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1 **Kayak drifter surface velocity observation for 2D hydraulic model validation**

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3 Running head: Kayak drifter surface velocity for 2D model validation

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21

22 **ABSTRACT**

23 Advances in remote sensing, informatics, software and microprocessors enable meter-
24 resolution two-dimensional (2D) hydrodynamic models that produce nearly a census of
25 ecohydraulic conditions over long river segments with 10^5 to 10^8 computational elements.
26 It is difficult to test statistical and spatial model performance at such scope using fixed-
27 point velocity measurements, because field methods are so expensive, laborious, slow, and
28 restricted by safety factors. This study evaluated low-cost water surface particle tracking by
29 kayak with real time kinematic GPS for 2D model validation using 7.2 km of the lower
30 Yuba River in California. Observed flows were between 15 to 140 m^3/s , which were in-
31 channel up to and including bankfull conditions. The coefficients of determination between
32 5780 observations and 2D model predictions were 0.79 and 0.80 for velocity magnitude
33 and direction, respectively. When surface speed was downscaled and compared to modeled
34 depth-averaged velocity, median unsigned difference was 15.5%. Standard hydrological
35 model performance metrics affirmed satisfactory validation. Surface tracking provided the
36 novel benefit of enabling validation of velocity direction, and that testing found satisfactory
37 performance using all metrics. Having 10 to 1000 times more data enables robust statistical
38 testing and spatial analysis of both speed and direction, which outweighs the loss of depth-
39 averaged data. Both fixed-point and kayak particle tracking methods are useful tools to
40 help evaluate 2D model performance.

41 Keywords: 2D hydraulic modeling; hydraulic validation; river velocity; river drifters;
42 particle tracking

43

44 1. INTRODUCTION

45 For over 3,000 years people have recorded water velocity according to its literal definition by
46 tracking the displacement of surface particles along a path through time. According to Lumpkin
47 and Pazos (2007), surface particle tracking of ocean currents has been a common practice for
48 centuries, but real-time radio and satellite tracking modernized the technique to produce
49 continuous velocity vector data (Swallow, 1955; Davis, 1991). Today there are ~2,000 ocean
50 drifters perpetually. Surface drifter data is taken as observational truth to calibrate other ocean
51 observation systems (Ducet et al., 2000) and validate ocean circulation models (Lumpkin &
52 Garzoli, 2005; Blockley et al, 2012). Overall, surface drifters are a legitimate, accurate, and
53 widely accepted technology for surface water velocity observation (Fratantoni, 2001). Two
54 journal articles (Stockdale et al., 2007; Han et al., 2016) and some conference proceedings tested
55 drifters in nontidal rivers. Given the utility of drifters in validating ocean circulation models, this
56 study evaluates that for two-dimensional (depth-averaged) hydrodynamic (2D) models of rivers.

57 1.1. *Need For More 2D Model Validation*

58 Today, 2D modeling is essential for river research, management, and rehabilitation, because it
59 addresses spatial patterns of geomorphic processes and ecological conditions. This ascent
60 synergizes with rapid progress in meter-resolution remote sensing (Mandlbürger et al., 2015),
61 faster microprocessors, large informatics systems, and computational parallelization (Huxley &
62 Syme, 2016). Studies aiding 2D model development that address boundary conditions (Casas et
63 al., 2010), wetting/drying schemes (Tchamen & Kahawita, 1998), and mesh discretization
64 (Horritt et al., 2006) guide our understanding of model capabilities.

65 One aspect of 2D modeling is being left behind – validation of velocity vectors. Airborne,
66 boat, and ground technologies provide an abundance of depth data, while velocity validation
67 remains reliant upon fixed-point, scalar speed measurement. Few studies report vector validation,
68 as it requires precise orientation and a multidimensional sensor. Discussion of velocity methods
69 and validation, including advantages and limitations, are in the supplementary file.

70 1.2. *Large-Scale Particle Image Velocimetry*

71 Large-scale particle image velocimetry (LSPIV) can map surface velocity vectors in a fixed,
72 small domain by querying image frames through time (Fujita et al., 1998). Commonly, river
73 LSPIV involves mounting cameras onto telescoping poles, helicopters, or electric drones,
74 depending on cost, stability, flight time, and hazard considerations. Le Coz et al. (2010)
75 demonstrated both the potential and numerous challenges with this technology (see
76 supplementary file for further details).

77 1.3. *Kayak Surface Particle Tracking*

78 A handful of studies have piloted surface drifters with differential GPS in low-wind rivers to
79 obtain velocity along floating paths, but for meter-scale 2D models, real-time kinematic (RTK)
80 GPS is required (see supplementary section 1.3 for details). Drifters have fewer weather, flow,
81 and accessibility limitations than LSPIV and data processing is simpler. They can travel long
82 distances, operate for many hours, and sample a greater diversity of hydraulic conditions. For
83 example, in one six-hour float of 14.3 km, two people recorded 10,250 observations from 0–4.2
84 m/s, including in gyres and rapids.

85 When a river has gradually varying changes to velocity, then depth and the thickness of
86 the surface layer moving at the same velocity are key differences between oceans and rivers that

87 change the technological specifications for a drifter. Ocean drifters use drogues that are
88 submerged, tethered weights (or parachutes) to resist wind and move with the thick surface layer.
89 However, rivers are usually too shallow for drogues. Even without drogues, passive drifters get
90 stuck on the bed (Stockdale et al., 2007) or in vegetation.

91 Often 2D models simulate complex hydraulics with abrupt current accelerations that
92 drifters do not adjust to for some distance. This occurs at riffle/rapid entrances and exits,
93 dissipating jets, in shear zones between fast and slow currents, and in flow recirculations (i.e.
94 eddies or gyres) (Figure 1). The heavier a drifter is, the more it deviates when currents change
95 abruptly. Consequently, drifters in these settings cannot be passive. They need help to move with
96 accelerations. Today, the best solution is manual course correction.

97 This study investigated such challenging hydraulics. For a 100-m wide river, a manned
98 kayak is a suitable drifter, because it is $< 1\%$ of channel width and as wide as a computational
99 element. Hull displacement depends on boat specifications and operator weight, but can be ~ 10
100 cm. Operator weight aids drifter submergence deeper into the surface layer.

101 We have performed seven years of testing kayak drifter observation with people of
102 different paddling skills. Most of the time no manual correction is needed. People can be quickly
103 trained to make infrequent minor adjustments in complex hydraulics. Even a small vector
104 deviation is readily evident and countered almost instantly. Abundant bubbles and particles move
105 with the current for a kayaker to monitor current pattern. More may be added as needed.

106 Having a mindful operator enables beneficial operations that improve data collection,
107 processing, and analysis. An operator can start/stop data collection in response to GPS precisions
108 or an unsatisfactory kayak vector. An operator has control over the conditions being sampled to

109 sample diverse conditions in complex hydraulics at question in 2D model performance (Brown
110 & Pasternack, 2012).

111 *1.4. Study Objectives*

112 Given the goal of enhancing 2D model validation, study objectives involved (i) evaluating the
113 capabilities of kayak surface velocity vector measurement for 2D model validation; (ii)
114 comparing model-prediction errors of this technique with those of traditional fixed-point
115 validation; (iii) testing for discharge dependence of steady-state model performance; and (iv)
116 using drifter data to better evaluate spatial uncertainties in 2D models. Even though data from
117 drifters and fixed-point observations are different and the metrics to decide what constitutes
118 better performance vary between scientists, putting both types of data through thorough
119 validation procedures provides insights about their advantages and disadvantages. Secondly,
120 the supplementary file presents a model validation sensitivity analysis of the parameter used to
121 convert surface velocity to depth-averaged velocity. Regardless of surface particle tracking
122 method, this study develops and tests how such velocity data is used to evaluate 2D models.
123 Given strict journal page limits, full details and extra information for all sections of this study are
124 provided in a supplementary file, including figures referred to as “Figure S#” below.

125 **2. STUDY AREA**

126 The regulated 37.5 km lower Yuba River (LYR) begins downstream of Englebright Dam, fed by
127 a 3,490 km² catchment (Figure 2). It is a wandering cobble/gravel-bed river (Figure 1) with
128 sparse woody vegetation, little entrenchment, an average channel slope of 0.16%, and an average
129 bankfull width of 97 m. Daguerre Point Dam (DPD) is a low-height, historic, partial sediment
130 barrier present in the LYR that influences the longitudinal profile of the river. Water diversions

131 at DPD remove $\sim 1\text{--}10\text{ m}^3/\text{s}$ of the flow. River and diversion flows are quantified by gaging
132 stations along the river, as explained in the supplementary materials file. Due to the storage of
133 historical hydraulic mining sediments in the river valley and a relatively unconstrained winter
134 flood regime, the LYR is unique in the region for having rejuvenation of diverse geomorphic
135 units and streambed substrate (Wyrick & Pasternack, 2014; Pasternack & Wyrick, 2016).

136 3. METHODS

137 3.1. *2D Hydrodynamic Modeling*

138 Topography and bathymetry were mapped to produce a 1-m resolution DEM using ground-
139 based, boat-based, and airborne methods (Carley et al., 2012). To exemplify data resolution,
140 within and beyond the wetted area at $24.92\text{ m}^3/\text{s}$, overall point density downstream of the
141 Highway 20 Bridge was 59 and 554 points per 100 m^2 , respectively. As previously published in ten
142 journal articles (e.g. Wyrick & Pasternack, 2014; Gonzalez & Pasternack, 2015, Gibson &
143 Pasternack, 2016), SRH-2D (v. 2.1) was used to simulate meter-scale, non-vegetated, in-channel
144 river hydraulics in the LYR from 8.50 to $3,126\text{ m}^3/\text{s}$ (0.06 to 22 times bankfull discharge).

145 3.2. *Fixed-Point Hydraulic Data*

146 Fixed-point hydraulic data were obtained using standard methods detailed in the supplementary
147 materials. Locations were within close radio range ($\sim 0\text{--}3\text{ km}$) of an RTK GPS base station to
148 keep time latency low and base station corrections more accurate. A total of 199 fixed-point
149 observations of depth and velocity were made at $\sim 2\text{ m}$ intervals along 17 cross sections (Figure
150 S1), while a different set of 199 points captured water surface elevations. Data were collected on
151 different dates at steady, regulated discharges of 15.26 , 22.51 , and $22.57\text{ m}^3/\text{s}$.

152 3.3. *Kayak Velocity Measurement*

153 Kayak drifter velocity vector data (5780 observations) were collected at six discharges (17.61–
154 141.9 m³/s) between December 15, 2009 and July 1, 2010 along 7.2 km, but this whole length
155 was not traversed in one day. One path was done each day either upstream or downstream of
156 DPD. There was no attempt to replicate or differentiate paths for different days or flows. The
157 7.2-km length passed through 10 of the cross-sections. Others were located further upstream but
158 still in the same river conditions.

159 Kayakers simply got on a path and stayed on it. If the current took the boat closer to or
160 farther away from a bank, then so be it- that was left to chance. Today, we pause data collection
161 frequently to move to different velocity streamlines. This maximizes the range of velocities
162 observed, improves equal-effort sampling across the velocity range, and allows mapping of
163 recirculations.

164 To evaluate the efficacy of the drifting strategy to sample diverse hydrogeomorphic
165 conditions, kayak velocity point locations were analyzed for proximity to the riverbank toe (point
166 distance tool in ArcGIS[®] 10.x) and presence within each of the in-channel morphological units
167 (spatial join tool in ArcGIS[®] 10.x) mapped by Wyrick and Pasternack (2014). For the entire
168 LYR, the average width between bank toes is 59.4 m, so the average distance from bank toe to
169 centreline is 29.7 m. Relative to those metrics, the range of distances of kayak velocity
170 observations away from the bank toe was 0.03 – 37.6 m (median of 13.7 m, standard deviation of
171 6.9 m). When “close to bank” is defined as within 1/5 of the average half width of the river (<
172 5.94 m), then 13% of kayak velocity data met this criterion. Turning to morphological
173 representation, fast glide (1711 points) and run (1134) were sampled most. Chute, pool, slow
174 glide, riffle, and riffle transition each had 393-802 observations. The least sampled unit was

175 slackwater, which still had 97 observations. These data substantiate that repeatedly drifting along
176 a single streamline for several kilometers per day for a few days will capture hydraulic diversity.

177 Velocity vector equations are in the supplementary materials file. Velocity magnitude
178 was calculated as the horizontal displacement from one GPS position to the next, divided by the
179 change in time between position measurements. This value was assigned to the midpoint
180 coordinates. Velocity direction was assigned using the differences in northing and easting of
181 consecutive position measurements.

182 Kayak position was measured on a fixed time interval using a Trimble[®] R7 RTK GPS
183 rover linked by radio to a local R7 base station GPS within 3 km of the rover, yielding
184 centimetre-to-decimetre scale horizontal accuracy. GPS satellite clocks are specified to record
185 time to within 40 ns of Coordinated Universal Time (Allan et al., 1997), but GPS data collectors
186 only store values to the nearest 1 s. Initially, measurements were recorded at 3-s intervals, but the
187 time step was adjusted to 5 s in later runs (17.6 m³/s, 23.1 m³/s, and 141.9 m³/s) to reduce the
188 relative effect of GPS time-recording precision limitations on velocity calculations. For a fixed
189 sampling interval, it does not matter if the GPS clock is exactly on the integer second for each
190 sample, only that the sampling keeps a constant interval. Because the method of determining
191 time does not change over time, the sampling interval should remain fixed. In this case, slower
192 velocities are more prone to error than fast velocities, because they involve shorter distances, so
193 positional error is a larger fraction of distance. Velocity precision was calculated as the sum of
194 the GPS horizontal precisions for the two positions used to compute a velocity divided by the
195 time to traverse between the two positions. Any velocity with absolute precision worse than 0.03
196 m/s was discarded, so a strict quality criterion was applied.

197 3.4. *Data Analysis*

198 3.4.1. *Validation Data Preparation*

199 Validation data consisted of three types: fixed-point observations, unadjusted surface velocity
200 vectors, and adjusted (depth-averaged) velocity magnitude. For each location of an observation,
201 GPS coordinates were imported to ArcGIS[®]. Then model values there were interpolated from
202 triangulated irregular networks built using the irregular, meter-scale point clouds of model
203 outputs.

204 3.4.2. *Model Performance Indicators*

205 There are no standards for 2D model validation. Common metrics are reviewed by Pasternack
206 (2011), while others exist for hydrological validation (Moriassi et al., 2007). Concepts and
207 algorithms for validating 2D model velocity direction in river eddies are non-existent whereas
208 atmospheric and ocean studies often report visual comparisons. Metrics and their threshold
209 values are detailed in the supplementary file.

210 Metrics used herein include (i) basic statistical measures for signed and unsigned
211 deviations and percent differences; (ii) regression analysis metrics of slope, y-intercept, r^2 , p-
212 value, regression slope standard error, and regression intercept standard error; and (iii) the
213 hydrological metrics Nash-Sutcliffe efficiency (NSE), percent bias (PBIAS), and the root mean
214 square error-observations standard deviation ratio (RSR). Regression slope standard error is the
215 average distance that observed values fall from the regression line and thus indicates how wrong
216 the regression model is on average using the units of the response variable.

217 3.4.3. *Direct 2D Model Validation*

218 Validation metrics were computed using fixed-point depth and velocity data collected by
219 wading. They were also computed using observed kayak surface velocity direction versus

220 modeled velocity direction. For raw kayak surface velocity magnitude, the only viable test
221 involved regression analysis as surface and averaged velocities are related and different only by a
222 scaling coefficient (Hulsing et al., 1966; Rantz, 1982). That does not affect the regression's
223 coefficient of determination or p-value.

224 3.4.4. *Adjusting Kayak Surface Velocity To Mean Velocity*

225 A depth-averaged velocity constant (DAVC) of 0.71 was taken from unpublished profiles
226 collected at one site on the LYR by the authors, which also matched vertical velocity profile data
227 collected in a similar setting (Pasternack et al., 2006). Similar values of 0.72–0.79 were reported
228 by Dramais et al. (2011) for similar conditions. A DAVC sensitivity analysis is in supplementary
229 section 3.4.4.

230 3.4.5. *Testing Discharge Dependence of Model Error*

231 The number of flows to be observed at steady state and over what range for 2D model validation
232 is an important open question. Flood hazard models are used to protect society from extreme
233 events never observed, yet parameters are necessarily calibrated and validated during safe, steady
234 in-channel flows. If any aspect of a 2D model is discharge-dependent, it is the bed-roughness
235 parameter.

236 The deeper water is relative to bed roughness, the lower Manning's n might be.
237 Alternately, the increase in very rough, shallow areas along channel flanks that comes with
238 increasing discharge can offset the increased bed submergence in the thalweg to keep the overall
239 cross-sectional roughness the same. Increased roughness along the flanks affects thalweg
240 hydraulics (Abu-Aly et al., 2013).

241 There are no 2D model validation datasets as of yet involving meter-scale resolution
242 topography in which Manning’s n was held constant, and then velocity and depth errors were
243 inversely related to each other and both a function of relative submergence. Thus, fixed-point
244 and kayak validations were checked for any trend in velocity error as a function of depth. There
245 are also no specific tests of discharge-dependence of model performance, either. The kayak
246 method enabled such a test infeasible by wading. Validation was performed using only the subset
247 of velocities recorded during the lowest and highest observed flows (17.6 m³/s and 141.9 m³/s) to
248 determine whether validation results would differ from those using data from all flows and see if
249 the data plotted along the same trend line.

250 3.4.6. *Comparing Validation Outcomes*

251 Practitioners want to know what value they get for deploying a traditional fixed-point strategy or
252 this new kayak drifter strategy at the holistic level. This does not require head-to-head sampling
253 of the same points by the two methods, as it is a comparison of two strategies. One benefit in
254 attempting comparison is not to say that one method is necessarily “better” than another, but to
255 convey what kinds of outcomes are likely in each case and why. Another benefit is to reveal how
256 one’s sense of whether a model is validated or not might depend on the type and abundance of
257 data collected, which is currently not understood. Finally, each approach can do unique things, so
258 what is gained by trying direction validation and more spatial analysis of speed error? Readers
259 can judge for themselves what technical metrics and qualitative comparisons to value.

260 In our own assessment of fixed-point and kayak surface data collection methods for our future
261 validation needs, we found value in four comparisons. The ability of the kayak method to yield
262 abundant, diverse direction data is uncontested by typical fixed-point sampling, so that is not

263 comparable. First, the range of flows and depths where velocities were measured, as well as the
264 range of velocities, are meaningful comparative indicators of what each strategy can accomplish.
265 Model validation data should span actual conditions. Second, head-to-head scatter plot validation
266 tests need a roughly uniform distribution of velocity values as well as enough points in each
267 velocity bin to represent the distribution of prediction deviations about the mean value in each
268 bin. This was assessed using the velocity statistical data for each method. Third, all quantitative
269 validation metrics were compared between methods. Finally, locations with > 50% model error
270 were compared for the two techniques with a histogram analysis. Considered together, these
271 provided a broad-based evaluation of fixed-point versus kayak 2D model validation strategies
272 without necessarily aiming to say that one is better than another.

