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### Title

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### Permalink

<https://escholarship.org/uc/item/06j4p2d0>

### Journal

AJP Regulatory Integrative and Comparative Physiology, 325(5)

### ISSN

0363-6119

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### Publication Date

2023-11-01

### DOI

10.1152/ajpregu.00065.2023

Peer reviewed

1 **Current definitions of the breathing cycle in alveolar breath-by-breath gas exchange analysis**

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26  
27 **Submission Type:** Review Article

28 **Running head title:** Definitions of the human breathing cycle

29 **Text-only word count:** 6604

30 **Number of references:** 66

31 **Numbers of Figures:** 6

32 **Numbers of Tables:** 1

33 **Abstract word count:** 220

34 **ABSTRACT**

35 Identification of the breathing cycle forms the basis of any breath-by-breath gas exchange analysis.  
36 Classically, the breathing cycle is defined as the time interval between the beginning of two  
37 consecutive inspiration phases. Based on this definition, several research groups have developed  
38 algorithms designed to estimate the volume and rate of gas transferred across the alveolar  
39 membrane (“alveolar gas exchange”); however, most algorithms require measurement of lung  
40 volume at the beginning of the  $i^{\text{th}}$  breath ( $V_{L_{i-1}}$  – i.e., the end-expiratory lung volume of the  
41 preceding  $i^{\text{th}}$  breath). The main limitation of these algorithms is that direct measurement of  $V_{L_{i-1}}$  is  
42 challenging and often unavailable. Two solutions avoid the requirement to measure  $V_{L_{i-1}}$  by  
43 redefining the breathing cycle. One method defines the breathing cycle as the time period between  
44 two equal fractional concentrations of lung expired oxygen ( $F_{O_2}$ ) (or carbon dioxide;  $F_{CO_2}$ ),  
45 typically in the alveolar phase, whereas the other uses the time period between equal values of the  
46  $F_{O_2}/F_{N_2}$  (or  $F_{CO_2}/F_{N_2}$ ) ratios. Thus, these methods identify the breathing cycle by analyzing the gas  
47 fraction traces rather than the gas flow signal. In this review, we define the traditional approach and  
48 two alternative definitions of the human breathing cycle and present the rationale for redefining  
49 this term. We also explore the strengths and limitations of the available approaches and provide  
50 implications for future studies.

51

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53 **Keywords:** Respiratory cycle, gas exchange, kinetics, exercise, cardiopulmonary exercise testing,  
54 lung gas stores

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## 61 **Introduction**

62 Identification of the breathing cycle forms the basis of the quantitative analysis of alveolar breath-  
63 by-breath (B-by-B) gas exchange (1, 2). Classically, the breathing cycle is identified by analyzing  
64 the gas flow signal from a flow meter, where the zero-crossing points represent the transition  
65 between inspiratory and expiratory phases, and vice versa. The gas flow, together with the gas  
66 fractions, are generally collected at the mouth and used to estimate alveolar gas exchange on a B-  
67 by-B basis. However, accurate and reliable estimation of gas transfer across the alveolar membrane  
68 ( $\dot{V}O_{2A}$  and  $\dot{V}CO_{2A}$ ) requires changes in B-by-B lung gas stores to be known (2).

69 Several research groups have developed algorithms and methods to estimate the B-by-B  
70 alveolar gas exchange; however, most algorithms require knowledge of the absolute lung volume at  
71 the beginning of the  $i^{\text{th}}$  breath ( $V_{Li-1}$ ; i.e., the end-expiratory lung volume of the preceding  $i^{\text{th}}$   
72 breath) (3–8). Due to the technical complexity of measuring  $V_{Li-1}$ , it is generally estimated rather  
73 than measured directly (9, 10). However, different values of  $V_{Li-1}$  lead to different B-by-B alveolar  
74 gas exchange estimations (11). In addition,  $V_{Li-1}$  is not stable during exercise (7, 12) and is affected  
75 by body position (13) and exercise modality (e.g., walking, running, and cycling) (14). Therefore,  
76 the validity of these techniques depends largely on the validity of the  $V_{Li-1}$  measurement.

77 Grønlund (15) conceived an ingenious solution to overcome the issues related to the  
78 determination of  $V_{Li-1}$ ; however, this solution required redefining the breathing cycle. In  
79 Grønlund's algorithm a single breathing cycle is identified between two points on successive, but  
80 not necessarily consecutive, breaths with the same fractional concentration (or partial pressure) of  
81 lung  $O_2$  (or  $CO_2$ ) occurring typically in the alveolar phase ( $F_{O_2}$  or  $F_{CO_2}$ ). Intra-breath integration of  
82 gas flow and concentration fractions is performed between these two points, allowing the estimation  
83 of alveolar gas exchange without the need for  $V_{Li-1}$  measurement (see below). A modification of  
84 this technique has been proposed by Cettolo and Francescato that also eliminates need to measure

85  $V_{Li-1}$ , but uses a different redefinition of the breathing cycle (16). This algorithm (16) defines the  
86 breathing cycle as the time interval elapsed between two successive, but not necessarily  
87 consecutive, breaths with the same fractional concentration of lung  $O_2/N_2$  (or  $CO_2/N_2$ ) ratio,  
88 typically in the alveolar phase ( $F_{O_2}/F_{N_2}$  or  $F_{CO_2}/F_{N_2}$ ). Therefore, these two techniques use gas  
89 fractional concentration signals instead of gas flow signals to define the breathing cycle (Table 1).

90 This review presents the current definitions of the human breathing cycle and provides the  
91 rationale behind the use of alternative definitions, which arises from the need to estimate alveolar  
92 gas exchange. A brief description of gas exchange measurements at the mouth level is provided to  
93 facilitate the understanding of different alveolar corrections (more in-depth information on mouth  
94 measurements can be found elsewhere (1, 2, 4, 17–19)). Moreover, we summarize the main  
95 limitations of applying one technique over another and present implications for future research. We  
96 have focused our review on definitions of the breathing cycle using B-by-B open-circuit systems  
97 that measure the inspired and expired gas flows and volumes. Historical perspectives of the  
98 development of B-by-B gas exchange analysis, including details of the equipment, measurements,  
99 and volume and gas corrections, are available elsewhere (1, 2, 4, 17–25).

100

101

\*TABLE 1 NEAR HERE\*

102

### 103 **The classical definition of the breathing cycle for B-by-B gas exchange analysis**

104 Remarkable developments in real-time B-by-B open-circuit systems during the second half of the  
105 20<sup>th</sup> century made it possible to quantify the inspired and expired gas volumes in real-time (1, 18,  
106 20). The breathing cycle was identified based on these techniques and used to quantify external  
107 respiration (i.e., exchange of  $O_2$  and  $CO_2$  between the alveoli and pulmonary capillary) on a B-by-B  
108 basis.

109 In general, a cycle can be defined as a series of incidences of the same condition that are  
110 repeated over time. Accordingly, the breathing cycle can be defined as the time interval between  
111 two equal incidences (i.e., inspiration or expiration phases). Convention defines “a breath” from the  
112 time interval between the beginning of two consecutive inspiration phases (Figure 1).

113

114 \*FIGURE 1 NEAR HERE\*

115

116 The first step in identifying the breathing cycle is to detect the beginning and end of each  
117 inspiration and expiration phase. This requires analysis of the gas flow signal ( $\dot{V}$ ) from the flow  
118 meter. Theoretically, zero-crossing points of the flow signals can be used to identify the start and  
119 end of each inspiration and expiration phase, as the sign of the flow signal changes with inhalation  
120 and exhalation (Figure 1). However, the flow signal, being a digitalized signal, rarely presents an  
121 absolute zero value. Therefore, the nearest points to zero in the flow signal are generally used in B-  
122 by-B gas exchange analysis to provide a reasonable estimation of the transition points between  
123 inspiration and expiration, and vice versa (12).

124 Determining the beginning and end of each inspiration and expiration phase enables the  
125 estimation of the inspiratory and expiratory volumes. The volume of the inspired ( $V_{in}$ ) and expired  
126 ( $V_{ex}$ ) gas is determined by integrating the flow signal during the inspiration and expiration phases  
127 of the  $i^{\text{th}}$  breath, respectively.

