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Chemical routes to materials



Synthesis and characterization of aluminum diboride products using ²⁷AI, ¹¹B NMR and ab initio studies

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ABSTRACT

Understanding different bonding environments in various metal borides provides insight into their structures and physical properties. Polycrystalline aluminum diboride (AlB₂) samples have been synthesized and compared both with a commercial sample and with the literature. One issue that arose is the relative ease with which boron-rich and aluminum deficient phases of aluminum borides can be presented in AlB₂. Here, we report ²⁷Al, ¹¹B nuclear magnetic resonance (NMR) spectroscopy and first-principles calculations on AlB₂ in order to shed light on these different bonding environments at the atomic level and compare the structural and electronic properties of the products of different preparations. Along with the aforementioned, the present study also takes an indepth look at the nature of the ¹¹B and ²⁷Al nuclear spin–lattice relaxation recovery data for the AlB₂ and other superhard materials. The nuclear spin-lattice relaxation has been measured for a static sample and with magic-angle spinning. The combination of NMR and band structure calculations highlights the synthetic challenges with superhard materials.

Introduction

Boron interacts with metals to produce compounds with a variety of structures. For example, at least five different binary compounds formed between tungsten and boron have been reported: W_2B , WB (two crystal structures), WB₂, W_2B_4 (formerly described as W_2B_5), and WB₄ [1–4]. Metal borides also exhibit a range of interesting physical properties, including superconductivity [5] and superhardness [6]. Understanding the different bonding environments in the various metal borides provides insight into the structures and their physical properties. Nuclear magnetic resonance (NMR) spectroscopy can provide information on these different bonding environments at the atomic level.

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We began this series of investigations with a ¹⁰B and ¹¹B NMR study of elemental boron [7], which has interesting properties of its own and also provides insight into boron-rich metal boride phases. This was followed by ¹¹B studies of ReB₂ [8] and WB₂ [9]. The experimental NMR details are discussed in depth in these studies. In particular, the ¹¹B quadrupolar frequencies, v_Q , at 275 kHz for ReB₂ and even less for WB₂, are small enough [9] for the radio frequency (RF) pulse to excite the full ¹¹B resonance, including the satellite transitions. Such considerations are important in spin–lattice relaxation measurements. In conductors such as the metal borides, the spin–lattice relaxation rate provides information on the density of states at the Fermi level.

We now report the results of our investigation of aluminum diboride, AlB₂. The structural motif of AlB₂ differs from that of ReB₂ and WB₂. In the AlB₂ type [10] structure, the layers of boron atoms form flat hexagonal rings. The boron layers are separated by planes of metal atoms in which the metal atoms are located between the centers of two hexagonal boron rings. Each metal atom interacts with six boron atoms in the boron plane above the metal atom and with six boron atoms in the boron plane below the metal atom.

Aluminum diboride further differs from ReB₂ in that both the metal and the boron atoms are easily amenable to study by NMR. Several NMR investigations of AlB₂ have been previously reported [11–18]. However, while there is but a single aluminum site [10] in AlB₂, the literature for AlB₂ shows spectra with a single ²⁷Al NMR resonance, but at three different reported shifts of 1640 ppm [12], 880 ppm [13, 15, 17], and 100 ppm [18]. In general, there has been more agreement among the various studies for the ¹¹B shift.

Along with the issue of the observed ²⁷Al shifts reported for AlB₂, the present study also takes an indepth look at the nature of the nuclear spin–lattice relaxation recovery data for the quadrupolar nuclei in this compound. Specifically with regard to the experimental NMR parameters, the larger ¹¹B quadrupolar frequency, v_Q , at 540 kHz in AlB₂ prevents the RF pulse from fully exciting the entire ¹¹B resonance. Remarkably, the ¹¹B spin–lattice relaxation data from a single-pulse saturation experiment were better fit with the "slow irradiation" model rather than the "fast irradiation" model. Obtaining the characteristic spin–lattice relaxation time under these experimental conditions has been examined with various pulse techniques on both static samples and samples studied with magic-angle spinning (MAS).

Experimental

Aluminum diboride, AlB₂, was first synthesized from the elements, amorphous boron (Strem, USA) and aluminum powder (Strem, USA), using an electric arc furnace in a manner similar to that previously described for ReB₂ [8]. A second sample was prepared in a tube furnace reaction using aluminum metal powder (Strem, USA) and amorphous boron (Strem, USA) sealed in a quartz ampule, with a slight excess of boron (nominally AlB_{2.2}). The ampule was placed in the tube furnace, heated to 910 °C, and held at this temperature for 12 h before cooling back to ambient temperature. A third sample of AlB₂, commercially available, was purchased from Sigma-Aldrich. The synthetic preparation of the commercial sample differs from our preparations, involving a reaction between aluminum metal and boron trioxide $(B_2O_3).$

The first sample produced via arc melting contained a slight excess of boron (AlB_{2.3}), and the sample was flipped and re-arced to promote homogeneity. The samples were ground to fine powders in a Plattner-style mortar and pestle and washed with dilute HCl to remove any iron contamination introduced during grinding. Utilizing powder X-ray diffraction (pXRD), with an X'Pert Pro diffractometer PANalytical (Netherlands), the arc-melted sample was found to contain aluminum diboride (AlB₂), significant aluminum metal, and other boron-rich aluminum boride phases (AlB₁₂, AlB₃₁). These results suggest incomplete mixing/reaction between the elements during the arc-melting process.