273 **4. RESULTS**

274 *4.1. 2D Model Validation Using Fixed-Point Velocities*

275 Fixed-point velocity magnitude data showed a typical 2D model validation outcome, with the
276 points generally along a 1:1 line for observed versus modelled and the best-fit line showing a
277 bias (Figure 3a). Model validation metrics using fixed-point data exceeded all performance
278 standards (Table 1). Thus, the 2D model is validated.

279 *4.2. 2D Model Validation Using Kayak Observations*

280 *4.2.1. Statistical Velocity Validation*

281 The results of DAVC sensitivity analysis are in the supplementary file. Using the DAVC value
282 of 0.71, performance indicators surpassed validation thresholds farther than they did using fixed-
283 point data (Figure 3b). There is so much data in the plot that it is not possible to see the outcome

284 that the majority of the residuals are very close to the 1:1 line; thus, it is necessary to focus on
285 the quantitative performance metrics (Table 1). Once again, the 2D model is validated by every
286 single metric comparing against kayak observations. Considering the standard error of the
287 regression slope and intercept values, both are low and they help to appreciate that a regression
288 plot with thousands of points often hides the true precision of the results, which in this case is
289 quite high. In fact, the standard error of the slope for the kayak data was 8.4 times lower than that
290 for the fixed-point data, while that of the intercept was 5.9 times lower. Similar to fixed-point
291 data, kayak data showed a bias in which low values were over-predicted and high values under-
292 predicted, indicating the typical 2D model problem of insufficient lateral velocity gradients.

293 Descriptive statistics revealed a mean difference of -0.095 m/s, standard deviation (SD)
294 of 0.228 m/s, mean velocity error of 4.4%, and error SD of 29.0%. Similar to the fixed-point data
295 and other studies, the kayak data found the largest errors at the lowest observed velocities
296 (Figure 4). The unsigned (aka absolute value) median error was 15.5%. Only seven observations
297 had absolute errors > 160% and they were all for very low velocities. When velocity was above
298 0.5 m/s, errors were almost all < 100%. Considering the cumulative distribution function of
299 velocity error for all the kayak data, 12.7, 58.7, and 90% of the modeled values were within 0.03,
300 0.15 m/s and 0.34 m/s, respectively.

301 4.2.2. *No Discharge Dependence of Model Error Found*

302 When steady state model performance was judged using only velocities observed at the highest
303 and lowest flows (n=1,336; DAVC=0.71), the r^2 was 0.80 and the slope was 0.90 (Figure 5).
304 This represents a 1.4% difference in the r^2 and a 9.4% difference in slope with the validation
305 performed for the entire dataset. The mean difference in velocities and SD was -0.072 m/s and
306 0.219 m/s, respectively, while the mean error was 6.1% (Table 2a). These represent 24, 4, and

307 39% changes, respectively, from the values obtained from the entire dataset. Considering the
308 cumulative distribution function of velocity error using only velocities observed at the highest
309 and lowest flows revealed that 12.5, 61.9, and 90.0% of modeled values were within 0.03, 0.15,
310 and 0.38 m/s, respectively.

311 When velocity deviations between the model and fixed-point data were regressed against
312 observed depth, there was no significant trend. The same outcome was obtained when deviations
313 between model and kayak velocities were regressed against modeled depths. These results
314 further affirm that there is no discharge dependence on model performance and there is no
315 control of relative submergence on velocity error when using a constant Manning's n in a 2D
316 model of a gravel/cobble river over the full range of in-channel flows. These findings are
317 important, as they go against expectation. Most likely, relative submergence is too small of an
318 effect for in-channel flows. If it matters anywhere, it is in the shallowest edge zone and in
319 vegetated terrain, where Manning's n increases to values of 0.1-0.3.

320 4.2.3. *Spatial Velocity Validation*

321 Spatial analysis of velocity deviations enabled by kayak data revealed consistent locations of
322 poor 2D model performance, either associated with localized DEM deficiencies or steep riverbed
323 slopes. The discussion of the former is not novel and is relegated to the supplementary file. The
324 study found consistently large differences at the entrances and exits of riffles, which is where
325 abrupt slope changes occur (Figure 6). Because the kayak was manned and kept moving at the
326 speed of the water in these locations, this error is attributable to the 2D model. Entrances and
327 exits of riffles are often steeply sloped, causing a violation of the 2D model's horizontal flow
328 assumption in exactly this fashion. The average difference for the three areas shown in Figure 6
329 was -0.18 m/s, with an absolute difference of 0.36 m/s, both of which are about double the values

330 for the entire dataset. We have observed this effect before in our other unpublished validation
331 datasets with fixed-point data, so we are confident to attribute this to the 2D model, but it is rare
332 to have cross-sections in these locations that are challenging to holding position in (whether by
333 wading or by motorboat), so there has been insufficient data to see this longitudinal effect clearly
334 until now.

335 4.2.4. *Directional Validation*

336 Velocity direction validation plots and metrics substantially exceeded common threshold values
337 for model performance (Table 1; Figure 7; Figure S8), though there were subpar locations.
338 Standard error of the regression slope and intercept were extremely low. The 2D model generally
339 performed within the 9° criterion (Table 2b). The mean raw direction difference was -0.11° with
340 a SD of 9.7° . Histogram analysis of differences revealed that 15% of model predicted values
341 were within 1° of observed values, 62% were within 5° , and 86% were within 10° . The mean
342 absolute error was 2.7% with a SD of 3.8%. A similar analysis of the directional error showed
343 that 88%, 98%, and 99.8% of predicted values had errors less than 5%, 10%, and 25%,
344 respectively.

345 Although almost all differences were $< 45^\circ$, there were 20 outliers. Of these, half
346 occurred in model-predicted eddies along a complex bank that the kayak did not experience at
347 those locations (Figures S5 and S8). This problem is attributable to mesh structure and resolution
348 compared to submeter effects of topographic roughness along the water's edge. Modelers do not
349 carefully design meter-scale mesh structure along banks for long distances, and bank conditions
350 changes with discharge anyway.

351 Another effect observed in eddy validation involved the occurrence of a model eddy
352 slightly shifted or scaled differently than the real eddy. This small spatial difference can cause a
353 large apparent error in magnitude when compared at a fixed point, even if the results are correct
354 for the same relative position in an eddy. Thus, head-to-head velocity direction comparisons are
355 problematic in the vicinity of eddies.

356 4.3. *Comparing Validation Outcomes*

357 The maximum estimated depth-averaged kayak velocity was 2.44 m/s (double that measured
358 while wading). The kayak data r^2 was 0.22 higher than that for fixed-point data, backed by an
359 order of magnitude more points to assess statistical assumptions and confidence. The smallest
360 kayak regression slope was 0.9 (DAVC=0.64) and even that was larger than the highest
361 benchmark established by Lane et al. (1999). Comparison of locations with error > 50% model
362 error is in the supplementary file.

363 Histograms of observed velocities between the two methods show that kayak
364 measurements had a better distribution (Figure 8). Nearly 30% of fixed-point measurements
365 were 0.25–0.5 m/s, while kayak-observed velocities had a peak with only 25% between 0.5–0.75
366 m/s. Approximately 60% of velocities were < 1 and 0.75 m/s for fixed-point and kayak data,
367 respectively. The upper tail is noticeably larger for kayak data. In the future, if mindful effort
368 was made to direct the kayak through diverse and unwadable conditions, then the kayak dataset
369 would far exceed the range and value of a fixed-point dataset.

370 It was demonstrated in Section 4.2.3 that there were discrepancies between modeled and
371 observed kayak velocities into and out of riffles. Velocities were measured on one of these riffles
372 (Figure 6b) during the cross-sectional fixed-point survey (Cross-sections 3 and 4). Side-by-side
373 visual inspection of both sets of data (Figure 9) at cross-section 4 revealed the trend that

374 measurements made on the inside one-half of the channel (river-right) had larger differences
375 (average absolute difference = 0.42 m/s) than the measurements made on the outside one-half of
376 the channel (river-left) (average absolute difference = 0.20 m/s). This observation was consistent
377 for both velocity measurement methods suggesting a 2D model problem, not a kayak method
378 problem.

379 **5. DISCUSSION**

380 Using common fixed-point validation methods, our 2D model performed on par with scientific
381 literature. The same occurred using kayak data. Most people prefer to get an outcome with less
382 effort and lower cost. Having established satisfactory performance from both strategies,
383 discussion focuses on the additional benefits enabled by kayak velocity reconnaissance. The
384 supplementary file includes two additional subsections that detail limitations and future
385 improvements.

386 *5.1. Improved Sampling of Deep And Fast Areas*

387 Compared to the < 1.3 m wadable depths for fixed-point measurement in the ambient currents,
388 the kayak had no depth or velocity constraint in the testbed river. This also enabled a wide range
389 of discharges to be sampled, including a flow above the representative bankfull discharge that
390 covered point and medial bars. This capability is especially important for validating 2D models
391 in floods and steeper mountain rivers (Pasternack & Senter, 2011). Kayaks use no fuel and
392 require less maintenance and set-up time than a motorboat. Some comparison to acoustic
393 Doppler current profiling is discussed in the supplementary materials file as is the discharge-
394 dependence analysis.

395 5.2. *Improved Sampling Of Statistical Structure*

396 Statistical analysis of model performance using kayak data differed from that using fixed-point
397 data, because the former involved an order of magnitude more data spanning a wider range of
398 flows, depths, and velocities. Collection of kayak data is less time consuming, so the same effort
399 by both methods yields a substantial difference in test data. These advantages provide a
400 beneficial capability for characterizing the statistical structures of deviation residuals. Specific
401 numerical outcomes on statistical performance are discussed in the supplementary materials file.

402 This study also showed that the kayak method more evenly represented velocities across
403 a wider range (Figure 8). A 2D model can over-predict low velocities and under-predict high
404 velocities, so a higher range, more evenly distributed dataset aids testing for this. May et al.
405 (2009) found a significant local bias of this nature, but that study was impacted by the
406 occurrence of most observations in the 1.5–3.0 m/s range.

407 Kayak velocity measurements were made along longitudinal transects in this study, but
408 paths were not always centered on the thalweg. As a result, data spanned morphological unit
409 types with hundreds of points each and sampled all positions across the channel. This more
410 appropriately represented the complete range of varying hydraulics typical of low-flow velocity
411 fields in shallow gravel-bed rivers compared to the fixed-point approach that miss important
412 transitions and peak velocities.

413 5.3. *Improved Spatial Testing*

414 Another novel outcome of this study was that modelers can now map and compare observations
415 for long river segments using kayak drifters. When mapped, areas with higher uncertainty that
416 would benefit from multiple sampling runs can be easily identified. In particular, for this study

417 there were consistently large differences between model and observed results at the entrances
418 and exits of riffles using both observational methods (Figure 6). With bathymetric LiDAR and
419 multibeam echosounding, meter to sub-meter resolution 2D models are reaching the natural
420 limitation in accuracy imposed by their inherent structural assumptions regarding 2D flows and
421 sub-grid scale turbulence.

422 5.4. *Putting The 2D In 2D Model Validation*

423 The ability of surface particle tracking to map velocity direction adds a sorely needed dimension
424 to 2D model validation. Test results showed a strong correlation between observed and predicted
425 flow direction. The averaged and measured directions matched up well for the ambient flow, and
426 where vectors converged or diverged. The more flow obstructions a river has, the more eddies it
427 will have and thus the greater need for more comprehensive spatial pattern analysis of velocity
428 vectors.

429 Using a fixed-point method with a multi-axis sensor adds a significantly cumbersome
430 requirement of precisely characterizing sensor direction in the same coordinates as used in a 2D
431 model. The kayak, by contrast, was carried along by the water, which eliminated the uncertainty
432 about direction of flow. GPS data collection with the kayak is natively set to collect data in the
433 same coordinate system as the 2D model. Although some error is inevitable due to kayak
434 momentum and GPS time-recording precision, operator course corrections was anecdotally
435 highly beneficial. Direction validation is now practical and cost effective.

436 6. CONCLUSIONS

437 No hydrodynamic model is free of uncertainty, so modelers are responsible for evaluating and
438 conveying limitations to stakeholders. As a community, 2D hydraulic modelers should tackle

439 spatial patterns of velocity deviation and offer diverse statistical validation metrics. Standardized
440 methods using drifter data can provide those advancements. With regard to the four primary
441 objectives, this study found that:

- 442 • Kayak surface velocity tracking is well suited for 2D model validation (section 4.2).
- 443 • On a comparative basis, kayak data outperformed fixed-point data for all but one metric
444 (sections 4.3 and 5). There is no metric that fixed-point methods can obtain that kayak
445 methods cannot also obtain to test a 2D model.
- 446 • There is no discharge dependence of 2D model performance in most cases, because there
447 is nothing fundamentally different about open-channel hydraulics over a wide range of
448 flows in many settings (section 4.2.2).
- 449 • Kayak surface velocity tracking provides significantly more data for the same cost
450 compared to fixed-point observation, it enables evaluation of velocity spatial patterns,
451 and it addresses velocity magnitude direction (sections 4.2.3 and 4.2.4).

452 Each data collection approach has assumptions, uncertainties, and limitations, though
453 people are well acclimatized to those for fixed-point methods and so tend to downplay them.
454 Although there is uncertainty when choosing a DAVC, the numerous benefits of kayak mapping
455 discovered in this study suggest that practitioners should add this capability to more completely
456 validate model predictions. Nevertheless, there are times when fixed-point methods are more
457 useful than kayak methods, too.

458 7. GEOLOCATION

459 39°13'13" N, 121°20'7" W

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563

Table 1. Velocity validation metrics comparing fixed-point and kayak observations.

Validation metrics.	Velocity magnitude		Velocity direction
	Fixed-point	Kayak	
Trendline slope	0.78	1.00	0.90
Trendline r^2	0.57	0.79	0.80
Regression slope standard error	0.0455	0.0054	0.0059
Regression intercept standard error	0.035	0.006	1.24
NSE	0.52	0.75	0.79
PBIAS	-4.40%	9.87%	0.05%
RSR	0.69	0.50	0.46

Note. NSE = Nash–Sutcliffe efficiency; PBIAS = percent bias; RSR = root mean square error–observations standard deviation ratio.

Table 2. Descriptive statistics for modeled versus kayak-observed highest and lowest velocity magnitude and direction. ABS is the absolute value.

(A) Velocity magnitude (m/s)				
Statistic	V_{Diff}	$ABS(V_{Diff})$	V_{Error}	$ABS(V_{Error})$
Mean	-0.072	0.163	6.1%	18.2%
Standard Error	0.006	0.004	0.6%	0.4%
Median	-0.066	0.109	8.3%	14.1%
Standard Deviation	0.219	0.162	22.8%	15.0%
Range	2.011	1.238	167.0%	94.5%
Minimum	-1.238	0.000	-72.5%	0.0%
Maximum	0.772	1.238	94.5%	94.5%
(B) Velocity direction (deg)				
Statistic	Dir_{Diff}	$ABS(Dir_{Diff})$	Dir_{Error}	$ABS(Dir_{Error})$
Mean	-0.11	5.49	-0.06%	2.66%
Standard Error	0.13	0.10	0.06%	0.05%
Median	-0.01	3.75	0.00%	1.81%
Standard Deviation	9.65	7.94	4.65%	3.82%
Range	406.06	228.48	196.68%	102.04%
Minimum	-228.48	0.00	-102.04%	0.00%
Maximum	177.58	228.48	94.64%	102.04%

564 **Figure Captions**

565 Figure 1. Photos illustrating the diversity of hydraulic conditions on the low Yuba River.

566 Figure 2. Lower Yuba River corridor below the Highway 20 Bridge, its local and regional
567 context, 2D model reach domains, and geomorphic reaches.

568 Figure 3. Model predicted depth-averaged velocities versus observations from (a) fixed-point
569 measurement and (b) kayak measured velocities using $DAVC=0.71$. It is not possible to convey
570 the small residuals of the majority of kayak points, so refer to the standard error of the slope
571 metric in the text.

572 Figure 4. Absolute velocity error versus observed kayak velocities ($DAVC = 0.71$).

573 Figure 5. Predicted model velocities versus kayak-based velocity results ($DAVC = 0.71$) for the
574 highest and lowest flows in the study (141.9 and $17.6 \text{ m}^3/\text{s}$, respectively).

575 Figure 6. Differences between modeled and observed kayak velocities near riffles.

576 Figure 7. Observed versus model-predicted direction of flow. The largest errors are in model-
577 predicted eddies that were either not present in reality or were not located where the kayak
578 drifted. Even a small difference in model eddy size and shape can cause large directional
579 deviations.

580 Figure 8. Percent distribution of 2D model velocity errors binned by observed velocity,
581 comparing results between fixed-point and kayak datasets.

582 Figure 9. Differences of kayak and cross-section fixed-point velocities with modeled velocities
583 showing consistency in trends across the channel.

