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Aubert, B
Bona, M
Boutigny, D
et al.

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Measurements of Partial Branching Fractions for $\bar{B} \rightarrow X_u l \bar{\nu}$ and Determination of $|V_{ub}|$

B. Aubert,¹ M. Bona,¹ D. Boutigny,¹ Y. Karyotakis,¹ J. P. Lees,¹ V. Poireau,¹ X. Prudent,¹ V. Tisserand,¹ A. Zghiche,¹ J. Garra Tico,² E. Grauges,² L. Lopez,³ A. Palano,³ M. Pappagallo,³ G. Eigen,⁴ B. Stugu,⁴ L. Sun,⁴ G. S. Abrams,⁵ M. Battaglia,⁵ D. N. Brown,⁵ J. Button-Shafer,⁵ R. N. Cahn,⁵ Y. Groysman,⁵ R. G. Jacobsen,⁵ J. A. Kadyk,⁵ L. T. Kerth,⁵ Yu. G. Kolomensky,⁵ G. Kukartsev,⁵ D. Lopes Pegna,⁵ G. Lynch,⁵ L. M. Mir,⁵ T. J. Orimoto,⁵ I. L. Osipenkov,⁵ M. T. Ronan,^{5,*} K. Tackmann,⁵ T. Tanabe,⁵ W. A. Wenzel,⁵ P. del Amo Sanchez,⁶ C. M. Hawkes,⁶ A. T. Watson,⁶ H. Koch,⁷ T. Schroeder,⁷ D. Walker,⁸ D. J. Asgeirsson,⁹ T. Cuhadar-Donszelmann,⁹ B. G. Fulsom,⁹ C. Hearty,⁹ T. S. Mattison,⁹ J. A. McKenna,⁹ M. Barrett,¹⁰ A. Khan,¹⁰ M. Saleem,¹⁰ L. Teodorescu,¹⁰ V. E. Blinov,¹¹ A. D. Bukin,¹¹ V. P. Druzhinin,¹¹ V. B. Golubev,¹¹ A. P. Onuchin,¹¹ S. I. Serednyakov,¹¹ Yu. I. Skovpen,¹¹ E. P. Solodov,¹¹ K. Yu. Todyshev,¹¹ M. Bondioli,¹² S. Curry,¹² I. Eschrich,¹² D. Kirkby,¹² A. J. Lankford,¹² P. Lund,¹² M. Mandelkern,¹² E. C. Martin,¹² D. P. Stoker,¹² S. Abachi,¹³ C. Buchanan,¹³ S. D. Foulkes,¹⁴ J. W. Gary,¹⁴ F. Liu,¹⁴ O. Long,¹⁴ B. C. Shen,¹⁴ G. M. Vitug,¹⁴ L. Zhang,¹⁴ H. P. Paar,¹⁵ S. Rahatlou,¹⁵ V. Sharma,¹⁵ J. W. Berryhill,¹⁶ C. Campagnari,¹⁶ A. Cunha,¹⁶ B. Dahmes,¹⁶ T. M. Hong,¹⁶ D. Kovalskyi,¹⁶ J. D. Richman,¹⁶ T. W. Beck,¹⁷ A. M. Eisner,¹⁷ C. J. Flacco,¹⁷ C. A. Heusch,¹⁷ J. Kroseberg,¹⁷ W. S. Lockman,¹⁷ T. Schalk,¹⁷ B. A. Schumm,¹⁷ A. Seiden,¹⁷ M. G. Wilson,¹⁷ L. O. Winstrom,¹⁷ E. Chen,¹⁸ C. H. Cheng,¹⁸ F. Fang,¹⁸ D. G. Hitlin,¹⁸ I. Narsky,¹⁸ T. Piatenko,¹⁸ F. C. Porter,¹⁸ R. Andreassen,¹⁹ G. Mancinelli,¹⁹ B. T. Meadows,¹⁹ K. Mishra,¹⁹ M. D. Sokoloff,¹⁹ F. Blanc,²⁰ P. C. Bloom,²⁰ S. Chen,²⁰ W. T. Ford,²⁰ J. F. Hirschauer,²⁰ A. Kreisel,²⁰ M. Nagel,²⁰ U. Nauenberg,²⁰ A. Olivas,²⁰ J. G. Smith,²⁰ K. A. Ulmer,²⁰ S. R. Wagner,²⁰ J. Zhang,²⁰ A. M. Gabareen,²¹ A. Soffer,^{21,†} W. H. Toki,²¹ R. J. Wilson,²¹ F. Winklmeier,²¹ D. D. Altenburg,²² E. Feltresi,²² A. Hauke,²² H. Jasper,²² J. Merkel,²² A. Petzold,²² B. Spaan,²² K. Wacker,²² V. Klose,²³ M. J. Kobel,²³ H. M. Lacker,²³ W. F. Mader,²³ R. Nogowski,²³ J. Schubert,²³ K. R. Schubert,²³ R. Schwierz,²³ J. E. Sundermann,²³ A. Volk,²³ D. Bernard,²⁴ G. R. Bonneaud,²⁴ E. Latour,²⁴ V. Lombardo,²⁴ Ch. Thiebaut,²⁴ M. Verderi,²⁴ P. J. Clark,²⁵ W. Gradl,²⁵ F. Muheim,²⁵ S. Playfer,²⁵ A. I. Robertson,²⁵ J. E. Watson,²⁵ Y. Xie,²⁵ M. Andreotti,²⁶ D. Bettoni,²⁶ C. Bozzi,²⁶ R. Calabrese,²⁶ A. Cecchi,²⁶ G. Cibinetto,²⁶ P. Franchini,²⁶ E. Luppi,²⁶ M. Negrini,²⁶ A. Petrella,²⁶ L. Piemontese,²⁶ E. Prencipe,²⁶ V. Santoro,²⁶ F. Anulli,²⁷ R. Baldini-Ferrolì,²⁷ A. Calcaterra,²⁷ R. de Sangro,²⁷ G. Finocchiaro,²⁷ S. Pacetti,²⁷ P. Patteri,²⁷ I. M. Peruzzi,^{27,‡} M. Piccolo,²⁷ M. Rama,²⁷ A. Zallo,²⁷ A. Buzzo,²⁸ R. Contri,²⁸ M. Lo Vetere,²⁸ M. M. Macri,²⁸ M. R. Monge,²⁸ S. Passaggio,²⁸ C. Patrignani,²⁸ E. Robutti,²⁸ A. Santroni,²⁸ S. Tosi,²⁸ K. S. Chaisanguanthum,²⁹ M. Morii,²⁹ J. Wu,²⁹ R. S. Dubitzky,³⁰ J. Marks,³⁰ S. Schenk,³⁰ U. Uwer,³⁰ D. J. Bard,³¹ P. D. Dauncey,³¹ R. L. Flack,³¹ J. A. Nash,³¹ W. Panduro Vazquez,³¹ M. Tibbetts,³¹ P. K. Behera,³² X. Chai,³² M. J. Charles,³² U. Mallik,³² J. Cochran,³³ H. B. Crawley,³³ L. Dong,³³ V. Eyges,³³ W. T. Meyer,³³ S. Prell,³³ E. I. Rosenberg,³³ A. E. Rubin,³³ Y. Y. Gao,³⁴ A. V. Gritsan,³⁴ Z. J. Guo,³⁴ C. K. Lae,³⁴ A. G. Denig,³⁵ M. Fritsch,³⁵ G. Schott,³⁵ N. Arnaud,³⁶ J. Béguilleux,³⁶ A. D'Orazio,³⁶ M. Davier,³⁶ G. Grosdidier,³⁶ A. Höcker,³⁶ V. Lepeltier,³⁶ F. Le Diberder,³⁶ A. M. Lutz,³⁶ S. Pruvot,³⁶ S. Rodier,³⁶ P. Roudeau,³⁶ M. H. Schune,³⁶ J. Serrano,³⁶ V. Sordini,³⁶ A. Stocchi,³⁶ W. F. Wang,³⁶ G. Wormser,³⁶ D. J. Lange,³⁷ D. M. Wright,³⁷ I. Bingham,³⁸ J. P. Burke,³⁸ C. A. Chavez,³⁸ J. R. Fry,³⁸ E. Gabathuler,³⁸ R. Gamet,³⁸ D. E. Hutchcroft,³⁸ D. J. Payne,³⁸ K. C. Schofield,³⁸ C. Touramanis,³⁸ A. J. Bevan,³⁹ C. Clarke,³⁹ K. A. George,³⁹ F. Di Lodovico,³⁹ W. Menges,³⁹ R. Sacco,³⁹ G. Cowan,⁴⁰ H. U. Flaecher,⁴⁰ D. A. Hopkins,⁴⁰ S. Paramesvaran,⁴⁰ F. Salvatore,⁴⁰ A. C. Wren,⁴⁰ D. N. Brown,⁴¹ C. L. Davis,⁴¹ J. Allison,⁴² D. Bailey,⁴² N. R. Barlow,⁴² R. J. Barlow,⁴² Y. M. Chia,⁴² C. L. Edgar,⁴² G. D. Lafferty,⁴² T. J. West,⁴² J. I. Yi,⁴² J. Anderson,⁴³ C. Chen,⁴³ A. Jawahery,⁴³ D. A. Roberts,⁴³ G. Simi,⁴³ J. M. Tuggle,⁴³ G. Blaylock,⁴⁴ C. Dallapiccola,⁴⁴ S. S. Hertzbach,⁴⁴ X. Li,⁴⁴ T. B. Moore,⁴⁴ E. Salvati,⁴⁴ S. Saremi,⁴⁴ R. Cowan,⁴⁵ D. Dujmic,⁴⁵ P. H. Fisher,⁴⁵ K. Koeneke,⁴⁵ G. Sciolla,⁴⁵ M. Spitznagel,⁴⁵ F. Taylor,⁴⁵ R. K. Yamamoto,⁴⁵ M. Zhao,⁴⁵ Y. Zheng,⁴⁵ S. E. Mclachlin,^{46,*} P. M. Patel,⁴⁶ S. H. Robertson,⁴⁶ A. Lazzaro,⁴⁷ F. Palombo,⁴⁷ J. M. Bauer,⁴⁸ L. Cremaldi,⁴⁸ V. Eschenburg,⁴⁸ R. Godang,⁴⁸ R. Kroeger,⁴⁸ D. A. Sanders,⁴⁸ D. J. Summers,⁴⁸ H. W. Zhao,⁴⁸ S. Brunet,⁴⁹ D. Côté,⁴⁹ M. Simard,⁴⁹ P. Taras,⁴⁹ F. B. Viaud,⁴⁹ H. Nicholson,⁵⁰ G. De Nardo,⁵¹ F. Fabozzi,^{51,§} L. Lista,⁵¹ D. Monorchio,⁵¹ C. Sciacca,⁵¹ M. A. Baak,⁵² G. Raven,⁵² H. L. Snoek,⁵² C. P. Jessop,⁵³ K. J. Knoepfel,⁵³ J. M. LoSecco,⁵³ G. Benelli,⁵⁴ L. A. Corwin,⁵⁴ K. Honscheid,⁵⁴ H. Kagan,⁵⁴ R. Kass,⁵⁴ J. P. Morris,⁵⁴ A. M. Rahimi,⁵⁴ J. J. Regensburger,⁵⁴ S. J. Sekula,⁵⁴ Q. K. Wong,⁵⁴ N. L. Blount,⁵⁵ J. Brau,⁵⁵ R. Frey,⁵⁵ O. Igonkina,⁵⁵ J. A. Kolb,⁵⁵ M. Lu,⁵⁵ R. Rahmat,⁵⁵ N. B. Sinev,⁵⁵ D. Strom,⁵⁵ J. Strube,⁵⁵ E. Torrence,⁵⁵ N. Gagliardi,⁵⁶ A. Gaz,⁵⁶ M. Margoni,⁵⁶ M. Morandin,⁵⁶ A. Pompili,⁵⁶ M. Posocco,⁵⁶ M. Rotondo,⁵⁶ F. Simonetto,⁵⁶ R. Stroili,⁵⁶ C. Voci,⁵⁶ E. Ben-Haim,⁵⁷ H. Briand,⁵⁷ G. Calderini,⁵⁷ J. Chauveau,⁵⁷ P. David,⁵⁷ L. Del Buono,⁵⁷ Ch. de la Vaissière,⁵⁷ O. Hamon,⁵⁷ Ph. Leruste,⁵⁷ J. Malclès,⁵⁷ J. Ocariz,⁵⁷ A. Perez,⁵⁷ J. Prendki,⁵⁷ L. Gladney,⁵⁸ M. Biasini,⁵⁹ R. Covarelli,⁵⁹

