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¹ Effective optical properties of absorbing nanoporous ² and nanocomposite thin films

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9 This paper aims at developing numerically validated models for predicting the through-plane 10 effective index of refraction and absorption index of nanocomposite thin films. First, models for the effective optical properties of such materials are derived from previously reported analysis applying 11 the volume averaging theory (VAT) to Maxwell's equations. The transmittance and reflectance of 12 nanoporous thin films are computed by solving Maxwell's equations and the associated boundary 13 conditions at all interfaces using finite element methods. The effective optical properties of the films 14 are retrieved by minimizing the root mean square of the relative errors between the computed and 15 theoretical transmittance and reflectance. Nanoporous thin films made of SiO₂ and TiO₂ consisting 16 of cylindrical nanopores and nanowires are investigated for different diameters and various 17 porosities. Similarly, electromagnetic wave transport through dielectric medium with embedded 18 metallic nanowires are simulated. The numerical results are compared with predictions from widely 19 20 used effective property models including (1) the Maxwell-Garnett theory, (2) the Bruggeman effective medium approximation, (3) the parallel, (4) series, (5) Lorentz-Lorenz, and (6) the VAT 21 models. Very good agreement is found with the VAT model for both the effective index of refraction 22 and absorption index. Finally, the effect of volume fraction on the effective index of refraction and 23 absorption index predicted by the VAT model is discussed. For certain values of wavelengths and 24 25 volume fractions, the effective index of refraction or absorption index of the composite material can 26 be smaller than that of both the continuous and dispersed phases. These results indicate guidelines for designing nanocomposite materials with desired optical properties. © 2006 American Institute of 27 *Physics*. [DOI: 10.1063/1.2402327] 28

29

30 I. INTRODUCTION

In recent years, synthesis and characterization of nano-31 32 composite thin films in general and nanoporous in particular, **33** have been the subject of intense study.^{1–4} Potential applica-**34** tions include dye-sensitized solar cells, ^{5–7} low-k dielectric **35** materials,^{8,9} biosensors,^{10–12} and optical devices including **36** waveguides,^{13–15} Bragg reflectors and Fabry-Perot **37** filters.^{16–22} For example, in order to confine and propagate 38 electromagnetic waves within a waveguide, the guide region 39 itself must have a higher index of refraction than the sur-40 rounding cladding.²³ On the other hand, Bragg reflectors and 41 Fabry-Perot filters are built by generating alternating layers 42 with prescribed thickness and index of refraction. This ge-43 ometry uses constructive and destructive interferences to se-44 lectively reflect or transmit at desired wavelengths. In each 45 of these optical applications, the index of refraction is tuned 46 by controlling the morphology and porosity of the nanosize 47 pores formed by electrochemical etching of silicon, for ex-48 ample. Optimizing the performance of a given component 49 requires accurate knowledge of the effect of porosity, pore shape and size as well as the optical properties of each phase ⁵⁰ on the effective optical properties of the nanocomposite me- ⁵¹ dium. ⁵²

Various effective property models have been proposed in 53 the literature and were discussed in our previous study.²⁴ In 54 brief, the Maxwell-Garnett theory (MGT)²⁵ was first devel- 55 oped to model the effective electric permittivity of heteroge- 56 neous media consisting of monodispersed spheres arranged 57 in a cubic lattice structure within a continuous matrix and of 58 diameter much smaller than the wavelength of the incident 59 electromagnetic (EM) wave. Then, the effective dielectric 60 constant $\varepsilon_{r,eff}$ is expressed as 61

$$\varepsilon_{r,\text{eff}} = \varepsilon_{r,c} \left[1 - \frac{3\phi(\varepsilon_{r,c} - \varepsilon_{r,d})}{2\varepsilon_{r,c} + \varepsilon_{r,d} + \phi(\varepsilon_{r,c} - \varepsilon_{r,d})} \right], \tag{1}$$

where $\varepsilon_{r,c}$ and $\varepsilon_{r,d}$ are the dielectric constant of the continu- 63 ous and dispersed phases, respectively, while ϕ is the poros- 64 ity. For dispersed phase volume fractions larger than $\pi/6$ 65 $\simeq 52\%$ and polydispersed spheres the Bruggeman²⁶ model 66 gives the following implicit equation for $\varepsilon_{r,eff}$: 67

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$$1 - \phi = \frac{\left(\frac{\varepsilon_{r,\text{eff}}}{\varepsilon_{r,c}} - \frac{\varepsilon_{r,d}}{\varepsilon_{r,c}}\right)}{\left[\left(\frac{\varepsilon_{r,\text{eff}}}{\varepsilon_{r,c}}\right)^{1/3} \left(1 - \frac{\varepsilon_{r,d}}{\varepsilon_{r,c}}\right)\right]}.$$
(2)

69 On the other hand, the Lorentz-Lorenz model gives the ef-**70** fective index of refraction $n_{\rm eff}$ as

71
$$\left(\frac{n_{\rm eff}^2 - 1}{n_{\rm eff}^2 + 2}\right) = (1 - \phi) \left(\frac{n_c^2 - 1}{n_c^2 + 2}\right) + \left(\varphi \frac{n_d^2 - 1}{n_d^2 + 2}\right),$$
 (3)

72 where n_c and n_d are the index of refraction of the continuous 73 and dispersed phases, respectively. Alternatively, the parallel 74 model gives the effective property ψ_{eff} as a linear function of 75 the properties of the continuous and dispersed phases, i.e.,

76
$$\psi_{\text{eff}} = (1 - \phi)\psi_c + \phi\psi_d.$$
(4)