584



Figure 1

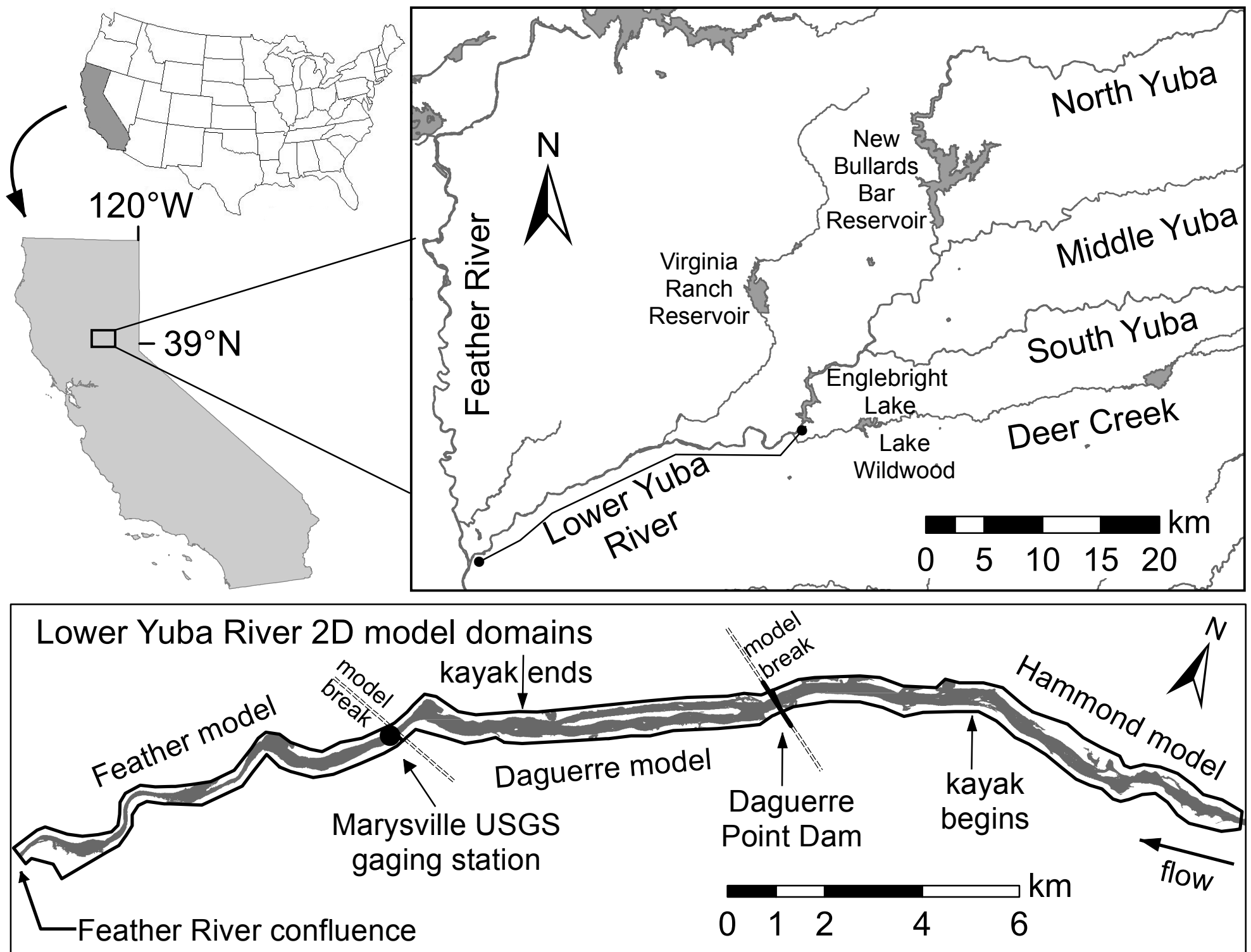


Figure 2

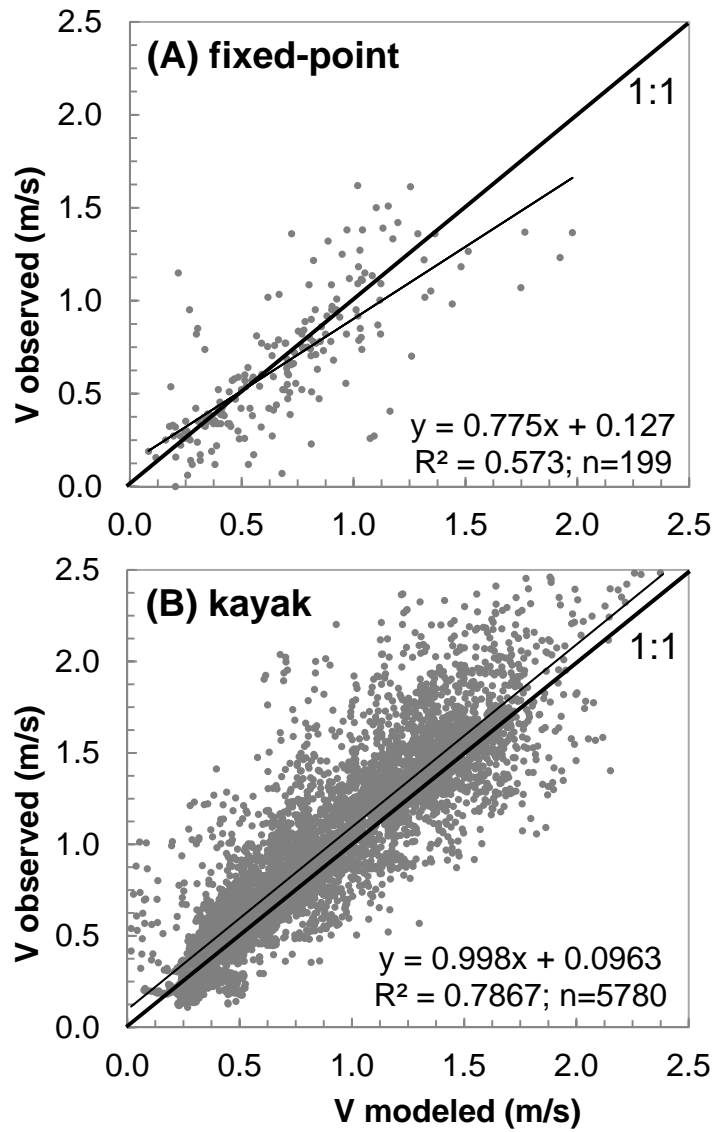
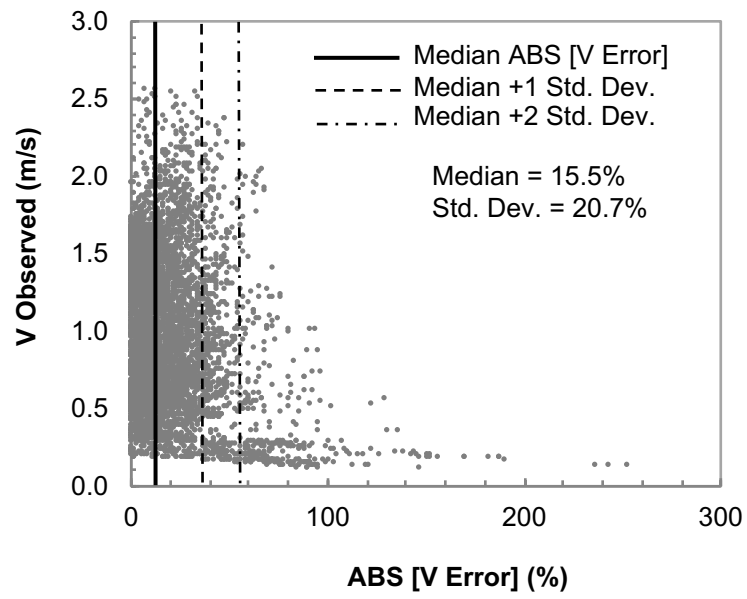


Figure 3



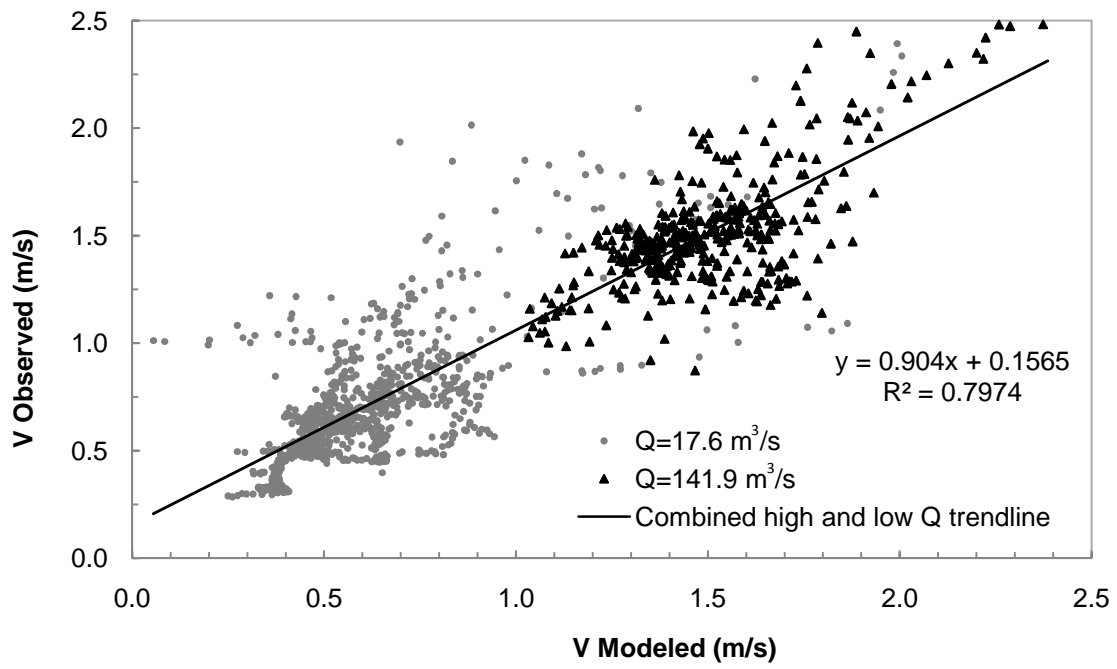
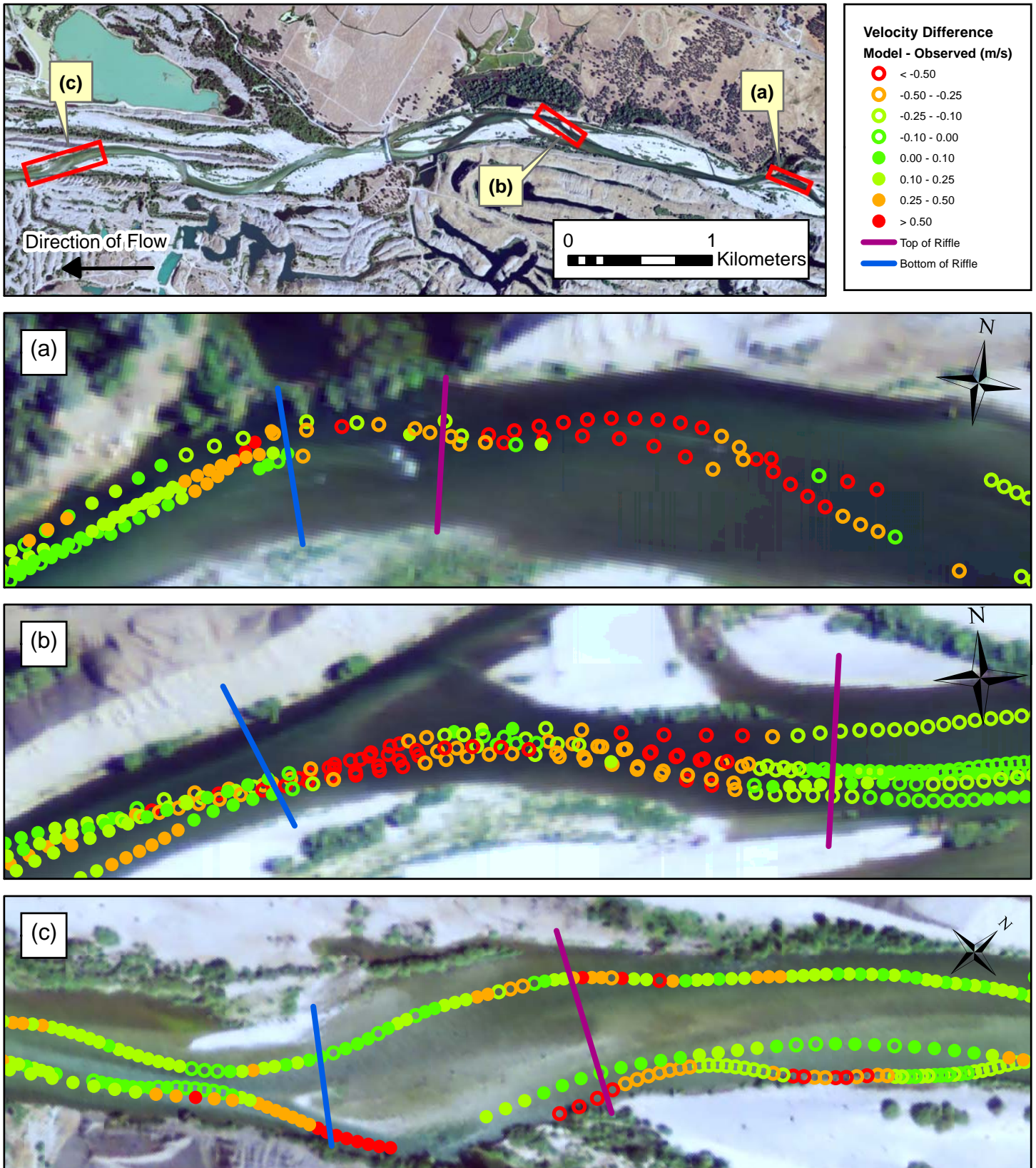


Figure 5



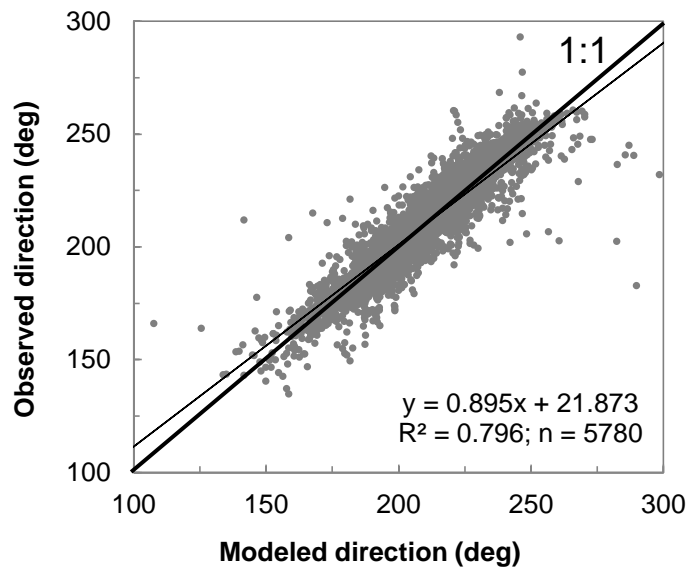


Figure 7

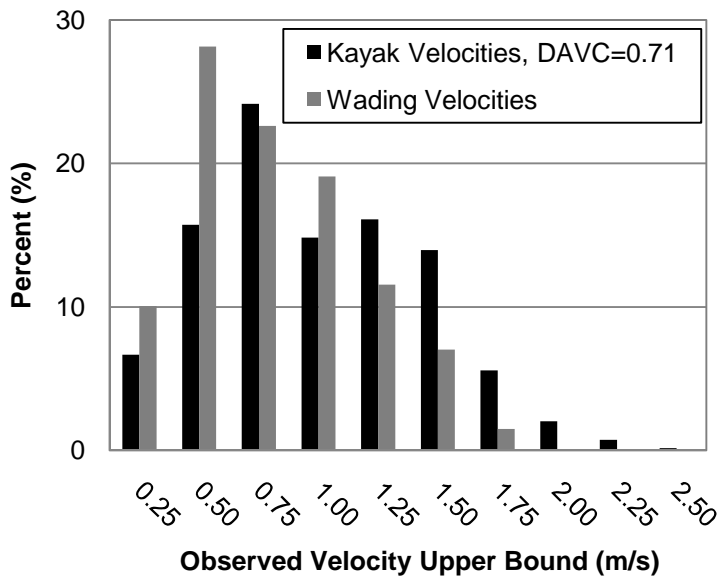


Figure 8

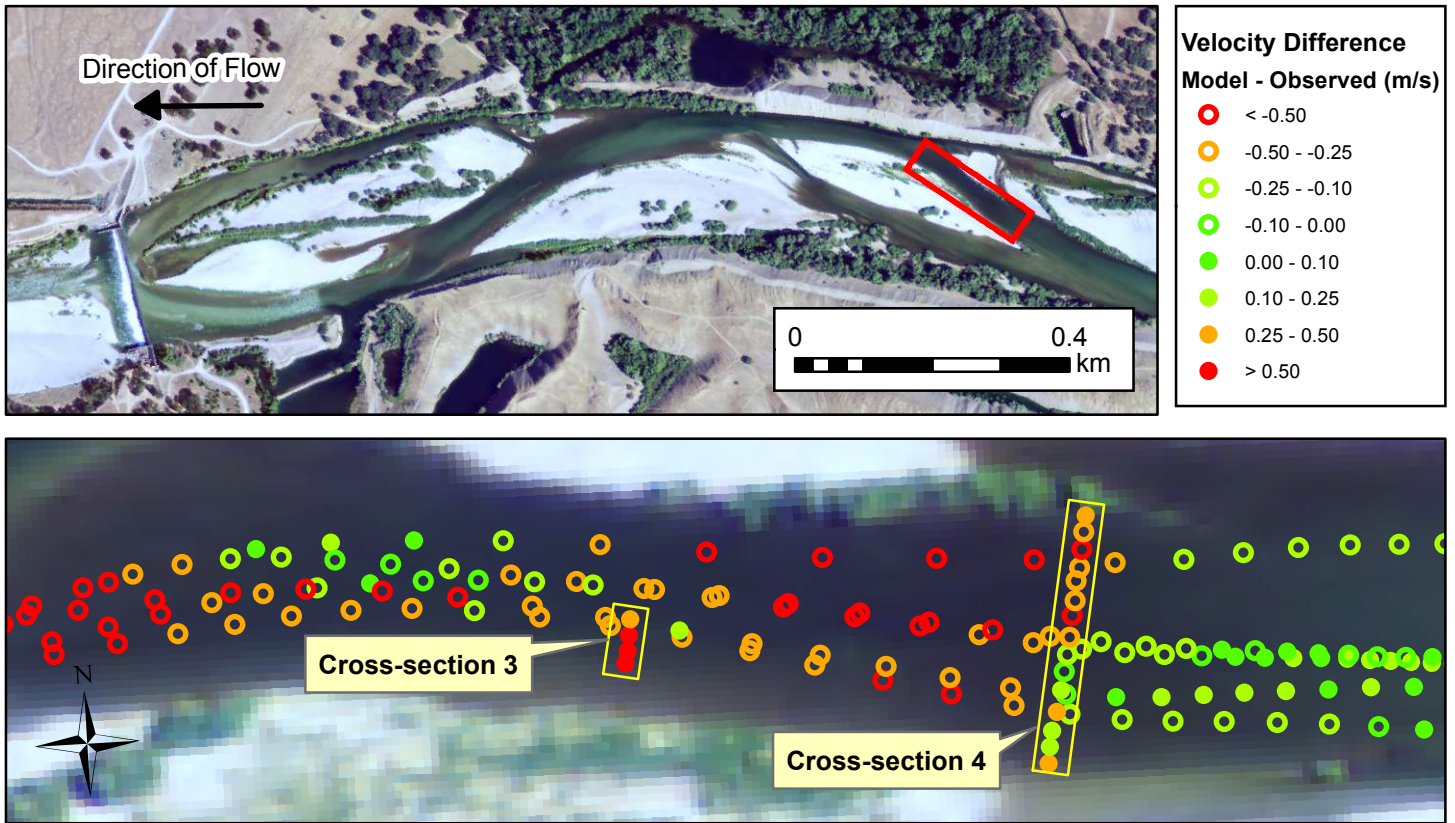


Figure 9

Kayak drifter surface velocity observation for 2D hydraulic model validation

SUPPLEMENTARY MATERIALS

This file is organized with sections that parallel those in the article for convenience in locating text to see more details on any topic of interest.

1 Introduction Supplements

1.1 Need For More 2D Model Validation

Scientific progress benefiting from 2D modeling includes studies of river hydraulics (Waddle, 2010; Strom et al., 2016), environmental flows (Reinfelds et al., 2010), hydrogeomorphic processes (Pasternack et al., 2008; Sawyer et al., 2010), floodplain inundation (Tayefi et al., 2007), urban flooding (Yu & Lane, 2006; Mason et al., 2007), aquatic meso- and micro-habitat quality (Clark et al., 2008; Kammel et al., 2016), and river design assessment (Elkins et al., 2007; Lee et al., 2010; Brown & Pasternack, 2016). In general, 2D modeling studies are using very little data for validating velocity performance, and this means that models just aim for the simplest performance criteria with little analysis of where and when such models work well or not. Studies that exemplify what is commonly done with 2D model velocity validation include Ghanem et al., 1996; Lane et al., 1999; Stewart, 2000; Ballard & Gard, 2003; Wheaton et al., 2004; Pasternack et al., 2006; Elkins et al., 2007; Brown & Pasternack, 2008. Velocity is commonly observed at just 2-10 cross-sections, even when validating 1-10 km long models

21 (see citations in previous paragraph for examples of this). Data collection usually involves
22 standing in the flow with a 1D current meter or lowering a current meter on a cable from a boat
23 to obtain time-averaged velocity measurements over 30-60 s at each of 1-3 locations in a
24 vertical profile. This limits the locations and flows at which data are collected. Acoustic
25 Doppler current profilers (ADCPs) are infrequently used for velocity measurements by moving
26 across a measured section and creating a series of 5-s averaged vertical velocity profiles (e.g.
27 Tiffan et al., 2002; May et al., 2009). From the literature, there may be 10-30 observations per
28 cross-section, yielding ~ 50-300 total observation points to test a model, and that still leaves
29 velocity direction untested.