E. Manoni,⁵⁹ C. Angelini,⁶⁰ G. Batignani,⁶⁰ S. Bettarini,⁶⁰ M. Carpinelli,⁶⁰ R. Cenci,⁶⁰ A. Cervelli,⁶⁰ F. Forti,⁶⁰ M. A. Giorgi,⁶⁰ A. Lusiani,⁶⁰ G. Marchiori,⁶⁰ M. A. Mazur,⁶⁰ M. Morganti,⁶⁰ N. Neri,⁶⁰ E. Paoloni,⁶⁰ G. Rizzo,⁶⁰ J. J. Walsh,⁶⁰ J. Biesiada,⁶¹ P. Elmer,⁶¹ Y. P. Lau,⁶¹ C. Lu,⁶¹ J. Olsen,⁶¹ A. J. S. Smith,⁶¹ A. V. Telnov,⁶¹ E. Baracchini,⁶² F. Bellini,⁶² G. Cavoto,⁶² D. del Re,⁶² E. Di Marco,⁶² R. Faccini,⁶² F. Ferrarotto,⁶² F. Ferroni,⁶² M. Gaspero,⁶² P. D. Jackson,⁶² L. Li Gioi,⁶² M. A. Mazzoni,⁶² S. Morganti,⁶² G. Piredda,⁶² F. Polci,⁶² F. Renga,⁶² C. Voena,⁶² M. Ebert,⁶³ T. Hartmann,⁶³ H. Schröder,⁶³ R. Walldi,⁶³ T. Adye,⁶⁴ G. Castelli,⁶⁴ B. Franek,⁶⁴ E. O. Olaiya,⁶⁴ W. Roethel,⁶⁴ F. F. Wilson,⁶⁴ S. Emery,⁶⁵ M. Escalier,⁶⁵ A. Gaidot,⁶⁵ S. F. Ganzhur,⁶⁵ G. Hamel de Monchenault,⁶⁵ W. Kozanecki,⁶⁵ G. Vasseur,⁶⁵ Ch. Yèche,⁶⁵ M. Zito,⁶⁵ X. R. Chen,⁶⁶ H. Liu,⁶⁶ W. Park,⁶⁶ M. V. Purohit,⁶⁶ R. M. White,⁶⁶ J. R. Wilson,⁶⁶ M. T. Allen,⁶⁷ D. Aston,⁶⁷ R. Bartoldus,⁶⁷ P. Bechtel,⁶⁷ R. Claus,⁶⁷ J. P. Coleman,⁶⁷ M. R. Convery,⁶⁷ J. C. Dingfelder,⁶⁷ J. Dorfan,⁶⁷ G. P. Dubois-Felsmann,⁶⁷ W. Dunwoodie,⁶⁷ R. C. Field,⁶⁷ T. Glanzman,⁶⁷ S. J. Gowdy,⁶⁷ M. T. Graham,⁶⁷ P. Grenier,⁶⁷ C. Hast,⁶⁷ W. R. Innes,⁶⁷ J. Kaminski,⁶⁷ M. H. Kelsey,⁶⁷ H. Kim,⁶⁷ P. Kim,⁶⁷ M. L. Kocian,⁶⁷ D. W. G. S. Leith,⁶⁷ S. Li,⁶⁷ S. Luitz,⁶⁷ V. Luth,⁶⁷ H. L. Lynch,⁶⁷ D. B. MacFarlane,⁶⁷ H. Marsiske,⁶⁷ R. Messner,⁶⁷ D. R. Muller,⁶⁷ C. P. O'Grady,⁶⁷ I. Ofte,⁶⁷ A. Perazzo,⁶⁷ M. Perl,⁶⁷ T. Pulliam,⁶⁷ B. N. Ratcliff,⁶⁷ A. Roodman,⁶⁷ A. A. Salnikov,⁶⁷ R. H. Schindler,⁶⁷ J. Schwiening,⁶⁷ A. Snyder,⁶⁷ D. Su,⁶⁷ M. K. Sullivan,⁶⁷ K. Suzuki,⁶⁷ S. K. Swain,⁶⁷ J. M. Thompson,⁶⁷ J. Va'vra,⁶⁷ A. P. Wagner,⁶⁷ M. Weaver,⁶⁷ W. J. Wisniewski,⁶⁷ M. Wittgen,⁶⁷ D. H. Wright,⁶⁷ A. K. Yarritu,⁶⁷ K. Yi,⁶⁷ C. C. Young,⁶⁷ V. Ziegler,⁶⁷ P. R. Burchat,⁶⁸ A. J. Edwards,⁶⁸ S. A. Majewski,⁶⁸ T. S. Miyashita,⁶⁸ B. A. Petersen,⁶⁸ L. Wilden,⁶⁸ S. Ahmed,⁶⁹ M. S. Alam,⁶⁹ R. Bula,⁶⁹ J. A. Ernst,⁶⁹ V. Jain,⁶⁹ B. Pan,⁶⁹ M. A. Saeed,⁶⁹ F. R. Wappler,⁶⁹ S. B. Zain,⁶⁹ M. Krishnamurthy,⁷⁰ S. M. Spanier,⁷⁰ R. Eckmann,⁷¹ J. L. Ritchie,⁷¹ A. M. Ruland,⁷¹ C. J. Schilling,⁷¹ R. F. Schwitters,⁷¹ J. M. Izen,⁷² X. C. Lou,⁷² S. Ye,⁷² F. Bianchi,⁷³ F. Gallo,⁷³ D. Gamba,⁷³ M. Pelliccioni,⁷³ M. Bomben,⁷⁴ L. Bosisio,⁷⁴ C. Cartaro,⁷⁴ F. Cossutti,⁷⁴ G. Della Ricca,⁷⁴ L. Lanceri,⁷⁴ L. Vitale,⁷⁴ V. Azzolini,⁷⁵ N. Lopez-March,⁷⁵ F. Martinez-Vidal,⁷⁵ D. A. Milanes,⁷⁵ A. Oyanguren,⁷⁵ J. Albert,⁷⁶ Sw. Banerjee,⁷⁶ B. Bhuyan,⁷⁶ K. Hamano,⁷⁶ R. Kowalewski,⁷⁶ I. M. Nugent,⁷⁶ J. M. Roney,⁷⁶ R. J. Sobie,⁷⁶ P. F. Harrison,⁷⁷ J. Ilic,⁷⁷ T. E. Latham,⁷⁷ G. B. Mohanty,⁷⁷ H. R. Band,⁷⁸ X. Chen,⁷⁸ S. Dasu,⁷⁸ K. T. Flood,⁷⁸ J. J. Hollar,⁷⁸ P. E. Kutter,⁷⁸ Y. Pan,⁷⁸ M. Pierini,⁷⁸ R. Prepost,⁷⁸ S. L. Wu,⁷⁸ and H. Neal⁷⁹

