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**STATE OF CALIFORNIA DEPARTMENT OF FISH AND GAME**  
**FISH BULLETIN No. 116**  
**Fitting A Von Bertalanffy Growth Curve By Least Squares Including Tables**  
**of Polynomials**



By  
*PATRICK K. TOMLINSON*  
and  
*NORMAN J. ABRAMSON*  
1961



## FOREWORD

The von Bertalanffy growth equation and the generalisations of it presented by Richards (1959), have in recent years proved most useful in studies of fish population dynamics and for the practical assessment of the status of exploited stocks and the effects of fisheries regulations. These equations are, therefore, being increasingly applied to a wide variety of data on the size and age of aquatic animals, and it has been evident that the rough and ready methods of determining parameter values—usually graphical ones—were not satisfactory for all the purposes to which they were being applied. For some purposes it is indeed sufficient that the calculated curve for chosen parameter values should graduate the observed data adequately, as judged by eye, although even in this case an objective, repeatable method of obtaining those values is obviously desirable. Recently, however, attention has been focused by fisheries biologists on the parameters themselves, with regard to their physiological significance, the effects of both biotic and abiotic environmental factors on them, and the relations between them and other population parameters such as natural mortality rates, fecundity, and maturity characteristics. Thus, the extent to which  $k$  or  $[L8]$ , or both, vary with food supply, and hence with population density was discussed at an early stage in the application of these equations and Taylor (1958, 1959) and Holt (1959, 1960) have considered the relation between  $k$  and water temperature.

At several recent international symposia various aspects of the application of the von Bertalanffy equation and the interpretation of its parameters, have been prominent in contributed papers and discussion of them. A general graphical method for examining the growth data has been published (Gulland and Holt, 1959) and the use of this and other methods in the analysis of fish tagging experiments was discussed at the North Atlantic Fish Marking Symposium organized by the International Commission for the Northwest Atlantic Fisheries at Woods Hole, Massachusetts, in June 1961 (*ICNAF Spec. Publ.* (4), in press). At the fifth Ciba Foundation Colloquium on Ageing, in London, 1959, dealing with the Lifespan of Animals, evidence was presented that the parameters  $[L8]$  and  $k$  were correlated with natural mortality and life-span, both inter-specifically and intra-specifically, and that the regression constants had a taxonomic significance. It was also suggested that these parameters might be related to the metabolic parameters for the species (see Beverton and

Holt, 1959). Again, at the Symposium on the Exploitation of Natural Animal Populations organised by the British Ecological Society in Durham, England, March 1960, a relation was demonstrated, on an inter-specific basis, between the growth parameters and the mean size of fish at maturity (Proceedings in press). To explore such lines of work further it was essential to have a method of parameter estimation which is quick and easy to apply, according to generally understood criteria, and for which estimates of variance are also available.

In a different field, but one of growing importance, suitable methods are needed for analysing the results of fish-culture experiments, and it seems likely that the application of forms of the generalised equation referred to here will prove more powerful and discriminatory than the usual procedure of considering growth increments over a measured time interval, or average specific growth rates, without reference to the ages and sizes of the fish in the experimental batches.

For all these reasons this exposition of a method for simple and rapid estimation by least squares, in the case where ages are equally spaced, but sample sizes are not necessarily constant, is to be welcomed at this time. The tables presented will be particularly useful, when, as we must recognise is usually the case, the fisheries research workers concerned do not have access to high speed computers.—*Sidney J. Holt, Chief, Fisheries Biology Branch, Food and Agriculture Organization of the United Nations, Rome, September 1961.*

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June 1961



## 1. INTRODUCTION

Historically, the growth of animals has been described by a variety of functions which relate size increase to a unit of time. These functions vary from a straight-line relationship to the more complex asymptotic-type curve. The methods of fitting straight lines and simple curves, such as quadratic polynomials, are well documented and will not be mentioned further in this paper.

Fish growth is often represented by a function which is asymptotic to some average maximum size the fish will attain. A useful regression formula for representing these curves is

$$y = a + \beta\rho^x \tag{1}$$

where

$$0 < \rho < 1.$$

### FORMULA

This regression formula has three parameters, with  $a$  representing the asymptotic value of  $y$ . Stevens (1951) showed the utility of this basic curve by writing Gompertz's law, the logistic curve, and Mitscherlich's law in this form. It is also possible to write the growth curves of von Bertalanffy (1938) in this way.

The objective of this paper is to present a useful method for fitting Beverton's (1954) modification of the von Bertalanffy growth-in-length curve, but the method is adaptable to any curve which can be written in the basic form of equation (1). The tables in the Appendix, and the worked example should provide sufficient information for fitting a von Bertalanffy curve. The physiological aspects of von Bertalanffy growth functions, including more general equations than that described here, are discussed by von Bertalanffy (1957).

In the past, the methods used to fit a von Bertalanffy curve to observed fish length have required inefficient techniques such as guessing-by-eye (von Bertalanffy, 1938) or approximation-through-transformation (Beverton and Holt, 1957; Ricker, 1958). The method presented in this paper is not only easy to use, but is based on the efficient, well-accepted technique of least squares. Under the assumption of normality, the least squares method produces estimates which are equivalent to maximum likelihood estimates.

With high speed electronic computing equipment, other iterative methods or an adaption of the described method may be used to obtain very accurate estimates of the parameters of the von Bertalanffy curve. Stevens (1951) developed an iterative procedure for fitting (1) and Nelder



(1961) gives an iterative method for fitting a generalized logistic curve which includes (1) as a special case. Nelder's method does not require the x's to be equally spaced and assumes a constant variance for log y rather than for y. However, the following description and the tables in the Appendix should be useful to workers who do not have access to an electronic computer.

## 2. ESTIMATING THE PARAMETERS

Pimentel-Gomes and Malavolta (1949) and Pimentel-Gomes (1953) described a procedure for estimating the parameters of the curve,  $y = A[1 - 10^{-c(x+b)}]$  by the method of least squares. This curve, introduced by Elih. Alfred Mitscherlich (1930), is known as Mitscherlich's regression law and has been used primarily with fertilizer experiments. Here, Pimentel-Gomes' method of estimation is extended to fit a form (Beverton, 1954) of the von Bertalanffy growth-in-length curve,

$$l_t = L_\infty[1 - e^{-k(t-t_0)}], \quad (2)$$

FORMULA

by the method of least squares, when there is an equal time interval between age groups.

### 2.1. Age Group Sample Sizes Equal

Consider the function

$$Q = \sum_{i,j} \{l_{ij} - L_\infty [1 - e^{-k(t_j-t_0)}]\}^2, \quad \begin{array}{l} i = 1, \dots, r_j \\ j = 1, \dots, p, \end{array}$$

FORMULA

where  $r_j$  is the number of fish sampled from the  $j$ th age group and  $p$  is the number of age groups.

Differentiating with respect to  $L_\infty$ ,  $k$  and  $t_0$  and setting the partial derivatives equal to zero will give the following normal equations:

$$\begin{aligned} \sum_{i,j} l_{ij} - nL_\infty + L_\infty e^{kt_0} \sum_{i,j} e^{-kt_j} &= 0 \\ \sum_{i,j} l_{ij} t_j e^{-kt_j} - L_\infty \sum_{i,j} t_j e^{-kt_j} + L_\infty e^{kt_0} \sum_{i,j} t_j e^{-2kt_j} &= 0 \\ \sum_{i,j} l_{ij} e^{-kt_j} - L_\infty \sum_{i,j} e^{-kt_j} + L_\infty e^{kt_0} \sum_{i,j} e^{-2kt_j} &= 0, \end{aligned} \quad (3)$$

FORMULA

$l_{ij}$  = length of the  $i$ th fish belonging to the  $j$ th age group  
 $t_j$  = age of fish in the  $j$ th age group,  $t_1 = 0$   
 $L_\infty$  = maximum expected length  
 $t_0$  = hypothetical age at zero length  
 $k$  = constant which is proportional to the rate of destruction of body materials  
 $n = \sum r_j$ .

FORMULA

[L8],  $t_0$  and  $k$  are the parameters to be estimated in fitting the von Bertalanffy curve.

Following the solution of Pimentel-Gomes (1953), let  $t_j = m_j q$ , where  $q$  is a constant interval between ages and  $m_j$  is an integer. Also let  $z = e^{-kq}$ . Then, if a nontrivial solution of (3) exists,

$$\begin{vmatrix}
 \sum_{i,j} l_{ij} & n & \sum_{i,j} z^{m_j} \\
 \sum_{i,j} t_j l_{ij} z^{m_j} & \sum_{i,j} t_j z^{m_j} & \sum_{i,j} t_j z^{2m_j} \\
 \sum_{i,j} l_{ij} z^{m_j} & \sum_{i,j} z^{m_j} & \sum_{i,j} z^{2m_j}
 \end{vmatrix} = 0. \quad (4)$$

FORMULA

In the case where there is a constant number of measurements within each age group ( $r_j = r$  for all  $j$ ), the expansion of this determinant along the first column and division by  $qr^3 z(1-z)^3$  yields

$$\bar{l}_1 J_{p1}(z) + \dots + \bar{l}_j J_{pj}(z) + \dots + \bar{l}_p J_{pp}(z) = 0, \quad (5)$$

FORMULA

where  $l_j$  is the mean length of the fish in the  $j$ th age group.

By using the polynomial (5) and the tables of  $J_{pj}(z)$  listed in the Appendix,  $z$  can be obtained by successive trials. If the sign of equation (5) at  $z = 0.01$  differs from the sign at  $z = 0.99$ ,  $z$  may be estimated by using the tables. When the point is reached such that the solution gives a sign at  $z = a$  which is different from that at  $a + 0.01$ , linear interpolation is used to find the zero solution.

With  $z$ , estimating [L8],  $t_0$  and  $k$  is reduced to simple algebra. Since

$$z = e^{-kq},$$

then

$$k = \frac{1}{q} \log_e z^{-1}. \quad (6)$$

FORMULA

From (3), omitting one equation,

$$\sum_{i,j} l_{ij} = nL_{\infty} - L_{\infty} e^{kt_0} \sum_{i,j} e^{-kt_j} \quad (7)$$

$$\sum_{i,j} l_{ij} e^{-kt_j} = L_{\infty} \sum_{i,j} e^{-kt_j} - L_{\infty} e^{kt_0} \sum_{i,j} e^{-2kt_j}.$$

FORMULA

System (7) can be solved as two linear equations in two unknowns,  $L_{\infty}$  and  $t_0$ . The solution of (7) is obtained by letting

$$B = L_{\infty} e^{kt_0}$$

$$z^{m_j} = e^{-kt_j}.$$

FORMULA

Dividing (7) by  $r$ ,

$$\sum_j \bar{l}_j = pL_{\infty} - B \sum_j z^{m_j} \quad (8)$$

$$\sum_j \bar{l}_j z^{m_j} = L_{\infty} \sum_j z^{m_j} - B \sum_j z^{2m_j}$$

FORMULA

where

$$\bar{l}_j$$

FORMULA

= observed mean length for  $j$ th age group and  $m_j = j - 1$ . Using determinants, the solution of (8) is

$$D = \left( \sum_j z^{m_j} \right)^2 - p \sum_j z^{2m_j}$$

$$\hat{L}_{\infty} = \frac{1}{D} \left( \sum_j \bar{l}_j z^{m_j} \sum_j z^{m_j} - \sum_j \bar{l}_j \sum_j z^{2m_j} \right) \quad (9)$$

$$\hat{B} = \frac{1}{D} \left( p \sum_j \bar{l}_j z^{m_j} - \sum_j \bar{l}_j \sum_j z^{m_j} \right)$$

and

$$\hat{t}_0 = \frac{1}{k} \log_e (\hat{B} / \hat{L}_{\infty}). \quad (10)$$

FORMULA

This solution fits the curve to the mean lengths of the age groups and can be applied to any data listed as

$$\bar{l}_1, \bar{l}_2, \dots, \bar{l}_p.$$

FORMULA

For an equal number of observations in each age group, a true least squares line is obtained when the variances of the  $l_{ij}$  are assumed equal.

## 2.2. Age Group Sample Sizes Not All Equal

Usually a collection of age-length data does not contain an equal number of observations from each age group. In this situation, equal-sized random sub-samples may be selected from the age groups containing a sufficient number of observations, or all of the data may be used. If the latter choice is made, a weighted least squares fitting procedure is appropriate.

Let

$$Q_w = \sum_j w_j \{ \bar{l}_j - L_\infty [1 - e^{-k(t_j - t_0)}] \}^2$$

FORMULA

be the sum of weighted squared residuals which is to be minimized, where

$$\bar{l}_j = \frac{1}{r_j} \sum_i l_{ij}$$

FORMULA

and  $w_j$  is the non-negative weight associated with the  $j$ th age group. The differentiation of this function with respect to the parameters results in a set of normal equations. When the substitutions of the previous section are performed for  $t_j$  and  $e^{-kt_j}$ , the equation

$$\begin{vmatrix} \sum_j w_j \bar{l}_j & \sum_j w_j & \sum_j w_j z^{m_j} \\ \sum_j w_j \bar{l}_j t_j z^{m_j} & \sum_j w_j t_j z^{m_j} & \sum_j w_j t_j z^{2m_j} \\ \sum_j w_j \bar{l}_j z^{m_j} & \sum_j w_j z^{m_j} & \sum_j w_j z^{2m_j} \end{vmatrix} = 0, \quad (11)$$

FORMULA

which is analogous to (4), may be obtained. An iterative procedure is used to obtain  $z$ , and the rest of the solution follows the method for the case of equal sample sizes. Because the  $w_j$  are factors of the polynomials, a separate solution is required for each set of weights and preparing tables is not practical.

The  $w_j$  should be inversely proportional to the variances of the  $[l_j]$  so that if the variance is assumed constant for all observations,  $w_j = n_j/n$  ( $n_j$  is the number of observations on the  $j$ th age group) is an appropriate weight.

### 3. THE VARIANCES OF THE PARAMETER ESTIMATES FOR EQUAL SAMPLE SIZES

With an equal number of observations in each age group and assuming equal variances for the  $l_{ij}$ , it is possible to determine the variances of the estimates of the parameters. However, it should be kept in mind that the distribution of these estimated parameters will, in general, be unknown so that caution is needed in interpreting the variances.

The solutions for the variances follow the method of Pimentel-Gomes (1953), which is derived from that of Stevens (1951). Writing these solutions, using the notation of Stevens (1951), gives

$$\begin{aligned}
 V(\hat{L}_\infty) &= F_{aa}s^2/r \\
 V(\hat{k}) &= F_{rr}s^2/(qzB)^2 \\
 V(\hat{t}_0) &= \frac{q^2s^2(\log_{10}e)^2}{r(\log_{10}z)^2} \left[ \left(\frac{1}{L_\infty}\right)^2 F_{aa} + \left(\frac{1}{-B}\right)^2 F_{bb} + \left(\frac{u}{-B}\right)^2 F_{rr} \right. \\
 &\quad \left. - \left(\frac{2}{-BL_\infty}\right)F_{ab} - \left(\frac{2u}{-BL_\infty}\right)F_{ar} + \left(\frac{2u}{B^2}\right)F_{br} \right],
 \end{aligned} \tag{12}$$

where

$$u = (\log_{10} L_\infty/B)/z \log_{10} z$$

$$s^2 = \text{residual variance}$$

$$r = \text{number of observations in each age group}$$

FORMULA

and  $F_{aa}, F_{bb}, F_{rr}, F_{ab}, F_{ar}, F_{br}$  are components of the reciprocal of the matrix,

$$\begin{bmatrix}
 p & \sum_j z^{m_j} & z^{-1} \sum_j m_j z^{m_j} \\
 \sum_j z^{m_j} & \sum_j z^{2m_j} & z^{-1} \sum_j m_j z^{2m_j} \\
 z^{-1} \sum_j m_j z^{m_j} & z^{-1} \sum_j m_j z^{2m_j} & z^{-2} \sum_j m_j^2 z^{2m_j}
 \end{bmatrix} \tag{13}$$

FORMULA

Computing the reciprocal of (13) gives

$$\begin{bmatrix}
 F_{aa} & F_{ab} & F_{ar} \\
 F_{ab} & F_{bb} & F_{br} \\
 F_{ar} & F_{br} & F_{rr}
 \end{bmatrix} \tag{14}$$

FORMULA

The residual variance,  $s^2$ , may be computed from

$$s^2 = \sum_{i,j} (l_{ij} - \hat{l}_j)^2 / (n - 3) \tag{15}$$

FORMULA

where  $[l_j]$  = expected mean length of the  $j$ th age as computed from the fitted line.

## 4. EXAMPLE SOLUTION

### 4.1. Estimating the Parameters

For this example, the data in Table 1 were randomly chosen from the length-at-age information available for California yellowtail (*Seriola dorsalis*). The ages are the actual ages at the time of capture. A von Bertalanffy curve was fitted to the complete data by Baxter, *et al.* (1960) using the method described by Beverton and Holt (1957). The original data were considered random, and after stratifying these by age groups, a simple random sample of 11 measurements was chosen from within each of the first eight age groups.

TABLE 1  
Lengths in Millimeters by Age Group for California Yellowtail, *Seriola dorsalis*

	Age Group								
	I	II	III	IV	V	VI	VII	VIII	
	480	636	659	735	887	834	855	993	
	548	688	645	837	843	844	915	964	
	503	699	666	777	858	934	940	967	
	485	652	662	748	894	882	905	962	
	595	662	637	772	841	892	854	909	
	497	554	762	790	787	839	914	1020	
	583	559	666	749	846	861	862	925	
	442	668	652	764	834	865	859	922	
	475	645	733	763	806	934	895	909	
	530	559	634	800	805	876	922	969	
	468	622	685	745	759	904	903	982	
Sum-----	5606	6944	7401	8480	9160	9665	9824	10522	
$\bar{l}_j$ -----	509.64	631.27	672.82	770.91	832.73	878.64	893.09	956.55	$n = 88$

TABLE 1  
Lengths in Millimeters by Age Group for California Yellowtail, *Seriola dorsalis*

Since the first age is  $t_1 = 1$ , and the method of fitting requires  $t_1 = 0$ , it is necessary to subtract 1 from each  $t_j$ . Then,

$$\begin{aligned} t'_j &= t_j - 1 \\ t'_0 &= t_0 - 1. \end{aligned} \tag{16}$$

FORMULA

The line now being fitted is

$$l'_t = L_\infty [1 - e^{-k(t'-t'_0)}]. \tag{17}$$

FORMULA

The value of  $z$  is found by using the table for  $J_{\theta j}(z)$  and formula (5). Table 2 demonstrates the technique. Now, from equation (6), with  $q = 1$  and  $z = 0.8373$  (by linear interpolation in Table 2),

$$\hat{k} = \log_e \frac{1}{0.8373} = 0.1776. \tag{18}$$

FORMULA

For the solution of the system (8) it is necessary to compute the values in Table 3.  
Then, using (9)

$$\begin{aligned}
 D &= (4.661504)^2 - (8)(3.150056) = -3.470828 \\
 \hat{L}_\infty &= \frac{-3896.903013}{-3.470828} = 1122.759 \\
 \hat{B} &= \frac{-2111.958014}{-3.470828} = 608.488,
 \end{aligned}
 \tag{19}$$

*FORMULA*

and from equation (10)

$$\hat{t}'_0 = \left( \frac{1}{0.1776} \right) \log_e \frac{608.488}{1122.759} = -3.4493
 \tag{20}$$

*FORMULA*

or from equation (16)

$$\hat{t}_0 = -2.4493.$$

*FORMULA*

To find the fitted lengths at age  $t$ , it is only necessary to evaluate equation (2) as in Table 4.

TABLE 2  
Finding  $z$  by Successive Trials

Mean Length	$\bar{l}_1$	$\bar{l}_2$	$\bar{l}_3$	$\bar{l}_4$	$\bar{l}_5$	$\bar{l}_6$	$\bar{l}_7$	$\bar{l}_8$	$\sum_{j=1}^8 \bar{l}_j J_{8j}(z)$
	$J_{81}(z)$	$J_{82}(z)$	$J_{83}(z)$	$J_{84}(z)$	$J_{85}(z)$	$J_{86}(z)$	$J_{87}(z)$	$J_{88}(z)$	
$z = 0.01$	0	-6	1	1	1	1	1	1	1216.9
$z = 0.99$	1086	139	-481	-782	-769	-450	171	1086	-129412.9
$z = 0.50$	22	-29	-28	-14	0	10	17	21	7329.8
$z = 0.90$	526	-9	-305	-402	-339	-146	150	526	-26162.2
$z = 0.80$	235	-52	-174	-187	-128	-26	99	234	8535.0
$z = 0.84$	324.381	-43.291	-219.050	-254.895	-191.100	-58.632	118.901	323.686	-714.9807
$z = 0.83$	299.248	-46.237	-207.033	-235.949	-173.179	-49.059	113.737	298.472	1909.9154

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TABLE 2  
Finding  $z$  by Successive Trials



**TABLE 3**  
**Values for Solving System (8)**

$m_j$	$z^{m_j}$	$z^{2m_j}$	$\bar{l}_j$	$\bar{l}_j z^{m_j}$
0.....	1.000000	1.000000	509.6	509.6
1.....	0.837300	0.701071	631.3	528.58749
2.....	0.701071	0.491501	672.8	.
3.....	0.587007	0.344577	770.9	.
4.....	0.491501	0.241573	832.7	.
5.....	0.411534	0.169360	878.6	.
6.....	0.344577	0.118733	893.1	.
7.....	0.288514	0.083241	956.6	.
Totals.....	4.661504	3.150056	6145.6	3316.9726213

*TABLE 3*  
*Values for Solving System (8)*

**TABLE 4**  
**Computing the Fitted Lengths**

$$l_t = 1122.8 [1 - e^{-0.1776(t+2.4493)}]$$

$t$	$t + 2.4493$	$(0.1776)(t + 2.4493)$	$e^{-0.1776(t+2.4493)}$	$1 - e^{-0.1776(t+2.4493)}$	$\hat{l}_t$
1.....	3.4493	0.61260	0.54194	0.45806	514.31
2.....	4.4493	0.79020	0.45375	0.54625	613.33
3.....	5.4493	0.96780	0.37992	0.62008	696.23
4.....	6.4493	1.14540	0.31810	0.68190	765.64
5.....	7.4493	1.32300	0.26634	0.73366	823.75
6.....	8.4493	1.50060	0.22300	0.77700	872.42
7.....	9.4493	1.67820	0.18671	0.81329	913.16
8.....	10.4493	1.85580	0.15633	0.84367	947.27

*TABLE 4*  
*Computing the Fitted Lengths*

## 4.2. Estimating the Variance

The values for the components of matrix (13) can be obtained from Table 3.

Thus, solving for the components of (13) yields

$$\begin{bmatrix} 8 & 4.661504 & 14.464584 \\ 4.661504 & 3.150056 & 6.958056 \\ 14.464584 & 6.958056 & 31.695266 \end{bmatrix}. \quad (21)$$

*FORMULA*

The inverse of matrix (21) will contain the components of the matrix (14), which are

$$\begin{aligned} F_{aa} &= 26.477509 & F_{bb} &= 22.827520 \\ F_{ab} &= -24.250721 & F_{br} &= 6.055839 \\ F_{ar} &= -6.759631 & F_{rr} &= 1.786966. \end{aligned} \quad (22)$$

*FORMULA*

The residual variance is calculated using the right hand side of the identity

$$\sum_{i,j} (l_{ij} - \hat{l}_j)^2 = \sum_{i,j} l_{ij}^2 - 2 \sum_j \hat{l}_j \sum_i l_{ij} + r \sum_j \hat{l}_j^2.$$

From values in Tables 1 and 4,

$$\begin{aligned} \sum_{i,j} l_{ij}^2 &= 53842822, \quad r \sum_j \hat{l}_j^2 = 53707408.095, \quad \text{and} \quad \sum_j 2\hat{l}_j \sum_i l_{ij} \\ &= 107406317.78. \end{aligned}$$

Therefore, from equation (15),  $s^2 = 1693.086$ .

Using (12), (15), (19) and (22) gives  $V(\hat{L}_\infty) = 4075.336$ ,  $V(\hat{k}) = 0.001060$ , and  $V(\hat{t}'_0) = 0.1970$ , and since  $t_0 = t'_0 + 1$ ,  $V(\hat{t}_0) = V(\hat{t}'_0) = 0.1970$ .

*FORMULA*

## 5. SUMMARY

The von Bertalanffy growth-in-length curve,

$$l_t = L_\infty [1 - e^{-k(t-t_0)}],$$

*FORMULA*

is often used to describe fish growth.

When the ages are equally spaced, this function may be fitted by least squares using a technique developed by Pimentel-Gomes and Malavolta (1949) for fitting Mitscherlich's Law.

The solution involves writing the matrix of the coefficients of the normal equations as a function of one unknown,  $z = e^{-kq}$ . A solution for  $z$  is obtained by setting the determinant of the matrix equal to zero and solving by iteration. The three parameters of the curve are then easily estimated.

Where the sample sizes for each age group are equal, tables of polynomials make possible a rapid solution. The polynomials,  $J_{pi}(z)$ , are tabled for fitting the curve to data with from 4 to 18 age groups.

Unequal sample sizes require a weighted solution for which tables are not practical.

In the case of equal sample sizes, variances of the estimated parameters may be obtained by using a method of Stevens (1951).

A worked example illustrates the method of curve fitting and variance estimation for the equal-sample-size situation.

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## APPENDIX

### TABLES OF POLYNOMIALS $J_{\mathbf{p},\mathbf{j}}(z)$

These are the tabulation of

$$J_{\mathbf{p},\mathbf{j}}(z) = \left[ \sum_j m_j z^{m_j} \sum_j z^{2m_j} - \sum_j z^{m_j} \sum_j m_j z^{2m_j} + m_j z^{m_j} \left( \sum_j z^{m_j} \right)^2 \right. \\ \left. - p m_j z^{m_j} \sum_j z^{2m_j} + p z^{m_j} \sum_j m_j z^{2m_j} - z^{m_j} \sum_j z^{m_j} \sum_j m_j z^{m_j} \right] \\ / z(1 - z)^3,$$

FORMULA

( $j = 1, \dots, p; m_j = j - 1$ ), for

$$0.01 \leq z \leq 0.99$$

FORMULA

by an increment in  $z$  of 0.01, and for

$$4 \leq p \leq 18$$

FORMULA

. Because the division by  $z(1 - z)^3$  was performed numerically, values for  $z = 0$  and  $z = 1$  could not be obtained. In the column headings of the tables,  $J_{\mathbf{p},\mathbf{j}}(z)$  is represented by  $\mathbf{j}, \mathbf{p}, \mathbf{j}$ .

The calculations were performed in double-precision arithmetic on the IBM 7090 computer at Western Data Processing Center, University of California, Los Angeles. With the 7090 FORTRAN II program, tables for any value of  $p$  and any interval in  $z$  can be compiled. The program utilizes a double-precision subroutine developed by the Rocketdyne Division of North American Aviation, Inc. The tabled values should be accurate to eight significant digits.