30 Although 2D model validation using fixed-point velocity is well documented, there are
31 important operational limitations. First, how many observations and in what pattern are needed
32 to produce a satisfactory accounting of model performance? Many studies use fewer than 10
33 cross-sections and choose transects with relatively simple velocity vector patterns, as these are
34 often locations required for discharge measurements. For example, Tiffan et al. (2002) used
35 just two ADCP cross-sections (one “simple” and one “more complex”) at two discharges to
36 validate a 33-km long 2D model. A few hundred points sounds like a lot, but given the breadth
37 of uncertainty of real velocity conditions, not only are individual measurements error-prone,
38 but the statistical sampling regime is inadequate for models spanning tens to hundreds of
39 kilometres.

40 Large-scale 2D flow patterns are important to geomorphic processes and ecological
41 conditions, and there is a pressing need to have the data to ensure that 2D models represent
42 those correctly. The velocity vector field is the hallmark of 2D modeling, yet hardly anyone is
43 validating such vectors in real-world applications. Velocity patterns can be significantly varied

44 in a model by selection of a turbulence closure scheme and the associated parameter values.
45 Overall, improvement of 2D model velocity validation is a key need to better characterize
46 uncertainty in 2D models and improve the perception of 2D models by the public, which is
47 often sceptical of numerical models (Ludwig, 2001; Van Asselt and Rotmans, 2002).

48 Second, collection of point-velocity measurements and use of an ADCP are too time-
49 consuming and still have significant errors and uncertainties. Using a fixed-point velocity
50 sensor, depth-averaged velocity data requires measurements made during 0.5–3 min per
51 vertical, plus the time to set up and relocate. This creates an infeasible timeframe to collect a
52 dense mesh of velocity points and span a large area at a reasonable cost. For ADCP, an
53 individual vertical velocity profile only takes a minimum of 5 s (though > 30 s should be used
54 to be consistent with standard fixed-point protocols), but transects should be made at a slower
55 speed than the ambient velocity (20% of it), and transects need to be repeated 4–6 times to get
56 a reasonable time-averaged estimate of the flow field. Proper recording of the orientation of the
57 3D vector in the flow field is challenging. Operation of boats for ADCP aimed at velocity
58 mapping is more difficult than for discharge gaging, because it involves navigating through
59 diverse conditions, including locations where ADCP performs poorly, such as along the bank,
60 in shallows, and where there are air bubbles. The diversity of hydraulics also generates more
61 challenges for and uncertainties in ADCP velocity accuracy. ADCP has much promise, if it is
62 further developed for velocity mapping instead of discharge gaging, including thorough testing
63 for this purpose. Mueller et al. (2007) present important errors with ADCP velocity
64 measurements, while Lee et al. (2011) make a compelling case for the need of a low-cost
65 velocity vector mapping solution instead of ADCP. Ultimately, ADCP remains expensive,

66 complex, and inaccessible to many potential 2D model users, especially biologists who are
67 increasingly using 2D models but don't want to become professional hydrographers as well.

68 Third, wading and motorboat approaches to data collection are limited by flow
69 conditions precluding 2D model validation in the most important places to understand
70 geomorphic processes. Observations by wading requires a low combination of depth and
71 velocity as well as a lack of hazards around the wader (Milanesi et al., 2015). Motorboats have
72 a much wider range of capabilities, but they have trouble in shallows, near flow obstacles, over
73 rapids, and in some flood conditions. These challenges inhibit equal-effort sampling among
74 diverse ecohydraulic conditions, which ought to be required for 2D model validation.

75 Finally, the scale of velocity observation and prediction are often incommensurate.
76 Velocity sensors sample 0.5–100 mm, while 2D model grid cells are 500–10,000 mm, creating
77 a mismatch for comparison, especially in light of turbulence, whose intensity also varies
78 spatially and over these scales. ADCP units have a trade-off with range versus resolution (e.g.
79 Sontek/YSI Inc, 2007), making them ineffective in rivers whose spatially variable depths and
80 velocities transcend the selected range and resolution parameters. Historically the problem was
81 particularly bad for shallow rivers, given that an ADCP cannot measure velocity close to the
82 water's surface due to its blanking distance. However, range and resolution options are
83 improving. They also require precise orientation in the 2D model's coordinate system, which is
84 problematic with bottom tracking and differential GPS. Moreover, using a 3D velocity profiler
85 to validate a 2D model can introduce errors due to differing averaging methods of varying
86 spatial scales (Pasternack et al., 2006).

87 *1.2 Large-Scale Particle Image Velocimetry*

88 Some additional LSPIV studies include Creutin et al. (2003), Hauet et al. (2009), Fujita
89 & Kunita (2011), Lewis & Rhodes (2015), Detert & Weitbrecht (2015), and Cre lle et al.
90 (2016). For brevity, these citations had to be cut out of the article. More articles are likely
91 available, especially including conference proceedings, as this a rapidly emerging area of
92 inquiry. LSPIV has significant challenges for use in widespread velocity vector validation of
93 2D models. Platforms are commonly operated in clear-sky weather over smaller channels
94 accessible to camera mounting systems, whereas 2D model validation is needed for a wide
95 range of river sizes with limited accessibility during a wide range of flows and precipitation
96 intensity. Fixed-view domains at the scale of <100 m long by 70 m wide used in LSPIV have
97 limited applicability for 2D models that span 10-100 km long by 10-500 m wide channels,
98 which is a primary reason why oceanographers use drifters. The legal and regulatory context
99 for aerial platforms is presently uncertain. Regardless of acquisition platform, LSPIV methods
100 require substantial data processing with many additive potential sources of uncertainty at this
101 time. Data acquisition and processing to obtain surface velocity vectors over tens to hundreds
102 of kilometres is not presently available.

103 *1.3 Kayak Surface Particle Tracking*

104 There are only two journal articles (Stockdale et al., 2007; Han et al., 2016) and a few
105 conference proceedings (Swick and MacMahon, 2009; Emory et al., 2010; Lee et al., 2011)
106 testing drifters in nontidal rivers, and they all used differential GPS. None of these compared
107 drifter results against fixed-point observations, though some report past studies of error
108 estimates. The purpose of this supplemental section is to provide background information on
109 those past studies, help readers understand the accuracy of kayak surface particle tracking

110 method (using RTK GPS) in more detail, and explain why there is value in selecting RTK GPS
111 over regular or differential GPS, when possible.

112 Several of the past efforts have primarily served to report technological developments
113 and secondarily to share descriptive data from test deployments. Stockdale et al. (2010)
114 developed flat, packaged river surface drifters with on-board differential GPS. They produced
115 a velocity vector map of a 400-m long test site. Swick and MacMahan (2009) developed
116 cylindrical differential GPS drifters with ballast to keep them upright. They deployed 6-16
117 drifters in 3 settings to produce both Lagrangian and Eulerian (averaged) statistical analyses.
118 Emery et al. (2010) developed commercial spherical river drifters. They deployed five of them
119 at one test site and one at another test site. Lee et al. (2011) developed another differential GPS
120 drifter technology similar to that of Stockdale et al. (2010), but then in their research they
121 added a thorough data-processing framework. They used drifters to collect 45 trajectories with
122 ~ 7000 observations to map velocity vectors in a 100 m long by 10-15 m wide channel. Finally,
123 Han et al. (2016) developed a spherical drifter similar to that of Emery et al. (2010). They
124 deployed 50 drifters to analyze riverine surface mixing characteristics.

125 In general, with a good satellite configuration, GPS has ~ 3-m horizontal accuracy,
126 while differential GPS has ~ 1-m horizontal accuracy. For an ambient current of 1 m/s moving
127 in a straight line, two positions that are off by 1 or 3 m extra away from each other (i.e., the
128 worst-case scenario) yield a velocity error of 300% or 700%, respectively. In contrast, an RTK
129 GPS with 0.02-m or 0.05-m accuracy has a worse-case velocity error of just 4% or 10%,
130 respectively. That is an enormous difference, especially for 2D model validation. Our
131 viewpoint is that most stakeholders and independent reviewers expect observational data to be
132 of a high-quality to serve for model validation purposes. Thus, the extra cost of RTK GPS is

133 necessary. Other potential uses of river drifters may not require this. However, the cost of RTK
134 GPS has dropped so much over the last decade that it is getting difficult to justify avoiding the
135 expenditure. In regions where RTK GPS is still excessively expensive or outright unavailable,
136 more work would be required to ascertain if DGPS is satisfactory for 2D model validation
137 purposes.

138 Stockdale et al. (2008) used a Royaltek™ BlueGPS (RBT3000) that samples position at
139 1 Hz, with a reacquisition time of 0.1 s for each reading on average. This unit a built-in
140 differential capability using the United States' Federal Aviation Administration Wide Area
141 Augmentation System (WAAS) as well as Europe's European Geostationary Navigation
142 Overlay Service (EGNOS). These systems have similar specifications with their corrections.
143 Differential corrections are provided every ~ 0.2 Hz. WAAS provides a conservative position
144 accuracy of 3 m or better (for both lateral and vertical measurements) at least 95% of the time
145 (Zhang et al., 2014). It is reported with different actual performances in horizontal accuracy,
146 typically in the 1-3 m range (e.g., Ariens Specialty Brands LLC, 2014).

147 Lee et al. (2011) used a MediaTek GPS module FPGMMOPA1. The technical
148 specifications for this model number are no longer available on the MediaTek website, but the
149 authors report a positional accuracy of 3 m, which is consistent with native GPS performance
150 absent any differential correction. Lee et al. (2011) state a measured average velocity "error" of
151 0.175 m/s comparing drifters versus fixed-point observations.

152 Both Stockdale et al. (2008) and Lee et al. (2011) both applied additional statistical
153 methods to help diminish the effects of individual point velocity estimation errors on bulk
154 results for larger subsets of data. Stockdale et al. (2008) simply divided the river into cells and
155 then computed the average velocity in each section. Lee et al. (2011) also divided the river into

156 cells, but they computed a diversity of statistics to characterize motion of the bulk flow field.
157 Such methods allow for more relaxation of point-scale expectations as long as the bulk field is
158 acceptable to within specified tolerances for the derived statistics. It remains to be seen what
159 performance metrics will be acceptable to the scientific and practitioner 2D modeling
160 community for such approaches, but this is a good start. Overall, Stockdale et al. (2008) and
161 Lee et al. (2011) provide enough discussion of velocity accuracy to insure that the method is
162 worthwhile to develop further, and there is now ample justification for new studies to carefully
163 test drifters more comprehensively.

164 *1.4 Study Objectives*

165 None.

166 **2 Study Site Supplements**

167 None.

168 **3 Methods Supplements**

169 Field data collection efforts were explicitly intended to characterize geomorphic, hydrologic
170 and hydraulic attributes of the LYR at roughly meter-scale resolution in support of a near-
171 census approach to river assessment, including 2D hydrodynamic modeling. The types of data
172 collected included topography and bathymetry (Pasternack, 2009; White et al., 2010; Carley et
173 al., 2012) as well as hydraulic data: water surface elevation, depth, velocity magnitude and
174 velocity direction (Barker, 2011; Pasternack et al., 2014). Details about spatial coverage,
175 resolution and accuracy for the digital elevation model (DEM) and 2D hydrodynamic modeling
176 used in this study are provided below.

177 *3.1 2D hydrodynamic modeling details*

178 This study only used the portion of the LYR topographic map from the highway 20 Bridge
179 down to the confluence with the Feather River. On September 21, 2008 Aero-Metric, Inc.
180 (Seattle, WA) acquired Light Detection and Ranging (LiDAR) data of the river corridor during
181 a constant low flow typical of the period when hydro facility maintenance takes place (24.437
182 m³/s (863 cfs) between Englebright Dam and Daguerre Point Dam; 17.613 m³/s (622 cfs)
183 below Daguerre Point Dam where irrigation diversions occur). The target point spacing was
184 0.74 m. Compared against 8769 ground-based RTK GPS observations of elevation along flat
185 surfaces, 84.7% of LiDAR points were within 0.06 m, another 14.0% were within 0.12 m, and
186 almost all of the remained of the data were within 0.18 m. All in-water LIDAR points were
187 removed from the dataset using a shoreline boundary polygon.

188 Boat-based bathymetric surveys were performed during low flows in August and
189 September of 2008 as well as during higher flows in March and May 2009 by Environmental
190 Data Solutions. An array of four echosounders were stationed across the bow with ~1.8 m
191 spacing and used to obtain longitudinal swaths of bathymetric points. It was cost-prohibitive to
192 wade all wetted areas inaccessible to the boat, but a set of key “data gap” locations was
193 identified based on iterative map production checks and filled in by ground-based RTK GPS
194 surveying in November 2009.

195 A comprehensive set of uncertainty analyses were performed to ensure that the datasets
196 were accurate and intercomparable (Barker, 2010). Ground points on the uneven natural
197 surface were compared between ground-based and boat-based surveys, ground-based and
198 LiDAR surveys, and boat-based and LiDAR surveys. Surveys were also inter-compared at
199 carefully surveyed water surface elevation shots along the water’s edge, where there was less

200 surface variability. Vertical datums were checked between survey methods to ensure
 201 compatibility.

202 After the final gap-fill survey, all the points were brought into ArcGIS® 9.3.1 software,
 203 visualized as a map, and edited to remove any obvious errors. In narrow backwater channels
 204 and other gap-fill areas that contained interpolation errors, breaklines were created to better
 205 represent landform features. Additionally, some large areas that contained very few points
 206 were augmented so that channel characteristics were maintained. Finally, using the spatial join
 207 function in ArcGIS, consistency between data sets was assessed to ensure there were not any
 208 major discrepancies between different mapping methods.

209 Basic information describing topographic and bathymetric field data in the Yuba River
 210 in the areas investigated in this study are reported in the box below.

211

Attribute	Description
Aerial extent	From Highway 20 Bridge to confluence with Feather River
Years of data collection	Most bathymetry was mapped in late August to early September 2008, with some high-flow data collection in March and May 2009 as well as small additional near-bank and near-DPD gaps mapped in November 2009. Ground-based topographic surveys were done in November 2008 and November 2009. LiDAR of the terrestrial river corridor was flown on September 21, 2008.
Bathymetric Resolution	Within the 24.92 m ³ /s inundation area, points were collected along longitudinal lines, some cross-sections and some localized grids. The average grid point spacing is one point every 1.3 m. (59.8 pts/100 m ²).
Topographic Resolution	Outside the 24.92 m ³ /s inundation area, points were mostly collected with lidar, yielding an average grid point spacing of one point every 0.43 m. (554 pts/100 m ²).
Bathymetric Accuracy	Comparison of overlapping echosounder and total station survey points at one site yielded observed differences of 50% within 0.15 m, 75% within 0.18 m and 94% within 0.3 m. Comparison of boat-based water edge shots versus RTK GPS surveyed water's edge shots yielded observed differences of 75% within 0.03 m, 91% within 0.061 m and

	99% within 0.15 m.
Topographic Accuracy	Compared against 8,769 ground-based RTK GPS observations of elevation along flat surfaces, 54% of LIDAR points were within 0.03 m, 86% were within 0.061 m and virtually all of the data were within 0.15 m. Regular total station control point checks yielded accuracies of 0.0091-0.018 m. RTK GPS observations had vertical precisions of 0.018 m. Comparison of lidar water edge points versus the same for RTK GPS yielded observed differences of 30% within 0.03 m, 57% within 0.061 m and 92% within 0.15 m.

212

213 In this study, the Sedimentation and River Hydraulics – Two-Dimensional Version 2.1 (SRH-
214 2D v2.1) model was used to simulate river hydraulics as well as predict flow velocities and
215 directions (Lai, 2008). SRH-2D v2.1 focuses specifically on 2D modeling of river systems by
216 using the depth averaged St. Venant equations:

$$217 \quad \frac{\partial h}{\partial t} + \frac{\partial hU}{\partial x} + \frac{\partial hV}{\partial y} = e \quad (1)$$

$$218 \quad \frac{\partial hU}{\partial t} + \frac{\partial hUU}{\partial x} + \frac{\partial hVU}{\partial y} = \frac{\partial hT_{xx}}{\partial x} + \frac{\partial hT_{xy}}{\partial y} - gh \frac{\partial z}{\partial x} - \frac{\tau_{bx}}{\rho} + D_{xx} + D_{xy} \quad (2)$$

$$219 \quad \frac{\partial hV}{\partial t} + \frac{\partial hUV}{\partial x} + \frac{\partial hVV}{\partial y} = \frac{\partial hT_{xy}}{\partial x} + \frac{\partial hT_{yy}}{\partial y} - gh \frac{\partial z}{\partial y} - \frac{\tau_{by}}{\rho} + D_{yx} + D_{yy} \quad (3)$$

220 where t is time, x and y are horizontal Cartesian coordinates, h is water depth, U and V are
221 depth-averaged velocity components in x and y directions, respectively, e is excess rainfall rate,
222 g is gravitational acceleration, T_{xx} , T_{xy} , and T_{yy} are depth-averaged turbulent stresses, D_{xx} , D_{xy} ,
223 D_{yx} , and D_{yy} are dispersion terms due to depth averaging, $z = z_b + h$ is water surface elevation,
224 z_b is bed elevation, ρ is water density, and τ_{bx} , τ_{by} are the bed shear stresses (friction). Dispersion
225 terms represent the conversion of kinetic energy into internal energy by viscous shear stress
226 since small scale turbulence is not fully represented in this model. Bed friction is calculated
227 using the Manning's roughness equation as follows:

228
$$\begin{pmatrix} \tau_{bx} \\ \tau_{by} \end{pmatrix} = \rho C_f \left(\frac{U}{V} \right) \sqrt{U^2 + V^2}; \quad C_f = \frac{gn^2}{h^3} \quad (4)$$

229 where n is the Manning's roughness coefficient.

230 In order to solve these St. Venant equations a finite-volume numerical method was used
231 which requires the use of a computational mesh. The Surface-water Modeling System® (SMS)
232 version 10.1 graphical user interface (Aquaveo, LLC, Provo, UT) was used to produce the
233 meshes. A hybrid structured-unstructured, arbitrarily-shaped mesh was produced in SMS using
234 both quadrilateral and triangular elements. Typical nodal spacing for the mesh was ~1.5 m.
235 Although this mesh size is smaller than the resolution of bathymetric data collected by the
236 boat, several studies have shown that reasonable results can still be predicted in areas with
237 sparse topographic coverage (Anderson and Bates, 1994; French and Clifford, 2000; Marks
238 and Bates, 2000). Based on past experience with mesh-resolution testing to evaluate issues
239 such as numerical diffusion and numerical stability, this mesh resolution is more than high
240 enough to avoid those problems for the finite-volume method. Topographic (x,y,z) points and
241 breaklines were then imported from ArcGIS® software into SMS software where they were
242 then used to interpolate elevations to the mesh.

