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3 **Relative roles of energy and momentum fluxes in the**
4 **tropical response to extratropical thermal forcing**

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14 **Abstract**

15 This study investigates the transient responses of atmospheric energy and momentum
16 fluxes to a time-invariant extratropical thermal heating in an atmospheric model
17 coupled to an aquaplanet mixed layer ocean with the goal of understanding the
18 mechanisms and time-scales governing the extratropical-to-tropical connection. Two
19 distinct stages are observed in the teleconnection: (1) A decrease in the meridional
20 temperature gradient in midlatitudes leads to a rapid weakening of the eddy
21 momentum flux and a slight reduction of the Hadley cell strength in the forced
22 hemisphere. (2) The subtropical trades in the forced hemisphere decrease and reduce
23 evaporation. The resulting change to sea surface temperature leads to the development
24 of a cross-equatorial Hadley cell, and the Intertropical Convergence Zone shifts to
25 the warmer hemisphere. The Hadley cell weakening in the first stage is related to
26 decreased eddy momentum flux divergence, and the response time-scale is
27 independent of the mixed layer depth. In contrast, the time taken for the development
28 of the cross-equatorial cell in the latter stage increase as the mixed layer depth
29 increases. Once developed, the deep tropical cross-equatorial cell response is an order
30 of magnitude stronger than the initial subtropical response and dominates the

31 anomalous circulation. The analysis combines the momentum and energetic
32 perspectives on this extratropical-to-tropical teleconnection and moreover shows that
33 the subtropical circulation changes associated with the momentum budget occur with
34 a time-scale that is distinct from the deep tropical response determined by the thermal
35 inertia of the tropical ocean.

36 **1. Introduction**

37 Forcings in the extratropics have been observed to influence the location of
38 tropical precipitation in modeling studies, paleo records, and 20th-century climate (e.g.
39 Kang et al. 2008, Chiang and Bitz 2005, Broccoli et al. 2006). The energetic and the
40 momentum perspectives offer two alternative approaches for studying the extratropical
41 influence on Hadley circulation (Chiang and Friedman 2012, Schneider et al. 2014,
42 Donohoe and Voigt 2017, Kang et al. 2018, Schneider and Bordoni 2008; Bordoni and
43 Schneider 2010), but these approaches have been kept largely separate from each other
44 in previous studies. Our goal is to combine both approaches to evaluating the transient
45 circulation responses to an idealized perpetual extratropical thermal forcing in order to
46 build towards a mechanistic understanding of tropical circulation responses to
47 extratropical forcings.

48 The underlying principle of the energetic framework is that the Hadley
49 circulation alters in such a way as to accommodate the interhemispheric transfer of
50 atmospheric energy as demanded by the extratropical forcing (Kang et al. 2008).

51 Moist static energy (MSE, $m = C_p T + gz + Lq$) in the upper troposphere is slightly
52 larger than the near-surface atmosphere because the gravitational potential energy

53 (gz) in the upper troposphere is much greater than in the near-surface atmosphere,
54 more than compensating the larger specific heat ($C_p T$) and latent heat (Lq) in the low-
55 level atmosphere. Also, eddy contribution to meridional energy transport in the
56 tropics is usually negligible. Therefore, the total atmospheric MSE transport in tropics
57 tends to have the opposite direction as the mass transport in the lower branch of the
58 Hadley cell. Kang et al. (2009) define the moist stability, $\Delta m \equiv \frac{F}{v_2}$, where $F = \langle \overline{mv} \rangle$
59 is the vertically integrated zonal-mean meridional atmospheric energy transport and
60 v_2 is the mass transport of the lower branch of the Hadley circulation. With this
61 convention, the sign of Δm is positive when energy is transported in the direction of
62 the low level flow. Hence the gross moist stability in the tropics is negative. Since the
63 variation in gross moist stability, the amount of energy transported per unit mass
64 transport, is usually small (Kang et al. 2009, Hill et al. 2015), the changes of energy
65 transport are accomplished via Hadley cell adjustments. An interhemispheric contrast
66 in the energy source tends to induce an anomalous cross-equatorial streamfunction,
67 with the upper branch transporting the gravitational potential energy towards the
68 hemisphere being cooled and the lower branch transporting mass and moisture
69 towards the hemisphere being warmed. The Intertropical Convergence Zone (ITCZ) is

70 expected to lie near the “energy flux equator”, where the atmospheric meridional
71 energy flux changes sign (Kang et al. 2008; Schneider et al. 2014; Kang 2020).

72 This framework has been usefully applied to interpret the tropical precipitation
73 responses to various extratropical forcings, such as imposed sea ice or ice sheet (Chiang
74 and Bitz 2005; Cvijanovic and Chiang 2013), anthropogenic aerosol emission
75 (Yoshimori and Broccoli 2009; Hwang et al. 2013), freshwater hosing in North Atlantic
76 (Zhang and Delworth 2005; Broccoli et al. 2006), excessive insolation related to cloud
77 biases in the Southern Ocean (Hwang and Frierson 2013), and forcing atmospheric
78 models with energy flux at the surface (q-flux) (Broccoli et al. 2006; Kang et al. 2009).

79 Another perspective points to the importance of the interaction between Hadley
80 circulation and eddies from a momentum perspective (Becker et al. 1997; Kim and Lee
81 2001; Walker and Schneider 2006; Schneider and Bordoni 2008; Bordoni and
82 Schneider 2010). The underlying idea is that variations in midlatitude eddies result in
83 momentum flux convergence changes in the subtropics that are compensated by
84 changes to the tropical overturning circulation. Starting with the Reynolds-averaging
85 inviscid momentum equation, assuming steady-state, and neglecting vertical advection
86 and vertical eddy terms, one can obtain an approximate balance equation between eddy

87 momentum flux divergence (\bar{S}), zonal-mean meridional advection of planetary vorticity
88 ($f \cdot \bar{v}$), and relative vorticity ($\bar{\zeta} \cdot \bar{v}$) in the upper troposphere:

89
$$(f + \bar{\zeta})\bar{v} = f(1 - Ro)\bar{v} \approx \frac{1}{a \cos^2 \vartheta} \frac{\partial}{\partial \vartheta} (\cos^2 \vartheta \overline{u'v'}) \equiv \bar{S} \quad (1.1)$$

90 where overbars $\bar{\cdot}$ indicate time mean and zonal mean. The equation suggests that the
91 eddies play a dominant contribution to the momentum budget if the Rossby number
92 ($Ro = -\bar{\zeta}/f$) is small.

93 The influence of eddy momentum flux ($\overline{u'v'}$) on the strength of Hadley cell and
94 monsoon circulation has been reported in the statistical analyses of interannual
95 variability (Caballero 2007; Walker and Schneider 2006), the inter-model spread of
96 general circulation model (GCM) biases (Caballero 2008), and a series of idealized
97 GCM experiment with changing the latitude of maximum radiative-equilibrium surface
98 temperature (Schneider and Bordoni 2008; Bordoni and Schneider 2010).

99 The energetic and momentum perspectives offer independent explanations for the
100 extratropical influence on Hadley circulation (Chiang and Friedman 2012; Kang 2020).
101 Given a hemispheric asymmetric extratropical forcing, the energetic perspective
102 predicts an anomalous cross-equatorial response in the deep tropics, shifting the Hadley

103 cell center and displacing the ITCZ. In contrast, the momentum perspective highlights
104 the balance between the Hadley cell strength and eddy momentum flux divergence in
105 the subtropics, where the Rossby number is small and vertical advection of momentum
106 flux is negligible. In order for this perspective to apply to the entire tropics, Schneider
107 (2006) used Eq.1.1 to classify different regimes of the Hadley circulation: a
108 momentum-conserving regime that responds directly to thermal forcing (Lindzen and
109 Hou 1988) and a small Rossby number regime that the circulation strength is largely
110 determined by eddies (Walker and Schneider 2006). The transition of the two regimes
111 has been used to interpret an abrupt development of a cross-equatorial monsoonal cell
112 (Schneider and Bordoni 2008; Bordoni and Schneider 2010).

113 Our goal is to deduce mechanisms for the Hadley circulation responses to
114 extratropical forcings. There are two aspects that makes our study unique: first, we
115 combine the analysis of both the energetic and momentum budgets in the same
116 experimental setting, and second we analyze the transient situation in order to
117 determine cause and effect, keeping in mind that budgets provide only diagnostic
118 relationships. Previous studies that investigated transient responses to extratropical
119 forcings mostly only focus on air-sea coupling feedback mechanisms and energy

120 transport (e.g. Dong and Sutton 2002, Chiang and Bitz 2005, Chiang et al. 2008,
121 Cvijanovic and Chiang 2012, Woelfle et al. 2015). On the other hand, previous studies
122 that evaluated momentum budget (e.g. Caballero 2007, Schneider and Bordoni 2008;
123 Bordoni and Schneider 2010) report statistical relationships between Hadley cell
124 strength and eddy momentum flux divergence, but in such cases the causal relationship
125 can only be assumed. Merlis et al. (2012) investigated both the angular momentum
126 balance and energy balance in simulations with varying orbital precession and found
127 the Hadley circulation responses to be energetically constrained. However, similar to
128 studies focusing on the seasonal cycle, the radiative forcings are not confined to
129 extratropics in their experiments.

130 We also modify the mixed layer depth in our simulations to examine what sets the
131 time-scale of the teleconnection. Previous studies using an energetic approach reported
132 a 1~2 year response time for wind-evaporation-sea surface temperature (SST) feedback
133 to induce significant tropical SST and circulation changes in simulations with realistic
134 mixed layer depth, and it has been assumed that the time-scale arises from the thermal
135 inertia of the mixed layer (e.g. Dong and Sutton 2002, Chiang and Bitz 2005, Chiang
136 et al. 2008, Cvijanovic and Chiang 2012, Woelfle et al. 2015). This assumption

137 however discounts a potential contribution from extratropical atmospheric circulation
138 changes independent of the mixed layer. By varying the mixed-layer depth and
139 changing the time-scale of the teleconnection, we provide an experimental situation
140 that further reveals the relative roles of energy and momentum to the teleconnection.

141 Because of the very small signal to noise ratio of the initial tropical circulation
142 responses to extratropical thermal forcing, we decide to simplify the experimental setup
143 by using an aquaplanet without seasonality. The setup and the detailed calculations
144 provided in section 2 allows us to cleanly diagnose the transient evolution without the
145 complication of the seasonal cycle or the influence of stationary eddies. We explore the
146 equilibrium and the transient responses in both the energetic and momentum
147 frameworks in section 3. We find that the tropical circulation responses exhibit two
148 distinct stages: (1) an initial subtropical response that occurs rapidly and can be
149 interpreted via the momentum perspective and (2) a deep tropical circulation
150 adjustment that is strongly dependent on mixed layer depth and are consistent with the
151 energetic perspective. A mechanism for the initial stage triggering the deep tropical
152 circulation adjustments is proposed. In section 4, we summarize our findings and

- 153 discuss the necessity for constructing a model hierarchy to systematically understand
- 154 the mechanisms with various time-scales.

155 **2. Methods**

156 **2.1 Model setup**

157 We use an aquaplanet version of Geophysical Fluid Dynamics Laboratory (GFDL)
158 Atmospheric Model 2.1 (AM2.1; Anderson et al. 2004; Delworth et al. 2006) coupled
159 with a motionless mixed layer ocean that allows thermodynamic atmosphere-ocean
160 interactions. The horizontal resolution of the model is 2° latitude \times 2.5° longitude, and
161 the vertical resolution of the model is 24 levels. There is no seasonal cycle, a fixed
162 surface albedo (i.e. no sea ice or snow feedback), and steady insolation is applied,
163 varying only with latitude so that it provides the present-day Earth's annual mean
164 insolation at all times. The insolation is computed based on an obliquity of 23.5 degrees.