128

$$129 \quad V_{in_i} = \int_{t_{bi_i}}^{t_{ei_i}} \dot{V}_{in} \cdot dt \quad (1)$$

$$130 \quad V_{ex_i} = \int_{t_{be_i}}^{t_{ee_i}} \dot{V}_{ex} \cdot dt \quad (2)$$

131

132 where  $t_{bi}$  and  $t_{ei}$  are the time instants at which the inspiration phase begins and ends of breath  $i$ ,  
 133 respectively, whereas  $t_{be}$  and  $t_{ee}$  are the time instants at which the expiration phase begins and  
 134 ends for the  $i^{\text{th}}$  breath, respectively. The total time ( $t_{TOT}$ ) over the  $i^{\text{th}}$  breath can be defined as  
 135  $t_{TOTi} = t_{in_i} + t_{ex_i}$ , where  $t_{ex_i}$  and  $t_{in_i}$  are the expiratory and inspiratory times, respectively.

136 It is then possible to derive other important ventilatory-based variables over a breathing cycle,  
 137 such as tidal volume ( $V_T$ ), breathing rate ( $B_R$ ), expired flow ( $\dot{V}_E$ ), and inspired flow ( $\dot{V}_I$ ) from  $V_{ex_i}$ ,  
 138  $V_{in_i}$ ,  $t_{ex_i}$ , and  $t_{in_i}$ .  $V_T$ ,  $B_R$ ,  $\dot{V}_E$ , and  $\dot{V}_I$  (commonly expressed in  $\text{L}\cdot\text{min}^{-1}$  for  $\dot{V}_E$  and  $\dot{V}_I$ ,  $\text{breaths}\cdot\text{min}^{-1}$   
 139 for  $B_R$ , and L for  $V_T$ ) for each breath from this flow signal (see (1, 4, 17, 25) for the relevant  
 140 equations).

141 Several commercial automated B-by-B systems do not compute  $V_{in}$  (and the associated  $\dot{V}_I$ )  
 142 directly. Instead, these variables are estimated using the nitrogen balance approach:  $V_{in} \cdot F_{IN_2} =$   
 143  $V_{ex} \cdot F_{EN_2}$  (i.e., the so-called Haldane's correction; reviewed in Ward, 2018)), where  $F_{IN_2}$  and  $F_{EN_2}$   
 144 are the mean fractions of nitrogen ( $N_2$ ) during the inspiration and expiration phases, respectively.

145

$$146 \quad V_{in} = V_{ex} \cdot \frac{F_{EN_2}}{F_{IN_2}} \quad (3)$$

147

148 Since B-by-B systems generally also do not measure the  $N_2$  fraction directly, and as there is  
 149 only a negligible quantity of other inert gases in the inspired air,  $F_{N_2}$  is commonly estimated as  
 150 follows:  $F_{N_2} = 1 - (F_{O_2} + F_{CO_2})$ . Accordingly,  $\dot{V}_I$  for breath  $i$  can be determined as follows:

151

$$152 \quad \dot{V}_{Ii} = \dot{V}_{Ei} \cdot \frac{1 - F_{EO_2i} - F_{ECO_2i}}{1 - F_{IO_2i} - F_{ICO_2i}} \quad (4)$$

153

154 However, this Haldane correction is intrinsically flawed when applied to B-by-B gas  
 155 exchange analysis, as it assumes constancy in the lung  $N_2$  stores, which, over the duration of a  
 156 single breathing cycle, occurs only when the breathing exchange ratio ( $RER = \dot{V}CO_2/\dot{V}O_2$ ) is equal  
 157 to 1 and consecutive end-expiratory lung volumes are precisely equal (2). Fluctuations in the end-  
 158 expiratory lung volume at rest (29) and during exercise (7) cause subsequent changes in the  
 159 fractional composition of the lung gas. Therefore, to facilitate accurate alveolar gas exchange  
 160 measurement,  $\dot{V}_I$  should be measured directly.

161 Identifying the beginning and end of the inspiration and expiration phases of breath  $i$  also  
 162 enables quantification of the volumes of the inspired and expired gas. The total volume of  $O_2$  and  
 163  $CO_2$  exchanged at the mouth over the  $i^{\text{th}}$  breath ( $VO_{2iM}$  and  $VCO_{2iM}$ , respectively) is determined by  
 164 the difference between their inspired and expired volumes.

165

$$166 \quad VO_{2iM} = \int_{t_{bi}}^{t_{ei}} F_{IO_2} \cdot \dot{V}_{in} \cdot dt - \int_{t_{bei}}^{t_{eei}} F_{EO_2} \cdot \dot{V}_{ex} \cdot dt \quad (5)$$

$$167 \quad VCO_{2iM} = \int_{t_{bei}}^{t_{eei}} F_{ECO_2} \cdot \dot{V}_{ex} \cdot dt - \int_{t_{bi}}^{t_{ei}} F_{ICO_2} \cdot \dot{V}_{in} \cdot dt \quad (6)$$

168

169 where  $F_{IO_2}$  and  $F_{EO_2}$  are the instantaneous  $O_2$  fractions in the inspired and expired gas of breath  $i$ ,  
 170 and  $F_{ICO_2}$  and  $F_{ECO_2}$  are the instantaneous  $CO_2$  fractions in the inspired and expired gas over the  $i^{\text{th}}$   
 171 breath, respectively. Therefore, the intra-breath integration of flow and gas tensions is performed  
 172 over the inspiration and expiration phases of breath  $i$ , from which the volumes of  $O_2$  and  $CO_2$   
 173 exchanged at the mouth during a single breathing cycle are obtained (Figure 1 depicts gas flow  
 174 (panel A), and  $O_2$ , and  $CO_2$  gas tension traces (panel B and C, respectively) used to perform the  
 175 intra-breath integration).



176 Some studies have shown that the use of  $VO_{2M}$  instead of  $VO_{2A}$  amplifies the intrinsic B-by-B  
 177 variability in  $O_2$  exchange (2, 5–7, 10, 12). Similar results were expected for the difference between  
 178 the B-by-B variability of  $VCO_{2M}$  and  $VCO_{2A}$ , although the B-by-B variability for the alveolar  $CO_2$   
 179 exchange could be greater than for  $O_2$  exchange (5). In contrast, the average values of  $VO_{2M}$  and  
 180  $VCO_{2M}$  during steady-state conditions can be considered an unbiased average of the alveolar gas  
 181 exchange (i.e.,  $VO_{2A}$  and  $VCO_{2A}$ ) (7, 10, 12). However, the differences between external gas  
 182 exchange measured at the mouth and that between the alveolar space and pulmonary capillary can  
 183 be substantial during the work rate transition phases (4, 30), as neither Equations 5 nor 6 consider  
 184 the changes in the volumes of each gas stored in the lung. Therefore, distinguishing between gas  
 185 exchange at the mouth and the alveoli under these conditions is of paramount importance.

186 Several approaches designed to estimate  $VO_{2A}$  and  $VCO_{2A}$  from measurements of gas volumes  
 187 exchanged at the mouth have been proposed (for a complete review, please see Capelli et al. (2)).  
 188 Each of these approaches derives from the pioneering work of Auchincloss et al. (3). The alveolar-  
 189 capillary gas transfer over breath  $i$  differs from the transfer measured at the mouth by the changes in  
 190 the lung gas stores over the same breath:

191

$$192 \quad VO_{2iA} = VO_{2iM} - \Delta VO_{2iS} \quad (7)$$

$$193 \quad VCO_{2iA} = VCO_{2iM} + \Delta VCO_{2iS} \quad (8)$$

194

195 where  $\Delta VO_{2iS}$  and  $\Delta VCO_{2iS}$  represent the changes in the volumes of  $O_2$  and  $CO_2$  stored in the lung,  
 196 respectively. The net transfer of  $O_2$  or  $CO_2$  at the alveolar level approaches that value measured at  
 197 the mouth only when metabolism is in a steady-state condition and consecutive end-expiratory lung  
 198 volumes are precisely equal. However,  $\Delta VO_{2iS}$  and  $\Delta VCO_{2iS}$  are rarely zero when considering a

199 single breathing cycle, and therefore changes in the lung gas stores must be considered for valid  
 200 estimation of alveolar-capillary gas transfer over the  $i^{\text{th}}$  breath (i.e.,  $VO_{2iA}$  and  $VCO_{2iA}$ ) (2).

