., J.-I. H. prepared the samples. H.-S. H., M.-Y. I., K.-S. L. analysed data. K.-S.  
15 L., H.-S. H. carried out the micromagnetic simulations. H.-S. H., M.-Y. I., K.-S. L. prepared  
16 the manuscript, which incorporates critical input from all authors.

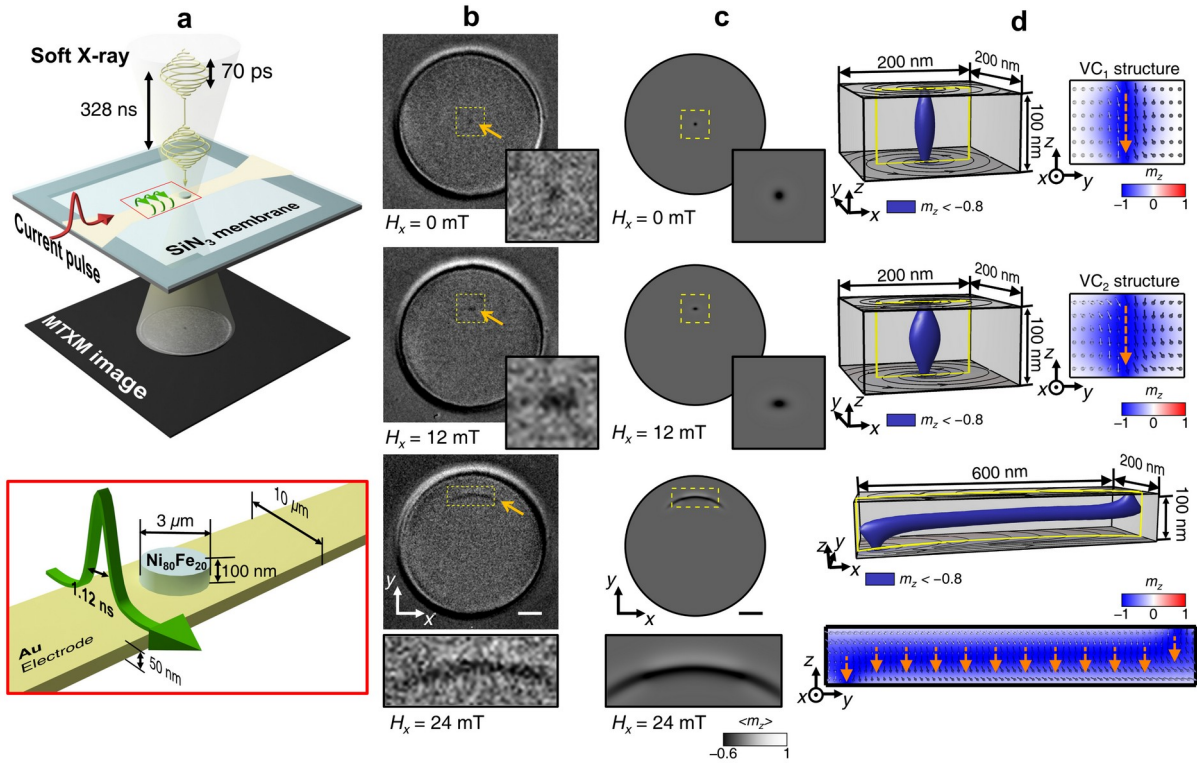
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18 **Competing financial interests**