(BABAR Collaboration)

¹Laboratoire de Physique des Particules, IN2P3/CNRS et Université de Savoie, F-74941 Annecy-Le-Vieux, France²Universitat de Barcelona, Facultat de Física, Departament ECM, E-08028 Barcelona, Spain³Università di Bari, Dipartimento di Fisica and INFN, I-70126 Bari, Italy⁴University of Bergen, Institute of Physics, N-5007 Bergen, Norway⁵Lawrence Berkeley National Laboratory and University of California, Berkeley, California 94720, USA⁶University of Birmingham, Birmingham, B15 2TT, United Kingdom⁷Ruhr Universität Bochum, Institut für Experimentalphysik I, D-44780 Bochum, Germany⁸University of Bristol, Bristol BS8 1TL, United Kingdom⁹University of British Columbia, Vancouver, British Columbia, Canada V6T 1Z1¹⁰Brunel University, Uxbridge, Middlesex UB8 3PH, United Kingdom¹¹Budker Institute of Nuclear Physics, Novosibirsk 630090, Russia¹²University of California at Irvine, Irvine, California 92697, USA¹³University of California at Los Angeles, Los Angeles, California 90024, USA¹⁴University of California at Riverside, Riverside, California 92521, USA¹⁵University of California at San Diego, La Jolla, California 92093, USA¹⁶University of California at Santa Barbara, Santa Barbara, California 93106, USA¹⁷University of California at Santa Cruz, Institute for Particle Physics, Santa Cruz, California 95064, USA¹⁸California Institute of Technology, Pasadena, California 91125, USA¹⁹University of Cincinnati, Cincinnati, Ohio 45221, USA²⁰University of Colorado, Boulder, Colorado 80309, USA²¹Colorado State University, Fort Collins, Colorado 80523, USA²²Universität Dortmund, Institut für Physik, D-44221 Dortmund, Germany²³Technische Universität Dresden, Institut für Kern- und Teilchenphysik, D-01062 Dresden, Germany²⁴Laboratoire Leprince-Ringuet, CNRS/IN2P3, Ecole Polytechnique, F-91128 Palaiseau, France²⁵University of Edinburgh, Edinburgh EH9 3JZ, United Kingdom²⁶Università di Ferrara, Dipartimento di Fisica and INFN, I-44100 Ferrara, Italy²⁷Laboratori Nazionali di Frascati dell'INFN, I-00044 Frascati, Italy²⁸Università di Genova, Dipartimento di Fisica and INFN, I-16146 Genova, Italy²⁹Harvard University, Cambridge, Massachusetts 02138, USA

- ³⁰Universität Heidelberg, Physikalisches Institut, Philosophenweg 12, D-69120 Heidelberg, Germany
- ³¹Imperial College London, London SW7 2AZ, United Kingdom
- ³²University of Iowa, Iowa City, Iowa 52242, USA
- ³³Iowa State University, Ames, Iowa 50011-3160, USA
- ³⁴Johns Hopkins University, Baltimore, Maryland 21218, USA
- ³⁵Universität Karlsruhe, Institut für Experimentelle Kernphysik, D-76021 Karlsruhe, Germany
- ³⁶Laboratoire de l'Accélérateur Linéaire, IN2P3/CNRS et Université Paris-Sud 11, Centre Scientifique d'Orsay, B. P. 34, F-91898 Orsay Cedex, France
- ³⁷Lawrence Livermore National Laboratory, Livermore, California 94550, USA
- ³⁸University of Liverpool, Liverpool L69 7ZE, United Kingdom
- ³⁹Queen Mary, University of London, E1 4NS, United Kingdom
- ⁴⁰University of London, Royal Holloway and Bedford New College, Egham, Surrey TW20 0EX, United Kingdom
- ⁴¹University of Louisville, Louisville, Kentucky 40292, USA
- ⁴²University of Manchester, Manchester M13 9PL, United Kingdom
- ⁴³University of Maryland, College Park, Maryland 20742, USA
- ⁴⁴University of Massachusetts, Amherst, Massachusetts 01003, USA
- ⁴⁵Massachusetts Institute of Technology, Laboratory for Nuclear Science, Cambridge, Massachusetts 02139, USA
- ⁴⁶McGill University, Montréal, Québec, Canada H3A 2T8
- ⁴⁷Università di Milano, Dipartimento di Fisica and INFN, I-20133 Milano, Italy
- ⁴⁸University of Mississippi, University, Mississippi 38677, USA
- ⁴⁹Université de Montréal, Physique des Particules, Montréal, Québec, Canada H3C 3J7
- ⁵⁰Mount Holyoke College, South Hadley, Massachusetts 01075, USA
- ⁵¹Università di Napoli Federico II, Dipartimento di Scienze Fisiche and INFN, I-80126, Napoli, Italy
- ⁵²NIKHEF, National Institute for Nuclear Physics and High Energy Physics, NL-1009 DB Amsterdam, The Netherlands
- ⁵³University of Notre Dame, Notre Dame, Indiana 46556, USA
- ⁵⁴The Ohio State University, Columbus, Ohio 43210, USA
- ⁵⁵University of Oregon, Eugene, Oregon 97403, USA
- ⁵⁶Università di Padova, Dipartimento di Fisica and INFN, I-35131 Padova, Italy
- ⁵⁷Laboratoire de Physique Nucléaire et de Hautes Energies, IN2P3/CNRS, Université Pierre et Marie Curie-Paris6, Université Denis Diderot-Paris7, F-75252 Paris, France
- ⁵⁸University of Pennsylvania, Philadelphia, Pennsylvania 19104, USA
- ⁵⁹Università di Perugia, Dipartimento di Fisica and INFN, I-06100 Perugia, Italy
- ⁶⁰Università di Pisa, Dipartimento di Fisica, Scuola Normale Superiore and INFN, I-56127 Pisa, Italy
- ⁶¹Princeton University, Princeton, New Jersey 08544, USA
- ⁶²Università di Roma La Sapienza, Dipartimento di Fisica and INFN, I-00185 Roma, Italy
- ⁶³Universität Rostock, D-18051 Rostock, Germany
- ⁶⁴Rutherford Appleton Laboratory, Chilton, Didcot, Oxon OX11 0QX, United Kingdom
- ⁶⁵DSM/Dapnia, CEA/Saclay, F-91191 Gif-sur-Yvette, France
- ⁶⁶University of South Carolina, Columbia, South Carolina 29208, USA
- ⁶⁷Stanford Linear Accelerator Center, Stanford, California 94309, USA
- ⁶⁸Stanford University, Stanford, California 94305-4060, USA
- ⁶⁹State University of New York, Albany, New York 12222, USA
- ⁷⁰University of Tennessee, Knoxville, Tennessee 37996, USA
- ⁷¹University of Texas at Austin, Austin, Texas 78712, USA
- ⁷²University of Texas at Dallas, Richardson, Texas 75083, USA
- ⁷³Università di Torino, Dipartimento di Fisica Sperimentale and INFN, I-10125 Torino, Italy
- ⁷⁴Università di Trieste, Dipartimento di Fisica and INFN, I-34127 Trieste, Italy
- ⁷⁵IFIC, Universitat de Valencia-CSIC, E-46071 Valencia, Spain
- ⁷⁶University of Victoria, Victoria, British Columbia, Canada V8W 3P6
- ⁷⁷Department of Physics, University of Warwick, Coventry CV4 7AL, United Kingdom
- ⁷⁸University of Wisconsin, Madison, Wisconsin 53706, USA
- ⁷⁹Yale University, New Haven, Connecticut 06511, USA