The second sample produced in the tube furnace reaction underwent pXRD analysis, which indicated phase-pure AlB₂, with smaller amounts of aluminum metal and Al₂O₃. The observed aluminum oxide may arise from surface oxidation of the aluminum metal.

The commercially available sample was analyzed using pXRD, and showed phase-pure AlB_2 , with both aluminum metal and aluminum oxide (Al_2O_3) . In this case, some of the aluminum oxide may correlate with the synthesis method used commercially (i.e., reacting aluminum metal with B_2O_3). This would be in

addition to the aluminum oxide arising from the aluminum metal surface. For experimental purposes, the tube furnace AlB_2 product is most similar to the Sigma-Aldrich sample. All the pXRD spectra are shown in Fig. 1. It should also be noted that ²⁷Al NMR spectra [14, 17, 18] previously in the literature for AlB_2 indicate the presence of significant aluminum metal in the samples. Due to the presence of aluminum metal in all of these samples (including the literature reports), there was interest in comparing the spectra of the products from different preparations.

The NMR data were acquired with a Bruker DSX-300 spectrometer using both magic-angle spinning (MAS) and wideline techniques. Nuclei observed included ¹¹B at a frequency of 96.29 MHz, ²³Na at 79.39 MHz, ²⁷Al at 78.20 MHz, and ²⁰⁷Pb at 62.79 MHz. The NMR samples were ground to – 325 mesh (< 44 μ m) to minimize radio frequency (RF) skin-depth effects. Due to the conductivity [11] of AlB₂ (reported to be "not very different, and perhaps even greater, than that of aluminum metal (skin depth = 19 μ m at 20 °C"), each sample was also mixed with an equal volume of NaCl to reduce particle-to-particle contact. The mixing with NaCl provided significant improvements in both the tuning of the NMR probes and in achieving higher MAS sample spinning rates. For sample temperature measurements [19–21], one AlB₂ sample was mixed with an equal volume of NaCl.



Figure 1 X-ray diffractograms for experimentally produced AlB_2 samples (top 3 spectra): arc melted (red), flux growth (green), and Strem chemical (blue); the bottom line patterns are JCPDS references for AlB_2 03-065-3381 (red) and AlB_{12} 00-012-0640 (blue). The arc-melted sample (top red) contained predominantly

 AlB_2 and AlB_{12} , but also contained aluminum metal and higher boride species (e.g., AlB_{66}). The flux grown sample (blue) contained trace amounts of aluminum metal; the commercially available sample contained traces of aluminum oxide, residual from the synthetic process.



MAS spectra of the aluminum diboride powder mixed with either NaCl or PbNO₃ were acquired with a standard Bruker MAS probe using a 4-mm outside diameter zirconia rotor with a sample spinning rate of either 5 or 12.3 kHz. The ¹¹B $\pi/2$ pulse width for the MAS experiments was 5 μ s as measured on an aqueous solution of boric acid. The ¹¹B background from the boron nitride stator in the MAS probe was minimized by the use of the Elimination of Artifacts in NMR SpectroscopY (EASY) pulse sequence [22]. The ²⁷Al $\pi/2$ pulse width was 9 μ s as measured on an aqueous solution of AlCl₃. The ²³Na $\pi/2$ pulse width was 3 μ s as measured on an aqueous solution of AlCl₃. The ²³Na $\pi/2$ pulse width was 9 μ s.

A static sample of the aluminum diboride powder mixed with NaCl was placed in a standard Bruker X-nucleus wideline probe with a 5-mm solenoid coil with the sample confined to the length of the RF coil. The use of a polyimide coil support and a quartz sample tube removed any ¹¹B background that might arise from the presence of sodium borosilicate glass. The ¹¹B $\pi/2$ pulse width was 5 µs as measured with an aqueous boric acid standard. For both the MAS and wideline probes, the "solid-state" 90-*degree* pulse width was reduced by a factor of ($I + \frac{1}{2}$), where *I* is the nuclear spin, in comparison with the 90-*degree* pulse width for the same nucleus measured in solution [23, 24].

