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# 1 Ohm's Law for Ion Conduction in Lithium and 2 Beyond-Lithium Battery Electrolytes

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## 1ABSTRACT

2 The viability of next generation lithium and beyond-lithium battery  
3 technologies hinges on the development of electrolytes with improved  
4 performance. Comparing electrolytes is not straightforward, as multiple  
5 electrochemical parameters affect the performance of an electrolyte.  
6 Additional complications arise due to the formation of concentration  
7 gradients in response to dc potentials. We propose a modified version of  
8 Ohm's law to analyze current through binary electrolytes driven by a small  
9 dc potential. We show that the proportionality constant in Ohm's law is given  
10 by the product of the ionic conductivity,  $\kappa$ , and the ratio of currents in the  
11 presence ( $i_{ss}$ ) and absence ( $i_{\Omega}$ ) of concentration gradients,  $\rho_{+i}$ . The  
12 importance of  $\rho_{+i}$  was recognized by J. Evans, C.A. Vincent, and P.G. Bruce  
13 [*Polymer* 28, 2324 (1987)]. The product  $\kappa\rho_{+i}$  is used to rank order a  
14 collection of electrolytes. Ideally, both  $\kappa$  and  $\rho_{+i}$  should be maximized, but  
15 we observe a trade-off between these two parameters, resulting in an upper  
16 bound. This trade-off is analogous to the famous Robeson upper bound for  
17 permeability and selectivity in gas separation membranes. Designing  
18 polymer electrolytes that overcome this trade-off is a worthwhile but  
19 ambitious goal.

20

# 1MAIN TEXT

## 2 I. INTRODUCTION

3 In a battery, the passage of ionic current between the cathode and  
4anode is enabled by the electrolyte. The dependence of the current on the  
5potential drop between the electrodes is at the core of battery design and  
6engineering.<sup>1,2</sup> The kind of device that can be powered by a battery is limited  
7by the maximum current that can be passed safely through the electrolyte.

8 The starting point for understanding the relationship between potential  
9drop and current is Ohm's law. For a simple conductor with one charge  
10carrier, such as a copper wire (Fig. 1a), the current density,  $i$ , is proportional  
11to the potential drop per unit length,  $\Delta V/L$ , and Ohm's law can be written as:

$$i = \sigma \frac{\Delta V}{L}, \quad (1)$$

12

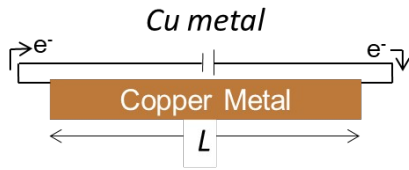
13where  $\sigma$  is the electronic conductivity of the material. All materials are  
14electrically neutral and have at least two charge carriers; the one charge  
15carrier approximation is valid because the compensating copper cations are  
16essentially immobile. Current density versus  $\Delta V/L$  for copper is presented in  
17Fig. 1b, where the slope,  $m$ , is given by  $5.8 \times 10^5 \text{ S cm}^{-1}$ .<sup>3</sup> In this case,  $m = \sigma$ .  
18For a copper wire, carrier concentration gradients do not develop as the  
19copper cations are stationary and charge neutrality is maintained.

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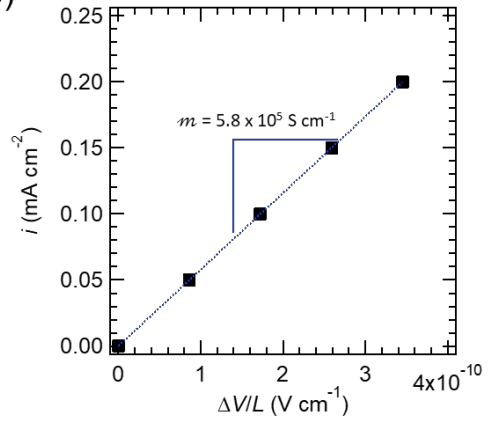
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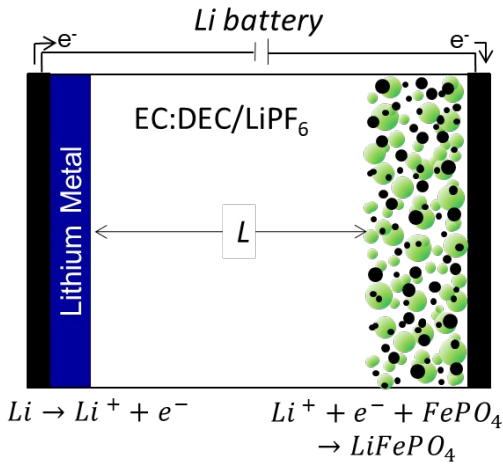
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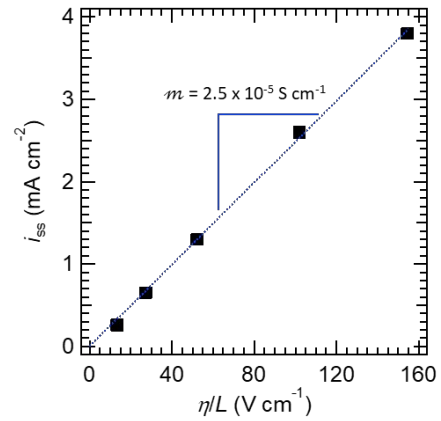
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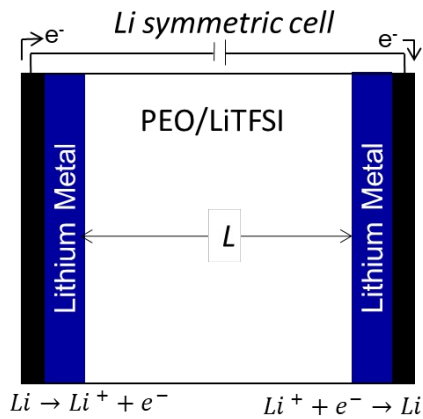
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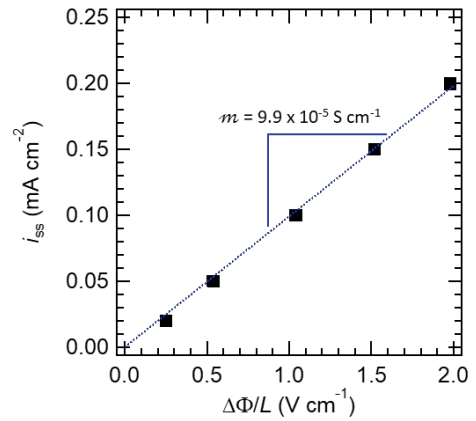
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(e)



(f)



3

**1Figure 1.** Empirical relationship between current density and normalized potential  
2drop across three types of cells. a) Schematic of a piece of copper metal, which is  
3an electronic conductor. b) Current density,  $i$ , as a function of normalized voltage  
4drop,  $V/L$ , for the copper metal depicted in Fig 1a. Adapted from Ref.3. c)  
5Schematic of a battery with a lithium metal anode, a lithium iron phosphate  
6cathode, and an EC:DEC/LiPF<sub>6</sub> electrolyte. d) Steady-state current density,  $i_{ss}$ , as a  
7function of normalized overpotential,  $\eta/L$ , for the battery depicted in Fig. 1c. Adapted  
8from Ref.4. e) Schematic of a lithium symmetric cell containing a PEO/LiTFSI  
9electrolyte. f) Steady-state current density,  $i_{ss}$ , as a function of normalized voltage  
10drop over the electrolyte,  $\Phi/L$ , in the cell depicted in Fig. 1e. Adapted from Ref.5.  
11The difference between values of  $m$  obtained in electronic and ionic conductors is  
12ten orders of magnitude.

13 An example of a rechargeable battery is shown schematically in Fig.  
141c. It consists of a lithium metal anode and a lithium iron phosphate, LiFePO<sub>4</sub>,  
15cathode separated by an EC:DEC/LiPF<sub>6</sub> electrolyte in a porous separator.  
16During discharge, the passage of ionic current through the electrolyte from  
17the anode to the cathode is driven by an overpotential,  $\eta$ , which is the  
18equilibrium potential of the cell minus the operating voltage,  $U^0 - V$ .<sup>1</sup> When  
19an overpotential is present, concentration gradients develop across the  
20electrolyte because both cations (in this case, Li<sup>+</sup>) and anions (PF<sub>6</sub><sup>-</sup>) are  
21mobile in the system. Under a constant overpotential, this would result in a  
22time-dependent current density until the concentration gradient reaches  
23steady-state. Only Li<sup>+</sup> ions are transported across electrode/electrolyte

1 interfaces; this also affects the nature of the gradients. In Fig. 1d, we plot the  
2 steady-state current density,  $i_{ss}$ , as a function of the overpotential per unit  
3 length,  $\eta/L$ , for the cell depicted in Fig. 1c.<sup>4</sup> It appears that the relationship  
4 between  $i_{ss}$  and  $\eta/L$  is approximately linear, similar to the copper wire.  
5 However, the slope,  $m = 2.5 \times 10^{-5} \text{ S cm}^{-1}$ , is not equal to the conductivity of  
6 the electrolyte. It reflects numerous processes that include charge transfer  
7 between the electrodes and the electrolyte, diffusion of lithium in the  
8 cathode, and diffusion and migration of ions in the electrolyte. Thus, the  
9 relationship between  $i_{ss}$  and  $\eta/L$  in Fig. 1d, although it appears linear, is not a  
10 manifestation of Ohm's law.