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We present partial branching fractions for inclusive charmless semileptonic B decays $\bar{B} \rightarrow X_u \ell \bar{\nu}$, and the determination of the Cabibbo-Kobayashi-Maskawa matrix element $|V_{ub}|$. The analysis is based on a sample of 383×10^6 $Y(4S)$ decays into $B\bar{B}$ pairs collected with the BABAR detector at the SLAC PEP-II e^+e^- storage rings. We select events using the invariant mass M_X of the hadronic system, the invariant mass squared, q^2 , of the lepton and neutrino pair, the kinematic variable P_+ , or one of their combinations. We then determine partial branching fractions in limited regions of phase space: $\Delta\mathcal{B} = (1.18 \pm 0.09_{\text{stat}} \pm 0.07_{\text{syst}} \pm 0.01_{\text{theor}}) \times 10^{-3}$ ($M_X < 1.55 \text{ GeV}/c^2$), $\Delta\mathcal{B} = (0.95 \pm 0.10_{\text{stat}} \pm 0.08_{\text{syst}} \pm 0.01_{\text{theor}}) \times 10^{-3}$

($P_+ < 0.66 \text{ GeV}/c$), and $\Delta\mathcal{B} = (0.81 \pm 0.08_{\text{stat}} \pm 0.07_{\text{syst}} \pm 0.02_{\text{theor}}) \times 10^{-3} (M_X < 1.7 \text{ GeV}/c^2, q^2 > 8 \text{ GeV}^2/c^4)$. Corresponding values of $|V_{ub}|$ are extracted using several theoretical calculations.

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In the standard model the element V_{ub} of the Cabibbo-Kobayashi-Maskawa (CKM) quark-mixing matrix [1] plays a critical role in tests of the prediction of CP violation. Since the rate for charmless semileptonic decays, $\bar{B} \rightarrow X_u \ell \bar{\nu}$ [2], is proportional to $|V_{ub}|^2$, and the hadronic and leptonic currents are factorizable, the best method to extract this quantity is to measure branching fractions for such decays [3]. Experimentally, the principal challenge is to separate the rare $\bar{B} \rightarrow X_u \ell \bar{\nu}$ decays from the approximately 50 times larger $\bar{B} \rightarrow X_c \ell \bar{\nu}$ background. Given that the u quark is much lighter than the c quark, regions of phase space can be defined where the background is suppressed. To relate the decay rate of the B meson to $|V_{ub}|$, parton level calculations have to be corrected for perturbative and nonperturbative QCD effects. A variety of QCD calculations are available to determine these corrections [4–6].

In this Letter, we present a measurement of partial branching fractions for inclusive charmless semileptonic decays, $\bar{B} \rightarrow X_u \ell \bar{\nu}$ [7]. $Y(4S) \rightarrow B\bar{B}$ events are tagged by the full reconstruction of a hadronic decay of one of the B mesons (B_{reco}). The semileptonic decay of the second B meson (B_{recoil}) is identified by the presence of an electron or a muon. This technique results in a low event selection efficiency but allows the determination of the momentum, charge, and flavor of the B mesons.

We use three kinematic variables to separate $\bar{B} \rightarrow X_u \ell \bar{\nu}$ decays from the dominant $\bar{B} \rightarrow X_c \ell \bar{\nu}$ background: M_X , the invariant mass of the hadronic system $X_{u,c}$; q^2 , the invariant mass squared of the lepton-neutrino system; and $P_+ \equiv E_X - |\vec{P}_X|$ [4,5], where E_X and $\vec{P}_X$ are the energy and momentum of the hadronic system $X_{u,c}$ calculated in the B rest frame. We measure the fraction of partial rates of charmless semileptonic decays $\Delta R_{u/sl} = \Delta\mathcal{B}(\bar{B} \rightarrow X_u \ell \bar{\nu})/\mathcal{B}(\bar{B} \rightarrow X \ell \bar{\nu})$ in restricted phase-space regions, corrected for resolution effects. The resulting partial branching fractions are used to calculate $|V_{ub}|$ following theoretical prescriptions.