The NMR spectral data were acquired by either single-pulse (with a dead time of 8.5 µs) or a quadrupolar echo sequence [25] with an interpulse spacing, τ , of 15 µs. The ¹¹B NMR spectra were acquired with a delay of five times the spin-lattice relaxation time (T_1) as determined by a saturationrecovery technique [26]. In the various ¹¹B saturationrecovery experiments, three different saturation methods were used. These included either a singlesaturation or а pulse pulse sequence $(p3_x - 130 \ \mu s - p3_y - 150 \ \mu s - p3_{-x} - 141 \ \mu s$ $p3_{-\nu} - 137 \mu s$ -) repeated 125 times for a total of 500 RF pulses (p3) applied. The RF pulse p3 was 4.25 µs, a value experimentally determined by minimizing the remaining signal 100 µs after the saturation pulse

sequence. The intervening times between the p3 pulses in the saturation sequence are chosen to be longer than the time for the NMR signal to dephase into the noise of the baseline after a single pulse. For the ¹¹B saturation-recovery experiment with MAS at a rate of 5 kHz, the method of pulsing asynchronously

to the sample spinning given by Yesinowski [27] was used.

The ¹¹B chemical shift scale was calibrated using the unified Ξ scale [28], relating the nuclear shift to the ¹H resonance of dilute tetramethylsilane in CDCl₃ at a frequency of 300.13 MHz. The reference compound for defining zero ppm is BF₃ etherate [28]. The chemical shift referencing was experimentally verified with the ¹¹B resonance of an aqueous solution of boric acid [29] at pH 4.4.

Spectral simulations were performed with the solids simulation package ("solaguide") in the Top-Spin (Version 3.1) NMR software program from Bruker BioSpin.

The hexagonal structure of AlB₂ with space group of P6/mmm was considered in our calculations. The computed lattice constants a = b = 3.007 Å and c = 3.2744 Å are consistent with the experimental value [30]. The boron atoms locating at B (1/3, 1/6, 1/6)1/2) and B (1/6, 1/3, 1/2) form honeycomb layers that are separated by the hexagonal close-packed aluminum. The electronic structure was calculated with the full potential linearized augmented plane wave (LAPW) method implemented in WIEN2 k (v16.1) package [31]. The general gradient approximation (GGA) of Perdew et al. [32] was used for exchange-correlation potential. The converged basis corresponds to $R_{\min}K_{\max} = 7.0$, where R_{\min} is the minimum LAPW sphere radius and K_{max} is the plane wave cutoff. The first Brillouin zone was sampled with $16 \times 16 \times 12$ *k*-points.

Results and discussion

During the course of this investigation, the challenges of synthesizing metal diborides from "light" maingroup elements became apparent. One issue that arose is the relative ease with which boron-rich phases of aluminum borides can be prepared. As powder X-ray diffraction is relatively insensitive to the boron atoms, very long data acquisition times are generally required to fully identify the presence of these "light" main-group boride phases. However, these phases easily manifest themselves by magnetic resonance spectroscopy. The ¹¹B NMR spectrum of a static polycrystalline sample of such boron-rich phases is shown in Fig. 2a. The spectrum is nearly identical to the "two split lines" [33] observed in elemental boron [7], Fig. 2b. Although both the



Figure 2 ¹¹B NMR spectra of static polycrystalline samples at ambient temperature of *a* boron-rich phases AIB_{12} and AIB_{31} (bottom), *b* elemental boron (middle), and *c* commercial AIB_2 (top).

"second-order quadrupole effect" [33] and "two distinct boron sites" [34] had been proposed in the literature, this spectral effect in elemental boron was demonstrated to arise from isotropic bulk magnetic susceptibility [7]. In elemental boron, partial occupancy of unit cell sites results in defects yielding paramagnetic centers that can be observed by electron paramagnetic resonance (EPR) spectroscopy [7]. EPR spectra (not shown) were also acquired on these boron-rich phases and are nearly identical to those of elemental boron [7].

This point of the relative ease of formation of boron-rich metal borides with the "light" main-group element of aluminum is raised because a very similar "doublet" has been previously reported [13] for MgB₂ and interpreted as a "dipolar doublet." If such a "doublet" arises from isotropic bulk magnetic susceptibility, as in the cases of elemental boron and the boron-rich aluminum boride phases, then the splitting will be dependent upon the particle size [7]. In addition, the sample will yield a measurable EPR spectrum. Such issues as these might provide an alternative explanation for the doublet structure in the MgB₂ spectrum. This will be pursued in a separate publication.

²⁷Al NMR highlights another synthetic challenge with AlB₂. Figure 3 shows the ²⁷Al MAS spectrum of



Figure 3 27 Al MAS spectrum of a commercial AlB₂ sample from Sigma-Aldrich.

the commercial AlB₂ sample from Sigma-Aldrich that contains three resonances. As mentioned in the "Introduction," the literature for AlB₂ reports three different ²⁷Al shifts at 1640 ppm [12], 880 ppm [13, 15, 17], and 100 ppm [18]. Despite its assignment as the resonance for AlB₂ in Ref. [12], the peak around 1680 ppm, showing spinning sidebands, has been identified as the Knight shift for aluminum metal [35, 36]. The assignment of this peak as attributed to aluminum metal has been experimentally confirmed by the addition of aluminum powder to the sample [14] and is in agreement with the results found here. The peak around 880 ppm, which does not narrow under MAS, is consistent with that assigned as AlB₂ in several studies [13–15, 17]. The peak around 0 ppm could rise from aluminum oxide, presumably from the surface of the aluminum metal particles and from aluminum metal reacting with boron trioxide.