11 In Fig. 1e, a schematic for a symmetric cell consisting of an electrolyte  
12 sandwiched between two identical non-blocking electrodes is presented. In  
13 this perspective, we focus on symmetric cells comprising either lithium or  
14 sodium foil electrodes and electrolytes containing a lithium or sodium salt,  
15 respectively. This cell, popularized by pioneering work of Evans, Vincent, and  
16 Bruce, and others,<sup>6-8</sup> is similar to that shown in Fig. 1c with one crucial  
17 difference:  $U^0 = 0V$ . This cell enables a fair comparison of the ion transport  
18 properties of different electrolytes: the symmetry of the cell allows electrode  
19 effects to be deconvoluted from the properties of the electrolyte. In Fig. 1f,  
20 we plot  $i_{ss}$  as a function of the potential drop across the electrolyte,  $\Delta\Phi/L$ , for  
21 a cell with lithium foil electrodes and an electrolyte comprising poly(ethylene  
22 oxide) (PEO) and bis(trifluoromethylsulfonyl)amine lithium salt (LiTFSI).<sup>5</sup>

1 Here, the slope  $m = 9.9 \times 10^{-5} \text{ S cm}^{-1}$  is not equal to the ionic conductivity of  
2 the electrolyte. However, unlike in a full battery,  $m$  is related to the  
3 properties of the electrolyte alone. In our effort to design high performance  
4 electrolytes, it is the slope in Fig. 1f which we wish to maximize. Many  
5 publications, however, disregard this. It is fairly common, these days, to  
6 invent a new electrolyte, measure the ionic conductivity, and declare victory  
7 if it is greater than that of a baseline electrolyte.

8       The purpose of this perspective is to analyze symmetric cell data  
9 obtained from different electrolytes. Evans, Bruce, and Vincent<sup>6,9</sup> and  
10 Watanabe et al.,<sup>10</sup> modeled symmetric cells containing dilute and ideal  
11 electrolytic solutions. In later studies, Newman and coworkers<sup>1,11</sup> considered  
12 symmetric cells containing concentrated electrolytic solutions and developed  
13 the relationships between  $m$  and intrinsic transport and thermodynamic  
14 properties of the electrolyte. This perspective is focused on small applied  
15 potentials wherein the concentration dependence of the relevant electrolyte  
16 properties can be neglected. Based on the work in Refs.5–11, we develop a  
17 framework for measuring the Ohm's law coefficient which allows us to  
18 produce a rank ordered list of electrolytes based on their ability to maximize  
19 the flux of lithium or sodium cations. We conclude by discussing the  
20 limitations of our approach as, ultimately, the rank ordering of electrolytes  
21 needs to be reassessed in the presence of significant concentration gradients  
22 for practical devices.

23



## 1 II. THEORY

2 Electrolytes of interest comprise a salt  $z_1z_2$  dissolved in a matrix.  
3 Characterization of ion transport typically begins with measurement of the  
4 ionic conductivity,  $\kappa$ , by ac impedance spectroscopy. A powerful feature of ac  
5 impedance spectroscopy is that  $\kappa$  is measured without introducing significant  
6 concentration gradients. When a dc potential,  $\Delta\Phi$ , is applied across an  
7 electrolyte of dimension  $L$  in a symmetric cell (Fig. 1e), there are, by  
8 definition, no concentration gradients at the first instant of polarization ( $t =$   
9  $0^+$ ). The initial current density,  $i_0$ , at  $t = 0^+$  is given by:

$$10 \quad i_0 = \kappa \frac{\Delta\Phi}{L}. \quad \text{With time, i.e. at } t > 0, \text{ salt concentration gradients develop in the}$$

(2)

11 cell and eventually the gradient becomes time-invariant. The measured  
12 current density decreases with time as these concentration gradients  
13 develop and reaches a steady value at long times. We refer to the current  
14 obtained at long times as  $i_{ss}$ .

15 In the limit of small applied potentials, an expression for  $i_{ss}$  can be  
16 derived based on concentrated solution theory,<sup>11,12</sup>

$$17 \quad i_{ss} = \frac{\kappa}{1+Ne} \frac{\Delta\Phi}{L},$$

(3)

18 where  $Ne$  is a dimensionless parameter that we call the Newman number.  $Ne$   
19 is given by

1  $Ne = a\kappa RT$  where  $R$  is the gas constant,  $T$  is the temperature,  $F$  is Faraday  
 2 constant,  $D$  is the restricted diffusion coefficient of the salt,  $c$  is the salt  
 3 concentration,  $t_{+}^{0}$  is the transference number of the cation with respect to  
 4 the velocity of the solvent,  $\gamma_{\pm}$  is the mean molal activity coefficient of the  
 5 electrolyte, and  $m$  is the salt molality. The parameter  $a$  is related to the  
 6 stoichiometry of the salt:

$$7 a = \frac{\nu}{z_{+} z_{-}}$$

8 where  $\nu$  is the total number of cations and anions to which the salt  
 9 dissociates,  $\nu_{+}$  is the total number of cations to which the salt dissociates,  
 10 and  $z_{+}$  is the charge number of the cation. (For a binary salt,  $a = 2$ .)  
 11 Equations 3 and 4 are based on Newman's concentrated solution theory  
 12 wherein electrolytes are characterized by three transport parameters,  $\kappa$ ,  $D$ ,

13 and  $t_{+}^{0}$ , and a thermodynamic factor,  $T_f = 1 + \frac{d \ln \gamma_{\pm}}{d \ln m}$ . This theory builds on the

14 work of Onsager<sup>13</sup> who recognized that ion transport in binary electrolytes is  
 15 governed by three Stefan-Maxwell diffusion coefficients,  $D_{0-}$ ,  $D_{0+}$  and  $D_{\pm}$ .  
 16 Relationships between  $\kappa$ ,  $D$ , and  $t_{+}^{0}$ , and the Stefan-Maxwell diffusion  
 17 coefficients are given in Ref. 11.

18 While all four parameters ( $\kappa$ ,  $D$ ,  $t_{+}^{0}$ , and  $T_f$ ) dictate the time-  
 19 dependent current at a given applied potential, explicit knowledge of all

1 these parameters is not required to determine  $i_{ss}$  or  $Ne$ . In fact,  $Ne$  can be  
 2 determined in a single experiment by measuring  $i_0$  and  $i_{ss}$  at constant dc  
 3 polarization,  $\Delta\Phi$ , over the electrolyte:

$$4 \frac{i_{ss}}{i_0} = \frac{1}{1+Ne} \quad (6)$$

5 Bruce and Vincent pioneered the measurement of  $i_{ss}/i_0$ .<sup>6,9</sup>

6 Equations 6 and 4 can be recast as:

$$7 \frac{i_{ss}}{i_0} = \beta + \frac{t_{+i^0}}{\beta+1} \quad (7)$$

8 where

$$9 \beta = \nu \frac{D_{0+i}}{D_{\pm i} \frac{c}{c_0}} \quad (8)$$

10 and  $c_0$  is the solvent concentration. Equations 7 and 8 were first derived by  
 11 Balsara and Newman.<sup>11</sup> Only in the limit  $c \rightarrow 0$ ,  $\beta \rightarrow 0$  does

$$12 \frac{i_{ss}}{i_0} = t_{+i^0} \quad (9)$$

13 a result presented by Bruce and Vincent.<sup>9</sup> Determining the range of  
 14 concentration over which  $\beta$  is small enough such that Eq. 9 is valid requires  
 15 knowledge of the Stefan-Maxwell diffusion coefficients. For dilute 0.01 M  
 16 aqueous potassium chloride (Fig. 14.1 of Ref.1),  $D_{\pm i} = 1.1 \times 10^{-7} \text{ cm}^2 \text{ s}^{-1}$ ,  $D_{0+i}$

1 =  $1.9 \times 10^{-5} \text{ cm}^2 \text{ s}^{-1}$ ,  $c_0 = 56 \text{ mol L}^{-1}$ ,  $\beta = 0.031$  and Eq. 9 is a good approximation. However, most practical electrolytes are not dilute. For a 1 M aqueous potassium chloride solution,  $D_{\pm} = 1.9 \times 10^{-6} \text{ cm}^2 \text{ s}^{-1}$ ,  $D_{0+} = 2.0 \times 10^{-4}$ ,  $c_0 = 53.6 \text{ mol L}^{-1}$ , and  $\beta = 0.20$ . For 2.6 M PEO/LiTFSI (Fig. 3 and 4 of Ref.14),  $D_{\pm} = 4.0 \times 10^{-9} \text{ cm}^2 \text{ s}^{-1}$ ,  $D_{0+} = 1.1 \times 10^{-8} \text{ cm}^2 \text{ s}^{-1}$ ,  $c_0 = 16 \text{ mol L}^{-1}$ , and  $\beta = 0.44$ . Equation 9 is not a good approximation for either 1M KCl or 2.6 M PEO/LiTFSI.