Z	J 4, 1	J 4, 2	J 4, 3	J 4, 4
.01	0.020	-2.040	0.580	1.040
.02	0.041	-2.081	0.559	1.081
.03	0.063	-2.123	0.537	1.123
.04	0.085	-2.165	0.515	1.165
.05	0.108	-2.208	0.492	1.208
.06	0.132	-2.251	0.468	1.251
.07	0.156	-2.295	0.444	1.295
.08	0.181	-2.340	0.419	1.340
.09	0.207	-2.385	0.393	1.385
.10	0.234	-2.432	0.366	1.432
.11	0.262	-2.479	0.338	1.479
.12	0.290	-2.526	0.309	1.527
.13	0.320	-2.575	0.280	1.575
.14	0.350	-2.624	0.249	1.624
.15	0.382	-2.674	0.218	1.674
.16	0.414	-2.724	0.186	1.725
.17	0.447	-2.776	0.152	1.777
.18	0.482	-2.828	0.117	1.829
.19	0.517	-2.881	0.082	1.882
.20	0.554	-2.934	0.045	1.935
.21	0.591	-2.988	0.407	1.991
.22	0.630	-3.044	0.368	2.046
.23	0.670	-3.100	0.327	2.103
.24	0.711	-3.157	0.285	2.160
.25	0.754	-3.215	0.242	2.219
.26	0.798	-3.273	0.198	2.278
.27	0.843	-3.333	0.152	2.338
.28	0.889	-3.393	0.105	2.399
.29	0.937	-3.454	0.056	2.461
.30	0.986	-3.516	0.006	2.524
.31	1.037	-3.579	-0.046	2.588
.32	1.089	-3.642	-0.099	2.653
.33	1.142	-3.707	-0.154	2.719
.34	1.197	-3.772	-0.211	2.785
.35	1.254	-3.838	-0.269	2.853
.36	1.312	-3.905	-0.329	2.922
.37	1.372	-3.973	-0.391	2.992
.38	1.434	-4.042	-0.454	3.063
.39	1.497	-4.112	-0.520	3.135
.40	1.562	-4.182	-0.587	3.208
.41	1.628	-4.254	-0.656	3.282
.42	1.697	-4.326	-0.728	3.357
.43	1.767	-4.400	-0.801	3.434
.44	1.839	-4.474	-0.876	3.511
.45	1.913	-4.549	-0.954	3.590
.46	1.989	-4.625	-1.034	3.669
.47	2.067	-4.702	-1.116	3.750
.48	2.147	-4.779	-1.200	3.832
.49	2.229	-4.858	-1.286	3.916
.50	2.312	-4.937	-1.375	4.000

TABLE

Z	J 4.1	J 4.2	J 4.3	J 4.4
.51	2.299	-5.018	-1.466	4.086
.52	2.487	-5.099	-1.569	4.172
.53	2.677	-5.182	-1.656	4.260
.54	2.870	-5.265	-1.755	4.350
.55	2.765	-5.349	-1.856	4.440
.56	2.862	-5.434	-1.960	4.532
.57	2.961	-5.520	-2.067	4.625
.58	3.063	-5.606	-2.175	4.719
.59	3.167	-5.694	-2.288	4.815
.60	3.274	-5.782	-2.403	4.912
.61	3.383	-5.872	-2.521	5.010
.62	3.494	-5.962	-2.642	5.110
.63	3.608	-6.053	-2.766	5.211
.64	3.725	-6.145	-2.893	5.313
.65	3.845	-6.238	-3.023	5.417
.66	3.967	-6.332	-3.156	5.522
.67	4.091	-6.427	-3.293	5.628
.68	4.219	-6.522	-3.433	5.736
.69	4.349	-6.619	-3.576	5.845
.70	4.482	-6.716	-3.722	5.956
.71	4.618	-6.814	-3.872	6.068
.72	4.757	-6.913	-4.026	6.182
.73	4.899	-7.013	-4.183	6.297
.74	5.044	-7.113	-4.343	6.413
.75	5.191	-7.215	-4.508	6.531
.76	5.342	-7.317	-4.676	6.651
.77	5.496	-7.420	-4.848	6.772
.78	5.654	-7.524	-5.024	6.894
.79	5.814	-7.629	-5.203	7.018
.80	5.978	-7.734	-5.387	7.144
.81	6.145	-7.841	-5.575	7.271
.82	6.315	-7.948	-5.767	7.400
.83	6.488	-8.056	-5.963	7.530
.84	6.663	-8.164	-6.163	7.662
.85	6.840	-8.274	-6.368	7.796
.86	7.020	-8.384	-6.577	7.931
.87	7.218	-8.495	-6.791	8.068
.88	7.409	-8.606	-7.008	8.206
.89	7.604	-8.719	-7.231	8.346
.90	7.802	-8.832	-7.458	8.488
.91	8.004	-8.946	-7.690	8.631
.92	8.210	-9.060	-7.927	8.777
.93	8.420	-9.175	-8.168	8.923
.94	8.634	-9.291	-8.415	9.072
.95	8.852	-9.408	-8.666	9.222
.96	9.073	-9.525	-8.922	9.374
.97	9.299	-9.643	-9.184	9.528
.98	9.528	-9.761	-9.451	9.684
.99	9.762	-9.880	-9.723	9.841

FITTING A GROWTH CURVE

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TABLE



Z	J 5, 1	J 5, 2	J 5, 3	J 5, 4	J 5, 5
.01	0.031	-3.071	0.959	1.040	1.041
.02	0.062	-3.144	0.916	1.080	1.085
.03	0.096	-3.218	0.872	1.120	1.131
.04	0.130	-3.295	0.825	1.160	1.180
.05	0.167	-3.374	0.776	1.200	1.232
.06	0.204	-3.454	0.725	1.239	1.286
.07	0.244	-3.537	0.671	1.279	1.343
.08	0.285	-3.622	0.615	1.318	1.403
.09	0.328	-3.709	0.557	1.357	1.467
.10	0.373	-3.798	0.496	1.396	1.533
.11	0.421	-3.890	0.432	1.435	1.603
.12	0.470	-3.984	0.365	1.473	1.676
.13	0.522	-4.081	0.295	1.511	1.753
.14	0.576	-4.179	0.222	1.548	1.833
.15	0.633	-4.281	0.146	1.585	1.917
.16	0.692	-4.385	0.067	1.621	2.005
.17	0.754	-4.492	-0.016	1.657	2.097
.18	0.819	-4.601	-0.103	1.692	2.193
.19	0.888	-4.713	-0.193	1.726	2.293
.20	0.959	-4.829	-0.288	1.760	2.397
.21	1.034	-4.946	-0.387	1.792	2.506
.22	1.113	-5.067	-0.490	1.824	2.620
.23	1.195	-5.191	-0.597	1.854	2.739
.24	1.282	-5.318	-0.709	1.883	2.863
.25	1.372	-5.448	-0.826	1.911	2.991
.26	1.467	-5.581	-0.948	1.938	3.125
.27	1.566	-5.718	-1.075	1.962	3.265
.28	1.670	-5.858	-1.208	1.986	3.410
.29	1.779	-6.001	-1.347	2.007	3.561
.30	1.893	-6.147	-1.491	2.027	3.718
.31	2.013	-6.297	-1.641	2.044	3.881
.32	2.138	-6.451	-1.798	2.059	4.051
.33	2.270	-6.608	-1.961	2.072	4.228
.34	2.407	-6.768	-2.132	2.082	4.411
.35	2.551	-6.933	-2.309	2.089	4.602
.36	2.701	-7.101	-2.494	2.094	4.799
.37	2.859	-7.272	-2.686	2.095	5.003
.38	3.023	-7.448	-2.886	2.093	5.218
.39	3.196	-7.627	-3.093	2.087	5.439
.40	3.376	-7.811	-3.312	2.077	5.669
.41	3.565	-7.998	-3.538	2.064	5.907
.42	3.762	-8.189	-3.773	2.046	6.154
.43	3.968	-8.385	-4.017	2.023	6.410
.44	4.184	-8.584	-4.271	1.996	6.676
.45	4.409	-8.788	-4.536	1.963	6.951
.46	4.644	-8.995	-4.811	1.925	7.237
.47	4.890	-9.207	-5.097	1.881	7.532
.48	5.147	-9.423	-5.394	1.831	7.838
.49	5.415	-9.643	-5.703	1.774	8.156
.50	5.695	-9.867	-6.023	1.711	8.484

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FISH BULLETIN NO. 116

TABLE

Z	J 6, 1	J 6, 2	J 6, 3	J 6, 4	J 6, 5
.51	5.988	-10.096	-6.357	1.640	8.825
.52	6.293	-10.328	-6.703	1.862	9.177
.53	6.611	-10.565	-7.063	1.475	9.542
.54	6.943	-10.807	-7.436	1.380	9.919
.55	7.289	-11.052	-7.823	1.276	10.310
.56	7.651	-11.302	-8.226	1.163	10.714
.57	8.027	-11.556	-8.643	1.040	11.132
.58	8.420	-11.814	-9.076	0.906	11.564
.59	8.829	-12.076	-9.525	0.761	12.011
.60	9.255	-12.342	-9.991	0.605	12.474
.61	9.699	-12.613	-10.474	0.436	12.952
.62	10.161	-12.887	-10.975	0.255	13.446
.63	10.643	-13.166	-11.494	0.061	13.957
.64	11.144	-13.448	-12.033	-0.148	14.485
.65	11.666	-13.734	-12.590	-0.371	15.030
.66	12.208	-14.024	-13.168	-0.610	15.593
.67	12.773	-14.318	-13.766	-0.865	16.176
.68	13.361	-14.616	-14.386	-1.136	16.777
.69	13.972	-14.917	-15.027	-1.425	17.398
.70	14.607	-15.221	-15.691	-1.733	18.039
.71	15.267	-15.529	-16.379	-2.060	18.700
.72	15.954	-15.840	-17.090	-2.407	19.384
.73	16.667	-16.154	-17.826	-2.775	20.089
.74	17.408	-16.471	-18.587	-3.166	20.816
.75	18.177	-16.791	-19.374	-3.579	21.567
.76	18.977	-17.114	-20.188	-4.016	22.342
.77	19.806	-17.439	-21.030	-4.478	23.141
.78	20.668	-17.766	-21.900	-4.967	23.965
.79	21.562	-18.095	-22.800	-5.482	24.815
.80	22.490	-18.427	-23.729	-6.023	25.692
.81	23.452	-18.759	-24.689	-6.590	26.595
.82	24.450	-19.094	-25.680	-7.204	27.527
.83	25.486	-19.429	-26.704	-7.860	28.487
.84	26.559	-19.765	-27.762	-8.560	29.477
.85	27.672	-20.102	-28.854	-9.314	30.497
.86	28.826	-20.440	-29.980	-9.954	31.548
.87	30.021	-20.777	-31.148	-10.732	32.631
.88	31.259	-21.114	-32.343	-11.548	33.746
.89	32.542	-21.451	-33.581	-12.406	34.895
.90	33.871	-21.788	-34.858	-13.303	36.078
.91	35.247	-22.120	-36.175	-14.248	37.297
.92	36.672	-22.453	-37.533	-15.237	38.551
.93	38.146	-22.783	-38.933	-16.275	39.843
.94	39.672	-23.111	-40.376	-17.357	41.172
.95	41.252	-23.436	-41.863	-18.485	42.541
.96	42.886	-23.758	-43.395	-19.681	43.949
.97	44.576	-24.076	-44.974	-20.924	45.398
.98	46.324	-24.389	-46.600	-22.223	46.889
.99	48.131	-24.697	-48.275	-23.581	48.422

TABLE 6. JACOBI POLYNOMIALS

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TABLE

Z	J 6, 1	J 6, 2	J 6, 3	J 6, 4	J 6, 5	J 6, 6
.01	0.041	-4.102	0.938	1.040	1.041	1.041
.02	0.084	-4.206	0.874	1.079	1.085	1.085
.03	0.129	-4.314	0.806	1.117	1.131	1.132
.04	0.176	-4.423	0.734	1.154	1.180	1.181
.05	0.223	-4.540	0.659	1.191	1.231	1.234
.06	0.277	-4.658	0.580	1.226	1.285	1.290
.07	0.332	-4.780	0.497	1.261	1.342	1.349
.08	0.389	-4.906	0.409	1.294	1.401	1.413
.09	0.450	-5.035	0.317	1.325	1.463	1.480
.10	0.513	-5.169	0.221	1.355	1.528	1.552
.11	0.580	-5.307	0.119	1.384	1.596	1.628
.12	0.651	-5.450	0.012	1.410	1.667	1.709
.13	0.726	-5.597	-0.101	1.435	1.742	1.795
.14	0.804	-5.748	-0.219	1.458	1.819	1.887
.15	0.887	-5.903	-0.344	1.478	1.899	1.984
.16	0.975	-6.066	-0.474	1.495	1.982	2.088
.17	1.068	-6.233	-0.612	1.510	2.069	2.198
.18	1.166	-6.404	-0.757	1.522	2.159	2.315
.19	1.269	-6.582	-0.909	1.530	2.232	2.430
.20	1.379	-6.765	-1.069	1.535	2.300	2.570
.21	1.495	-6.953	-1.237	1.536	2.449	2.710
.22	1.617	-7.148	-1.414	1.533	2.555	2.859
.23	1.747	-7.349	-1.600	1.526	2.660	3.016
.24	1.884	-7.556	-1.795	1.514	2.770	3.183
.25	2.029	-7.770	-2.001	1.496	2.884	3.360
.26	2.183	-7.990	-2.216	1.474	3.002	3.547
.27	2.346	-8.217	-2.443	1.445	3.123	3.745
.28	2.519	-8.451	-2.682	1.409	3.248	3.957
.29	2.702	-8.693	-2.932	1.367	3.376	4.180
.30	2.895	-8.942	-3.195	1.317	3.508	4.415
.31	3.100	-9.198	-3.472	1.260	3.643	4.666
.32	3.318	-9.462	-3.763	1.194	3.782	4.931
.33	3.548	-9.734	-4.068	1.118	3.924	5.211
.34	3.792	-10.015	-4.389	1.033	4.070	5.508
.35	4.051	-10.303	-4.725	0.938	4.219	5.821
.36	4.325	-10.601	-5.079	0.831	4.371	6.153
.37	4.614	-10.907	-5.450	0.712	4.523	6.504
.38	4.923	-11.221	-5.840	0.581	4.683	6.874
.39	5.256	-11.545	-6.250	0.435	4.844	7.266
.40	5.606	-11.878	-6.679	0.273	5.007	7.680
.41	5.962	-12.220	-7.131	0.099	5.172	8.117
.42	6.330	-12.572	-7.604	-0.093	5.340	8.579
.43	6.702	-12.933	-8.101	-0.303	5.509	9.066
.44	7.088	-13.305	-8.622	-0.532	5.680	9.581
.45	7.490	-13.686	-9.169	-0.782	5.852	10.124
.46	8.149	-14.077	-9.745	-1.053	6.025	10.698
.47	8.698	-14.477	-10.344	-1.347	6.198	11.303
.48	9.217	-14.889	-10.976	-1.665	6.371	11.941
.49	9.799	-15.310	-11.637	-2.010	6.544	12.614
.50	10.415	-15.741	-12.331	-2.382	6.715	13.324

TABLE

Z	J 6, 1	J 6, 2	J 6, 3	J 6, 4	J 6, 5	J 6, 6
.51	11.068	-16.183	-13.058	-2.783	6.884	14.073
.52	11.759	-16.635	-13.821	-3.216	7.031	14.862
.53	12.490	-17.097	-14.619	-3.683	7.215	15.693
.54	13.265	-17.569	-15.456	-4.184	7.374	16.570
.55	14.085	-18.051	-16.333	-4.723	7.529	17.493
.56	14.933	-18.543	-17.252	-5.302	7.677	18.466
.57	15.812	-19.044	-18.214	-5.923	7.819	19.491
.58	16.844	-19.555	-19.221	-6.589	7.952	20.570
.59	17.932	-20.073	-20.276	-7.302	8.076	21.706
.60	18.960	-20.605	-21.379	-8.066	8.189	22.902
.61	20.110	-21.142	-22.535	-8.888	8.290	24.161
.62	21.327	-21.688	-23.744	-9.757	8.377	25.486
.63	22.613	-22.242	-25.008	-10.669	8.448	26.889
.64	23.973	-22.803	-26.331	-11.627	8.502	28.346
.65	25.410	-23.371	-27.714	-12.631	8.537	29.889
.66	26.929	-23.945	-29.161	-13.686	8.559	31.512
.67	28.535	-24.524	-30.673	-14.795	8.540	33.218
.68	30.230	-25.108	-32.254	-15.964	8.503	35.012
.69	32.021	-25.695	-33.905	-17.196	8.438	36.897
.70	33.913	-26.285	-35.631	-18.497	8.341	38.879
.71	35.910	-26.877	-37.433	-20.772	8.209	40.962
.72	38.019	-27.469	-39.315	-22.424	8.039	43.151
.73	40.245	-28.061	-41.280	-24.181	7.828	45.459
.74	42.593	-28.650	-43.332	-26.048	7.572	47.885
.75	45.071	-29.236	-45.473	-28.030	7.267	50.401
.76	47.685	-29.817	-47.707	-30.135	6.909	53.065
.77	50.442	-30.391	-50.038	-32.368	6.493	55.861
.78	53.350	-30.956	-52.468	-34.736	6.014	58.795
.79	56.415	-31.510	-55.003	-37.247	5.468	61.877
.80	59.646	-32.051	-57.645	-39.909	4.849	65.110
.81	63.050	-32.577	-60.399	-42.728	4.151	68.503
.82	66.638	-33.095	-63.268	-45.715	3.368	72.062
.83	70.418	-33.603	-66.258	-48.876	2.494	75.795
.84	74.398	-34.097	-69.371	-52.222	1.522	79.710
.85	78.580	-34.574	-72.614	-55.761	0.444	83.816
.86	83.003	-34.882	-76.989	-59.504	-0.748	88.120
.87	87.648	-35.227	-81.502	-63.461	-2.022	92.632
.88	92.527	-35.594	-86.157	-67.643	-3.506	97.362
.89	97.651	-35.989	-90.959	-72.061	-5.090	102.318
.90	103.022	-36.141	-95.914	-76.726	-6.823	107.511
.91	108.784	-36.341	-95.025	-81.652	-8.717	112.952
.92	114.768	-36.487	-99.299	-86.851	-10.781	118.650
.93	121.000	-36.574	-103.741	-92.336	-13.028	124.619
.94	127.674	-36.594	-108.356	-98.121	-15.471	130.869
.95	134.835	-36.544	-113.150	-104.222	-18.131	137.412
.96	141.927	-36.417	-118.128	-110.652	-20.993	144.253
.97	149.599	-36.206	-123.296	-117.428	-24.101	151.432
.98	157.656	-35.904	-128.660	-124.567	-27.461	158.935
.99	166.117	-35.503	-134.226	-132.083	-31.088	166.786

FITTING A GROWTH CURVE

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TABLE

Z	J 7, 1	J 7, 2	J 7, 3	J 7, 4	J 7, 5	J 7, 6	J 7, 7
.01	0.051	-5.132	0.918	1.039	1.041	1.041	1.041
.02	0.105	-5.269	0.831	1.077	1.085	1.085	1.085
.03	0.162	-5.410	0.740	1.114	1.121	1.122	1.122
.04	0.221	-5.555	0.644	1.149	1.179	1.181	1.181
.05	0.284	-5.706	0.542	1.182	1.220	1.224	1.224
.06	0.350	-5.862	0.435	1.213	1.264	1.290	1.290
.07	0.420	-6.023	0.322	1.242	1.340	1.349	1.350
.08	0.493	-6.190	0.203	1.269	1.398	1.412	1.414
.09	0.571	-6.362	0.078	1.293	1.459	1.480	1.482
.10	0.653	-6.541	-0.055	1.314	1.523	1.551	1.555
.11	0.740	-6.725	-0.195	1.332	1.589	1.627	1.632
.12	0.832	-6.917	-0.343	1.347	1.657	1.708	1.715
.13	0.930	-7.115	-0.499	1.358	1.728	1.793	1.804
.14	1.033	-7.319	-0.663	1.364	1.802	1.884	1.899
.15	1.143	-7.532	-0.837	1.367	1.877	1.981	2.000
.16	1.259	-7.751	-1.020	1.365	1.955	2.083	2.109
.17	1.383	-7.979	-1.214	1.357	2.035	2.192	2.225
.18	1.514	-8.214	-1.418	1.344	2.118	2.307	2.350
.19	1.653	-8.458	-1.634	1.324	2.202	2.429	2.483
.20	1.802	-8.711	-1.862	1.298	2.288	2.558	2.626
.21	1.959	-8.973	-2.103	1.265	2.377	2.695	2.780
.22	2.127	-9.244	-2.357	1.224	2.466	2.840	2.944
.23	2.306	-9.525	-2.625	1.175	2.558	2.993	3.120
.24	2.496	-9.817	-2.909	1.116	2.650	3.155	3.308
.25	2.699	-10.118	-3.208	1.048	2.744	3.326	3.511
.26	2.915	-10.431	-3.525	0.968	2.838	3.506	3.728
.27	3.145	-10.754	-3.859	0.878	2.933	3.697	3.960
.28	3.391	-11.089	-4.212	0.774	3.028	3.899	4.210
.29	3.653	-11.436	-4.585	0.658	3.122	4.111	4.477
.30	3.933	-11.796	-4.979	0.527	3.217	4.335	4.754
.31	4.231	-12.168	-5.395	0.380	3.310	4.571	5.072
.32	4.550	-12.554	-5.835	0.216	3.401	4.820	5.402
.33	4.899	-12.953	-6.300	0.034	3.490	5.082	5.755
.34	5.254	-13.365	-6.790	-0.167	3.577	5.357	6.135
.35	5.643	-13.793	-7.306	-0.389	3.660	5.647	6.542
.36	6.058	-14.235	-7.857	-0.635	3.739	5.941	6.978
.37	6.503	-14.692	-8.436	-0.904	3.812	6.271	7.446
.38	6.978	-15.164	-9.047	-1.200	3.880	6.607	7.947
.39	7.486	-15.653	-9.693	-1.525	3.940	6.960	8.485
.40	8.029	-16.158	-10.375	-1.879	3.992	7.330	9.061
.41	8.611	-16.679	-11.096	-2.267	4.035	7.718	9.679
.42	9.233	-17.218	-11.858	-2.689	4.067	8.124	10.341
.43	9.899	-17.773	-12.662	-3.150	4.086	8.550	11.051
.44	10.612	-18.347	-13.512	-3.651	4.091	8.995	11.811
.45	11.375	-18.938	-14.409	-4.185	4.080	9.460	12.626
.46	12.193	-19.546	-15.357	-4.756	4.052	9.946	13.499
.47	13.068	-20.174	-16.358	-5.368	4.003	10.454	14.435
.48	14.005	-20.819	-17.415	-6.124	3.932	10.984	15.437
.49	15.009	-21.483	-18.531	-6.977	3.836	11.536	16.510
.50	16.085	-22.165	-19.710	-7.992	3.712	12.111	17.659

TABLE

Z	J 7, 1	J 7, 2	J 7, 3	J 7, 4	J 7, 5	J 7, 6	J 7, 7
.51	17.237	-22.865	-20.954	-8.574	3.556	12.709	18.890
.52	18.472	-23.584	-22.268	-9.527	3.367	13.332	20.209
.53	19.794	-24.320	-21.654	-10.557	3.199	13.978	21.630
.54	21.212	-25.074	-21.118	-11.669	2.869	14.649	23.131
.55	22.730	-25.845	-20.663	-12.868	2.453	15.344	24.748
.56	24.357	-26.632	-20.292	-14.161	2.180	16.063	26.480
.57	26.101	-27.433	-20.012	-15.553	1.792	16.807	28.332
.58	27.869	-28.253	-19.826	-17.057	1.277	17.576	30.315
.59	29.771	-29.085	-19.739	-18.674	0.723	18.368	32.436
.60	32.117	-29.929	-19.757	-20.414	0.095	19.184	34.706
.61	34.415	-30.785	-19.885	-22.287	-0.614	20.022	37.134
.62	36.879	-31.650	-20.128	-24.300	-1.413	20.882	39.730
.63	39.518	-32.522	-20.493	-26.464	-2.309	21.763	42.507
.64	42.340	-33.400	-20.985	-28.789	-3.313	22.663	45.477
.65	45.375	-34.280	-21.611	-31.286	-4.432	23.581	48.653
.66	48.621	-35.161	-20.377	-33.967	-5.679	24.515	52.047
.67	52.098	-36.038	-19.390	-36.845	-7.063	25.462	55.676
.68	55.823	-36.908	-18.638	-39.932	-8.599	26.419	59.555
.69	59.812	-37.767	-18.088	-43.243	-10.298	27.384	63.700
.70	64.083	-38.612	-18.787	-46.763	-12.176	28.353	68.109
.71	68.660	-39.436	-19.665	-50.597	-14.247	29.321	72.863
.72	73.559	-40.234	-20.728	-54.672	-16.528	30.284	77.919
.73	78.895	-41.000	-21.983	-59.037	-19.038	31.226	83.330
.74	84.421	-41.728	-23.447	-63.711	-21.795	32.171	89.088
.75	90.133	-42.419	-25.121	-68.713	-24.800	33.083	95.248
.76	96.067	-43.037	-27.017	-74.065	-28.136	33.963	101.826
.77	102.252	-43.602	-29.245	-79.789	-31.797	34.803	108.848
.78	111.120	-44.094	-31.816	-85.910	-35.737	35.593	116.344
.79	119.903	-44.502	-34.639	-92.434	-40.076	36.323	124.345
.80	127.436	-44.814	-37.726	-99.466	-44.813	36.980	132.884
.81	136.455	-45.019	-41.088	-106.915	-49.979	37.551	141.995
.82	146.100	-45.101	-44.763	-114.802	-55.609	38.022	151.715
.83	156.413	-45.065	-48.800	-123.009	-61.740	38.376	162.085
.84	167.439	-44.836	-53.244	-131.498	-68.411	38.595	173.145
.85	179.224	-44.454	-58.069	-140.296	-75.664	38.660	184.940
.86	191.819	-43.881	-63.219	-149.351	-83.544	38.548	197.518
.87	205.277	-43.094	-68.674	-158.671	-92.100	38.237	210.927
.88	219.655	-42.072	-74.389	-168.270	-101.384	37.699	225.221
.89	235.014	-40.789	-80.376	-178.161	-111.450	36.907	240.456
.90	251.416	-39.218	-86.649	-188.310	-122.367	35.828	256.691
.91	268.930	-37.331	-93.200	-198.728	-134.170	34.429	273.990
.92	287.627	-35.095	-100.103	-209.466	-146.955	32.672	292.419
.93	307.585	-32.477	-110.211	-221.579	-160.785	30.517	311.950
.94	328.883	-29.440	-120.758	-234.824	-175.737	27.919	332.667
.95	351.607	-25.945	-131.768	-249.261	-191.862	24.829	355.629
.96	375.849	-21.950	-143.223	-264.856	-209.339	21.195	379.823
.97	401.704	-17.408	-155.187	-281.567	-228.170	16.969	405.156
.98	429.275	-12.272	-167.602	-300.388	-248.485	12.061	431.612
.99	458.668	-6.488	-180.542	-321.270	-270.391	6.432	459.301

FITTING A GROWTH CURVE

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TABLE

Z	J 8, 1	J 8, 2	J 8, 3	J 8, 4	J 8, 5	J 8, 6	J 8, 7	J 8, 8
.01	0.062	-0.103	0.897	1.039	1.041	1.041	1.041	1.041
.02	0.126	-0.201	0.789	1.076	1.085	1.085	1.085	1.085
.03	0.195	-0.305	0.674	1.111	1.131	1.132	1.132	1.132
.04	0.266	-0.436	0.553	1.144	1.179	1.181	1.181	1.181
.05	0.342	-0.573	0.425	1.174	1.220	1.224	1.224	1.224
.06	0.423	-0.706	0.290	1.200	1.263	1.269	1.269	1.269
.07	0.507	-0.836	0.148	1.224	1.308	1.319	1.319	1.319
.08	0.597	-1.000	0.003	1.244	1.356	1.412	1.414	1.414
.09	0.693	-1.209	-0.162	1.260	1.406	1.479	1.482	1.482
.10	0.793	-1.462	-0.331	1.273	1.457	1.550	1.555	1.555
.11	0.900	-1.764	-0.509	1.280	1.581	1.626	1.632	1.633
.12	1.013	-2.114	-0.697	1.283	1.647	1.706	1.715	1.716
.13	1.134	-2.514	-0.897	1.280	1.715	1.791	1.804	1.806
.14	1.262	-2.961	-1.108	1.271	1.784	1.881	1.898	1.901
.15	1.398	-3.459	-1.331	1.255	1.853	1.977	2.000	2.004
.16	1.543	-4.007	-1.567	1.233	1.927	2.078	2.108	2.114
.17	1.698	-4.611	-1.817	1.203	2.001	2.183	2.224	2.232
.18	1.863	-5.276	-2.081	1.164	2.075	2.298	2.348	2.359
.19	2.038	-6.007	-2.361	1.116	2.150	2.417	2.481	2.496
.20	2.225	-6.809	-2.658	1.059	2.225	2.543	2.623	2.648
.21	2.425	-7.686	-2.972	0.990	2.300	2.676	2.776	2.801
.22	2.639	-8.641	-3.305	0.910	2.375	2.816	2.939	2.972
.23	2.867	-9.677	-3.657	0.817	2.449	2.963	3.113	3.155
.24	3.111	-10.794	-4.031	0.710	2.522	3.118	3.300	3.353
.25	3.372	-11.994	-4.426	0.588	2.593	3.281	3.500	3.567
.26	3.651	-13.281	-4.846	0.450	2.661	3.452	3.715	3.797
.27	3.950	-14.659	-5.290	0.295	2.726	3.632	3.944	4.047
.28	4.271	-16.132	-5.762	0.130	2.788	3.820	4.190	4.316
.29	4.614	-17.704	-6.261	-0.076	2.844	4.018	4.453	4.606
.30	4.982	-19.379	-6.791	-0.294	2.895	4.224	4.734	4.921
.31	5.378	-21.164	-7.353	-0.536	2.940	4.440	5.035	5.261
.32	5.802	-23.067	-7.949	-0.805	2.976	4.664	5.338	5.629
.33	6.257	-25.098	-8.581	-1.102	3.004	4.899	5.703	6.027
.34	6.747	-27.268	-9.252	-1.430	3.021	5.143	6.072	6.458
.35	7.273	-29.581	-9.963	-1.792	3.025	5.397	6.466	6.925
.36	7.839	-32.043	-10.718	-2.190	3.016	5.660	6.888	7.430
.37	8.447	-34.663	-11.519	-2.627	2.992	5.932	7.339	7.978
.38	9.102	-37.448	-12.369	-3.105	2.950	6.215	7.821	8.571
.39	9.807	-40.408	-13.272	-3.632	2.887	6.506	8.337	9.214
.40	10.567	-43.557	-14.229	-4.207	2.802	6.806	8.887	9.912
.41	11.385	-46.901	-15.246	-4.835	2.692	7.114	9.475	10.668
.42	12.267	-50.446	-16.325	-5.522	2.553	7.439	10.103	11.487
.43	13.218	-54.200	-17.471	-6.272	2.382	7.783	10.773	12.376
.44	14.244	-58.170	-18.688	-7.080	2.175	8.083	11.487	13.340
.45	15.351	-62.363	-19.979	-7.950	1.929	8.317	12.250	14.386
.46	16.546	-66.796	-21.350	-8.931	1.638	8.456	13.063	15.520
.47	17.835	-71.486	-22.807	-10.007	1.298	8.507	13.930	16.751
.48	19.230	-76.450	-24.353	-11.156	0.903	8.438	14.854	18.087
.49	20.736	-81.706	-25.994	-12.404	0.447	8.279	15.838	19.538
.50	22.363	-87.272	-27.737	-13.762	-0.070	8.015	16.880	21.108