165 **2.2 Experimental design**

166 A set of experiments is performed with prescribed extratropical thermal forcing and
167 varying mixed layer depth. The extratropical thermal forcing is applied between 50°S
168 and 80°S by directly adding a source of heat into the oceanic mixed layer energy budget
169 equation, as specified analytically in Eq. 2.1 below and Figure 1a. Unlike Kang et al.
170 (2008) and Kang et al. (2009), we only prescribe forcing in one hemisphere, allowing

171 us to track the evolution of heating originated from one location. This forcing is
172 representative of ocean heat uptake or ocean heat release in a changing climate, or
173 changes in other components that would affect net radiation at the surface, such as sea
174 ice, aerosol, and clouds. The equation of the imposed heating, denoted H , is

$$175 \quad \begin{cases} H = -A \sin\left(\frac{\phi+50^\circ}{30^\circ}\pi\right) & \text{For } -80^\circ < \phi < -50^\circ, \\ H = 0 & \text{otherwise,} \end{cases} \quad (2.1)$$

176 where A sets the maximum strength of the forcing (W m^{-2}) and ϕ is latitude in
177 degrees. To obtain significant transient responses with limited ensemble members, we
178 select a relatively large value of A , 60 W m^{-2} , so that a total of 2.12PW is added to the
179 mixed layer. The imposed hemispherically asymmetric forcing is about half of the
180 range of the earth's seasonal cycle. Indeed, the single cross-equatorial cell in the
181 equilibrium response (Figure 1c) implies our findings may offer insights for
182 understanding seasonal cycle transition, while not changing insolation in the tropics
183 directly and focusing on the extratropical influence. The strong forcing, however, does
184 raise the question of relevance of our results to climate change signals, the latter which
185 tends to be a lot smaller in magnitude. We have performed other cases with A being
186 30 W m^{-2} or 10 W m^{-2} , and the equilibrium responses are qualitatively similar, albeit
187 smaller in magnitude.

188 To investigate the role of SST in setting the response time-scales, we perform cases
189 with 50m (MLD50), 100m (MLD100), and 200m (MLD200) mixed layer depth. Since
190 the magnitudes of the initial midlatitude temperature and wind responses depend on
191 mixed layer depth, we set the same mixed layer depth in the forced region to 200m in
192 all experiments and only alter the mixed layer depth elsewhere. The unrealistically deep
193 mixed layer depths (i.e. 200m) outside the forced region allow us to cleanly separate
194 the processes solely related to atmospheric dynamics and those involving air-sea
195 interactions. We have additionally performed a case with observed zonal mean annual
196 mean mixed layer depth, which amounts to about 35m in the tropics (25°S~25°N). The
197 proposed two-stage responses can be also found in the case with observed mixed layer
198 depth, with the response time-scales being similar to the case with 50m mixed layer
199 depth.

200 The control case with 50m mixed layer depth and no prescribed forcing is run for 36
201 years. The 60 ensemble members of MLD200 cases are run for 3 years and 5 of them
202 are extended to 48 years, reaching equilibrium around year 10. The MLD100/50
203 experiments are also ran for 3 years, but only 30 ensemble members are run.

204 **2.3 Indices**

205 The Southern Hemisphere Hadley cell index (φ_{SH}) is defined to be the averaged
 206 mass streamfunction between 15°S~25°S at 700hPa, measuring the strength of the
 207 extreme of the Hadley circulation in the Southern Hemisphere. The cross-equatorial
 208 Hadley cell index (φ_{EQ}) is calculated by averaging the mass streamfunction between
 209 5°S~5°N at 700hPa. The altitude 700hPa is chosen because the maximum of mass
 210 streamfunction appears in this altitude in the control climate.

211 The ITCZ is generally co-located with the ascending branch of Hadley circulation
 212 and is thus tightly linked with cross-equatorial circulation. Following Adam et al.
 213 (2016a), the location of ITCZ is calculated as

$$214 \quad \varphi_{ITCZ} = \frac{\int_{\varphi_1}^{\varphi_2} \varphi [\cos(\varphi)P(\varphi)]^N d\varphi}{\int_{\varphi_1}^{\varphi_2} [\cos(\varphi)P(\varphi)]^N d\varphi}, \quad (2.2)$$

215 where $N=10$, $\varphi_1 = 20^\circ\text{S}$, $\varphi_2 = 20^\circ\text{N}$, and P represents the zonal mean precipitation
 216 at the latitude φ .

217 Another index that is representative of the behavior of Hadley circulation is the
 218 energy flux equator, the latitude where the vertical column integrated zonal mean
 219 energy transport $\langle \overline{vm} \rangle$ vanishes (Kang et al. 2018).

220 Previous studies suggested that the boundary layer cross-equatorial flow, as well
 221 as the anomalous cross-equatorial Hadley cell, are driven by cross-equatorial SST
 222 gradients (Lindzen and Nigam 1987; Chang et al. 2000; Chiang and Bitz 2005;
 223 Cvijanovic and Chiang 2013). Here we define the interhemispheric asymmetric SST
 224 index (Δ_{SST}) as the SST difference between EQ~10°S and EQ~10°N to measure the
 225 interhemispheric SST asymmetry in the deep tropical region.

226 To investigate eddy activity responses to the imposed forcing, we calculate
 227 Eliassen-Palm flux (E-P flux) in log-pressure and spherical coordinates (as in
 228 Andrews 1987):

$$229 \quad F^\phi \equiv \rho_R \cos \phi \left[\bar{u}_z \frac{\overline{v'\theta'}}{\bar{\theta}_z} - \overline{u'v'} \right]$$

$$230 \quad F^z \equiv \rho_R \cos \phi \left[\left\{ f - \frac{(\bar{u} \cos \phi)_\phi}{a \cos \phi} \right\} \frac{\overline{v'\theta'}}{\bar{\theta}_z} - \overline{u'w'} \right] \quad (2.3)$$

231 Here, ϕ is latitude and $z = -H \ln(p/p_R)$, where $H=7.5\text{km}$, p is pressure and p_R is
 232 a reference pressure. The overbar denotes zonal mean and time mean. $\rho_R =$
 233 $\rho_0 \exp(-Z/H)$ where ρ_0 is a constant. f is the Coriolis coefficient and subscripts ϕ, z
 234 denote partial derivatives.

235 **3. Results**

236 **3.1 Equilibrium responses**

237 We first present the equilibrium responses, calculated by averaging the last 30
238 years of each simulation. For all figures in this paper, only signals that are statistically
239 significant are shown. The anomalous warming is most apparent at the heating location
240 and extends to the tropics, shifting ITCZ southward (Figures 1b and 1d). The imposed
241 heating decreases the meridional temperature gradient of the southern subtropics and
242 weakens the subtropical jet in the Southern Hemisphere (defined as the latitude of the
243 zonal wind maximum of the entire tropics, which is located around 200 hpa) (Figure
244 1c). In the Northern Hemisphere, surface temperature decreases slightly in the
245 subtropics and is nearly unchanged in extratropics. The northern subtropical jet is
246 strengthened. The temperature, precipitation, and circulation responses in Figure 1 are
247 nearly identical in the cases with different mixed layer depth. Increasing mixed layer
248 depth has little influence on the equilibrium responses, consistent with Kang et al.
249 (2008). In the next two sections, we take MLD200 case as an example to demonstrate
250 the equilibrium responses in the momentum and the energetics perspectives.

251 **3.1.1 Equilibrium responses in the momentum perspective**

252 In the control case, the eddy momentum flux convergence peaks at around 40°N
253 and 40°S (blue shading in Figure 2a, see also the climatological E-P flux in Figure 1c),
254 where the eddy driven jets located (defined as the latitudes of maximum zonal wind at
255 850hPa). In the subtropics, the eddy stress, the horizontal eddy momentum flux
256 divergence ($S \equiv \frac{1}{a \cos^2 \vartheta} \frac{\partial}{\partial \vartheta} (\cos^2 \vartheta \overline{u'v'})$), is balanced by meridional advection of
257 absolute vorticity in the upper branch of the Hadley cell, with the poleward flows in the
258 upper branches collocated with positive S (Figure 2a; refer to Eq.1.1 for the momentum
259 balance).

260 The steady-state responses of circulation and momentum fluxes in our
261 experiments are consistent with previous studies demonstrating the influence of eddies
262 on Hadley cell via varying insolation (Bordoni and Schneider 2008; Schneider and
263 Bordoni 2008; Bordoni and Schneider 2010), interannual variability (Caballero 2007),
264 or on the spread of GCMs' climatological biases (Caballero 2008). In subtropics, the
265 variations in eddy stress are accompanied by variations in Hadley cell strength. When
266 imposing heating in the southern extratropics, eddy stress and Hadley cells weaken in
267 the southern tropics and strengthen in the northern tropics (compare Figures 2a and 2b
268 or see Figure 2c for anomalies).

269 3.1.2 Equilibrium responses in the energetics perspective

270 Driven by the uneven distribution of insolation, the atmosphere transports energy
271 poleward in both hemispheres in the control case (black line in Figure 3a). In
272 extratropics, eddies transport both DSE and moisture poleward. In most of the tropics,
273 the mean meridional overturning circulation plays the main role of transporting energy
274 away from ITCZ, with the poleward DSE transport in the upper troposphere
275 outweighing the equatorward moisture transport near the surface (red and blue lines in
276 Figure 3a).

277 The equilibrium responses of energy fluxes in Figures 3b and 3c are consistent with
278 previous modeling studies with various extratropical forcings (Kang et al. 2008; Kang
279 et al. 2009; Swann et al. 2011; Hwang et al. 2013; Chiang and Friedman 2012;
280 Schneider et al. 2014) and can be understood via the energetic framework. In a stable
281 atmosphere, the total atmospheric energy transport (or MSE transport) is in the same
282 direction as the DSE transport but in the opposite direction to moisture transport.
283 Responding to the imposed heating in the Southern Hemisphere, the Hadley cell
284 transports excessive energy to the Northern Hemisphere. Both the energy flux equator
285 and the ITCZ shift southward (Figures 1d and 3b).

286 3.2 Transient responses

287 Figure 4 shows the evolution of SST and circulation in all three experiments
288 during the first three years after imposing the time-invariant extratropical forcing. To
289 allow a direct comparison with the steady-state responses in Figure 1, time slices of
290 year 9 of the experiments when the system approaches equilibrium are plotted in the
291 same format (in the right columns). The propagation speed of the anomalous warming
292 depends on latitudes, with the subtropical region ($\sim 20^{\circ}\text{S}$) warming faster than the
293 surrounded latitudes. The dependency of propagation speed on latitudes suggests
294 atmospheric circulation (instead of diffusive processes) playing a critical role in the
295 teleconnection between the tropics and extratropics. Two distinct stages of the tropical
296 meridional mass streamfunction responses are observed – a weakening centering at
297 around 20°S occurring at around month 4 for all three experiments and an anomalous
298 cross-equatorial cell develops later. We define the start time of the first stage as the day
299 when the change of the strength of the southern cell ($\delta\varphi_{SH}$) becomes detectable¹. The

¹ Follow Deser et al. 2012, we evaluate when the ensemble mean anomalies of the targeted index first become detectable at the 95% significant level, using a 2-sided Student's t-test, where the spread is computed using the individual simulation anomalies from all ensemble members and each ensemble member's indices are assumed to be independent. A 15-day running mean is applied when plotting the

300 day of the anomalous cross-equatorial cell ($\delta\varphi_{EQ}$) first becomes significant marks the
301 start time of Stage 2. As shown in Figure 5, the time-scale for observing statistically
302 significant weakening of the southern cell (Stage 1) is independent of mixed layer depth,
303 whereas the time-scale for developing a statistically significant anomalous cross-
304 equatorial cell (Stage 2) increases with mixed layer depth. Once developed, the
305 anomalous cross-equatorial cell strengthens throughout the simulations and dominate
306 the equilibrium responses.

307 In the following two sections, we take the MLD200 case as an example to
308 demonstrate that the two distinct stages of the tropical circulation responses are driven
309 by different mechanisms. The southern subtropical responses in the first stage can be
310 interpreted by the momentum perspective, and the deep tropical responses in the second
311 stage are mostly consistent with the energetic perspective.

312 **3.2.1 Transient responses from the momentum perspective**

313 Figure 6a shows the time series of anomalous eddy momentum divergence (i.e. eddy
314 stress, δS) and the product of Coriolis parameter and anomalous upper-level

time series of individual ensemble members (in Figures 6 and 7). The smoothing has little influence on the start time quantified here.

315 meridional wind ($\delta f \bar{v}$). Poleward of 15 degrees, where local Rossby number ($Ro \equiv$
316 $-\bar{\zeta}/f$) is smaller than 0.4, variations of eddy momentum flux divergence (δS) are
317 mostly balanced by anomalous zonal-mean meridional advection of planetary
318 vorticity ($\delta f \bar{v}$) (see Eq. 1.1). For example, at Stage 1, anomalous positive eddy stress
319 (red color centering around 45°S) is balanced by anomalously positive planetary
320 vorticity advection ($\delta f \bar{v}$, solid contours), and anomalous negative eddy stress (blue
321 color centering around 25°S) is balanced by anomalously negative planetary vorticity
322 advection ($\delta f \bar{v}$, dashed contours). The Coriolis parameter f is negative in Southern
323 Hemisphere, so anomalously negative planetary vorticity advection (i.e., negative
324 $\delta f \bar{v}$) in southern subtropics is consistent with reduced northerly in the upper level and
325 the weakened (more positive) southern Hadley cell (Figure 6b). After entering Stage 2
326 and throughout the whole simulation, any variation of Hadley cell strength
327 (demonstrated as $\delta f \bar{v}$ in the Figure 6a) poleward of 15 degrees is always
328 accompanied by a variation of eddy stress ($\overline{\delta S}$) with the same sign.