19 The authors declare no competing financial interests.

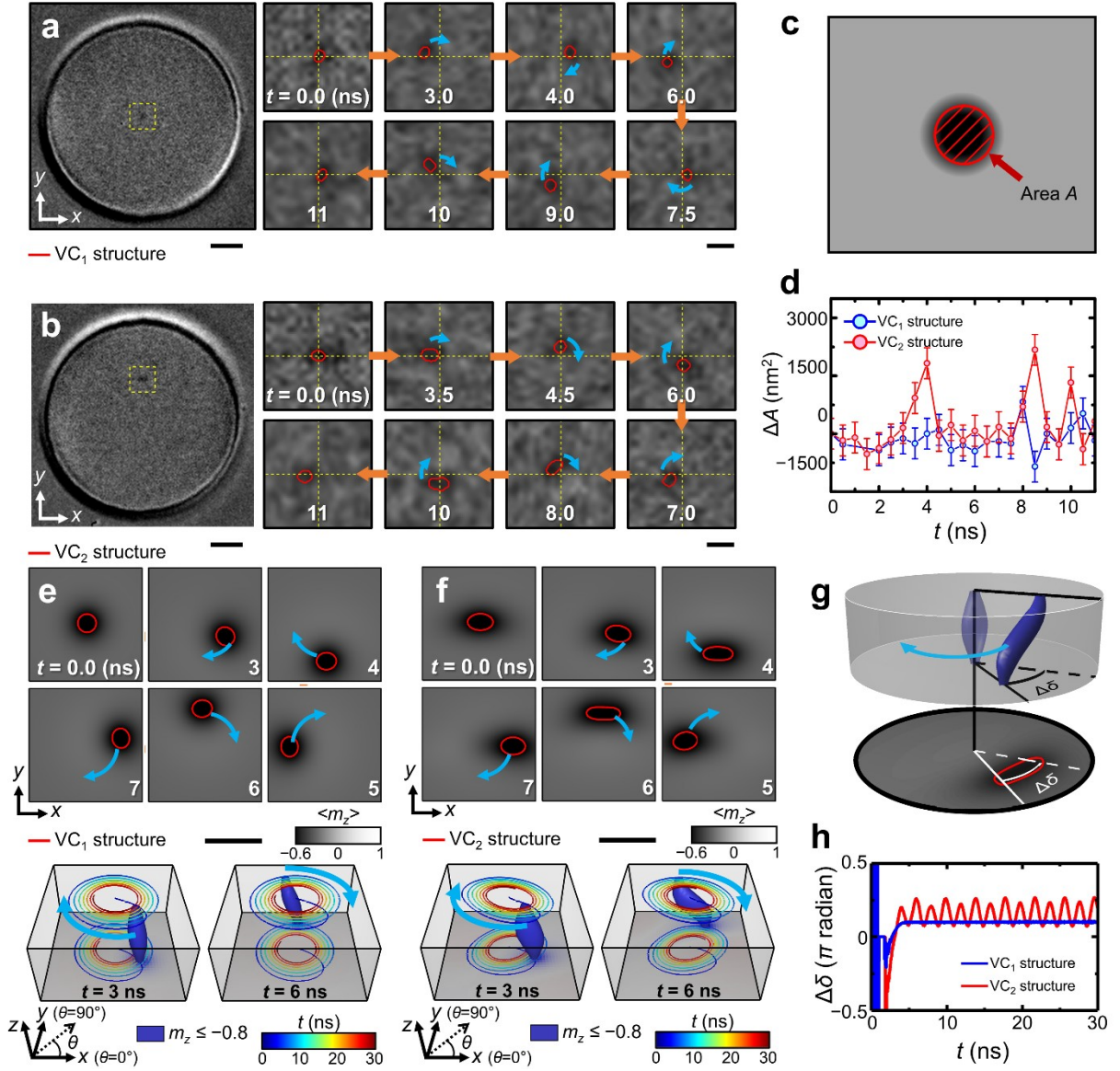
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# 1 Figures