TABLE

Z	J 8, 1	J 8, 2	J 8, 3	J 8, 4	J 8, 5	J 8, 6	J 8, 7	J 8, 8
.51	24.123	-29.886	-29.588	-15.226	-0.674	10.446	18.001	22.814
.52	26.025	-30.903	-31.553	-16.836	-1.354	10.767	19.187	24.666
.53	28.083	-31.945	-33.839	-18.772	-2.126	11.075	20.448	26.676
.54	30.310	-33.014	-35.854	-20.456	-2.998	11.366	21.789	28.837
.55	32.720	-34.107	-38.205	-22.460	-3.982	11.635	23.213	31.225
.56	35.329	-35.222	-40.701	-24.713	-5.088	11.878	24.725	33.794
.57	38.133	-36.359	-43.351	-27.113	-6.330	12.087	26.330	36.583
.58	41.212	-37.513	-46.162	-29.712	-7.720	12.256	28.031	39.610
.59	44.524	-38.684	-49.146	-32.527	-9.275	12.378	29.824	42.865
.60	48.114	-39.866	-52.312	-35.575	-11.009	12.444	31.744	46.461
.61	52.003	-41.056	-55.671	-38.873	-12.942	12.444	33.765	50.331
.62	56.217	-42.250	-59.233	-42.442	-15.092	12.367	35.903	54.332
.63	60.785	-43.442	-63.012	-46.303	-17.482	12.201	38.161	58.601
.64	65.737	-44.625	-67.018	-50.478	-20.134	11.932	40.546	64.039
.65	71.105	-45.792	-71.265	-54.992	-23.073	11.545	43.063	69.410
.66	76.926	-46.935	-75.767	-59.871	-26.329	11.022	45.714	75.238
.67	83.238	-48.044	-80.536	-65.143	-29.930	10.345	48.506	81.963
.68	90.083	-49.109	-85.589	-70.839	-33.910	9.492	51.433	88.428
.69	97.408	-50.117	-90.839	-76.990	-38.305	8.439	54.528	95.876
.70	105.260	-51.054	-96.604	-83.633	-43.154	7.169	57.796	103.669
.71	114.295	-51.904	-102.599	-90.804	-48.500	5.625	61.158	112.730
.72	123.769	-52.651	-108.941	-98.543	-54.390	3.802	64.708	122.246
.73	134.047	-53.273	-115.650	-106.804	-60.873	1.654	68.417	132.271
.74	145.196	-53.749	-122.740	-115.902	-68.004	-0.859	72.286	143.773
.75	157.291	-54.055	-130.222	-125.617	-75.845	-2.782	76.315	155.926
.76	170.411	-54.161	-138.146	-136.022	-84.459	-5.164	80.502	169.108
.77	184.644	-54.057	-146.501	-147.382	-93.917	-8.009	84.844	183.408
.78	200.083	-53.648	-155.317	-159.749	-104.216	-11.227	89.337	198.918
.79	216.831	-52.957	-164.614	-174.057	-115.690	-14.836	93.973	215.739
.80	234.997	-51.920	-174.413	-186.774	-128.157	-18.839	98.744	233.982
.81	254.701	-50.490	-184.735	-201.676	-141.828	-33.076	103.639	253.764
.82	276.071	-48.615	-195.601	-218.339	-156.796	-46.577	108.642	275.215
.83	299.248	-46.227	-207.033	-235.949	-173.179	-61.639	113.737	298.472
.84	324.381	-43.291	-219.050	-254.895	-191.100	-78.632	118.901	323.686
.85	351.633	-39.707	-231.673	-275.272	-210.605	-96.413	124.108	351.019
.86	381.181	-35.407	-244.923	-297.182	-232.119	-115.834	129.328	380.645
.87	413.216	-30.204	-258.818	-320.733	-255.502	-137.137	134.534	412.755
.88	447.941	-24.304	-273.378	-346.040	-281.044	-160.581	139.654	447.533
.89	485.380	-17.303	-288.619	-373.247	-308.921	-187.437	144.665	485.259
.90	526.372	-9.186	-304.558	-402.423	-339.331	-216.494	149.568	526.114
.91	570.575	0.172	-321.208	-433.768	-372.493	-247.761	154.109	570.373
.92	618.468	10.910	-338.581	-467.407	-408.638	-291.463	158.394	618.317
.93	670.333	23.179	-356.688	-503.498	-448.018	-347.530	162.378	670.244
.94	726.333	37.144	-375.334	-542.205	-490.906	-407.193	165.861	726.480
.95	787.419	52.687	-395.122	-583.705	-537.394	-479.788	168.430	787.574
.96	853.328	70.907	-415.453	-628.184	-588.400	-565.960	170.459	853.303
.97	924.683	91.120	-436.519	-675.838	-643.661	-656.963	171.603	924.674
.98	1001.629	113.863	-458.312	-726.877	-703.747	-760.483	171.700	1001.626
.99	1085.531	139.396	-480.813	-781.519	-769.051	-889.642	170.568	1085.530

FITTING A GROWTH CURVE

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TABLE



Z	J 9, 1	J 9, 2	J 9, 3	J 9, 4	J 9, 5	J 9, 6	J 9, 7	J 9, 8	J 9, 9
.01	0.072	-7.193	0.877	1.039	1.041	1.041	1.041	1.041	1.041
.02	0.148	-7.394	0.746	1.075	1.085	1.085	1.085	1.085	1.085
.03	0.227	-7.601	0.608	1.108	1.131	1.132	1.132	1.132	1.132
.04	0.312	-7.816	0.463	1.138	1.170	1.181	1.181	1.181	1.181
.05	0.401	-8.039	0.309	1.165	1.229	1.234	1.234	1.234	1.234
.06	0.495	-8.270	0.146	1.187	1.282	1.289	1.290	1.290	1.290
.07	0.595	-8.510	-0.027	1.206	1.337	1.349	1.350	1.350	1.350
.08	0.701	-8.758	-0.209	1.219	1.393	1.412	1.414	1.414	1.414
.09	0.814	-9.016	-0.402	1.228	1.452	1.479	1.482	1.482	1.482
.10	0.933	-9.284	-0.606	1.231	1.512	1.550	1.554	1.555	1.555
.11	1.060	-9.562	-0.823	1.228	1.574	1.625	1.632	1.633	1.633
.12	1.195	-9.851	-1.052	1.219	1.637	1.705	1.715	1.716	1.717
.13	1.338	-10.151	-1.295	1.202	1.701	1.789	1.803	1.806	1.806
.14	1.491	-10.462	-1.552	1.177	1.767	1.878	1.898	1.901	1.902
.15	1.654	-10.786	-1.825	1.144	1.835	1.973	1.999	2.004	2.005
.16	1.828	-11.123	-2.113	1.101	1.899	2.072	2.107	2.114	2.115
.17	2.013	-11.473	-2.420	1.048	1.966	2.177	2.225	2.232	2.234
.18	2.211	-11.837	-2.745	0.984	2.032	2.288	2.348	2.359	2.362
.19	2.423	-12.216	-3.089	0.908	2.097	2.404	2.478	2.495	2.499
.20	2.649	-12.610	-3.454	0.818	2.161	2.527	2.620	2.642	2.647
.21	2.891	-13.020	-3.842	0.714	2.223	2.656	2.771	2.800	2.807
.22	3.151	-13.446	-4.254	0.594	2.282	2.790	2.922	2.970	2.980
.23	3.428	-13.890	-4.691	0.457	2.339	2.932	3.105	3.153	3.166
.24	3.726	-14.352	-5.155	0.302	2.391	3.079	3.280	3.351	3.368
.25	4.046	-14.834	-5.647	0.126	2.438	3.234	3.487	3.564	3.586
.26	4.389	-15.335	-6.171	-0.072	2.480	3.395	3.698	3.793	3.823
.27	4.757	-15.856	-6.727	-0.294	2.514	3.562	3.923	4.041	4.073
.28	5.153	-16.400	-7.317	-0.542	2.541	3.736	4.163	4.309	4.357
.29	5.578	-16.966	-7.943	-0.818	2.558	3.916	4.420	4.598	4.659
.30	6.036	-17.555	-8.613	-1.125	2.563	4.102	4.694	4.910	4.987
.31	6.530	-18.169	-9.323	-1.465	2.556	4.295	4.986	5.247	5.343
.32	7.061	-18.808	-10.078	-1.842	2.535	4.493	5.297	5.612	5.731
.33	7.634	-19.473	-10.882	-2.259	2.498	4.696	5.629	6.006	6.153
.34	8.252	-20.167	-11.739	-2.719	2.439	4.903	5.983	6.432	6.613
.35	8.918	-20.888	-12.646	-3.225	2.360	5.115	6.359	6.893	7.114
.36	9.638	-21.639	-13.614	-3.783	2.256	5.330	6.760	7.392	7.661
.37	10.416	-22.421	-14.645	-4.396	2.125	5.547	7.186	7.931	8.238
.38	11.258	-23.235	-15.743	-5.068	1.962	5.765	7.639	8.514	8.909
.39	12.168	-24.082	-16.912	-5.807	1.763	5.982	8.120	9.145	9.621
.40	13.152	-24.962	-18.158	-6.616	1.529	6.198	8.630	9.828	10.398
.41	14.219	-25.877	-19.484	-7.502	1.248	6.409	9.171	10.567	11.249
.42	15.375	-26.828	-20.898	-8.473	0.918	6.615	9.744	11.367	12.179
.43	16.629	-27.815	-22.405	-9.535	0.534	6.812	10.351	12.233	13.197
.44	17.988	-28.840	-24.011	-10.695	0.087	6.998	10.992	13.169	14.311
.45	19.464	-29.903	-25.723	-11.964	-0.428	7.169	11.670	14.182	15.532
.46	21.068	-31.004	-27.548	-13.350	-1.019	7.321	12.385	15.278	16.869
.47	22.809	-32.145	-29.494	-14.863	-1.690	7.450	13.138	16.465	18.335
.48	24.703	-33.324	-31.569	-16.515	-2.467	7.551	13.931	17.748	19.942
.49	26.764	-34.543	-33.782	-18.317	-3.343	7.618	14.764	19.126	21.704
.50	29.006	-35.801	-36.143	-20.282	-4.337	7.644	15.638	20.637	23.638

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FISH BULLETIN NO. 116

TABLE

Z	J 9, 1	J 9, 2	J 9, 3	J 9, 4	J 9, 5	J 9, 6	J 9, 7	J 9, 8	J 9, 9
.51	31.448	-37.098	-38.660	-22.426	-6.460	7.622	16.554	22.261	25.759
.52	34.108	-38.831	-41.346	-24.783	-8.728	7.544	17.311	24.017	28.088
.53	37.007	-39.801	-44.210	-27.309	-8.155	7.400	18.509	25.915	30.644
.54	40.170	-41.204	-47.266	-30.084	-7.760	7.180	19.548	27.966	33.451
.55	43.620	-42.639	-50.525	-33.107	-11.562	6.870	20.626	30.183	36.535
.56	47.385	-44.102	-54.002	-36.400	-13.581	6.457	21.742	32.579	39.922
.57	51.468	-45.580	-57.711	-39.986	-15.841	5.925	22.894	35.166	43.644
.58	55.991	-47.065	-61.665	-43.860	-18.368	5.257	24.077	37.960	47.734
.59	60.901	-48.614	-65.884	-48.140	-21.191	4.433	25.288	40.977	52.230
.60	66.270	-50.139	-70.382	-52.766	-24.340	3.430	26.521	44.232	57.173
.61	72.143	-51.691	-75.178	-57.801	-27.850	2.224	27.769	47.744	62.608
.62	78.570	-53.170	-80.260	-63.279	-31.728	0.786	29.025	51.522	68.585
.63	85.605	-54.654	-85.739	-69.238	-36.110	-0.916	30.278	55.615	75.159
.64	93.306	-56.068	-91.546	-75.722	-40.947	-2.918	31.517	60.015	82.390
.65	101.747	-57.487	-97.732	-82.773	-46.323	-5.238	32.736	64.755	90.345
.66	110.995	-58.802	-104.320	-90.441	-52.293	-7.983	33.988	69.838	99.098
.67	121.131	-60.019	-111.334	-98.779	-58.918	-11.142	34.985	75.348	108.729
.68	132.244	-61.115	-118.800	-107.843	-66.208	-14.791	35.991	81.254	119.328
.69	144.432	-62.059	-126.743	-117.696	-74.415	-18.994	36.880	87.601	130.994
.70	157.804	-62.819	-135.190	-128.404	-83.442	-23.820	37.619	94.419	143.834
.71	172.476	-63.336	-144.169	-140.040	-93.440	-29.348	38.170	101.738	157.968
.72	188.580	-63.626	-153.707	-152.952	-104.507	-35.666	38.461	109.689	173.528
.73	206.258	-63.779	-163.836	-166.414	-116.752	-42.871	38.530	118.004	190.659
.74	225.669	-63.810	-174.583	-181.328	-130.295	-51.073	38.231	127.017	209.519
.75	246.987	-62.300	-185.979	-197.522	-145.267	-60.393	37.526	136.662	230.287
.76	270.403	-60.833	-198.034	-215.102	-161.813	-70.967	36.339	146.972	253.154
.77	296.129	-58.968	-210.838	-234.183	-180.091	-82.947	34.583	157.983	278.335
.78	324.390	-56.317	-224.362	-254.889	-200.273	-96.860	32.158	169.729	306.094
.79	355.447	-52.874	-238.653	-277.352	-222.551	-111.814	28.950	182.245	336.602
.80	389.579	-48.518	-253.741	-301.716	-247.133	-129.097	24.828	195.565	370.232
.81	427.092	-43.115	-269.650	-328.134	-274.247	-148.581	19.645	209.720	407.270
.82	468.527	-36.516	-286.406	-356.772	-304.144	-170.022	13.252	224.741	448.060
.83	513.654	-28.547	-304.029	-387.807	-337.098	-195.208	5.398	240.654	492.983
.84	563.483	-19.021	-322.537	-421.430	-373.408	-222.934	-4.074	257.484	542.458
.85	618.262	-7.723	-341.944	-457.846	-413.403	-254.113	-15.428	275.248	596.947
.86	678.486	3.587	-362.257	-497.272	-457.441	-289.075	-28.943	293.959	656.957
.87	744.696	21.177	-383.477	-539.944	-505.915	-328.273	-44.953	313.622	723.046
.88	817.488	59.348	-405.098	-586.113	-559.251	-372.183	-63.750	334.232	795.828
.89	897.516	80.433	-428.605	-636.045	-617.919	-421.343	-85.794	355.775	875.979
.90	985.495	84.814	-452.469	-690.026	-682.429	-476.333	-111.515	378.221	964.242
.91	1082.215	112.901	-477.153	-748.361	-753.337	-537.896	-141.419	401.625	1061.434
.92	1188.537	145.164	-502.600	-811.374	-831.251	-606.479	-175.074	425.924	1168.454
.93	1305.410	182.122	-528.740	-879.411	-916.854	-683.147	-216.121	450.432	1286.288
.94	1433.871	224.333	-555.480	-952.836	-1010.806	-768.085	-262.276	475.836	1416.023
.95	1575.059	272.502	-582.705	-1032.040	-1113.953	-864.062	-315.344	501.694	1558.849
.96	1730.222	327.288	-610.274	-1117.454	-1227.130	-970.947	-376.228	527.826	1716.079
.97	1900.728	389.492	-638.014	-1209.454	-1351.267	-1088.717	-445.938	554.021	1889.150
.98	2086.073	460.010	-665.720	-1308.560	-1487.376	-1220.471	-525.602	580.934	2079.642
.99	2293.897	539.817	-693.145	-1415.238	-1636.554	-1367.039	-616.485	605.458	2289.289

FITTING A GROWTH CURVE

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TABLE

Z	J 10, 1	J 10, 2	J 10, 3	J 10, 4	J 10, 5	J 10, 6	J 10, 7	J 10, 8	J 10, 9
.01	0.082	-8.224	0.856	1.038	1.041	1.041	1.041	1.041	1.041
.02	0.169	-8.456	0.704	1.074	1.085	1.085	1.085	1.085	1.085
.03	0.260	-8.697	0.542	1.105	1.131	1.132	1.132	1.132	1.132
.04	0.357	-8.946	0.372	1.133	1.179	1.181	1.181	1.181	1.181
.05	0.460	-9.205	0.192	1.156	1.229	1.234	1.234	1.234	1.234
.06	0.568	-9.474	0.001	1.174	1.281	1.289	1.290	1.290	1.290
.07	0.683	-9.753	-0.201	1.187	1.335	1.349	1.350	1.350	1.350
.08	0.805	-10.042	-0.415	1.195	1.391	1.412	1.414	1.414	1.414
.09	0.935	-10.343	-0.642	1.196	1.448	1.478	1.482	1.482	1.482
.10	1.073	-10.656	-0.882	1.190	1.506	1.549	1.554	1.555	1.555
.11	1.220	-10.980	-1.137	1.176	1.566	1.624	1.632	1.633	1.633
.12	1.376	-11.318	-1.407	1.155	1.627	1.703	1.715	1.716	1.717
.13	1.541	-11.669	-1.693	1.124	1.688	1.787	1.803	1.806	1.806
.14	1.720	-12.034	-1.997	1.084	1.749	1.875	1.897	1.901	1.902
.15	1.910	-12.414	-2.319	1.032	1.810	1.968	1.998	2.004	2.005
.16	2.112	-12.808	-2.660	0.969	1.871	2.067	2.106	2.114	2.115
.17	2.328	-13.220	-3.023	0.894	1.930	2.170	2.221	2.232	2.234
.18	2.560	-13.649	-3.408	0.804	1.988	2.278	2.344	2.359	2.362
.19	2.808	-14.095	-3.817	0.699	2.044	2.392	2.476	2.495	2.499
.20	3.073	-14.559	-4.251	0.577	2.096	2.511	2.576	2.611	2.617
.21	3.357	-15.044	-4.713	0.438	2.145	2.635	2.706	2.759	2.807
.22	3.662	-15.548	-5.203	0.278	2.189	2.765	2.826	2.909	2.989
.23	3.990	-16.074	-5.721	0.097	2.228	2.900	3.096	3.151	3.196
.24	4.342	-16.622	-6.279	-0.107	2.260	3.040	3.278	3.348	3.368
.25	4.720	-17.193	-6.879	-0.337	2.285	3.185	3.473	3.560	3.586
.26	5.126	-17.789	-7.496	-0.595	2.308	3.335	3.680	3.788	3.822
.27	5.564	-18.411	-8.164	-0.883	2.301	3.490	3.900	4.035	4.077
.28	6.036	-19.059	-8.875	-1.205	2.292	3.649	4.135	4.300	4.353
.29	6.544	-19.735	-9.632	-1.565	2.268	3.811	4.384	4.587	4.656
.30	7.089	-20.441	-10.439	-1.960	2.228	3.977	4.650	4.896	4.985
.31	7.684	-21.177	-11.298	-2.399	2.168	4.145	4.932	5.229	5.338
.32	8.323	-21.944	-12.213	-2.886	2.087	4.314	5.231	5.589	5.725
.33	9.014	-22.746	-13.190	-3.424	1.981	4.484	5.548	5.978	6.143
.34	9.761	-23.582	-14.230	-4.017	1.847	4.654	5.884	6.397	6.603
.35	10.570	-24.454	-15.341	-4.671	1.681	4.821	6.240	6.849	7.102
.36	11.446	-25.363	-16.525	-5.392	1.479	4.983	6.616	7.337	7.645
.37	12.396	-26.312	-17.790	-6.184	1.257	5.141	7.013	7.864	8.238
.38	13.426	-27.301	-19.139	-7.055	0.995	5.289	7.431	8.432	8.884
.39	14.545	-28.332	-20.580	-8.012	0.692	5.427	7.871	9.045	9.589
.40	15.759	-29.407	-22.120	-9.063	0.347	5.551	8.334	9.707	10.360
.41	17.081	-30.527	-23.764	-10.216	-0.243	5.657	8.819	10.420	11.201
.42	18.519	-31.692	-25.221	-11.480	-0.775	5.741	9.326	11.188	12.120
.43	20.084	-32.906	-27.400	-12.967	-1.387	5.799	9.859	12.017	13.123
.44	21.789	-34.168	-29.408	-14.589	-2.089	5.825	10.408	12.910	14.223
.45	23.642	-35.479	-31.355	-16.341	-2.891	5.813	10.982	13.871	15.425
.46	25.677	-36.841	-33.852	-17.874	-3.806	5.755	11.575	14.906	16.739
.47	27.863	-38.254	-36.309	-19.870	-4.846	5.645	12.187	16.020	18.177
.48	30.211	-39.718	-38.973	-22.055	-6.026	5.471	12.816	17.218	19.751
.49	32.691	-41.233	-41.752	-24.447	-7.363	5.225	13.458	18.505	21.474
.50	35.359	-42.799	-44.764	-27.064	-8.873	4.908	14.111	19.888	23.361

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FISH BULLETIN NO. 116

TABLE

Z	J 10, 1	J 10, 2	J 10, 3	J 10, 4	J 10, 5	J 10, 6	J 10, 7	J 10, 8	J 10, 9
.51	39.032	-44.415	-47.988	-29.928	-10.577	4.463	14.771	21.373	25.428
.52	42.409	-46.079	-51.440	-31.061	-12.468	3.919	13.432	22.866	27.488
.53	46.323	-47.788	-55.136	-36.488	-14.658	3.243	16.087	24.673	30.166
.54	50.509	-49.539	-59.093	-40.238	-17.087	2.416	16.730	26.501	32.880
.55	55.106	-51.328	-63.331	-44.338	-19.815	1.416	17.311	28.437	35.833
.56	60.168	-53.150	-67.870	-48.823	-22.874	0.215	17.938	30.547	39.111
.57	65.715	-55.007	-72.731	-53.728	-26.303	-1.213	18.490	32.777	42.678
.58	71.829	-56.861	-77.936	-59.092	-30.143	-2.903	18.950	35.155	46.588
.59	78.563	-58.720	-83.510	-64.938	-34.441	-4.889	19.360	37.688	50.870
.60	85.983	-60.594	-89.478	-71.373	-39.247	-7.215	19.659	40.370	55.562
.61	94.165	-62.434	-95.868	-78.387	-44.619	-9.927	19.832	43.229	60.701
.62	103.192	-64.234	-102.708	-85.937	-50.621	-13.080	19.818	46.250	66.328
.63	113.159	-65.971	-110.029	-94.444	-57.321	-16.732	19.676	49.441	72.494
.64	124.168	-67.619	-117.861	-103.614	-64.800	-20.932	19.274	52.803	79.245
.65	136.337	-69.177	-126.233	-113.611	-73.142	-25.817	18.566	56.317	86.636
.66	149.795	-70.518	-135.196	-124.603	-82.445	-31.412	17.588	60.038	94.727
.67	164.687	-71.691	-144.770	-136.287	-92.815	-37.836	16.180	63.901	103.583
.68	181.174	-72.615	-154.998	-149.688	-104.372	-45.197	14.326	67.916	113.274
.69	199.437	-73.232	-165.919	-164.009	-117.243	-53.620	11.918	72.069	123.874
.70	219.678	-73.476	-177.572	-179.663	-131.582	-63.244	8.868	76.341	135.467
.71	242.130	-73.267	-189.999	-196.771	-147.544	-74.227	5.068	80.707	148.142
.72	267.015	-72.515	-203.239	-215.467	-165.310	-86.744	0.369	85.133	161.998
.73	294.643	-71.117	-217.333	-235.806	-185.079	-100.994	-5.311	89.579	177.127
.74	325.317	-68.950	-232.323	-258.215	-207.072	-117.202	-12.200	93.990	193.652
.75	359.387	-65.876	-248.248	-282.596	-231.233	-135.618	-20.469	98.393	211.685
.76	397.244	-61.734	-265.145	-309.223	-258.732	-156.226	-30.336	102.437	231.367
.77	439.372	-56.342	-283.039	-338.208	-288.968	-180.242	-42.033	106.206	252.821
.78	486.109	-49.487	-301.991	-370.040	-322.374	-207.125	-55.904	109.763	276.199
.79	538.149	-40.628	-321.997	-404.684	-359.915	-237.574	-72.217	113.066	301.657
.80	596.049	-30.387	-343.057	-442.486	-401.397	-272.040	-91.365	114.926	329.360
.81	660.488	-17.549	-365.271	-483.721	-447.470	-311.027	-113.776	116.233	359.482
.82	731.221	-2.050	-388.550	-528.686	-498.927	-353.103	-139.333	116.838	392.207
.83	812.095	16.522	-412.913	-577.703	-555.417	-404.899	-170.391	115.199	427.727
.84	901.054	38.637	-438.339	-631.115	-618.445	-461.139	-205.781	112.204	466.244
.85	1000.151	64.834	-464.746	-690.293	-688.377	-524.091	-246.818	107.061	507.965
.86	1110.561	95.723	-492.119	-752.633	-765.949	-596.176	-294.319	99.312	553.104
.87	1233.098	131.998	-520.324	-819.262	-851.374	-676.884	-349.208	88.421	601.879
.88	1370.726	174.449	-549.238	-896.632	-947.345	-767.832	-412.539	73.761	654.511
.89	1523.378	223.973	-578.696	-978.029	-1053.948	-870.271	-485.594	54.602	711.218
.90	1693.976	281.287	-608.481	-1066.567	-1170.167	-985.598	-569.457	30.096	772.216
.91	1883.955	348.444	-638.327	-1162.663	-1299.895	-1115.375	-665.931	-0.745	837.710
.92	2093.779	425.851	-667.905	-1296.987	-1443.544	-1261.346	-776.664	-39.061	907.894
.93	2331.977	515.287	-696.811	-1380.059	-1602.556	-1425.459	-903.622	-89.175	982.039
.94	2596.366	618.426	-724.560	-1492.562	-1778.513	-1609.886	-1049.029	-143.616	1062.087
.95	2889.084	737.161	-749.467	-1621.139	-1976.152	-1817.051	-1215.401	-213.147	1148.145
.96	3216.633	873.630	-774.133	-1778.425	-2188.389	-2049.654	-1405.578	-296.801	1238.469
.97	3581.903	1030.245	-794.429	-1951.439	-2429.282	-2310.703	-1622.769	-399.618	1333.652
.98	3989.243	1209.732	-810.474	-2100.635	-2689.146	-2603.656	-1870.393	-516.188	1434.510
.99	4443.479	1415.162	-821.115	-2280.890	-2979.471	-2931.935	-2153.135	-637.700	1539.959

FITTING A GROWTH CURVE

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TABLE

Z	J 10, 10
.01	1.041
.02	1.085
.03	1.132
.04	1.181
.05	1.234
.06	1.290
.07	1.350
.08	1.414
.09	1.482
.10	1.555
.11	1.633
.12	1.717
.13	1.806
.14	1.902
.15	2.005
.16	2.115
.17	2.234
.18	2.362
.19	2.500
.20	2.649
.21	2.809
.22	2.982
.23	3.170
.24	3.373
.25	3.593
.26	3.832
.27	4.091
.28	4.373
.29	4.679
.30	5.013
.31	5.377
.32	5.775
.33	6.209
.34	6.684
.35	7.204
.36	7.773
.37	8.397
.38	9.083
.39	9.835
.40	10.662
.41	11.572
.42	12.574
.43	13.675
.44	14.895
.45	16.238
.46	17.721
.47	19.358
.48	21.169
.49	23.172
.50	25.389