201 Changes in lung gas stores depend on the changes in the lung volume and alveolar gas  
 202 fractions (1–3):

203

$$204 \quad \Delta VO_{2iS} = V_{Li-1} \cdot (F_{AO_{2i}} - F_{AO_{2i-1}}) + F_{AO_{2i}} \cdot \Delta V_{Li} \quad (9)$$

$$205 \quad \Delta VCO_{2iS} = V_{Li-1} \cdot (F_{ACO_{2i}} - F_{ACO_{2i-1}}) + F_{ACO_{2i}} \cdot \Delta V_{Li} \quad (10)$$

206

207 where  $V_{Li-1}$  is the end-expiratory lung volume;  $F_{AO_{2i-1}}$  and  $F_{ACO_{2i-1}}$  are the alveolar fractions of O<sub>2</sub>  
 208 and CO<sub>2</sub> of the preceding breath (i.e.,  $i-1$ ), respectively;  $F_{AO_{2i}}$  and  $F_{ACO_{2i}}$  are the alveolar fractions of  
 209 O<sub>2</sub> and CO<sub>2</sub> in the current breath  $i$ , respectively; and  $\Delta V_{Li}$  is the change in the lung volume  
 210 occurring over breath  $i$ . Therefore, the changes in the lung gas stores depend mainly on two factors:  
 211 1) changes in the overall alveolar gas fractions of O<sub>2</sub> and CO<sub>2</sub> between the beginning and the end of  
 212 breath  $i$  (i.e., the first term on the right-hand side of Equations 9 and 10,  $F_{AO_{2i}} - F_{AO_{2i-1}}$  and  
 213  $F_{ACO_{2i}} - F_{ACO_{2i-1}}$ , respectively), and 2) the changes in lung volume (i.e., the second term on the  
 214 right-hand side of Equations 9 and 10,  $\Delta V_{Li}$ ).

215  $\Delta V_{Li}$  can be determined by assuming no alveolus-to-capillary N<sub>2</sub> exchange (i.e.,  $VN_{2A} =$   
 216  $VN_{2M} - \Delta VN_{2S} = 0$ ; where  $VN_{2A}$  and  $VN_{2M}$  are the amounts of N<sub>2</sub> exchanged at the alveolus and  
 217 mouth levels, respectively, and  $\Delta VN_{2S}$  is the change in the volume of N<sub>2</sub> in the lung over a  
 218 breathing cycle). By substituting  $\Delta VN_{2S}$  into Equation 9 (i.e.,  $\Delta VN_{2S} = V_{Li-1} \cdot (F_{AN_{2i}} -$   
 219  $F_{AN_{2i-1}}) + F_{AN_{2i}} \cdot \Delta V_{Li}$ ),  $\Delta V_{Li}$  can be determined as follows:

220

221 
$$\Delta V_{L_i} = \frac{VN_{2_iM} - V_{L_{i-1}} (F_{AN_{2_i}} - F_{AN_{2_{i-1}}})}{F_{AN_{2_i}}} \quad (11)$$

222

223 where the amount of N<sub>2</sub> exchanged at the mouth level over the breath *i* (i.e.,  $VN_{2_iM}$ ) can be  
 224 determined as follows:

225

226 
$$VN_{2_iM} = \int_{t_{bi}}^{t_{ei}} F_{IN_2} \cdot \dot{V}_{in} \cdot dt - \int_{t_{be}}^{t_{ee}} F_{EN_2} \cdot \dot{V}_{ex} \cdot dt \quad (12)$$

227

228 Beaver et al. (4) proposed an alternative approach to determine  $\Delta V_{L_i}$ :

229

230 
$$\Delta V_{L_i} = \frac{V_{in_i} \left( \frac{1-F_{IH_2O_i}}{1-F_{AH_2O_i}} \right) - V_{ex_i} \left( \frac{1-F_{EH_2O_i}}{1-F_{AH_2O_i}} \right) - VO_{2_iM} + VCO_{2_iM} + V_{L_{i-1}} \left[ (F_{AO_{2_i}} - F_{AO_{2_{i-1}}}) + (F_{ACO_{2_i}} - F_{ACO_{2_{i-1}}}) \right]}{1-F_{AO_{2_i}} - F_{ACO_{2_i}}}$$

231

(13)

232 where  $\left( \frac{1-F_{IH_2O_i}}{1-F_{AH_2O_i}} \right)$  and  $\left( \frac{1-F_{EH_2O_i}}{1-F_{AH_2O_i}} \right)$  account for the water vapor pressure in the inspired and expired  
 233 volumes, respectively, and  $F_{AO_2}$  and  $F_{ACO_2}$  are alveolar fractions of O<sub>2</sub> and CO<sub>2</sub> of the breath *i* and  
 234 preceding one (i.e., *i*-1). This approach presents some advantages. First,  $\Delta V_{L_i}$  can be expressed in  
 235 terms of measured quantities, which is convenient from a computational perspective. Second,  
 236 compared to Equation 11, the Beaver et al.'s approach is less prone to estimation errors when the  
 237 inspired gas fractions are transiently changed. For instance, when the inspired  $F_{N_2}$  changes  
 238 significantly, which may occur when manipulating inspired gas fractions (e.g., supplemental  
 239 oxygen), the terms  $VN_{2_iM}$  and  $V_{L_{i-1}} (F_{AN_{2_i}} - F_{AN_{2_{i-1}}})$  in Equation 11 are large and nearly the same

240 in magnitude during a transient period. This will expose Equation 11 to a higher error sensitivity  
241 and, in some cases, it cannot be used (4).

242 The only quantity that remains to be determined is  $V_{Li-1}$ , which is not directly measurable  
243 using Equations 9, 10, 11, and 13. Therefore, a pre-determined value for  $V_{Li-1}$  must be chosen. In  
244 their pioneering work, Auchincloss et al. (3) proposed setting  $V_{Li-1}$  equal to the functional residual  
245 capacity (*FRC*) of the subject (hereinafter referred to as the A algorithm). Other research groups  
246 made the same assumptions, in which *FRC* was either directly determined prior to exercise (4, 7,  
247 10) or indirectly estimated using predictive equations (31).

248 Wessel et al. (32) suggested that, since the quantity  $F_{AO_{2i}} - F_{AO_{2i-1}}$  (and  $F_{ACO_{2i}} - F_{ACO_{2i-1}}$ )  
249 is likely to be rather small, the term  $V_{Li-1} \cdot (F_{AO_{2i}} - F_{AO_{2i-1}})$  (and  $V_{Li-1} \cdot (F_{ACO_{2i}} - F_{ACO_{2i-1}})$ )  
250 can be neglected; thus,  $V_{Li-1}$  can be assumed to equal 0 L. However, this approach was  
251 subsequently questioned by di Prampero and Lafortuna (11) who demonstrated that setting  $V_{Li-1}$   
252 equal to 0 changes the alveolar gas exchange measure. Moreover, they also showed that selecting  
253 different values of  $V_{Li-1}$  leads to a change in the B-by-B estimation and variability of  $VO_{2iA}$  and  
254  $VCO_{2iA}$  (Figure 2) (11).

255 Swanson (6) proposed an alternative approach based on the assumption that most of the B-by-  
256 B gas exchange variability at the mouth level is the result of B-by-B changes in lung gas stores.  
257 Swanson proposed selecting  $V_{Li-1}$  as the lung volume that yields the lowest B-by-B variability in  
258 gas exchange (ref). He defined this volume as the ‘effective lung volume’, which represents the  
259 end-expiratory lung volume that ‘effectively’ participates in alveolar gas exchange (a practical  
260 example of the ‘effective lung volume’ is shown in Figure 2C). Swanson’s approach yields a lower  
261 B-by-B  $VO_{2A}$  and  $VCO_{2A}$  variability compared to that of the A algorithm (5), which might be  
262 particularly useful for detecting time-based events in gas exchange (such as the gas exchange  
263 threshold). Nevertheless, this technique has some limitations. Since the effective lung volume can

264 only be calculated *a posteriori*, this method does not allow for real-time monitoring of gas  
265 exchange. Moreover, when applied to the rest-exercise transition, this technique assumes a  
266 deterministic variation of FRC as a function of time, which is a questionable assumption (2). In  
267 addition, B-by-B variability in gas exchange are a result of both physiologic events, such as  
268 rhythmic changes in pulmonary capillary blood flow with the breathing and cardiac cycles and the  
269 consequence of computational artifacts. di Prampero and Lafortuna (11) pointed out that it is  
270 difficult to distinguish between these effects, and stressed the notion that a valid alveolar gas  
271 exchange measure largely relies on the validity of  $V_{Li-1}$  assessment on a B-by-B basis (11).