77 The series model, on the other hand, is expressed as

$$\frac{1}{\psi_{\text{eff}}} = \frac{1-\phi}{\psi_c} + \frac{\phi}{\psi_d}.$$
(5)

79 In addition, del Rio *et al.*²⁷ suggested the following effective **80** model for electrical conductivity based on the reciprocity **81** theorem

82
$$\sigma_{\rm eff} = \sigma_c \frac{1 + \phi(\sqrt{\sigma_c}/\sigma_d - 1)}{1 + \phi(\sqrt{\sigma_d}/\sigma_c - 1)}.$$
 (6)

83 Recently, del Rio and Whitaker^{28,29} applied the volume av-84 eraging theory (VAT) to Maxwell's equations for an en-85 semble of dispersed domains of arbitrary shape in a continu-86 ous matrix. They predicted the effective dielectric constant 87 $\varepsilon_{r,eff}$, relative permeability $\mu_{r,eff}$, and electrical conductivity 88 σ_{eff} of a two-phase mixture as²⁸

89
$$\varepsilon_{r,eff} = (1 - \phi)\varepsilon_{r,c} + \phi\varepsilon_{r,d},$$
 (7)

90
$$1/\mu_{r,eff} = (1 - \phi)/\mu_{r,c} + \phi/\mu_{r,d},$$
 (8)

91
$$\sigma_{\text{eff}} = (1 - \phi)\sigma_c + \phi\sigma_d.$$
 (9)

 The range of validity of these expressions was discussed in details, and a set of inequalities to be satisfied was developed by del Rio and Whitaker.²⁸ Their model has been numeri- cally validated by Braun and Pilon²⁴ for the effective through-plane index of refraction of *nonabsorbing* nano- porous media with open and closed cylindrical nanopores of various shapes and sizes corresponding to a wide range of porosity. The other models, however, underpredicted the nu-merical results.²⁴

101 Moreover, validation of the above models against experi-102 mental data often yields contradictory results.³⁰ These con-103 tradictions can be attributed to the fact that first, some of 104 these models were not developed for the index of refraction 105 but for the dielectric constant. However, they have been used 106 for optical properties (e.g., Refs. 8, 9, 31, and 13). Second, 107 unlike the present study, some of these models have also 108 been derived by considering a unit cell containing one pore 109 with uniform incident electromagnetic fields thus ignoring 110 possible interference taking place between adjacent 111 pores.^{25,26,32} Finally, large experimental uncertainty may exist in the measure of the porosity and the retrieval of the ¹¹² complex index of refraction from transmittance and reflec- ¹¹³ tance measurements. The latter is very sensitive to the sur- ¹¹⁴ face roughness of the film and to the uniformity and value of ¹¹⁵ the film thickness. Unfortunately, often, neither the film ¹¹⁶ thickness *L* nor the experimental uncertainty for both ϕ and ¹¹⁷ $m_{\rm eff}$ are reported. ¹¹⁸

The present study extends our previous investigation to 119 absorbing nanocomposite thin films. It aims at modeling 120 both the through-plane effective index of refraction and ab- 121 sorption index of (1) nanoporous thin films consisting of 122 horizontally aligned cylindrical nanopores or nanowires with 123 different diameters and various porosities and of (2) dielec- 124 tric medium with embedded metallic nanowires. Such thin 125 films are anisotropic and this study focuses on properties in 126 the direction normal to the film surface. It is limited to non- 127 magnetic materials for which $\mu_{r,c} = \mu_{r,d} = \mu_{r,eff} = 1$. Spectral 128 normal-normal transmittance and reflectance are obtained by 129 numerically solving Maxwell's equations and used to re- 130 trieve the effective index of refraction and absorption index. 131 The numerical results are then compared with previously re- 132 viewed models. Finally, the VAT model is analyzed in de- 133 tails. 134

II. ANALYSIS

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A. Optical properties from volume averaging theory 136

The index of refraction *n* and the absorption index *k* of 137 homogeneous media can be expressed in terms of the real 138 part of their dielectric constant ε_r and of their electrical conductivity σ as²³ 140

$$n^{2} = \frac{1}{2} \left[\varepsilon_{r} + \sqrt{\varepsilon_{r}^{2} + \left(\frac{\lambda\sigma}{2\pi c_{0}\varepsilon_{0}}\right)^{2}} \right], \qquad (10) \ \mathbf{141}$$

$$k^{2} = \frac{1}{2} \left[-\varepsilon_{r} + \sqrt{\varepsilon_{r}^{2} + \left(\frac{\lambda\sigma}{2\pi c_{0}\varepsilon_{0}}\right)^{2}} \right], \qquad (11) \ \mathbf{142}$$

where λ is the wavelength of incident radiation, c_0 is the 143 speed of light in vacuum, and ε_0 is the permittivity of free 144 space. The expression derived by Del Rio and Whitaker²⁸ for 145 the effective dielectric constant $\varepsilon_{r,eff}$ and electrical conduc- 146 tivity σ_{eff} of a two-phase medium [Eqs. (7) and (9)] can be 147 used to derive the effective optical properties of a two-phase 148 nanocomposite material 149

$$n_{\rm eff}^2 = \frac{1}{2} [A + \sqrt{A^2 + B^2}], \tag{12}$$

$$k_{\rm eff}^2 = \frac{1}{2} [-A + \sqrt{A^2 + B^2}], \tag{13}$$

where

$$A = \varepsilon_{r,\text{eff}} = \phi(n_d^2 - k_d^2) + (1 - \phi)(n_c^2 - k_c^2)$$
(14) 153

and

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1-3

155
$$B = \frac{\lambda \sigma_{\text{eff}}}{2\pi c_0 \varepsilon_0} = 2n_d k_d \phi + 2n_c k_c (1 - \phi).$$
(15)

 In particular, when the dispersed phase is vacuum, $\varepsilon_{r,d} = n_d$ = 1, and $k_d = \sigma_d = 0$. Note also that, unlike other effective property models, the above VAT models for $n_{\rm eff}$ and $k_{\rm eff}$ de- pend on both the real and complex parts of the complex indices of refraction of the dispersed and continuous phases. In other words, $R_{\rm calc}$ and k_d affect not only $k_{\rm eff}$ but also $n_{\rm eff}$.