This resonance around 0 ppm differs somewhat in shift from the lone report [18] of 100 ppm as the assignment for the ²⁷Al resonance for AlB₂. However, there is a possible explanation for the observation of a ²⁷Al shift for AlB₂ differing from the numerous reports of a resonance around 880 ppm. X-ray diffraction data and density measurements in previous studies [16, 37] have indicated an Al deficiency in AlB₂. Loa et al. [37] have calculated the band structure and density of states for stoichiometric AlB₂. The π -type bands derived from the boron p_z states and bands with Al-s character are partially filled. Based on the rigid-band picture they argued that AlB₂ with a 10% Al deficiency (e.g., Al_{0.9}B₂) would result in a

removal of 0.3 Al valence electrons, which is sufficient to greatly deplete the number of electrons in the band of Al-*s* states.

To verify this picture, we have carried out a calculation for the $2 \times 2 \times 2$ superstructure of AlB₂ with central Al atom removed, which effectively corresponds to AlB₂ with 12.5% aluminum deficiency, i.e., Al_{0.85}B₂. After fully relaxing the internal coordinates of every atom, we calculated the electronic structure and show it in Fig. 4. We found that the 12.5% aluminum deficiency completely removes the electron pocket around Γ (Fig. 4b) as claimed in Ref. [37]. However, in contrast to the statement on the complete depletion of the Al-*s* band, we found reasonable amount of bands with Al-*s* character around the Fermi level that are mainly contributed from the H point (Fig. 4a). As a result of the diminished but not complete depletion of the Al-



Figure 4 Electronic structure and density of states (DOS) of **a** AlB₂ and **b** Al_{0.85}B₂. The orbital projections of Al and B in single AlB₂ unit cell are displayed as circles in (**a**). 12.5% aluminum deficiency in (**b**) is effectively simulated by removing

one Al from the $2 \times 2 \times 2$ superstructure of AlB₂. At the left- and right-hand sides of (**b**) the comparison of the atomic- and orbital-resolved DOS to the rescaled total DOS are shown.

s states, a reduction of the 27 Al Knight shift would be expected. The observed 27 Al shift (Fig. 3) may be dependent upon the aluminum deficiency.

The ²⁷Al MAS spectrum in Fig. 3 was acquired using a single pulse of 0.5 µs in order to provide as quantitative a spectrum as possible [23, 24]. Integration of the spectrum indicates that about 28% of the aluminum atoms are present as aluminum metal and about 67% present as AlB₂. The remaining 5% of the aluminum atoms are present as the oxide. Very similar results were obtained from the AlB₂ sample prepared by the tube furnace method. It should also be noted that the ²⁷Al spectra given in Refs. 14, 17 and 18 all show a significant aluminum metal resonance in addition to that assigned to AlB₂. As can be inferred from these data from these different samples, preparing AlB₂ completely free of aluminum metal is difficult. The inclusion of aluminum metal within the AlB₂ samples makes it difficult to easily identify the metal boride phase by X-ray powder diffraction in such "light" main-group metal borides. As noted above, ¹¹B NMR and EPR spectra can be useful in indicating the presence of boron-rich metal boride phases in the sample.

The ¹¹B and ²⁷Al NMR spectral parameters for AlB₂ are given in Table 1. Figure 5 shows the fit of a shielding anisotropy model to the ¹¹B experimental data. As was previously assumed [16] for ¹¹B in



Figure 5 Experimental ¹¹B spectrum of a static sample of AlB_2 is shown in blue. The smooth redline is a simulated fit of a shielding anisotropy model. The extracted parameters are given in Table 1.

Al_{0.9}B₂, the two principal axis systems for the quadrupolar interaction and for the shielding anisotropy are coincident for ¹¹B in AlB₂. The parameters for the quadrupolar interaction were determined from the Variable Offset Cumulative Spectra (VOCS) [38] shown in Fig. 6.

The ¹¹B VOCS spectrum in Fig. 6 allows the ¹¹B quadrupolar frequency to be determined directly from the observed spectral satellites in this first-order quadrupolar spectrum. Using this experimental

Table 1 ²⁷Al and ¹¹B NMR quadrupolar and shielding parameters of AlB₂

	$\delta_{\rm iso}$, ^{a,b} (ppm)	C_Q^c (MHz)	$v_Q^d \; (\text{MHz})$	$\eta_{ m q}^{ m e}$	$\delta^{\rm b}_{11}$ (ppm)	$\delta^{\rm b}_{22}$ (ppm)	$\delta^{\rm b}_{33}$ (ppm)	$\zeta_{\rm csa}^{\rm f}$ (ppm)	$\eta_{ m s}^{ m g}$	$\Omega^{\rm h}$ (ppm)	κ^{i}
$Al^{11}B_2$ static $Al^{11}B_2$ MAS	- 6.0 - 7.7	1.10	0.550	0	138.5	- 78.3	- 78.3	145	0	217	- 1
²⁷ AlB ₂	880	0.533 ^j	0.080 ^j								