TABLE

Z	J 10, 10
.51	27.843
.52	30.563
.53	33.377
.54	36.291
.55	40.030
.56	44.748
.57	49.321
.58	54.401
.59	60.048
.60	66.328
.61	73.310
.62	81.079
.63	89.727
.64	99.354
.65	110.079
.66	122.028
.67	135.249
.68	150.181
.69	166.728
.70	185.183
.71	205.770
.72	228.743
.73	254.382
.74	283.003
.75	314.960
.76	350.649
.77	390.513
.78	435.049
.79	484.813
.80	540.428
.81	602.591
.82	672.083
.83	749.780
.84	836.661
.85	933.824
.86	1042.496
.87	1164.035
.88	1300.040
.89	1452.178
.90	1622.395
.91	1812.857
.92	2025.983
.93	2264.480
.94	2531.378
.95	2830.065
.96	3164.340
.97	3538.455
.98	3957.106
.99	4425.647

FITTING A GROWTH CURVE

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TABLE

Z	J 11, 1	J 11, 2	J 11, 3	J 11, 4	J 11, 5	J 11, 6	J 11, 7	J 11, 8	J 11, 9
.01	0.092	-0.255	0.835	1.038	1.041	1.041	1.041	1.041	1.041
.02	0.190	-0.519	0.991	1.072	1.085	1.085	1.085	1.085	1.085
.03	0.293	-0.702	0.477	1.102	1.130	1.132	1.132	1.132	1.132
.04	0.408	-10.077	0.282	1.127	1.173	1.181	1.181	1.181	1.181
.05	0.538	-10.272	0.075	1.147	1.228	1.234	1.234	1.234	1.234
.06	0.641	-10.078	-0.144	1.161	1.280	1.289	1.290	1.290	1.290
.07	0.771	-10.906	-0.376	1.169	1.333	1.349	1.350	1.350	1.350
.08	0.909	-11.326	-0.621	1.170	1.388	1.411	1.414	1.414	1.414
.09	1.056	-11.670	-0.882	1.183	1.444	1.478	1.482	1.482	1.482
.10	1.213	-12.027	-1.158	1.148	1.501	1.548	1.554	1.555	1.555
.11	1.380	-12.399	-1.451	1.124	1.559	1.623	1.632	1.633	1.633
.12	1.557	-12.785	-1.761	1.091	1.618	1.702	1.714	1.716	1.717
.13	1.747	-13.187	-2.091	1.046	1.674	1.785	1.803	1.806	1.806
.14	1.949	-13.606	-2.441	0.990	1.732	1.872	1.897	1.901	1.902
.15	2.165	-14.041	-2.813	0.921	1.788	1.964	1.998	2.004	2.005
.16	2.396	-14.495	-3.207	0.837	1.843	2.061	2.105	2.114	2.113
.17	2.644	-14.968	-3.626	0.739	1.895	2.162	2.220	2.231	2.234
.18	2.909	-15.460	-4.072	0.624	1.945	2.268	2.342	2.358	2.362
.19	3.192	-15.974	-4.545	0.490	1.991	2.379	2.473	2.494	2.499
.20	3.497	-16.509	-5.048	0.337	2.032	2.495	2.612	2.640	2.647
.21	3.824	-17.067	-5.583	0.161	2.067	2.615	2.761	2.798	2.807
.22	4.174	-17.650	-6.153	-0.038	2.096	2.739	2.919	2.967	2.979
.23	4.552	-18.257	-6.759	-0.263	2.117	2.808	3.088	3.149	3.165
.24	4.957	-18.891	-7.404	-0.516	2.128	3.001	3.267	3.345	3.367
.25	5.394	-19.553	-8.091	-0.801	2.128	3.127	3.458	3.556	3.584
.26	5.864	-20.244	-8.826	-1.119	2.115	3.276	3.691	3.783	3.820
.27	6.372	-20.965	-9.602	-1.474	2.087	3.448	3.877	4.027	4.073
.28	6.919	-21.718	-10.434	-1.869	2.042	3.561	4.105	4.291	4.352
.29	7.510	-22.505	-11.320	-2.308	1.978	3.706	4.348	4.575	4.652
.30	8.148	-23.327	-12.265	-2.795	1.891	3.850	4.604	4.880	4.978
.31	8.838	-24.186	-13.274	-3.335	1.778	3.994	4.876	5.210	5.332
.32	9.585	-25.083	-14.351	-3.932	1.637	4.154	5.162	5.564	5.716
.33	10.395	-26.020	-15.500	-4.592	1.463	4.270	5.464	5.946	6.134
.34	11.272	-26.999	-16.728	-5.319	1.251	4.400	5.782	6.357	6.589
.35	12.223	-28.022	-18.040	-6.122	0.997	4.521	6.116	6.809	7.084
.36	13.257	-29.091	-19.442	-7.007	0.696	4.631	6.465	7.276	7.622
.37	14.379	-30.207	-20.941	-7.981	0.342	4.726	6.831	7.789	8.206
.38	15.600	-31.373	-22.545	-9.052	-0.073	4.803	7.212	8.339	8.848
.39	16.929	-32.591	-24.261	-10.231	-0.555	4.858	7.609	8.931	9.544
.40	18.377	-33.862	-26.097	-11.527	-1.113	4.887	8.020	9.567	10.303
.41	19.956	-35.188	-28.063	-12.951	-1.757	4.882	8.444	10.249	11.131
.42	21.678	-36.571	-30.168	-14.515	-2.496	4.859	8.881	10.981	12.033
.43	23.560	-38.013	-32.424	-16.233	-3.342	4.751	9.327	11.766	13.017
.44	25.617	-39.515	-34.842	-18.119	-4.308	4.608	9.780	12.606	14.091
.45	27.867	-41.079	-37.433	-20.190	-5.409	4.402	10.238	13.504	15.262
.46	30.332	-42.706	-40.212	-22.463	-6.661	4.121	10.697	14.465	16.540
.47	33.033	-44.396	-43.155	-24.957	-8.081	3.754	11.151	15.489	17.934
.48	35.997	-46.150	-46.390	-27.694	-9.690	3.286	11.595	16.582	19.456
.49	39.252	-47.968	-49.822	-30.608	-11.510	2.701	12.022	17.744	21.114
.50	42.829	-49.849	-53.506	-33.993	-13.567	1.982	12.424	18.979	22.923

TABLE

Z	J 11, 1	J 11, 2	J 11, 3	J 11, 4	J 11, 5	J 11, 6	J 11, 7	J 11, 8	J 11, 9
.01	46.765	-51.792	-57.461	-37.610	-15.887	1.107	12.791	20.289	24.897
.02	51.098	-53.793	-61.709	-41.578	-18.403	0.653	13.111	21.674	27.049
.03	55.874	-55.850	-66.270	-45.933	-21.449	-1.208	13.370	23.157	29.395
.04	61.142	-57.957	-71.171	-50.712	-24.764	-2.705	13.552	24.617	31.951
.05	66.960	-60.109	-76.436	-55.907	-28.492	-4.474	13.696	26.202	34.726
.06	73.389	-62.296	-82.092	-61.713	-32.681	-6.555	13.801	27.983	37.769
.07	80.500	-64.508	-88.170	-68.032	-37.386	-8.993	13.879	29.943	41.071
.08	88.374	-66.732	-94.701	-74.968	-42.668	-11.838	13.938	31.967	44.662
.09	97.069	-68.973	-101.719	-82.582	-48.594	-15.150	13.983	34.148	48.567
.10	106.777	-71.146	-109.259	-90.942	-55.241	-18.994	14.016	36.574	52.811
.11	117.520	-73.291	-117.359	-100.121	-62.694	-23.446	14.039	39.250	57.417
.12	129.437	-75.456	-126.090	-110.202	-71.047	-28.392	14.052	42.198	62.415
.13	142.732	-77.306	-135.403	-121.272	-80.408	-34.528	14.056	45.455	67.831
.14	157.507	-79.098	-145.434	-133.430	-90.865	-41.366	14.051	49.069	73.695
.15	173.866	-80.680	-156.198	-146.784	-102.640	-49.229	14.037	53.094	80.036
.16	192.315	-81.991	-167.745	-161.453	-115.793	-58.262	14.014	57.475	86.883
.17	212.788	-82.959	-180.125	-177.596	-130.310	-68.625	13.981	62.266	94.296
.18	235.650	-83.499	-193.390	-195.296	-147.005	-80.502	13.939	67.529	102.215
.19	261.199	-83.206	-207.562	-215.711	-165.459	-94.102	13.888	73.241	110.755
.20	289.772	-82.870	-222.784	-236.070	-186.112	-109.660	13.829	79.481	119.911
.21	321.751	-81.443	-239.021	-259.533	-209.224	-127.446	13.764	86.350	129.705
.22	357.507	-79.002	-256.354	-285.304	-233.086	-147.763	13.693	93.866	140.151
.23	397.710	-75.537	-274.832	-313.610	-264.021	-170.956	13.617	102.150	151.269
.24	442.731	-70.642	-294.505	-344.636	-296.392	-197.418	13.537	111.269	163.031
.25	493.258	-64.115	-315.400	-378.828	-332.403	-227.592	13.453	121.274	175.452
.26	550.900	-55.648	-337.583	-416.300	-373.105	-261.982	13.366	132.219	188.496
.27	615.759	-44.880	-361.030	-457.351	-418.404	-301.159	13.276	144.170	202.118
.28	688.454	-31.413	-385.822	-502.065	-469.061	-345.769	13.181	157.181	216.249
.29	769.088	-14.745	-411.896	-552.078	-535.703	-396.544	13.082	171.290	230.940
.30	856.857	5.680	-439.247	-606.377	-619.031	-454.314	12.979	186.568	246.208
.31	959.075	30.511	-467.825	-665.900	-698.822	-520.020	12.873	203.050	262.052
.32	1074.211	60.303	-497.549	-731.122	-788.946	-594.223	12.764	220.806	278.511
.33	1204.037	96.236	-528.299	-802.554	-877.369	-679.628	12.652	240.007	295.619
.34	1349.448	139.618	-559.905	-880.743	-969.166	-776.095	12.537	260.808	303.228
.35	15115.508	190.922	-592.143	-966.275	-1066.334	-883.665	12.420	283.261	311.519
.36	1701.984	251.801	-624.718	-1059.775	-1169.801	-1010.076	12.301	307.529	320.561
.37	1912.411	323.820	-657.251	-1161.909	-1287.453	-1141.295	12.180	333.840	330.380
.38	2150.059	408.783	-689.263	-1273.379	-1431.098	-1311.942	12.057	362.363	338.280
.39	2418.534	508.772	-720.156	-1394.626	-1622.582	-1463.325	11.932	393.147	348.212
.40	2721.910	626.185	-749.192	-1527.325	-1813.909	-1699.474	11.806	426.356	353.341
.41	3094.846	763.785	-775.460	-1671.381	-2027.306	-1933.179	11.679	462.054	319.100
.42	3525.557	924.254	-797.857	-1827.927	-2265.238	-2198.009	11.552	500.305	296.932
.43	3891.002	1112.748	-815.040	-1997.813	-2530.428	-2498.111	11.425	541.166	262.584
.44	4386.400	1331.973	-825.393	-2181.869	-2825.881	-2857.981	11.298	584.666	214.334
.45	4947.909	1587.261	-830.076	-2381.040	-3154.014	-3222.731	11.171	630.863	148.617
.46	5582.642	1884.158	-817.470	-2596.075	-3521.178	-3658.210	11.044	680.739	61.589
.47	6300.880	2229.633	-794.111	-2827.902	-3928.086	-4150.902	10.917	734.278	-51.357
.48	7113.727	2629.183	-753.620	-3076.957	-4381.854	-4708.119	10.790	791.476	-193.622
.49	8033.694	3092.975	-692.111	-3344.182	-4888.520	-5338.075	10.663	852.396	-377.640

FITTING A GROWTH CURVE

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TABLE



Z	J 11, 10	J 11, 11
.01	1.041	1.041
.02	1.085	1.085
.03	1.132	1.132
.04	1.181	1.181
.05	1.234	1.234
.06	1.290	1.290
.07	1.350	1.350
.08	1.414	1.414
.09	1.482	1.482
.10	1.555	1.555
.11	1.633	1.633
.12	1.717	1.717
.13	1.806	1.806
.14	1.902	1.902
.15	2.005	2.005
.16	2.115	2.115
.17	2.234	2.234
.18	2.362	2.362
.19	2.500	2.500
.20	2.649	2.649
.21	2.809	2.810
.22	2.982	2.983
.23	3.170	3.171
.24	3.373	3.374
.25	3.593	3.595
.26	3.831	3.835
.27	4.090	4.095
.28	4.372	4.378
.29	4.678	4.687
.30	5.012	5.023
.31	5.376	5.391
.32	5.773	5.793
.33	6.206	6.233
.34	6.680	6.715
.35	7.199	7.244
.36	7.767	7.825
.37	8.389	8.465
.38	9.072	9.188
.39	9.821	9.944
.40	10.645	10.800
.41	11.550	11.746
.42	12.546	12.791
.43	13.643	13.949
.44	14.851	15.232
.45	16.183	16.655
.46	17.652	18.236
.47	19.273	19.992
.48	21.064	21.947
.49	23.042	24.123
.50	25.229	26.549

TABLE

Z	J 11, 10	J 11, 11
.51	27.647	29.254
.52	30.328	32.275
.53	33.284	35.650
.54	36.564	39.484
.55	40.196	43.647
.56	44.220	48.197
.57	48.681	53.176
.58	53.626	58.619
.59	59.111	64.589
.60	65.194	71.147
.61	71.944	78.351
.62	79.454	86.161
.63	87.746	94.631
.64	96.974	103.724
.65	107.218	113.504
.66	118.592	123.940
.67	131.220	135.090
.68	145.243	146.901
.69	160.815	159.421
.70	178.105	172.812
.71	197.303	187.009
.72	218.618	202.016
.73	242.283	217.818
.74	268.551	234.466
.75	297.704	251.905
.76	330.053	270.188
.77	365.940	289.364
.78	405.740	309.484
.79	449.866	330.598
.80	498.771	352.859
.81	552.051	376.315
.82	610.346	401.015
.83	673.347	427.008
.84	741.796	454.352
.85	815.390	483.098
.86	894.833	513.298
.87	980.860	544.993
.88	1074.211	578.234
.89	1175.648	613.076
.90	1284.948	650.560
.91	1402.974	690.731
.92	1529.500	733.635
.93	1665.594	779.322
.94	1812.267	827.848
.95	1969.664	879.161
.96	2137.840	933.317
.97	2316.881	990.365
.98	2506.888	1050.365
.99	2707.988	1113.385

FITTING A GROWTH CURVE

TABLE

Z	J 12, 1	J 12, 2	J 12, 3	J 12, 4	J 12, 5	J 12, 6	J 12, 7	J 12, 8	J 12, 9
.01	0.103	-10.285	0.815	-1.038	1.041	1.041	1.041	1.041	1.041
.02	0.211	-10.581	0.619	-1.071	1.085	1.085	1.085	1.085	1.085
.03	0.326	-10.888	0.411	-1.099	1.130	1.132	1.132	1.132	1.132
.04	0.448	-11.207	0.191	-1.122	1.178	1.181	1.181	1.181	1.181
.05	0.577	-11.538	-0.042	-1.138	1.228	1.234	1.234	1.234	1.234
.06	0.715	-11.882	-0.288	-1.148	1.279	1.289	1.290	1.290	1.290
.07	0.859	-12.239	-0.550	-1.151	1.331	1.348	1.350	1.350	1.350
.08	1.013	-12.611	-0.827	-1.145	1.385	1.411	1.414	1.414	1.414
.09	1.178	-13.007	-1.122	-1.131	1.440	1.477	1.482	1.482	1.482
.10	1.353	-13.429	-1.434	-1.107	1.495	1.548	1.554	1.555	1.555
.11	1.540	-13.817	-1.765	-1.073	1.551	1.622	1.632	1.633	1.633
.12	1.739	-14.252	-2.116	-1.027	1.606	1.700	1.714	1.716	1.717
.13	1.951	-14.705	-2.489	-0.968	1.691	1.782	1.802	1.805	1.806
.14	2.178	-15.177	-2.889	-0.896	1.714	1.869	1.891	1.891	1.892
.15	2.421	-15.669	-3.307	-0.809	1.766	1.960	1.997	2.003	2.005
.16	2.681	-16.181	-3.744	-0.706	1.815	2.055	2.104	2.113	2.115
.17	2.959	-16.715	-4.229	-0.584	1.860	2.155	2.218	2.231	2.234
.18	3.257	-17.272	-4.755	-0.443	1.902	2.259	2.340	2.358	2.361
.19	3.577	-17.853	-5.323	-0.281	1.938	2.367	2.470	2.494	2.499
.20	3.921	-18.459	-5.945	-0.096	1.968	2.479	2.608	2.640	2.647
.21	4.290	-19.091	-6.624	-0.115	1.990	2.594	2.755	2.796	2.807
.22	4.686	-19.752	-7.362	-0.354	2.003	2.714	2.912	2.965	2.979
.23	5.113	-20.444	-8.160	-0.623	2.006	2.839	3.079	3.146	3.165
.24	5.573	-21.161	-9.029	-0.926	1.996	2.961	3.256	3.342	3.366
.25	6.068	-21.913	-9.918	-1.264	1.973	3.088	3.443	3.551	3.583
.26	6.602	-22.699	-10.849	-1.643	1.932	3.216	3.642	3.777	3.818
.27	7.179	-23.529	-11.841	-2.064	1.873	3.345	3.853	4.029	4.073
.28	7.802	-24.418	-11.962	-2.533	1.793	3.474	4.076	4.281	4.349
.29	8.472	-25.376	-13.008	-3.054	1.687	3.603	4.311	4.562	4.648
.30	9.204	-26.414	-14.092	-3.632	1.554	3.723	4.559	4.864	4.973
.31	9.993	-27.195	-15.251	-4.271	1.388	3.842	4.819	5.189	5.325
.32	10.848	-28.221	-16.488	-4.979	1.180	3.953	5.093	5.539	5.707
.33	11.776	-29.295	-17.812	-5.769	0.943	4.055	5.379	5.914	6.123
.34	12.783	-30.417	-19.227	-6.623	0.654	4.145	5.678	6.317	6.574
.35	13.878	-31.592	-20.741	-7.575	0.312	4.229	5.989	6.749	7.064
.36	15.069	-32.820	-22.361	-8.624	-0.089	4.273	6.312	7.213	7.597
.37	16.362	-34.105	-24.096	-9.781	-0.557	4.308	6.646	7.710	8.177
.38	17.777	-35.448	-25.955	-11.054	-1.109	4.333	6.989	8.242	8.807
.39	19.317	-36.852	-27.946	-12.456	-1.728	4.283	7.341	8.811	9.493
.40	20.998	-38.320	-30.081	-13.998	-2.431	4.214	7.698	9.429	10.239
.41	22.826	-39.854	-32.370	-15.696	-3.280	4.097	8.060	10.069	11.050
.42	24.846	-41.456	-34.827	-17.562	-4.239	3.924	8.422	10.761	11.933
.43	27.046	-43.128	-37.463	-19.615	-5.314	3.683	8.789	11.498	12.886
.44	29.458	-44.873	-40.293	-21.873	-6.550	3.399	9.139	12.289	13.937
.45	32.104	-46.691	-43.333	-24.355	-7.955	2.967	9.467	13.110	15.072
.46	35.009	-48.585	-46.500	-27.085	-9.551	2.451	9.782	13.988	16.295
.47	38.204	-50.556	-50.111	-30.086	-11.360	1.818	10.089	14.914	17.646
.48	41.719	-52.603	-53.386	-33.386	-13.410	1.044	10.317	15.889	19.101
.49	45.593	-54.727	-57.046	-37.014	-15.728	0.107	10.614	16.911	20.681
.50	49.864	-56.927	-62.315	-41.005	-18.348	-1.019	10.646	17.979	22.396

FISH BULLETIN NO. 116

TABLE

Z	J 12, 1	J 12, 2	J 12, 3	J 12, 4	J 12, 5	J 12, 6	J 12, 7	J 12, 8	J 12, 9
.51	54.581	-59.201	-67.017	-45.395	-21.307	-2.301	10.698	19.090	24.254
.52	59.794	-61.545	-72.078	-50.223	-24.645	-3.954	10.640	20.241	26.268
.53	65.662	-63.905	-77.328	-55.235	-28.409	-5.834	10.476	21.424	28.446
.54	71.951	-66.424	-83.398	-61.380	-32.632	-8.045	10.153	22.632	30.802
.55	79.057	-68.943	-89.721	-67.814	-37.430	-10.633	9.649	23.855	33.346
.56	86.904	-71.590	-96.353	-74.895	-42.810	-13.661	8.925	25.079	36.090
.57	95.647	-74.081	-103.874	-82.692	-48.866	-17.186	7.939	26.288	39.044
.58	105.376	-76.967	-111.783	-91.279	-55.681	-21.285	6.640	27.461	42.229
.59	116.214	-79.253	-120.396	-100.786	-63.347	-26.039	4.988	28.570	45.627
.60	128.300	-81.732	-129.490	-111.156	-71.969	-31.546	2.855	29.584	49.274
.61	141.795	-84.188	-139.384	-122.637	-81.665	-37.912	0.221	30.463	53.166
.62	156.878	-86.496	-150.043	-135.290	-92.568	-45.265	-3.030	31.157	57.314
.63	173.755	-88.623	-161.523	-149.239	-104.827	-53.744	-7.096	31.699	61.713
.64	192.661	-90.505	-173.881	-164.617	-118.609	-63.513	-11.835	31.745	66.361
.65	213.864	-92.065	-187.180	-181.276	-134.104	-74.708	-17.065	31.381	71.251
.66	237.667	-93.299	-201.455	-200.279	-151.524	-87.691	-24.670	30.713	76.369
.67	264.420	-93.824	-216.829	-223.910	-171.108	-102.534	-35.048	29.515	81.681
.68	294.320	-93.778	-233.371	-243.668	-193.125	-119.625	-48.035	27.140	87.163
.69	328.420	-92.911	-251.088	-268.777	-217.380	-139.220	-64.901	24.008	92.759
.70	366.641	-91.030	-270.075	-296.479	-245.712	-161.701	-85.961	19.709	98.405
.71	409.777	-87.911	-290.397	-327.043	-277.008	-187.483	-85.582	13.989	104.011
.72	458.399	-83.284	-312.115	-369.766	-312.168	-217.009	-105.187	6.348	109.463
.73	513.617	-76.829	-335.280	-407.570	-351.759	-250.908	-128.372	-2.971	114.615
.74	574.995	-68.168	-359.937	-439.011	-396.297	-289.709	-153.407	-14.901	119.281
.75	646.008	-56.855	-386.116	-464.279	-446.314	-334.149	-187.258	-30.013	123.228
.76	729.812	-42.256	-413.830	-534.199	-502.596	-383.034	-224.595	-48.630	126.166
.77	817.776	-24.052	-443.060	-589.284	-568.803	-443.287	-268.313	-71.545	127.735
.78	921.111	-1.204	-473.790	-649.888	-637.980	-509.961	-319.447	-99.586	127.489
.79	1038.596	27.058	-505.914	-719.710	-717.139	-586.259	-379.201	-132.732	124.884
.80	1172.276	61.757	-539.312	-790.291	-807.172	-673.556	-448.967	-175.138	119.252
.81	1324.500	104.097	-573.794	-871.270	-908.418	-773.423	-530.358	-225.164	109.776
.82	1497.970	153.404	-609.662	-963.334	-1022.262	-887.650	-625.245	-285.414	95.468
.83	1695.752	217.615	-644.847	-1058.216	-1150.260	-1013.283	-735.791	-357.774	75.125
.84	1921.539	292.414	-689.579	-1165.697	-1294.151	-1167.655	-864.503	-444.465	47.293
.85	2179.319	382.187	-745.072	-1283.692	-1455.882	-1358.628	-1014.283	-548.098	10.222
.86	2473.862	489.626	-749.331	-1412.798	-1637.629	-1533.636	-1188.485	-671.738	-38.206
.87	2810.006	617.860	-780.557	-1554.187	-1841.820	-1746.740	-1390.901	-818.896	-109.532
.88	3193.813	770.676	-808.091	-1708.696	-2071.164	-2011.678	-1626.288	-994.008	-179.896
.89	3636.690	952.318	-830.372	-1877.270	-2328.680	-2302.940	-1899.361	-1291.940	-279.686
.90	4141.529	1167.585	-845.468	-2060.850	-2617.723	-2635.634	-2216.807	-1448.410	-404.447
.91	4719.879	1423.307	-851.003	-2260.356	-2942.022	-3015.570	-2584.938	-1740.284	-559.630
.92	5388.730	1723.319	-844.072	-2476.638	-3305.714	-3449.356	-3011.844	-2085.528	-731.148
.93	6142.735	2082.625	-821.137	-2710.444	-3719.379	-3944.902	-3507.041	-2469.664	-986.571
.94	7014.458	2504.086	-777.899	-2962.669	-4170.075	-4509.283	-4080.855	-2974.961	-1274.748
.95	8014.658	3000.690	-709.161	-3233.699	-4681.386	-5154.131	-4742.038	-3542.850	-1626.216
.96	9162.644	3586.105	-608.665	-3532.285	-5253.457	-5889.272	-5515.510	-4211.921	-2033.489
.97	10480.018	4274.279	-468.863	-3851.880	-5935.027	-6727.500	-6406.722	-4956.572	-2571.419
.98	11994.147	5083.889	-289.718	-4158.735	-6607.481	-7682.576	-7437.985	-5926.067	-3197.611
.99	13732.648	6034.439	-83.405	-4502.723	-7404.878	-8779.766	-8630.823	-7015.028	-3932.913

FITTING A GROWTH CURVE

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TABLE

Z	J 12, 10	J 12, 11	J 12, 12
.01	1.041	1.041	1.041
.02	1.085	1.085	1.085
.03	1.132	1.132	1.132
.04	1.181	1.181	1.181
.05	1.234	1.234	1.234
.06	1.290	1.290	1.290
.07	1.350	1.350	1.350
.08	1.414	1.414	1.414
.09	1.482	1.482	1.482
.10	1.555	1.555	1.555
.11	1.633	1.633	1.633
.12	1.717	1.717	1.717
.13	1.806	1.806	1.806
.14	1.902	1.902	1.902
.15	2.005	2.005	2.005
.16	2.115	2.115	2.115
.17	2.234	2.234	2.234
.18	2.362	2.362	2.362
.19	2.500	2.500	2.500
.20	2.649	2.649	2.649
.21	2.809	2.810	2.810
.22	2.982	2.983	2.983
.23	3.170	3.171	3.171
.24	3.373	3.374	3.375
.25	3.592	3.595	3.596
.26	3.831	3.834	3.835
.27	4.090	4.095	4.096
.28	4.371	4.378	4.380
.29	4.677	4.685	4.690
.30	5.010	5.023	5.027
.31	5.373	5.391	5.396
.32	5.770	5.792	5.800
.33	6.202	6.232	6.243
.34	6.675	6.714	6.729
.35	7.182	7.245	7.262
.36	7.727	7.823	7.849
.37	8.317	8.461	8.496
.38	8.956	9.164	9.209
.39	9.641	9.938	9.998
.40	10.379	10.792	10.870
.41	11.171	11.735	11.835
.42	12.005	12.778	12.907
.43	12.890	13.925	14.077
.44	13.825	15.210	15.420
.45	14.810	16.627	16.864
.46	15.848	18.200	18.538
.47	16.943	19.947	20.572
.48	18.092	21.890	22.423
.49	19.301	24.031	24.719
.50	20.579	26.458	27.292

TABLE

Z	J 18, 10	J 18, 11	J 18, 12
.51	27.338	29.141	30.178
.52	29.942	31.134	33.419
.53	32.815	33.474	37.064
.54	35.987	36.205	41.108
.55	39.489	43.375	45.792
.56	43.355	48.040	51.008
.57	47.624	53.260	56.898
.58	52.295	59.198	63.556
.59	57.338	65.656	71.088
.60	63.280	72.999	79.619
.61	69.617	81.235	89.288
.62	76.608	90.477	100.238
.63	84.318	100.862	112.714
.64	92.819	112.508	126.869
.65	102.186	125.600	142.967
.66	112.503	140.317	161.291
.67	123.857	156.898	182.154
.68	136.345	175.478	205.938
.69	150.067	196.419	233.101
.70	165.131	219.980	264.088
.71	181.649	246.514	299.486
.72	199.737	276.381	339.950
.73	219.517	310.013	386.232
.74	241.111	347.892	439.214
.75	264.639	390.557	499.891
.76	290.219	438.618	569.425
.77	317.962	492.759	649.160
.78	347.963	553.750	740.641
.79	380.301	622.437	845.638
.80	415.024	699.850	966.275
.81	452.141	787.019	1104.804
.82	491.612	885.182	1264.271
.83	533.323	995.706	1447.609
.84	577.074	1120.116	1658.614
.85	622.548	1260.115	1901.374
.86	669.282	1417.601	2181.435
.87	716.627	1594.687	2504.002
.88	765.703	1793.716	2874.884
.89	809.340	2017.287	3304.817
.90	852.007	2268.273	3799.745
.91	889.731	2549.841	4371.635
.92	919.694	2865.474	5030.704
.93	939.698	3218.967	5792.682
.94	944.567	3614.546	6672.118
.95	929.872	4056.677	7690.737
.96	889.313	4550.282	8867.236
.97	815.210	5100.823	10227.843
.98	698.114	5713.329	11801.693
.99	526.434	6394.363	13622.653