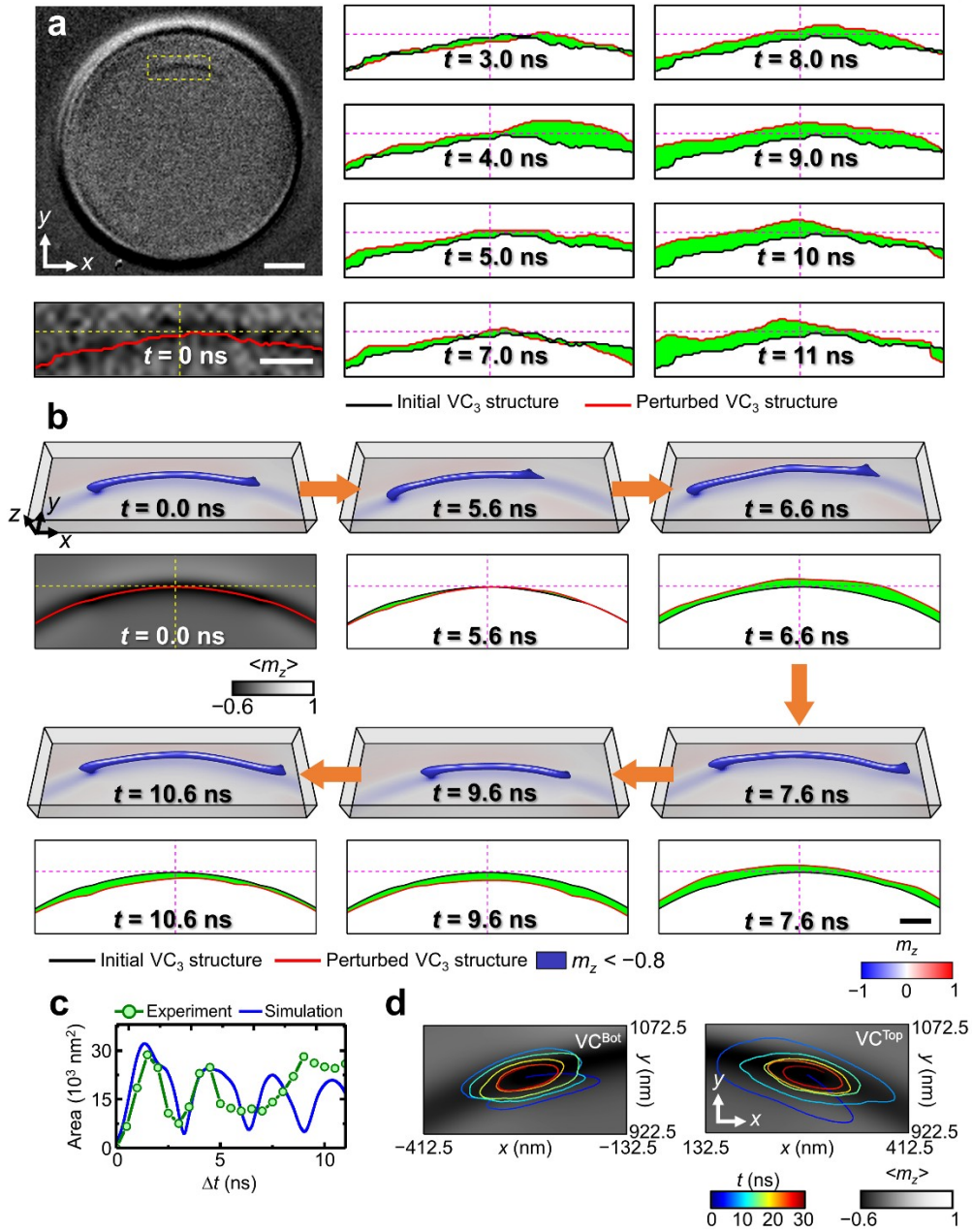
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3 **Figure 1 | Controlling the shape and dimension of the vortex core structure.** (a)  
 4 Schematic of the experimental setup of the magnetic transmission X-ray microscopy  
 5 (MTXM). The zoomed image in the red box is inserted with the permalloy (Py, Ni<sub>80</sub>Fe<sub>20</sub>)  
 6 circular disk of diameter 3 μm and thickness 100 nm on 50 nm-thick Au electrode. (b)  
 7 out-of-plane magnetic structures observed in a Permalloy (Py, Ni<sub>80</sub>Fe<sub>20</sub>) circular disk of diameter  
 8 3 μm and thickness 100 nm by magnetic transmission X-ray microscopy (MTXM) with  
 9 varying the magnetic field H<sub>x</sub> in the x-axis (scale bar: 500 nm). Zoomed images of the out-of-  
 10 plane magnetic structures are inserted. The black and white contrasts indicate the downward  
 11 and upward out-of-plane magnetic components, respectively. The vortex core structures are  
 12 indicated by orange arrows. (c) Simulated magnetization images corresponding to MTXM  
 13 images (scale bar: 500 nm). (d) The internal magnetization configurations of vortex core  
 14 structures marked by the yellow dashed box in Fig. 1c. The magnetization configurations  
 15 representing the cross-section of vortex core structures are visualized.