The analysis uses a sample of 383×10^6 $Y(4S)$ decays into $B\bar{B}$ pairs, corresponding to an integrated luminosity of 347.4 fb^{-1} , collected with the *BABAR* detector [8]. Charmless semileptonic $\bar{B} \rightarrow X_u \ell \bar{\nu}$ decays are simulated as a combination of three-body decays ($X_u = \pi, \eta, \eta', \rho, \omega, \dots$) [9] and decays to nonresonant hadronic final states X_u [10]. The motion of the b quark inside the B meson is modeled with the shape function parametrization given in Ref. [10]. The simulation of the $\bar{B} \rightarrow X_c \ell \bar{\nu}$ background uses a heavy quark effective theory parametrization of form factors for $B \rightarrow D^* \ell \nu$ [11,12], and models for $\bar{B} \rightarrow D\pi \ell \bar{\nu}$, $D^* \pi \ell \bar{\nu}$ [13], and for $\bar{B} \rightarrow D \ell \bar{\nu}$, $D^{**} \ell \bar{\nu}$ [9]. The

simulation of the hadronization is performed by JETSET 7.4 [14]. We use GEANT4 [15] to simulate the detector response.

To reconstruct a large sample of hadronically decaying B mesons, $B_{\text{reco}} \rightarrow \bar{D}^{(*)} Y^\pm$ are selected. Here, the system $Y^\pm$ consists of hadrons with a total charge of ± 1 , composed of $n_1 \pi^\pm n_2 K^\pm n_3 K_S^0 n_4 \pi^0$, where $n_1 + n_2 \leq 5$, $n_3 \leq 2$, and $n_4 \leq 2$. The kinematic consistency of B_{reco} candidates is checked with two variables, $m_{\text{ES}} = \sqrt{s/4 - \vec{p}_B^2}$ and $\Delta E = E_B - \sqrt{s}/2$. Here $\sqrt{s}$ is the total energy in the $Y(4S)$ center of mass frame, and $\vec{p}_B$ and E_B denote the momentum and energy of the B_{reco} candidate in the same frame. We require $\Delta E = 0$ within 3 standard deviations as measured for each decay mode. For each of the B_{reco} decay modes, the purity $\mathcal{P}$ is estimated using Monte Carlo (MC) simulation. $\mathcal{P}$ is defined as the ratio of signal over background events with $m_{\text{ES}} \geq 5.27 \text{ GeV}/c^2$. Only modes for which $\mathcal{P}$ exceeds 20% are used. On average, we reconstruct at least one B candidate in 0.3% (0.5%) of the $B^0 \bar{B}^0$ ($B^+ B^-$) events. For events with more than one reconstructed B decay, the decay mode with the highest purity is selected.

We determine the number of B_{reco} candidates from an unbinned maximum likelihood fit to the m_{ES} distribution. The data are fit to the sum of three contributions: signal B_{reco} decays, combinatorial background from $B\bar{B}$ events, and continuum ($e^+ e^- \rightarrow q\bar{q}$, $q = u, d, s, c$) events. A threshold function [16] is used to describe the combinatorial and continuum backgrounds. To obtain a good description of the signal m_{ES} distribution, we adopt the modified Gaussian function used in Ref. [17] to account for energy losses of photons in the detector. Fits to the m_{ES} distribution are shown in Fig. 1. Semileptonic decays $\bar{B} \rightarrow X \ell \bar{\nu}$ of

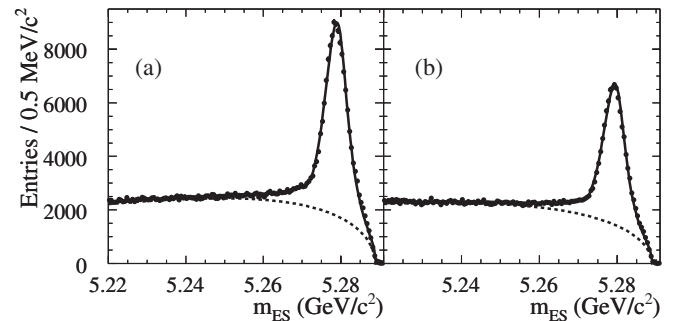


FIG. 1. The m_{ES} distribution for data (full circles) is shown together with the results of the fit (solid line) for selected semileptonic decays from $B^+ B^-$ events (a) and $B^0 \bar{B}^0$ events (b). The dashed line shows the contribution from combinatorial and continuum background.

the B_{recoil} candidate are identified by an electron or muon with momentum, p_ℓ^* , defined in the $\bar{B}$ rest frame, greater than 1 GeV/c. For charged B_{reco} candidates, we require the charge of the lepton to be consistent with a prompt semileptonic $\bar{B}$ decay. For neutral B_{reco} candidates, both charge-flavor combinations are retained and the known average $B^0\text{--}\bar{B}^0$ mixing rate [18] is used to extract the prompt lepton yield.

The hadronic system X in the decay $\bar{B} \rightarrow X\ell\bar{\nu}$ is reconstructed from charged tracks and energy depositions in the calorimeter that are not associated with the B_{reco} candidate or the identified lepton. We reconstruct K_S^0 by performing a mass-constrained fit to $\pi^+\pi^-$ pairs with an invariant mass in the range 0.473–0.523 GeV/c². The neutrino four-momentum p_ν is estimated from the missing momentum four-vector $p_{\text{miss}} = p_{Y(4S)} - p_{B_{\text{reco}}} - p_X - p_\ell$, where all momenta are measured in the laboratory frame and $p_{Y(4S)}$ refers to the $Y(4S)$ meson.

To select $\bar{B} \rightarrow X_u\ell\bar{\nu}$ candidates, we require exactly one charged lepton with $p_\ell^* > 1$ GeV/c, charge conservation ($Q_X + Q_\ell + Q_{B_{\text{reco}}} = 0$), and a missing mass consistent with zero ($m_{\text{miss}}^2 < 0.5$ GeV²/c⁴). These criteria suppress the dominant $\bar{B} \rightarrow X_c\ell\bar{\nu}$ decays, many of which contain additional leptons or an undetected K_L^0 meson. We suppress the $B \rightarrow D^*\ell\nu$ background by reconstructing the low momentum π^+ from the $D^{*+} \rightarrow D^0\pi^+$ decay. Since the momentum of the π^+ is almost collinear with the D^{*+} momentum $p_{D^{*+}}$, we can approximate the D^{*+} energy as $E_{D^{*+}} \simeq m_{D^{*+}} \times E_\pi/145$ MeV/c². The neutrino mass $m_{\text{veto}}^2 = (p_B - p_{D^{*+}} - p_\ell)^2$ is peaked at zero for background events. The requirement $m_{\text{veto}}^2 < -3$ GeV²/c⁴ reduces the $B \rightarrow D^*\ell\nu$ background by about 36% while keeping more than 90% of signal events. We reject events with charged kaons or K_S^0 in the B_{recoil} to reduce the background from $\bar{B} \rightarrow X_c\ell\bar{\nu}$ decays.