8 We thus define the current ratio,  $\rho_{+}$ , which can be rewritten on the basis of Eq. 6 as

$$10 \rho_{+} = \frac{i_{ss}}{i_0} = \frac{1}{1 + Ne^+} \quad (10)$$

11 The current ratio is an intrinsic property of an electrolyte, irrespective of whether it is dilute or concentrated. The transference number,  $t_{+}$ , is defined as the fraction of current carried by the cation in a solution of uniform salt concentration and is only approximated by  $\rho_{+}$  when  $\beta$  is small.

14 For this reason, we prefer to use  $\rho_{+}$  to refer to the current ratio,  $\frac{i_{ss}}{i_0}$ , rather than using  $t_{+}$  or “the transference number” as is commonly done in the literature. This point was alluded to by Bruce and Gray in 1995, who referred to this current ratio as “the limiting current fraction”.<sup>15</sup>

18 The discussion thus far ignores the resistance of the electrode/electrolyte interface. In practice, when a dc voltage,  $\Delta V$ , is supplied to a symmetric cell, the potential drop across the electrolyte,  $\Delta\Phi$ ,

1 will be reduced by an amount equal to the product of the interfacial  
 2 resistance and the current. Assuming other sources of ohmic loss are  
 3 negligible,

$$4 \quad \Delta\Phi = \Delta V - iR_i A \quad (11)$$

where  $R_i$  is the interfacial impedance that is readily measured

5 by ac impedance spectroscopy,  $A$  is the electrochemically active surface  
 6 area of the electrode, and  $i$  is the current density through the symmetric cell.

7 We can combine Eq. 2, 3, 10 and 11 to obtain a useful expression

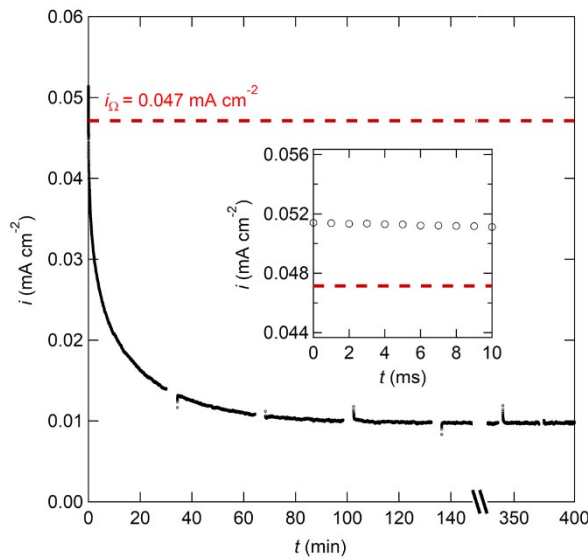
$$8 \quad \rho_{+,0} = \frac{i_{ss} (\Delta V - i_0 R_{i,0} A)}{i_0 (\Delta V - i_{ss} R_{i,ss} A)} \quad (12)$$

where  $i_{ss}$  and  $i_0$  refer to steady-state and initial current

9 density through a symmetric cell as in Eq. 11. The importance of corrections  
 10 for interfacial resistance was recognized by Evans, Bruce and Vincent<sup>6</sup> and  
 11 Watanabe et al.<sup>10</sup> We use the term  $\rho_{+,0}$  in Eq. 12 to clarify that this current  
 12 ratio is based on a measured value of  $i_0$ , which we discuss next.

13 In order to apply Eq. 10-12, the value of  $i_0$  must be measured. A practical  
 14 approach is to take the first data point measured after the potential is  
 15 applied. However, this method is inherently problematic because the current  
 16 is a strong function of time in the first instant of polarization. An example of  
 17 such a measurement is shown in Fig. 2. A small potential,  $\Delta V = 8.9$  mV, was  
 18 applied across a lithium symmetric cell ( $A = 0.079$  cm<sup>2</sup> and  $L = 0.050$  cm)  
 19 containing a 35 kg mol<sup>-1</sup> PEO/LiTFSI electrolyte with salt concentration  $r =$   
 200.010, where  $r$  is defined as the molar ratio of lithium ions to ethylene oxide

1moieties. A sampling rate of  $1 \text{ ms}^{-1}$  was used for the first few seconds. Figure  
 22 presents the current response over the entire time window (400 min)  
 3required to reach steady-state and the inset highlights the first 10 ms. Over  
 4the first 10 ms, the current is approximately constant with time. Thus, we  
 5have confidence that the current density we measure,  $i_0 = 0.051 \text{ mA cm}^{-2}$ ,  
 6truly captures the initial current.



7

8**Figure 2.** A plot of current density versus time in a lithium symmetric cell

9containing a PEO/LiTFSI electrolyte with  $r = 0.010$  after applying a potential of

10 $\Delta V = 8.9 \text{ mV}$  across the  $L = 0.050 \text{ cm}$  electrolyte. The current response over the

11entire time window (400 min) required to reach a steady-state is presented as a

12function of time. (The breaks in the curve are due to ac impedance measurements.)

13The inset highlights the first 10 ms, when the current is approximately constant with

14time. The dashed red line represents the value of  $i_{\Omega} = 0.047 \text{ mA cm}^{-2}$  calculated

15from Eq. 14. The high sampling frequency at early times provides confidence that

1the measured initial current density is accurate. In this case, the first measurement  
2of current density ( $i_0 = 0.051 \text{ mA cm}^{-2}$ ) is in reasonable agreement with  $i_\Omega$ .

3 An alternative that has been proposed<sup>6,16-23</sup> is to calculate  $i_0$  by combining  
4Eq. 2 and 11. In this case,

$$5 i_0 = \kappa \frac{(\Delta V - i_0 R_i A)}{L}. \quad (13)$$

6We can rearrange Eq. 13 to solve for  $i_0$ . We refer to this calculated current  
7density as  $i_\Omega$  because it is a statement of Ohm's law (Eq. 1):

$$8 i_\Omega = \frac{\Delta V}{L/\kappa + R_i A}. \quad (14)$$

9For the electrolyte and cell used in Fig. 2,  $\kappa = 0.33 \text{ mS cm}^{-1}$  and  $R_i = 495 \Omega$ ,  
10yielding  $i_\Omega = 0.047 \text{ mA cm}^{-2}$  (shown as a red dashed line in Fig. 2). We see  
11reasonable agreement between  $i_0$  and  $i_\Omega$  from this experiment. The  
12advantage of using  $i_\Omega$  instead of  $i_0$  is that it is based on parameters that are  
13easily measured ( $\Delta V$ ,  $L$ ,  $R_i$ ,  $\kappa$ , and  $A$ ). Further rationale for this is discussed  
14in Section IV. For the purposes of this paper, we define  $\rho_{+i}$  as:

$$15 \rho_{+i} = \frac{i_{ss} (\Delta V - i_\Omega R_{i,0} A)}{i_\Omega (\Delta V - i_{ss} R_{i,ss} A)}. \quad (15)$$

1Eq. 15 differs from Eq. 12 only in the use of  $i_{\Omega}$  for  $i_0$ . In the discussion below,  
 2electrolytes are characterized by two transport properties,  $\kappa$  and  $\rho_{+i}$ . We use  
 3Eq. 15 to calculate  $\rho_{+i}$ .

#### 4 III. DATA

5 To select the systems used in this perspective, we studied the 472 papers  
 6which cited Evans, Vincent, and Bruce’s 1987 paper titled “Electrochemical  
 7measurement of transference numbers in polymer electrolytes”<sup>6</sup> since 2010.  
 8Only a small fraction of these papers reported all parameters necessary for  
 9our analysis. These parameters are listed in Table I.

10**Table I.** List of parameters related to the Evans, Vincent, and Bruce measurement  
 11of  $i_{ss}/i_0$  gathered for the electrolyte systems described in this study. We also list  
 12their symbols and descriptions.