162 B. Governing equations and numerical **163** implementation

164 In order to develop the numerical model, let us first con-165 sider a surrounding environment (medium 1, n_1 , $k_1=0$) from 166 which an electromagnetic wave is incident on an absorbing 167 thin film (medium 2, n_2 , k_2) deposited onto an absorbing 168 dense substrate (medium 3, n_3 , k_3). A linearly polarized 169 plane wave in transverse electric (TE) mode is incident nor-170 mal to the film top surface and propagates through the two-171 dimensional thin film along the *x* direction. As the wave 172 propagates in the *x*-*y* plane, it has only one electric field 173 component in the *z* direction, while the magnetic field has 174 two components in the *x*-*y* plane (i.e., perpendicularly polar-175 ized), such that in a general time-harmonic form

176
$$\tilde{E}(x,y,t) = E_z(x,y)e^{i\omega t}\vec{e}_z,$$

177
178 $\vec{H}(x,y,t) = [H_x(x,y)\vec{e}_x + H_y(x,y)\vec{e}_y]e^{i\omega t}.$
(16)

 Here, \vec{E} is the electric field vector, \vec{H} is the magnetic field vector, \vec{e}_x , \vec{e}_y , and \vec{e}_z are the unit vectors, and $\omega = 2\pi c_0/\lambda$ is the angular frequency of the wave. For general time-varying fields in a conducting medium, Maxwell's equations can be written as

184
$$\nabla \times \left[\frac{1}{\mu_r \mu_0} \nabla \times \vec{E}(x, y, t)\right] - \omega^2 \varepsilon_r^* \varepsilon_0 \vec{E}(x, y, t) = 0, \quad (17)$$

$$\nabla \times \left[\frac{1}{\varepsilon_r^* \varepsilon_0} \nabla \times \vec{H}(x, y, t)\right] - \omega^2 \mu_r \mu_0 \vec{H}(x, y, t) = 0, \quad (18)$$

 where μ_0 and μ_r are the magnetic permeability of vacuum and the relative magnetic permeability, respectively, while ε_r^* (= $n^2 - k^2 - i2nk$) is the complex dielectric constant. The associated boundary conditions are

190
$$\vec{n} \times (\vec{H}_1 - \vec{H}_2) = 0$$
 (19)

191 at the surroundings-film interface,

$$192 \qquad \vec{n} \times \vec{H} = 0 \tag{20}$$

193 at symmetry boundaries,

194
$$\sqrt{\mu_r \mu_0} (\vec{n} \times \vec{H}) + \sqrt{\varepsilon_0 \varepsilon_r^* \vec{E}} = 0$$
 (21)

195 at the film-substrate interface, and

196
$$\sqrt{\mu_0 \mu_r} (\vec{n} \times \vec{H}) + \sqrt{\varepsilon_0 \varepsilon_r^*} \vec{E} = 2\sqrt{\varepsilon_0 \varepsilon_r^*} \vec{E}_0,$$
 (22)

197 at the source surface, where \vec{n} is the normal vector to the 198 appropriate interface. Equation (21) corresponds to the im211

pedance boundary condition for a semi-infinite substrate ¹⁹⁹ while Eq. (22) is the low reflecting boundary condition to 200 model the imaginary source surface where the incident elec- 201 tromagnetic wave $\vec{E}_0 = E_0 \vec{e}_z$ is emitted and that is transparent 202 to the reflected waves. 203

Moreover, the Poynting vector $\vec{\pi}$ is defined as the cross 204 product of the electric and magnetic vectors, $\vec{\pi} = \frac{1}{2} \text{Re}\{\vec{E} \text{ 205} \times \vec{H}\}$. Its magnitude corresponds to the energy flux carried 206 by the propagating electromagnetic wave. Averaging the *x* 207 component of the Poynting vector at location (*x*, *y*) over a 208 period $2\pi/\omega$ of the EM wave gives²³ 209

$$|\pi_x|_{avg}(x,y) = -\frac{1}{2} \operatorname{Re}\{E_z H_y^*\}$$
 210

and

$$|\pi_y|_{avg}(x,y) = \frac{1}{2} \operatorname{Re}\{E_z H_x^*\}.$$
 (23)

The $H_x(x,y)\vec{e}_x + H_y(x,y)\vec{e}_y$ incident electric field $\vec{E}_0 = E_{0z}\vec{e}_z$ 213 and, therefore, the incident time-averaged Poynting vector 214 $|\vec{\pi}_0|_{avg}$ are imposed at all locations along the source surface. 215 The values of the *x* component of the Poynting vector along 216 the film-substrate interface are then calculated numerically 217 and averaged along the boundary to yield $|\pi_{x,t}|_{avg}$. The trans- 218 mittance of the thin film is then recovered by taking the ratio 219 of the transmitted film to the incident average Poynting vec- 220 tors, i.e., $T_{num} = |\pi_{x,t}|_{avg} / |\pi_{x,0}|_{avg}$. Similarly, the magnitude of 221 ^A the *x* component of the reflected time-averaged Poynting 222 vector $|\pi_{x,r}|_{avg}$ is computed numerically, and the reflectance 223 of the film is computed according to $R_{num} = |\pi_{x,r}|_{avg} / |\pi_{x,0}|_{avg}$. 224