To extract the distribution in the variables M_X , P_+ , and the combination of M_X and q^2 , we perform fits to the B_{reco} m_{ES} distributions for subsamples of events in individual bins for each of the variables, and subsequently separate the signal from the combinatorial and continuum backgrounds for the three distributions. The resulting distributions are presented in Fig. 2. To reduce the systematic uncertainties in the derivation of the branching fractions, we determine the ratios of the partial branching fractions to the total semileptonic branching fraction. This is done for restricted regions of phase space, $M_X < 1.55$ GeV/c², $P_+ < 0.66$ GeV/c, and $(M_X < 1.7$ GeV/c², $q^2 > 8.0$ GeV²/c⁴). Specifically, we define this ratio as

$$\frac{\Delta\mathcal{B}(X_u\ell\bar{\nu}_\ell)}{\mathcal{B}(X\ell\bar{\nu}_\ell)} = \frac{(N_u - N_u^{\text{out}} - BG_u)/(\epsilon_{\text{sel}}^u \epsilon_{\text{kin}}^u)}{(N_{\text{sl}} - BG_{\text{sl}})} \frac{\epsilon_{\ell}^{\text{sl}} \epsilon_t^{\text{sl}}}{\epsilon_{\ell}^u \epsilon_t^u}, \quad (1)$$

where N_u refers to the number of observed events, BG_u to the estimated number of background events, and N_u^{out} to the signal events that migrate from outside the kinematic region into the signal region. They are determined by a χ^2 fit to the measured spectra with signal and background shapes determined from MC simulation. $N_{\text{sl}} = 181074 \pm 706$ and $BG_{\text{sl}} = 12185 \pm 78$ are the number of semileptonic events, extracted with a m_{ES} fit, and the corresponding background, determined from simulation. The efficiency ϵ_{sel}^u denotes the fraction of selected B_{reco} -tagged signal events with a high-energy lepton. The model-dependent efficiency ϵ_{kin}^u accounts for the loss of selected events generated in the kinematic region that migrate outside this region. The efficiency of the tag and lepton selection, ϵ_t and ϵ_ℓ , differ slightly for the signal and the semileptonic samples, due to differences in the lepton momentum distribution and the multiplicity of the recoiling B meson. To convert the ratio in Eq. (1) to partial branching fractions, we use the total semileptonic branch-

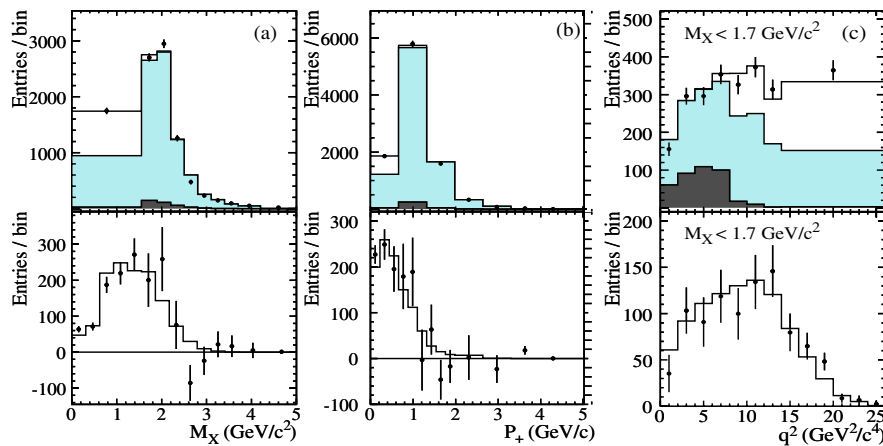


FIG. 2 (color online). Upper row: measured M_X (a), P_+ (b), and q^2 with $M_X < 1.7$ GeV/c² (c) spectra (data points). The result of the fit to the sum of three MC contributions is shown in the histograms: $\bar{B} \rightarrow X_u\ell\bar{\nu}$ decays generated inside (no shading) and outside (dark shading) the selected kinematic region, and $\bar{B} \rightarrow X_c\ell\bar{\nu}$ and other background (light shading). Lower row: corresponding spectra for $\bar{B} \rightarrow X_u\ell\bar{\nu}$ after $\bar{B} \rightarrow X_c\ell\bar{\nu}$ and other background subtraction; they have been rebinned in order to show the shape of the kinematic variables.

TABLE I. Summary of the fitted number of events and efficiencies, $\Delta\mathcal{B}(\bar{B} \rightarrow X_u \ell \bar{\nu})$, and extracted $|V_{ub}|$ for the three kinematic cuts. The first uncertainty is statistical, the second systematic. For $\Delta\mathcal{B}$, the third uncertainty is due to the theoretical knowledge of the signal efficiency; for the $|V_{ub}|$ values, it comes from the theoretical uncertainty on $\Delta\zeta$. For Ref. [4] we use the exponential parametrization of the shape function.