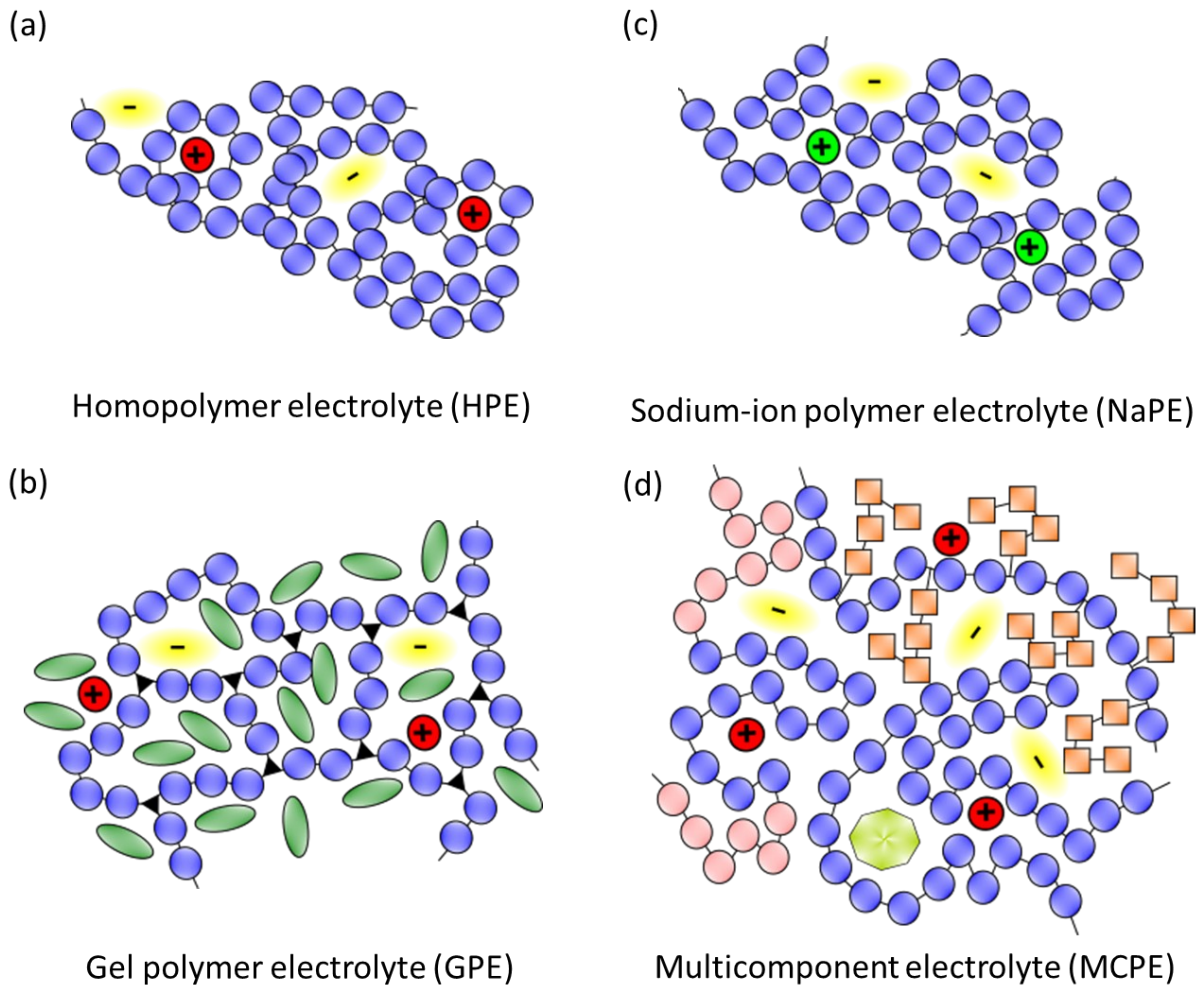
| Parameter                        | Symbol     | Description   |
|----------------------------------|------------|---|
| ionic conductivity, blocking     | $K_b$      | ionic conductivity of the electrolyte measured by ac impedance using blocking electrodes (e.g. stainless steel) |
| ionic conductivity, non-blocking | $K_{nb}$   | ionic conductivity measured by ac impedance using non-blocking electrodes (e.g. lithium metal)                  |
| applied voltage                  | $\Delta V$ | constant voltage applied by the potentiostat in order to elicit a steady-state current density                  |
| current density, initial         | $i_0$      | initial current density measured after polarization at $\Delta V$   |
| current density, steady-state    | $i_{ss}$   | current density measured at steady-state in response to $\Delta V$  |
| interfacial resistance, initial  | $R_{i,0}$  | interfacial resistance measured by ac impedance spectroscopy just before $\Delta V$ is applied                  |



|                                      |            |  |
|--------------------------------------|------------|--|
| interfacial resistance, steady-state | $R_{i,ss}$ | interfacial resistance measured by ac impedance spectroscopy after the steady-state current is reached |
| bulk resistance                      | $R_b$      | bulk resistance measured in the cell during the steady-state current experiment                        |
| cell thickness                       | $L$        | distance between electrodes; electrolyte thickness   |
| interfacial area                     | $A$        | nominal electrode area in contact with the electrolyte   |

1

2        The four categories of electrolytes covered in this study are pictured in  
3 Fig. 3: homopolymer electrolytes containing a lithium salt and no solvent  
4 (HPE), gel polymer electrolytes containing a crosslinked polymer mixed with  
5 a solvent and a lithium salt (GPE), polymer electrolytes containing a sodium  
6 salt (NaPE), and multicomponent polymer electrolytes containing a polymer  
7 mixed with a salt and at least one additional component (MCPE). The  
8 additional component in the MCPEs may be another polymer (blended or  
9 covalently bonded), an ionic liquid, or a ceramic particle. All of the  
10 electrolytes were designed to transport lithium ions except for those placed  
11 in the sodium electrolyte category. A long-form description of each  
12 electrolyte, its category, and its reference is provided in Table II.



1

**2Figure 3.** Schematics of the four categories of electrolytes analyzed in this  
 3perspective. (a) Simple homopolymer electrolytes containing a lithium salt (HPE).  
 4Blue spheres represent monomer beads on a polymer chain, red spheres indicate  
 5lithium cations, and yellow ovals represent the negative counterion. (b) Gel or  
 6crosslinked polymer electrolytes (GPE). Black triangles represent crosslinks in a  
 7polymer network and green ovals represent solvent molecules. (c) Polymer  
 8electrolytes containing a sodium salt (NaPE). Green spheres represent sodium  
 9cations. (d) Multicomponent polymer electrolytes (MCPE). The schematic depicts  
 10several types of MCPEs. Pink spheres represent a second monomer type on a  
 11copolymer chain, orange cubes represent ionic liquid side chains grafted to a

1polymer chain, and the green octagon represents a nanoparticle dispersed in the  
2polymer.

3

4**Table II.** Long-form descriptions of the electrolyte systems analyzed in this  
5perspective and their categories: HPE - homopolymer electrolyte, GPE - gel polymer  
6electrolyte, MCPE - multicomponent polymer electrolyte, NaPE - sodium ion polymer  
7electrolyte.

| <b>Electrolyte description</b>   | <b>Category</b> | <b>Ref</b> |
|--|-----------------|------------|
| polyethylene oxide with bis(trifluoromethylsulfonyl)amine lithium salt (PEO/LiTFSI) with 0.017 moles of LiTFSI per mole of ether oxygen ( $r = 0.017$ )  | HPE             | 21         |
| PEO/LiTFSI with $r = 0.08$   | HPE             | 17         |
| poly(diethylene oxid-alt-oxymethylene) with LiTFSI (P(2EO-MO)/LiTFSI) with 0.04 moles of LiTFSI per mole of oxygen ( $r = 0.04$ )                        | HPE             | 18         |
| P(2EO-MO)/LiTFSI with $r = 0.08$   | HPE             | 18         |
| P(2EO-MO)/LiTFSI with $r = 0.14$   | HPE             | 18         |
| perfluoroether containing 8 carbon atoms with dimethyl carbonate end groups and bis(fluorosulfonyl)imide lithium salt (C8-DMC/LiFSI) with 5.84 wt% LiFSI | HPE             | 22         |
| C8-DMC/LiFSI with 19.9 wt% LiFSI   | HPE             | 22         |
| perfluoropolyether with hydroxyl end groups containing 10 fluoro-ether oxygens (PFPE <sub>D10</sub> -Diol) and 9.1 wt% LiTFSI                            | HPE             | 23         |
| perfluoropolyether with dimethyl carbonate end groups containing 10 fluoro-ether oxygens (PFPE <sub>D10</sub> -DMC) and 9.1 wt% LiTFSI                   | HPE             | 23         |
| PEO/LiTFSI gel mixed with tetraethylene glycol dimethyl ether (TEGDME)   | GPE             | 24         |
| 80 wt% methoxy-PEO-methacrylate and 20 wt% hexadecal-PEO-methacrylate copolymerized into a matrix (PMH20) with LiClO <sub>4</sub> salt                   | GPE             | 25         |
| crosslinked PEO plasticized by TEGDME with LiTFSI  | GPE             | 26         |
| PEO/LiTFSI blended with poly[(trifluoromethyl)sulfonyl acrylamide] (PA-LiTFSI)   | MCPE            | 27         |