FITTING A GROWTH CURVE

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TABLE

Z	J 13, 1	J 13, 2	J 13, 3	J 13, 4	J 13, 5	J 13, 6	J 13, 7	J 13, 8	J 13, 9
.01	0.113	-11.316	0.794	1.038	1.041	1.041	1.041	1.041	1.041
.02	0.233	-11.644	0.576	1.070	1.085	1.085	1.085	1.085	1.085
.03	0.359	-11.984	0.345	1.096	1.130	1.132	1.132	1.132	1.132
.04	0.493	-12.337	0.101	1.116	1.178	1.181	1.181	1.181	1.181
.05	0.635	-12.704	-0.158	1.132	1.277	1.253	1.254	1.254	1.254
.06	0.789	-13.086	-0.433	1.135	1.278	1.289	1.290	1.290	1.290
.07	0.947	-13.482	-0.725	1.132	1.330	1.348	1.350	1.350	1.350
.08	1.118	-13.895	-1.034	1.120	1.383	1.411	1.414	1.414	1.414
.09	1.299	-14.224	-1.361	1.098	1.436	1.477	1.482	1.482	1.482
.10	1.495	-14.770	-1.709	1.065	1.490	1.547	1.554	1.555	1.555
.11	1.699	-15.235	-2.079	1.021	1.543	1.621	1.631	1.633	1.633
.12	1.920	-15.719	-2.471	0.963	1.596	1.698	1.714	1.716	1.717
.13	2.155	-16.222	-2.887	0.890	1.647	1.790	1.802	1.805	1.806
.14	2.407	-16.749	-3.330	0.803	1.697	1.896	1.896	1.901	1.902
.15	2.677	-17.296	-3.801	0.698	1.743	1.996	1.996	2.003	2.003
.16	2.965	-17.867	-4.301	0.574	1.785	2.099	2.103	2.113	2.115
.17	3.274	-18.462	-4.833	0.430	1.825	2.147	2.147	2.211	2.214
.18	3.606	-19.084	-5.398	0.263	1.858	2.219	2.338	2.337	2.361
.19	3.962	-19.732	-6.001	0.073	1.885	2.354	2.467	2.493	2.496
.20	4.345	-20.409	-6.642	-0.145	1.903	2.462	2.604	2.639	2.647
.21	4.756	-21.115	-7.325	-0.392	1.912	2.574	2.750	2.795	2.806
.22	5.198	-21.853	-8.052	-0.670	1.910	2.688	2.905	2.963	2.978
.23	5.672	-22.624	-8.827	-0.983	1.895	2.804	3.070	3.144	3.164
.24	6.188	-23.430	-9.654	-1.335	1.865	2.921	3.244	3.338	3.365
.25	6.742	-24.273	-10.535	-1.728	1.817	3.039	3.429	3.547	3.582
.26	7.340	-25.153	-11.475	-2.166	1.750	3.157	3.624	3.772	3.817
.27	7.986	-26.074	-12.479	-2.655	1.659	3.273	3.830	4.013	4.071
.28	8.685	-27.038	-13.551	-3.198	1.543	3.385	4.046	4.272	4.340
.29	9.441	-28.046	-14.696	-3.800	1.397	3.494	4.274	4.550	4.644
.30	10.260	-29.101	-15.919	-4.468	1.216	3.596	4.513	4.848	4.967
.31	11.148	-30.205	-17.227	-5.208	0.998	3.690	4.762	5.169	5.318
.32	12.111	-31.360	-18.627	-6.026	0.735	3.772	5.023	5.513	5.696
.33	13.158	-32.570	-20.124	-6.929	0.423	3.839	5.293	5.881	6.110
.34	14.295	-33.836	-21.726	-7.927	0.056	3.889	5.573	6.275	6.558
.35	15.533	-35.162	-23.442	-9.039	-0.375	3.917	5.862	6.697	7.044
.36	16.881	-36.550	-25.281	-10.243	-0.876	3.919	6.158	7.148	7.571
.37	18.350	-38.003	-27.252	-11.542	-1.458	3.889	6.459	7.629	8.145
.38	19.954	-39.523	-29.366	-13.028	-2.130	3.820	6.764	8.142	8.765
.39	21.706	-41.115	-31.634	-14.683	-2.904	3.706	7.070	8.688	9.439
.40	23.622	-42.780	-34.068	-16.473	-3.792	3.538	7.373	9.269	10.171
.41	25.718	-44.522	-36.682	-18.445	-4.800	3.307	7.670	9.884	10.965
.42	28.016	-46.344	-39.490	-20.615	-5.970	3.003	7.956	10.535	11.826
.43	30.557	-48.247	-42.508	-23.003	-7.294	2.611	8.225	11.221	12.760
.44	33.305	-50.234	-45.753	-25.637	-8.802	2.119	8.469	11.944	13.772
.45	36.348	-52.309	-49.245	-28.534	-10.514	1.599	8.681	12.701	14.867
.46	39.698	-54.471	-53.002	-31.724	-12.459	0.763	8.850	13.492	16.032
.47	43.359	-56.724	-57.017	-35.266	-14.663	-0.142	8.964	14.315	17.353
.48	47.462	-59.066	-61.405	-39.105	-17.159	-1.229	9.008	15.165	18.717
.49	51.960	-61.499	-65.100	-43.307	-19.984	-2.227	8.996	16.039	20.130
.50	56.955	-64.020	-71.161	-48.092	-25.179	-4.070	8.818	16.929	21.818

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FISH BULLETIN NO. 116

TABLE

Z	J 13, 1	J 13, 2	J 13, 3	J 13, 4	J 13, 5	J 13, 6	J 13, 7	J 13, 8	J 13, 9
.51	62.443	-66.628	-76.618	-53.237	-26.780	-5.894	8.540	17.828	23.547
.52	68.550	-69.318	-82.565	-58.040	-30.867	-8.642	8.104	18.725	25.404
.53	75.329	-72.085	-88.858	-65.229	-35.470	-10.564	7.478	19.606	27.394
.54	82.864	-74.918	-95.714	-72.164	-40.656	-13.315	6.622	20.554	29.520
.55	91.249	-77.808	-103.116	-79.815	-46.528	-16.961	5.493	21.249	31.788
.56	100.594	-80.738	-111.109	-88.258	-53.141	-20.975	4.037	21.964	34.198
.57	111.021	-83.690	-119.741	-97.578	-60.598	-25.643	2.192	22.566	36.750
.58	122.671	-86.658	-129.065	-107.869	-69.009	-31.061	-0.115	23.017	39.440
.59	135.706	-89.650	-139.136	-119.253	-78.462	-37.242	-2.968	23.269	42.263
.60	150.308	-92.389	-150.015	-131.795	-89.186	-44.614	-6.467	23.264	45.207
.61	166.691	-95.104	-161.764	-145.676	-101.244	-53.024	-10.728	22.930	48.255
.62	184.994	-97.696	-174.452	-161.023	-114.842	-62.741	-15.887	22.183	51.383
.63	205.795	-99.912	-188.150	-177.995	-130.178	-73.559	-22.102	20.925	54.556
.64	229.114	-101.841	-202.953	-196.770	-147.476	-86.903	-29.560	19.027	57.712
.65	255.417	-103.514	-218.877	-217.545	-166.988	-101.827	-38.478	16.546	60.851
.66	283.125	-104.190	-236.965	-240.529	-189.033	-119.027	-49.108	12.703	63.838
.67	312.726	-104.334	-254.078	-265.993	-213.845	-138.843	-61.748	7.589	66.596
.68	343.781	-103.524	-274.407	-294.177	-241.882	-161.662	-76.744	1.632	69.063
.69	396.637	-101.535	-295.406	-325.267	-273.331	-187.934	-94.459	-6.211	70.904
.70	448.944	-98.983	-318.881	-359.933	-309.265	-218.175	-115.487	-16.307	72.107
.71	504.667	-92.829	-343.494	-398.239	-349.617	-252.977	-140.250	-28.915	72.372
.72	568.110	-85.364	-369.867	-440.644	-395.194	-293.624	-169.461	-44.595	71.403
.73	640.433	-75.198	-397.870	-487.611	-446.682	-339.102	-203.846	-63.702	68.830
.74	722.985	-61.741	-427.700	-539.625	-504.856	-392.114	-244.295	-87.260	64.296
.75	817.327	-44.291	-459.326	-597.217	-570.397	-453.103	-291.839	-116.026	56.977
.76	925.276	-22.005	-492.985	-669.970	-644.897	-523.287	-347.671	-151.030	46.467
.77	1048.940	6.126	-527.704	-731.518	-728.883	-603.985	-413.204	-193.453	31.849
.78	1191.771	41.305	-564.238	-809.351	-823.827	-696.848	-499.076	-244.766	12.117
.79	1353.622	84.971	-602.064	-895.815	-931.163	-803.683	-590.203	-306.666	-13.601
.80	1540.814	138.840	-640.859	-991.115	-1022.516	-926.595	-685.824	-381.180	-47.843
.81	1756.215	204.960	-680.173	-1096.310	-1189.715	-1068.006	-809.532	-470.711	-91.390
.82	2004.333	285.772	-719.397	-1212.315	-1344.824	-1220.702	-954.441	-578.109	-146.685
.83	2290.422	384.187	-757.726	-1340.096	-1520.167	-1417.889	-1124.038	-706.757	-216.458
.84	2620.611	503.670	-794.107	-1489.659	-1718.555	-1633.254	-1329.565	-860.655	-303.868
.85	3002.052	648.349	-827.184	-1653.042	-1942.326	-1881.033	-1554.821	-1044.546	-412.765
.86	3443.091	823.196	-855.228	-1834.295	-2195.773	-2166.096	-1826.499	-1264.045	-547.791
.87	3953.477	1033.874	-876.047	-1989.461	-2481.183	-2494.036	-2144.210	-1525.901	-714.537
.88	4548.595	1287.313	-889.884	-2191.359	-2803.880	-2871.273	-2513.093	-1857.678	-919.424
.89	5229.741	1592.313	-884.294	-2411.449	-3168.064	-3305.180	-2949.351	-2298.678	-1171.475
.90	6024.461	1958.090	-863.989	-2649.971	-3578.855	-3804.200	-3437.425	-2650.701	-1479.486
.91	6946.924	2396.503	-820.656	-2907.680	-4041.936	-4378.016	-4020.406	-3175.846	-1855.442
.92	8018.368	2921.295	-747.736	-3184.854	-4565.001	-5037.717	-4743.121	-3799.771	-2313.334
.93	9263.632	3549.190	-637.165	-3481.963	-5190.795	-5795.990	-5552.161	-4540.611	-2870.015
.94	10711.753	4299.381	-476.047	-3796.519	-5811.148	-6667.333	-6496.833	-5419.770	-3545.543
.95	12396.702	5185.080	-281.280	-4128.903	-6533.019	-7668.311	-7599.602	-6462.502	-4364.023
.96	14338.217	6253.688	30.809	-4476.140	-7385.515	-8817.829	-8886.391	-7698.094	-5314.268
.97	16642.761	7537.663	415.466	-4834.613	-8318.491	-10137.415	-10388.146	-9163.139	-6550.713
.98	19504.704	9055.463	814.259	-5199.132	-9382.564	-11651.592	-12139.325	-10887.492	-7994.487
.99	22407.636	10862.608	1533.733	-5562.497	-10329.064	-13388.229	-14181.644	-12950.338	-9734.726

FITTING A GROWTH CURVE

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TABLE



Z	J 18, 10	J 18, 11	J 18, 12	J 18, 13
.01	1.041	1.041	1.041	1.041
.02	1.085	1.085	1.085	1.085
.03	1.132	1.132	1.132	1.132
.04	1.181	1.181	1.181	1.181
.05	1.234	1.234	1.234	1.234
.06	1.290	1.290	1.290	1.290
.07	1.350	1.350	1.350	1.350
.08	1.414	1.414	1.414	1.414
.09	1.482	1.482	1.482	1.482
.10	1.555	1.555	1.555	1.555
.11	1.633	1.633	1.633	1.633
.12	1.717	1.717	1.717	1.717
.13	1.806	1.806	1.806	1.806
.14	1.902	1.902	1.902	1.902
.15	2.005	2.005	2.005	2.005
.16	2.115	2.115	2.115	2.115
.17	2.234	2.234	2.234	2.234
.18	2.362	2.362	2.362	2.362
.19	2.500	2.500	2.500	2.500
.20	2.649	2.649	2.649	2.649
.21	2.809	2.810	2.810	2.810
.22	2.982	2.983	2.983	2.983
.23	3.170	3.171	3.171	3.171
.24	3.372	3.374	3.375	3.375
.25	3.592	3.595	3.596	3.596
.26	3.830	3.834	3.835	3.836
.27	4.089	4.095	4.096	4.097
.28	4.370	4.378	4.380	4.381
.29	4.676	4.686	4.689	4.691
.30	5.008	5.022	5.027	5.029
.31	5.371	5.390	5.396	5.398
.32	5.766	5.791	5.800	5.803
.33	6.198	6.230	6.243	6.247
.34	6.669	6.712	6.728	6.734
.35	7.184	7.240	7.261	7.270
.36	7.747	7.819	7.848	7.860
.37	8.364	8.456	8.494	8.510
.38	9.039	9.157	9.207	9.226
.39	9.779	9.929	9.995	10.023
.40	10.590	10.781	10.866	10.964
.41	11.480	11.720	11.831	11.881
.42	12.457	12.758	12.901	12.967
.43	13.529	13.907	14.089	14.176
.44	14.708	15.177	15.410	15.523
.45	16.002	16.585	16.850	17.027
.46	17.425	18.149	18.519	18.710
.47	18.989	19.878	20.349	20.594
.48	20.706	21.802	22.353	22.708
.49	22.600	23.940	24.680	25.083
.50	24.679	26.318	27.241	27.755

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911 '0X NLEHTLIG HSEH

TABLE

Z	J 15, 10	J 15, 11	J 15, 12	J 15, 13
.51	26.965	28.064	30.113	30.766
.52	29.479	31.910	33.337	34.164
.53	32.342	35.193	36.960	38.004
.54	35.278	38.853	41.035	42.349
.55	38.815	43.036	45.624	47.274
.56	42.278	47.491	50.796	52.863
.57	46.299	52.377	56.532	59.214
.58	50.709	58.257	63.221	66.440
.59	55.543	64.602	70.668	74.673
.60	60.837	71.652	78.992	84.054
.61	66.627	79.617	88.629	94.790
.62	72.933	88.477	99.435	107.055
.63	79.855	98.393	111.687	121.096
.64	87.373	109.459	125.589	137.189
.65	95.545	121.844	141.375	155.658
.66	104.411	135.693	159.311	176.961
.67	114.003	151.175	179.704	201.246
.68	124.351	168.481	202.904	229.315
.69	135.474	187.819	229.314	261.654
.70	147.383	209.423	259.393	298.951
.71	160.071	233.545	293.669	342.007
.72	173.510	260.465	332.747	391.757
.73	187.644	290.487	377.321	449.294
.74	202.383	323.943	428.185	515.898
.75	217.688	361.190	486.250	593.063
.76	233.600	402.613	552.538	682.540
.77	248.624	448.622	628.308	796.382
.78	263.610	499.649	714.963	936.991
.79	277.824	556.146	813.797	1047.186
.80	290.524	618.375	926.993	1210.274
.81	300.875	687.404	1056.234	1400.139
.82	307.807	763.085	1204.139	1621.339
.83	309.960	846.047	1373.301	1879.234
.84	305.609	936.663	1566.787	2180.122
.85	292.947	1035.225	1788.095	2531.412
.86	268.176	1141.807	2041.208	2941.820
.87	228.983	1256.663	2330.676	3421.607
.88	179.792	1379.263	2661.666	3982.858
.89	88.271	1509.092	3040.051	4639.804
.90	-24.744	1645.106	3472.495	5409.218
.91	-176.830	1785.665	3966.851	6310.870
.92	-376.797	1928.363	4530.756	7368.072
.93	-637.596	2089.804	5174.750	8608.319
.94	-973.691	2205.324	5909.385	10064.040
.95	-1403.146	2288.944	6746.852	11773.509
.96	-1948.622	2431.442	7700.815	13781.807
.97	-2636.314	2602.309	8786.815	16142.505
.98	-3497.475	2828.653	10020.922	18918.770
.99	-4574.618	3100.775	11422.832	22183.512

FITTING A GROWTH CURVE

TABLE

Z	J 14, 1	J 14, 2	J 14, 3	J 14, 4	J 14, 5	J 14, 6	J 14, 7	J 14, 8	J 14, 9
.01	0.123	-12.346	0.274	1.037	1.041	1.041	1.041	1.041	1.041
.02	0.254	-12.700	0.534	1.068	1.085	1.085	1.085	1.085	1.085
.03	0.392	-13.079	0.780	1.093	1.130	1.132	1.132	1.132	1.132
.04	0.539	-13.487	0.010	1.111	1.177	1.181	1.181	1.181	1.181
.05	0.694	-13.871	-0.275	1.121	1.226	1.233	1.234	1.234	1.234
.06	0.859	-14.230	-0.578	1.122	1.322	1.329	1.330	1.330	1.330
.07	1.035	-14.726	-0.899	1.114	1.328	1.348	1.350	1.350	1.350
.08	1.222	-15.179	-1.240	1.096	1.380	1.411	1.414	1.414	1.414
.09	1.421	-15.651	-1.601	1.066	1.432	1.477	1.482	1.482	1.482
.10	1.633	-16.142	-1.985	1.024	1.484	1.546	1.554	1.555	1.555
.11	1.859	-16.653	-2.393	0.969	1.536	1.620	1.631	1.633	1.633
.12	2.101	-17.186	-2.826	0.899	1.586	1.697	1.714	1.716	1.717
.13	2.360	-17.741	-3.286	0.813	1.634	1.778	1.802	1.805	1.806
.14	2.636	-18.320	-3.775	0.709	1.679	1.863	1.893	1.901	1.902
.15	2.932	-18.924	-4.295	0.586	1.721	1.952	1.995	2.003	2.005
.16	3.249	-19.553	-4.847	0.442	1.758	2.044	2.102	2.113	2.115
.17	3.590	-20.210	-5.436	0.275	1.790	2.140	2.215	2.231	2.234
.18	3.955	-20.895	-6.062	0.083	1.815	2.239	2.336	2.357	2.361
.19	4.347	-21.611	-6.729	-0.136	1.832	2.341	2.464	2.492	2.499
.20	4.768	-22.358	-7.439	-0.386	1.839	2.446	2.600	2.638	2.646
.21	5.222	-23.139	-8.185	-0.668	1.834	2.553	2.745	2.794	2.806
.22	5.710	-23.955	-9.002	-0.986	1.817	2.662	2.899	2.962	2.978
.23	6.236	-24.808	-9.891	-1.344	1.784	2.772	3.061	3.142	3.164
.24	6.804	-25.700	-10.778	-1.744	1.733	2.882	3.233	3.335	3.364
.25	7.417	-26.632	-11.737	-2.191	1.662	2.991	3.414	3.543	3.581
.26	8.078	-27.608	-12.802	-2.690	1.567	3.097	3.605	3.766	3.815
.27	8.794	-28.629	-13.918	-3.245	1.445	3.200	3.806	4.005	4.069
.28	9.568	-29.698	-15.110	-3.862	1.293	3.298	4.017	4.262	4.343
.29	10.407	-30.816	-16.384	-4.546	1.106	3.388	4.237	4.537	4.640
.30	11.316	-31.988	-17.747	-5.305	0.879	3.469	4.467	4.832	4.962
.31	12.303	-33.214	-19.204	-6.144	0.607	3.538	4.705	5.148	5.310
.32	13.375	-34.499	-20.765	-7.073	0.284	3.590	4.953	5.486	5.688
.33	14.540	-35.845	-22.436	-8.099	-0.096	3.624	5.208	5.848	6.098
.34	15.807	-37.255	-24.236	-9.232	-0.542	3.634	5.469	6.234	6.542
.35	17.188	-38.732	-26.144	-10.482	-1.061	3.615	5.734	6.643	7.023
.36	18.693	-40.280	-28.202	-11.862	-1.683	3.562	6.003	7.083	7.544
.37	20.337	-41.901	-30.409	-13.384	-2.359	3.469	6.272	7.548	8.109
.38	22.132	-43.600	-32.778	-15.062	-3.100	3.326	6.538	8.042	8.721
.39	24.096	-45.379	-35.322	-16.911	-4.081	3.127	6.798	8.565	9.384
.40	26.245	-47.242	-38.056	-18.950	-5.134	2.861	7.047	9.116	10.102
.41	28.602	-49.192	-40.995	-21.196	-6.359	2.516	7.279	9.696	10.878
.42	31.188	-51.233	-44.155	-25.671	-7.713	2.078	7.488	10.305	11.717
.43	34.030	-53.367	-47.566	-30.369	-9.278	1.533	7.666	10.941	12.623
.44	37.155	-55.609	-51.218	-35.405	-11.059	0.864	7.809	11.602	13.601
.45	40.597	-57.929	-55.161	-40.719	-13.081	0.049	7.889	12.286	14.656
.46	44.393	-60.381	-59.411	-46.371	-15.370	-0.955	7.908	12.988	15.790
.47	48.583	-62.896	-63.963	-52.398	-17.977	-2.113	7.846	13.703	17.009
.48	53.215	-65.555	-68.935	-58.840	-20.924	-3.517	7.683	14.425	18.317
.49	58.342	-68.277	-74.269	-65.739	-24.261	-5.182	7.397	15.145	19.717
.50	64.024	-71.122	-80.026	-73.144	-28.036	-7.149	6.992	15.851	21.212

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TABLE

Z	J 14, 1	J 14, 2	J 14, 3	J 14, 4	J 14, 5	J 14, 6	J 14, 7	J 14, 8	J 14, 9
.01	70.331	-74.066	-86.245	-61.111	-32.306	-9.462	6.346	16.529	22.804
.02	77.341	-77.104	-92.965	-67.669	-42.177	-12.177	5.512	17.161	24.493
.03	85.142	-80.228	-100.228	-74.975	-42.950	-15.354	4.418	17.757	26.279
.04	93.837	-83.489	-108.082	-83.016	-48.756	-19.064	3.013	18.197	28.159
.05	103.442	-86.692	-116.576	-91.993	-55.723	-23.388	1.236	18.541	30.127
.06	114.390	-89.997	-125.766	-101.750	-63.594	-28.419	-0.983	18.716	32.174
.07	126.634	-93.321	-135.710	-112.602	-72.488	-34.265	-2.723	18.673	34.286
.08	140.150	-96.631	-146.472	-124.635	-82.536	-41.049	-4.785	18.357	36.444
.09	155.039	-99.889	-158.122	-137.937	-93.891	-48.914	-7.179	17.691	38.622
.10	172.633	-103.043	-170.731	-152.713	-106.724	-58.024	-10.140	16.589	40.789
.11	192.000	-106.030	-184.378	-169.065	-121.230	-68.569	-12.122	14.948	42.890
.12	213.850	-108.773	-199.146	-187.191	-137.629	-80.707	-13.910	12.640	44.877
.13	238.639	-111.175	-215.122	-207.294	-156.174	-94.870	-15.917	9.513	46.670
.14	266.481	-113.117	-232.399	-229.597	-177.152	-111.170	-18.195	5.387	48.177
.15	298.156	-114.433	-251.071	-254.348	-200.887	-130.003	-20.440	0.042	49.279
.16	334.120	-115.004	-271.237	-281.827	-227.730	-151.756	-22.900	-4.784	49.823
.17	375.021	-114.501	-292.966	-312.343	-268.164	-176.880	-25.280	-15.404	49.632
.18	421.611	-112.827	-316.445	-346.240	-292.609	-205.894	-27.700	-26.195	48.469
.19	474.769	-109.908	-341.679	-383.902	-311.052	-239.398	-29.901	-39.603	46.059
.20	535.516	-104.106	-368.786	-425.752	-325.856	-278.089	-31.663	-56.172	42.025
.21	605.050	-96.412	-397.841	-472.263	-425.991	-322.770	-199.521	-76.541	35.960
.22	684.769	-85.572	-428.903	-525.054	-482.845	-371.374	-259.486	-101.480	27.325
.23	776.308	-70.969	-462.004	-581.402	-547.339	-433.982	-286.631	-131.907	15.466
.24	881.387	-51.744	-497.141	-643.298	-620.521	-502.843	-342.214	-168.023	-0.414
.25	1002.855	-26.837	-534.262	-716.137	-703.584	-582.408	-407.716	-213.841	-21.292
.26	1142.735	4.948	-573.252	-794.919	-797.884	-674.356	-484.881	-268.229	-48.539
.27	1304.595	45.195	-613.609	-882.350	-904.966	-780.636	-575.759	-333.063	-83.069
.28	1491.428	93.794	-655.922	-979.345	-1029.583	-903.504	-682.760	-413.282	-127.196
.29	1708.169	158.764	-698.837	-1086.868	-1184.728	-1043.577	-808.725	-508.862	-182.808
.30	1959.664	237.004	-742.016	-1205.945	-1321.659	-1209.887	-956.994	-623.901	-252.802
.31	2251.624	333.697	-784.589	-1337.664	-1499.639	-1399.950	-1131.500	-762.215	-340.101
.32	2592.006	452.773	-825.391	-1485.160	-1700.464	-1619.838	-1336.872	-928.364	-448.678
.33	2988.256	598.977	-862.884	-1643.600	-1932.511	-1874.269	-1578.556	-1127.796	-583.250
.34	3450.549	773.039	-895.063	-1820.157	-2193.772	-2168.707	-1862.967	-1367.012	-749.538
.35	3990.531	966.877	-919.333	-2013.982	-2490.417	-2509.475	-2197.650	-1653.777	-954.486
.36	4622.944	1283.842	-932.377	-2226.148	-2827.110	-2903.893	-2391.485	-1997.359	-1206.317
.37	5361.440	1589.009	-929.954	-2457.597	-3209.062	-3360.420	-3054.925	-2408.823	-1515.836
.38	6228.109	1984.535	-906.699	-2709.048	-3642.210	-3888.836	-3600.258	-2901.372	-1894.899
.39	7245.037	2465.085	-855.842	-2989.803	-4132.976	-4500.433	-4241.940	-3469.769	-2538.412
.40	8439.482	3048.342	-768.876	-3273.047	-4688.606	-5208.234	-4996.963	-4196.776	-3224.769
.41	9843.793	3752.629	-635.153	-3584.768	-5317.061	-6027.257	-5885.302	-5038.832	-3615.808
.42	11496.367	4612.619	-441.381	-3914.418	-6027.073	-6974.785	-6930.419	-6046.643	-4438.048
.43	13442.798	5650.389	-171.019	-4259.158	-6828.170	-8070.700	-8159.867	-7251.054	-5483.542
.44	15737.231	6965.142	196.472	-4614.559	-7730.632	-9337.822	-9605.977	-8686.996	-6731.010
.45	18444.006	8424.895	686.528	-4974.122	-8745.481	-10802.326	-11306.680	-10408.651	-8247.215
.46	21639.388	10260.784	1330.393	-5328.664	-9884.373	-12494.177	-13396.444	-12469.897	-10088.597
.47	25414.836	12478.986	2167.467	-5665.537	-11159.459	-14447.594	-15657.343	-14910.451	-12323.228
.48	29877.793	15157.958	3244.927	-5967.684	-12583.128	-16701.696	-18420.350	-17853.793	-15033.193
.49	35196.905	18362.008	4621.728	-6212.458	-14167.706	-19260.694	-21666.774	-21321.037	-18517.366