272 Busso and Robbins (5) suggested yet another alternative, which is also based on minimizing  
273 B-by-B variability in gas exchange; data suggest that it provides the lowest B-by-B  $VO_{2A}$  and  
274  $VCO_{2A}$  variability (5). They proposed that  $V_{Li-1} = FRC$  and assumed that the ‘true’ change in  
275 alveolar end-expiratory gas fraction (i.e.,  $F_{AO_{2i}} - F_{AO_{2i-1}}$  and/or  $F_{ACO_{2i}} - F_{ACO_{2i-1}}$ ) lies between 0  
276 and the change in end-tidal gas fraction (i.e.,  $F_{ETO_{2i}} - F_{ETO_{2i-1}}$  and/or  $F_{ETCO_{2i}} - F_{ETCO_{2i-1}}$ );  
277 implying that the ‘true’ alveolar O<sub>2</sub> and CO<sub>2</sub> exchange is compromised within those obtained using  
278 Wessel’s and Auchincloss’s approach. Using a nine-compartment, non-homogeneous, tidally  
279 ventilated and constantly perfused lung model that reproduces a realistic breathing pattern, Busso  
280 and Robbins elegantly tested the validity of this method. Although appealing, this method presents  
281 similar limitations to that of Swanson – primarily that the requirements for *a posteriori* processing  
282 prevents real-time monitoring of gas exchange. A detailed review on different  $V_{Li-1}$ -based  
283 algorithms designed to estimate B-by-B alveolar gas exchange can be found elsewhere (1, 2).  
284 However a central tenet and limitation of these flow-based approaches is measurement of  $V_{Li-1}$   
285 that, as described above, is methodologically challenging and often unavailable.

286

287

\*FIGURE 2 NEAR HERE\*

288

289 Notably, the development of techniques based on optical reflectance motion analysis (i.e.,  
290 optoelectronic plethysmography, OEP) has enabled the accurate estimation of lung volumes at any  
291 point of the breathing cycle and, in turn, the determination of changes in  $V_{Li-1}$  for each breath (7,  
292 12, 30, 33, 34). However, when using OEP-based techniques, independent estimation of the vital  
293 capacity ( $VC$ ) and  $FRC$  is still required to estimate  $\dot{V}O_{2A}$  and  $\dot{V}CO_{2A}$  (7). Using this technique,  
294 Aliverti et al. (7) showed that  $V_{Li-1}$  changes between the onset and end of exercise, suggesting that  
295 the use of a constant value for  $V_{Li-1}$  would likely introduce an estimation error in the alveolar gas  
296 exchange computation. Despite its robustness, this technique is not free from limitations. For  
297 instance, the overall volume changes of the chest wall measured by OEP-based techniques can  
298 include blood volume shifts inside and outside of the thorax compartment, which could introduce an  
299 estimation error when assessing changes in  $V_{Li-1}$  (35, 36). This technique is certainly appealing;  
300 however, its application is demanding, time-consuming, and requires measures of  $VC$  and  $FRC$ ,  
301 which represent the primary limitation of this approach.

302

### 303 **Different definitions of the breathing cycle in the B-by-B gas exchange analysis**

304 To circumvent the issues related to measurements of  $V_{Li-1}$ , Grønlund (15) proposed a radically  
305 different solution; however, this requires the breathing cycle to be redefined. Rather than  
306 performing the integration of flow and gas fraction signals within the inspiration and expiration  
307 phases, it is performed between two successive expirations with equal  $F_{O_2}$  (or  $F_{CO_2}$ ) values,  
308 typically in the alveolar phase (Figure 3); the important point to note is that these equal  $F_{O_2}$  (or  
309  $F_{CO_2}$ ) values do not necessarily occur in consecutive breaths, or necessarily at a common time  
310 or lung volume during a subsequent breathing cycle (Figure 4, panel A). Thus, Grønlund defined a  
311 single breathing cycle as the time interval between two equal points of  $F_{O_2}$  (or  $F_{CO_2}$ ) on successive  
312 expirations, i.e.,  $F_{O_2}(t1) = F_{O_2}(t2)$ , where  $t1$  and  $t2$  are the time instants with two equal  $F_{O_2}$  values.  
313 By Grønlund's definition, the time interval between  $t1$  and  $t2$  represents the total time of a given

314 breathing cycle, where  $t1$  is the start and  $t2$  is the end of a cycle, which can be (and commonly is)  
 315 different from the time interval between the beginning of two consecutive inspiration phases (i.e.,  
 316 the conventional breathing cycle). Grønlund's astute solution makes the term  $(F_{AO_{2i}} - F_{AO_{2i-1}})$  of  
 317 Equation 11 equal to 0; thus,  $V_{Li-1}$  can be omitted from the computation. Therefore, according to  
 318 Grønlund's algorithm (hereinafter referred to as the G algorithm), the volume of  $O_2$  exchanged at  
 319 the alveolar level over breath  $i$  is reduced to:

320

$$321 \quad VO_{2iA} = \int_{t1_i}^{t2_i} (\dot{V}_{in} - \dot{V}_{ex}) \cdot F_{O_2} \cdot dt - \int_{t1_i}^{t3_i} (\dot{V}_{in} - \dot{V}_{ex}) \cdot F_{N_2} \cdot F_{O_2(t1_i)} \cdot (F_{N_2(t1_i)})^{-1} \cdot dt -$$

$$322 \quad \int_{t2_i}^{t3_i} \dot{V}_{ex} \cdot F_{O_2(t1_i)} \cdot dt \quad (14)$$

323

324 To note, only the variables marked with  $(t1)$  are constant values for the considered breath  $i$  (i.e.,  
 325  $F_{O_2(t1_i)}$  and  $(F_{N_2(t1_i)})^{-1}$ , the fraction of  $O_2$  and  $N_2$  at the time instant  $t1$ ), while the others change  
 326 over time (i.e.,  $\dot{V}_{in}$ ,  $\dot{V}_{ex}$ ,  $F_{O_2}$ ,  $F_{N_2}$ , which are variables varying over time). As originally pointed out  
 327 by Grønlund (15), Equation 14 is very similar to that proposed earlier by Beaver et al. 1981 (i.e.,  
 328 Equation A9 in (4)), with the substantial difference of how a single breathing cycle is identified.

329 According to Equation 7, Equation 14 can be rewritten as follows:

330

$$331 \quad VO_{2iA} = \int_{t1_i}^{t2_i} (\dot{V}_{in} - \dot{V}_{ex}) \cdot F_{O_2} \cdot dt - F_{O_2(t1_i)} \cdot \Delta V_{Li} \quad (15)$$

332

333 where,

334

335 
$$\Delta V_{Li} = \frac{\int_{t1_i}^{t3_i} (\dot{V}_{in} - \dot{V}_{ex}) \cdot F_{N_2} \cdot dt}{F_{N_2(t1_i)}} - \int_{t2_i}^{t3_i} \dot{V}_{ex} \cdot dt$$
 (16)

336

337 The second term on the right-hand side of Equation 15 accounts for the lung gas storage,  
 338 where  $\Delta V_{Li}$  can be determined from N<sub>2</sub> balance (Equation 16).  $F_{N_2(t1_i)}$  corresponds to the N<sub>2</sub> gas  
 339 fraction at  $t1$  and is used as a reference value for identifying  $F_{N_2}$  at  $t3$  ( $F_{N_2(t3_i)}$ ), such that  $F_{N_2(t1_i)} =$   
 340  $F_{N_2(t3_i)}$  (Figure 3). Therefore,  $t3$  is identified using the  $F_{N_2}$  signal, which satisfies the condition  
 341  $F_{N_2(t1_i)} = F_{N_2(t3_i)}$ . Thus, Equation 11 can be reduced to Equation 16, which represents the changes  
 342 in the alveolar volume occurring over the  $i^{\text{th}}$  breath. If  $t3$  does not temporally coincide with  $t2$ ,  
 343 volume correction  $\int_{t2_i}^{t3_i} \dot{V}_E \cdot dt$  must be applied (Figures 3 and 6), a correction that assumes gas  
 344 exchange from  $t2_i$  to  $t3_i$  with a RER=1. Notably, straightforward modifications, which are not  
 345 described here for simplicity, makes it possible to obtain VCO<sub>2A</sub> (e.g., applying Eq 8, inverting the  
 346 subtraction of the inspired and expired volumes from  $(\dot{V}_I - \dot{V}_E)$  to  $(\dot{V}_E - \dot{V}_I)$  and considering the  
 347  $F_{CO_2}$  instead of the  $F_{O_2}$  trace).