329 The momentum balance does not indicate a causal relationship. Through imposing
330 idealized forcing confined in the extratropics and investigating the transient evolutions
331 of the responses in experiments with varying mixed layer depth, we attribute the initial

332 weakening of southern Hadley cell (φ_{SH}) in Stage 1 to reduced eddy momentum flux
333 divergence (\bar{S}) in the subtropics. The imposed surface heating at 50°~80°S could lead
334 to a reduction of \bar{S} in the southern subtropics via a baroclinic and a barotropic process
335 (See Shaw et al. 2020 and the Appendix for more detailed description of the two
336 processes). Further analyses show the baroclinic process dominates: Both the stability
337 near the surface and the meridional temperature gradient decrease at the equatorward
338 side of the imposed heating, reducing eddy heat flux in the climatological baroclinic
339 zone (around 45 °S). Associated with the reduction of eddy source, poleward eddy
340 momentum flux and its divergence (\bar{S}) in the subtropics also decrease (Figure A1).

341 Although the equilibrium responses of momentum fluxes in subtropics discussed in
342 Section 3.1.1 fulfill the momentum balance between Hadley cell strength (φ_{SH}) and
343 eddy stress (\bar{S}), our investigation of the transient evolutions suggests the equilibrium
344 responses are distinct from Stage 1 eddy-momentum driven response in terms of
345 latitudinal positions and strengths (compare the equilibrium responses on the right
346 column to the Stage 1 responses on the left in Figure 6). Moreover, there is a noticeable
347 recovery stage in between. We defer the interpretations of the recovery stage, which

348 involve interactions among SST, eddy stress (\bar{S}), and Hadley cell strength, to the end
349 of section 3.2.3.

350 Note that the signal to noise ratios of these eddy-driven responses are small. After
351 applying a 15-day running mean to remove high frequency internal variability in
352 individual ensemble members, the spread of anomalous eddy stress ($\overline{\delta S}$) across
353 ensemble members still reaches $1.3 \times 10^{-5} \text{ m/s}^2$, which is larger than the y-axis in
354 Figure 6c. The spread of anomalous southern Hadley cell strength among ensemble
355 members is also much larger compared with the change in ensemble mean. While we
356 are able to demonstrate the existence of Stage 1 using 60 ensemble members,
357 identifying the time-scale of Stage 1 is not possible for individual ensemble members.
358 It remains an open question as to how the eddy-driven mechanism discussed above
359 plays a role in individual realizations. When accessing the spread across the ensemble
360 members, there is a statistically significant positive correlation ($R=0.6$) between
361 anomalous eddy stress ($\overline{\delta S}$) and anomalous Hadley cell strength ($\delta\varphi_{SH}$) at the time the
362 ensemble-mean responses entering Stage 1, indicating the two factors dominating the
363 momentum balance at this stage.

364 **3.2.2 Transient responses from the energetic perspective**

365 For the MLD200 case, there is no significant change in energy transport and meridional
366 mass streamfunction in the deep tropics before month 13. The development of the cross-
367 equatorial cell at the 2nd stage is tightly linked with the anomalous interhemispheric
368 SST gradient in the tropics ($\delta \Delta_{SST}$). When the anomalous interhemispheric SST
369 gradient in the tropics ($\delta \Delta_{SST}$) becomes significant (at month 13), the anomalous mass
370 streamfunction develops and the energy flux equator shifts southward (Figures 7b and
371 7c). There is an approximate 3-month lag between the cross-equatorial cell and the shift
372 of the energy flux equator. Further analysis shows a close linkage between the energy
373 flux equator, the cross-equatorial MSE transport, and the ITCZ. The three variables all
374 lag the anomalous mass streamfunction ($\delta \varphi_{EQ}$) by three months for the MLD200
375 setting (quantitative analyses not shown, but precipitation and energy flux equator
376 responses are plotted in Figures 7a and 7d). Once they all become statistically
377 significant, the southward shift of the energy flux equator and the anomalous cross-
378 equatorial cell are consistent with the energetics framework.

379 Our transient analysis suggests that it is only when the southern tropical SST heats
380 sufficiently and the ITCZ shifts that the extratropical energy supply can be exported to
381 the other hemisphere across the equator (Cvijanovic and Chiang 2012). With a deeper

382 mixed layer, it takes longer for the SSTs to adjust, causing Stage 2 responses to emerge
383 with a larger lag (Figure 5). The SST gradients drive the anomalous cross-equatorial
384 cell, and the MSE transport adjust accordingly. Wei and Bordoni (2018) and Wei and
385 Bordoni (2020) also emphasize a crucial role of SST gradient, reporting the migration
386 of ITCZ lagging the variation of energy flux equator during the climatological seasonal
387 cycle. In our Stage 2 responses, both the changes in cross-equatorial cell and the
388 meridional mean circulation component of the cross-equatorial MSE transport occur at
389 the time when the anomalous interhemispheric SST gradient ($\delta \Delta_{SST}$) become
390 statistically significant. The 3-month lag between the energy flux equator and the
391 anomalous interhemispheric SST gradient is explained by the eddy component of the
392 MSE transport².

393 Note that the signal-to-noise ratio of the anomalous cross-equatorial streamfunction in
394 Stage 2 is larger than that of the anomalous southern cell strength in Stage 1 (Figure

² The eddy component dominates the meridional MSE transport right around the ITCZ region in AM2, which differs from observation. The lead-lag relationship reported here could be a result of this model bias, therefore, we only emphasize the key role of SST gradient in determining the response time-scale of the cross-equatorial cell. Echoing the take-home message in Wei and Bordoni (2018), one needs to be caution when applying the energetic framework to interpret the responses in shorter time-scales. The transient evolution of the cross-equatorial cell could be different from the transient evolution of the MSE transport.

395 6b). While the time-scale of developing a cross-equatorial cell cannot be accurately
396 quantified in a single ensemble, the characteristics of the anomalous cross-equatorial
397 cell are detectable for all ensemble members. There is a statistically significant positive
398 correlation ($R=0.8$) between the anomalous interhemispheric asymmetric SST index
399 ($\delta \Delta_{SST}$) and the strength of anomalous cross-equatorial cell $\delta\varphi_{EQ}$ at the time the
400 ensemble mean response entering Stage 2, supporting the crucial role of SST gradient.
401 The anomalous interhemispheric SST gradient ($\delta \Delta_{SST}$), the strength of anomalous
402 cross-equatorial Hadley cell ($\delta\varphi_{EQ}$), and the cross-equatorial MSE transport all
403 strengthen with a constant rate before approaching the new equilibrium state (not
404 shown). The equilibrium state in the right columns in Figure 7 could simply be
405 interpreted as a fully developed response of Stage 2.

406 **3.2.3 Connecting the two stages: the role of wind-evaporation-SST feedback**

407 In this section, we discuss how the weakening of southern Hadley cell in Stage 1
408 may lead to the cross-equatorial cell in Stage 2 via the wind-evaporation-SST feedback.

409 Through careful inspection of the transient evolution (Figure 7) and comparison
410 among the three experiments of different mixed layer depth (Figure 5), the time-scale
411 for developing the cross-equatorial cell appears to be tightly linked with the

412 interhemispheric SST gradient. Following Xie et al. (2010), Jia and Wu (2013), and
413 Hwang et al. (2017), we combine the mixed layer energy budget and the linearized
414 version of the aerodynamic bulk formula of latent heat flux

$$415 \quad \rho c_p H \frac{\partial T}{\partial t} = \delta SW + \delta LW + \delta LH_{wind} + \delta LH_{SST} + \delta LH_{RH} + \delta LH_{dT} + \delta SH$$

416 to analyze the surface energy budget in Southern Hemisphere subtropics to explore
417 factors influencing SST. ρ is the density of seawater, c_p is the specific heat of
418 seawater, H is mixed layer depth, T is the mixed layer temperature (equal to the SST),
419 and the symbols δ on the right-hand side denote anomalies, calculated as the
420 difference of the heating experiment (at the month of interest) and the control
421 experiment. δSW is anomalous net downward shortwave radiation, δLW is
422 anomalous net downward longwave radiation, δSH is anomalous sensible heat flux,
423 δLH_{wind} , δLH_{SST} , δLH_{RH} , and δLH_{dT} respectively are anomalous latent heat flux
424 associated with changes in surface wind speed, SST, relative humidity, and the stability
425 of the boundary layer (the difference between surface temperature and 2m air
426 temperature).

427 Figure 8a suggests that changes in latent heat flux related to changes in wind speed
428 (δLH_{wind}) is the main factor contributing to the heating tendency in southern tropics.

429 This role of wind speed suggests a link between the momentum-driven Stage 1 and the
430 energetic related Stage 2. We hypothesize that weakening of eddy stress \bar{S} in Stage 1
431 could lead to the cross-equatorial Hadley cell through the following four steps,
432 illustrated in Figure 9: (1) The reduction of \bar{S} at the edge of the southern cell is
433 balanced by the reduced planetary vorticity advection due to reduced poleward flow at
434 the upper branch. (2) To satisfy momentum balance in the subtropics, the reduction of
435 \bar{S} aloft must be balanced by the reduction of friction at the surface, requiring weakened
436 surface easterlies. Consistently, by mass continuity, the meridional component of
437 surface wind weakens with the weaker poleward flow in the upper branch. The
438 weakened southeasterly surface wind results in decreasing evaporation. (3) Reduced
439 evaporation at the surface leads to increasing SST in the southern tropics, driving the
440 cross-equatorial Hadley cell. (4) As the cross-equatorial Hadley cell strengthens, the
441 upper branch transports energy northward. The cross-equatorial Hadley cell also leads
442 to a subtle increase in surface wind speed and evaporation in the northern tropics, which
443 further enhances the interhemispheric SST gradient and the cross-equatorial Hadley
444 cell. In this view, the anomalous eddy stress ($\delta\bar{S}$) in the upper troposphere, anomalous
445 Hadley cell in southern subtropics, and reduced evaporation are connected, supporting

446 the hypothesis linking the momentum and the energetic perspective via the wind-
447 evaporation-SST feedback.

448 The large ensemble spreads in Figure 8a and Figure 6b question if the linkage
449 between Stage 1 and Stage 2 described above explains the transition in individual
450 ensemble members. While we cannot exclude the possibility of other mechanisms
451 triggering the development of the cross-equatorial cell in individual ensemble members,
452 an evaluation across the ensemble members supports our hypothesis. At the start time
453 of Stage 2 defined from the ensemble mean, 56 out of 60 ensemble members simulate
454 the anomalous cross-equatorial cell in the deep tropics. Among these 56 ensemble
455 members, all but 2 exhibit an anomalously weak southern Hadley cell and surface wind
456 speed in the southern subtropics.. The two exceptions that do not exhibit weakening of
457 the southern Hadley cell despite having developed a cross equatorial Hadley cell
458 anomaly had previously exhibited an extended period with a weakened southern Hadley
459 cell. This suggest that while it is difficult to pinpoint the onset of stage 1 in and
460 individual integration, it appears that if the Southern Hadley cell weakens over some
461 suitable integration period, it may be enough to initiate stage 2.

462 A closer examination reveals that, before the anomalous cross-equatorial cell fully
463 develops and the southern Hadley cell almost diminishes, there is an intermediate stage
464 that the eddy stress (\bar{S}) and the Hadley cell in the southern subtropics recover in the
465 ensemble mean time series (see Figure 6, as described in Section 3.2.1). We suspect
466 this intermediate stage can be explained by the feedback among the SST gradient, the
467 eddy stress, and the Hadley cell strength in the subtropics. The wind-evaporation-SST
468 feedback discussed in the previous paragraph is strongest at around 25°S. As a result,
469 SST in the region warms more rapidly than other latitudes, leading to an increasing
470 meridional SST gradient on the polar side and decreasing meridional SST gradient on
471 the equatorward side (Figure 4). The increasing SST gradient on the polar side is
472 accompanied by increasing eddy heat and momentum fluxes (not shown), the eddy
473 stress (\bar{S}) and the southern Hadley cell thus re-strengthen (Figures 6b and 6c). The re-
474 strengthening reduces the wind-evaporation-SST feedback and the anomalously
475 positive meridional SST gradient eventually diminishes. The duration of the recovery
476 stage increases with the mixed layer depth (Figure 4), supporting the role of SST.