FITTING A GROWTH CURVE

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TABLE

Z	J 14, 10	J 14, 11	J 14, 12	J 14, 13	J 14, 14
.01	1.041	1.041	1.041	1.041	1.041
.02	1.085	1.085	1.085	1.085	1.085
.03	1.132	1.132	1.132	1.132	1.132
.04	1.181	1.181	1.181	1.181	1.181
.05	1.234	1.234	1.234	1.234	1.234
.06	1.290	1.290	1.290	1.290	1.290
.07	1.350	1.350	1.350	1.350	1.350
.08	1.414	1.414	1.414	1.414	1.414
.09	1.482	1.482	1.482	1.482	1.482
.10	1.555	1.555	1.555	1.555	1.555
.11	1.633	1.633	1.633	1.633	1.633
.12	1.717	1.717	1.717	1.717	1.717
.13	1.806	1.806	1.806	1.806	1.806
.14	1.902	1.902	1.902	1.902	1.902
.15	2.005	2.005	2.005	2.005	2.005
.16	2.115	2.115	2.115	2.115	2.115
.17	2.234	2.234	2.234	2.234	2.234
.18	2.362	2.362	2.362	2.362	2.362
.19	2.500	2.500	2.500	2.500	2.500
.20	2.649	2.649	2.649	2.649	2.649
.21	2.809	2.810	2.810	2.810	2.810
.22	2.982	2.983	2.983	2.983	2.983
.23	3.169	3.171	3.171	3.171	3.171
.24	3.372	3.374	3.375	3.375	3.375
.25	3.592	3.595	3.596	3.596	3.596
.26	3.830	3.834	3.835	3.836	3.836
.27	4.088	4.094	4.096	4.097	4.097
.28	4.369	4.377	4.380	4.381	4.381
.29	4.674	4.686	4.689	4.691	4.691
.30	5.007	5.022	5.027	5.029	5.029
.31	5.368	5.389	5.396	5.398	5.399
.32	5.763	5.790	5.800	5.803	5.804
.33	6.193	6.229	6.242	6.247	6.249
.34	6.663	6.709	6.727	6.734	6.736
.35	7.176	7.236	7.260	7.270	7.273
.36	7.736	7.815	7.847	7.859	7.864
.37	8.350	8.451	8.492	8.510	8.517
.38	9.020	9.150	9.205	9.228	9.238
.39	9.755	9.919	9.991	10.022	10.036
.40	10.559	10.768	10.861	10.922	10.921
.41	11.441	11.703	11.824	11.879	11.904
.42	12.406	12.736	12.892	12.964	12.997
.43	13.465	13.877	14.077	14.172	14.217
.44	14.625	15.140	15.394	15.518	15.578
.45	15.898	16.536	16.859	17.021	17.100
.46	17.293	18.083	18.492	18.701	18.806
.47	18.822	19.797	20.315	20.482	20.721
.48	20.500	21.698	22.346	22.662	22.875
.49	22.337	23.808	24.619	25.062	25.301
.50	24.351	26.149	27.163	27.727	28.038

TABLE

Z	J 14, 10	J 14, 11	J 14, 12	J 14, 13	J 14, 14
.51	28.555	28.750	30.013	30.730	31.133
.52	28.968	31.640	33.208	34.117	34.638
.53	31.607	34.832	36.785	37.943	38.614
.54	34.490	38.453	40.824	42.270	43.132
.55	37.638	42.394	45.355	47.172	48.276
.56	41.060	46.812	50.454	52.732	54.141
.57	44.805	51.726	56.197	59.046	60.841
.58	48.866	57.192	62.670	66.225	68.505
.59	53.271	63.271	69.972	74.297	77.287
.60	58.059	70.033	78.213	83.213	87.367
.61	63.186	77.550	87.522	94.543	98.953
.62	68.725	85.905	98.041	106.486	112.292
.63	74.663	95.186	109.855	120.273	127.672
.64	81.002	105.490	123.391	135.272	145.429
.65	87.733	116.821	138.618	151.493	165.962
.66	94.855	129.280	155.858	170.294	189.733
.67	102.271	143.813	175.382	190.938	217.307
.68	109.983	159.119	197.498	223.975	249.315
.69	117.884	176.234	222.557	258.702	286.529
.70	125.851	195.091	250.952	295.290	329.848
.71	133.718	215.822	282.131	337.520	380.338
.72	141.260	238.554	319.595	385.855	439.259
.73	148.179	263.404	360.910	441.866	508.101
.74	154.086	290.470	407.714	506.552	588.629
.75	158.477	319.822	460.719	581.208	682.957
.76	160.706	351.488	520.720	667.737	793.505
.77	159.946	385.455	588.605	767.793	923.283
.78	155.147	421.548	665.356	883.617	1075.773
.79	144.981	460.596	752.058	1017.797	1255.139
.80	127.776	499.198	849.503	1173.321	1466.338
.81	101.433	539.772	960.188	1353.670	1715.274
.82	65.324	580.469	1084.316	1562.897	2008.983
.83	10.166	630.101	1223.787	1805.723	2355.856
.84	-62.128	687.032	1380.184	2087.640	2765.910
.85	-138.641	749.038	1555.149	2415.041	3251.107
.86	-228.684	713.242	1750.346	2793.990	3825.741
.87	-451.071	735.717	1967.407	3237.298	4506.907
.88	-664.475	731.831	2207.855	3750.715	5315.061
.89	-937.842	693.839	2472.998	4347.446	6274.693
.90	-1285.917	634.090	2763.781	5040.949	7415.153
.91	-1726.867	532.600	3080.597	5846.888	8771.540
.92	-2283.060	374.331	3423.020	6783.393	10386.068
.93	-2982.000	142.145	3789.471	7871.426	12309.289
.94	-3857.477	-186.195	4176.762	9135.176	14601.885
.95	-4869.958	-638.797	4579.523	10602.527	17339.722
.96	-6135.294	-1250.941	4988.458	12305.658	20601.321
.97	-8006.765	-2007.146	5394.355	14281.080	24500.759
.98	-10407.658	-3145.072	5776.886	16571.335	29161.316
.99	-12709.042	-4548.371	6113.010	19224.271	34735.349

FITTING A GROWTH CURVE

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TABLE

Z	J 15, 1	J 15, 2	J 15, 3	J 15, 4	J 15, 5	J 15, 6	J 15, 7	J 15, 8	J 15, 9
.01	0.134	-13.377	0.753	1.037	1.041	1.041	1.041	1.041	1.041
.02	0.275	-13.798	0.491	1.007	1.085	1.085	1.085	1.085	1.085
.03	0.425	-14.173	0.214	1.090	1.130	1.132	1.132	1.132	1.132
.04	0.584	-14.508	-0.080	1.105	1.177	1.181	1.181	1.181	1.181
.05	0.753	-15.007	-0.392	1.112	1.226	1.233	1.234	1.234	1.234
.06	0.932	-15.494	-0.723	1.109	1.276	1.280	1.280	1.280	1.280
.07	1.123	-15.969	-1.074	1.096	1.326	1.348	1.350	1.350	1.350
.08	1.326	-16.403	-1.446	1.071	1.377	1.410	1.414	1.414	1.414
.09	1.542	-16.978	-1.841	1.034	1.428	1.476	1.482	1.482	1.482
.10	1.773	-17.514	-2.261	0.983	1.479	1.545	1.554	1.555	1.555
.11	2.019	-18.072	-2.707	0.917	1.528	1.619	1.631	1.633	1.633
.12	2.282	-18.653	-3.180	0.835	1.575	1.695	1.714	1.716	1.717
.13	2.564	-19.260	-3.684	0.733	1.620	1.776	1.801	1.805	1.806
.14	2.865	-19.892	-4.219	0.615	1.662	1.860	1.895	1.901	1.902
.15	3.188	-20.551	-4.789	0.474	1.699	1.947	1.995	2.003	2.005
.16	3.534	-21.239	-5.394	0.310	1.730	2.038	2.101	2.113	2.115
.17	3.905	-21.957	-6.039	0.121	1.755	2.132	2.214	2.230	2.234
.18	4.303	-22.707	-6.725	-0.097	1.771	2.229	2.333	2.356	2.361
.19	4.732	-23.490	-7.457	-0.345	1.779	2.329	2.461	2.492	2.498
.20	5.192	-24.308	-8.236	-0.626	1.774	2.393	2.597	2.637	2.646
.21	5.688	-25.163	-9.066	-0.944	1.757	2.433	2.740	2.793	2.806
.22	6.222	-26.057	-9.951	-1.302	1.724	2.437	2.892	2.960	2.977
.23	6.798	-26.992	-10.895	-1.704	1.673	2.740	3.052	3.139	3.163
.24	7.420	-27.969	-11.903	-2.153	1.602	2.842	3.221	3.323	3.363
.25	8.091	-28.992	-12.979	-2.655	1.507	2.942	3.400	3.509	3.560
.26	8.816	-30.063	-14.128	-3.214	1.384	3.038	3.587	3.700	3.813
.27	9.601	-31.184	-15.356	-3.836	1.231	3.128	3.782	3.998	4.066
.28	10.452	-32.357	-16.668	-4.526	1.043	3.210	3.987	4.252	4.340
.29	11.373	-33.587	-18.072	-5.292	0.815	3.283	4.200	4.525	4.636
.30	12.373	-34.875	-19.574	-6.141	0.541	3.342	4.421	4.816	4.956
.31	13.458	-36.224	-21.181	-7.081	0.216	3.385	4.640	5.128	5.303
.32	14.638	-37.638	-22.903	-8.120	-0.167	3.409	4.883	5.469	5.679
.33	15.921	-39.120	-24.748	-9.268	-0.616	3.408	5.122	5.835	6.085
.34	17.319	-40.674	-26.725	-10.536	-1.140	3.378	5.364	6.192	6.525
.35	18.843	-42.302	-28.846	-11.938	-1.748	3.312	5.607	6.593	7.002
.36	20.506	-44.010	-31.122	-13.482	-2.431	3.205	5.848	7.018	7.517
.37	22.323	-45.800	-33.566	-15.186	-3.201	3.048	6.084	7.467	8.075
.38	24.310	-47.676	-36.190	-17.067	-4.191	2.833	6.312	7.941	8.678
.39	26.485	-49.642	-39.011	-19.140	-5.258	2.548	6.525	8.440	9.329
.40	28.870	-51.703	-42.045	-21.427	-6.478	2.183	6.719	8.963	10.032
.41	31.486	-53.862	-45.309	-23.948	-7.870	1.723	6.887	9.508	10.790
.42	34.361	-56.122	-48.822	-26.728	-9.458	1.153	7.019	10.074	11.697
.43	37.524	-58.489	-52.636	-29.794	-11.294	0.454	7.103	10.659	12.685
.44	41.007	-60.964	-56.684	-33.176	-13.318	-0.394	7.135	11.258	13.749
.45	44.848	-63.551	-61.081	-36.907	-15.650	-1.415	7.093	11.867	14.841
.46	49.090	-66.253	-65.824	-41.023	-18.297	-2.637	6.962	12.479	15.923
.47	53.789	-69.071	-70.943	-45.566	-21.268	-4.091	6.722	13.086	16.679
.48	58.973	-72.096	-76.472	-50.582	-24.698	-5.814	6.350	13.677	17.908
.49	64.731	-75.059	-82.446	-56.121	-28.549	-7.849	5.817	14.249	19.213
.50	71.154	-78.228	-88.963	-62.240	-32.968	-10.242	5.091	14.757	20.591

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 PHYS. BULLETIN, NO. 116

TABLE

Z	J 15, 1	J 15, 2	J 15, 3	J 15, 4	J 15, 5	J 15, 6	J 15, 7	J 15, 8	J 15, 9
.51	78.233	-81.509	-93.887	-69.003	-37.842	-13.031	4.132	15.310	22.040
.52	86.159	-84.806	-103.413	-76.481	-43.426	-16.339	2.884	15.371	23.553
.53	94.981	-88.380	-111.622	-84.733	-49.743	-20.179	1.323	15.812	25.129
.54	104.845	-91.949	-120.480	-92.809	-56.869	-24.639	-0.644	15.803	26.731
.55	115.882	-95.586	-130.074	-101.042	-64.975	-29.875	-3.083	15.771	28.405
.56	128.250	-99.268	-140.472	-110.270	-74.123	-35.941	-6.081	15.588	30.069
.57	142.153	-102.965	-151.741	-127.714	-84.475	-42.989	-9.743	14.678	31.716
.58	157.744	-106.678	-163.959	-141.512	-96.191	-51.169	-14.191	13.559	33.310
.59	175.326	-110.240	-177.206	-156.820	-109.454	-60.638	-19.568	11.934	34.801
.60	195.162	-113.707	-191.570	-173.812	-124.473	-71.658	-26.043	9.685	36.131
.61	217.583	-116.961	-207.144	-192.684	-141.485	-84.403	-33.815	6.964	37.223
.62	242.968	-119.965	-224.028	-213.632	-160.762	-99.166	-43.118	2.704	37.979
.63	271.702	-122.417	-242.327	-236.963	-182.613	-116.269	-54.227	-2.402	38.278
.64	304.482	-124.346	-262.149	-262.889	-207.391	-136.032	-67.469	-8.903	37.969
.65	341.733	-125.696	-283.610	-291.737	-235.502	-158.964	-83.224	-17.099	36.864
.66	384.221	-126.465	-306.855	-323.849	-267.408	-185.090	-101.944	-27.347	34.729
.67	432.772	-124.540	-331.910	-359.639	-303.637	-216.209	-124.161	-40.079	31.275
.68	488.337	-121.749	-358.980	-399.444	-344.794	-251.759	-150.502	-55.812	26.145
.69	552.115	-116.957	-388.141	-443.831	-391.571	-292.940	-181.709	-75.168	18.900
.70	625.388	-109.541	-419.489	-493.300	-444.761	-340.640	-218.634	-98.893	8.999
.71	709.754	-98.887	-453.698	-548.441	-503.271	-395.907	-262.372	-127.883	-4.223
.72	807.080	-84.201	-489.016	-609.909	-571.139	-459.969	-314.084	-163.214	-21.583
.73	919.509	-64.512	-527.248	-678.426	-652.553	-534.217	-375.233	-206.178	-44.089
.74	1049.829	-38.631	-567.743	-754.788	-741.874	-620.334	-447.527	-258.328	-72.943
.75	1200.952	-5.101	-610.370	-839.870	-843.655	-720.249	-532.987	-321.539	-109.673
.76	1376.605	97.869	-654.895	-934.924	-959.676	-816.184	-634.007	-398.025	-156.112
.77	1581.148	162.432	-709.944	-1040.082	-1091.968	-970.791	-753.418	-490.599	-211.510
.78	1819.768	161.283	-747.964	-1157.967	-1242.849	-1127.122	-804.579	-602.229	-287.621
.79	2098.642	247.676	-795.162	-1287.657	-1414.965	-1308.745	-1061.465	-737.054	-378.813
.80	2425.137	355.993	-841.440	-1432.207	-1611.327	-1519.829	-1258.793	-899.996	-492.204
.81	2808.050	489.659	-883.305	-1592.812	-1833.359	-1765.227	-1492.151	-1095.781	-632.827
.82	3257.895	656.690	-924.761	-1769.280	-2090.948	-2050.698	-1708.106	-1332.088	-806.832
.83	3787.249	863.133	-957.163	-1964.431	-2382.495	-2382.573	-2094.698	-1616.773	-1021.734
.84	4411.177	1118.223	-979.049	-2178.569	-2714.972	-2798.817	-2481.066	-1920.632	-1286.713
.85	5147.734	1432.961	-985.915	-2413.936	-3093.977	-3218.302	-2928.324	-2372.537	-1612.983
.86	6018.282	1820.533	-971.941	-2670.169	-3523.793	-3741.456	-3479.577	-2869.642	-2014.238
.87	7049.733	2297.069	-929.644	-2948.061	-4017.436	-4350.407	-4120.308	-3468.074	-2507.199
.88	8272.443	2883.965	-849.452	-3247.437	-4573.796	-5059.244	-4871.119	-4188.499	-3112.279
.89	9724.300	3694.290	-719.159	-3567.240	-5212.220	-5884.318	-5777.665	-5055.454	-3854.398
.90	11450.532	4838.545	-523.263	-3995.307	-5933.422	-6844.574	-6841.874	-6098.981	-4765.960
.91	13505.603	6573.446	-242.124	-4537.842	-6750.577	-7961.667	-8102.380	-7344.838	-5878.666
.92	15955.133	8993.923	149.069	-4618.919	-7674.708	-9201.735	-9595.445	-8866.211	-7241.970
.93	18878.252	12344.948	681.587	-4079.737	-8717.487	-10773.165	-11363.968	-10684.903	-8910.856
.94	22370.302	16933.772	1394.764	-5237.815	-10001.030	-12529.809	-13458.656	-12873.262	-10931.922
.95	26546.475	22982.673	2337.979	-5645.616	-11207.996	-14570.194	-16039.415	-15996.199	-13447.367
.96	31845.750	30922.314	3723.114	-5996.289	-12670.184	-16938.369	-18873.938	-18673.607	-16466.861
.97	37355.942	39655.784	5177.393	-6086.652	-14316.764	-19684.649	-22354.635	-22483.766	-20227.088
.98	44176.806	50453.648	7248.137	-6134.849	-16199.506	-22665.997	-26476.648	-27065.041	-24771.102
.99	53342.414	66660.002	9905.489	-5997.316	-18123.472	-26546.922	-31340.507	-32575.981	-30324.029

FITTING A GROWTH CURVE

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TABLE



Z	J 15, 10	J 15, 11	J 15, 12	J 15, 13	J 15, 14	J 15, 15
.01	1.041	1.041	1.041	1.041	1.041	1.041
.02	1.085	1.085	1.085	1.085	1.085	1.085
.03	1.132	1.132	1.132	1.132	1.132	1.132
.04	1.181	1.181	1.181	1.181	1.181	1.181
.05	1.234	1.234	1.234	1.234	1.234	1.234
.06	1.290	1.290	1.290	1.290	1.290	1.290
.07	1.350	1.350	1.350	1.350	1.350	1.350
.08	1.414	1.414	1.414	1.414	1.414	1.414
.09	1.482	1.482	1.482	1.482	1.482	1.482
.10	1.555	1.555	1.555	1.555	1.555	1.555
.11	1.633	1.633	1.633	1.633	1.633	1.633
.12	1.717	1.717	1.717	1.717	1.717	1.717
.13	1.806	1.806	1.806	1.806	1.806	1.806
.14	1.902	1.902	1.902	1.902	1.902	1.902
.15	2.005	2.005	2.005	2.005	2.005	2.005
.16	2.115	2.115	2.115	2.115	2.115	2.115
.17	2.234	2.234	2.234	2.234	2.234	2.234
.18	2.362	2.362	2.362	2.362	2.362	2.362
.19	2.500	2.500	2.500	2.500	2.500	2.500
.20	2.648	2.649	2.649	2.649	2.649	2.649
.21	2.809	2.810	2.810	2.810	2.810	2.810
.22	2.982	2.983	2.983	2.983	2.983	2.983
.23	3.169	3.171	3.171	3.171	3.171	3.171
.24	3.372	3.374	3.375	3.375	3.375	3.375
.25	3.591	3.595	3.598	3.598	3.598	3.598
.26	3.829	3.834	3.835	3.839	3.839	3.839
.27	4.088	4.094	4.098	4.097	4.097	4.097
.28	4.368	4.377	4.380	4.381	4.381	4.381
.29	4.673	4.685	4.689	4.690	4.691	4.691
.30	5.005	5.021	5.027	5.029	5.029	5.029
.31	5.366	5.388	5.396	5.398	5.399	5.399
.32	5.759	5.789	5.799	5.803	5.804	5.805
.33	6.189	6.227	6.241	6.247	6.248	6.249
.34	6.667	6.707	6.726	6.734	6.738	6.737
.35	7.198	7.238	7.259	7.269	7.273	7.274
.36	7.726	7.811	7.845	7.859	7.864	7.866
.37	8.335	8.445	8.490	8.509	8.516	8.519
.38	9.002	9.142	9.202	9.227	9.237	9.242
.39	9.733	9.909	9.987	10.021	10.035	10.041
.40	10.528	10.754	10.855	10.900	10.920	10.929
.41	11.400	11.685	11.816	11.876	11.903	11.915
.42	12.354	12.712	12.881	12.969	12.996	13.013
.43	13.399	13.846	14.063	14.166	14.215	14.238
.44	14.541	15.099	15.375	15.510	15.575	15.607
.45	15.790	16.484	16.853	17.010	17.097	17.139
.46	17.157	18.015	18.469	18.687	18.802	18.859
.47	18.650	19.710	20.271	20.364	20.715	20.793
.48	20.282	21.586	22.291	22.668	22.866	22.970
.49	22.064	23.664	24.548	25.029	25.299	25.428
.50	24.007	25.966	27.070	27.684	28.023	28.208

TABLE

Z	J 18, 10	J 18, 11	J 18, 12	J 18, 13	J 18, 14	J 18, 15
.01	26.125	28.516	29.802	30.673	31.113	31.338
.02	28.431	31.342	33.052	34.043	34.611	34.934
.03	30.836	34.474	36.594	37.846	38.478	39.003
.04	33.435	37.945	40.566	42.145	43.080	43.642
.05	36.299	41.791	45.024	47.009	48.215	48.940
.06	39.480	46.051	50.030	52.520	54.061	55.005
.07	43.036	50.768	55.656	58.772	60.735	61.961
.08	46.885	55.988	61.482	65.871	68.467	69.954
.09	50.820	61.761	68.496	73.843	77.108	79.157
.10	55.009	68.140	77.102	83.129	87.135	89.772
.11	59.483	75.181	86.113	93.593	98.822	102.041
.12	64.105	82.942	96.227	105.227	111.903	116.246
.13	68.965	91.484	107.679	119.147	127.169	132.724
.14	74.077	100.869	120.541	134.706	144.781	151.374
.15	79.077	111.106	135.022	152.496	165.127	174.166
.16	84.174	122.402	151.234	172.850	188.694	200.164
.17	89.144	134.659	169.671	196.155	215.927	230.533
.18	93.823	147.967	190.369	222.858	247.545	266.069
.19	97.991	162.350	213.511	253.471	284.238	307.720
.20	101.965	177.811	239.375	288.587	326.939	356.616
.21	105.278	194.318	268.827	328.887	376.613	414.107
.22	108.155	211.796	301.616	375.156	434.491	481.811
.23	102.493	230.108	338.317	428.297	502.002	561.661
.24	97.822	249.057	379.255	489.345	580.829	655.079
.25	89.167	268.258	425.046	559.491	672.964	767.549
.26	75.294	287.302	475.804	646.097	780.766	899.714
.27	54.651	305.518	532.288	732.724	906.985	1056.499
.28	25.284	322.013	594.539	820.150	1054.938	1243.745
.29	-15.256	335.586	663.019	961.404	1228.201	1464.292
.30	-70.638	344.632	737.919	1101.788	1432.275	1728.179
.31	-142.869	347.039	819.297	1262.908	1671.707	2042.911
.32	-238.631	340.035	906.990	1447.701	1933.246	2418.766
.33	-363.211	320.013	1000.510	1659.462	2284.626	2898.183
.34	-524.082	282.304	1098.777	1901.866	2674.093	3406.223
.35	-730.023	220.882	1200.693	2178.982	3134.159	4051.146
.36	-984.031	128.012	1303.432	2495.276	3675.907	4835.104
.37	-1328.997	-6.213	1403.650	2855.597	4314.860	5754.998
.38	-1753.149	-194.443	1496.570	3265.137	5088.803	6873.521
.39	-2288.681	-452.784	1574.651	3729.351	5958.786	8220.441
.40	-2962.667	-801.705	1638.979	4253.830	7009.798	9844.159
.41	-3809.320	-1267.160	1646.468	4844.100	8251.016	11803.643
.42	-4870.588	-1882.003	1609.851	5505.330	9717.504	14170.770
.43	-6198.433	-2687.757	1496.181	6241.905	11460.262	17033.231
.44	-7837.391	-3746.758	1271.166	7056.819	13467.774	20498.044
.45	-9926.563	-5095.132	907.061	7950.862	15917.104	24695.954
.46	-12594.061	-6845.809	539.975	8921.482	18775.557	29786.665
.47	-15712.934	-9093.190	-483.547	9961.241	22152.127	35985.536
.48	-19201.308	-11968.274	-1680.851	11055.780	26159.664	43711.491
.49	-24654.275	-15635.301	-3334.657	12181.121	30846.300	52566.636

FITTING A GROWTH CURVE

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TABLE

Z	J 16, 1	J 16, 2	J 16, 3	J 16, 4	J 16, 5	J 16, 6	J 16, 7	J 16, 8	J 16, 9
.01	0.144	-14.408	0.722	1.037	1.041	1.041	1.041	1.041	1.041
.02	0.296	-14.831	0.449	1.096	1.085	1.085	1.085	1.085	1.085
.03	0.448	-15.271	0.148	1.067	1.130	1.132	1.132	1.132	1.132
.04	0.629	-15.728	-0.171	1.100	1.177	1.181	1.181	1.181	1.181
.05	0.811	-16.203	-0.509	1.103	1.225	1.233	1.234	1.234	1.234
.06	1.005	-16.698	-0.807	1.096	1.272	1.299	1.299	1.299	1.299
.07	1.211	-17.212	-1.248	1.077	1.325	1.348	1.359	1.359	1.359
.08	1.429	-17.747	-1.652	1.046	1.373	1.410	1.414	1.414	1.414
.09	1.653	-18.305	-2.081	1.001	1.424	1.476	1.481	1.482	1.482
.10	1.913	-18.885	-2.537	0.941	1.479	1.545	1.554	1.555	1.555
.11	2.179	-19.490	-3.021	0.865	1.530	1.618	1.631	1.633	1.633
.12	2.464	-20.130	-3.535	0.771	1.565	1.694	1.713	1.716	1.717
.13	2.768	-20.778	-4.083	0.657	1.607	1.774	1.801	1.805	1.805
.14	3.094	-21.463	-4.664	0.522	1.644	1.857	1.894	1.901	1.902
.15	3.443	-22.179	-5.283	0.363	1.676	1.943	1.994	2.003	2.005
.16	3.818	-22.925	-5.941	0.178	1.702	2.033	2.100	2.113	2.115
.17	4.220	-23.705	-6.642	-0.034	1.720	2.125	2.212	2.230	2.234
.18	4.652	-24.519	-7.389	-0.277	1.728	2.220	2.332	2.356	2.361
.19	5.116	-25.369	-8.184	-0.554	1.725	2.316	2.458	2.491	2.498
.20	5.616	-26.258	-9.022	-0.867	1.710	2.414	2.593	2.636	2.646
.21	6.154	-27.187	-9.906	-1.221	1.679	2.513	2.735	2.791	2.805
.22	6.734	-28.159	-10.901	-1.618	1.631	2.611	2.882	2.958	2.977
.23	7.360	-29.175	-11.909	-2.064	1.562	2.708	3.043	3.137	3.162
.24	8.035	-30.239	-13.028	-2.562	1.470	2.803	3.210	3.329	3.362
.25	8.765	-31.352	-14.261	-3.118	1.351	2.893	3.385	3.534	3.578
.26	9.554	-32.518	-15.613	-3.738	1.202	2.978	3.568	3.755	3.812
.27	10.409	-33.738	-17.094	-4.426	1.017	3.055	3.759	3.990	4.064
.28	11.335	-35.017	-18.727	-5.191	0.793	3.122	3.958	4.243	4.337
.29	12.339	-36.357	-19.769	-6.038	0.524	3.177	4.163	4.512	4.632
.30	13.429	-37.762	-21.401	-6.978	0.204	3.215	4.375	4.800	4.951
.31	14.613	-39.234	-23.158	-8.017	-0.174	3.233	4.592	5.107	5.296
.32	15.901	-40.777	-25.041	-9.167	-0.618	3.227	4.813	5.434	5.669
.33	17.303	-42.395	-27.060	-10.437	-1.139	3.192	5.046	5.782	6.073
.34	18.831	-44.093	-29.225	-11.841	-1.738	3.122	5.299	6.150	6.509
.35	20.498	-45.873	-31.548	-13.390	-2.435	3.010	5.579	6.540	6.981
.36	22.319	-47.740	-34.033	-15.101	-3.238	2.858	5.882	6.952	7.490
.37	24.309	-49.698	-36.722	-16.989	-4.162	2.678	6.207	7.386	8.040
.38	26.488	-51.752	-39.603	-19.072	-5.222	2.359	6.585	7.841	8.634
.39	28.875	-53.906	-42.701	-21.369	-6.435	1.969	6.953	8.316	9.273
.40	31.494	-56.165	-46.034	-23.904	-7.821	1.504	7.392	8.809	9.961
.41	34.371	-58.532	-49.623	-26.701	-9.402	0.959	6.494	9.319	10.701
.42	37.535	-61.012	-53.489	-29.786	-11.203	0.226	6.549	9.843	11.495
.43	41.018	-63.610	-57.657	-33.191	-13.251	-0.626	6.544	10.376	12.349
.44	44.859	-66.329	-62.151	-36.948	-15.579	-1.653	6.465	10.913	13.255
.45	49.100	-69.173	-67.001	-41.096	-18.222	-2.880	6.295	11.446	14.224
.46	53.788	-72.145	-72.238	-45.677	-21.220	-4.341	6.013	11.967	15.254
.47	58.979	-75.247	-77.896	-50.757	-24.621	-6.072	5.595	12.465	16.345
.48	64.734	-78.479	-84.012	-56.357	-28.475	-8.116	5.012	12.924	17.505
.49	71.123	-81.843	-90.627	-62.508	-32.842	-10.521	4.231	13.329	18.702
.50	78.229	-85.356	-97.785	-69.343	-37.788	-13.344	3.211	13.659	19.961