348

\*FIGURE 3 NEAR HERE\*

350

351 Therefore, according to the G algorithm (15) the intra-breath interval time of breath  $i$  is  
 352 defined as the time interval between two points on successive expirations in which the lung O<sub>2</sub>  
 353 fractional concentration is the same, i.e.,  $F_{O_2(t1_i)} = F_{O_2(t2_i)}$  (Figure 3). Generally,  $t1$  is selected  
 354 within the second half of the first expiration after the dead space has fully expired (10, 37), where  
 355 the condition  $F_{O_2(t1_i)} = F_{O_2(t2_i)}$  is satisfied (Figures 3 and 4) (10, 37). Since the condition  
 356  $F_{O_2(t1_i)} = F_{O_2(t2_i)}$  can be met several times within breath  $i$ , and selecting different  $t1$ - $t2$  couples  
 357 may lead to different  $\dot{V}O_{2A}$  and  $\dot{V}CO_{2A}$  (15), it is also necessary to determine which  $t1$  and  $t2$



358 should be chosen. Capelli et al. (10) proposed a robust technique to identify  $t1-t2-t3$ , which enables  
359 the reliable measurement of  $\dot{V}O_{2A}$  (see Capelli et al. (10) for further details).

360 The condition  $F_{O_2(t1_i)} = F_{O_2(t2_i)}$  may not be satisfied between two consecutive breaths. In  
361 such cases, the subsequent expiration phase (i.e., following two standard breathing cycles after the  
362  $i$ th breath) can be used to satisfy the condition  $F_{O_2(t1_i)} = F_{O_2(t2_i)}$ , which results in integration over  
363 a longer time interval (Figure 4A) (10, 37). Although unlikely, a given reference value at  $t1$  may not  
364 be attained at  $t2$  over a long series of breaths, which would result in losing the breath considered  
365 (Figure 4B) (see Capelli et al. for further details) (10). This may occur during hyperventilation,  
366 where tachypnea increases the slope of the alveolar partial pressure of expired  $O_2$  (and  $CO_2$ ) (38)  
367 (see below for further details).

368

369

\*FIGURE 4 NEAR HERE\*

370

371 The use of the G algorithm presents some advantages over the use of other  $V_{Li-1}$ -dependent  
372 algorithms, especially when attempting to characterize the B-by-B alveolar gas exchange kinetics  
373 during the transition to or from different work rates. For instance, di Prampero and Lafortuna  
374 showed that the A algorithm is likely to be exposed to an estimation error of the duration of  $\dot{V}O_{2A}$   
375 Phase I during the rest-exercise transition, and the magnitude of this error is highly dependent on  
376 the accuracy of  $V_{Li-1}$  (11). They also showed that assuming  $V_{Li-1}$  equal to 0 (i.e., Wessel et al.'s  
377 approach) causes wide variability in the estimation of the duration of phase 1 compared with  
378 assuming  $V_{Li-1}$  equals FRC. This instability might be due to the failure of the assumption that  
379  $V_{Li-1} = 0$  to completely account for changes in lung gas stores (11). Moreover, by comparing the G  
380 and A algorithms at the onset of exercise in the moderate-intensity domain, Cautero et al.  
381 demonstrated that the time constant of phase 2  $\dot{V}O_{2A}$  kinetics ( $\tau_2$ ) obtained when using the A  
382 algorithm was systematically greater than that obtained with the G algorithm ( $34.3 \pm 9.18s$  vs.  $45.0$

383  $\pm 10.66s$ , respectively) (37). Notably, the authors found a positive correlation between  $\tau_2$  and  $V_{Li-1}$ ,  
384 suggesting that choosing greater  $V_{Li-1}$  values leads to a systematic increase in  $\dot{V}O_2 \tau_2$ . Indeed,  
385 increases in  $V_{Li-1}$  amplifies the contribution of  $F_{AO_2i} - F_{AO_2i-1}$  (see Equation 9) and  $F_{AN_2i} -$   
386  $F_{AN_2i-1}$  (see Equation 11) in the  $\dot{V}O_{2A}$  computation, which results in  $\dot{V}O_{2A}$  kinetic distortions (see  
387 Cautero et al. (37) and Capelli et al. (2) for further details). Therefore, the use of the G algorithm  
388 can help prevent distortions caused by inaccuracy in the estimation or measurement of  $V_{Li-1}$ .  
389 However, we note that the ‘true’ alveolar  $\dot{V}O_2$  (and  $\dot{V}CO_2$ ) kinetics are unknown. It may be possible  
390 to use simulations of gas flow traces with different kinetic features to elucidate which algorithm  
391 provides the most realistic response kinetic estimation (see below).

392 Cettolo and Francescato (16) recently proposed an alternative algorithm designed to measure  
393 alveolar gas exchange, which also circumvents the requirement to assess  $V_{Li-1}$  by redefining the  
394 breathing cycle. Rather than considering the intra-breath interval time using the condition  $F_{O_2}(t1_i) =$   
395  $F_{O_2}(t2_i)$ , the start and the end of each breath  $i$  are defined by satisfying the condition  $\frac{F_{O_2}(t1_i)}{F_{N_2}(t1_i)} =$   
396  $\frac{F_{O_2}(t2_i)}{F_{N_2}(t2_i)}$  (or  $\frac{F_{CO_2}(t1_i)}{F_{N_2}(t1_i)} = \frac{F_{CO_2}(t2_i)}{F_{N_2}(t2_i)}$ ), typically in the alveolar phase (Figure 5) (where  $t1$  and  $t2$   
397 conceptually have the same meaning as  $t1$  and  $t2$  in Equation 14; see below for further details).  
398 Similar to the G algorithm, this condition makes the term  $(F_{AO_2i} - F_{AO_2i-1})$  of Equation 11 equal  
399 0, allowing  $V_{Li-1}$  to be omitted from the computation. Thus, the breathing cycle can be defined as  
400 the time interval between two equal values of  $\frac{F_{O_2}}{F_{N_2}}$  (or  $\frac{F_{CO_2}}{F_{N_2}}$ ) on successive, but not necessarily  
401 consecutive, expiration phases.

402 Cettolo and Francescato (16) reorganized Equation 7, which is essentially the method  
403 proposed by Auchincloss et al. (3).

404

405 
$$VO_{2iA} = VO_{2iM} - \frac{F_{AO_{2i}}}{F_{AN_{2i}}} \cdot VN_{2iM} + V_{Li-1} \cdot \left( \frac{F_{AO_{2i-1}} \cdot F_{AN_{2i}} - F_{AO_{2i}} \cdot F_{AN_{2i-1}}}{F_{AN_{2i}}} \right) \quad (17)$$

406

407 Considering the condition  $\frac{F_{O_2(t1_i)}}{F_{N_2(t1_i)}} = \frac{F_{O_2(t2_i)}}{F_{N_2(t2_i)}}$ , Equation 17 reduces to

408

409 
$$VO_{2iA} = \int_{t1_i}^{t2_i} (\dot{V}_I - \dot{V}_E) \cdot F_{O_2} \cdot dt - \frac{F_{O_2(t1_i)}}{F_{N_2(t1_i)}} \cdot \int_{t1_i}^{t2_i} (\dot{V}_I - \dot{V}_E) \cdot F_{N_2} \cdot dt \quad (18)$$

410

411 Equation 18 is a simplified version of Equation 15; straightforward modifications, which will  
 412 not be described here, make it possible to also obtain alveolar CO<sub>2</sub> exchange. Notably, although *t1*  
 413 and *t2* in Equation 18 have the same conceptual meanings as *t1* and *t2* in Equations 14 and 15, they  
 414 are defined differently (i.e.,  $\frac{F_{O_2(t1_i)}}{F_{N_2(t1_i)}} = \frac{F_{O_2(t2_i)}}{F_{N_2(t2_i)}}$ ) (16) (Figures 3 and 5).

415

416 \*FIGURE 5 NEAR HERE\*

417

418 Equation 18 presents several advantages from a computational perspective. For instance, the  
 419 Cettolo and Francescato algorithm (hereinafter referred to as the CF algorithm) does not require the  
 420 definition of *t3*, which must be determined when using the G algorithm (Figure 5). Moreover,  
 421 identifying the breathing cycle using the  $FO_2/FN_2$  and  $FCO_2/FN_2$  ratio traces may help identify  
 422 outlier breaths. The  $FN_2$  trace generally shows greater noise and signal distortion compared to the  
 423  $FO_2/FN_2$  and  $FCO_2/FN_2$  ratio traces, which may affect the identification of *t1-t2-t3* (not present in  
 424 the CF algorithm). Furthermore, the  $FO_2/FN_2$  and  $FCO_2/FN_2$  ratio traces have signal amplitudes  
 425 that are greater than that of  $FN_2$  alone, which may reduce variability associated with trace detection

426 in real time (16, 39). Nevertheless, the advantage of using  $FO_2/FN_2$  and/or  $FCO_2/FN_2$  ratio traces,  
427 instead of  $FO_2$  and  $FN_2$  and/or  $FCO_2$  and  $FN_2$ , have yet to be determined by independent research  
428 groups under different exercise conditions and/or using different modalities (see below).