Finally, the above equations were solved numerically us- 225 ing a commercially available finite element solver (FEMLAB 226 3.0) applying the Galerkin finite element method on unstruc- 227 tured meshes. The two-dimensional (2D) Maxwell equations 228 are solved in the frequency domain using a 2D transverse 229 electric (TE) wave formulation as described by Eq. (16). In 230 particular, the discretization uses second-order elements to 231 solve for the electric field.³³ 232

In order to validate the numerical implementation of this 233 system of equations, a system composed of a dense absorb- 234 ing thin film $(n_2=1.7, k_2)$ of thickness *L* deposited on a per- 235 fectly reflective substrate $(n_3=k_3\rightarrow\infty)$ in air $(n_1=1, k_1=0)$ 236 was simulated. The value of k_2 was varied over three orders 237 of magnitude from 0.001 to 1, and the infinitely large optical 238 constants of the substrate were imposed as $n_3=k_3=10^6$. Nor- 239 mal reflectivity of the system was computed and plotted as a 240 function of $\pi L/\lambda$.³⁰ The numerical solutions match the ana-241 lytical solutions found in Ref. 23, for example.

Figure 1 schematically shows the geometry of the simu- 243 lated nanocomposite thin film on a semi-infinite substrate. 244 The Maxwell equations are solved in both phases separately 245 as previously described. Equation (19) is used as the bound- 246 ary condition not only at the incident vacuum-film interface 247 but also at all continuous/dispersed phase interfaces. Figure 1 248 is a schematic representation of an actual model consisting of 249 three nanopores or nanowires of diameter D=10 nm and cell 250 width H of 20 nm corresponding to a volume fraction ϕ 251 $= \pi D^2/4H^2 = 0.1963$. Figure 1 also indicates material proper- 252



FIG. 1. Schematic of the physical model and the corresponding finite element grid of the absorbing nanoporous thin film along with the boundary conditions.

²⁵³ ties of the different domains and the locations at which each²⁵⁴ of the boundary conditions are applied. Note that the lines²⁵⁵ separating two adjacent cubic cells do not correspond to an²⁵⁶ actual boundary conditions.

 Finally, it is important to note that Maxwell's equations are generally applied to macroscopic averages of the fields which can vary widely in the vicinity of individual atoms where they undergo quantum mechanical effects. In addition, both the matrix and the nanodomains are treated as homoge- neous and isotropic with index of refraction n and absorption index k equal to that of the bulk.

264 III. RETRIEVAL OF EFFECTIVE COMPLEX INDEX OF 265 REFRACTION

 The effective complex index of refraction of the nano- composite thin film was retrieved by minimizing the root mean square of the relative error for the transmittance δT and reflectance δR defined as

$$\delta T^2 = \frac{1}{N} \sum_{i=1}^{N} \left[\frac{T_{\text{calc}}(\lambda_i) - T_{\text{num}}(\lambda_i)}{T_{\text{num}}(\lambda_i)} \right]^2 \text{ and}$$

271

272

$$\delta R^{2} = \frac{1}{N} \sum_{i=1}^{N} \left[\frac{R_{\text{calc}}(\lambda_{i}) - R_{\text{num}}(\lambda_{i})}{R_{\text{num}}(\lambda_{i})} \right]^{2},$$

 where $T_{\text{num}}(\lambda_i)$ and $R_{\text{num}}(\lambda_i)$ are the transmittance and reflec- tance computed numerically using FEMLAB 3.0 while $T_{\text{calc}}(\lambda_i)$ and $R_{\text{calc}}(\lambda_i)$ are the transmittance and reflectance predicted from the electromagnetic wave theory at *N* different wave-lengths λ_i between 400 and 900 nm.

 In predicting the theoretical transmittance T_{calc} and re- flectance R_{calc} from the EM wave theory, polarization effects are disregarded since (1) the incident EM wave is normal to the surface, i.e., the plane of incidence is not defined and the components of the polarization cannot be distinguished²³ and (2) scattering is neglected as the nanopores or nanowires are much smaller than the wavelength of the EM wave. In addi-tion, nonlinear optical effects are neglected and surface 301

323

waves are not observed in the current situation as resonance ²⁸⁶ modes were not excited for the materials and wavelengths ²⁸⁷ considered. Finally, we assume that all interfaces are opti- ²⁸⁸ cally smooth, i.e., surface roughness is much smaller than the ²⁸⁹ wavelength of the incident EM wave. This assumption may ²⁹⁰ not be satisfied in practice and scattering by the sometimes ²⁹¹ rough film surface can be observed. ^{34–36} ²⁹²