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FISH BULLETIN NO. 116

TABLE

Z	J 16, 1	J 16, 2	J 16, 3	J 16, 4	J 16, 5	J 16, 6	J 16, 7	J 16, 8	J 16, 9
.01	86.143	-88.955	-105.535	-76.905	-43.389	-16.650	1.906	18.879	21.265
.02	94.971	-92.691	-113.931	-83.276	-49.732	-20.515	0.290	13.396	22.602
.03	104.834	-96.536	-123.030	-94.548	-56.915	-25.025	-1.792	13.877	23.959
.04	115.873	-100.473	-132.866	-104.822	-65.049	-30.280	-4.328	13.562	25.316
.05	128.249	-104.487	-143.596	-116.213	-74.261	-36.207	-7.438	12.964	26.646
.06	142.148	-108.546	-155.207	-128.830	-84.697	-43.211	-11.229	12.010	27.945
.07	157.785	-112.617	-167.811	-142.878	-96.522	-51.776	-15.828	10.615	29.081
.08	175.409	-116.654	-181.494	-158.458	-109.924	-61.374	-21.383	8.674	30.088
.09	195.309	-120.599	-196.332	-175.773	-125.121	-72.514	-28.070	6.061	30.863
.10	217.823	-124.377	-212.488	-195.029	-142.358	-85.438	-36.066	2.624	31.324
.11	243.343	-127.895	-230.010	-216.454	-161.918	-100.429	-45.705	-1.821	31.454
.12	272.226	-131.063	-249.036	-240.308	-184.126	-117.815	-57.181	-7.486	30.816
.13	303.310	-133.643	-269.687	-269.882	-209.352	-137.077	-70.878	-14.603	29.337
.14	342.921	-135.541	-292.063	-296.302	-238.021	-161.360	-87.187	-23.647	27.304
.15	388.868	-136.855	-316.387	-329.554	-270.622	-188.481	-106.388	-34.822	23.831
.16	437.109	-136.219	-342.703	-369.291	-307.715	-219.944	-129.645	-48.684	18.850
.17	491.578	-134.526	-371.176	-407.333	-349.944	-256.433	-157.077	-65.704	11.805
.18	556.314	-130.464	-401.935	-453.478	-398.048	-298.830	-189.524	-86.746	2.488
.19	631.347	-123.996	-435.180	-504.804	-452.879	-348.607	-228.076	-112.445	-9.988
.20	717.775	-114.277	-470.770	-562.156	-515.414	-405.197	-273.796	-148.841	-26.290
.21	817.811	-100.468	-509.017	-626.252	-586.777	-471.624	-328.006	-182.116	-47.352
.22	933.855	-81.254	-549.868	-697.891	-668.201	-548.877	-392.276	-228.699	-74.319
.23	1068.765	-56.197	-593.291	-777.957	-761.351	-638.699	-468.470	-283.311	-108.603
.24	1223.954	-22.474	-639.167	-867.422	-867.738	-743.262	-538.825	-354.032	-151.035
.25	1409.508	20.290	-687.259	-967.359	-989.442	-865.023	-606.368	-437.572	-206.447
.26	1624.321	76.010	-737.175	-1078.313	-1128.659	-1006.884	-730.054	-538.369	-274.756
.27	1876.266	146.576	-788.310	-1203.354	-1287.991	-1172.233	-845.854	-660.690	-360.079
.28	2172.406	236.581	-839.781	-1342.017	-1470.403	-1365.125	-1122.782	-808.777	-466.371
.29	2521.246	350.597	-890.337	-1496.311	-1679.283	-1590.190	-1333.231	-967.999	-598.491
.30	2933.038	493.479	-938.248	-1667.694	-1918.502	-1852.949	-1587.548	-1204.860	-762.415
.31	3420.168	672.627	-981.161	-1857.633	-2192.473	-2159.856	-1887.329	-1467.235	-965.488
.32	3997.611	896.706	-1019.912	-2067.337	-2598.211	-2518.477	-2242.642	-1784.696	-1216.743
.33	4683.501	1176.450	-1038.295	-2298.762	-2865.409	-2937.685	-2667.319	-2188.716	-1527.289
.34	5499.829	1525.156	-1042.755	-2552.314	-3276.437	-3427.871	-3171.295	-2633.462	-1910.789
.35	6473.291	1959.304	-1022.011	-2828.892	-3746.590	-4001.203	-3771.011	-3195.724	-2384.032
.36	7636.334	2499.226	-966.568	-3128.375	-4283.851	-4671.907	-4484.929	-3876.296	-2967.759
.37	9028.441	3170.588	-864.094	-3450.268	-4897.177	-5456.609	-5335.049	-4709.124	-3687.355
.38	10697.707	4004.430	-698.643	-3792.778	-5596.396	-6374.665	-6347.697	-5697.542	-4574.154
.39	12702.779	5059.941	-449.655	-4151.402	-6392.202	-7438.672	-7554.252	-6963.354	-5666.686
.40	15115.229	6325.491	-90.701	-4520.159	-7296.068	-8704.843	-8992.152	-8368.199	-7012.366
.41	18022.499	7921.170	412.111	-4889.466	-8320.085	-10173.576	-10706.033	-10140.230	-8699.541
.42	21531.491	9901.389	1102.149	-5245.271	-9476.977	-11860.969	-12749.978	-12287.120	-10710.901
.43	25773.025	12359.411	2034.796	-5567.554	-10778.165	-13894.629	-14844.095	-14888.202	-13222.077
.44	30967.262	15469.726	3280.456	-5828.371	-12236.097	-16223.585	-18087.896	-18019.887	-16114.496
.45	37130.480	19195.516	4929.601	-6089.321	-13860.316	-18969.850	-21448.301	-21841.225	-20120.608
.46	44383.351	23894.435	7095.864	-6298.327	-15637.611	-22135.830	-25072.014	-26461.161	-24894.977
.47	52891.077	29777.184	9724.438	-6475.311	-17529.830	-25868.865	-30384.653	-32402.104	-30569.414
.48	62629.074	36968.636	13399.159	-6526.900	-19771.305	-30110.182	-36434.745	-38901.431	-37662.025
.49	73623.383	45687.778	18392.827	-6489.414	-22065.432	-34670.314	-43097.078	-47159.788	-46387.591

FITTING A GROWTH CURVE

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TABLE

Z	J 16, 10	J 16, 11	J 16, 12	J 16, 13	J 16, 14	J 16, 15	J 16, 16
.01	1.041	1.041	1.041	1.041	1.041	1.041	1.041
.02	1.085	1.085	1.085	1.085	1.085	1.085	1.085
.03	1.132	1.132	1.132	1.132	1.132	1.132	1.132
.04	1.181	1.181	1.181	1.181	1.181	1.181	1.181
.05	1.234	1.234	1.234	1.234	1.234	1.234	1.234
.06	1.290	1.290	1.290	1.290	1.290	1.290	1.290
.07	1.350	1.350	1.350	1.350	1.350	1.350	1.350
.08	1.414	1.414	1.414	1.414	1.414	1.414	1.414
.09	1.482	1.482	1.482	1.482	1.482	1.482	1.482
.10	1.555	1.555	1.555	1.555	1.555	1.555	1.555
.11	1.633	1.633	1.633	1.633	1.633	1.633	1.633
.12	1.717	1.717	1.717	1.717	1.717	1.717	1.717
.13	1.806	1.806	1.806	1.806	1.806	1.806	1.806
.14	1.902	1.902	1.902	1.902	1.902	1.902	1.902
.15	2.005	2.005	2.005	2.005	2.005	2.005	2.005
.16	2.115	2.115	2.115	2.115	2.115	2.115	2.115
.17	2.234	2.234	2.234	2.234	2.234	2.234	2.234
.18	2.362	2.362	2.362	2.362	2.362	2.362	2.362
.19	2.500	2.500	2.500	2.500	2.500	2.500	2.500
.20	2.648	2.649	2.649	2.649	2.649	2.649	2.649
.21	2.809	2.810	2.810	2.810	2.810	2.810	2.810
.22	2.982	2.983	2.983	2.983	2.983	2.983	2.983
.23	3.169	3.171	3.171	3.171	3.171	3.171	3.171
.24	3.372	3.374	3.375	3.375	3.375	3.375	3.375
.25	3.591	3.595	3.596	3.596	3.596	3.596	3.596
.26	3.829	3.834	3.835	3.836	3.836	3.836	3.836
.27	4.087	4.094	4.096	4.097	4.097	4.097	4.097
.28	4.367	4.377	4.380	4.381	4.381	4.381	4.381
.29	4.672	4.685	4.689	4.690	4.691	4.691	4.691
.30	5.005	5.021	5.027	5.029	5.029	5.029	5.029
.31	5.363	5.387	5.395	5.398	5.399	5.399	5.400
.32	5.756	5.788	5.799	5.803	5.804	5.805	5.805
.33	6.184	6.225	6.241	6.246	6.248	6.249	6.249
.34	6.650	6.705	6.726	6.733	6.736	6.737	6.738
.35	7.159	7.230	7.258	7.269	7.273	7.274	7.275
.36	7.715	7.806	7.843	7.858	7.864	7.866	7.867
.37	8.321	8.430	8.488	8.508	8.516	8.519	8.521
.38	8.983	9.134	9.198	9.225	9.227	9.231	9.233
.39	9.706	9.899	9.983	10.019	10.034	10.041	10.044
.40	10.496	10.740	10.849	10.898	10.919	10.928	10.932
.41	11.359	11.667	11.808	11.872	11.901	11.914	11.920
.42	12.302	12.688	12.870	12.955	12.994	13.012	13.020
.43	13.331	13.815	14.048	14.159	14.212	14.237	14.248
.44	14.455	15.058	15.356	15.501	15.572	15.605	15.621
.45	15.681	16.430	16.809	16.998	17.092	17.138	17.160
.46	17.018	17.945	18.425	18.671	18.785	18.827	18.888
.47	18.475	19.620	20.225	20.542	20.706	20.790	20.832
.48	20.060	21.470	22.252	22.638	22.853	22.966	23.025
.49	21.784	23.514	24.470	24.981	25.272	25.422	25.502
.50	23.656	25.774	26.968	27.633	28.000	28.200	28.308

TABLE

Z	J 16, 10	J 16, 11	J 16, 12	J 16, 13	J 16, 14	J 16, 15	J 16, 16
.51	25.684	28.271	29.760	30.606	31.081	31.346	31.493
.52	27.878	31.030	32.881	33.954	34.569	34.919	35.116
.53	30.246	34.077	36.372	37.729	38.522	38.982	39.247
.54	32.793	37.440	40.280	41.961	43.011	43.614	43.968
.55	35.524	41.151	44.656	46.808	48.116	48.994	49.374
.56	38.441	45.242	49.558	52.259	53.631	54.596	55.080
.57	41.541	49.745	55.050	58.432	60.564	61.896	62.721
.58	44.817	54.698	61.206	65.431	68.143	69.867	70.855
.59	48.253	60.136	68.105	73.373	76.814	79.041	80.472
.60	51.855	66.063	73.858	82.302	86.750	89.620	91.465
.61	55.498	72.610	84.502	92.643	98.151	101.840	104.292
.62	59.219	79.714	94.208	104.303	111.249	115.982	119.180
.63	62.917	87.435	105.075	117.573	126.319	132.377	136.541
.64	66.495	95.790	117.254	132.685	143.677	151.419	156.826
.65	69.822	104.791	130.828	149.901	163.696	173.371	180.580
.66	72.729	114.431	146.008	169.524	186.811	199.385	208.454
.67	74.962	124.679	162.936	191.896	213.529	229.517	241.229
.68	76.323	135.476	181.782	217.408	244.445	264.744	279.847
.69	76.351	146.719	202.721	246.501	280.255	305.992	325.439
.70	74.602	158.332	223.624	279.978	321.772	354.996	379.371
.71	70.471	169.845	251.561	317.504	369.949	411.180	445.290
.72	63.189	181.171	279.780	360.616	425.900	478.094	519.191
.73	51.783	191.778	310.702	409.727	490.929	556.714	609.487
.74	35.023	201.632	344.398	465.632	566.562	649.550	717.104
.75	11.359	208.165	380.864	529.308	654.581	759.195	845.597
.76	-21.170	212.017	419.991	601.421	757.071	888.863	999.285
.77	-65.013	211.196	461.512	688.319	876.466	1042.403	1188.429
.78	-123.258	203.678	504.948	787.022	1015.605	1234.432	1405.440
.79	-192.777	187.100	549.527	880.713	1177.796	1440.433	1670.146
.80	-269.434	158.196	594.075	988.605	1360.889	1667.343	1960.112
.81	-348.282	112.796	636.882	1130.899	1587.354	2002.687	2376.046
.82	-423.966	45.518	675.515	1278.722	1844.372	2366.441	2842.291
.83	-498.008	-50.561	708.591	1443.035	2145.931	2800.082	3406.445
.84	-570.333	-184.323	725.460	1624.495	2492.931	3317.543	4090.123
.85	-641.833	-307.149	723.815	1823.275	2890.290	3935.601	4919.009
.86	-702.213	-413.089	699.167	2038.800	3372.037	4674.464	5928.529
.87	-750.714	-492.222	634.180	2269.402	3921.310	5558.478	7166.322
.88	-780.469	-537.737	515.810	2511.836	4559.251	6616.981	8653.067
.89	-797.848	-547.306	324.183	2760.633	5298.260	7885.328	10480.233
.90	-797.266	-502.312	33.174	3007.237	6153.606	9406.119	12713.911
.91	-6461.427	-3660.538	-391.459	3238.848	7138.883	11230.688	15448.157
.92	-8199.105	-4913.928	-994.426	3436.883	8273.030	13420.875	18799.596
.93	-10378.618	-6531.074	-1823.932	3574.958	9372.955	16051.149	22912.844
.94	-13110.127	-8611.691	-2983.674	3616.172	11056.574	19211.138	27967.378
.95	-16531.020	-11281.711	-4447.627	3599.622	12746.913	22908.970	34186.177
.96	-20812.376	-14701.154	-6446.622	3185.795	14640.978	27373.373	41846.476
.97	-26168.267	-19071.973	-9446.375	2550.439	16707.532	33090.869	51293.143
.98	-32863.786	-24649.562	-13157.911	1476.783	19124.202	39657.082	62853.612
.99	-41230.347	-31756.468	-18032.788	-204.777	21703.283	47588.406	77368.861

FITTING A GROWTH CURVE

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TABLE

Z	J 17, 1	J 17, 2	J 17, 3	J 17, 4	J 17, 5	J 17, 6	J 17, 7	J 17, 8	J 17, 9
.01	0.154	-15.438	0.712	1.036	1.041	1.041	1.041	1.041	1.041
.02	0.318	-15.805	0.406	1.065	1.084	1.085	1.085	1.085	1.085
.03	0.491	-16.296	-0.082	1.084	1.109	1.112	1.112	1.112	1.112
.04	0.675	-16.858	-0.261	1.095	1.177	1.181	1.181	1.181	1.181
.05	0.870	-17.370	-0.626	1.094	1.255	1.253	1.254	1.254	1.254
.06	1.077	-17.902	-1.012	1.083	1.274	1.289	1.290	1.290	1.290
.07	1.298	-18.455	-1.422	1.059	1.323	1.348	1.350	1.350	1.350
.08	1.534	-19.031	-1.858	1.021	1.372	1.410	1.414	1.414	1.414
.09	1.785	-19.632	-2.321	0.969	1.421	1.475	1.481	1.482	1.482
.10	2.033	-20.257	-2.812	0.900	1.468	1.544	1.554	1.555	1.555
.11	2.239	-20.908	-3.335	0.813	1.513	1.617	1.631	1.633	1.633
.12	2.445	-21.588	-3.890	0.707	1.555	1.692	1.713	1.716	1.717
.13	2.672	-22.296	-4.480	0.579	1.593	1.771	1.801	1.805	1.806
.14	3.323	-25.035	-5.108	0.428	1.627	1.854	1.894	1.901	1.902
.15	3.699	-23.806	-5.777	0.251	1.654	1.939	1.963	1.963	1.963
.16	4.102	-24.611	-6.488	0.047	1.674	2.027	2.098	2.112	2.115
.17	4.535	-25.452	-7.245	-0.189	1.685	2.117	2.211	2.230	2.233
.18	5.001	-26.330	-8.052	-0.477	1.685	2.210	2.329	2.355	2.361
.19	5.501	-27.248	-8.912	-0.765	1.672	2.304	2.455	2.490	2.498
.20	6.040	-28.208	-9.829	-1.108	1.645	2.398	2.589	2.635	2.646
.21	6.620	-29.211	-10.807	-1.497	1.601	2.492	2.730	2.790	2.805
.22	7.249	-30.260	-11.850	-1.934	1.538	2.585	2.878	2.956	2.977
.23	7.921	-31.350	-12.964	-2.424	1.451	2.676	3.034	3.125	3.162
.24	8.631	-32.508	-14.153	-2.971	1.338	2.763	3.199	3.326	3.361
.25	9.439	-33.712	-15.423	-3.582	1.196	2.844	3.370	3.530	3.577
.26	10.293	-34.973	-16.781	-4.261	1.019	2.918	3.549	3.749	3.810
.27	11.216	-36.292	-18.223	-5.017	0.803	2.983	3.735	3.983	4.062
.28	12.218	-37.677	-19.786	-5.855	0.544	3.035	3.928	4.235	4.354
.29	13.305	-39.128	-21.448	-6.785	0.234	3.071	4.126	4.500	4.628
.30	14.483	-40.648	-23.228	-7.814	-0.133	3.088	4.329	4.784	4.945
.31	15.708	-42.243	-25.135	-8.954	-0.565	3.081	4.535	5.087	5.289
.32	17.104	-43.916	-27.189	-10.214	-1.069	3.046	4.743	5.408	5.660
.33	18.685	-45.671	-29.372	-11.607	-1.656	2.976	4.959	5.748	6.060
.34	20.343	-47.511	-31.724	-13.145	-2.330	2.866	5.154	6.108	6.493
.35	22.153	-49.443	-34.250	-14.844	-3.122	2.707	5.351	6.488	6.960
.36	24.132	-51.470	-36.963	-16.720	-4.036	2.491	5.538	6.887	7.463
.37	26.296	-53.597	-39.879	-18.791	-5.064	2.207	5.709	7.305	8.006
.38	28.666	-55.829	-43.015	-21.076	-6.253	1.845	5.859	7.749	8.590
.39	31.265	-58.170	-46.390	-23.598	-7.613	1.389	5.989	8.191	9.218
.40	34.119	-60.628	-50.023	-26.362	-9.165	0.829	6.094	8.656	9.891
.41	37.255	-63.202	-53.937	-29.453	-10.934	0.136	6.101	9.131	10.613
.42	40.708	-65.902	-58.156	-32.844	-12.948	-0.709	6.078	9.612	11.384
.43	44.513	-68.732	-62.707	-36.587	-15.258	-1.707	5.982	10.093	12.206
.44	48.712	-71.695	-67.619	-40.721	-17.849	-2.912	5.795	10.567	13.080
.45	53.332	-74.799	-72.553	-45.287	-20.794	-4.316	5.497	11.025	14.007
.46	58.488	-78.058	-78.654	-50.332	-24.145	-6.016	5.063	11.453	14.984
.47	64.179	-81.423	-84.850	-55.908	-27.980	-8.020	4.486	11.842	16.009
.48	70.496	-84.953	-91.254	-62.073	-32.253	-10.419	3.772	12.169	17.080
.49	77.518	-88.628	-98.811	-68.898	-37.158	-13.196	2.942	12.414	18.189
.50	85.297	-92.446	-106.671	-76.449	-42.672	-16.459	1.928	12.559	19.328

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FISH BULLETIN NO. 116

TABLE

Z	J 17, 1	J 17, 2	J 17, 3	J 17, 4	J 17, 5	J 17, 6	J 17, 7	J 17, 8	J 17, 9
.51	94.056	-96.402	-115.189	-84.812	-48.942	-20.256	-0.325	12.543	20.484
.52	103.797	-100.489	-124.425	-94.079	-56.047	-24.669	-2.382	12.332	21.641
.53	114.696	-104.993	-134.445	-104.333	-61.968	-29.881	-4.919	11.909	22.777
.54	126.913	-109.004	-143.321	-115.750	-73.223	-35.917	-8.028	11.215	23.864
.55	140.633	-113.292	-157.131	-128.558	-84.658	-42.944	-11.815	10.135	24.864
.56	156.069	-117.829	-169.561	-142.454	-93.298	-51.110	-16.407	8.693	25.732
.57	173.468	-122.274	-181.903	-158.074	-108.005	-59.603	-21.353	6.913	26.496
.58	193.117	-126.675	-199.060	-175.447	-123.707	-71.632	-28.629	3.745	26.812
.59	215.353	-130.963	-215.538	-194.784	-140.833	-84.449	-36.943	0.115	26.855
.60	240.368	-135.052	-233.457	-216.921	-160.351	-99.912	-46.246	-4.534	26.418
.61	269.218	-138.830	-252.942	-240.324	-182.468	-116.580	-57.725	-10.438	25.352
.62	301.844	-142.158	-274.127	-267.094	-207.645	-136.631	-71.426	-17.870	23.475
.63	338.075	-144.859	-297.153	-296.070	-236.295	-159.016	-87.760	-27.069	20.559
.64	381.658	-146.712	-322.169	-330.334	-268.918	-186.962	-107.213	-38.794	16.322
.65	430.470	-147.439	-349.528	-367.016	-308.092	-218.385	-130.360	-52.985	10.416
.66	485.554	-146.694	-378.784	-409.239	-348.481	-254.999	-157.886	-70.576	2.410
.67	541.142	-144.943	-419.090	-455.928	-398.850	-297.378	-190.066	-92.182	-8.228
.68	625.702	-138.944	-443.191	-508.115	-452.084	-346.784	-229.486	-118.651	-22.155
.69	711.980	-130.723	-482.417	-566.546	-513.201	-404.291	-275.682	-151.904	-40.180
.70	812.062	-118.538	-522.472	-631.980	-587.379	-471.266	-339.565	-190.480	-63.304
.71	928.442	-101.341	-565.418	-705.294	-669.976	-549.314	-395.777	-238.580	-92.759
.72	1061.114	-77.823	-611.258	-787.421	-764.563	-640.325	-473.272	-297.121	-130.063
.73	1222.072	-46.301	-659.909	-879.422	-872.950	-746.324	-565.389	-368.096	-177.091
.74	1408.446	-4.918	-711.168	-982.459	-997.229	-870.528	-674.924	-454.810	-236.155
.75	1626.658	49.638	-764.664	-1097.805	-1139.810	-1015.425	-805.220	-559.872	-310.108
.76	1883.625	118.667	-819.804	-1226.839	-1303.473	-1184.851	-960.284	-687.457	-402.470
.77	2186.999	207.915	-873.690	-1371.043	-1491.416	-1383.927	-1144.915	-842.329	-517.588
.78	2546.071	321.712	-931.020	-1531.081	-1707.318	-1615.220	-1364.871	-1030.359	-660.834
.79	2972.138	466.218	-983.452	-1711.276	-1953.398	-1887.187	-1622.057	-1258.622	-838.843
.80	3478.969	649.140	-1031.935	-1910.966	-2240.486	-2206.036	-1939.765	-1635.781	-1059.820
.81	4083.373	880.121	-1071.484	-2131.431	-2568.096	-2580.063	-2312.954	-1872.384	-1333.913
.82	4801.904	1171.236	-1097.888	-2375.300	-2944.498	-3019.049	-2758.586	-2281.297	-1674.679
.83	5671.743	1587.620	-1104.822	-2643.306	-3375.738	-3534.313	-3291.011	-2778.220	-2094.666
.84	6711.785	1998.250	-1081.917	-2936.089	-3872.961	-4140.012	-3927.601	-3382.320	-2616.126
.85	7961.003	2376.939	-1024.027	-3253.517	-4441.931	-4831.483	-4680.043	-4117.009	-3261.914
.86	9473.129	3303.386	-910.517	-3594.302	-5063.662	-5687.634	-5600.338	-5010.888	-4061.598
.87	11302.770	4215.717	-734.174	-3955.492	-5836.932	-6670.389	-6601.437	-6008.911	-5051.835
.88	13518.000	5390.074	-439.865	-4331.757	-6689.549	-7825.382	-7998.575	-7423.804	-6278.087
.89	16208.763	6797.739	-24.812	-4714.458	-7657.883	-9182.513	-9694.867	-9037.707	-7796.730
.90	19483.835	8601.705	563.640	-5060.376	-8756.773	-10776.534	-11442.322	-11004.735	-9607.790
.91	23477.808	10866.703	1380.886	-5440.044	-9998.932	-12647.697	-13693.233	-13402.667	-12008.028
.92	28337.957	13711.310	2498.732	-5735.512	-11396.204	-14842.404	-16392.205	-16326.975	-14894.202
.93	34331.689	17284.975	4010.114	-5957.427	-12958.424	-17413.821	-19628.484	-19894.205	-18471.007
.94	41656.998	21776.112	6035.148	-5991.112	-14691.766	-20422.563	-23408.618	-24246.675	-22907.325
.95	50563.734	27422.372	8729.809	-5821.520	-16596.430	-23507.016	-28151.771	-29538.128	-28463.969
.96	61724.470	34523.615	12291.268	-5326.259	-18663.370	-28033.642	-33733.041	-36040.526	-35218.222
.97	75364.042	43438.228	16979.780	-4398.201	-20969.719	-32796.398	-40407.822	-49552.188	-43665.671
.98	92194.397	54703.629	23125.833	-2761.389	-23172.740	-38316.901	-48396.395	-63607.750	-54141.661
.99	112990.404	68863.881	31155.440	-258.867	-25501.133	-44691.715	-57949.065	-85389.949	-67129.368

FITTING A GEOMETRIC CURVE

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TABLE



Z	J 17, 10	J 17, 11	J 17, 12	J 17, 13	J 17, 14	J 17, 15	J 17, 16	J 17, 17
.01	1.041	1.041	1.041	1.041	1.041	1.041	1.041	1.041
.02	1.085	1.085	1.085	1.085	1.085	1.085	1.085	1.085
.03	1.132	1.132	1.132	1.132	1.132	1.132	1.132	1.132
.04	1.181	1.181	1.181	1.181	1.181	1.181	1.181	1.181
.05	1.234	1.234	1.234	1.234	1.234	1.234	1.234	1.234
.06	1.290	1.290	1.290	1.290	1.290	1.290	1.290	1.290
.07	1.350	1.350	1.350	1.350	1.350	1.350	1.350	1.350
.08	1.414	1.414	1.414	1.414	1.414	1.414	1.414	1.414
.09	1.482	1.482	1.482	1.482	1.482	1.482	1.482	1.482
.10	1.555	1.555	1.555	1.555	1.555	1.555	1.555	1.555
.11	1.633	1.633	1.633	1.633	1.633	1.633	1.633	1.633
.12	1.717	1.717	1.717	1.717	1.717	1.717	1.717	1.717
.13	1.806	1.806	1.806	1.806	1.806	1.806	1.806	1.806
.14	1.902	1.902	1.902	1.902	1.902	1.902	1.902	1.902
.15	2.005	2.005	2.005	2.005	2.005	2.005	2.005	2.005
.16	2.115	2.115	2.115	2.115	2.115	2.115	2.115	2.115
.17	2.234	2.234	2.234	2.234	2.234	2.234	2.234	2.234
.18	2.362	2.362	2.362	2.362	2.362	2.362	2.362	2.362
.19	2.500	2.500	2.500	2.500	2.500	2.500	2.500	2.500
.20	2.648	2.649	2.649	2.649	2.649	2.649	2.649	2.649
.21	2.809	2.809	2.810	2.810	2.810	2.810	2.810	2.810
.22	2.982	2.983	2.983	2.983	2.983	2.983	2.983	2.983
.23	3.169	3.171	3.171	3.171	3.171	3.171	3.171	3.171
.24	3.371	3.374	3.375	3.375	3.375	3.375	3.375	3.375
.25	3.591	3.594	3.596	3.596	3.596	3.596	3.596	3.596
.26	3.828	3.834	3.835	3.835	3.835	3.835	3.835	3.835
.27	4.086	4.094	4.096	4.097	4.097	4.097	4.097	4.097
.28	4.366	4.376	4.380	4.381	4.381	4.381	4.381	4.381
.29	4.670	4.684	4.689	4.690	4.691	4.691	4.691	4.691
.30	5.001	5.020	5.026	5.028	5.029	5.029	5.029	5.029
.31	5.361	5.386	5.395	5.398	5.399	5.399	5.400	5.400
.32	5.733	5.786	5.798	5.803	5.804	5.805	5.805	5.805
.33	6.119	6.224	6.240	6.246	6.248	6.249	6.249	6.249
.34	6.514	6.705	6.725	6.733	6.736	6.737	6.738	6.738
.35	7.151	7.227	7.257	7.268	7.273	7.274	7.275	7.275
.36	7.704	7.802	7.842	7.857	7.864	7.866	7.867	7.867
.37	8.307	8.433	8.485	8.507	8.516	8.519	8.521	8.521
.38	8.964	9.126	9.193	9.224	9.239	9.241	9.243	9.244
.39	9.682	9.888	9.978	10.017	10.034	10.041	10.044	10.045
.40	10.465	10.726	10.843	10.895	10.918	10.928	10.932	10.934
.41	11.318	11.648	11.800	11.869	11.900	11.914	11.920	11.923
.42	12.249	12.664	12.859	12.959	12.992	13.011	13.029	13.034
.43	13.264	13.782	14.033	14.153	14.209	14.236	14.248	14.254
.44	14.369	15.016	15.335	15.492	15.567	15.604	15.621	15.629
.45	15.571	16.375	16.782	16.982	17.086	17.133	17.159	17.171
.46	16.878	17.874	18.390	18.633	18.787	18.854	18.887	18.903
.47	18.297	19.528	20.178	20.519	20.694	20.785	20.831	20.854
.48	19.836	21.351	22.170	22.407	22.538	22.609	22.622	22.635
.49	21.501	23.561	24.589	24.949	25.231	25.413	25.499	25.544
.50	23.300	25.578	26.862	27.578	27.972	28.187	28.304	28.367