243 Because of the large size of the study area, the desire for computational efficiency,
244 meter-scale model resolution commensurate with the best of the available topographic data,
245 and the order-of-magnitude range of flows being assessed, the river between the Highway 20
246 Bridge and the Feather River confluence was split into three model reaches: (1) Hammon
247 Reach [HR – HWY 20 Bridge to DPD], (2) Daguerre Reach [DGR – DPD to Marysville
248 Gauging Station], and (3) Feather Reach [FR – Marysville Gauging Station to Feather River
249 Confluence]. These do not correspond with the geomorphic reach delineation for the LYR, but
250 are purely for computational balance and efficiency. Higher and lower flow meshes

251 (corresponding with flow ranges of ~ 42 - $141 \text{ m}^3/\text{s}$ and $<42 \text{ m}^3/\text{s}$, respectively) were then
252 created for each model reach to limit the amount of unnecessary dry areas being modeled in the
253 lower-flow simulations. Models were run for 28 steady flows ranging from 8.50 to $3,126 \text{ m}^3/\text{s}$
254 (0.06 to 22 times bankfull discharge).

255 Channel roughness was primarily addressed during the mapping effort by creating a
256 highly detailed DEM, but unresolved roughness issues were addressed by using a global
257 Manning's n coefficient. The use of a constant roughness-coefficient value for unvegetated
258 substrate was justified on the LYR, because the New Years 2006 flood with a peak flow of \sim
259 $3087 \text{ m}^3/\text{s}$ ($\sim 19.5 \cdot Q_{\text{bankfull}}$) was observed to erase much of the spatial variability in bed surface
260 grain size distribution. This occurs because the underlying valley fill is composed of relatively
261 homogeneous hydraulic mining sediment deposited prior to the construction of Englebright
262 Dam (Pasternack, 2008). Substrate observation after the even larger 1997 flood found that it
263 took 5-7 years for an armor layer to re-establish itself in riffles and chutes. Flows $< 141 \text{ m}^3/\text{s}$
264 are mostly (but not always) constrained inside the bankfull channel dimensions devoid of
265 vegetation, rendering it unnecessary to account for vegetation in the roughness coefficient in
266 this study. It is possible that adding additional roughness for near-bank vegetation and steep
267 banks would improve hydraulic prediction, but without a systematic, objective approach to
268 distributing near-bank roughness at the time this study was conducted, it is beyond the scope of
269 this investigation. Observed WSE values obtained during the gap-fill survey were compared
270 against model-predicted WSE values for different simulations using $n=0.035$, 0.04 , and 0.045
271 for all model reaches. Statistical error and histogram analyses comparing the different values
272 found that 0.04 yielded the most accurate predictions, so that value was used in the model
273 validation investigations reported in this study.

274 Aside from channel roughness, turbulence closure and the model's boundary conditions
275 must also be assigned. Turbulence closure was achieved using the parabolic/zero equation
276 model (Lai, 2008), with eddy viscosity varying as a function of depth and shear velocity,
277 modified by an eddy viscosity coefficient of 0.6 based on the long-standing representative
278 value taken from historical dye studies (Fischer et al., 1979). The eddy viscosity term is a
279 practical strategy for calculation that ignores the small-scale vortices in the motion and
280 calculates a large-scale motion with eddy viscosity which characterizes the transport and
281 dissipation of energy in the smaller-scale flow. This approach and coefficient was previously
282 validated for use in a pool-riffle-run sequence on this same river (Moir and Pasternack, 2008;
283 Sawyer et al., 2010). Eddy viscosity should not be confused with eddy diffusivity, which is
284 used with any dependent variable (a scalar or a component of a vector) in the discretization of
285 the governing equations to represent the process by which substances are mixed.

286 The boundary conditions required for SRH-2D are input flows and corresponding exit
287 WSE. Input flows were obtained from the Yuba River at Smartville (#11418000), Deer Creek
288 at Mooney Flat Road (#11418500), and Yuba River at Marysville (#11421000) United States
289 Geological Survey (USGS) gaging stations. Corresponding downstream WSE values were
290 collected in two ways. Since the DGR downstream boundary was located at the Marysville
291 gauging station, WSE values were readily available from the professional rating relation for
292 that gage. For the other model reaches, downstream WSE values were observed using a
293 suitably mounted Level TROLL® 500 water level sensor (In-Situ Inc., Fort Collins, Colorado).
294 The lag time between gage-recorded discharges and local WSE was optimized for by
295 statistically matching fluctuations in corresponding records to yield the highest correlation
296 between lagged records.

297 Model simulations were comprehensively validated for flows ranging over an order of
 298 magnitude of discharge (0.1 to 1.0 times bankfull) using three approaches: (i) traditional cross-
 299 sectional validation methods, (ii) comparison of LiDAR-derived water surface returns against
 300 modeled water surface elevations and (iii) Lagrangian particle tracking with RTK GPS to
 301 assess the velocity vectors. Model set-up and performance details are reported in the box
 302 below:
 303

Attribute	Description
Model domains	For this study, there were 3 modeling reaches to make the computational process more efficient. They are given the abbreviations, HR, DGR and FR below.
Computation mesh type	All model domains use an unstructured mesh with triangular and polygonal elements.
Computational Mesh Resolution	<p>HR: For flows 0-36.81 m³/s, 0.91 m internodal spacing. For flows 36.81-212.4 m³/s, 1.5 m internodal spacing. For flows >283.2 m³/s, 3 m internodal spacing.</p> <p>DGR: For flows 0-36.81 m³/s, 1.5 m internodal spacing. For flows 36.81-212.4 m³/s, 1.5 m internodal spacing. For flows >283.2 m³/s, 3 m internodal spacing.</p> <p>FR: For flows 0-36.81 m³/s, 1.5 m internodal spacing. For flows 36.81-212.4 m³/s, 1.5 m internodal spacing. For flows >283.2 m, 3 m internodal spacing.</p>
Discharge Range of Model	8.495 to 3126 m ³ /s.
Downstream WSE data/model source	<p>HR: Continuous direct observation of WSE at flows <~623.0 m³/s. For higher flows the downstream WSE was taken as the upstream WSE from the HR model at that flow.</p> <p>DGR: Reach ends exactly at Marysville gaging station, so the WSE data is of the highest quality and abundance. Continuous WSE data for all flows ~14.16 - 3126 m³/s.</p> <p>FR: Continuous direct observation of WSE at flows <~623.0 m³/s. For higher flows the downstream WSE was set to yield an upstream WSE equal to that at the Marysville gage.</p>
River roughness	Because the scientific literature reports no consistent variation of Manning's n as a function of stage-dependent relative roughness or the whole wetted area of a

specification	river (i.e., roughness/depth), a constant value was used for all unvegetated sediment as follows: 0.04 for the HR, DGR, and FR models (based on validation testing of 0.03, 0.035, 0.04, 0.045 and 0.05 as possible options). This study did not use spatially distributed vegetated roughness, because the majority of flows were in-channel and it was not warranted.
Eddy viscosity specification	Parabolic turbulence closure with an eddy velocity that scales with depth, shear velocity and a coefficient (e_0) that can be selected between ~ 0.05 to 0.8 based on expert knowledge and local data indicators. $Q < 283.2 \text{ m}^3/\text{s}$: $e_0 = 0.6$ $Q \geq 283.2 \text{ m}^3/\text{s}$: $e_0 = 0.1$
Hydraulic Validation Range	Point observations of WSE were primarily collected at $24.92 \text{ m}^3/\text{s}$, with some observations during higher flows, but not systematically analyzed. Velocity observations were collected for flows ranging from 15.01 - $141.9 \text{ m}^3/\text{s}$. Cross-sectional validation data collected at $22.65 \text{ m}^3/\text{s}$ above DPD and $15.29 \text{ m}^3/\text{s}$ below DPD.
Model mass conservation (Calculated vs Given Q)	0.001 to 1.98 %
WSE prediction accuracy	At $24.92 \text{ m}^3/\text{s}$ there are 197 observations. Mean raw deviation is -0.0018 m . 27% of deviations within 0.03 m , 49% of deviations within 0.076 m , 70% within 1.5 m , 94% within 0.3 m . These results are better than the inherent uncertainty in LiDAR obtained topographic and water surface elevations.
Depth prediction accuracy	From cross-sectional surveys, predicted vs observed depths yielded a correlation (r) of 0.81.
Velocity magnitude prediction accuracy	5780 observations yielding a scatter plot correlation (r) of 0.887. Median error of 16%. Percent error metrics include all velocities (including $V < 0.3 \text{ m/s}$, which tends to have high error percentages) yielding a rigorous standard of reporting.
Velocity direction prediction accuracy	5780 observations yielding a scatter plot correlation (r) of 0.892. Median error of 4%. Mean error of 6%. 61% of deviations within 5 degrees and 86% of deviations within 10 degrees.

304

305

Using the workflow of Pasternack (2011), SRH-2D model outputs were processed to

306

produce rasters of depth and velocity within the wetted area for each discharge. The first task

307 involved creating the wetted area polygon for each discharge. To do this, point files of depth
308 results were first converted to triangular irregular networks (TIN) and then to a series of
309 0.9144-m hydraulic raster files. Depth cells greater than zero were used to create a wetted area
310 boundary applied to all subsequent hydraulic rasters. Next, the SRH-2D hydraulic outputs for
311 depth and depth-averaged velocity were converted from point to TIN to raster files within
312 ArcGIS 10.1 staying within the wetted area for each discharge. The complete dataset was a
313 series of 0.9144-m resolution hydraulics rasters derived from SRH-2D hydrodynamic flow
314 simulations at the following discharges: 8.5, 9.9, 11.3, 12.7, 15.0, 17.0, 17.6, 19.8, 22.7, 24.9,
315 26.3, 28.3, 36.8, 42.5, 48.1, 56.6, 70.8, 85.0, 113.3, 141.6, 212.4, 283.2, 424.8, 597.5, 849.5,
316 1195.0, 2389.9 and 3126.2 m³/s.

317 Despite best efforts with modern technology and scientific methods, the 2D models
318 used in this study have uncertainties and errors. Previously it has been reported that 2D models
319 tend to underrepresent the range of hydraulic heterogeneity that likely exists due to insufficient
320 topographic detail and overly efficient lateral transfer of momentum (Pasternack et al., 2004;
321 MacWilliams et al., 2006). For this study those deficiencies result in a conservative outcome,
322 such that there could be more fine details to the sizes and shapes of peak velocity patches than
323 what is revealed herein. Overall, this study involves model-based scientific exploration with
324 every effort made to match reality at near-census resolution over tens of kilometers of river
325 length using current technology, but recognizing that current models do have uncertainties.

326 3.2 *Fixed-Point Hydraulic Data*

327 WSE observations were collected along the LYR between the Highway 20 Bridge and the
328 Feather River confluence using a Leica® System 1200 RTK-GPS ($\Delta H= 1$ cm, $\Delta Z=2$ cm). In
329 total, 199 points were used to compare observed and modeled WSE values. Measurements

330 were collected over the course of two weeks in November 2009. During this period flows
331 remained constant at 24.9 m³/s above DPD and 15.0 m³/s below.

332 A total of 199 point-based field observations of depth and velocity were made at ~ 2 m
333 intervals along 17 cross sections (Fig. S1) on December 8-10, 2009. Seventeen cross-sections
334 constitute a large number relative to published journal articles that report 2D model validation
335 (see citations in the article's section 1.1), but a small number to assess a 36-km-long model
336 domain. Discharge above Daguerre Point Dam was 22.521 and 22.57 m³/s, but 15.26 m³/s
337 below it due to irrigation diversions. Cross-sections were chosen based on whether or not they
338 were wadable and also if the given cross-section spanned a wide range of velocities. Wherever
339 possible, measurements spanned the full channel, but in some cases, cross-sections became un-
340 wadable and measurements were only made as far out into the current as possible. This is a
341 common problem limiting 2D model validation. The water surface elevation was also
342 measured at the water's edge on either side of the river. Point-velocity measurements were
343 made using either a Marsh-McBirney® Flo-Mate ($\pm 33 \text{ mm s}^{-1}$ root mean square error)
344 electromagnetic current meter sampling at 30 Hz or a Price AA mechanical impellor current
345 meter (Fulford, 2001). Both methods averaged velocity measurements over 40 s with sensors
346 positioned at 0.6 of the depth to obtain a measure of the depth-averaged velocity (Buchanan
347 and Somers, 1969; Rantz, 1982; Smart, 1999; Pasternack et al., 2006). Depths for all points
348 were measured using the depth-setting wading rods equipped with the velocity sensors. For the
349 Marsh-McBirney Flo-Mate wading rod, depths were measured to a resolution of ± 1 cm, while
350 the Price AA flow meter wading rod depths were measured to resolution of ± 3 cm.

351 3.3 *Kayak Velocity Measurement*

352 Kayak velocity data was collected at six discharges, including 17.61, 23.13, 30.95, 105.3,

353 114.9, and 141.9 m³/s. Water surface velocity (V_t) at time t was calculated by determining the
 354 total horizontal displacement from one point to the next and then dividing that displacement by
 355 the change in time (Δt) between position measurements:

$$356 \quad \Delta N_t = N_t - N_{t-1} \quad \Delta E_t = E_t - E_{t-1} \quad (5, 6)$$

$$357 \quad dH_t = \sqrt{(\Delta N_t)^2 + (\Delta E_t)^2} \quad (7)$$

$$358 \quad V_t = \frac{dH_t}{\Delta t} \quad (8)$$

359 where N_t is the northing, E_t is the easting, and dH_t is the total horizontal displacement at time
 360 t . This velocity was then assigned to a horizontal coordinate (X_t, Y_t) that is located at the
 361 midpoint of the observed positions used to calculate the velocity.

$$362 \quad X_t = E_{t-1} + \frac{\Delta E_t}{2} \quad (9)$$

$$363 \quad Y_t = N_{t-1} + \frac{\Delta N_t}{2} \quad (10)$$

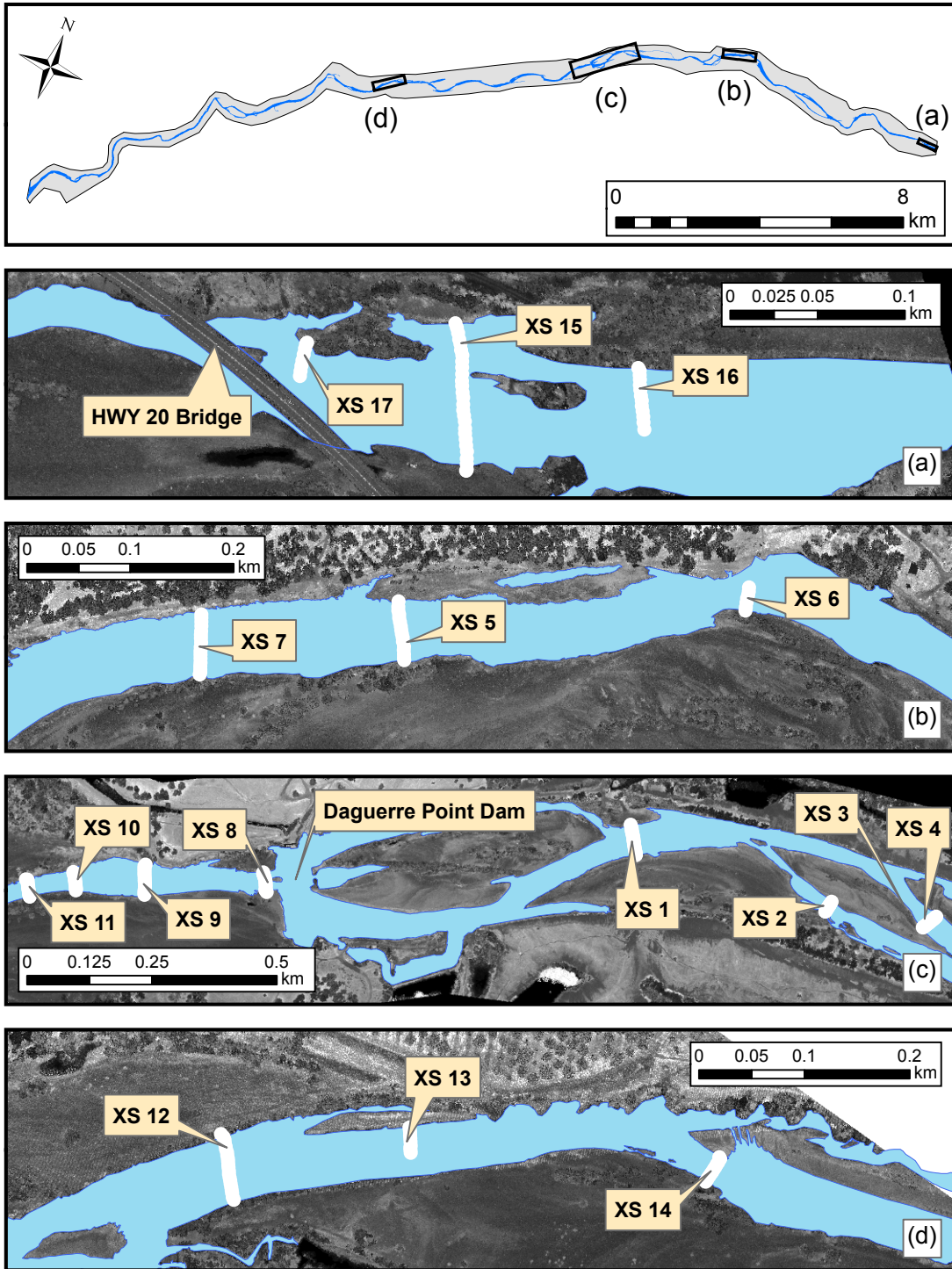
364 Finally, in order to create a velocity vector, a direction value (θ_t) was assigned to each
 365 coordinate using the differences in the northing and easting of consecutive position
 366 measurements:

$$367 \quad \theta_t = \left(\tan^{-1} \frac{\Delta N_t}{\Delta E_t} \right) * \frac{180^\circ}{\pi} \quad \Delta E_t > 0, \Delta N_t > 0 \quad (11a)$$

$$368 \quad \theta_t = \left\{ \left(\tan^{-1} \frac{\Delta N_t}{\Delta E_t} \right) * \frac{180^\circ}{\pi} \right\} + 360^\circ \quad \Delta E_t > 0, \Delta N_t < 0 \quad (11b)$$

$$369 \quad \theta_t = \left\{ \left(\tan^{-1} \frac{\Delta N_t}{\Delta E_t} \right) * \frac{180^\circ}{\pi} \right\} + 180^\circ \quad \Delta E_t < 0, \Delta N_t < 0 \quad (11c)$$

370 where the direction is in degrees. When $\theta_t = 0$, that means the vector is directed due east.