477 **4. Summary and Discussion**

478 The atmospheric circulation responses to extratropical thermal forcing are
479 investigated using GFDL AM2.1 coupled to a mixed layer ocean, through an analysis
480 of the transient responses to an abrupt imposition of the forcing. Our result suggests
481 two distinct stages of the response (as demonstrated in Figure 10).

482 **(a) Stage 1: Hadley cell in the forced hemisphere weakens**

483 Surface temperature in the forced region increases after the surface heating in the
484 Southern Hemisphere high latitudes is imposed. The imposed high latitude heating
485 decreases meridional temperature gradient and boundary-layer stability in midlatitudes
486 and subtropics, leading to a reduction of both eddy heat flux and momentum flux
487 (Figure 10c). The southern cell thus weakens to balance the reduction of eddy
488 momentum flux divergence in the subtropics (Figure 10a). The anomalous Hadley
489 circulation is limited to the Southern Hemisphere in this stage, and there is very little
490 change in tropical SST and precipitation (Figure 10g). While the idea of extratropical
491 eddy influencing the strength of Hadley cell is not new, the causal relationship is clearer
492 in our simulations compared with previous studies. For studies investigating seasonal
493 cycles (i.e. Bordoni and Schneider 2010), the insolation in the tropics varies, therefore,

494 it is difficult to identify the root cause for variation of local Rossby number and thus
495 the abrupt transition of the monsoon circulations. Similarly, the positive correlation
496 between Hadley cell strength and eddy stress demonstrated in Caballero (2008) among
497 a group of global climate models does not indicate a causal relationship. In our
498 simulations, the imposed extratropical forcing is the root cause of all of the responses.
499 In addition, the time-scale for Stage 1 responses is independent of mixed layer depth
500 (Figure 5), supporting the interpretation that this stage being controlled by atmospheric
501 momentum flux changes.

502 **(b) Stage 2: cross-equatorial Hadley cell responses**

503 The reduction of eddy momentum flux divergence in Stage 1 also leads to
504 decreasing easterly trades at the surface (Figure 10e), reducing evaporation and
505 resulting in warmer SST in the SH subtropics. Once the anomalous warming propagates
506 to deep tropics and the inter-hemispheric temperature gradient becomes significant, an
507 anomalous cross-equatorial cell develops and the tropical precipitation shifts southward
508 (Figures 10b, 10f, 10h). The cross-equatorial cell is confined in the deep tropics, where
509 angular momentum is nearly constant. Once developed, the anomalous cross-equatorial
510 cell is an order of magnitude stronger than the anomalous Hadley circulation in Stage

511 1. The larger signal-to-noise ratio in the second stage may explain why the energetic
512 framework has more support in the literature than the momentum perspective. The
513 equilibrium responses are qualitatively similar to the responses in Stage 2. The
514 momentum balance of the equilibrium responses can be explained by the momentum
515 advection of the cross-equatorial Hadley cell – the Hadley cell and the eddy stress
516 weaken in southern tropics and strengthen in northern tropics. The response time-scale
517 of the anomalous cross-equatorial cell is roughly proportional to mixed layer depth
518 (Figure 5), suggesting the critical roles of air-sea interactions and boundary layer
519 processes in triggering the cross-equatorial cell. The necessity of using the
520 thermodynamic perspective to explain the anomalous Hadley cell strength in the deep
521 tropics is consistent with Singh et al. 2017. Through comparing two idealized
522 simulations with and without large-scale eddies, they suggested the upper layer eddy
523 momentum flux may affect boundary layer entropy (and thus the strength of Hadley
524 cell) by inducing a low-level frictional flow that reduces the ability of the Hadley cell
525 to transport heat poleward.

526 The particular model configuration employed in our study was key to revealing the
527 complex transient evolutions of the extratropical-to-tropical teleconnection. This is

528 unlike the tropical-to-extratropical teleconnection, whose pathway and time-scale
529 could be understood via anomalous stationary planetary wave propagation generated
530 from Rossby wave sources resulting from convective changes in the tropical Pacific
531 (Wallace and Gutzler 1981; Hoskins and Karoly 1981). Once developed, the planetary
532 scale stationary wave patterns are steady, unless there are variations in background
533 wind. The two-stage transient evolution of the tropical responses to extratropical
534 thermal forcings reported in our study might be less relevant for a single tropical
535 weather event triggered by extratropical perturbation. They could be, however, crucial
536 for understanding the decadal variabilities or the transient evolution of
537 anthropogenically forced climate change in the tropics. For transient climate
538 responses, i.e. 1% increase CO₂ or standard RCP forcing scenarios, it is likely that
539 mechanisms with various time-scales all playing a role in shaping the forced
540 responses.

541 Our experimental setup and a large number of ensemble members allow us to
542 reveal the two-stage mechanisms operating in the inter-annual time-scale that are not
543 represented in simplified models with fixed SST (or relaxing toward an equilibrium
544 SST), while isolating the roles of stationary waves and ocean dynamics. A more careful

545 and systematic evaluation of the magnitudes and time-scales of various mechanisms
546 through a hierarchy of numerical models of the atmosphere-ocean-land system is
547 important to obtain a full picture understanding of extratropical influences on tropical
548 climate. Some open questions that can be addressed using models with different
549 complexity include:

550 (1) The influence of seasonality: Eddies are stronger in the winter hemisphere.
551 However, the influence of eddy momentum flux may be more apparent for the
552 weak summer Hadley cell in the subtropics, where the Rossby number is small
553 and the Hadley cell is closer to an eddy-driven regime (Eq. 1.1; Kang and Lu
554 2012). It is yet to be explored how would the time-scales for the two stages vary
555 in simulations with seasonally varying insolation.

556 (2) The influence of zonal asymmetry: In our zonally symmetric aquaplanet model,
557 the surface boundary is covered by a uniform mixed layer ocean. The eddy-
558 mean flow interactions may be damped by the large thermal inertia of the mixed
559 layer ocean, as the mean circulation is strongly constrained by SST. In a more
560 realistic configuration, the small heat capacity of landmasses and the shallow
561 mixed layer depth in the eastern oceanic basins may allow stronger feedback

562 between eddy momentum flux and regional mean circulations, which then
563 strengthen the responses in the momentum-driven stage (Stage 1). In addition,
564 including zonal asymmetry also induces zonal variations of storm tracks and
565 eddy momentum flux, allowing eddies to affect local Hadley cell. The wind-
566 evaporation-SST mechanism may be more concentrated in the eastern basins,
567 where the climatological trades are more organized and the mixed layer depth
568 is shallower, altering the time-scale of the tropical responses.

569 (3) The influence of dynamical ocean: We have not considered the role of the
570 dynamical ocean, which is reported to damp the tropical atmospheric
571 circulation responses in many recent studies (Deser et al. 2015; Kay et al. 2016;
572 Tomas et al. 2016; Hawcroft et al. 2017; Kang et al. 2018). While we do not
573 expect changes in ocean dynamics playing critical roles for Stage 1 responses,
574 the time-scale of the cross-equatorial Hadley cell response may be affected by
575 the damping mechanism of Ekman transport (Schneider 2014, Green and
576 Marshall 2017, Kang et al. 2018). Through investigating responses in long
577 simulations (more than 50 years) in fully coupled models, Wang et al. (2018),
578 Lin (2020), and Kang et al. (2020) further suggest a hemispherically symmetric

579 Hadley cell response emerge as some oceanic processes affect SST along the
580 cold tongue, potentially overwhelming the Stage 2 cross-equatorial cell
581 responses in decadal time-scales.

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589 are publicly available at <https://doi.org/10.6084/m9.figshare.12978476>

590 **Appendix**

591 **Changes in wave activities**

592 Section 3.2.1 explains changes in eddy momentum flux divergence ($\delta\bar{S}$) in the
593 subtropics via E-P flux. Here, we investigate factors contributing to variations in E-P
594 flux.

595 The initial warming in the forced region weakens the climatological pattern of eddy
596 heat and momentum flux, as indicated by the downward pointing arrows in
597 midlatitudes and equatorward pointing arrows in subtropics. The weakening could be
598 observed soon after imposing the forcing (before the occurrence of Stage 1) and is
599 amplified throughout the simulations.

600 **a. The baroclinic mechanism – a reduction of wave source**

601 Based on Eq.2.3, the horizontal heat flux ($\overline{v'\theta'}$), the stability ($\bar{\theta}_z$), and the vertical
602 eddy momentum flux $\overline{v'w'}$ can all influence the vertical component of E-P flux. The
603 Imposed heating reduces the temperature gradient (blue contours in Figure A1(e)) and
604 thus leads to the weakening of poleward eddy heat flux (red contours in Figure
605 A1(e)). Also, the imposed heating propagates horizontally and vertically, increasing
606 temperature at around 750hpa more than those near the surface. The lower

607 tropospheric stability between 30°S~60°S increases (blue contours in Figure A1(f)).
608 Both reducing horizontal heat flux and increasing stability contribute positivity to the
609 reduction of the vertical component of E-P flux. The contribution from vertical eddy
610 momentum flux is an order of magnitude smaller (not shown). We hypothesize that
611 the reduction of baroclinicity on the equatorward side of the forcing reduces the wave
612 source near the surface and thus decreases the momentum flux aloft. The reduction of
613 wave sources and the associated momentum flux changes are consistent with those in
614 global warming simulations, although the initial triggers differ (Frierson 2008; Lorenz
615 and DeWeaver 2014).

616 **b. The barotropic mechanism – eddy mean flow interactions**

617 Another possible explanation for the weakening of eddy momentum flux divergence
618 at the edge of the Hadley cell is the barotropic eddy-mean flow interaction mechanism
619 (Chen et al. 2008; Lu et al. 2008). As shown in Figure A2, we do not find it to be the
620 key mechanism leading to the reduction of eddy momentum flux divergence (\bar{S}) in
621 the subtropics. As reviewed by Shaw (2020), the mechanism is as follow: The
622 imposed warming modifies the meridional temperature gradient in the baroclinic
623 zone. Through thermal wind adjustments, zonal mean zonal wind alters. The eddy

624 phase speed is expected to change, which shifts the critical latitudes (where
625 background zonal mean zonal wind equals eddy phase speed) and affects eddy
626 momentum flux divergence (\bar{S}). While imposing heating does lead to decreasing
627 temperature gradient and reducing zonal mean zonal wind in midlatitudes in our
628 simulation, the eddy phase speed does not change significantly. The limited influence
629 of the background wind on the eddy phase speed is likely due to the baroclinic zone
630 being more equatorward (around 40°S) than the regions with strong background wind
631 speed change (50°S~60°S). The zonal mean zonal wind changes in the subtropics are
632 also small in Stage 1. The largest contribution of anomalous eddy momentum flux
633 appears to arise from eddies with the phase speeds that are similar to that contribute to
634 most of the eddy momentum flux in the control case, implying changes in eddy
635 momentum flux may be originated from changes in eddy sources described in the
636 baroclinic mechanism.

637 **References**

- 638 Adam, O., T. Bischoff, and T. Schneider, 2016: Seasonal and Interannual Variations of
639 the Energy Flux Equator and ITCZ. Part I: Zonally Averaged ITCZ Position.
640 *Journal of Climate*, **29**, 3219-3230.
- 641 Andrews, D. G., 1987: On the interpretation of the Eliassen- Palm flux
642 divergence. *Quarterly Journal of the Royal Meteorological Society*, *113*(475),
643 323-338.
- 644 Becker, E., G. Schmitz, and R. GeprÄGs, 1997: The feedback of midlatitude waves
645 onto the Hadley cell in a simple general circulation model. *Tellus A*, **49**, 182-199.
- 646 Bordoni, S., and T. Schneider, 2008: Monsoons as eddy-mediated regime transitions of
647 the tropical overturning circulation. *Nature Geoscience*, **1**, 515-519.
- 648 ———, 2010: Regime Transitions of Steady and Time-Dependent Hadley Circulations:
649 Comparison of Axisymmetric and Eddy-Permitting Simulations. *Journal of the*
650 *Atmospheric Sciences*, **67**.
- 651 Broccoli, A., K. Dahl, and S. Ronald, 2006: Response of the ITCZ to Northern
652 Hemisphere cooling. *Geophysical Research Letters - GEOPHYS RES LETT*, **33**.