The Microsoft Excel Solver based on the generalized 293 reduced gradient nonlinear optimization method³⁷ was used 294 to identify the optimum n_{eff} and k_{eff} that minimizes the root 295 mean square δT and δR . The theoretical transmittance and 296 reflectance for homogeneous thin films under normal inci-297 dence are expressed as³⁸ 298

$$T_{\text{calc}}(\lambda) = \frac{\tau_{12}\tau_{23}e^{-\kappa_2 L}}{1 + 2r_{12}r_{23}e^{-\kappa_2 L}\cos(\delta_{12} + \delta_{23} - \zeta_2) + r_{12}^2r_{23}^2e^{-2\kappa_2 L}},$$
(25) 299

$$R_{\text{calc}}(\lambda) = \frac{r_{12}^2 + 2r_{12}r_{23}e^{-\kappa_2 L}\cos(\delta_{12} + \delta_{23} - \zeta_2) + r_{23}^2e^{-2\kappa_2 L}}{1 + 2r_{12}r_{23}e^{-\kappa_2 L}\cos(\delta_{12} + \delta_{23} - \zeta_2) + r_{12}^2r_{23}^2e^{-2\kappa_2 L}},$$
(26) 300

where

(24)

$$r_{ij}^{2} = \frac{(n_{i} - n_{j})^{2} + (k_{i} - k_{j})^{2}}{(n_{i} + n_{j})^{2} + (k_{i} + k_{j})^{2}}, \quad \tau_{ij} = \frac{n_{i}}{n_{j}} \frac{4(n_{i}^{2} + k_{i}^{2})}{(n_{i} + n_{j})^{2} + (k_{i} + k_{j})^{2}},$$
302

$$\tan \delta_{ij} = \frac{2(n_i k_j - n_j k_i)}{n_i^2 + k_i^2 - (n_j^2 + k_j^2)}, \quad \kappa_2 = 4\pi k_2 / \lambda, \text{ and}$$
(27)
304

$$\zeta_2 = 4\pi n_2 / \lambda \,. \tag{305}$$

Here, the subscripts 1 and 3 refer to the media above and 306 below the nanocomposite thin film treated as an effective 307 homogeneous and referred to by subscript 2. Validation of 308 the retrieval method combined with the numerically com- 309 puted transmittance was performed by simulating a dense 310 silicon absorbing thin film of thickness $L=1 \ \mu m$ surrounded 311 on both sides by vacuum $(n_1 = n_3 = 1.0, k_1 = k_3 = 0.0)$ and hav- 312 ing a constant complex index of refraction $m_2 = n_2 - ik_2 = 3.5$ 313 -i0.01 over the spectral interval from 440 to 1700 nm. The 314 values of n_2 and k_2 retrieved with the above mentioned op- 315 timization method fall within 9.0×10^{-6} % and 0.06% of the 316 input values, respectively. Therefore, both the numerical 317 simulation tool and the inverse method to retrieve the effec- 318 tive complex index of refraction of nanocomposite thin films 319 from transmittance and reflectance calculations have been 320 validated and can now be used. 321

IV. RESULTS AND DISCUSSION 322

A. Absorbing nanoporous media

Simulations of electromagnetic wave transport in nano- 324 porous absorbing SiO₂ thin film were conducted for various 325 porosities, film thicknesses, and pore shapes and sizes. First, 326 the continuous phase was assumed to be characterized by 327 constant optical properties $n_c=1.44$ and $k_c=0.01$ over the 328 spectral range from 400 to 900 nm while $n_d=n_1=1.0$, k_d 329 $=k_1=k_3=0.0$, and $n_3=3.39$. The optimization method previ- 330



FIG. 2. Evolution of the through-plane effective index of refraction and absorption index of nanoporous SiO_2 thin films as a function of L/D for films with 19.63% porosity and pore diameters of 10 and 100 nm.

 ously described was used to retrieve the through-plane effec- tive index of refraction n_{eff} and absorption index k_{eff} from the numerically computed transmittance. A numerically con- verged solution was obtained with more than 50,000 triangu- lar meshes for 250 wavelengths with a 2 nm increment. The pore diameter was 10 or 100 nm while the ratio of the film thickness *L* to pore diameter *D* varied from 10 to 200. Fi- nally, for a given pore diameter, the porosity ϕ varied from 0.0 to 0.7 by changing the dimensions of the cubic cells.

Figure 2 shows the evolution of the through-plane effec-341 tive index of refraction $n_{\rm eff}$ and absorption index $k_{\rm eff}$ as func-342 tions of the ratio L/D for a porosity ϕ equal to 0.1963. The 343 thick solid line corresponds to the predictions of the VAT 344 models given by Eqs. (12) and (13). The data points repre-345 sent the values retrieved from the numerically computed 346 transmittance by minimizing δT . As established for nonab-347 sorbing thin films,²⁴ the effective index of refraction $n_{\rm eff}$ as 348 well as the effective absorption index $k_{\rm eff}$ become indepen-349 dent of both the film thickness and the pore diameter for



FIG. 3. Root mean square δT as calculated according to Eq. (24) as a function of L/D.

350 thick enough films corresponding to L/D > 100 in the cases investigated. In addition, for porosity $\phi = 0.1963$, the VAT 351 model predicts the retrieved values of $n_{\rm eff}$ and $k_{\rm eff}$ for L/D 352 =200 within 0.13% and 0.075%, respectively. Finally, Fig. 3 353 shows the root mean square δT as a function of the ratio 354 L/D. The value of δT remains small and decreases as the 355 film thickness increases due to smoother interference fringes. 356 It also decreases as the bubble diameter decreases thanks to 357 reduction in scattering by the bubbles. For most cases (ex- 358 cept for L/D < 20 and D = 100nm), the numerical and calcu- 359 lated transmittances T_{num} and T_{calc} plotted for wavelengths 360 between 400 and 900 nm are undistinguishable. For ex- 361 ample, for D=10nm, L/D=150, and $\phi=0.3$, the maximum 362 relative error $|T_{\text{num}} - T_{\text{calc}}|/T_{\text{num}}$ is 0.07% while δT is equal to 363 2.04×10^{-4} . Note also that (i) all numerical results were con- 364 verged, i.e., independent of the number of meshes and (ii) the 365 root mean square remains relative small. Thus, the large 366 variations in $n_{\rm eff}$ and $k_{\rm eff}$ observed for small values of L/D 367 are attributed to interferences between nanopores whose ef- 368 fect tend to average out once enough pores are considered. 369 Then, beyond a critical film thickness to pore diameter ratio, 370 the medium behaves as homogeneous with some effective 371 properties. 372