371

372 **Figure S1. Locations of the 17 cross-sections where wading velocity measurements were**

373 **made.**

374 3.4 *Data Analysis*

375 3.4.1 *Velocity Data Preparation*

376 None.

377 3.4.2 *Model Performance Indicators*

378 Among 2D hydrodynamic modeling studies, there is a common suite of validation metrics used
379 in the peer-reviewed literature. Typical metrics include (i) basic statistical measures (i.e. mean,
380 median, and standard deviation) for signed and unsigned deviations as well as those for signed
381 and unsigned percent differences; (ii) regression analysis results in terms of slope, y-intercept,
382 r^2 , and p-value; and (iii) the same as the previous two, but segregating velocity data into small
383 versus large values, as values $< \sim 0.5$ m/s tend to have disproportionately higher error
384 percentages. There is no systematic agreement as to the performance indicators for these
385 metrics for 2D modeling, except that Ballard et al. (2010) proposed that r^2 should be > 0.36
386 (i.e. $r > 0.6$). Pasternack (2011) presented methodologies for 2D model validation and
387 recommended a few more performance metrics. First, the mean and median of the unsigned
388 velocity percent error should be $< 30\%$. Second, the slope of the regression should be > 0.9 ,
389 though this is a quite strict standard compared to most peer reviewed 2D models. Third, the y-
390 intercept should be $< 5\%$ of the maximum velocity. Finally the mean of unsigned velocity
391 direction error should be within 10%.

392 Given the lack of velocity direction validation studies, no performance benchmarks
393 existed *a priori*. Direction varies over 360° , so a 5% error corresponds with 18° . However, for
394 the mainstem thalweg where flow is directed downstream, then a more stringent criterion

395 might be to limit the range to 180° , yielding a 5% error metric of 9° , which was used in this
396 study. This is different from and more stringent than the 10% suggestion of Pasternack (2011).

397 To go deeper into error analysis than is commonly done with standard statistical metrics
398 for 2D model validation, this study also computed the metrics of regression slope standard
399 error and regression intercept standard error. The application of these metrics in this study
400 involved testing the 1:1 expectation of predictions versus observations. By definition, a 1:1
401 relationship is linear ($x=y$). Therefore, the regression function is properly expected to be linear
402 and the computation of standard error metrics assuming a linear regression is also proper for
403 this application.

404 In contrast to the 2D hydrodynamic modeling community, the hydrological modeling
405 community typically uses different metrics as performance indicators for discharge prediction.
406 The choice of metrics ultimately reflects the different nature of the data and different
407 expectations for model performance. Although there is no official standardization of validation
408 in hydrology either, there are a few widely used metrics. For example, Moriasi et al. (2007)
409 present a review of such metrics and that article has been cited more than 1,800 times. Moriasi
410 et al. (2007) does affirm the use of some common 2D modeling validation metrics, but it also
411 describes three common hydrological metrics: Nash-Sutcliffe efficiency (NSE), percent bias
412 (PBIAS), and the root mean square error-observations standard deviation ratio (RSR). The
413 performance standards for these metrics, as reported in that article, often rest on a single
414 reference, so they are not necessarily robust standards. Nevertheless, the standards for
415 discharge prediction are $NSE > 0.5$, $PBIAS$ within 25%, and $RSR < 0.7$. How these apply to
416 depth and velocity vector prediction is unknown, as almost no one uses these in 2D model

417 validation studies. As a new direction for 2D modeling validation, these metrics were applied
418 in this study.

419 Ballard et al. (2010a) suggested that an R-value of 0.6 ($R^2=0.36$) constitutes a validated
420 2D model. Peer-reviewed reports and journal articles have reported R^2 values and slopes
421 ranged from 0.25-0.92 and 0.66-0.86, respectively, in similar comparisons of model-predicted
422 versus field-measured velocities (e.g. Lane et al., 1999; Pasternack et al., 2006; Harrison and
423 Keller, 2007; May et al., 2009; Ballard et al., 2010a,b; Pasternack and Senter, 2011). These
424 values therefore were used as performance indicators, though the range of previously accepted
425 benchmark values for “validation” is so broad that no effort was made to judge the
426 appropriateness of a specific threshold value for use this study; it is left up to the reader to
427 decide that relative to the peer-reviewed literature values cited above. Histogram analysis and
428 descriptive statistics of differences between model-predicted and field-measured velocities
429 were also used to test model performance. Absolute velocity errors were compared with
430 observed velocities to determine how the model performed across the range of velocities and
431 determine if there were any noticeable trends. Furthermore, to help explain the cause of
432 velocity errors, model-predicted depths were evaluated as an indicator of topographic
433 uncertainty and Manning’s roughness parameterization. Cross-sectional analysis of model
434 performance relative to DEM structure was also evaluated to help visualize and explain model
435 errors. The above analyses constitute the typical suite of tests performed for 2D models in the
436 peer-reviewed journal literature. 2D Model Validation Using Fixed-Point Velocities

437 Wading-based depth and velocity data were directly compared with model results as one test of
438 model performance. The data also served as a benchmark for kayak-based velocity
439 performance. Observed velocities were graphed against model-predicted velocities and a linear

440 best-fit trendline was added to the data (likewise for depths). The coefficient of determination
441 (R^2) value of the best-fit line and slope were used as indicators of model performance.

442 **3.4.3 *Direct 2D Model Validation***

443 None.

444 **3.4.4 *Adjusting Kayak Surface Velocity To Mean Velocity***

445 According to Rantz (1982) using the data from the study conducted by Hulsing et al. (1966)
446 natural channels have a DAVC of ~0.85-0.86 for surface velocities. The raw data was collected
447 at cross-sections in channels classified into five types, phrased as: (1) natural trapezoidal-
448 shaped channel without overbank flow and no bridge piers or other manmade obstructions, (2)
449 natural channel with bridge piers, abutments or manmade obstructions that may affect the flow
450 pattern, (3) canal or manmade channel without overbank flow, (4) and (5) same as (1) and (3)
451 above, but with overbank-flow sections. They also span discharges of 0.031 to 18,000 m³/s
452 (Hulsing et al., 1966). As a result, the measurements generally reflect settings with a low
453 roughness:depth ratio. Meanwhile, Pasternack et al. (2006) collected full vertical velocity
454 profiles over an artificially constructed gravel bed in the Mokelumne River (similar to the bed
455 present in the lower Yuba River, except for the absence of any sand in the artificial
456 Mokelumne bed) and found that the slope of the least squared regression equation between the
457 observed mean column velocity and observed near-surface velocity was 0.71, with a sample
458 size of 23 and an R^2 of 0.672. Although the magnitude of the slope coefficient may change
459 with different depth:bed material ratios, the existence of this fundamental relation was
460 persistent and reliable. Furthermore, vertical velocity profiles collected in Timbuctoo Bend on
461 the LYR in an unpublished study (co-author Greg Pasternack, UC Davis) yielded a minimum

462 DAVC of 0.65, indicating that there is a range of possible DAVC's across rivers of diverse
463 flow:geometry ratios (though that was in 2004 before the big floods that stripped off the armor
464 layer causing the bed to become less rough).. Thus, in addition to testing Rantz's published
465 value of 0.85, the DAVC was varied to optimize three performance indicators with model-
466 predicted results. These indicators were (1) the mean velocity difference between observed and
467 predicted velocities (i.e. difference of ~0 m/s), (2) the mean error (i.e. mean error ~ 0%), and
468 (3) best-fit trendline slope of V_{modeled} versus V_{observed} (i.e. slope ~ 1). The goal of this test was
469 to see how the three DAVC values compared with each other and with the value published by
470 Rantz (1982).

471 **3.4.5 Testing Discharge Dependence of Model Error**

472 None.

473 **3.4.6 Comparing Validation Outcomes**

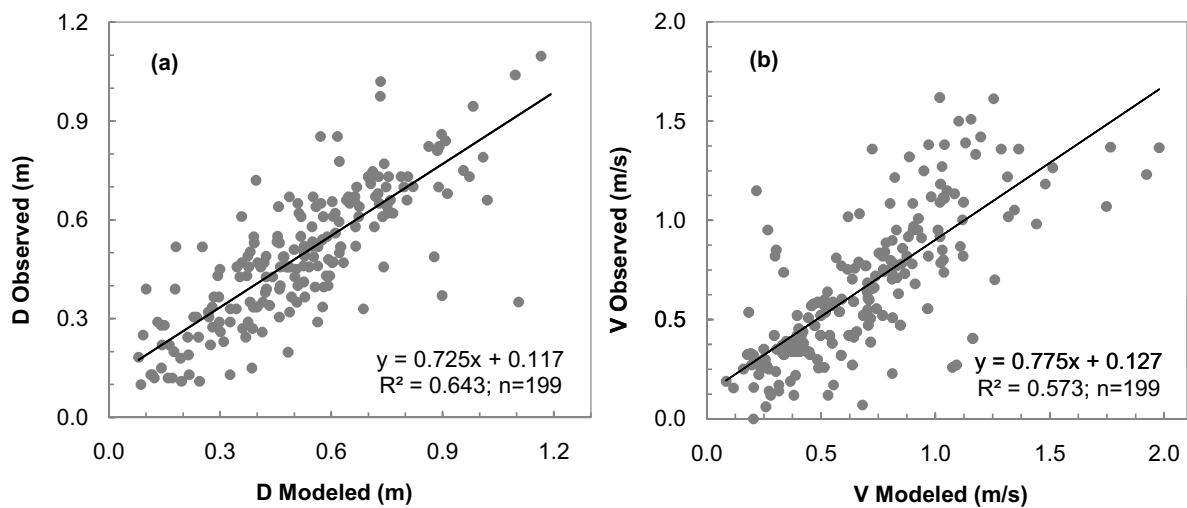
474 None.

475 **4 Results**

476 **4.1 2D Model Validation Using Fixed-Point Velocities**

477 Velocities were measured in depths < 1.23 m. The mean velocity was 0.67 m/s, with a range of
478 0.00–1.62 m/s. The average coefficient of variation of velocity was 0.39, with a range of 0.12–
479 0.70. Regression and correlation analyses of observed versus model-predicted depths and
480 velocities yielded statistically significant trendlines and correlations above the 95% confidence
481 level. For depth, the best-fit trendline had slope and R^2 values of 0.73 and 0.64, respectively
482 (Fig. S2a). For velocity, it had corresponding values of 0.78 and 0.57, respectively, indicating a

483 better 1:1 performance, but worse correlation performance than depth (Fig. S2b). Both
484 relations show a bias in which low values are over predicted and high values are under
485 predicted. Both indicators of performance are right in the middle of the range of peer-reviewed
486 2D-model validations. When modeled results were regressed on observations, the standard
487 error of the regression slope and intercept for velocity were 0.0455 and 0.035, respectively.
488 Both of these values are low and they help to appreciate that a regression plot with thousands
489 of points often hides the true precision of the results, which in this case is quite high. Using
490 hydrological performance indicators, the values of NSE, PBIAS, and RSR were 0.52, -4.4%,
491 and 0.69. These values are within the thresholds accepted by the hydrological community.



492

493 **Figure S2. Predicted model results versus measured, cross-sectional wading values with**
494 **calculated best-fit trendlines and linear regression for: (a) depths; (b) velocities.**

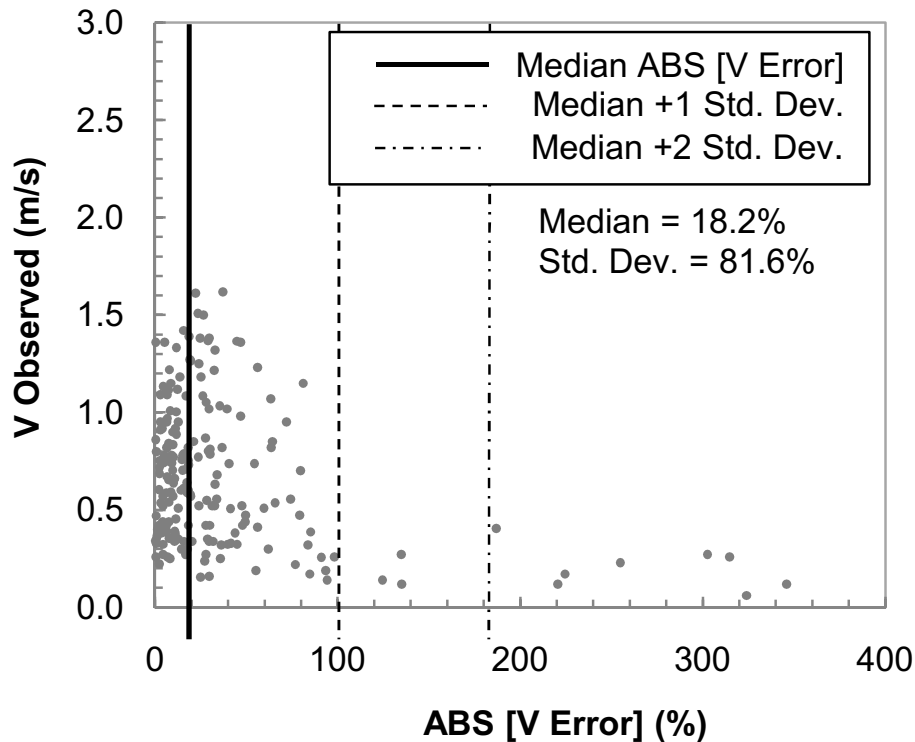
495 The mean value of raw differences between modeled and observed depths was 0.025 m
496 with a standard deviation (SD) of 0.140 m (Table S1). Histogram analysis showed that 20.1%
497 of modeled depths were within 0.03 m. of observed values and 77.4% were within 0.15 m. For
498 reference, the median bed material size in the vicinity of the cross-sections is ~ 0.06 m, so one

499 would not expect most deviations to be smaller than that. The mean absolute error was 25.5%
500 with a SD of 30.3%.

501 The mean raw difference of modeled and observed velocities for all the points was
502 0.029 m/s with a SD of 0.25 m/s (Table S1). The mean absolute error was 40.0% with a SD of
503 81.6%. The largest velocity errors (200-800%) correlated with some of the smallest observed
504 velocities (Fig. S3). Histogram analysis found that 16.1% of the modeled values were within
505 0.03 m/s of the observed values, 60.3% were within 0.15 m/s, and 90% were within 0.41 m/s.
506

Table S1. Descriptive statistics for modeled versus wading-based hydraulics.

	Depth (m)			
	D_{Diff}	$ABS(D_{Diff})$	D_{Error}	$ABS(D_{Error})$
Mean	0.025	0.102	9.3%	25.5%
Standard Error	0.010	0.007	2.7%	2.1%
Median	0.027	0.075	5.0%	17.2%
Standard Deviation	0.140	0.099	38.5%	30.3%
Range	1.092	0.755	289.6%	215.3%
Minimum	-0.337	0.000	-74.3%	0.0%
Maximum	0.755	0.755	215.4%	215.4%
	Velocity (m/s)			
	V_{Diff}	$ABS(V_{Diff})$	V_{Error}	$ABS(V_{Error})$
Mean	0.029	0.176	22.0%	40.0%
Standard Error	0.018	0.013	6.3%	5.8%
Median	0.014	0.111	2.3%	18.2%
Standard Deviation	0.253	0.183	88.2%	81.6%
Range	1.753	0.931	952.2%	870.9%
Minimum	-0.932	0.001	-81.1%	0.2%
Maximum	0.821	0.932	871.1%	871.1%