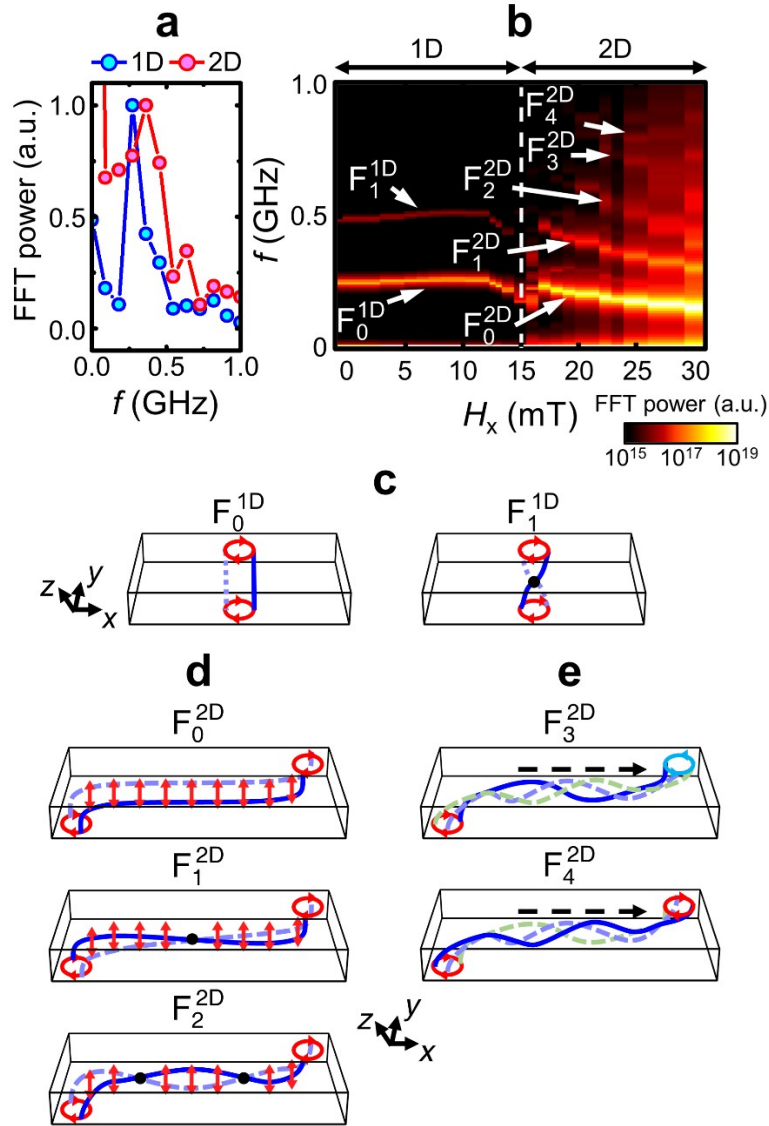
**Figure 2 | The dynamics of 1D vortex core structures.** **a-h**, Time-resolved X-ray images of the dynamic motions of VC<sub>1</sub> (**a**) and VC<sub>2</sub> (**b**) structures, respectively (scale bars in representative MTXM images and zoomed images are 500 nm and 100 nm, respectively). (**c**) The area *A* inside the red closed curve indicates the vortex core structure. (**d**) The variation of the *A* as a function of the time. The blue and red lines indicate the variation of *A* of VC<sub>1</sub> and VC<sub>2</sub> structures. The series of simulated magnetic images for the dynamic motions of VC<sub>1</sub> (**e**) and VC<sub>2</sub> (**f**) structures (above) in micromagnetic simulations (scale bar: 100 nm) and the snapshots of their internal magnetization structures captured at *t* = 3 and 6 ns with trajectory curves (below) of vortex cores on the top and bottom surfaces of the disk. (**g**) The schematic illustration of the X-ray imaging of the vortex core structure, and the phase difference between vortex cores on the top and bottom surfaces  $\Delta\delta$ . (**h**) The variation of  $\Delta\delta$  during the dynamic motions of vortex core structures. The blue and red lines indicate  $\Delta\delta$  of VC<sub>1</sub> and VC<sub>2</sub> structures, respectively.