Moreover, Fig. 4 compares the predictions of various 373 effective medium approaches applied to the through-plane 374 effective index of refraction $n_{\rm eff}$ and absorption index $k_{\rm eff}$ of 375 nanoporous thin films as a function of porosity for n_c 376 =1.44, k_c =0.01, n_d =1.0, k_d =0.0, D=10 nm, and L/D 377 = 150. Note that the series and reciprocity models cannot be 378computed for $k_{\rm eff}$ because $k_d = 0.0$. As intuitively expected, 379 $n_{\rm eff}$ and $k_{\rm eff}$ decrease as the porosity increases. Overall, good **380** agreement is found between the VAT model and the numeri- 381 cal results while the parallel, series, Maxwell-Garnett, and 382 reciprocity models applied to $n_{\rm eff}$ and $k_{\rm eff}$ underpredict the 383 numerical values. The same conclusions were obtained when 384 considering the effective index of refraction of nonabsorbing 385 nanoporous thin films.²⁴ Note that the values of $n_{\rm eff}$ predicted 386 by the Lorentz-Lorenz equation [Eq. (39)] fell within 0.2% 387 of the predictions of the Maxwell-Garnett model and, there- 388 fore, were omitted in Fig. 4 for the sake of clarity. In addi- 389



FIG. 4. Evolution of the through-plane effective index of refraction and absorption index as a function of porosity for nanoporous thin films with $n_c=1.44$, $k_c=0.01$, $n_d=1.0$, $k_d=0.0$, D=10 nm, and L/D=150.

³⁹⁰ tion, when the pores are open and consist of a set of alter-³⁹¹ nating columns of dispersed and continuous phase, ³⁹² perpendicular to the substrate, the dielectric constant can be ³⁹³ modeled using the parallel model given by Eq. (7).³⁰ There-³⁹⁴ fore, the VAT model for both n_{eff} and k_{eff} provides an accu-³⁹⁵ rate prediction of the effective optical properties of the nano-³⁹⁶ porous thin films simulated with various pore sizes and ³⁹⁷ porosities. The other effective property models appear not to ³⁹⁸ be appropriate for the reasons previously discussed.

 In addition, spectral calculations for nanoporous TiO_2 over the spectral range from 400 to 900 nm have been per- formed for cylindrical nanopores and nanowires of diameter D=10 nm and for porosity of 0.2146 as illustrated in Fig. 5. The overall film thickness L was such that L/D=150 to en- sure that the heterogeneous thin film behaves as homoge- neous with some effective properties. The spectral depen- dency of the complex index of refraction of bulk TiO₂ was accounted for by fitting reported experimental data^{39,40} with

^{#3} 408 a second-order polynomial to yield



FIG. 5. Morphology of simulated nanoporous with cylindrical nanopores (left) or nanowires (right) for ϕ =0.2146.

$$n_{c,\lambda} = 2.179 - 3.234 \times 10^{-4} \lambda + 7.967 \times 10^{-8} \lambda^2, \qquad (28) \ ^{409}$$

$$k_{c,\lambda} = 8.501 \times 10^{-4} + 1.264 \times 10^{-5}\lambda - 9.362 \times 10^{-9}\lambda^2,$$
(29) 410

where the wavelength λ is expressed in nanometers and var- 411 ies between 400 and 900 nm. First, the transmittance and 412 reflectance computed for cylindrical pores embedded in a 413 TiO₂ matrix and for cylindrical TiO₂ nanowires (Fig. 5) were 414 found to be identical. This indicates that beyond a critical 415 film thickness, the pore shape has no effect on the effective 416 optical properties of the nanocomposite materials as found 417 by Braun and Pilon²⁴ for nonabsorbing nanoporous thin 418 films. Note that the top surface of the thin film is optically 419 smooth and the film surface roughness due to the presence of 420 nanowires is not accounted for. 421

Finally, the theoretical transmittance and reflectance 422 were computed using Eqs. (25) and (27) for an homogeneous 423 thin film having effective spectral index of refraction and 424 absorption index predicted by the VAT model [Eqs. (12) and 425 (15)]. Figure 6 shows good agreement between the numerical 426 and theoretical transmittances and reflectances of a nano-427 porous TiO₂ thin film of porosity 0.2146. The maximum ab-428 solute errors in transmittance and reflectance were less than 0.03% and 0.0065%, respectively, and an average relative 430 error less than 3.0%. This confirms the validity of the VAT 431 model on a spectral basis for the effective complex refraction 432 of nanoporous media consisting of cylindrical pores in an absorbing matrix or of closely packed nanowires. 434

B. Dielectric medium with metallic nanowires 435

This section aims at assessing the validity of the VAT 436 model for dielectric materials or fluids containing metallic 437 nanowires. Let us consider a dielectric continuous phase of 438 complex index of refraction $m_c=1.4-i0.0$ containing gold 439 nanowires and having the same index of refraction as bulk 440 gold at 400 nm, i.e., $m_d=1.66-i1.96$.²³ Two nanowire diam- 441 eters *D* are considered namely 10 and 100 nm and, in all 442 cases, the overall film thickness *L* is such that L/D=150. 443 Then, the film can be treated as homogeneous and effective 444 properties can be defined. 445

400

500



FIG. 6. Comparison of theoretical and numerical spectral transmittance and reflectance of nanoporous TiO_2 with cylindrical nanopores and nanowires of diameter D=10 nm and porosity $\phi=0.2146$ over the wavelength range between 400 and 900 nm and film thickness L=150 D.