"Spectral parameters obtained from simulations in Fig. 4 bShifts referenced to the unified Ξ scale [28]

Sints referenced to the diffied E scale [20

^cQuadrupolar coupling constant { e^2qQ/\hbar } ^dQuadrupolar frequency { $3e^2qQ/[2I(2I - 1)\hbar]$ } ^e η = asymmetry { $0 \le \eta \le 1$ } ^f $\zeta_{csa} = \delta_{33} - \delta_{iso}$ ^g $\eta = (\delta_{22} - \delta_{11})/\zeta_{csa}$ ^h $\Omega = |\delta_{33} - \delta_{11}|$ ⁱ $\kappa = 3(\delta_{22} - \delta_{iso})/\Omega$

^jFrom Ref. 13

6000

4000



0

ppm

-2000

-4000

Figure 6 Partial ¹¹B VOCS result for the central and highfrequency satellite transition is shown on the bottom. These spectra were acquired with a quadrupolar echo sequence. The ¹¹B spectrum shown on the top was acquired with a single-pulse acquisition using a dead time of 8.5 μ s. The resulting roll in the baseline of the spectrum has been corrected.

2000

value of the quadrupolar frequency, the second-order quadrupolar contribution, with a spectral width of ca. 15 ppm, to the observed central transition lineshape shown in Fig. 5 is almost negligible compared to the full width of the central transition. This observed lineshape and linewidth of the central transition are dominated by the shielding anisotropy, the fit of which is shown in Fig. 5. In this simulation, the second-order quadrupolar interaction in essence provides the broadening function used in the simulation of the shielding anisotropy. These results are in agreement with those previously reported in Ref. 16.

NMR measurements of the spin–lattice relaxation rate provide a probe at the atomic level that yields information on the Fermi surface. For the spin–lattice relaxation of a half-integer quadrupolar nuclei in a non-cubic singe crystal, Andrew and Tunstall [39] showed that relaxation recovery is typically characterized by a multi-exponential function regardless of whether the relaxation mechanism is quadrupolar or magnetic in origin. The derivation assumed that there are no accidental degeneracies of the satellite energy levels with that of the central transition resulting from the crystal orientation in the static magnetic field. The multi-exponential recovery arises from the quadrupolar interaction creating unequal energy spacings in the Zeeman interaction.

The Andrew and Tunstall [39] model for saturation-recovery spin–lattice relaxation derived for magnetic relaxation of spin-3/2 nuclei with selective saturation of the central transition is given by the following equation:

$$\frac{M(\infty) - M(t)}{M(\infty)} = \left(0.4e^{-\frac{t}{T_1}} + 0.6e^{-6\frac{t}{T_1}}\right) \tag{1}$$

However, the equation that is typically fit to the experimental data "for the case of saturation of the central line of the ¹¹B NMR spectrum with a single rf pulse (or short sequence of pulses and for magnetic relaxation mechanism"¹¹ (*cf.*, Refs. 13, 14, 40 and 41) has different coefficients for the two exponential functions

$$\frac{M(\infty) - M(t)}{M(\infty)} = \left(0.1e^{-\frac{t}{T_1}} + 0.9e^{-6\frac{t}{T_1}}\right)$$
(2)

from those found in the Andrew and Tunstall [39] model given in Eq. (1), although the Andrew–Tunstall work is generally cited as the reference for Eq. (2). Usually, no further explanation for the differing equations is given. However, the apparent explanation depends upon the RF irradiation of the central transition [42]. Under the assumption that "the irradiation pulse(s) are chosen so that they disturb only the equilibrium of the central transition without affecting the population of the other energy levels" [42], i.e., "fast irradiation," then the saturation recovery is described by Eq. (2). However, if "the irradiation period is so long that the unperturbed levels will come to thermal equilibrium with the irradiated levels" [42], i.e., "slow irradiation," in this case the saturation recovery is described by Eq. (1). In short, the experimental details of the spin-lattice relaxation experiment are important in extracting a time constant for data analysis.