|   |      |    |
|---|------|----|
| Li <sub>7</sub> La <sub>3</sub> Zr <sub>2</sub> O <sub>12</sub> (LLZO) dispersed in poly(vinylidene fluoride-hexafluoropropylene) (PVDF-HFP)  | MCPE | 28 |
| polyhedral oligomeric silsesquioxane (POSS) grafted with ionic liquid (IL) side chains doped with LiTFSI  | MCPE | 29 |
| perfluoropolyether with 2 ethylene oxide units on each end terminated with dimethyl carbonate end groups containing 10 fluoro-ether oxygens (PFPE <sub>E10</sub> -DMC) and 9.1 wt% LiTFSI | MCPE | 23 |
| corn starch crosslinked with $\gamma$ -(2,3-Epoxypropoxy)propyltrimethoxysilane with LiTFSI   | MCPE | 30 |
| PEO blended with sodium carboxyl methyl cellulose (Na-CMC) with sodium perchlorate (NaClO <sub>4</sub> )  | NaPE | 31 |
| organic ionic plastic crystals consisting of triisobutylmethylphosphonium bis(fluorosulfonyl)imide with added bis(fluorosulfonyl)imide sodium salt (NaFSI)                                | NaPE | 32 |

1

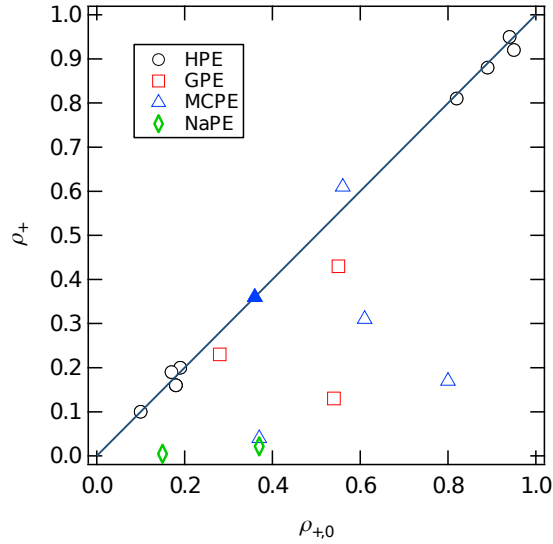
2 For each electrolyte in Table II, we calculated  $\rho_{+i}$  using Eq. 15 and the  
3 values of the parameters we obtained from the publication. For some  
4 references, all parameters were listed explicitly. In others, we needed to  
5 estimate the parameters from raw data such as Nyquist impedance spectra  
6 or current versus time plots. In three cases, the parameters needed were  
7 supplied in a personal communication from the authors.<sup>17,18,32</sup> Finally, if our  
8 calculated value for  $\rho_{+,0}$  differed substantially from the reported value  
9 (usually referred to by others as  $t_{+i}$ ), the reference was not included in this  
10 study. Only 13 out of the 472 papers satisfied all of the constraints. The most  
11 common reason a paper was excluded from our analysis was not reporting  $L$   
12 and  $A$ . Unfortunately, we could not find any papers which characterized  
13 single ion conductors that met all our requirements.

14

15

#### 1 IV. CHARACTERIZATION OF ELECTROLYTE PERFORMANCE

2 In most papers, the reported current ratio is based on the measured value  
3 of  $i_0$ . One criterion for including papers in this study was that all parameters  
4 needed to calculate  $i_\Omega$  from Eq. 14 were reported. We were thus able to  
5 calculate  $\rho_{+i}$  using Eq. 15 and compare it with the reported value,  $\rho_{+,0}$ ,  
6 obtained using Eq. 12. Fig. 4 is a plot of  $\rho_{+i}$  versus  $\rho_{+,0}$  for the 19 electrolytes  
7 listed in Table 2. For references that report only  $\rho_{+i}$ , we plot  $\rho_{+i=\rho_{+,0}}$ : these  
8 are represented by filled in symbols. Points which lie on the dashed line in  
9 Fig. 4 indicate that the measured value of  $i_0$  was consistent with the  
10 calculated value of  $i_\Omega$ . A significant number of data points in Fig. 4 fall well  
11 below the dashed line. A likely reason for this is the use of a sampling rate  
12 that is too slow to capture  $i_0$  accurately. Because the current density falls  
13 rapidly at early times (see Fig. 2), use of a less frequent sampling rate will  
14 result in a lower value of  $i_0$  and thus an inflated value of  $\rho_{+,0}$ .



1

2 **Figure 4.** Comparison of  $\rho_{+i\Omega}$  calculated using different values for the initial current  
3 for the electrolytes in Table II. On the vertical axis,  $\rho_{+i\Omega}$  is calculated using the initial  
4 current from Ohm's law,  $i_{\Omega}$ , as defined in Eq. 15. On the horizontal axis,  $\rho_{+,0}$  is  
5 calculated using the measured initial current density,  $i_0$ , as defined in Eq. 12. The  
6 dashed line indicates the case where  $i_{\Omega} = i_0$ . For references that report only  $\rho_{+i\Omega}$ , we  
7 plot  $\rho_{+i\Omega} = \rho_{+,0}$ : these are represented by filled in symbols.

8 While using  $i_{\Omega}$  to calculate  $\rho_{+i\Omega}$  has been proposed by some<sup>6,16-23</sup>, the  
9 literature is dominated by reports of  $\rho_{+,0}$  based on measured values of  $i_0$ . Our  
10 analysis suggests that  $\rho_{+i\Omega}$  is a more robust method for determining the  
11 current ratio of an electrolyte. For consistency, all calculations will utilize  $i_{\Omega}$   
12 beyond this point.

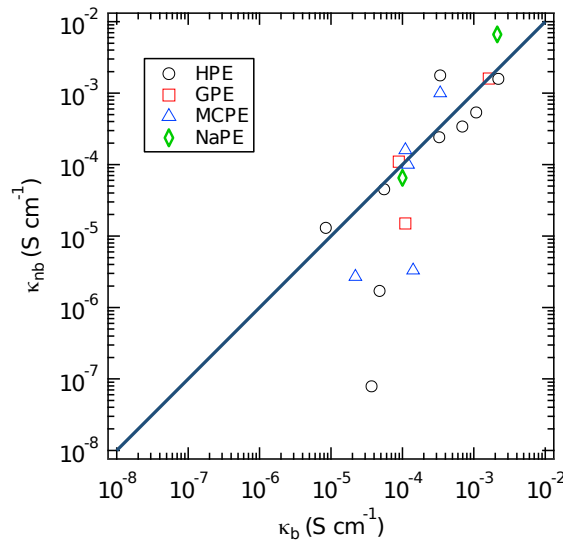
13 In principle, the conductivity of an electrolyte measured by ac impedance  
14 spectroscopy is a material property that should not depend on the electrodes  
15 used in the experiment. Either non-blocking electrodes (lithium or sodium

1metal), or blocking electrodes (stainless steel, aluminum, etc.) can be used  
 2when conducting ac impedance spectroscopy. Conductivities measured using  
 3non-blocking or blocking electrodes are denoted  $\kappa_{nb}$  and  $\kappa_b$ , respectively. Fig.  
 45 presents  $\kappa_{nb}$  versus  $\kappa_b$  for the electrolytes in Table II. For many electrolytes,  
 5 $\kappa_{nb}$  is significantly lower than  $\kappa_b$ . A few electrolytes show the opposite trend.  
 6It is not immediately clear whether  $\kappa_{nb}$  or  $\kappa_b$  should be used to quantify the  
 7performance of an electrolyte. To answer this question, we rearrange Eq. 3  
 8and 10 to obtain:

$$9 \quad \kappa \rho_{+i,i} = \frac{i_{ss}}{\Delta\Phi/L} \quad (16)$$

10This is a statement of Ohm's law for an electrolyte at steady-state under  
 11small polarization, where  $\kappa \rho_{+i,i}$  can be defined as the effective conductivity of  
 12the electrolyte at steady-state. In Fig. 6a we plot  $\kappa_b \rho_{+i,i}$  versus  $\frac{i_{ss}}{\Delta\Phi/L}$ , while in  
 13Fig. 6b we plot  $\kappa_{nb} \rho_{+i,i}$  versus  $\frac{i_{ss}}{\Delta\Phi/L}$ . The data in Fig. 6b are consistent with  
 14Eq. 16 while the data in Fig. 6a are not. Fig. 6 shows that only  $\kappa_{nb}$  can be  
 15used to accurately describe the experimental steady-state current. This is  
 16because  $\rho_{+i,i}$  and  $\kappa_{nb}$  are both measured in symmetric cells with non-blocking  
 17electrodes. For consistency, as we compare the  $\rho_{+i,i}$  of electrolytes, we must  
 18also use  $\kappa_{nb}$  when evaluating the performance of an electrolyte. Future  
 19studies aimed at characterizing new electrolytes should report both  $\kappa_b$  and