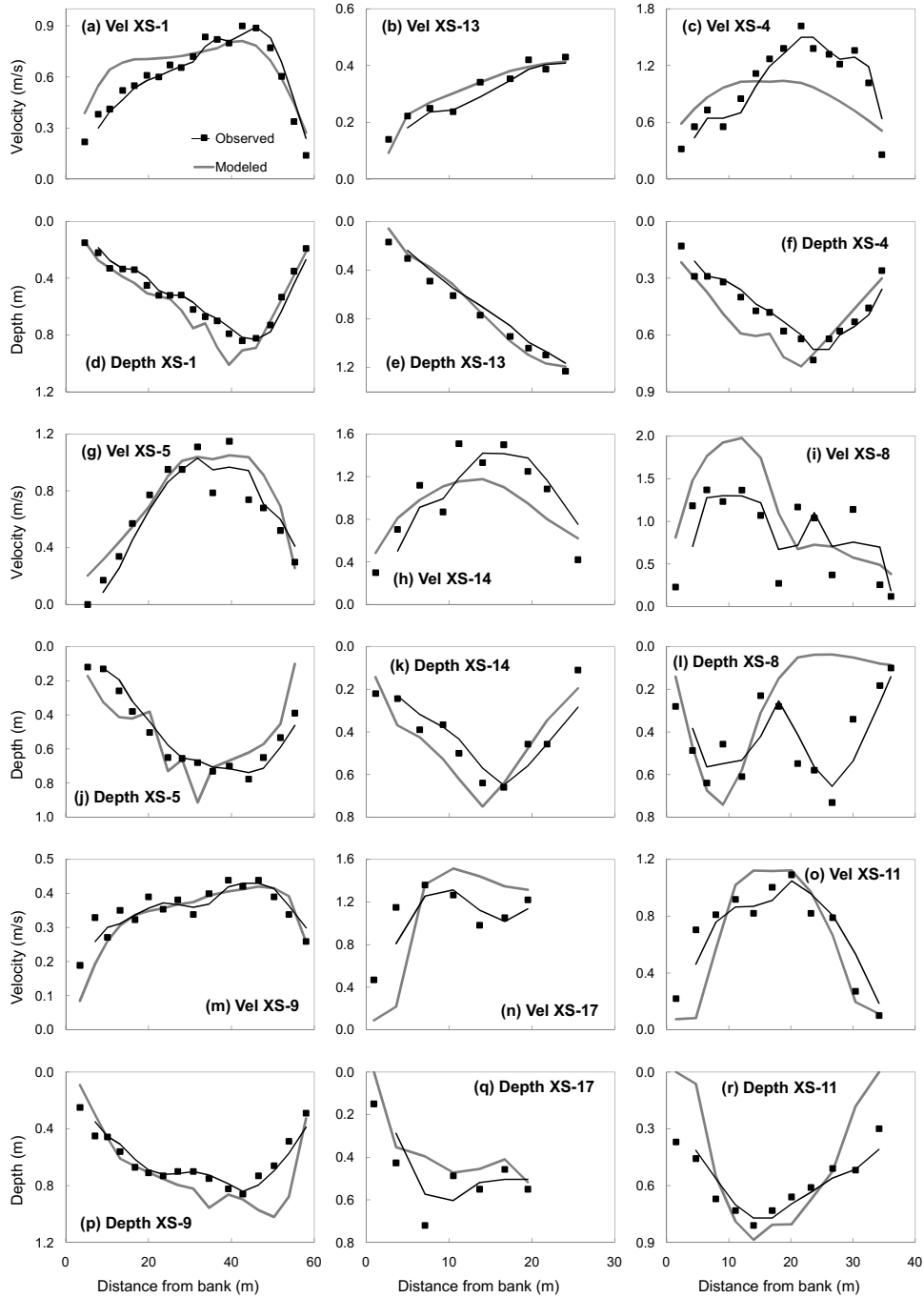


509

510 **Figure S3. Absolute velocity error versus wading velocities.**

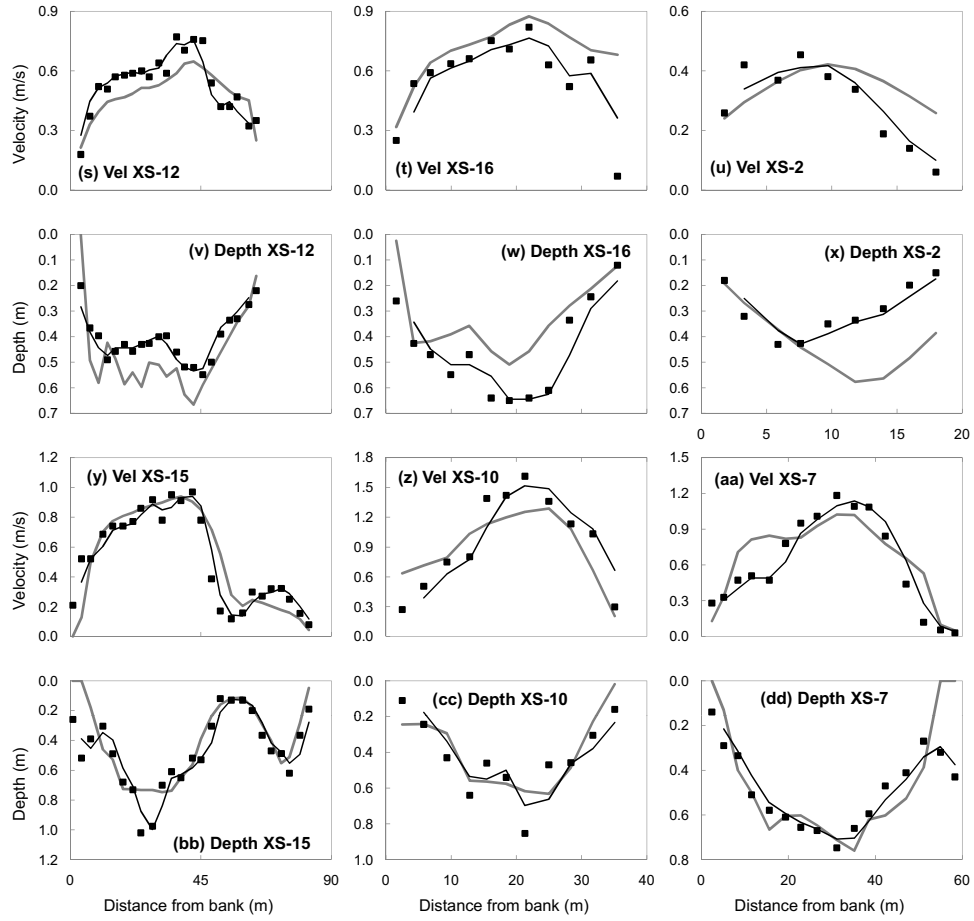
511 Cross-sectional comparisons of the lateral patterns of observed and modeled depths and
 512 velocities help explain the significant causes of model error and bias (Fig. S4). As is typical,
 513 cross-sections have low depths and velocities along the banks, except where there is forced
 514 scour. However, for some cross-sections, the model over-predicted both variables there (e.g.
 515 Fig. S4a,i,t,u). A poor specification of roughness would yield an inverse bias between depth
 516 and velocity, so that is unlikely to be the main cause. The choice to not use a different
 517 roughness value for banks than the ambient bed could still be a secondary factor causing bank
 518 velocities to be too high. An excessive eddy-viscosity coefficient disproportionately affects
 519 velocity, so adjusting that down in future studies might improve model performance (but that
 520 was not evaluated as part of this study). Finally, given a near-flat water surface across the
 521 cross-sections, the deviations in depth are a surrogate for topographic error (Pasternack et al.,

522 2006). Such error is attributable to the gap between the airborne LiDAR survey of terrestrial
523 topography and the boat-based survey of bathymetry; wherever the boat could not get within a
524 meter of the bank, meaningful landform variability may have been missed (Fig. S5). Although
525 there was an extensive effort to avoid inaccuracies in the DEM due to the large scale of the
526 project, inability to wade certain areas, along with time and monetary restrictions, a couple of
527 locations were not as detailed as required for accurate model predictions. TIN-based
528 interpolation during DEM production would then just cut off those features (e.g. Fig. S4l,n,r).
529 In other instances, boat-based bathymetric measurements simply appear to be faulty (e.g. Fig.
530 S4f,w). Observations made within 2.5 m of the model predicted wetted channel perimeter
531 averaged a difference in velocity of 0.072 m/s which is ~2.5 times larger than the mean for all
532 points. Furthermore, mean velocity error for the same points (45.8%) was ~24% higher than
533 the total mean.



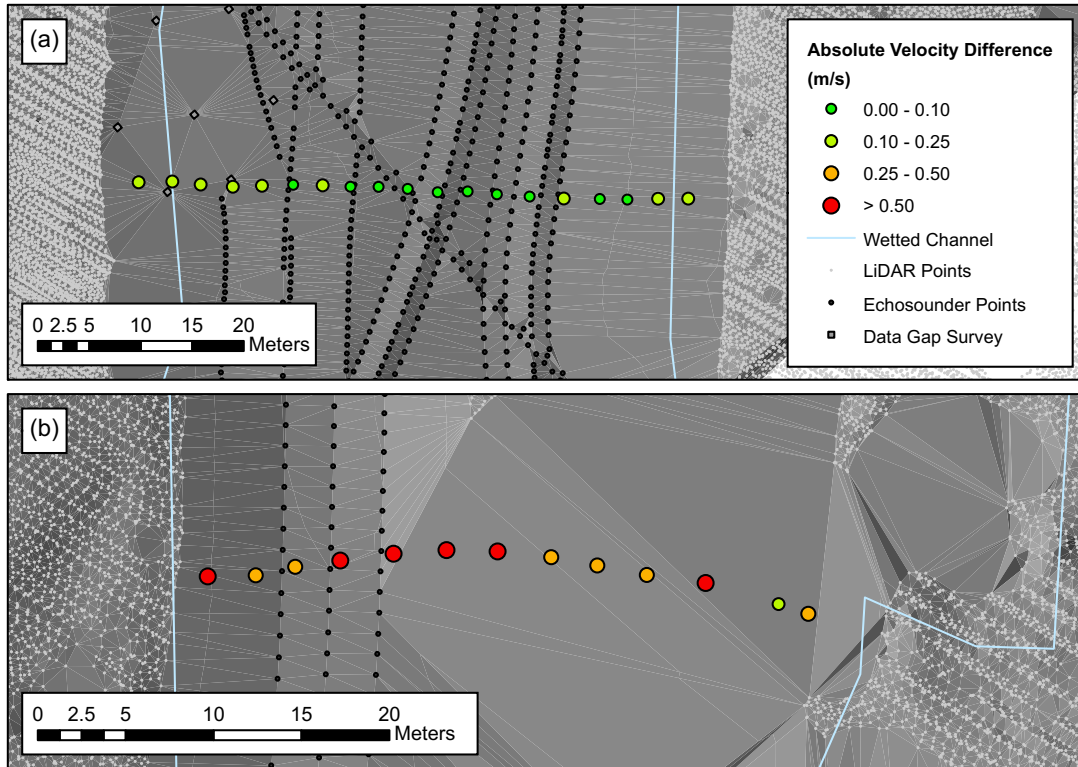
534

535 **Figure S4. Comparisons of observed versus predicted depths and velocities at all cross-**
 536 **sections. Field observations were fit with a curve using the local average to reduce**
 537 **measurement noise.**



538

539 **Figure S4. Continued.**



540

541 **Figure S5. Maps of the DEM showing the absolute difference between model velocities**
 542 **and measured, wading velocities: (a) small differences in velocity because of accurate**
 543 **representation of the land surface due to good survey coverage [XS 1] and (b) large**
 544 **differences in velocities due to poor, in channel survey coverage [XS 8].**

545 *4.2 2D Model Validation Using Kayak Observations*

546 Mean observed surface velocity was 0.87 m/s, with a range of 0.15–3.44 m/s respectively.

547 Kayak velocities were made at model-predicted depths of up to 4.37 m. Mean, minimum, and
 548 maximum kayak directional values were 208.0°, 134.7°, and 303.5° respectively.

549 *4.2.1 Statistical Velocity Validation*

550 Differencing results and velocity error analysis for Rantz’s published DAVC yielded the

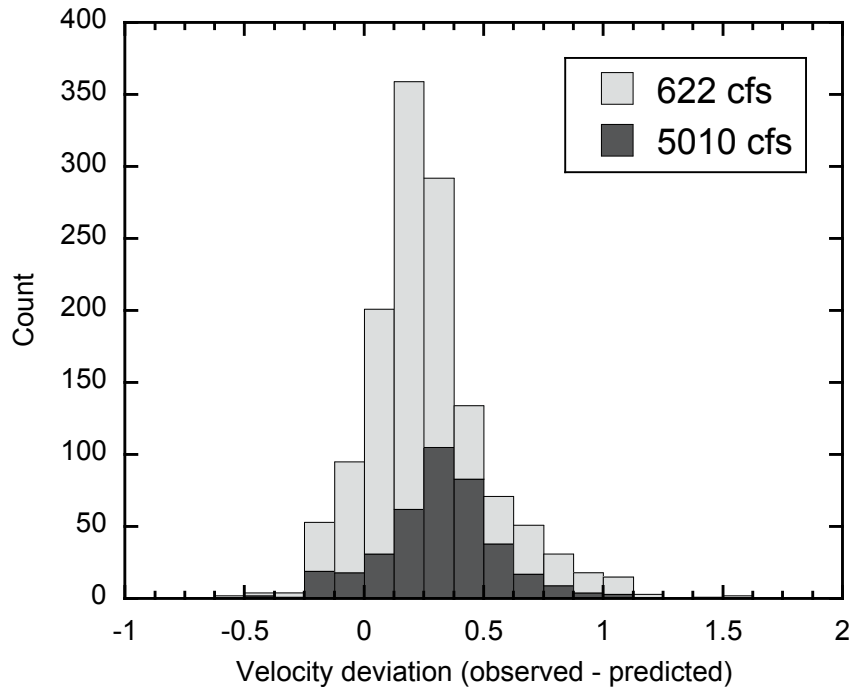
551 largest dissimilarities, of the four DAVCs tested, with the modeled results. The mean
552 difference was -0.285 m/s and SD was 0.286 m/s (Tables S2-S3). Mean error and SD of the
553 error were 20.1% and 24.3% respectively. The best-fit trendline slope was 1.195 with a y-
554 intercept of 0.115. Mean velocity-difference optimization obtained a DAVC equal to 0.64,
555 which resulted in a mean difference of 0.00 m/s, an absolute mean difference of 0.15 m/s, and a
556 standard deviation of 0.21 m/s. DAVC equal to 0.64 resulted in the largest mean, standard
557 deviation, and range for velocity error which was -6.1%, 32.3% and 388.4% respectively.
558 Mean error optimization resulted in a DAVC of 0.68. Mean error came out to be 0.1% with an
559 absolute error of 20.6% and a SD of 30.3%. Finally, trendline slope optimization resulted in a
560 DAVC equal to 0.71, the same as the value used for the 2D model validation. A description of
561 those results can be found in the previous section.

562 The analysis of varying the DAVC to optimize different parameters showed that DAVC
563 values were low compared to published values, most of which come from deeper, slower
564 channels with fine riverbed sediment. Although each of the DAVC metrics has its own
565 benefits, there is no obvious best choice. The DAVC of 0.64 with an optimized mean velocity
566 difference also has the best velocity difference distribution and error distribution. As
567 mentioned in the section 3.6.3, unpublished vertical velocity profiles collected by co-author
568 Pasternack and associates in Timbuctoo Bend on the LYR yielded a minimum DAVC of 0.65,
569 which is close to this value (though that was in 2004 before the big floods that stripped off the
570 armor layer causing the bed to become less rough). However, 0.65 was the lowest value found
571 in the published literature, which raises the question: Should observed values be adjusted to
572 match predicted values? While 0.64 seems like the best option based on the numbers, 0.71 is
573 likely to be the more realistic value. First, this value is the same that was calculated by

574 Pasternack et al. (2006) for 24 vertical profiles where full vertical velocity profiles were
575 measured. Second, although the mean velocity difference was -0.1 m/s for DAVC=0.71, this
576 can be explained by the fact that there were slightly more values at low velocities where the
577 model tended to over-predict velocity. After further experimentation with 2D models in diverse
578 channel settings, it is now thought that this can be improved in the future by significantly
579 reducing the eddy-viscosity coefficient for shallow gravel-bed rivers from the generic value of
580 $\sim 0.6-0.7$ to $\sim 0.075-0.1$, thereby enhancing the lateral gradient in velocity magnitude. It is
581 recommended that studies adjust this value specifically for improving the lateral gradient as
582 well as the pattern of eddies (Wheaton et al., 2004). Finally, this study was performed in a
583 channel with a high roughness to depth ratio, whereas classic studies yielding DAVCs of >0.8
584 were done in channels with low ratios. Extra roughness means a stronger vertical velocity
585 gradient and a lower DAVC. This likely is the reason for the large dissimilarity between model
586 and observed results when applying Rantz's DAVC of 0.85.

587 ***4.2.2 No Discharge Dependence of Model Error Found***

588 Probability density functions of the velocity deviations for each discharge are plotted, so
589 interested readers who attempt this approach can compare their distributions (Figure S6).
590 Mean, Standard deviation, skewness, and kurtosis values are 0.237, 0.263, 1.234, and 2.988 for
591 the lowest flow and 0.314, 0.240, -0.026, and 0.766 for the highest flow.



592

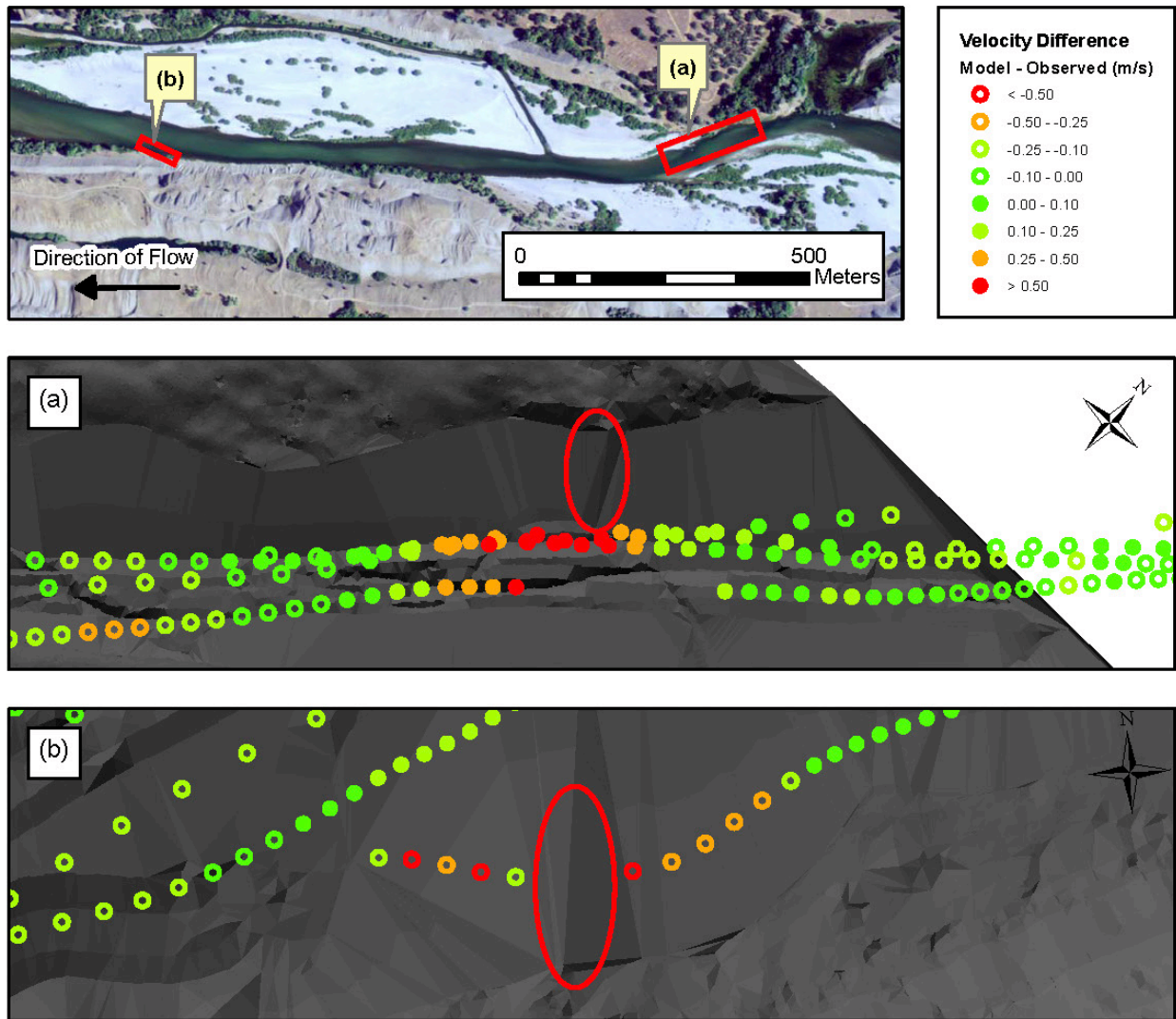
593 **Figure S6. Probability density functions of velocity deviations between observed and**
 594 **predicted by the 2D model.**

595

596 **4.2.3 Spatial Velocity Validation**

597 Despite efforts to avoid it, there were localized occurrences of poor topographic
 598 interpolation between in-channel single-beam echosounder points and out-of-water airborne
 599 LiDAR points, and these caused locally poor model performance (e.g. see Figure S7). In this
 600 study, there was an abundance of data available and breaklines were used in places where
 601 triangulation issues were evident at a coarser scale, but there were still localized data gaps.
 602 With ~ 36 km of river to map and model at one-meter resolution, it is costly and time-
 603 consuming to inspect every locality within the map, despite reasonable efforts to do so. In
 604 similar fashion for hydrological modeling, hardly any effort is made to thoroughly inspect

605 landscape DEMs to represent every nook and cranny. When creating a TIN through the gaps in
606 the point data, a triangle sometimes interpolated laterally from the bank to a point in the
607 channel creating a ridge extending into the channel (features circled in red Figure 76). The
608 model would interpret these features as constrictions or barriers, and would either accelerate
609 flow through the main channel (Figure S7a) or block flow (Figure S7b). Where available and
610 suitable today, bathymetric LiDAR and multibeam echosounding are replacing single-beam
611 echosounding, avoiding such problems. Another solution, though time-consuming, is to run a
612 coarse-resolution 2D model quickly, test the model against data to find the worst performing
613 localities, and fix them iteratively.