429 There are also limited data directly comparing the G and CF algorithms; thus, whether one  
430 algorithm can outperform the other is unclear. Some data suggest no differences in the alveolar B-  
431 by-B gas exchange estimation between the two algorithms; however, the comparison was  
432 performed over a limited range of  $\dot{V}O_2$ ,  $\dot{V}CO_2$ , and ventilatory rates (16). Notably, the CF algorithm  
433 was only recently introduced; hence, there are limited data showing its validity in assessing B-by-B  
434 alveolar gas exchange compared to the G algorithm (16, 39–42). Therefore, further investigations  
435 are warranted, to better understand whether substantial differences exist between these algorithms,  
436 and which more accurately measures the true physiologic response.

437

#### 438 **Limitations, methodological considerations, and future directions**

439 Employing the G or CF algorithms has the undoubted advantage of removing the need to  
440 measure  $V_{Li-1}$ , which is appealing from a practical perspective. However, redefining the breathing  
441 cycle for the B-by-B gas exchange analysis may present some limitations. First, as previously  
442 highlighted (1, 43), these techniques would benefit from validation conducted by independent  
443 research groups under different conditions. For instance, it would be of great interest to test these  
444 algorithms together, under different environmental conditions (e.g., hypoxia, hyperoxia), exercise  
445 modalities (e.g., running, cycling, walking), with different populations (e.g., patients with  
446 cardiovascular and lung diseases and athletes), body positions (e.g., supine and upright posture) or  
447 work rate protocols (e.g., square-wave, sinusoidal-wave, ramp- and step-incremental tests).  
448 Specifically, comparisons made under conditions where lung volumes, lung gas stores and/or  
449 ventilation-perfusion relationships are expected to vary would help to identify the algorithm that  
450 best characterizes the true physiologic response.

451 Second, Whipp et al. (43) pointed out that Grønlund's approach may provide a different  
452 breath duration under specific conditions, such as during the transition from rest to exercise,  
453 compared with that of the conventional flow-based approach. Since the slope of the alveolar partial  
454 pressure of expired  $O_2$  (and  $CO_2$ ) increase at the onset of exercise and during continued exercise  
455 (38), a particular intra-breath  $F_{O_2}$  reference value at  $t1$  might be reached earlier during the  
456 expiration phase at  $t2$ , which in turn would result in a shorter estimated breath duration, and  
457 differentially alter the durations of inspiratory and/or expiratory time (such as in  $t_I/t_E$  or  $t_I/t_{TOT}$ ), than  
458 with the conventional approach (43). The same concern applies to the CF algorithm (16), although  
459 specific aspects of this algorithm may help mitigate this concern (see below) (39, 41). However, no  
460 study has investigated the potential differences in breath duration among different algorithms;  
461 therefore, further investigations are required.

462 Whipp et al. (43) also stated that during acute hyperventilation, due to the large increment of  
463 the entire  $F_{AO_2}$  (or fall in  $F_{ACO_2}$ ), a given intra-breath  $F_{O_2}$  reference value at  $t1$  (or  $F_{CO_2}$ ) may not  
464 match any  $F_{O_2}$  (or  $F_{CO_2}$ ) value at  $t2$  in the expired phase, resulting in the potential loss of breath  
465 detection using the G algorithm (Figure 4B). This may negatively affect the analysis of gas  
466 exchange kinetics during the transition phases. Modifications in the CF algorithms may help reduce  
467 the influence of large changes in  $F_{O_2}/F_{N_2}$  (or  $F_{CO_2}/F_{N_2}$ ) on the identification of the breathing cycle  
468 (39, 41). Cettolo and Francescato have recently implemented a technique in which each breathing  
469 cycle is identified without considering the end timepoint of the preceding cycle and the start  
470 timepoint of the following one (i.e., the so-called "independent breath" algorithm) (39, 41).  
471 Therefore, each breathing cycle has its own  $t1$  and  $t2$ , where  $t1$  of the breath  $i+1$  does not  
472 necessarily correspond to  $t2$  of the breath  $i$  (i.e., non-contiguity in time of the breathing cycles,  
473 Figure 4C). This would increase the possibility of identifying the breathing cycle during outlying  
474 breaths (e.g., atypically large or small breaths such as a sigh or a pant) and reduce the negative  
475 effects of hyperventilation on the identification of the breathing cycle and gas exchange estimation

476 (39, 41). Although some promising findings have already been reported (39–42), utilization of this  
477 approach would benefit from further validation by independent research groups under different  
478 exercise conditions. Moreover, the impact of hyperventilation on gas exchange kinetics estimation  
479 when using the G algorithm remains to be systematically determined.

480       Concerns have been raised regarding how ventilatory-based variables are computed using the  
481 G and CF algorithms (1). Information is lacking regarding the inspired and expired volumes, which  
482 are needed to estimate other important variables such as  $\dot{V}_E$ ,  $\dot{V}_I$ , the ventilatory equivalents for O<sub>2</sub>  
483 and CO<sub>2</sub> (i.e.,  $\dot{V}_E/\dot{V}O_2$  and  $\dot{V}_E/\dot{V}CO_2$ , respectively), and inspiratory and expiratory time. However,  
484 it is worth noting that several (if not all) ventilatory-based variables can be determined using these  
485 approaches. The intra-breath integration of the positive flow signal values between  $t1$  and  $t2$  can  
486 provide the expired volume (i.e.,  $V_{ex}$ ), which can be used to derive other variables (such as  $\dot{V}_E$  and  
487  $V_T$ ) (Figure 6). Likewise, the intra-breath integration of negative values can provide the inspired  
488 volume (i.e.,  $V_{in}$ ), which in turn would enable the estimation of  $\dot{V}_I$  (Figure 6). This procedure would  
489 also theoretically enable the estimation of  $B_R$ , where  $T_{TOT}$  corresponds to the time period elapsing  
490 between  $t1$  and  $t2$  (Figure 6). Inspiratory and expiratory times are also computable in the G and CF  
491 algorithms, although their physiological meaning is questionable, as they do not refer to the start  
492 and end of a conventional inspiration and expiration phase, which are commonly used to gain  
493 insights into the mechanisms involved in the control of the transition phase between inspiration and  
494 expiration, or vice-versa (27, 44, 45). However, although these ventilatory-based variables are  
495 computable using the G and CF algorithms, they have not been reported in published works. It is  
496 currently unclear whether these algorithms would provide a reasonable estimation of ventilatory-  
497 based variables. Evaluation of variability and irregularity of ventilatory-based variables during  
498 CPET has the potential to detect underlying breathing pattern disorders (46, 47). For instance,  
499 Bansal et al. (48) showed that a  $\dot{V}_E$  approximate entropy (i.e., a measure of  $\dot{V}_E$  variability)  $> 0.88$   
500 conferred sensitivity and specificity to detect breathing pattern disorder of 70% and 80%,

501 respectively. Whether this ventilatory-based information, computed using  $V_{Li-1}$ -independent  
502 algorithms, provide the same valuable information is currently unknown. Further study is  
503 recommended to demonstrate that *all* cardiopulmonary exercise testing (CPET) variables can be  
504 precisely and accurately derived.

505

506

\*FIGURE 6 NEAR HERE\*

507

508 Similarly, quantitative analysis of ventilatory and gas exchange kinetics during exercise is  
509 commonly used to understand underlying metabolic and ventilatory control mechanisms (43, 49)  
510 and are modified in patients with chronic disease (50, 51). This is particularly true for the  
511 investigation of the control mechanisms of  $\dot{V}_E$ , where analysis of  $\dot{V}_E$  and  $\dot{V}CO_{2A}$  kinetics can  
512 provide important physiological information (52–56).

513 Analysis of other ventilatory-based variables can also provide useful information for athletes  
514 and populations with chronic disease (56–58). For instance,  $\dot{V}_E/\dot{V}O_2$  and  $\dot{V}_E/\dot{V}CO_2$  responses can be  
515 used to non-invasively identify the gas exchange threshold (59, 60) and for diagnostic and  
516 prognostic stratification (57, 61). Therefore, identifying the most appropriate and reliable way to  
517 quantify ventilatory-based variables is of paramount importance.