For nuclear spin-lattice relaxation experiments of half-integer quadrupolar nuclei, the radio frequency pulses that are used in the experiment need to be characterized. For the ¹¹B relaxation measurements performed with a static sample of AlB₂ in the wideline probe, the ¹¹B $\pi/2$ pulse width first was measured with an aqueous boric acid standard and determined to be 5 µs. Using the 360-degree pulse width gives a radio frequency field, $v_{\rm RF}$, of 50 kHz. In this case, the $v_{\rm RF}$ is an order of magnitude smaller than the quadrupolar frequency, $v_{\rm O}$, of 540 kHz previously reported for ¹¹B in AlB₂ [11, 13, 16]. For ¹¹B spectral acquisitions by either single-pulse or quadrupolar echo sequences ($\tau = 15 \ \mu s$), the "solidstate" 90-degree pulse width [23, 24], reduced by a factor of $(I + \frac{1}{2}) = 2$ where *I* is the nuclear spin, of 2.5 µs was used. Under these experimental conditions using a quadrupolar echo sequence, the RF pulse appears to be relatively "selective," as shown in the VOCS [38] given in Fig. 6. Specifically, RF excitation of the central transition shows no spectral intensity at the spectral singularity associated with the higher frequency satellite transition. Alternatively, RF excitation of the spectral singularity associated with the higher frequency satellite transition shows no intensity of the central transition. In comparison with the quadrupolar-echo spectra, the single-pulse spectrum acquired with a ringdown delay (or "deadtime") of 8.5 µs is shown in the top trace of Fig. 6. It should be noted that the baseline roll arising from the ringdown delay in this spectrum has been corrected. The single-pulse spectrum also suggests that the RF pulse is relatively "selective" in that the satellite transitions are not readily observed.

Although both $v_{RF} \ll v_O$ and the absence of spectral intensity of the singularity of the satellite transitions in the one-dimensional spectra when the RF is located at the central transition suggest that this experimental RF is relatively selective, this RF pulse is still able to excite nuclei much further away than the 50 kHz RF field might suggest. This effect is demonstrated with the ²⁷Al spectrum shown in Fig. 7. For the ¹¹B and ²⁷Al spectra of AlB₂ in this study, the AlB₂ samples were mixed with equal volumes of NaCl to minimize RF skin-depth issues with the conductive AlB₂, as described in the Experimental methods. With the wideline probe, the ²⁷Al $\pi/2$ pulse width was 9 µs as measured on an aqueous solution of AlCl₃. The "solid-state" 90-degree pulse width is 3 μ s as ²⁷Al is a spin-5/2 nucleus. The ²⁷Al spectrum



Figure 7 ²⁷Al NMR spectrum acquired using a pure NaCl sample with a wideline probe.

shown in Fig. 7 is from a sample of pure NaCl. The ²⁷Al signal around 0 ppm is a background signal from aluminum contained in the ceramic surrounding the RF coil in the wideline probe. In this case, ²⁷Al resonates at 78.172 MHz. The signal around 2395 ppm is an aliased ²³Na resonance from NaCl that resonates at 79.353 MHz, as evidenced by simply acquiring the same spectrum with an empty probe. In this case, the spectral width is 1 MHz, acquired with the shortest available dwell time of 0.5 µs. No filtering, either electronically or digitally, was used in the acquisition of the time domain signal. The ²³Na signal is aliased in from the right-hand side of the spectrum. The frequency range excited by a square RF pulse can be approximated by the Fourier transformation of a square, i.e., a sinc function [43]. The bandwidth for this frequency distribution is 1.2/(pulse width) Hz [43]. The "solid-state" 90-degree pulse width of 3 µs has a bandwidth of 0.4 MHz. However, excitation of the ²³Na resonance 1.166 MHz away from the ²⁷Al resonance occurs, as shown in Fig. 7. It should be noted that the bandwidth as given by the Fourier transformation takes into account only the pulse width (and not the RF power). As such, this bandwidth will differ from that of the radio frequency field, v_{RF} , which is based on the 360-degree pulse width. This ability to affect nuclear spins beyond the expected bandwidth comes into play in the measurement of ¹¹B spin–lattice relaxation times.

As noted above, the RF pulses can excite nuclei well beyond the expected bandwidth, although this may not be immediately evident in the one-dimensional spectra. This effect manifests itself in the ¹¹B saturation-recovery data shown in Fig. 8. Data sets for three different ¹¹B saturation-recovery experiments obtained from the Sigma-Aldrich AlB₂ are shown. The relaxation data sets in Fig. 8 show data covering variable delays spanning five orders of magnitude.

The first data set in Fig. 8 is from a saturation-recovery experiment using a single pulse of 4.5 μ s for saturation of a static sample of AlB₂. As can be seen, the experimental data are much better fit by the Andrew and Tunstall [39] model given in Eq. (1) rather than that by the "fast irradiation" model for a single pulse given in Eq. (2). The second experimental data set is also for a static sample. However, instead of a single RF pulse for saturation, a pulse train pulse of $(p3_x - 130 \ \mu s - p3_y - 150 \ \mu s - p3_{-x} - 141 \ \mu s - p3_{-y} - 137 \ \mu s -)$ repeated 125 times





Figure 8 ¹¹B NMR saturation-recovery spin–lattice relaxation data obtained from a single-pulse saturation (blue circles), a 500-pulse saturation train (black squares) and Yesinowski's [27] MAS technique. For the single-pulse saturation, the data have been fitted with both the slow irradiation (Andrew–Tunstall) and fast irradiation models (see text for discussion).

for a total of 500 RF pulses (p3) was applied. The third experimental data set was acquired with the technique of Yesinowski [27] using MAS at 5 kHz. In this MAS technique for measuring the spin–lattice relaxation time, a train of saturation pulses is applied asynchronously to the MAS in order to use the overlapping of the satellite and central transitions during the sample rotation so that both central and satellite transitions are saturated. It should be noted that all three techniques significantly saturate the ¹¹B magnetization. This is in contrast to the ¹¹B saturation-recovery experiments for ReB₂ [8] in which approximately 8% of the ¹¹B magnetization remained after applying the saturation technique.