- 653 Caballero, R., 2007: Role of eddies in the interannual variability of Hadley cell strength.
654 *Geophysical Research Letters*, **34**.
- 655 —, 2008: Hadley cell bias in climate models linked to extratropical eddy stress.
656 *Geophysical Research Letters*, **35**.
- 657 Chang, P., R. Saravanan, L. Ji, and G. C. Hegerl, 2000: The Effect of Local Sea Surface
658 Temperatures on Atmospheric Circulation over the Tropical Atlantic Sector.
659 *Journal of Climate*, **13**, 2195-2216.
- 660 Chen, G., J. Lu, and D. M. W. Frierson, 2008: Phase speed spectra and the latitude of
661 surface westerlies: Interannual variability and global warming trend. *Journal of*
662 *Climate*, *21*(22), 5942-5959.
- 663 Chiang, J. C. H., and C. M. Bitz, 2005: Influence of high latitude ice cover on the marine
664 Intertropical Convergence Zone. *Climate Dynamics*, **25**, 477-496.
- 665 Chiang, J. C. H., and A. R. Friedman, 2012: Extratropical Cooling, Interhemispheric
666 Thermal Gradients, and Tropical Climate Change. *Annual Review of Earth and*
667 *Planetary Sciences*, **40**, 383-412.

668 Chiang, J. C. H., W. Cheng, and C. M. Bitz, 2008: Fast teleconnections to the tropical
669 Atlantic sector from Atlantic thermohaline adjustment. *Geophysical Research*
670 *Letters*, **35**.

671 Cvijanovic, I., and J. C. H. Chiang, 2013: Global energy budget changes to high latitude
672 North Atlantic cooling and the tropical ITCZ response. *Climate Dynamics*, **40**,
673 1435-1452.

674 Delworth, T. L., and Coauthors, 2006: GFDL's CM2 Global Coupled Climate Models.
675 Part I: Formulation and Simulation Characteristics. *Journal of Climate*, **19**, 643-
676 674.

677 Deser, C., R. A. Tomas, and L. Sun, 2015: The Role of Ocean–Atmosphere Coupling
678 in the Zonal-Mean Atmospheric Response to Arctic Sea Ice Loss. *Journal of*
679 *Climate*, **28**, 2168-2186.

680 Deser, C., A. Phillips, V. Bourdette, and H. Teng, 2012: Uncertainty in climate change
681 projections: the role of internal variability. *Climate Dynamics*, **38**, 527-546.

682 Dong, B.-W., and R. T. Sutton, 2002: Adjustment of the coupled ocean–atmosphere
683 system to a sudden change in the Thermohaline Circulation. *Geophysical*
684 *Research Letters*, **29**, 18-11-18-14.

685 Donohoe, A., and A. Voigt, 2017: Why Future Shifts in Tropical Precipitation Will
686 Likely Be Small: Patterns and Mechanisms. 115-137.

687 Frierson, D. M., 2008: Midlatitude static stability in simple and comprehensive
688 general circulation models. *Journal of the atmospheric sciences*, 65(3), 1049-1062.

689 Green, B., & J. Marshall, 2017: Coupling of trade winds with ocean circulation damps
690 ITCZ shifts. *Journal of Climate*, 30(12), 4395-4411.

691 Hawcroft, M., J. M. Haywood, M. Collins, A. Jones, A. C. Jones, and G. Stephens,
692 2017: Southern Ocean albedo, inter-hemispheric energy transports and the double
693 ITCZ: global impacts of biases in a coupled model. *Climate Dynamics*, 48, 2279-
694 2295.

695 Hill, S. A., Ming, Y., & I. M. Held, 2015: Mechanisms of forced tropical meridional
696 energy flux change. *Journal of Climate*, 28(5), 1725-1742.

697 Hoskins, B. J., and D. J. Karoly, 1981: The Steady Linear Response of a Spherical
698 Atmosphere to Thermal and Orographic Forcing. *Journal of the Atmospheric*
699 *Sciences*, 38, 1179-1196.

700 Hwang, Y.-T., and D. M. W. Frierson, 2013: Link between the double-Intertropical
701 Convergence Zone problem and cloud biases over the Southern Ocean.
702 *Proceedings of the National Academy of Sciences*, **110**, 4935.

703 Hwang, Y.-T., D. M. W. Frierson, and S. M. Kang, 2013: Anthropogenic sulfate aerosol
704 and the southward shift of tropical precipitation in the late 20th century.
705 *Geophysical Research Letters*, **40**, 2845-2850.

706 Hwang, Y.-T., S.-P. Xie, C. Deser, and S. M. Kang, 2017: Connecting tropical climate
707 change with Southern Ocean heat uptake. *Geophysical Research Letters*, **44**, 9449-
708 9457.

709 Jia, F., and L. Wu, 2013: A Study of Response of the Equatorial Pacific SST to
710 Doubled-CO₂ Forcing in the Coupled CAM-1.5-Layer Reduced-Gravity Ocean
711 Model. *Journal of Physical Oceanography*, **43**, 1288-1300.

712 Kang, S. M., D. M. W. Frierson, and I. M. Held, 2009: The Tropical Response to
713 Extratropical Thermal Forcing in an Idealized GCM: The Importance of Radiative
714 Feedbacks and Convective Parameterization. *Journal of the Atmospheric Sciences*,
715 **66**, 2812-2827.

716 Kang, S. M., Y. Shin, and S.-P. Xie, 2018: Extratropical forcing and tropical rainfall
717 distribution: energetics framework and ocean Ekman advection. *npj Climate and*
718 *Atmospheric Science*, **1**, 20172.

719 Kang, S. M., I. M. Held, D. M. W. Frierson, and M. Zhao, 2008: The Response of the
720 ITCZ to Extratropical Thermal Forcing: Idealized Slab-Ocean Experiments with
721 a GCM. *Journal of Climate*, **21**, 3521-3532.

722 Kang, S. M., and J. Lu, 2012: Expansion of the Hadley cell under global warming:
723 Winter versus summer. *Journal of Climate*, **25**, 8387-8393.

724 Kang, S. M., 2020: Extratropical Influence on the Tropical Rainfall Distribution.
725 *Current Climate Change Reports*, **6**, 24-36.

726 Kang, S. M., S.-P. Xie, Y. Shin, H. Kim, Y.-T. Hwang, M. F. Stuecker, B. Xiang, M.
727 Hawcroft: Walker Circulation Response to Extratropical Radiative Forcing.
728 *Science Advances*, in revision

729 Kay, J. E., C. Wall, V. Yettella, B. Medeiros, C. Hannay, P. Caldwell, and C. Bitz, 2016:
730 Global Climate Impacts of Fixing the Southern Ocean Shortwave Radiation Bias
731 in the Community Earth System Model (CESM). *Journal of Climate*, **29**, 4617-
732 4636.

733 Kim, H.-k., and S. Lee, 2001: Hadley Cell Dynamics in a Primitive Equation Model.
734 Part II: Nonaxisymmetric Flow. *Journal of the Atmospheric Sciences*, **58**, 2859-
735 2871.

736 Lin, Y.-C., 2020: The fast and slow components of the tropical Pacific climate response
737 to extratropical forcings in a fully coupled model, *National Taiwan University*,
738 master thesis

739 Lindzen, R. S., and S. Nigam, 1987: On the Role of Sea Surface Temperature Gradients
740 in Forcing Low-Level Winds and Convergence in the Tropics. *Journal of the*
741 *Atmospheric Sciences*, **44**, 2418-2436.

742 Lindzen, R. S., and A. V. Hou, 1988: Hadley Circulations for Zonally Averaged
743 Heating Centered off the Equator. *Journal of the Atmospheric Sciences*, **45**, 2416-
744 2427.

745 Lorenz, D. J., and E. T. DeWeaver, 2007: Tropopause height and zonal wind response
746 to global warming in the IPCC scenario integrations. *Journal of Geophysical*
747 *Research: Atmospheres*, **112**(D10).

748 Lu, J., G. Chen, and D. M. W. Frierson, 2008: Response of the zonal mean atmospheric
749 circulation to El Niño versus global warming. *Journal of Climate*, 21(22), 5835-
750 5851.

751 Schneider, Tapio, 2006: The general circulation of the atmosphere. *Annual Review of*
752 *Earth and Planetary Sciences* 34.

753 Schneider, T., and S. Bordoni, 2008: Eddy-Mediated Regime Transitions in the
754 Seasonal Cycle of a Hadley Circulation and Implications for Monsoon Dynamics.
755 *Journal of the Atmospheric Sciences*, **65**, 915-934.

756 Schneider, T., T. Bischoff, and G. H. Haug, 2014: Migrations and dynamics of the
757 intertropical convergence zone. *Nature*, **513**, 45-53.

758 Shaw, T. A., 2019: Mechanisms of future predicted changes in the zonal mean mid-
759 latitude circulation. *Current Climate Change Reports*, 5(4), 345-357.

760 Swann, A., I. Fung, and J. Chiang, 2011: Mid-latitude afforestation shifts general
761 circulation and tropical precipitation. *Proceedings of the National Academy of*
762 *Sciences of the United States of America*, **109**, 712-716.

763 The, G. G. A. M. D. T., and Coauthors, 2004: The New GFDL Global Atmosphere and
764 Land Model AM2–LM2 Evaluation with Prescribed SST Simulations. *Journal of*
765 *Climate*, **17**, 4641–4673.

766 Tomas, R. A., C. Deser, and L. Sun, 2016: The Role of Ocean Heat Transport in the
767 Global Climate Response to Projected Arctic Sea Ice Loss. *Journal of Climate*, **29**,
768 6841–6859.

769 Walker, C. C., and T. Schneider, 2006: Eddy Influences on Hadley Circulations:
770 Simulations with an Idealized GCM. *Journal of the Atmospheric Sciences*, **63**,
771 3333–3350.

772 Wallace, J. M., and D. S. Gutzler, 1981: Teleconnections in the Geopotential Height
773 Field during the Northern Hemisphere Winter. *Monthly Weather Review*, **109**,
774 784–812.

775 Wang, K., Deser, C., Sun, L., & R. A. Tomas, 2018: Fast response of the tropics to an
776 abrupt loss of Arctic sea ice via ocean dynamics. *Geophysical Research*
777 *Letters*, **45**(9), 4264–4272.

778 Wei, H.-H., and S. Bordoni, 2018: Energetic Constraints on the ITCZ Position in
779 Idealized Simulations With a Seasonal Cycle. *Journal of Advances in Modeling*
780 *Earth Systems*.

781 Wei, H. H., & S. Bordoni, 2020: Energetic Constraints on the ITCZ position in the
782 Observed Seasonal Cycle from MERRA-2 Reanalysis. *Geophysical Research*
783 *Letters*, e2020GL088506.

784 Woelfle, M. D., C. S. Bretherton, and D. M. W. Frierson, 2015: Time scales of response
785 to antisymmetric surface fluxes in an aquaplanet GCM. *Geophysical Research*
786 *Letters*, **42**, 2555-2562.

787 Xie, S.-P., C. Deser, G. A. Vecchi, J. Ma, H. Teng, and A. T. Wittenberg, 2010: Global
788 Warming Pattern Formation: Sea Surface Temperature and Rainfall. *Journal of*
789 *Climate*, **23**, 966-986.

790 Yoshimori, M., and A. J. Broccoli, 2009: On the link between Hadley circulation
791 changes and radiative feedback processes. *Geophysical Research Letters*, **36**.

792 Zhang, R., and T. L. Delworth, 2005: Simulated Tropical Response to a Substantial
793 Weakening of the Atlantic Thermohaline Circulation. *Journal of Climate*, **18**,
794 1853-1860.

795

796 **Figure Caption List**

797 **Figure 1. Equilibrium responses of surface temperature, precipitation, and**
798 **atmospheric circulations.** (a) Latitudinal distribution of imposed forcing H (W/m^2).
799 (b) The zonal mean SST in all heating cases. (c) Anomalous zonal wind (shaded,
800 m/s), anomalous meridional mass streamfunction (green contours, $\text{CI} = 10^{11} \text{ kg}/\text{s}$) in
801 equilibrium in MLD200 case, and climatological zonal wind (black contours, $\text{CI} = 15$
802 m/s , zero contour omitted and negative dashed), and climatological E-P fluxes
803 (vectors, m^2/s^2). (d) Same as (b), but for precipitation.

804 **Figure 2. Equilibrium responses of circulation and momentum fluxes.** Zonal
805 mean of S (shaded, m/s^2) and mass streamfunction (green contours, with $\text{CI} =$
806 $10^{11} \text{ kg}/\text{s}$, solid for positive and dashed for negative contour, and grey contours for
807 zero) (a) in the control case, (b) in the MLD200 case, and (c) the anomalies (the
808 MLD200 case minus control). S in the control case are plotted as black contours (with
809 $\text{CI} = 10^{-5} \text{ m}/\text{s}^2$ zero contour omitted and negative dashed) in (c) for reference.