Wavelength, λ (nm)

600

700

800

900

446 Figure 7 compares the through-plane effective index of 447 refraction and absorption index of the nanocomposite me-448 dium retrieved from both numerical transmittance and reflec-449 tance with those predicted by the VAT model for volume **450** fraction of nanowires ϕ ranging from 0.0 to 0.7. Note that 451 the retrieved effective optical properties were obtained by **452** minimizing $\delta T + \delta R$ and were very sensitive to the initial **453** guess particularly for D=100 nm when transmittance was 454 very small. In those cases, the properties were retrieved by 455 minimizing only the root mean square δR . Overall, there 456 exist a relatively good agreement between the retrieved val-**457** ues of $n_{\rm eff}$ and $k_{\rm eff}$ at all nanowire volume fractions and for 458 both D=10 and 100 nm. The VAT model predicts the re-**459** trieved effective index of refraction $n_{\rm eff}$ within $\pm 6.2\%$ and **460** the effective absorption index k_{eff} within ±2.9%. The fact 461 that metallic nanowires have size dependent optical proper-462 ties has been ignored but can be accounted for provided that 463 these properties be measured independently.

464 Moreover, it is interesting to note that the presence of a 465 strongly absorbing dispersed phase such as metallic nano-466 wires reduces dramatically the effective index of refraction 467 of the composite medium even for small volume fractions ϕ . 468 For certain values of ϕ , the effective index of refraction n_{eff} 469 is smaller than that of either the continuous or dispersed 470 phases, i.e., $n_{\text{eff}} \leq \min(n_c, n_d)$. It also reaches a minimum at 471 the volume fraction $\phi_1=0.25$ as discussed in detail in the 472 next section. Simultaneously, the effective absorption index 473 increases significantly even for small metallic nanowire vol-474 ume fractions. Note also that if the film is thick enough for 475 the effective medium approximation to be valid, the metallic 476 nanowires can take various shapes and/or sizes without af-477 fecting the above predictions.

478 Finally, scattering by the nanopores and nanoparticles **479** can be neglected if their size is much smaller than the wave-**480** length of the incident radiation.^{41,42} A quantitative criterion



FIG. 7. Comparison between the VAT model and numerically retrieved effective index of refraction and absorption index of dielectric medium ($m_c = 1.4 - i0.0$) with embedded metallic nanowires ($m_d = 1.66 - i1.96$) for various volume fractions and nanowire diameter.

requires that the size parameter $\chi = \pi D/\lambda$ be much smaller ⁴⁸¹ than unity.⁴¹ This assumption is typically valid for absorbing ⁴⁸² nanocomposite materials and nanofluids in the visible and ⁴⁸³ infrared part of the spectrum. In the present study χ varies ⁴⁸⁴ between 0.011 and 0.25. In estimating T_{calc} and R_{calc} from the ⁴⁸⁵ EM wave theory, the fraction of energy scattered by nanop- ⁴⁸⁶ ores or nanowires was neglected compared with that trans- ⁴⁸⁷ mitted and reflected by the film along the incident direction. ⁴⁸⁸ This assumption was confirmed numerically for all reported ⁴⁸⁹ results by comparing the magnitude of the *y* component of ⁴⁹⁰ the Poynting vector perpendicular to the incident directions ⁴⁹¹ with its *x* component at all locations in the *x*-*y* plane, i.e., ⁴⁹² $|\pi_y|_{avg} \ll |\pi_x|_{avg}$.

C. Discussion of the effective VAT model

The objective of this section is to mathematically ana- 495 lyze the now numerically validated expressions of $n_{\rm eff}$ and 496 $k_{\rm eff}$ given by Eqs. (12) and (13). Their derivatives with re- 497 spect to volume fraction ϕ are expressed as 498

$$\frac{\partial n_{\text{eff}}^2}{\partial \phi} = \frac{1}{2} \left[\alpha + (A^2 + B^2)^{-1/2} (A \alpha + B \beta) \right], \tag{30}$$

500
$$\frac{\partial k_{\rm eff}^2}{\partial \phi} = \frac{1}{2} \left[-\alpha + (A^2 + B^2)^{-1/2} (A\alpha + B\beta) \right], \tag{31}$$

501 where

502
$$\alpha = \frac{\partial A}{\partial \phi} = (n_d^2 - k_d^2) - (n_c^2 - k_c^2)$$

503 and

$$\beta = \frac{\partial B}{\partial \phi} = 2(n_d k_d - n_c k_c). \tag{32}$$

505 Note that the derivatives of A and B with respect to porosity **506** ϕ denoted by α and β , respectively, are independent of po-**507** rosity. The effective properties $n_{\rm eff}$ and $k_{\rm eff}$ reach their maxi-508 mum or minimum when the first-order derivatives with re-509 spect to volume fraction vanish, i.e., when

510
$$(A^2 + B^2)^{-1/2}(A\alpha + B\beta) = -\alpha$$
 (33)

511 and

512
$$(A^2 + B^2)^{-1/2}(A\alpha + B\beta) = \alpha.$$
 (34)