$\kappa_{nb}$ . For cases where  $\kappa_b$  and  $\kappa_{nb}$  differ substantially, attempts should be made to understand the root cause as it may be an indication of electrolyte degradation or inconsistencies in cell fabrication. For ether-based polymer electrolytes, it may be an indication of physical dissolution (i.e. non-electrochemical) of lithium or sodium metal from the electrodes.<sup>33</sup>



6

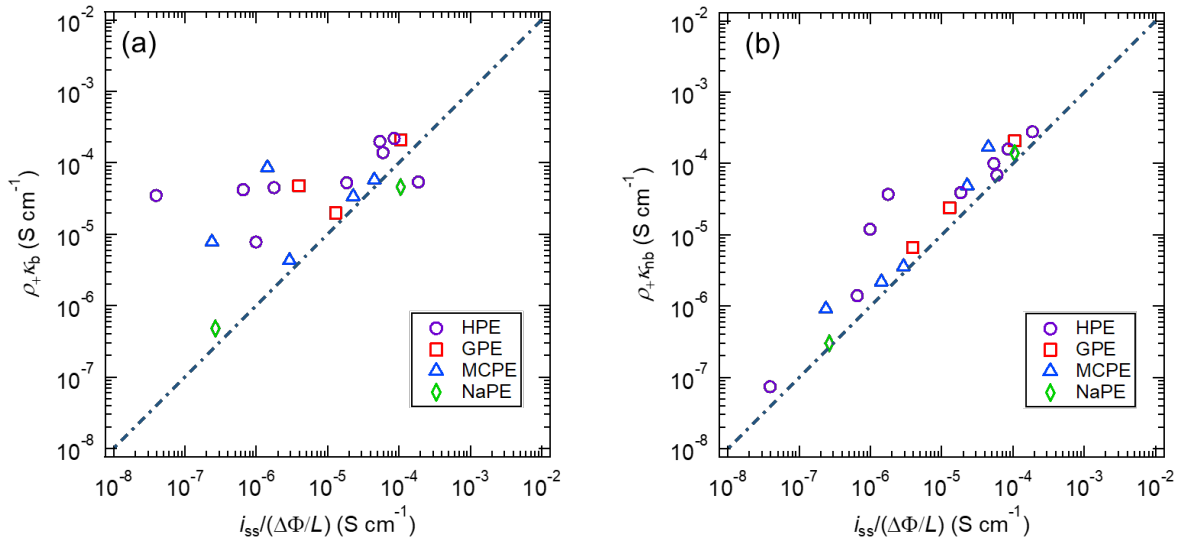
7 **Figure 5.** Ionic conductivity measured with non-blocking electrodes,  $\kappa_{nb}$ , versus

8 ionic conductivity measured with blocking electrodes,  $\kappa_b$ . The dashed line

9 represents the case where  $\kappa_b = \kappa_{nb}$ : principally, these two values should be the

10 same.





1

2 **Figure 6.** The effective conductivity,  $\kappa \rho_{+i}$ , versus the measured steady-state

3 current normalized by the voltage drop per unit length,  $\frac{i_{ss}}{\Delta\Phi/L}$ . (a) Plot with  $\kappa = \kappa_b$ ,

4 the conductivity measured with blocking electrodes and (b) Plot with  $\kappa = \kappa_{nb}$ , the

5 conductivity measured with non-blocking electrodes. The dashed line represents Eq.

6 16, a statement of Ohm's law for electrolytes under dc polarization at steady-state.

7 Only  $\kappa_{nb} \rho_{+i}$  data are reasonably consistent with Ohm's law. Rank ordering of

8 electrolytes is thus based on  $\kappa_{nb} \rho_{+i}$ .

## 9 V. TRADE-OFF BETWEEN CONDUCTIVITY AND SELECTIVE CATION

### 10 TRANSPORT

11 In an electrolyte, both cations and anions are mobile, but our main

12 interest is to maximize the flux of the working cation. This is similar to a gas

13 separation process wherein a membrane is used to concentrate a desired

14 species.<sup>34,35</sup> In this process, a pressure gradient is used to drive transport

1 through the membrane, which is designed such that one species is more  
2 permeable. Selective transport in this system is characterized by two  
3 parameters: (1) the permeability of species  $i$ ,  $P_i$ , relates the molar flux and  
4 driving force ( $\Delta P/L$ ), where  $\Delta P$  is the pressure drop across a membrane of  
5 thickness  $L$ , and (2) the selectivity of species  $i$ ,  $\alpha_{ij}$ , which is defined as  $P_i/P_j$   
6 where  $j$  refers to the other species being transported. Ideally, one would like  
7 to maximize both  $P_i$  and  $\alpha_{ij}$ . The difficulty of realizing this ideal was noted by  
8 Robeson, who showed that membranes with high permeability typically had  
9 low selectivity while membranes with high selectivity had low permeability.<sup>36</sup>  
10 When data from a large number of membranes were compiled on a plot of  
11 selectivity versus permeability, a clear upper bound was evident. Robeson  
12 presented a straight line on a log-log plot of selectivity versus permeability  
13 such that all compiled data lay below this line. This is referred to as the  
14 Robeson upper bound for gas separation.

15 We present a similar analysis for ion transport in polymer electrolytes  
16 under a **small** dc potential. Selective transport in this system is characterized  
17 by two parameters: (1) the conductivity,  $\kappa$ , relates the total current, with  
18 contributions from both ions, and driving force ( $\Delta\Phi/L$ ), and (2) the current  
19 ratio,  $\rho_{+/-}$ , which is a measure of selectivity for cation transport. Ideally, one  
20 would like to maximize  $\kappa$  and  $\rho_{+/-}$ .<sup>37-39</sup> In Fig. 7, we plot  $\rho_{+/-}$  versus  $\kappa_{nb}$  for the  
21 electrolytes in Table II. The line in Fig. 7 is analogous to the Robeson upper

1bound. The upper bound is defined empirically by  $\rho_{+i} = -0.64 - 0.34 \log K_{nb} i$ , where  $K_{nb}$   
2is in  $S\text{ cm}^{-1}$  and  $\rho_{+i}$  is bounded between 0 and 1.

3 The best electrolyte would be one that supports the highest steady-state  
4current density for a given applied potential, i.e. maximizing the slope in Fig.  
51f,  $m = K_{nb} \rho_{+i}$ . Since both parameters have been calculated, we can rank  
6order the electrolytes of interest. This is done in Table III, where the third  
7column gives the product  $K_{nb} \rho_{+i}$ . For completeness, we also give values of  $K_b$   
8,  $K_{nb}$ ,  $Ne$ ,  $\rho_{+i}$ , and  $t_{+i}$  (when known). The top six electrolytes are identified  
9by their rank in Fig. 7. Interestingly,  $\rho_{+i}$  is less than or equal to 0.2 for all six.  
10In other words, the best electrolytes to date rely on high ionic conductivity  
11rather than selective transport of cations, and efforts to achieve a value of  
12 $\rho_{+i}$  closer to 1 have come at the cost of a disproportionate reduction in ionic  
13conductivity. Considerable research has focused on surpassing the Robeson  
14upper bound because there is no physical reason that a membrane cannot  
15surpass it. The same is true for polymer electrolytes: future research aimed  
16at surpassing the upper bound presented in Fig. 7 seems warranted.