810 **Figure 3. Equilibrium responses of energy transports.** Northward atmospheric
811 energy transports (PW) (a) in the control case, (b) in the MLD200 case, and (c)
812 anomalies (the MLD200 case minus control), with total MSE transport in black,

813 contribution from DSE in red, contribution from moisture in blue. Note that in the
814 range of y axes are different between (a)(b) and (c).

815 **Figure 4. Time series of zonal mean meridional mass streamfunction and SST.**

816 Anomalous zonal mean meridional mass streamfunction at 700hPa (shaded, kg/s) and
817 SST (grey contours, CI = 0.3 °C, zero contour omitted and negative dashed) in cases
818 with (a) 200MLD, (b) 100MLD, and (c) 50 MLD. The vertical grey solid lines mark
819 the start times of Stage 1 and 2. The horizontal red lines indicate the northern edge of
820 imposed forcing. The right column shows the near-equilibrium responses.

821 **Figure 5. The start time of Stage 1 & 2.** The start time of Stage 1 (cross) and 2
822 (asterisk) in MLD 200/100/50 cases.

823 **Figure 6. Time series of Stage 1-associated responses in MLD200 case.**

824 Anomalous zonal mean (a) daily S (shaded, m/s^2) and daily f_v (blue contours with CI
825 = $5 \times 10^{-6} \text{ 1/s}^2$, zero contour omitted and negative dashed) in the upper atmosphere
826 (above 700hPa), (b) daily Southern Hemisphere Hadley cell (φ_{SH} , kg/s), (c) daily S
827 above 700hPa and between $15^\circ\text{S} \sim 25^\circ\text{S}$ (m/s^2), and (d) daily surface wind speed
828 between $15^\circ\text{S} \sim 25^\circ\text{S}$ (m/s). The vertical solid lines mark the start times of Stage 1 and
829 2. The right column shows the near-equilibrium responses. In (a), the horizontal red

830 line indicates the northern edge of imposed forcing and the horizontal grey lines mark
831 the latitude of 0.4 local Rossby number. The thick black lines in (b)~(d) indicate the
832 ensemble mean, with each ensemble in grey. Note that in (c), the range of y axes are
833 different between the left and right panel. The time series are smoothed by 15-day
834 running mean to remove high frequency internal variability.

835 **Figure 7. Time series of Stage 2-associated responses in MLD200 case.**

836 Anomalous zonal mean (a) northward MSE transport (shaded, PW), SST (grey
837 contours with CI = 0.3 °C, zero contour omitted and negative dashed), and anomalous
838 precipitation (contour = 1, 2, 4, 8, 16 mm/day, positive purple and negative green), (b)
839 daily cross-equatorial Hadley cell index (φ_{EQ} , kg/s), (c) daily interhemispheric
840 asymmetric SST index (Δ_{SST} , °C), and (d) energy flux equator (EFE, °). The vertical
841 solid lines mark the start times of Stage 1 and 2. The right column shows the near-
842 equilibrium responses. The horizontal red line in (a) indicates the northern edge of
843 imposed forcing. The thick black lines in (b)~(d) indicate the ensemble mean, with
844 each ensemble in light grey. Note that in (b)~(d), the range of y axes are different
845 between the left and right panels. The time series of daily data are smoothed by 15-
846 day running mean to remove high frequency internal variability.

847 **Figure 8. WES feedback.** (a) Mixed layer energy budget attribution in southern
848 tropical region (between the equator and the southern edge of the Hadley cell in the
849 SH, 27°S) during Stage 1 period. The errorbars mark the one standard deviation
850 departure from the ensemble mean of each variable. Anomalous (b) surface latent heat
851 flux due to wind change (W/m^2) and (c) surface shortwave flux (W/m^2) in SH tropical
852 region. The vertical dashed lines in (b) and (c) mark the start times of Stage 1 and 2,
853 respectively. The right column shows the near-equilibrium responses. The thick black
854 lines in (b)~(c) indicate the ensemble mean, with each ensemble in light grey.

855 **Figure 9. Schematic diagram of the two-stage response.** The upper panel shows the
856 anomalous mass stream function at 700 hPa (shaded, power of 10 kg/s), anomalous S
857 over 700hPa (light blue contours, $\text{CI} = 10^{-6} \text{ m}/\text{s}^2$), and northward DSE transport
858 anomaly (brown contours, $\text{CI} = 0.5 \text{ PW}$). The lower panel shows the latent heat
859 anomaly due to wind change (shaded, W/m^2), SST anomaly (yellow contours, $\text{CI} =$
860 0.3K), and northward moisture transport anomaly (brown contours, energy equivalent,
861 $\text{CI} = 0.5 \text{ PW}$, zero and positive are omitted). The blue and orange contours in vertical
862 panels show the anomalous mass streamfunction in two stages respectively ($\text{CI} =$
863 3×10^9 (left) and 2.4×10^{10} (right) kg/s).

864 **Figure 10. Two-stage responses of the MLD200 case.** (a) Anomalous zonal wind
865 (shaded, m/s), anomalous meridional mass stream function (green contours, with CI =
866 3×10^9 kg/s, zero contour omitted and negative dashed), and local absolute angular
867 momentum (grey contours, with CI = $\omega a^2/10$, ω is the angular speed, and a is the
868 radius of the Earth), (c) anomalous S (shaded, m/s^2) and E-P flux (vector, m^2/s^2), (e)
869 anomalous zonal mean zonal wind (m/s, plotted in blue) and meridional wind (m/s,
870 plotted in red), climatological zonal mean zonal wind (m/s, plotted in light blue) and
871 meridional wind (m/s, plotted in light red), and (g) anomalous zonal mean
872 precipitation (mm/day, plotted in blue) and surface temperature ($^{\circ}C$, plotted in red) in
873 Stage 1. (b)(d)(f)(h) are same as (a)(c)(e)(g), but for Stage 2. The CI of green contours
874 in (b) is 1.2×10^{10} kg/s, which is much larger than that in (a). The Stage 1 responses
875 refer to the differences between the average of the time period between the two start
876 dates of Stage 1 and 2 and the climatology. The Stage 2 responses are defined as the
877 differences between the average of the first year after the start date of Stage 2 and the
878 average of the time period between the two start dates of Stage 1 and 2.

879 **Figure A1. Responses of E-P flux and its divergence.** Climatological E-P flux
880 (arrows), divergence of E-P flux (shading, m/s^2), vertical gradient of potential

881 temperature (blue contours, K/m, with IC = 0.001 , zero contour bolded and negative
882 dashed), (a) eddy heat flux (red contours in left panel, Km/s, with IC = 2) and (b)
883 meridional gradient of potential temperature (red contours, K/m, with IC = 40).
884 Anomalous E-P flux, divergence of E-P flux, vertical gradient of potential
885 temperature (blue contours, K/m, with IC = 0.0001), (c) eddy heat flux (red contours
886 in left panel, Km/s, with IC = 1) and (d) meridional gradient of potential temperature
887 (red contours, K/m, with IC = 1). (e)-(h) as in (c)-(d) but (e)-(f) in Stage 1 and (g)-(h)
888 in Stage 2.

889 **Figure A2. Responses of zonal wind and eddy momentum flux.** Zonally average
890 zonal wind at 300hPa divided by $\cos\theta$ (heavy lines, m/s, solid line is climatology and
891 dashed line is ensemble mean of the MLD200 heating case), climatological (shading,
892 m^2/s^2) and anomalous (contours, with CI = 0.05 m^2/s^2 , zero contour omitted and
893 negative dashed) eddy momentum flux in Stage 1 at 300hPa. The hatching denotes
894 the significance at 95% confidence level.

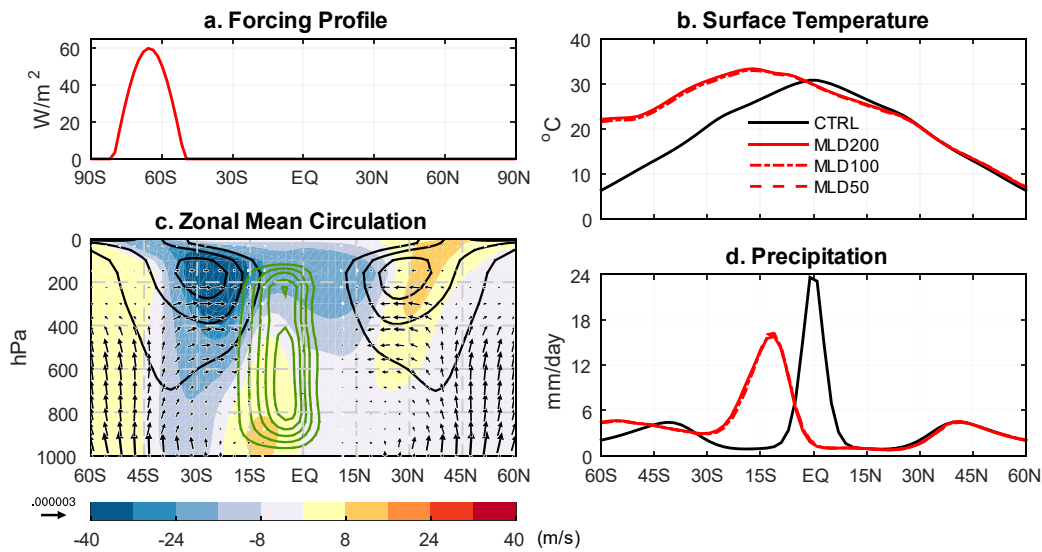


Figure 1. Equilibrium responses of surface temperature, precipitation, and atmospheric circulations. (a) Latitudinal distribution of imposed forcing H (W/m^2). (b) The zonal mean SST in all heating cases. (c) Anomalous zonal wind (shaded, m/s), anomalous meridional mass streamfunction (green contours, $\text{CI} = 10^{11} \text{ kg}/\text{s}$) in equilibrium in MLD200 case, and climatological zonal wind (black contours, $\text{CI} = 15 \text{ m}/\text{s}$, zero contour omitted and negative dashed), and climatological E-P fluxes (vectors, m^2/s^2). (d) Same as (b), but for precipitation.

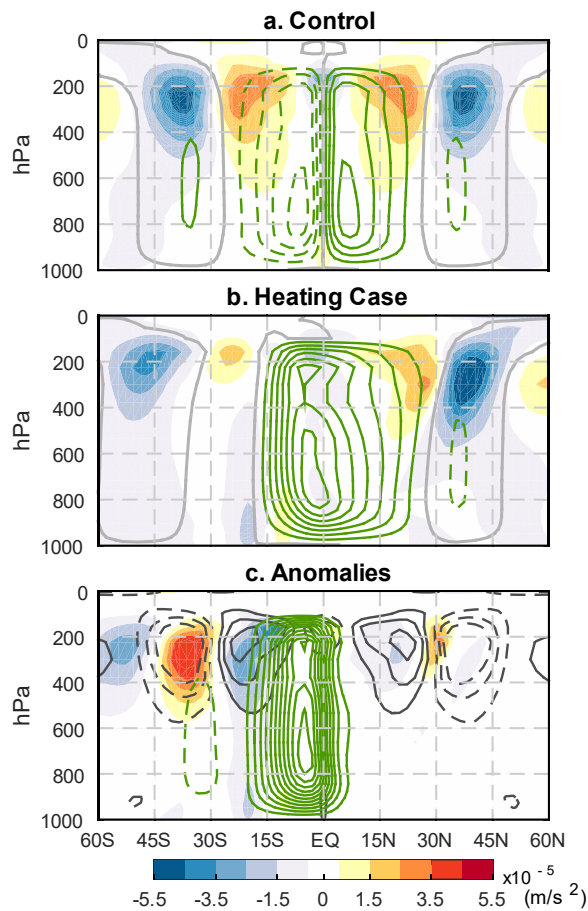


Figure 2. Equilibrium responses of circulation and momentum fluxes. Zonal

mean of S (shaded, m/s^2) and mass streamfunction (green contours, with $\text{CI} = 10^{11} \text{kg/s}$, solid for positive and dashed for negative contour, and grey contours for

zero) (a) in the control case, (b) in the MLD200 case, and (c) the anomalies (the

MLD200 case minus control). S in the control case are plotted as black contours (with

$\text{CI} = 10^{-5} \text{m/s}^2$ zero contour omitted and negative dashed) in (c) for reference.