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TABLE

Z	J 17, 10	J 17, 11	J 17, 12	J 17, 13	J 17, 14	J 17, 15	J 17, 16	J 17, 17
.51	25.237	28.020	29.622	30.532	31.044	31.329	31.487	31.574
.52	27.317	30.709	32.701	33.806	34.518	34.895	35.108	35.227
.53	29.545	33.967	36.139	37.600	38.455	38.950	39.235	39.388
.54	31.914	36.919	39.978	41.822	42.921	43.371	43.652	44.174
.55	34.427	40.489	44.266	46.286	47.990	48.847	49.352	49.654
.56	37.072	44.402	49.055	51.968	53.771	54.877	55.351	55.658
.57	39.856	48.082	54.404	58.052	60.353	61.790	62.681	63.229
.58	42.693	52.353	60.376	64.986	67.864	69.726	70.901	71.637
.59	45.612	58.437	67.041	72.729	76.446	78.853	80.398	81.584
.60	48.543	63.950	74.474	81.568	86.266	89.069	91.396	92.712
.61	51.420	69.906	82.758	91.560	97.516	101.506	104.159	105.910
.62	54.156	76.307	91.981	102.901	110.418	115.540	119.003	121.327
.63	56.692	83.144	102.233	115.761	123.231	131.793	136.308	139.381
.64	58.995	90.393	113.610	130.345	142.256	150.647	156.510	160.576
.65	60.144	98.063	126.210	146.884	161.843	172.354	181.169	185.619
.66	60.720	105.896	140.128	165.637	184.366	198.647	207.864	214.947
.67	60.661	113.951	155.454	186.891	210.386	227.737	240.487	249.747
.68	57.851	121.991	172.264	210.907	240.358	262.432	278.863	291.002
.69	55.397	129.772	190.616	238.219	274.943	302.959	324.136	340.022
.70	46.160	136.950	210.353	269.031	314.873	350.388	377.047	398.406
.71	35.065	143.065	231.990	303.821	360.993	405.968	441.012	468.102
.72	19.183	147.495	254.895	343.034	414.278	471.178	516.181	551.489
.73	-2.943	149.415	279.034	387.136	475.850	547.776	605.313	651.479
.74	-35.080	147.736	304.139	436.601	546.999	637.851	711.859	771.640
.75	-73.435	141.027	329.634	491.897	629.201	743.884	838.075	916.352
.76	-126.874	127.422	354.769	553.454	724.140	868.822	990.151	1091.003
.77	-196.870	104.480	378.433	621.627	833.726	1016.168	1171.375	1302.225
.78	-287.861	69.981	399.059	696.642	960.114	1190.080	1388.351	1558.203
.79	-405.531	17.117	414.471	778.516	1105.718	1395.497	1649.141	1869.048
.80	-556.831	-56.065	421.089	866.948	1273.216	1638.280	1924.370	2247.273
.81	-750.646	-150.046	416.666	961.169	1465.541	1925.374	2336.385	2708.388
.82	-998.115	-298.752	393.955	1059.741	1685.855	2265.007	2793.818	3271.646
.83	-1313.248	-486.994	349.267	1169.276	1937.495	2666.910	3242.312	3960.985
.84	-1713.668	-738.167	283.901	1259.062	2223.873	3142.569	4005.309	4896.212
.85	-2221.547	-1070.729	133.996	1350.963	2548.313	3705.318	4897.398	5944.496
.86	-2864.777	-1508.338	-60.434	1426.740	2913.809	4371.654	5779.311	7122.259
.87	-3678.450	-2081.294	-241.745	1476.133	3222.638	5159.690	6988.261	8607.549
.88	-4708.728	-2828.379	-709.345	1482.760	3775.918	6091.078	8386.338	10443.072
.89	-6095.179	-3799.215	-1291.704	1424.323	4272.650	7191.309	10130.361	13050.003
.90	-7943.734	-5037.259	-2046.188	1270.293	4808.822	8483.293	12448.217	16032.884
.91	-9710.404	-6683.627	-3077.556	979.018	5375.797	10018.685	14827.768	19735.624
.92	-12315.948	-8781.975	-4462.545	494.032	5938.225	11817.038	17672.380	24339.309
.93	-15599.759	-11484.711	-6315.794	-269.714	6531.140	13926.948	21808.478	30072.632
.94	-19737.229	-14960.896	-8782.489	-1387.450	7055.982	16395.378	26492.826	37223.728
.95	-24949.052	-19436.335	-12031.238	-3022.894	7475.194	19273.299	32215.053	46156.791
.96	-31512.877	-25156.393	-16366.809	-6348.943	7704.879	22614.152	39209.553	57332.538
.97	-39777.475	-32592.251	-22046.512	-9608.910	7624.877	26412.392	47769.047	71353.292
.98	-50185.142	-41911.675	-29501.362	-13121.066	7065.449	30899.384	58236.765	88898.322
.99	-63280.610	-53955.264	-39263.246	-18312.823	5789.369	35938.297	71030.519	110964.151

FITTING A GEOMETRIC CURVE

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TABLE

Z	J 18, 1	J 18, 2	J 18, 3	J 18, 4	J 18, 5	J 18, 6	J 18, 7	J 18, 8	J 18, 9
.01	0.165	-16.469	0.691	1.036	1.041	1.041	1.041	1.041	1.041
.02	0.339	-16.936	0.364	1.063	1.054	1.053	1.053	1.053	1.053
.03	0.504	-17.462	0.017	1.081	1.130	1.132	1.132	1.132	1.132
.04	0.720	-17.989	-0.332	1.088	1.176	1.181	1.181	1.181	1.181
.05	0.959	-18.536	-0.742	1.086	1.224	1.233	1.234	1.234	1.234
.06	1.150	-19.106	-1.157	1.070	1.272	1.289	1.290	1.290	1.290
.07	1.386	-19.698	-1.597	1.041	1.321	1.347	1.350	1.350	1.350
.08	1.638	-20.316	-2.064	0.996	1.369	1.409	1.413	1.414	1.414
.09	1.906	-20.959	-2.561	0.936	1.417	1.473	1.481	1.482	1.482
.10	2.193	-21.628	-3.088	0.858	1.462	1.543	1.554	1.555	1.555
.11	2.499	-22.327	-3.649	0.761	1.505	1.616	1.631	1.633	1.633
.12	2.826	-23.055	-4.244	0.645	1.545	1.691	1.713	1.716	1.717
.13	3.177	-23.814	-4.878	0.501	1.580	1.769	1.800	1.805	1.806
.14	3.552	-24.606	-5.553	0.334	1.609	1.851	1.893	1.901	1.902
.15	3.955	-25.434	-6.271	0.140	1.632	1.935	1.992	2.003	2.005
.16	4.387	-26.297	-7.035	-0.085	1.645	2.021	2.067	2.112	2.115
.17	4.851	-27.199	-7.849	-0.343	1.649	2.110	2.209	2.229	2.233
.18	5.349	-28.142	-8.716	-0.637	1.641	2.200	2.327	2.355	2.361
.19	5.886	-29.127	-9.640	-0.971	1.619	2.291	2.453	2.490	2.498
.20	6.464	-30.157	-10.620	-1.349	1.581	2.382	2.585	2.634	2.646
.21	7.086	-31.235	-11.678	-1.774	1.524	2.472	2.724	2.789	2.805
.22	7.758	-32.362	-12.800	-2.250	1.444	2.560	2.871	2.955	2.976
.23	8.483	-33.542	-13.998	-2.784	1.340	2.644	3.026	3.132	3.161
.24	9.266	-34.778	-15.278	-3.381	1.207	2.723	3.187	3.292	3.361
.25	10.114	-36.072	-16.645	-4.045	1.040	2.796	3.356	3.526	3.576
.26	11.031	-37.427	-18.107	-4.785	0.856	2.859	3.531	3.743	3.808
.27	12.024	-38.848	-19.671	-5.607	0.589	2.910	3.712	3.975	4.059
.28	13.101	-40.337	-21.345	-6.519	0.294	2.947	3.898	4.223	4.331
.29	14.271	-41.898	-23.136	-7.531	-0.057	2.965	4.089	4.487	4.623
.30	15.541	-43.533	-25.055	-8.651	-0.471	2.960	4.283	4.768	4.940
.31	16.923	-45.253	-27.112	-9.880	-0.956	2.929	4.478	5.066	5.281
.32	18.427	-47.065	-29.318	-11.261	-1.521	2.864	4.673	5.382	5.650
.33	20.067	-48.946	-31.684	-12.776	-2.176	2.760	4.864	5.715	6.048
.34	21.855	-50.900	-34.223	-14.450	-2.934	2.610	5.049	6.067	6.477
.35	23.808	-53.013	-36.952	-16.299	-3.809	2.404	5.223	6.436	6.939
.36	25.944	-55.290	-39.884	-18.340	-4.813	2.134	5.383	6.822	7.437
.37	28.282	-57.845	-43.036	-20.594	-5.965	1.787	5.521	7.223	7.972
.38	30.844	-60.585	-46.428	-23.981	-7.284	1.351	5.632	7.639	8.546
.39	33.655	-63.434	-50.079	-28.528	-8.790	0.810	5.707	8.066	9.162
.40	36.743	-65.988	-54.012	-33.859	-10.509	0.147	5.736	8.502	9.821
.41	40.140	-67.872	-58.232	-39.806	-12.466	-0.657	5.708	8.942	10.524
.42	43.881	-70.792	-62.824	-45.962	-14.653	-1.677	5.608	9.380	11.272
.43	48.008	-73.854	-67.758	-53.084	-17.225	-2.788	5.420	9.809	12.066
.44	52.565	-77.063	-73.087	-61.494	-20.101	-4.171	5.124	10.221	12.906
.45	57.605	-80.419	-78.844	-69.477	-23.266	-5.813	4.698	10.603	13.789
.46	63.187	-83.931	-85.070	-78.087	-26.670	-7.732	4.115	10.941	14.713
.47	69.379	-87.600	-91.805	-87.081	-31.272	-10.008	3.337	11.219	15.673
.48	76.259	-91.437	-99.057	-97.824	-36.056	-12.724	2.331	11.433	16.663
.49	83.914	-95.414	-106.996	-109.280	-41.436	-15.873	1.051	11.498	17.674
.50	92.446	-99.556	-115.558	-123.558	-47.558	-19.559	-0.559	11.411	18.691

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FISH BULLETIN NO. 116

TABLE

Z	J 18, 1	J 18, 2	J 18, 3	J 18, 4	J 18, 5	J 18, 6	J 18, 7	J 18, 8	J 18, 9
.51	101.972	-103.851	-124.844	-92.722	-54.498	-23.864	-2.560	11.203	19.699
.52	112.626	-108.288	-134.921	-102.885	-62.366	-28.889	-5.028	10.724	20.675
.53	124.502	-112.855	-145.864	-114.103	-71.288	-34.744	-8.032	9.676	21.589
.54	137.960	-117.534	-157.752	-126.686	-81.406	-41.963	-11.737	8.838	22.403
.55	152.026	-122.299	-170.674	-140.491	-92.898	-50.698	-16.204	7.294	23.070
.56	167.003	-127.144	-184.725	-156.073	-105.916	-60.726	-21.602	5.178	23.539
.57	182.169	-131.954	-200.010	-173.290	-120.712	-72.102	-28.102	2.385	23.796
.58	210.853	-136.699	-216.644	-192.483	-137.521	-81.921	-35.909	-1.238	23.902
.59	235.436	-141.331	-234.749	-213.830	-156.628	-96.410	-45.295	-5.877	22.799
.60	263.365	-145.729	-254.459	-237.600	-178.360	-113.247	-56.459	-11.794	21.447
.61	295.169	-149.766	-275.915	-264.257	-203.095	-132.814	-69.830	-19.141	19.263
.62	331.465	-153.280	-299.272	-293.965	-231.266	-155.538	-85.783	-28.363	16.015
.63	372.986	-156.096	-324.688	-327.172	-263.574	-182.094	-104.799	-39.819	11.410
.64	420.597	-157.865	-352.334	-364.316	-299.969	-212.785	-127.450	-53.978	5.122
.65	475.324	-158.450	-382.381	-405.894	-341.867	-248.960	-154.416	-71.426	-5.714
.66	538.389	-157.113	-415.006	-452.465	-389.572	-290.236	-186.510	-92.861	-14.428
.67	611.247	-153.636	-455.379	-504.659	-444.186	-338.287	-224.697	-119.132	-28.888
.68	695.637	-147.273	-488.661	-563.188	-506.686	-393.382	-270.136	-151.267	-47.530
.69	793.644	-137.213	-529.963	-628.830	-578.268	-461.401	-324.206	-190.517	-71.345
.70	907.771	-122.436	-574.480	-702.040	-660.323	-538.469	-388.569	-238.207	-101.622
.71	1041.033	-101.664	-622.172	-785.261	-754.458	-628.605	-465.180	-296.731	-139.914
.72	1197.069	-73.292	-673.042	-878.127	-862.539	-733.776	-556.438	-367.823	-188.148
.73	1380.286	-45.303	-726.945	-982.575	-986.726	-856.961	-665.186	-454.343	-248.714
.74	1596.027	14.836	-783.376	-1099.395	-1129.524	-1001.232	-794.845	-539.645	-324.567
.75	1850.763	83.212	-842.405	-1230.586	-1293.828	-1170.340	-949.335	-607.788	-419.371
.76	2152.308	165.135	-902.597	-1377.643	-1482.960	-1368.732	-1134.210	-643.733	-537.668
.77	2510.860	274.356	-963.869	-1542.248	-1700.878	-1611.672	-1353.843	-653.345	-685.092
.78	2937.712	414.348	-1021.494	-1726.190	-1951.952	-1875.402	-1618.631	-624.642	-868.637
.79	3447.634	603.148	-1075.813	-1931.288	-2241.359	-2197.318	-1843.262	-546.107	-1096.995
.80	4058.553	820.916	-1125.283	-2169.513	-2574.919	-2576.384	-2312.222	-409.473	-1380.971
.81	4792.580	1110.499	-1155.991	-2411.891	-2959.405	-3022.382	-2765.180	-2307.195	-1734.008
.82	5677.042	1478.158	-1170.232	-2690.315	-3402.427	-3548.291	-3308.446	-2817.239	-2172.846
.83	6745.787	1944.005	-1156.037	-2995.534	-3915.604	-4168.181	-3960.559	-3459.764	-2718.342
.84	8040.821	2535.987	-1101.223	-3326.811	-4499.594	-4899.495	-4743.813	-4209.667	-3396.503
.85	9614.378	3284.907	-989.615	-3693.238	-5174.110	-5752.402	-5688.356	-5129.339	-4239.774
.86	11531.528	4234.367	-799.658	-4091.198	-5947.884	-6780.747	-6817.880	-6265.763	-5288.658
.87	13874.489	5437.365	-562.761	-4454.277	-6835.531	-7982.531	-8180.103	-7656.474	-6593.746
.88	16741.798	6963.488	-61.103	-4832.058	-7844.298	-9400.523	-9822.289	-9359.456	-8218.255
.89	20263.617	8898.392	373.258	-5238.279	-8969.609	-11072.928	-11799.621	-11446.109	-10241.218
.90	24598.456	11354.696	1475.025	-5689.119	-10294.287	-12944.993	-14185.474	-14004.295	-12761.660
.91	29946.613	14473.179	2715.753	-5869.211	-11737.522	-13365.039	-17054.609	-17142.242	-15802.602
.92	36560.198	18435.833	4420.625	-6028.598	-13391.085	-14894.347	-20316.740	-20993.102	-19819.294
.93	44756.716	23274.042	6733.869	-5996.829	-15196.921	-17128.311	-24898.726	-25720.695	-24705.035
.94	54956.620	29886.194	9822.372	-5675.826	-17187.583	-20031.195	-29718.269	-31326.408	-30801.884
.95	67965.707	38650.545	14031.811	-4939.347	-19281.249	-23443.808	-35775.050	-38637.671	-38121.665
.96	84045.421	49454.722	19696.058	-3574.654	-21494.694	-24537.826	-43063.531	-47418.174	-47916.116
.97	103139.000	61722.616	27912.467	-1356.458	-23745.479	-40423.332	-51835.013	-58180.132	-59785.697
.98	127837.785	78654.479	36822.232	2066.674	-25878.629	-47271.889	-62364.302	-71399.250	-74612.992
.99	158799.628	100276.958	49780.792	7156.744	-27747.579	-55082.309	-74996.347	-87632.394	-93136.979

FITTING A GROWTH CURVE

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TABLE

Z	J 18, 10	J 18, 11	J 18, 12	J 18, 13	J 18, 14	J 18, 15	J 18, 16	J 18, 17	J 18, 18
.01	1.041	1.041	1.041	1.041	1.041	1.041	1.041	1.041	1.041
.02	1.085	1.085	1.085	1.085	1.085	1.085	1.085	1.085	1.085
.03	1.132	1.132	1.132	1.132	1.132	1.132	1.132	1.132	1.132
.04	1.181	1.181	1.181	1.181	1.181	1.181	1.181	1.181	1.181
.05	1.234	1.234	1.234	1.234	1.234	1.234	1.234	1.234	1.234
.06	1.290	1.290	1.290	1.290	1.290	1.290	1.290	1.290	1.290
.07	1.350	1.350	1.350	1.350	1.350	1.350	1.350	1.350	1.350
.08	1.414	1.414	1.414	1.414	1.414	1.414	1.414	1.414	1.414
.09	1.482	1.482	1.482	1.482	1.482	1.482	1.482	1.482	1.482
.10	1.555	1.555	1.555	1.555	1.555	1.555	1.555	1.555	1.555
.11	1.633	1.633	1.633	1.633	1.633	1.633	1.633	1.633	1.633
.12	1.717	1.717	1.717	1.717	1.717	1.717	1.717	1.717	1.717
.13	1.806	1.806	1.806	1.806	1.806	1.806	1.806	1.806	1.806
.14	1.902	1.902	1.902	1.902	1.902	1.902	1.902	1.902	1.902
.15	2.005	2.005	2.005	2.005	2.005	2.005	2.005	2.005	2.005
.16	2.115	2.115	2.115	2.115	2.115	2.115	2.115	2.115	2.115
.17	2.234	2.234	2.234	2.234	2.234	2.234	2.234	2.234	2.234
.18	2.362	2.362	2.362	2.362	2.362	2.362	2.362	2.362	2.362
.19	2.500	2.500	2.500	2.500	2.500	2.500	2.500	2.500	2.500
.20	2.648	2.649	2.649	2.649	2.649	2.649	2.649	2.649	2.649
.21	2.809	2.809	2.810	2.810	2.810	2.810	2.810	2.810	2.810
.22	2.983	2.983	2.983	2.983	2.983	2.983	2.983	2.983	2.983
.23	3.169	3.171	3.171	3.171	3.171	3.171	3.171	3.171	3.171
.24	3.371	3.374	3.375	3.375	3.375	3.375	3.375	3.375	3.375
.25	3.590	3.594	3.596	3.596	3.596	3.596	3.596	3.596	3.596
.26	3.828	3.834	3.835	3.836	3.836	3.836	3.836	3.836	3.836
.27	4.085	4.093	4.096	4.097	4.097	4.097	4.097	4.097	4.097
.28	4.365	4.376	4.380	4.381	4.381	4.381	4.381	4.381	4.381
.29	4.669	4.684	4.690	4.690	4.691	4.691	4.691	4.691	4.691
.30	4.999	5.019	5.028	5.028	5.029	5.029	5.029	5.029	5.029
.31	5.358	5.385	5.395	5.398	5.399	5.399	5.400	5.400	5.400
.32	5.749	5.785	5.798	5.803	5.804	5.805	5.805	5.805	5.805
.33	6.175	6.222	6.240	6.246	6.248	6.249	6.249	6.249	6.249
.34	6.638	6.700	6.724	6.733	6.736	6.737	6.738	6.738	6.738
.35	7.143	7.224	7.265	7.288	7.297	7.297	7.297	7.297	7.297
.36	7.693	7.798	7.840	7.857	7.863	7.866	7.867	7.867	7.867
.37	8.292	8.427	8.483	8.506	8.515	8.519	8.520	8.521	8.521
.38	8.946	9.118	9.192	9.223	9.236	9.241	9.243	9.244	9.244
.39	9.657	9.877	9.974	10.015	10.033	10.040	10.044	10.045	10.046
.40	10.433	10.712	10.837	10.892	10.917	10.927	10.932	10.934	10.935
.41	11.277	11.629	11.791	11.865	11.898	11.913	11.920	11.922	11.924
.42	12.196	12.639	12.848	12.945	12.990	13.010	13.020	13.024	13.026
.43	13.196	13.750	14.019	14.145	14.206	14.234	14.247	14.253	14.256
.44	14.282	14.973	15.315	15.482	15.563	15.602	15.620	15.629	15.633
.45	15.460	16.320	16.755	16.972	17.080	17.132	17.158	17.171	17.177
.46	16.738	17.802	18.354	18.635	18.778	18.850	18.885	18.903	18.912
.47	18.119	19.455	20.181	20.494	20.683	20.779	20.828	20.855	20.868
.48	19.611	21.251	22.107	22.575	22.822	22.952	23.019	23.054	23.072
.49	21.217	23.207	24.306	24.905	25.259	25.462	25.494	25.543	25.568
.50	22.941	25.379	26.754	27.620	27.941	28.172	28.297	28.364	28.400

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TABLE

Z	J 18, 10	J 18, 11	J 18, 12	J 18, 13	J 18, 14	J 18, 15	J 18, 16	J 18, 17	J 18, 18
.61	24.790	27.763	29.480	30.455	31.003	31.308	31.477	31.670	31.621
.62	26.751	30.382	32.516	33.754	34.463	34.867	35.094	35.222	35.293
.63	28.854	33.251	35.899	37.465	38.380	38.911	39.217	39.392	39.491
.64	31.020	36.288	39.667	41.843	43.021	43.518	43.920	44.194	44.302
.65	33.316	39.815	43.863	46.351	47.863	48.773	49.317	49.641	49.831
.66	35.685	42.545	48.553	51.659	53.884	54.780	55.363	55.840	56.203
.67	38.105	47.594	53.733	57.648	60.117	61.659	62.616	63.205	63.565
.68	40.588	51.974	59.511	64.407	67.551	69.593	70.812	71.603	72.096
.69	42.924	56.091	65.929	72.039	76.032	78.617	80.278	81.337	82.010
.69	45.106	61.742	73.047	80.457	85.719	89.053	91.228	92.648	93.561
.61	47.255	67.114	80.627	90.390	96.794	101.080	105.239	105.873	107.090
.62	48.973	72.781	89.634	101.380	109.467	114.979	118.706	121.209	122.879
.63	50.184	78.693	99.228	113.787	123.981	131.047	135.994	139.229	141.470
.64	50.675	84.779	109.766	127.780	140.616	149.657	155.074	160.357	163.380
.65	50.168	90.917	121.295	143.270	150.663	171.241	179.442	185.224	189.275
.66	48.310	96.909	133.847	161.948	181.380	196.098	206.935	214.247	219.866
.67	44.659	102.680	147.430	181.344	206.702	225.456	239.205	249.209	256.442
.68	38.611	107.777	162.015	203.707	235.541	259.393	277.152	290.276	299.043
.69	29.464	111.841	177.527	228.954	268.650	298.946	321.856	339.047	351.863
.70	19.281	114.327	193.818	257.993	308.555	345.995	374.610	397.096	414.113
.71	-2.111	114.509	210.642	288.362	350.265	398.988	436.970	466.342	488.905
.72	-27.165	111.434	227.621	323.967	400.276	461.978	510.805	549.128	579.002
.73	-69.830	103.859	244.199	361.341	457.676	535.454	598.394	648.313	687.821
.74	-103.447	90.123	259.575	403.271	525.148	621.879	702.356	767.397	819.588
.75	-163.979	68.129	272.624	448.813	608.066	722.839	826.044	910.667	979.548
.76	-240.228	51.097	281.780	497.790	698.483	841.089	973.362	1083.284	1174.217
.77	-338.971	-12.543	284.941	549.528	780.613	979.610	1149.055	1292.016	1411.711
.78	-466.238	-79.423	273.187	603.382	860.690	1141.969	1338.848	1544.518	1702.154
.79	-629.646	-171.320	260.633	667.630	1014.917	1331.885	1609.649	1850.698	2058.201
.80	-828.822	-296.970	254.059	740.953	1154.364	1554.991	1909.798	2222.654	2495.700
.81	-1105.930	-464.511	162.505	727.437	1309.841	1814.400	2290.354	2675.339	3034.538
.82	-1446.360	-688.181	66.721	794.960	1481.694	2118.234	2709.457	3227.248	3699.710
.83	-1879.338	-984.111	-75.553	845.792	1669.350	2472.661	3217.741	3861.291	4522.698
.84	-2439.112	-1373.690	-280.519	810.358	1871.761	2885.194	3838.838	4725.879	5543.218
.85	-3139.237	-1884.034	-569.552	765.408	2085.126	3364.139	4584.965	5736.282	6811.473
.86	-4016.383	-2550.737	-970.861	692.968	2303.790	3918.947	5481.629	6976.277	8391.027
.87	-5141.561	-3419.139	-1521.284	477.284	2518.305	4556.969	6550.387	8500.536	10362.505
.88	-6526.159	-4547.737	-2296.627	176.231	2713.013	5288.971	7854.865	10376.780	12828.349
.89	-8276.533	-6011.825	-3279.639	-289.424	2868.988	6122.411	9411.726	12989.670	16018.944
.90	-10965.682	-7908.978	-4604.981	-678.713	2951.119	7063.528	11291.889	15544.645	19930.497
.91	-13573.887	-10562.172	-6445.260	-1076.101	2914.173	8113.561	13526.812	19073.316	24685.239
.92	-17256.296	-13523.889	-8833.583	-1593.601	2692.429	9269.038	16218.839	23459.977	30844.576
.93	-21924.231	-17690.281	-12048.936	-2381.199	2195.388	10515.275	19442.555	28849.855	38079.133
.94	-27842.107	-23217.015	-16275.693	-3139.332	1287.959	11821.978	23295.979	35559.241	48475.748
.95	-35345.880	-29739.257	-21805.068	-4193.601	-262.366	13156.611	27891.517	43888.590	60999.068
.96	-44869.768	-38656.998	-29207.079	-5620.324	-1489.995	14869.995	33566.250	54258.170	75833.793
.97	-56928.402	-49874.659	-38878.798	-74183.695	-6021.201	15387.414	39881.029	67108.303	97027.188
.98	-72254.760	-64536.961	-51853.315	-103750.980	-11151.300	16681.521	47468.223	83121.988	122769.357
.99	-91650.486	-83312.189	-68259.271	-146626.808	-18548.047	16846.071	56426.383	103965.729	150638.817

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TABLE 18A-18B V. 01/11/11

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TABLE