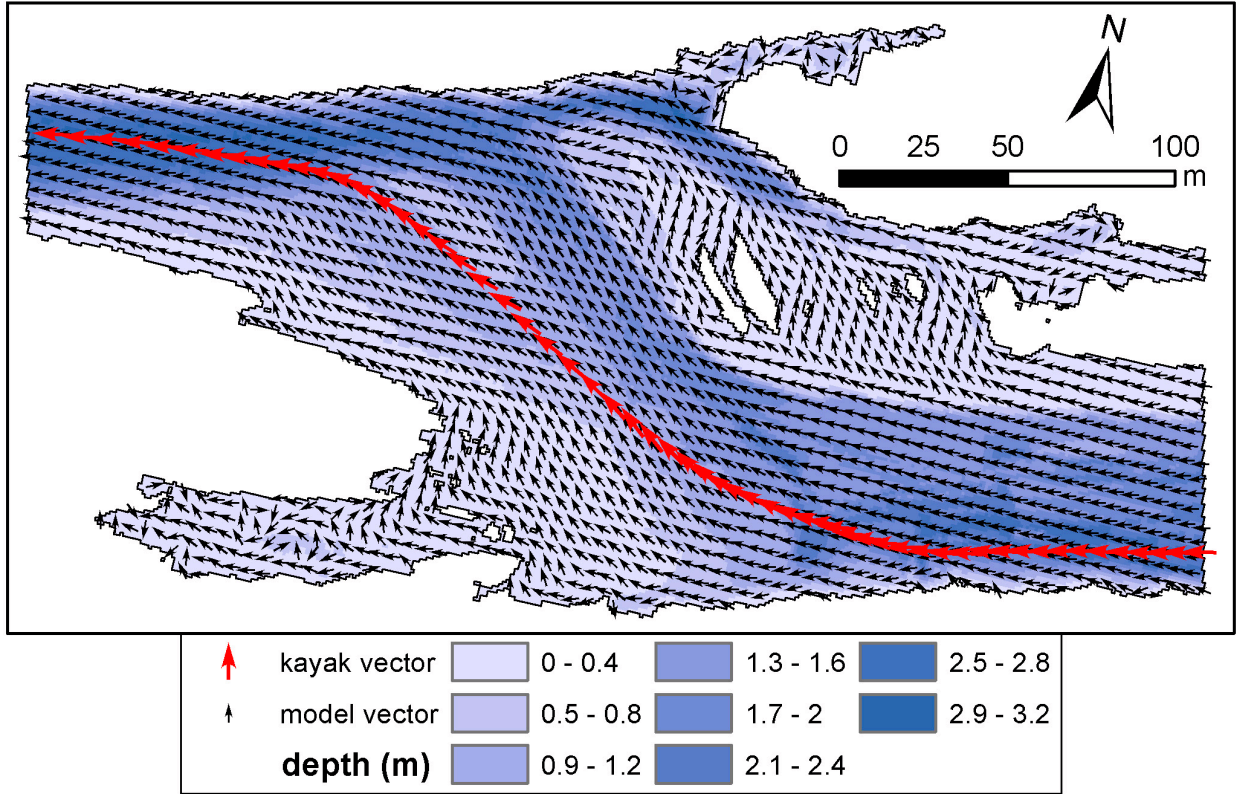


614

615 **Figure S7. Differences between modeled and observed kayak velocities due to locally**
 616 **inaccurate DEM interpolations.**

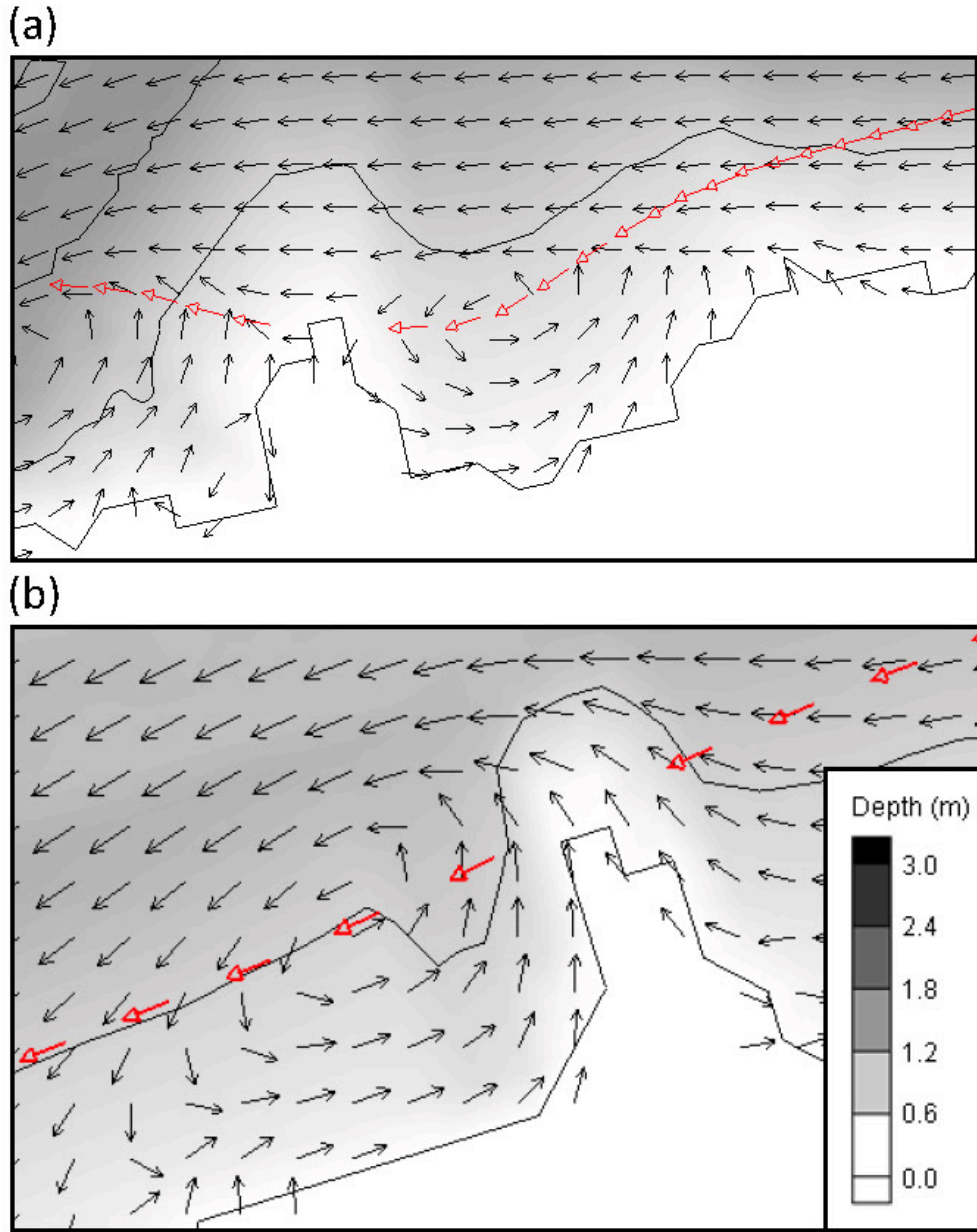
617 **4.2.4 Directional Validation**

618 This study led to the realization that validation of eddies important to stakeholders requires
 619 focused kayak data collection in which the boat recirculates several times around the eddy on
 620 different paths. Slow eddies require slow GPS time interval sampling of 10-30 s.



621

622 **Figure S8. Vector fields on a small portion of the Daguerre Point Dam reach at $105 \text{ m}^3/\text{s}$.**



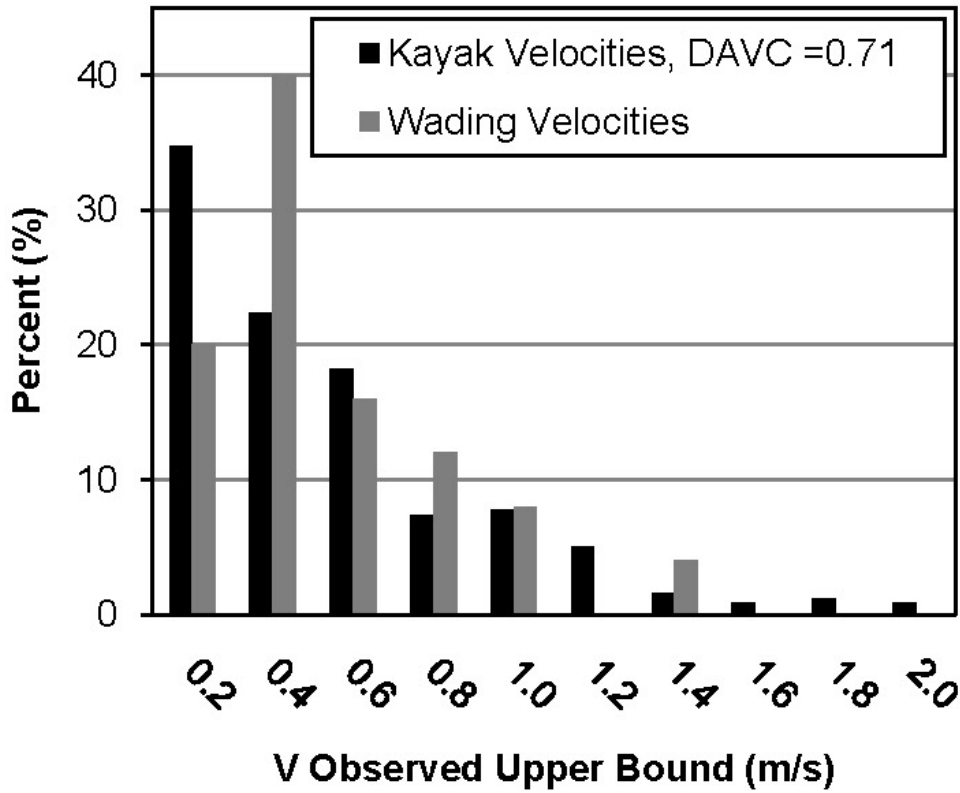
623

624 **Figure S9. Areas where the model predicted flow vectors differ greatly from the kayak**
625 **measured velocity vectors due to model predicted eddies.**

626 4.3 Comparing Validation Outcomes

627 Distributions of observed velocities with an $ABS(V_{error}) > 50\%$ for both fixed-point and kayak
628 velocity datasets showed important differences (Figure S10). The fixed-point dataset had a log-

629 normal distribution, while the kayak dataset had an exponential distribution. The peak of these
630 errors was higher with the fixed-point data than with the kayak data. The latter also showed a
631 longer upper tail.



632

633 **Figure S10. Distribution of observed fixed-point and kayak velocities with V Error >**

634 **50%.**

635

Table S2. Descriptive statistics for modeled versus kayak-based velocity deviations and percent errors for all DAVC values tested.

(A) Velocity Differences, Modeled - Observed (m/s)

Statistic	DAVC = 0.64		DAVC = 0.68	
	V _{Diff}	ABS(V _{Diff})	V _{Diff}	ABS(V _{Diff})
Mean	0.001	0.150	-0.054	0.159
Std. Error	0.009	0.006	0.009	0.007
Median	0.013	0.109	-0.036	0.111
Std. Dev.	0.210	0.147	0.219	0.160
Range	2.042	1.154	2.087	1.269
Min	-1.154	0.000	-1.269	0.000
Max	0.888	1.154	0.818	1.269

Statistic	DAVC = 0.71		DAVC = 0.85	
	V _{Diff}	ABS(V _{Diff})	V _{Diff}	ABS(V _{Diff})
Mean	-0.095	0.175	-0.285	0.314
Std. Error	0.010	0.007	0.004	0.003
Median	-0.072	0.120	-0.247	0.254
Std. Dev.	0.228	0.174	0.286	0.254
Range	2.127	1.355	2.377	1.756
Min	-1.355	0.000	-1.757	0.000
Max	0.772	1.355	0.620	1.757

(B) Velocity Error (%)

Statistic	DAVC = 0.64		DAVC = 0.68	
	V _{Error}	ABS(V _{Error})	V _{Error}	ABS(V _{Error})
Mean	-6.1	21.5	0.1	20.6
Std. Error	0.42	0.33	0.40	0.29
Median	-1.6	14.2	4.3	14.2
Std. Dev.	32.2	24.7	30.3	22.2
Range	388	292	366	269
Min	-292	0.00	-269	0.00
Max	96.5	292	96.7	269

Statistic	DAVC = 0.71		DAVC = 0.85	
	V _{Error}	ABS(V _{Error})	V _{Error}	ABS(V _{Error})
Mean	4.4	20.8	20.1	27.0
Std. Error	0.38	0.27	0.32	0.21
Median	8.4	15.6	23.5	25.3
Std. Dev.	29.0	20.7	24.3	16.2
Range	350	253	292	195
Min	-253	0.00	-195	0.04
Max	96.8	253	97.3	195

Table S3. Histogram analysis of kayak observed velocity.

<i>Velocity Difference Distribution</i>	DAVC = 0.64	DAVC = 0.68	DAVC = 0.71	DAVC = 0.85
Within 0.03 m/s	15.74%	13.91%	12.73%	4.88%
Within 0.15 m/s	64.62%	63.03%	58.67%	28.13%
<i>Error Distribution</i>				
Within 5%	19.88%	19.13%	17.37%	5.85%
Within 10%	37.13%	37.35%	34.26%	12.40%
Within 25%	73.04%	72.65%	70.48%	48.82%
<i>Best-Fit Line</i>				
Slope	0.900	0.956	0.998	1.195
Intercept (m/s)	0.087	0.092	0.096	0.115

638 **5 Discussion**

639 Using the same traditional methods of 2D-model validation as commonly reported in the peer-
640 reviewed literature, the LYR 2D model performed on par with past peer-reviewed studies
641 (Figs. S2, S4). Observed velocities for cross-sections 1, 5, 9, 11, 12, 13, 15, and 16 match
642 model-predicted velocity's trends, while those for cross-section 2, 4, and 8 showed major
643 discrepancies, which is typical in the literature. Depth and velocity test R^2 values of 0.64 and
644 0.57 were right in the middle to upper range of the values previously reported. Note that some
645 studies only report R (e.g. Ballard et al., 2010a,b), not R^2 , so care must be used in making
646 comparisons. Further, lateral patterns of deviations in depth and velocity showed smoothing
647 across the channel with lows too high and highs too low. This is a typical occurrence of errors
648 due to topographic uncertainty and errors due to an inadequate rate of velocity change
649 associated with excessively efficient turbulent mixing (MacWilliams et al., 2006) and perhaps
650 insufficient bank roughness (Abu-Aly et al., 2013).

651 *5.1 Improved Sampling of Deep And Fast Areas*

652 Boat-based ADCP can go into deep current, but it normally requires holding position to get a

653 good measurement and it is extremely difficult to collect boat-based ADCP data in fast,
654 hazardous conditions, locations with obstructions, and shallow water impacted by the ADCP's
655 blanking depth, all of which the kayak method can handle.

656 Similar results were obtained by only using the highest and lowest flows, indicating
657 that cost savings are possible and that model performance is likely insensitive to specific
658 discharges. This is promising, because it indicates that it may be unnecessary to do validations
659 at every discharge for which scientific analysis would be performed, and validating models for
660 hazardous floods is rarely feasible. It is really only necessary to collect new model calibration
661 and validation data when the hydraulic roughness structure changes a lot, such as when
662 vegetation becomes submerged (Abu-Aly et al., 2013).

663 *5.2 Improved Sampling Of Statistical Structure*

664 Testing 2D-model performance with the kayak observations yielded a 39% higher value for r^2
665 (0.79 versus 0.57), and the value of DAVC did not matter for this metric. This high correlation
666 between modeled and observed velocity is among the best in peer-reviewed reports and journal
667 articles evaluating a shallow gravel-bed river. After adjustment with the DAVC, the
668 comparative performance between velocity tracking versus fixed-point observations, as
669 measured with the standard error of the regression slope and intercept metrics, was ~6-9 times
670 better with the former approach. In terms of the hydrological performance metrics, both NSE
671 and RSR were significantly better in the velocity tracking results, while PBIS was better in the
672 fixed-point results.

673 *5.3 Improved Spatial Testing*

674 None.

675 5.4 *Putting The 2D In 2D Model Validation*

676 None.

677 5.5 *Important Kayak Limitations*

678 Sections 1.3 and 3.4 of the main article and supplementary file previously addressed the
679 uncertainties in kayak RTK GPS surface velocity measurements, so the focus here is on the
680 limitations of using such data in 2D model validation. Although the kayak RTK GPS method
681 of measuring surface velocity was valuable for fast, low-cost 2D model validation, it did have
682 some problems. First, there were major discrepancies between modeled and measured results at
683 very low velocities (Figure 4). The best solution would be to adjust the GPS time interval for
684 different flow speeds, so 5 s would be adequate for velocities of > 0.5 m/s, while 10–30 s
685 might be needed for 0–0.5 m/s speeds.

686 Second, GPS units only record time to the nearest second, so it is plausible that more
687 error is arising from inaccurate time stamps than spatial precisions. If the fixed time interval
688 sampling algorithm in the Trimble software uses the internal clock only to identify the time
689 interval, then the exact time does not matter and the error in change in time is likely quite low.
690 However, if the time interval is not truly fixed and hinges on the absolutely clock time,
691 recorded only to the nearest 1 s, then that would introduce uncertain error. For a 5 s time
692 interval, an error of 0.5 s (the worst possible for a 1 s clock) would yield a 10% error in
693 velocity, so that is significant. However, for any instant in time with a 5 s sampling interval,
694 the likelihood of 10% error is equal to that of 0% error, so one cannot account for this
695 quantitatively. Third, no surface particle tracking method is viable in high winds. High winds
696 can be more of a problem at slow base flows and over slow, shallow embayments than in the

697 thalweg of a large flood in the middle of a big storm. Finally, for a large enough flood, it may
698 be sensible to switch from a kayak to a larger boat, possibly motorized for safety and
699 effectiveness in that regime. Initial testing with a motorboat found that it was more difficult to
700 match the timing of speed adjustments and the boat was more sensitive to wind, but for large
701 floods it would be viable. Conversely, if a stream was only 1-20 m wide, then a manned kayak
702 would likely be too big of a drifter to be viable. Further discussion about future improvements
703 to kayak velocity mapping is provided in the supplementary materials file in section 5.6.

704 *5.6 Future Improvements*

705 In this study, velocities were largely measured in the thalweg and observations did not
706 accurately represent the whole range of velocities at each individual flow, especially with
707 insufficient sampling along channel banks and in very slow conditions. This caused a
708 clustering of observations and a velocity gap between high and low flows. Pasternack and
709 Senter (2011) built on this pilot effort and tested 2D model performance in a steep mountain
710 river over two orders of magnitude in the range in flow to assess validation sensitivity to
711 discharge, among other things. They took the approach of being sure to sample the full range
712 of safely accessible velocity bins by wading and kayak at every discharge, with less emphasis
713 placed on spatial coverage in light of the remote setting. Therefore, each day's dataset could be
714 used to produce a scatter plot validation test, yielding an even more robust statistical analysis
715 when all days were combined. This approach of mindful sampling to achieve a more equal
716 representation of each velocity bin each time out guarantees that a scatter plot can be made
717 from the available data even if higher flows never come, since one cannot usually preordain
718 what flows a river will deliver during the validation period. Thus, the best procedure involves
719 focusing on sampling a diversity of velocity vector conditions instead of staying on one

720 streamline. People should spend time mapping recirculating eddies, observing zero-velocity
721 locations, and going over the most aggressive chutes. This is done by starting and stopping the
722 GPS data collection as needed, as well as using a path identifier in the data description field.
723 Being on the drifter is the key to mindful mapping, and this in turn may lead to more robust
724 validation testing, because it enables more sampling in the periphery where survey data and
725 DEM representation are often worse making validation tests more useful to find such
726 problems. Also, 2D models typically better represent deeper flows than very shallow flows, so
727 more data collection in shallow, outlying areas of the channel would help strengthen the
728 validation process.

729 In the future, it may be beneficial to attach an echosounder and/or an ADCP to the
730 kayak to measure depths and velocity profiles to get more data for validation and to aid
731 interpretation of validation problems. Topographic error is the dominant cause of velocity error
732 (Figure S5), even with the high-quality topography collected for this study, so dual observation
733 is sensible.

734 **6 CONCLUSIONS**

735 None.

736 **7 GEOLOCATION**

737 39°13'13" N, 121°20'7" W

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