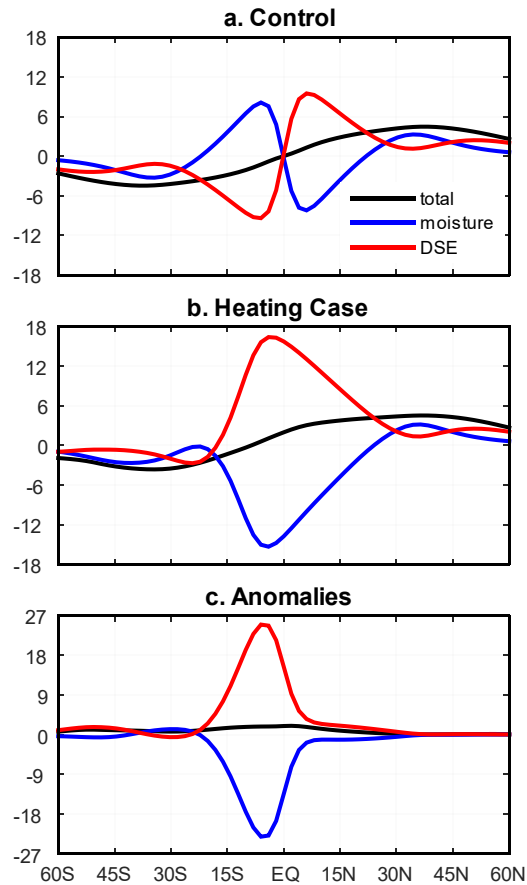


Figure 3. Equilibrium responses of energy transports. Northward atmospheric energy transports (PW) (a) in the control case, (b) in the MLD200 case, and (c) anomalies (the MLD200 case minus control), with total MSE transport in black, contribution from DSE in red, contribution from moisture in blue. Note that in the range of y axes are different between (a)(b) and (c).

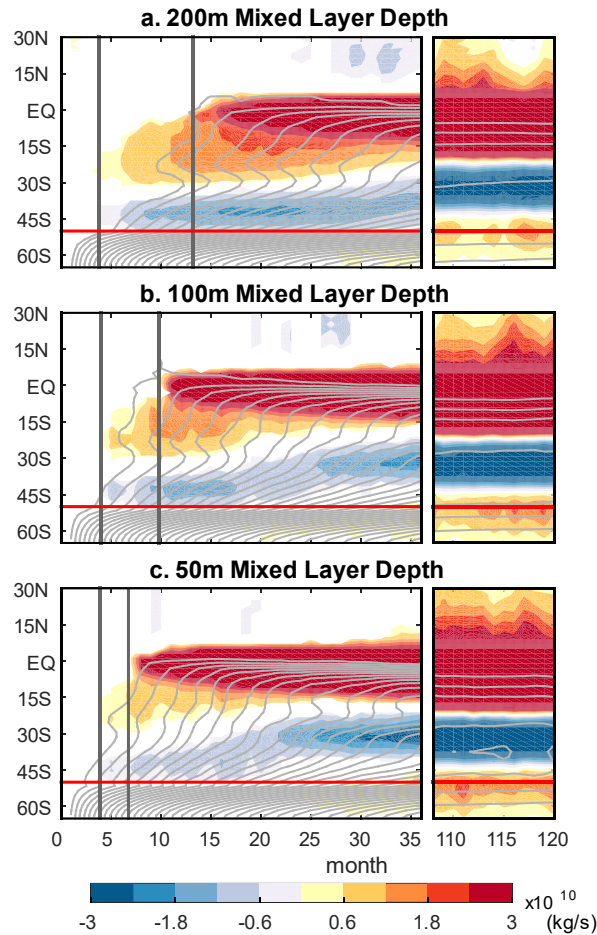


Figure 4. Time series of zonal mean meridional mass streamfunction and SST.

Anomalous zonal mean meridional mass streamfunction at 700hPa (shaded, kg/s) and SST (grey contours, CI = 0.3 °C, zero contour omitted and negative dashed) in cases with (a) 200MLD, (b) 100MLD, and (c) 50 MLD. The vertical grey solid lines mark the start times of Stage 1 and 2. The horizontal red lines indicate the northern edge of imposed forcing. The right column shows the near-equilibrium responses.

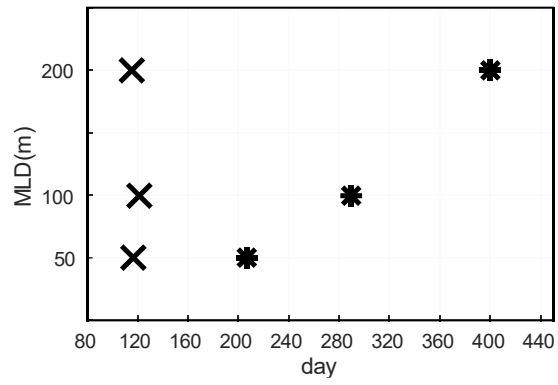


Figure. 5. The start time of Stage 1 & 2. The start time of Stage 1 (cross) and 2 (asterisk) in MLD 200/100/50 cases.

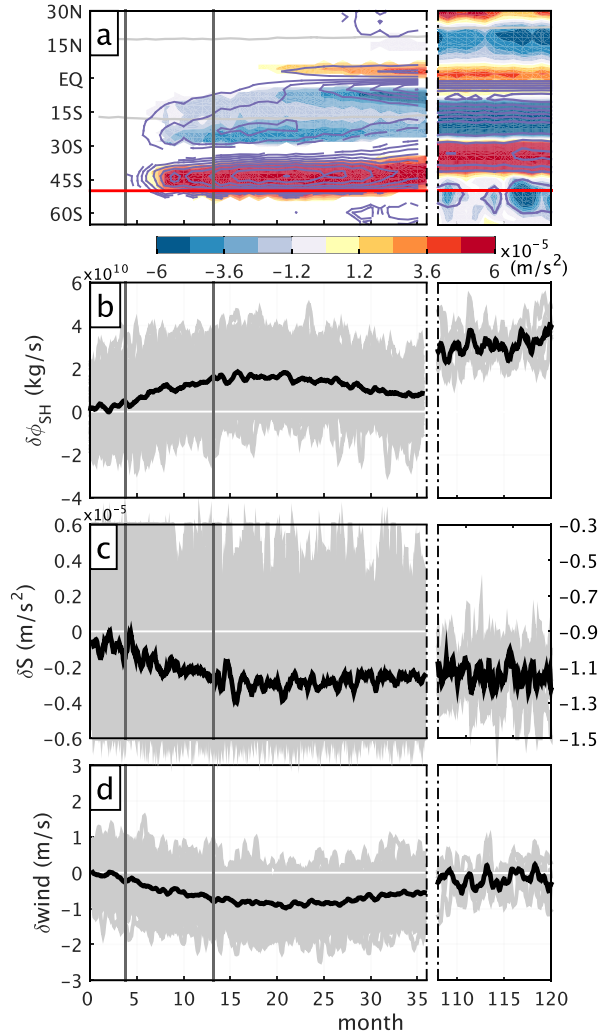


Figure 6. Time series of Stage 1-associated responses in MLD200 case.

Anomalous zonal mean (a) daily S (shaded, m/s^2) and daily f_v (blue contours with CI = $5 \times 10^{-6} \text{ 1/s}^2$, zero contour omitted and negative dashed) in the upper atmosphere (above 700hPa), (b) daily Southern Hemisphere Hadley cell (ϕ_{SH} , kg/s), (c) daily S above 700hPa and between $15^\circ\text{S} \sim 25^\circ\text{S}$ (m/s^2), and (d) daily surface wind speed between $15^\circ\text{S} \sim 25^\circ\text{S}$ (m/s). The vertical solid lines mark the start times of Stage 1 and 2. The right column shows the near-equilibrium responses. In (a), the horizontal red

line indicates the northern edge of imposed forcing and the horizontal grey lines mark the latitude of 0.4 local Rossby number. The thick black lines in (b)~(d) indicate the ensemble mean, with each ensemble in grey. Note that in (c), the range of y axes are different between the left and right panel. The time series are smoothed by 15-day running mean to remove high frequency internal variability.

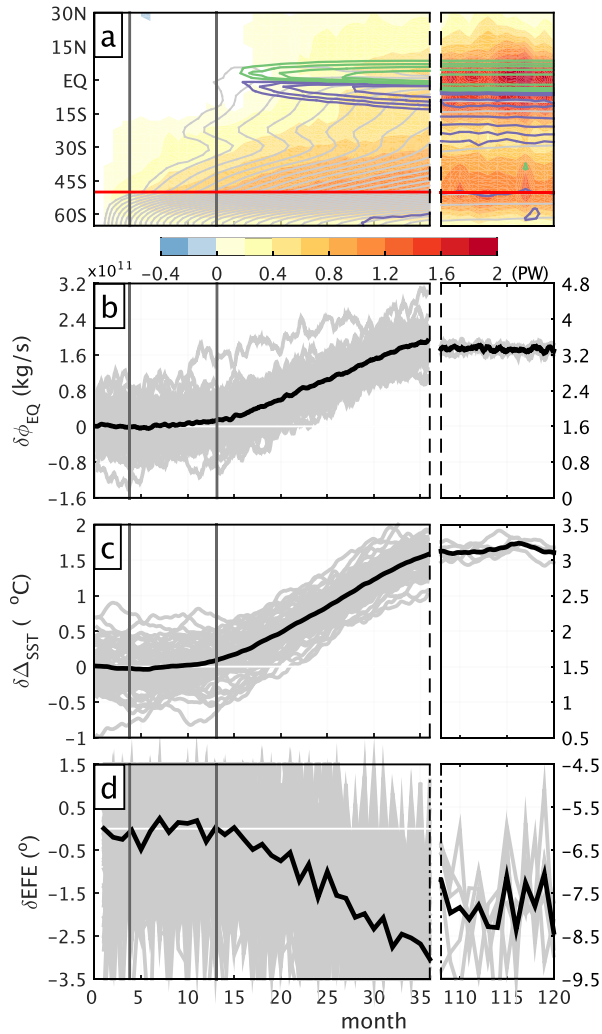


Figure 7. Time series of Stage 2-associated responses in MLD200 case.

Anomalous zonal mean (a) northward MSE transport (shaded, PW), SST (grey contours with $CI = 0.3 \text{ } ^\circ\text{C}$, zero contour omitted and negative dashed), and anomalous precipitation (contour = 1, 2, 4, 8, 16 mm/day, positive purple and negative green), (b) daily cross-equatorial Hadley cell index (φ_{EQ} , kg/s), (c) daily interhemispheric asymmetric SST index (Δ_{SST} , $^\circ\text{C}$), and (d) energy flux equator (EFE, $^\circ$). The vertical solid lines mark the start times of Stage 1 and 2. The right column shows the near-

equilibrium responses. The horizontal red line in (a) indicates the northern edge of imposed forcing. The thick black lines in (b)~(d) indicate the ensemble mean, with each ensemble in light grey. Note that in (b)~(d), the range of y axes are different between the left and right panels. The time series of daily data are smoothed by 15-day running mean to remove high frequency internal variability.

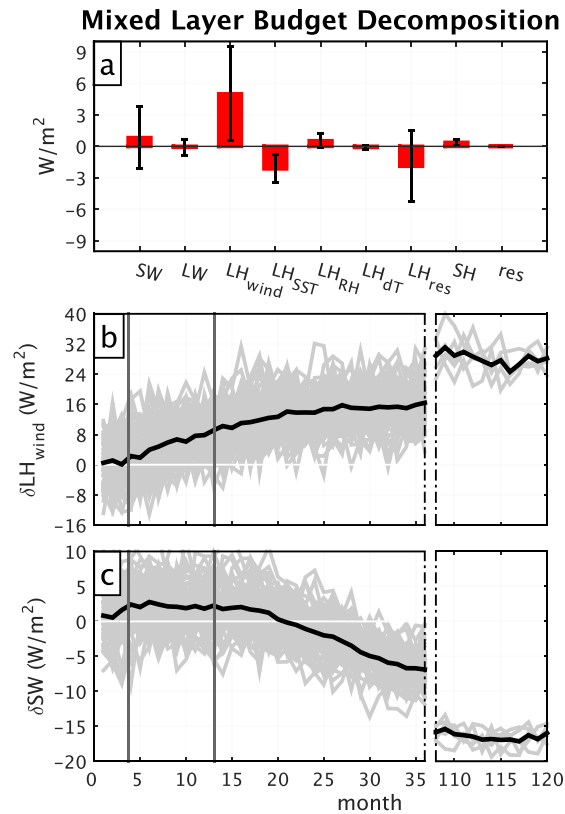


Figure 8. WES feedback. (a) Mixed layer energy budget attribution in southern tropical region (between the equator and the southern edge of the Hadley cell in the SH, 27°S) during Stage 1 period. The errorbars mark the one standard deviation departure from the ensemble mean of each variable. Anomalous (b) surface latent heat flux due to wind change (W/m^2) and (c) surface shortwave flux (W/m^2) in SH tropical region. The vertical dashed lines in (b) and (c) mark the start times of Stage 1 and 2, respectively. The right column shows the near-equilibrium responses. The thick black lines in (b)~(c) indicate the ensemble mean, with each ensemble in light grey.