513 Squaring both sides of Eqs. (33) and (34) yields the same 514 second-order polynomial in terms of the volume fraction ϕ . 515 Given the complex index of refraction of both phases, one 516 can solve for the critical volume fraction corresponding to a 517 minimum and/or maximum of the effective index of refrac-518 tion and/or absorption index. After rearrangement two roots **519** ϕ_1 and ϕ_2 can be found

520
$$\phi_1 = \frac{2[(\alpha^2 - \beta^2)n_c k_c - \alpha \beta (n_c^2 - k_c^2)]}{\beta (\alpha^2 + \beta^2)},$$
 (35)

521
$$\phi_2 = \frac{n_c k_c}{n_c k_c - n_d k_d}.$$
 (36)

522 In order to know whether $n_{\rm eff}$ and $k_{\rm eff}$ reach their maximum 523 or minimum, their second-order derivatives with respect to ϕ 524 have to be examined. Based on Eqs. (33) and (34), the **525** second-order derivatives of $n_{\rm eff}$ or $k_{\rm eff}$ are the same for ϕ_1 **526** and ϕ_2 and can be expressed as

$$\frac{\partial^2 n_{\rm eff}}{\partial \phi^2} \bigg|_{\phi_{1,2}} = \frac{1}{4n_{\rm eff}} \frac{(A\beta - B\alpha)^2}{(A^2 + B^2)^{3/2}},\tag{37}$$

528
$$\frac{\partial^2 k_{\text{eff}}}{\partial \phi^2} \bigg|_{\phi_{1,2}} = \frac{1}{4k_{\text{eff}}} \frac{(A\beta - B\alpha)^2}{(A^2 + B^2)^{3/2}}.$$
 (38)

529 Since the terms on the right-hand side of the above two equa-**530** tions are always positive, $n_{\rm eff}$ and $k_{\rm eff}$ can only reach a mini-531 mum.

532 However, for an arbitrary set of dispersed and continu-**533** ous phases, the values of ϕ_1 and ϕ_2 do not always fall in the 534 physically acceptable range of porosities between 0 and 1. **535** For positive values of the properties n_c , n_d , k_c , and k_d , one **536** can show that, unlike ϕ_1 , the second root ϕ_2 never falls **537** between 0 and 1.

Moreover, the following expressions can be used to 538 **539** identify whether ϕ_1 is the solution of Eqs. (33) or (34), i.e., **540** whether $n_{\rm eff}$ or $k_{\rm eff}$ reach a minimum at $\phi = \phi_1$

$$\chi = \frac{n_d k_d - n_c k_c}{n_c k_c (n_d^2 - k_d^2) - n_d k_d (n_c^2 - k_c^2)}.$$
(39)

If χ is strictly positive then $k_{\rm eff}$ reaches a minimum while $n_{\rm eff}$ 542 reaches a minimum if χ is strictly negative. Neither $n_{\rm eff}$ nor 543 $k_{\rm eff}$ reach a minimum if $\chi=0$. In the case of nanoporous 544 media, χ and ϕ_2 are constant and equal to -1 and 1, respec- 545 tively. Therefore $n_{\rm eff}$ can reach a minimum less than 1.0 at an 546 acceptable ϕ_1 . Finally, for the dielectric medium with em- 547 bedded metallic nanowires simulated previously, χ is strictly 548 negative and $n_{\rm eff}$ reaches a minimum. This is illustrated in 549 Fig. 7 where $n_{\rm eff}$ reaches a minimum of 1.33 at $\phi_1 = 0.25$. 550

Finally, this study constitutes the first two-dimensional 551 numerical validation for TE polarization of the VAT applied 552 to the three-dimensional Maxwell equations^{28,29} in two-phase 553 systems with dispersed domains of arbitrary shape. For com- 554 plete validation, the present study should be extended to both 555 a three-dimensional and transverse magnetic (TM) polariza- 556 tion cases. 557

V. CONCLUSIONS

The VAT models for the effective dielectric and electri- 559 cal properties of two-phase media²⁸ have been used to derive 560 the through-plane effective index of refraction $n_{\rm eff}$ and ab- 561 sorption index $k_{\rm eff}$ of nanoporous materials. Moreover, a nu- 562 merical scheme has been developed and implemented to 563 solve the Maxwell equations for a normally incident TE elec- 564 tromagnetic wave traveling through (1) nanoporous SiO₂ and 565 TiO_2 consisting of cylindrical pores or nanowires and (2) 566 dielectric medium containing cylindrical nanowires. All in- 567 terfaces were treated as optically smooth and the dispersed 568 phase volume fraction varied from 0.0 to 0.7. Calculations 569 were performed on a gray or spectral basis between 400 and 570 900 nm. The effective optical properties for the simulated 571 nanocomposite thin films were retrieved by minimizing the 572 root mean square of the relative errors for the transmittance 573 and reflectance. In all cases, the results for both $k_{\rm eff}$ and $n_{\rm eff}$ 574 are in good agreement with the predictions from the VAT 575 model. Finally, the numerically validated VAT model is dis- 576 cussed and used to predict the behavior of the optical prop- 577 erties of nanocomposite materials. It shows that under certain 578 conditions, the effective index of refraction or absorption 579 index of the composite material can be smaller than that of 580 both the continuous and dispersed phases. The same results 581 and conclusions are expected for spherical pores and nano- 582 particles. These results can be used to design and optimize 583 nanocomposite materials with tunable optical properties. As 584 well as to measure the porosity or nanowire volume fraction 585 provided that the film be thick enough to be treated as ho- 586 mogeneous with some effective properties and that all sur- 587 faces be optically smooth. 588

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