Applying the models to the various data sets in Fig. 8 with delays spanning five orders of magnitude can yield time constants from the fits that differ significantly from each other. It should also be noted that the first two data sets cannot be well fit with a single exponential function. For the first data set shown in Fig. 8, the recovery data are obtained with a single saturation pulse of 4.5 μ s, a value experimentally determined by minimizing the remaining signal 100 μ s after the saturation pulse. In contrast to "the case of saturation of the central line of the ¹¹B NMR spectrum with a single rf pulse (or short sequence of pulses and for magnetic relaxation mechanism" [13], Eq. (2) does not fit the experimental data nearly as

well as the Andrew and Tunstall [39] model given by Eq. (1). The Andrew–Tunstall model yields a T_1 of 6.8 s. However, the "fast irradiation" [42] of Eq. (2) is primarily composed of the exponential with a time constant of $T_1/6$. As a result, the (poorer) fit of Eq. (2) to the experimental data yields a significantly longer T_1 of 11.1 s. The important point is that the choice of mathematical model significantly affects the extracted time constant. In this case, the difference is almost a factor of two. The better fit of the Andrew-Tunstall model to the experimental data over that of the "fast irradiation" model suggests that the single RF pulse used for saturation affected the population of the other energy levels [42] rather than simply those of the central transition. Such a result is consistent with the observed fact that RF pulses used in this study excited nuclei well beyond the "RF field" or "RF bandwidth" determined from Fourier transform theory. The appropriate initial populations of the central and satellite transitions for application of the "fast irradiation" model are not created by the RF pulse used in the saturation-recovery experiment. As a result, an erroneous time constant is extracted.

This excitation effect of the RF pulses is further illustrated in the data set obtained using a saturation pulse train pulse of $(p3_x - 130 \mu s - p3_y - 150 \mu s$ $p_{3_{-x}} - 141 \ \mu s - p_{3_{-y}} - 137 \ \mu s$ -) repeated 125 times for a total of 500 RF pulses (p3). The spin-lattice saturation recovery as shown in Fig. 8 obviously takes longer than that for the application of a single RF pulse. Fitting this data set with a single exponential function with a time constant of T_1 yields a time constant of 4.3 s. That is, the application of multiple pulses for saturation is beginning to saturate the satellite transitions. For the case of full saturation of the central transition and the satellite transitions, a saturation recovery characterized by a single exponential function would be expected [8, 27]. The T_1 of 4.3 s form the pulse train saturation is shorter than the 6.8 s obtained from fitting the Andrew-Tunstall model to the single-pulse saturation data. This pulse sequence does not fully saturate the satellite transitions. As a result, the extracted time constant is not correct.

Finally, for comparison, fitting the saturation-recovery data acquired with the technique of Yesinowski [27] using MAS at 5 kHz with a single exponential function gives a T_1 of 5.5 s. The effects of spinning a conductive sample in a magnetic field, including both heating and braking, have been previously studied for CuI [44]. To check for these effects, the – 325 mesh AlB₂ sample was also mixed with an equal volume of PbNO₃. Monitoring of the ²⁰⁷Pb chemical shift [19–21] at a MAS spinning rate of 5 kHz indicated only a modest 3.6 K increase in sample temperature over that of the static sample. This is the small temperature increase expected from frictional heating of the sample under MAS at this spinning rate. With the small particles dispersed in the PbNO₃, there is no experimental evidence of sample heating due to the conductivity nor is there any evidence from the drive gas pressure required of any magnetic braking effect.

The ²⁷Al spin-lattice relaxation times were measured with a saturation-recovery experiment using a static sample. The comparatively small value of v_{O} of 80 kHz for aluminum in AlB₂ [13] means that the full ²⁷Al resonance, including satellite transitions, can be saturated with the radio frequency pulse. As a result, the saturation-recovery data are characterized by a single exponential function. At 294 K, the measured ²⁷Al spin–lattice relaxation time was 13 ms and ranged from 35 ms at 148 K to 8 ms at 423 K. The relaxation data as a function of temperature yield a Korringa product of $(T_1 * T) = 4.1$ sK. By using the spectral shift of 880 ppm, the Korringa ratio was estimated to be $R = \frac{K^2 T_1 T}{S} = 0.82$ where S = $(\gamma_e/\gamma_n)^2 (h/8\pi^2 k_B)$ for ²⁷Al nucleus. The obtained ratio is close to unity suggesting that the nuclear spinlattice relaxation mechanism can be described by the contribution of s-type carriers. However, based on our theoretical calculations both *s* and *p* states coexist at the Fermi level almost in an equal amount $[N_s^{Al}(E_F) = 0.058 \text{ states/eV f.u. and } N_p^{Al}(E_F) = 0.043$ states/eV f.u.] which can explain the value of the Korringa ratio to be closer to unity but less than it. This interesting result reveals the high sensitivity of the NMR parameters on both the total and partial DOS at the E_F . Applying now the same analysis on the ¹¹B relaxation data, the Korringa ratio found to be very small 0.023 that experimentally verifies the primacy of the p electrons at the partial DOS of boron sites in AlB₂ $[N_n^B(E_F) = 0.330$ states/eV f.u.]. The estimated orbital and Fermi-contact contributions in both nuclei are in conformity with the ab initio calculations as predicted for the partial density of states at the E_F for ²⁷Al $N_s^{Al}(E_F) = 0.058$ states/eV f.u. and