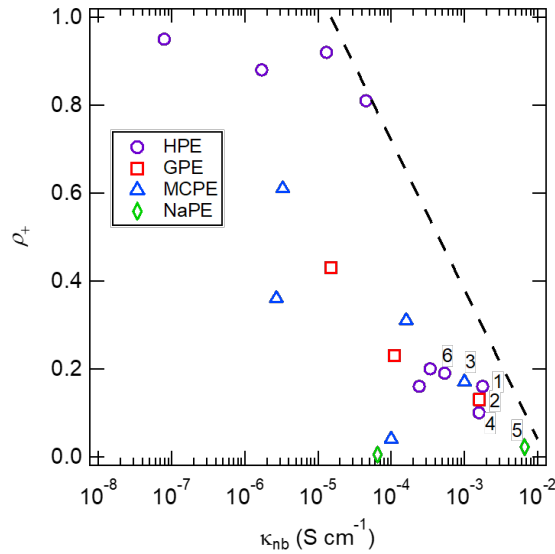
17 While our analysis focuses on the bulk properties of the electrolyte, we  
18recognize the importance of the electrolyte/electrode interface. Both  
19interfacial resistance and the stability of the electrolyte/electrode interface  
20contribute to the efficacy of an electrolyte in a battery. Our approach  
21accounts for interfacial resistance (Eq. 11-15). The rank ordering of  
22electrolytes is, however, based on bulk properties alone.

**1Table III.** Rank ordered list of electrolytes included in this study, in order of largest  
2to smallest  $K_{nb} \rho_{+Li}$ . The top-ranked electrolyte is the most efficacious. Rank,  
3electrolyte description, effective conductivity at steady-state ( $K_{nb} \rho_{+Li}$ ), blocking  
4electrode conductivity ( $K_b$ ), non-blocking electrode conductivity ( $K_{nb}$ ), Newman  
5number ( $Ne$ ), current ratio ( $\rho_{+Li}$ ), transference number  $t_{+Li}$  (when known), category,  
6and reference are presented for each electrolyte. All calculated parameters are  
7taken from the reference by methods described in Section III.

| Rank | Electrolyte (Ref)                                       | $K_{nb} \rho_{+Li}$<br>[mS/cm] | $K_b$<br>[mS/cm]     | $K_{nb}$<br>[mS/cm]  | $Ne$                 | $\rho_{+Li}$         | $t_{+Li}$ | Category |
|------|---|--------------------------------|----------------------|----------------------|----------------------|----------------------|-----------|----------|
| 1    | PEO/LiTFSI with $r = 0.017$ <sup>21</sup>               | 0.28                           | 0.34                 | 1.8                  | 5.4                  | 0.16                 |           | HPE      |
| 2    | PEO/LiTFSI gel mixed with TEGDME <sup>24</sup>          | 0.21                           | 1.6                  | 1.6                  | 6.8                  | 0.13                 |           | GPE      |
| 3    | Crosslinked cornstarch with LiTFSI <sup>30</sup>        | 0.17                           | 0.34                 | 1.0                  | 4.9                  | 0.17                 |           | MCPE     |
| 4    | PEO/LiTFSI with $r = 0.08$ <sup>17</sup>                | 0.16                           | 2.2                  | 1.58                 | 9.07                 | 0.10                 | 0.43      | HPE      |
| 5    | Organic ionic plastic crystals with NaFSI <sup>32</sup> | 0.14                           | 2.1                  | 6.6                  | 45                   | $2.2 \times 10^{-2}$ |           | NaPE     |
| 6    | P(2EO-MO)/LiTFSI with $r = 0.08$ <sup>18</sup>          | 0.10                           | 1.1                  | 0.54                 | 4.3                  | 0.19                 |           | HPE      |
| 7    | P(2EO-MO)/LiTFSI with $r = 0.04$ <sup>18</sup>          | $6.9 \times 10^{-2}$           | 0.69                 | 0.34                 | 3.9                  | 0.20                 |           | HPE      |
| 8    | LLZO dispersed in PVDF-HFP <sup>28</sup>                | $4.9 \times 10^{-2}$           | 0.11                 | 0.16                 | 2.3                  | 0.31                 |           | MCPE     |
| 9    | P(2EO-MO)/LiTFSI with $r = 0.14$ <sup>18</sup>          | $3.9 \times 10^{-2}$           | 0.33                 | 0.24                 | 5.2                  | 0.16                 |           | HPE      |
| 10   | C8-DMC with 19.9 wt% LiFSI <sup>22,40</sup>             | $3.7 \times 10^{-2}$           | $5.5 \times 10^{-2}$ | $4.5 \times 10^{-2}$ | 0.23                 | 0.81                 | -0.07     | HPE      |
| 11   | PMH20/LiClO <sub>4</sub> <sup>25</sup>                  | $2.4 \times 10^{-2}$           | $8.9 \times 10^{-2}$ | 0.11                 | 3.4                  | 0.23                 |           | GPE      |
| 12   | C8-DMC with 5.84 wt% LiFSI <sup>22,40</sup>             | $1.2 \times 10^{-2}$           | $8.5 \times 10^{-3}$ | $1.3 \times 10^{-2}$ | $9.0 \times 10^{-2}$ | 0.92                 | -0.97     | HPE      |
| 13   | Crosslinked PEO/LiTFSI with TEGDME <sup>26</sup>        | 6.7E-03                        | 0.110                | $1.5 \times 10^{-2}$ | 1.3                  | 0.43                 |           | GPE      |
| 14   | POSS with IL side chains and                            | $3.6 \times 10^{-2}$           | 0.120                | 0.10                 | 27                   | $4.0 \times 10^{-2}$ |           | MCPE     |

|    |  |                      |                       |                      |                      |                      |  |      |
|----|--|----------------------|-----------------------|----------------------|----------------------|----------------------|--|------|
|    | LiTFSI <sup>29</sup>                                   | -3                   |                       |                      |                      | 2                    |  |      |
| 15 | PEO/LiTFSI blended with PA-LiTFSI <sup>27</sup>        | $2.2 \times 10^{-3}$ | 0.141                 | $3.3 \times 10^{-3}$ | 0.64                 | 0.61                 |  | MCPE |
| 16 | PFPE10-DMC with 9.1 wt% LiTFSI <sup>23</sup>           | $1.4 \times 10^{-3}$ | $4.8 \times 10^{-2}$  | $1.7 \times 10^{-3}$ | 0.14                 | 0.88                 |  | MCPE |
| 17 | PFPEE10-DMC with 9.1 wt% LiTFSI <sup>23</sup>          | $9.1 \times 10^{-4}$ | $2.2 \times 10^{-2}$  | $2.7 \times 10^{-3}$ | 1.8                  | 0.36                 |  | MCPE |
| 18 | PEO/Na-CMC blend with NaClO <sub>4</sub> <sup>31</sup> | $3.0 \times 10^{-4}$ | 0.10                  | $6.5 \times 10^{-2}$ | 210                  | $4.8 \times 10^{-3}$ |  | NaPE |
| 19 | PFPE10-Diol with 9.1 wt% LiTFSI <sup>23</sup>          | $7.4 \times 10^{-5}$ | $3.70 \times 10^{-2}$ | $7.9 \times 10^{-5}$ | $5.0 \times 10^{-2}$ | 0.95                 |  | MCPE |

1



2

3 **Figure 7.** Plot of  $\rho_{+}$  versus  $\kappa_{nb}$  for the electrolytes in Table II. The dashed line  
4 is analogous to the Robeson upper bound in gas separation membranes, here  
5 defined by  $\rho_{+} = -0.64 - 0.34 \log \kappa_{nb}$ , where  $\kappa_{nb}$  is in  $S\ cm^{-1}$  and  $\rho_{+}$  is bounded between 0  
6 and 1. The six electrolytes with the highest  $\kappa_{nb} \rho_{+}$  in Table III are identified by their  
7 rank.

## 8 VI. DISCUSSION

1 The relationship between  $\rho_{+i}$  and transport properties of concentrated  
 2 electrolytes is quantified by Eq. 4-7. In Table III, there are some electrolytes  
 3 for which  $Ne$  is small (i.e.,  $Ne \leq 0.1$ ), and others for which  $Ne$  is large (i.e.,

4  $Ne \geq 10$ ). In the limit of small  $Ne$ ,  $\frac{1}{1+Ne} \approx 1 - Ne$  and Eq. 3 reduces to

$$5 \quad i_{ss} = \kappa(1 - Ne) \frac{\Delta\Phi}{L}, \quad (17)$$

6 which implies that the effective conductivity of the electrolyte at steady-  
 7 state is marginally reduced from that at  $t=0^{+i}$  by a factor equal to  $(1 - Ne)$ .

8 When  $Ne$  is large,  $1 + Ne \approx Ne$  and Eq. 3 can be combined with Eq. 4 and  
 9 written as

$$10 \quad i_{ss} = \frac{F^2 D c}{a R T i i i}$$

11 The surprising conclusion from Eq. 18 is that there is a class of ion  
 12 conductors for which the relationship between  $i_{ss}$  and  $\Delta\Phi/L$  is independent of  
 13 conductivity.