Method	N_u	N_u^{out}	BG_u	$\epsilon_{\text{sel}}^u \epsilon_{\text{kin}}^u$	$\frac{\epsilon_{\ell}^{\text{sl}} \epsilon_{\ell}^{\text{sl}}}{\epsilon_{\ell}^{\text{sl}} \epsilon_{\ell}^{\text{sl}}}$	$\Delta\mathcal{B}(\bar{B} \rightarrow X_u \ell \bar{\nu})(10^{-3})$	$ V_{ub} \times (10^{-3})$
M_X	803 ± 60	27 ± 2	923 ± 21	0.331 ± 0.003	0.76 ± 0.02	$1.18 \pm 0.09 \pm 0.07 \pm 0.01$	$4.27 \pm 0.16 \pm 0.13 \pm 0.30$ [4] $4.56 \pm 0.17 \pm 0.14 \pm 0.32$ [5] $3.88 \pm 0.19 \pm 0.16 \pm 0.28$ [4]
P_+	633 ± 63	48 ± 5	1183 ± 27	0.344 ± 0.003	0.81 ± 0.02	$0.95 \pm 0.10 \pm 0.08 \pm 0.01$	$3.99 \pm 0.20 \pm 0.16 \pm 0.24$ [5] $4.57 \pm 0.22 \pm 0.19 \pm 0.30$ [4]
M_X, q^2	562 ± 55	32 ± 2	789 ± 9	0.353 ± 0.005	0.79 ± 0.03	$0.81 \pm 0.08 \pm 0.07 \pm 0.02$	$4.64 \pm 0.23 \pm 0.19 \pm 0.25$ [5] $4.93 \pm 0.24 \pm 0.20 \pm 0.36$ [6]

ing fraction, $\mathcal{B}(\bar{B} \rightarrow X \ell \bar{\nu}) = (10.75 \pm 0.15)\%$ [18]. The resulting partial branching fractions for the three selected kinematic regions, along with parameters in Eq. (1), are listed in Table I. The statistical correlations between the M_X and (M_X, q^2) , P_+ analyses are 65%, 67%, 38%, respectively.

We consider several sources of systematic uncertainties. Detector-related uncertainties take into account particle (e , μ , K) identification (efficiency, misidentification), charged particle tracking efficiency, photon reconstruction efficiency, and K_L^0 interactions. We estimate the uncertainty due to signal and background modeling. The uncertainty on the signal modeling is due to the modeling of exclusive charmless semileptonic decays and gluon splitting into $s\bar{s}$ -quark pairs. We also calculate the uncertainties due to the nonperturbative parameters and the functional form of the shape function. The background simulation depends on the B and D branching fractions and $B \rightarrow D^* \ell \bar{\nu}$ form factors; the corresponding systematic uncertainties are calculated by varying all these quantities within their experimental errors. We estimate the error due to m_{ES} fits, coming from the uncertainty in the parametrization ansatz. Finally, we estimate the error due to MC statistics. The fractional contribution of each uncertainty is shown in Table II together with the total error.

The results of the partial branching fractions are translated into $|V_{ub}|$ in the context of recent QCD calculations [4–6], including estimates of theoretical uncertainties (see Table I). The hadronic input parameters, the b -quark mass m_b and the kinetic energy expectation value μ_π^2 , are ex-

tracted from moment measurements in $B \rightarrow X_s \gamma$ and $\bar{B} \rightarrow X_c \ell \bar{\nu}$. Their values in the kinetic scheme [19] are $m_b = (4.59 \pm 0.04) \text{ GeV}/c^2$ and $\mu_\pi^2 = (0.40 \pm 0.04) \text{ GeV}^2/c^2$ [20] and are translated into values in different schemes, as needed [4–6]. The partial branching fraction $\Delta\mathcal{B}(\bar{B} \rightarrow X_u \ell \bar{\nu})$ is related directly to $|V_{ub}|$ by the relation $|V_{ub}| = [\Delta\mathcal{B}(\bar{B} \rightarrow X_u \ell \bar{\nu})/\tau_b \Delta\zeta]^{1/2}$, where τ_b is the average B lifetime [18], and $\Delta\zeta$ is the prediction for the partial rate for $\bar{B} \rightarrow X_u \ell \bar{\nu}$ in the given phase-space region [4–6].

In summary, we have measured the branching fractions for inclusive charmless semileptonic B decays $\bar{B} \rightarrow X_u \ell \bar{\nu}$ in three overlapping regions of phase space. Relying on theoretical predictions, we extract values for the CKM matrix element $|V_{ub}|$ from our measured $\Delta\mathcal{B}$.

We find that the determinations of $|V_{ub}|$ agree at 1σ level in the BNLP [4] framework for the M_X and combined (M_X, q^2) analyses. The analysis based on P_+ differs from the two others at a 2.5σ level, as indicated also by other experiments [21]. The M_X analysis captures the largest portion of phase space and gives the most precise determination of $|V_{ub}|$. Within their stated theoretical uncertainties, the results based on BLNP and DGE [5] give consistent results. The result, based on the hadronic mass spectrum, supersedes our previously published measurement [3], reducing the relative uncertainty by 40%. These values are in good agreement with other inclusive $|V_{ub}|$ determinations, and they are somewhat higher, though compatible, than the results based on exclusive charmless semileptonic decays [18].

TABLE II. Contributions to the systematic uncertainty on the measured $\Delta\mathcal{B}(\bar{B} \rightarrow X_u \ell \bar{\nu})$, shown in percent (%) for the three kinematic cuts, from detector, shape function (input parameters and functional form), exclusive $\mathcal{B}(\bar{B} \rightarrow X_u \ell \bar{\nu})$, gluon splitting, exclusive $\mathcal{B}(\bar{B} \rightarrow X_c \ell \bar{\nu})$, $B \rightarrow D^* \ell \bar{\nu}$ form factors, $\mathcal{B}(D)$, m_{ES} fit, MC statistics. The last column gives the total systematic uncertainty.

Method	Detector	Shape function	$\mathcal{B}(\bar{B} \rightarrow X_u \ell \bar{\nu})$ $X_u = \pi, \rho, \dots$	Gluon splitting	$\mathcal{B}(\bar{B} \rightarrow X_c \ell \bar{\nu})$	$B \rightarrow D^* \ell \bar{\nu}$ form factors	$\mathcal{B}(D)$	m_{ES} fit	Monte Carlo statistics	Total
M_X	1.92	0.90	2.08	1.62	0.87	0.21	0.44	3.71	3.22	6.07
P_+	3.88	1.31	2.22	1.47	2.80	0.39	0.73	3.98	4.62	8.38
M_X, q^2	3.83	2.43	2.71	1.02	1.17	0.55	0.79	5.17	4.29	8.81

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*Deceased.

[†]Present address: Tel Aviv University, Tel Aviv, 69978, Israel.

[‡]Also at Università di Perugia, Dipartimento di Fisica, Perugia, Italy.

[§]Also at Università della Basilicata, Potenza, Italy.

^{||}Also at Universitat de Barcelona, Facultat de Física, Departament ECM, E-08028 Barcelona, Spain.

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