Table 2	Total	and Al	and B	partial	DOS	at t	the	Fermi	level	in
units of	states/e	eV f.u.	for AlE	B_2						

Alloy	$N_s (E_F)$	$N_{p_z} (E_F)$	$N_{p_{xy}} (E_F)$
Pure AlB ₂ total	0.062	0.339	0.034
В	0.004	0.324	0.006
Al	0.058	0.015	0.028
Al-deficient AlB ₂ total	0.026	0.039	0.016
В	0.002	0.031	0.001
Al	0.024	0.008	0.015

for ¹¹B $N_s^B(E_F) = 0.004$ states/eV f.u. (see Fig. 4 and Table 2).

The ²⁷Al spin-lattice relaxation rate was also measured for aluminum metal by using the resonance at 1680 ppm. The face-centered cubic aluminum lattice [45] requires the quadrupolar interactions to vanish by symmetry. As a result, the saturation-recovery data of aluminum metal are also characterized by a single exponential function. At 294 K, the measured ²⁷Al spin-lattice relaxation time was 2.4 ms, which may be compared with the reported [46] 6 ms measured at ambient temperature at a frequency of 16 MHz. The measured ²⁷Al spinlattice relaxation times ranged from 5.6 ms at 148 K to 1.6 ms at 423 K. The relaxation data as a function of temperature yield a product of $(T_1 * T) = 0.84$ sK, which is smaller than the previously reported [45] value of 1.85 sK.

For completeness to further illustrate spin-lattice relaxation behavior for quadrupolar nuclei, as ²³Na is similar to ¹¹B in being a spin-3/2 quadrupolar nucleus, the ²³Na spin–lattice relaxation for NaCl was also characterized. Sodium chloride crystallizes in a face-centered cubic lattice, with each ion surrounded by an octahedron of the oppositely charged ion. As a result of the cubic symmetry, the static quadrupolar interaction is zero. The ²³Na spin–lattice relaxation in a single crystal [47] was previously investigated at frequencies of 4.5 MHz and 12 MHz. Relaxation time constants, T₁, of 12 s at 298 K, 14.5 s at 273 K, and 28 s at 195 K were reported, which established the relaxation mechanism as quadrupolar (rather than magnetic) with van Kranendonk's theory [48]. Additionally, the study was specifically able to rule out the role of paramagnetic centers as playing a role in the nuclear spin relaxation. No dependence of T_1 upon crystal orientation with respect to the magnetic field was observed. In our experiments, the ²³Na



saturation-recovery data for a static sample of polycrystalline NaCl at 295 K measured at 79.39 MHz were well fit with a single exponential function that yielded a T_1 of 14.4 s. An inversion-recovery experiment, also well fit by a single exponential function, yielded a T_1 of 13.9 s. Finally, a fit of a single exponential function to the ²³Na inversion-recovery data for the same sample of polycrystalline NaCl at 295 K undergoing MAS yielded a T_1 of 14.1 s. As expected, with cubic symmetry such that only the central transition is observed, MAS does not change the ²³Na T_1 . For the static sample, the full width at half maximum is 2.78 kHz while the MAS spectrum gives a narrowed resonance with a full width at half maximum of 38 Hz.

Conclusions

For pure and Al-deficient AlB₂, ab initio calculations and NMR parameters characterizing both the density of states at the Fermi level, the electric field gradient and the shielding at both the boron and aluminum sites are presented. Band structure results reveal that aluminum deficiency completely removes the electron pocket around Γ of the band structure. However, in contrast to previous calculations, we found that a reasonable amount of bands with Al-s character around the Fermi level remain and mainly contribute from the H point. To verify this picture, ¹¹B and ²⁷Al spectral analysis and nuclear spin-lattice relaxation experiments were carried out for all samples with various pulse techniques. Characterization of the radio frequency pulses used in the relaxation measurements indicates that nutation frequencies are small in comparison with the quadrupolar interaction at the ¹¹B site. Interestingly, in contrast to expectations, the ¹¹B spin–lattice relaxation data from a single-pulse saturation experiment were better fit with the "slow irradiation" model rather than the "fast irradiation" model.

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