518 The impact of lung gas store changes on B-by-B alveolar  $O_2$  and  $CO_2$  exchange rates during  
519 progressive exercise (i.e., step-wise or ramp-incremental work-rate protocols) has received less  
520 attention compared to the responses occurring during square-wave work-rate protocols (reviewed in  
521 (2)). Since progressive exercise is commonly used in research and clinical evaluation, it is of  
522 paramount importance to understand whether the dynamic changes in the alveolar gas stores affect  
523 the B-by-B gas exchange and their derived variables (such as gas exchange threshold and the  
524 ventilatory equivalent for  $O_2$  and  $CO_2$ ). Indeed, the use of  $\dot{V}O_{2A}$  and  $\dot{V}CO_{2A}$  instead of  $\dot{V}O_{2M}$  and  
525  $\dot{V}CO_{2M}$  was shown to increase the B-by-B signal-to-noise ratio and reduce B-by-B variability (4, 7,

526 10–12), thereby potentially improving discrimination of time-based events in gas exchange.  
527 However, there are no studies exploring the effect of using different algorithms on threshold  
528 detection.

529 Mathematical simulations and mechanical gas exchange simulation systems may be used to  
530 assess the validity of different alveolar corrections on the measurements of gas exchange and  
531 kinetics. As previously mentioned, the ‘real’ alveolar gas exchange kinetics is unknown. Although  
532 speculative, simulating gas flow traces with different known kinetics could potentially help to  
533 compare different algorithms to identify the algorithm that provides the most accurate kinetic  
534 estimates. On the other hand, the use of mechanical gas exchange simulation systems could be  
535 employed to assess the validity of alveolar gas exchange measures during steady-state conditions  
536 and in the presence of an aberrant single breath (42). The application of these techniques seems  
537 feasible (5, 42, 62), but the paucity of studies using these approaches means that further  
538 investigation is needed.

539 Since  $\dot{V}O_{2A}$  and  $\dot{V}CO_{2A}$  can be obtained using different reference values at  $t1$ ,  $t2$  or  $t3$   
540 (depending on the algorithm used – G or CF), a given breathing cycle obtained for  $\dot{V}O_{2A}$  is not  
541 temporally aligned with that for  $\dot{V}CO_{2A}$ . Moreover,  $T_I$ ,  $T_E$  and  $T_{TOT}$  may not necessarily have the  
542 same durations when computed by these difference algorithms. Therefore, a temporal misalignment  
543 on a B-by-B basis between  $\dot{V}O_{2A}$  and  $\dot{V}CO_{2A}$ , although small, can occur. This issue can be partially  
544 overcome by interpolation and extrapolation. Second-by-second interpolation and extrapolation  
545 (rather than B-by-B) of data are commonly used in post-processing when investigating gas  
546 exchange kinetics of actual (52, 63, 64) and simulated data (53, 65). Although, again, the  
547 implications for altering the standard reporting format for research and clinical gas exchange and  
548 ventilatory variables has yet to be determined. Moreover, interpolation/extrapolation techniques  
549 might alter the data, especially during the rest-exercise transition period, potentially affecting the  
550 physiological interpretation.



551           Until recently, G and CF algorithms have typically only been applied to raw gas flow and gas  
552 concentration recordings post-processing. That is, they have not been used to provide a real-time B-  
553 by-B measure of gas exchange. However, the use of the CF algorithm in real-time data analysis is  
554 feasible (39). The CF algorithm can identify  $t1$  and  $t2$  within every single breath in real time as data  
555 are collected (39). Thus, similar to what occurs during the classical real-time analysis of gas  
556 exchange, the integration of flow and gas fractions can be performed independently in a single  
557 breath (the so-called “independent breath”), allowing real-time data visualization (39, 41). Although  
558 not yet tested, this modification could theoretically be implemented in the G algorithm. Further  
559 studies are required to identify the most efficient technical solution to implement these algorithms  
560 in automated real-time B-by-B systems.

561

#### 562 **A call to action**

563 Data show the clear advantages of using  $\dot{V}O_{2A}/\dot{V}CO_{2A}$  instead of  $\dot{V}O_{2M}/\dot{V}CO_{2M}$  in B-by-B gas  
564 exchange analysis. However, the requirement for substantial validation work that confirms the  
565 advantage of  $V_{Li-1}$ -independent algorithms to determine not only alveolar gas exchange, but also  
566 ventilatory-based variables, is prohibitive to making use of these routines. For example, it is still  
567 unclear which alveolar correction better reflects alveolar-to-capillary gas exchange, especially  
568 under the diverse range of conditions commonly observed in research and clinical CPET  
569 laboratories. In addition, the lack of open access to these algorithms for routine application is a key  
570 barrier limiting the use of alveolar corrections. We are unaware of any automated commercial  
571 system that has implemented an algorithm to measure B-by-B alveolar gas exchange. This is despite  
572 literature that shows the advantages of using  $\dot{V}O_{2A}/\dot{V}CO_{2A}$  instead of  $\dot{V}O_{2M}/\dot{V}CO_{2M}$  increases  
573 signal-to-noise and reduces distortions in gas exchange responses during exercise. Therefore, given:  
574 (i) the introduction of the algorithm by Auchincloss et al. in 1966 (3); (ii) the development of  
575 several solutions aimed at optimizing the estimation of alveolar gas exchange (2, 41); and (iii) the

576 large number of studies showing the importance of differentiating between  $\dot{V}O_{2M}/\dot{V}CO_{2M}$  and  $\dot{V}O_{2A}$   
577  $/\dot{V}CO_{2A}$  (2, 4–6, 10, 16, 30, 37, 40, 41, 66); it is surprising that manufacturers have not progressed  
578 past conventional B-by-B algorithms and developed commercial systems that provide alveolar gas  
579 exchange analysis alongside standard measurements. This would not only increase signal-to-noise  
580 to provide improved characterization of clinically-important variables from an exercise test, but  
581 would also enable implementation of the most suitable algorithm for a given purpose, satisfying a  
582 wide range of different needs in health and chronic disease. Incorporating different algorithms into  
583 commercial systems would advance the reach of these techniques and facilitate the progression of  
584 our knowledge on their validity and applicability under different exercise conditions.

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## 586 **Perspectives and Significance**

587 Although fundamental concerns have been raised in using alternative algorithms that change the  
588 definition of the breathing cycle, their benefit for increasing accuracy and precision of alveolar gas  
589 exchange measurement is appealing and promising. Nevertheless, the paucity of data describing the  
590 physiologic meaning of several ventilatory-based variables when using these alternative algorithms  
591 requires further investigation. In addition, further validation studies are required to assess these  
592 methods and their implementation in real-time for online analysis. This is essential to understand  
593 which algorithm best characterizes the ‘true’ physiological response in both clinical and research  
594 settings.

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608 **Glossary**

BTSP	Body Temperature, ambient Pressure, and Saturated water vapor
CPET	Cardiopulmonary exercise testing
CO <sub>2</sub>	Carbon dioxide
$\dot{V}_E, \dot{V}_I$	Expired flow rate, inspired flow rate
$\dot{V}_{in}, \dot{V}_{ex}$	Flow rate during inspiration and expiration, respectively
$F_{AO_2}, F_{ACO_2}, F_{AN_2}, F_{AH_2O}$	Alveolar gas concentrations
$F_{EO_2}, F_{ECO_2}, F_{EN_2}, F_{EH_2O}$	Fractional gas concentration in expirate
$F_{ETO_2}, F_{ETCO_2}$	End-tidal gas fraction
$F_{IO_2}, F_{ICO_2}, F_{IN_2}, F_{IH_2O}$	Fractional gas concentration in inspirate
$F_{N_2}(t_3)$	Fractional N <sub>2</sub> concentration at the time instant $t_3$
$F_{O_2}(t_1), F_{CO_2}(t_1), F_{N_2}(t_1)$	Fractional gas concentration at the time instant $t_1$

$F_{O_2(t2)}, F_{CO_2(t2)}, F_{N_2(t2)}$	Fractional gas concentration at the time instant $t2$
$FRC$	Functional residual capacity
$N_2$	Nitrogen
$OEP$	Optoelectronic plethysmography
$O_2$	Oxygen
$RER$	Respiratory exchange ratio
$STPD$	Standard Temperature and barometric Pressure, Dry
$t_{TOT}, t_{in}, t_{ex}$	Time interval of a breath, inspiratory time interval, expiratory time interval
$VC$	Vital capacity
$\dot{V}_E/\dot{V}O_2, \dot{V}_E/\dot{V}CO_2$	Ventilatory equivalents for $O_2$ and $CO_2$ , respectively
$V_{in}, V_{ex}$	Inspired volume, expired volume
$V_{Li}$	end-expiratory lung volume of the $i^{th}$ breath
$V_{Li-1}$	end-expiratory lung volume of the preceding breath
$VO_{2A}, VCO_{2A}$	Alveolar-to-capillary gas exchange volume
$\dot{V}O_{2A}, \dot{V}CO_{2A}$	Alveolar-to-capillary gas exchange rate
$VO_{2M}, VCO_{2M}, VN_{2M}$	Pulmonary gas exchange volume
$\dot{V}O_{2M}, \dot{V}CO_{2M}$	Pulmonary gas exchange rate
$V_T, B_R$	Tidal volume, breathing rate
$\Delta V_{Li}$	Changes in lung volume during breath interval
$\Delta VO_{2S}, \Delta VCO_{2S}, \Delta VN_{2S}$	Changes in lung gas content during breath interval

$\tau_2$

Time constant of phase II gas kinetic

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617 **Acknowledgements**

618 The authors are very grateful to Professor Pietro Enrico di Prampero who critically read the  
619 manuscript and provided valuable comments and suggestions.