15



1  
2 **Figure 3 | The dynamics of the 2D vortex core structure.** a-d, (a) The series of magnetic  
3 images for the dynamic motion of the VC<sub>3</sub> structure taken by time-resolved MTXM. The  
4 black line indicates the initial position of the VC<sub>3</sub> structure at  $t = 0$  ns. (scale bars in the  
5 representative MTXM images and zoomed images: 500 nm and 300 nm, respectively). (b)  
6 The snapshot images of the 3D magnetization configurations (above) of VC<sub>3</sub> structures and  
7 the core structures (below), which were obtained from micromagnetic simulation during the  
8 dynamic motion (scale bar: 100 nm). The red lines in Figs. 3a and 3b indicate the perturbed  
9 position of the VC<sub>3</sub> structure. The area between those two lines is filled in green colour. (c)  
10 The variations of the green-coloured area obtained from the experiment (green line) and  
11 simulation (blue line) data in Figs. 3a and 3b which show the perturbation of the dynamic

- 1 motions of the  $VC_3$  structure, quantitatively. **(d)** The trajectory curves of vortex cores on the
- 2 top and bottom surfaces of the disk obtained from the micromagnetic simulation.



1  
2 **Figure 4 | The oscillation modes of vortex core structures formed with varying the in-**  
3 **plane magnetic field. a-d, (a)** The fast Fourier transformation (FFT) power spectra for the  
4 1D and 2D vortex core structures obtained from the MTXM measurements. The red and blue  
5 lines indicate the normalized FFT power spectrum of VC<sub>1</sub> and VC<sub>3</sub> structures, respectively.  
6 **(b)** FFT power spectra for vortex core structures as function of  $H_x$  taken from micromagnetic  
7 simulation. The white dashed line indicates  $H_x = 15$  mT where the dimensional change of the  
8 vortex core structure from 1D to 2D occurs. The schematic illustrations of the zeroth- and  
9 higher-order modes of 1D ( $F_0^{1D}$ , and  $F_1^{1D}$ ) **(c)** and 2D ( $F_0^{2D}$ ,  $F_1^{2D}$ , and  $F_2^{2D}$ ) **(d)** vortex core  
10 structures. **(e)** The modes  $F_3^{2D}$ , and  $F_4^{2D}$  where spin-wave propagates along the domain wall  
11 of the 2D vortex core structure are schematically illustrated. The black dashed line indicates  
12 the spin-wave propagation direction. The clockwise and counter-clockwise gyrotropic  
13 motions of vortex cores on the top and bottom surfaces are denoted by the red and light blue  
14 arrows, respectively. The black dashed line indicates the spin-wave propagation direction.