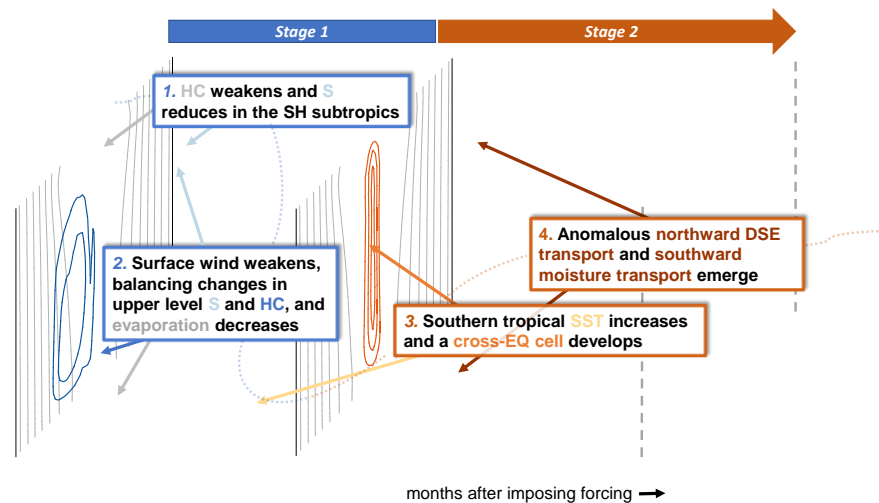


Figure 9. Schematic diagram of the two-stage response. The upper panel shows the anomalous mass stream function at 700 hPa (shaded, power of 10 kg/s), anomalous S over 700hPa (light blue contours, $CI = 10^{-6} \text{ m/s}^2$), and northward DSE transport anomaly (brown contours, $CI = 0.5 \text{ PW}$). The lower panel shows the latent heat anomaly due to wind change (shaded, W/m^2), SST anomaly (yellow contours, $CI = 0.3\text{K}$), and northward moisture transport anomaly (brown contours, energy equivalent, $CI = 0.5 \text{ PW}$, zero and positive are omitted). The blue and orange contours in vertical panels show the anomalous mass streamfunction in two stages respectively ($CI = 3 \times 10^9$ (left) and 2.4×10^{10} (right) kg/s).

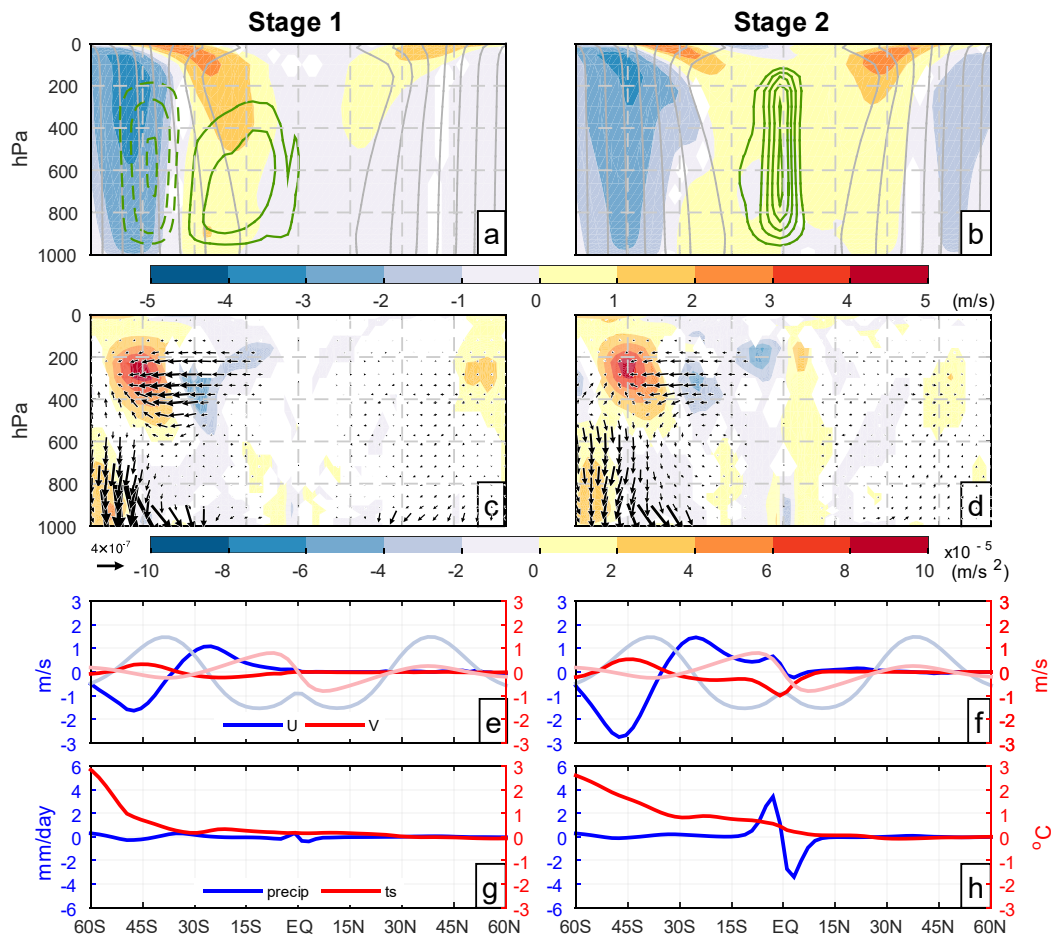


Figure 10. Two-stage responses of the MLD200 case. (a) Anomalous zonal wind (shaded, m/s), anomalous meridional mass stream function (green contours, with $CI = 3 \times 10^9 \text{ kg/s}$, zero contour omitted and negative dashed), and local absolute angular momentum (grey contours, with $CI = \omega a^2/10$, ω is the angular speed, and a is the radius of the Earth), (c) anomalous S (shaded, m^2/s^2) and E-P flux (vector, m^2/s^2), (e) anomalous zonal mean zonal wind (m/s, plotted in blue) and meridional wind (m/s, plotted in red), climatological zonal mean zonal wind (m/s, plotted in light blue) and meridional wind (m/s, plotted in light red), and (g) anomalous zonal mean

precipitation (mm/day, plotted in blue) and surface temperature ($^{\circ}\text{C}$, plotted in red) in Stage 1. (b)(d)(f)(h) are same as (a)(c)(e)(g), but for Stage 2. The CI of green contours in (b) is 1.2×10^{10} kg/s, which is much larger than that in (a). The Stage 1 responses refer to the differences between the average of the time period between the two start dates of Stage 1 and 2 and the climatology. The Stage 2 responses are defined as the differences between the average of the first year after the start date of Stage 2 and the average of the time period between the two start dates of Stage 1 and 2.

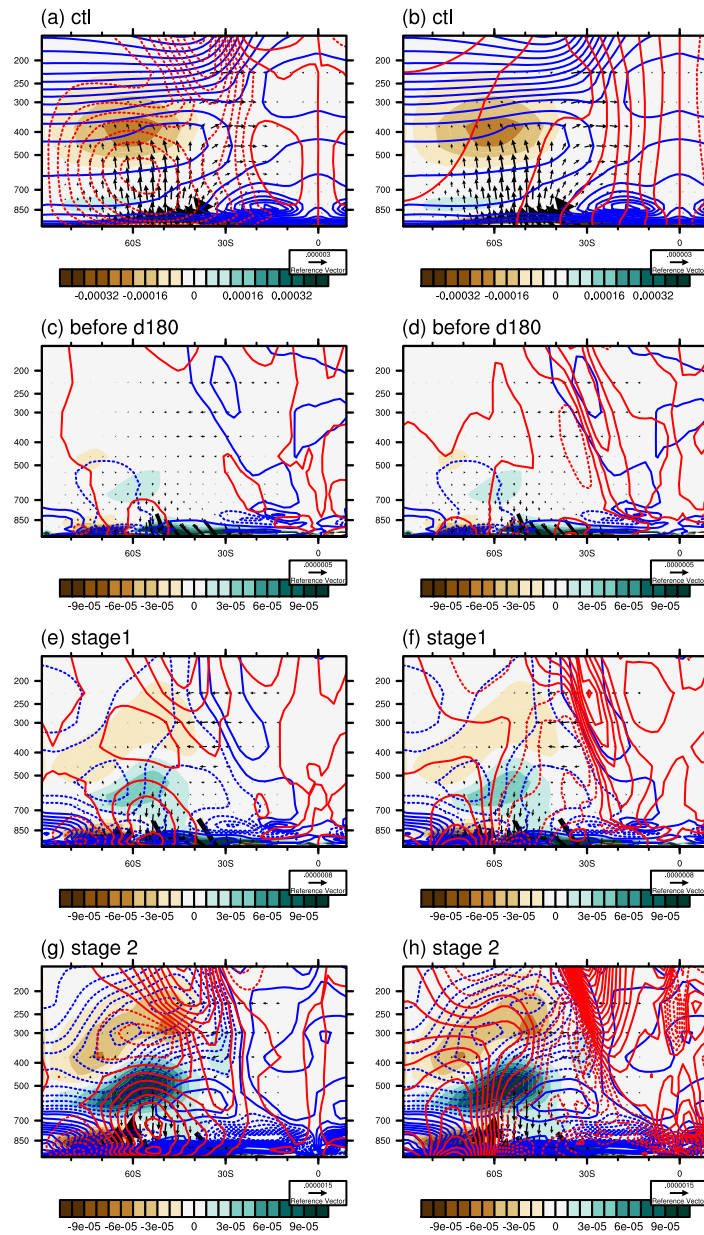


Figure A1. Responses of E-P flux and its divergence. Climatological E-P flux

(arrows), divergence of E-P flux (shading, m/s^2), vertical gradient of potential

temperature (blue contours, K/m , with $\text{IC} = 0.001$, zero contour bolded and negative

dashed), (a) eddy heat flux (red contours in left panel, Km/s , with $\text{IC} = 2$) and (b)

meridional gradient of potential temperature (red contours, K/m, with IC = 40).

Anomalous E-P flux, divergence of E-P flux, vertical gradient of potential

temperature (blue contours, K/m, with IC = 0.0001), (c) eddy heat flux (red contours

in left panel, Km/s, with IC = 1) and (d) meridional gradient of potential temperature

(red contours, K/m, with IC = 1). (e)-(h) as in (c)-(d) but (e)-(f) in Stage 1 and (g)-(h)

in Stage 2.

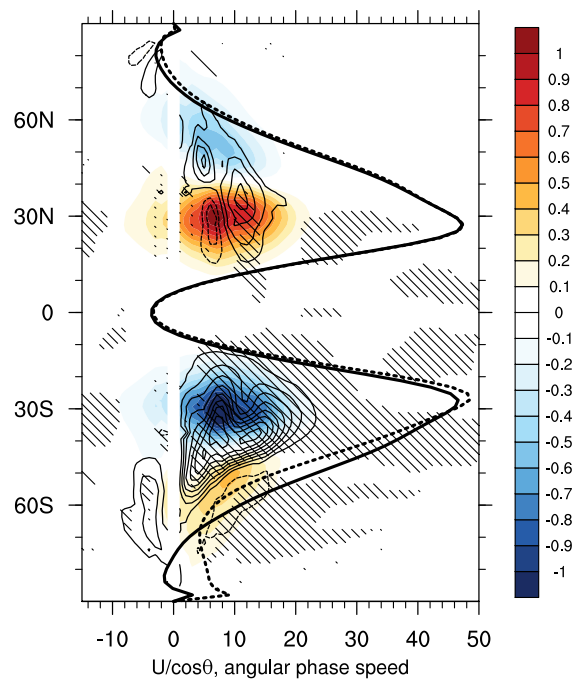


Figure A2. Responses of zonal wind and eddy momentum flux. Zonally average zonal wind at 300hPa divided by $\cos\theta$ (heavy lines, m/s, solid line is climatology and dashed line is ensemble mean of the MLD200 heating case), climatological (shading, m^2/s^2) and anomalous (contours, with $\text{CI} = 0.05 \text{ m}^2/\text{s}^2$, zero contour omitted and negative dashed) eddy momentum flux in Stage 1 at 300hPa. The hatching denotes the significance at 95% confidence level.