14 Maximizing  $\rho_{+i}$  is equivalent to minimizing  $Ne$ . It is clear from Eq. 4 that  
 15  $Ne$  may be reduced by either reducing  $\kappa$ , reducing  $(1 - t_{+i}^0)^2$ , reducing  $T_f$ , or  
 16 increasing  $D$ . Ultimately, we desire small values of  $Ne$  and large values of  $\kappa$ :  
 17 thus, reducing  $Ne$  by reducing  $\kappa$  is not desirable. On the other hand, reducing  
 18  $(1 - t_{+i}^0)^2$ , reducing  $T_f$ , or increasing  $D$  are desirable routes to increasing  $\rho_{+i}$ .

1 There are very few publications where  $t_{+i}$ ,  $T_f$ , and  $D$  are measured.<sup>2,14,16,40-41</sup>

2 Table III presents values of  $t_{+i}$  in cases where it has been reported. Note

3 that there is little correspondence between  $\rho_{+i}$  and  $t_{+i}$ .<sup>17</sup>

4 Our discussion has been limited to electrolytes under small applied dc  
5 potentials. Whether polarizations are large or small, the salt concentration  
6 gradients in the cell affect the current-voltage relationship. At large potential  
7 gradients obtained in practical batteries (Fig. 1c,d), the concentration  
8 dependence of  $\kappa$ ,  $D$ ,  $t_{+i}$ , and  $T_f$ , can no longer be ignored, and rank ordering  
9 electrolytes would require numerical calculations described in Refs. 5,38.

## 10 VII. CONCLUSION

11 Ion transport through a **binary** battery electrolyte is governed by four  
12 concentration dependent parameters:  $\kappa$ ,  $D$ ,  $t_{+i}$ , and  $T_f$ . Under large applied  
13 potentials typical of many battery applications, explicit knowledge of these  
14 four parameters and their concentration dependence is required to predict  
15 the relationship between  $i$  and  $\Delta\Phi/L$ . The problem is simplified for small  
16 applied potentials wherein two parameters govern the relationship between  $i$   
17 and  $\Delta\Phi/L$ :  $\kappa$  and  $\rho_{+i}$ . Data obtained from symmetric cells with non-blocking  
18 electrodes can be used to determine  $\rho_{+i}$  using Eq. 14 and 15. In principle,  $\kappa$   
19 can be determined using either blocking ( $\kappa_b$ ) or non-blocking electrodes ( $\kappa_{nb}$ ).  
20 Our study of the literature revealed a surprising discrepancy between these  
21 two measurements reported in a significant number of publications (see

1Table III). When a discrepancy was found,  $\kappa_{nb}$  was often significantly lower  
2than  $\kappa_b$ , although a few electrolytes show the opposite trend. While the  
3analysis reported here is based on  $\kappa_{nb}$ , it is likely that practical electrolytes  
4are those wherein the two conductivities are within experimental error, i.e.,  
5those that are unaffected by contact with the alkali metal of interest. Our  
6analysis is restricted to publications wherein both  $\kappa_{nb}$  and  $\rho_{+i}$  were rigorously  
7measured. Ideally, both  $\kappa_{nb}$  and  $\rho_{+i}$  should be maximized. However, there  
8appears to be a trade-off between these two parameters, resulting in an  
9upper bound ( $\rho_{+i} = -0.64 - 0.34 \log \kappa_{nb}$ , where  $\kappa_{nb}$  is in  $S\text{ cm}^{-1}$ ) that is analogous to one  
10exposed by Robeson for the relationship between permeability and  
11selectivity in gas separation membranes. Designing polymer electrolytes to  
12surpass this upper bound may enable next-generation lithium and sodium  
13batteries. In the limit of small applied potentials, the proportionality factor  
14between  $i$  and  $\Delta\Phi/L$  for binary electrolytes **at steady-state** is the product  
15 $\kappa_{nb} \rho_{+i}$ . This relationship is analogous to Ohm's law for electronic conductors.  
16When comparing electrolyte performance, the preferred electrolyte is the  
17one for which  $\kappa_{nb} \rho_{+i}$  is maximized. We use this principle to rank order  
18electrolytes. We hope this perspective will serve as a guide for quantifying  
19the efficacy of future electrolyte designs.

20

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7

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## 5LIST OF SYMBOLS

| Symbol       | Meaning   |
|--------------|---|
| $A$          | electrode area ( $\text{cm}^2$ )  |
| $a$          | salt stoichiometric coefficient   |
| $c$          | salt concentration ( $\text{mol cm}^{-3}$ )   |
| $c_0$        | solvent concentration ( $\text{mol cm}^{-3}$ )  |
| $D$          | restricted diffusion coefficient of the salt ( $\text{cm}^2 \text{s}^{-1}$ )  |
| $D_{0+i}$    | Stefan-Maxwell diffusion coefficient describing the interactions between the solvent and cation ( $\text{cm}^2 \text{s}^{-1}$ ) |
| $D_{0-i}$    | Stefan-Maxwell diffusion coefficient describing the interactions between the solvent and anion ( $\text{cm}^2 \text{s}^{-1}$ )  |
| $D_{\pm}$    | Stefan-Maxwell diffusion coefficient describing the interactions between the cation and anion ( $\text{cm}^2 \text{s}^{-1}$ )   |
| $F$          | Faraday constant ( $96485 \text{ C mol}^{-1}$ )   |
| $i$          | current density ( $\text{mA cm}^{-2}$ )   |
| $i_0$        | initial current density measured after polarization at $\Delta V$ ( $\text{mA cm}^{-2}$ )                                       |
| $i_{ss}$     | current density measured at steady-state in response to $\Delta V$ ( $\text{mA cm}^{-2}$ )                                      |
| $i_{\Omega}$ | initial current density calculated using Ohm's law at $t = 0^+$ , see equation 14 ( $\text{mA cm}^{-2}$ )                       |
| $L$          | electrolyte or membrane thickness (cm)  |
| $m$          | slope   |
| $m$          | salt molality ( $\text{mol kg}^{-1}$ )  |
| $M$          | general cation  |
| $Ne$         | Newman number   |
| $P_i$        | permeability of species $i$ ( $\text{mol m}^{-1} \text{s}^{-1} \text{Pa}^{-1}$ )  |
| $R$          | universal gas constant ( $8.314 \text{ J mol}^{-1} \text{K}^{-1}$ )   |
| $r$          | molar ratio of lithium cations to oxygens in the electrolyte  |
| $R_b$        | bulk resistance of the electrolyte measured by ac impedance spectroscopy ( $\Omega$ )   |
| $R_i$        | interfacial resistance between electrolyte and non-blocking electrode ( $\Omega$ )  |
| $R_{i,0}$    | interfacial resistance measured by ac impedance spectroscopy just before $\Delta V$ is applied ( $\Omega$ )                     |
| $R_{i,ss}$   | interfacial resistance measured by ac impedance spectroscopy after the steady-state current is reached ( $\Omega$ )             |

|          |   |
|----------|---|
| $T$      | temperature (K)   |
| $T_f$    | thermodynamic factor  |
| $t$      | time (s)  |
| $t_{+i}$ | transference number of the cation with respect to the velocity of the solvent |
| $U^0$    | battery open circuit potential (V)  |
| $V$      | battery operating voltage (V)   |
| $X$      | general anion   |
| $z_{+i}$ | charge number of cation   |
| $z_{-i}$ | charge number of anion  |

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| Symbol         | Meaning   |
|----------------|---|
| $\alpha_{i,j}$ | selectivity of species $i$ compared to species $j$                                  |
| $\beta$        | dimensionless parameter defined by Eq. 8  |
| $\gamma_{\pm}$ | mean molal activity coefficient of the electrolyte                                  |
| $\Delta\Phi$   | dc potential drop across an electrolyte, excluding ohmic drop across interfaces (V) |
| $\Delta P$     | pressure drop across a membrane (Pa)  |
| $\Delta V$     | dc potential drop across a symmetric cell (V)                                       |
| $\eta$         | overpotential (V)   |
| $\kappa$       | ionic conductivity ( $S\ cm^{-1}$ )   |
| $\kappa_b$     | ionic conductivity measured using blocking electrodes ( $S\ cm^{-1}$ )              |
| $\kappa_{nb}$  | ionic conductivity measured using non-blocking electrodes ( $S\ cm^{-1}$ )          |
| $\nu$          | total number of ions to which the salt dissociates                                  |
| $\nu_{+i}$     | number of cations in the dissociated salt   |
| $\nu_{-i}$     | number of anions in the dissociated salt  |
| $\rho_{+i}$    | current ratio obtained using $i_\Omega$   |
| $\rho_{+,0}$   | current ration obtained using $i_0$   |
| $\sigma$       | electronic conductivity ( $S\ cm^{-1}$ )  |

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