620 **Author contributions**

621 Conception or design of the work: M.G., C.G., W.W.S., H.B.R., R.C., C.F., and C.C.. Acquisition,  
622 analysis or interpretation of data for the work: M.G., C.G., W.W.S., H.B.R., R.C., C.F., and C.C..  
623 M.G. wrote the first draft of the manuscript. All the Authors revisited the work critically for  
624 important intellectual content. All authors approved the final version of the manuscript and agreed  
625 to be accountable for all aspects of the work in ensuring that questions related to the accuracy or  
626 integrity of any part of the work are appropriately investigated and resolved. All persons designated  
627 as authors qualify for authorship, and all those who qualify for authorship are listed.

628 **Funding**

629 Harry B. Rossiter is supported by grants from NIH (R01HL151452, R01HL153460, P50HD098593,  
630 R01DK122767) and the Tobacco Related Disease Research Program (T31IP1666).

### 631 **Competing interest**

632 Harry B. Rossiter reports consulting fees from Omnix Inc., and is involved in contracted clinical  
633 research with Boehringer Ingelheim, GlaxoSmithKline, Novartis, AstraZeneca, Astellas, United  
634 Therapeutics, Genentech and Regeneron. He is a visiting Professor at the University of Leeds, UK.

635 Richard Casaburi is involved in contracted research with United Therapeutics, Genentech, and  
636 Regeneron. He is an advisory board member for Inogen and Abbott and a speaker bureau member  
637 for GlaxoSmithKline. Carrie Ferguson is involved in contracted clinical research with United  
638 Therapeutics, Genentech, and Regeneron. She is a visiting Associate Professor at the University of  
639 Leeds, UK.

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821 **Figure captions**

822 **Figure 1.** Flow (panel A), partial pressure of oxygen (panel B) and partial pressure of carbon  
823 dioxide (panel C) during a series of breaths performed at a moderate exercise intensity in healthy-  
824 trained individual. The upper panel also depicts the zero-crossing points (open circle) identified  
825 using the MATLAB function “find\_cross.m” (26).

826 **Figure 2.** Single breath alveolar  $\dot{V}O_2$  (panel A) and  $\dot{V}CO_2$  (panel B) exchange as a function of  
827 ventilation computed on the same breath (continuous lines).  $\dot{V}O_{2M}/\dot{V}O_{2A}$  vs  $\dot{V}_I$  (panel A) and  
828  $\dot{V}CO_{2M}/\dot{V}CO_{2A}$  vs  $\dot{V}_E$  (panel B). Continuous lines (calculated on 100 breaths) depict differences  
829 from the expected value in alveolar gas exchange when using different  $V_{L,i-1}$  values (from 0 to 5 L)  
830 in Eqs 7 and 7. The dashed line depicts gas exchange at mouth ( $\dot{V}O_{2M}$  in panel A and  $\dot{V}CO_{2M}$  in  
831 panel B). Panel C shows the variability of alveolar  $\dot{V}O_2$  (open square) and  $\dot{V}CO_2$  (filled square)  
832 expressed as coefficient of variation (c.v., %), as a function of different  $V_{L,i-1}$  values. The  $V_{L,i-1}$  value

833 which gives the lowest computed  $\dot{V}O_{2A}$  and  $\dot{V}CO_{2A}$  variability is indicated by vertical arrows and  
834  $ELV_{\min}$  (effective lung volume; i.e.,  $ELV_{\min,O_2}$  and  $ELV_{\min,CO_2}$ , respectively). FRC (functional  
835 residual capacity) indicates when  $V_{L,i-1} = FRC$ . (Used and modified by permission; di Prampero and  
836 Lafortuna Breath-by-breath estimate of alveolar gas transfer variability in man at rest and during  
837 exercise. 1989. *J. Physiol.* 415, 459–475).

838 **Figure 3.** Partial pressure of  $O_2$  and  $N_2$  in mmHg ( $PO_2$  and  $PN_2$ , respectively) (top panel). The same  
839 data over a single respiratory cycle i.e., between the 5<sup>th</sup> and the 13<sup>th</sup> second (bottom panel).  $Exp_{i-1}$ ,  
840  $Insp_i$ , and  $Exp_i$  refer to the conventional expiration phase of the breath  $i-1$ , inspiration phase of the  
841 breath  $i$  and expiration phase breath  $i$ .  $t_d$  indicates the time after which the estimated dead space gas  
842 volume is fully expired. The reference value  $t1$  is chosen according to specific criteria (see text and  
843 Capelli et al. 2001 (10) for further details), while  $t2$  and  $t3$  are chosen to yield  $PO_2$  and  $PN_2$  equal to  
844  $t1$ , respectively. The respiratory cycle is defined as the time period elapsing between  $t1$  and  $t2$ .  
845 (Used by permission; Capelli C, Causero M, di Prampero PE. New perspectives in breath-by-breath  
846 determination of alveolar gas exchange in humans. *Pflugers Arch.* 2001;441(4):566–77.)

847 **Figure 4.** Panel A shows a particular case where a given  $F_{O_2}$  reference value at the time instant  $t1$   
848 does not meet any  $F_{O_2}$  value on the successive expiration to satisfy the condition  $F_{O_2(t1_i)} = F_{O_2(t2_i)}$ ,  
849 but during which a value equal to  $F_{O_2(t1_i)}$  is then met during the subsequent expiration. This results  
850 in an integration of gas and flow data over a longer time interval. The horizontal dotted line shows  
851 that the latest  $F_{O_2}$  value pertaining to the second expiration that coincides with the first  $F_{O_2}$  value  
852 would allow the identification of a respiratory cycle using the G algorithm. Panel B shows the effect  
853 of hyperventilation on  $FO_2$  ( $O_2$  fractional concentration in %) during three successive expirations.  
854 There are no  $F_{O_2}$  reference values at time instant  $t1$  that are met on two consecutive expirations,  
855 making the identification of a respiratory cycle using the G algorithm impossible. Panel C depicts  
856 the so-called “independent breath” algorithm, which allows the identification of two respiratory  
857 cycles ( $t1_i-t2_i$  and  $t1_{i+1}-t2_{i+1}$ ) during hyperventilation.  $FO_2/FN_2$  ratio (ratio of  $O_2$  and  $N_2$  fractions in

858 %). Here the summed duration of two successive breaths is larger than the summed duration of two  
859 conventional breaths defined by the beginning of two consecutive inspiration phases i.e.  
860 consecutive breaths overlap. See text for further details.

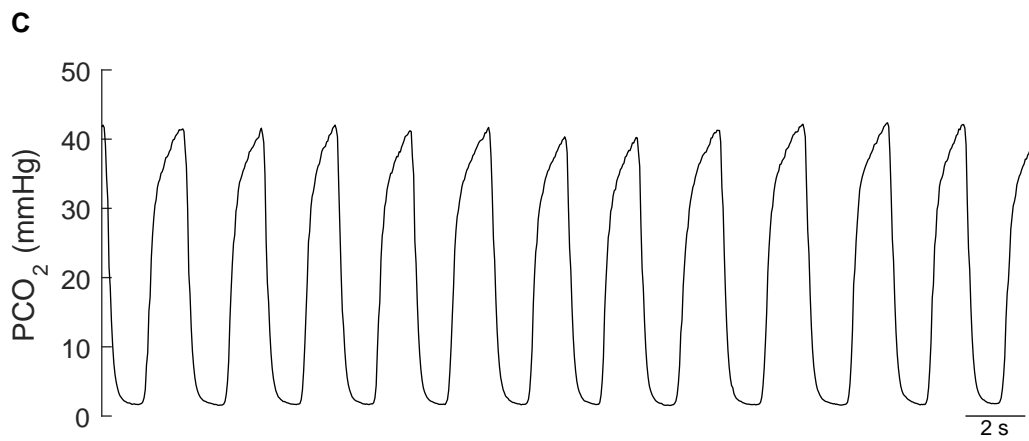
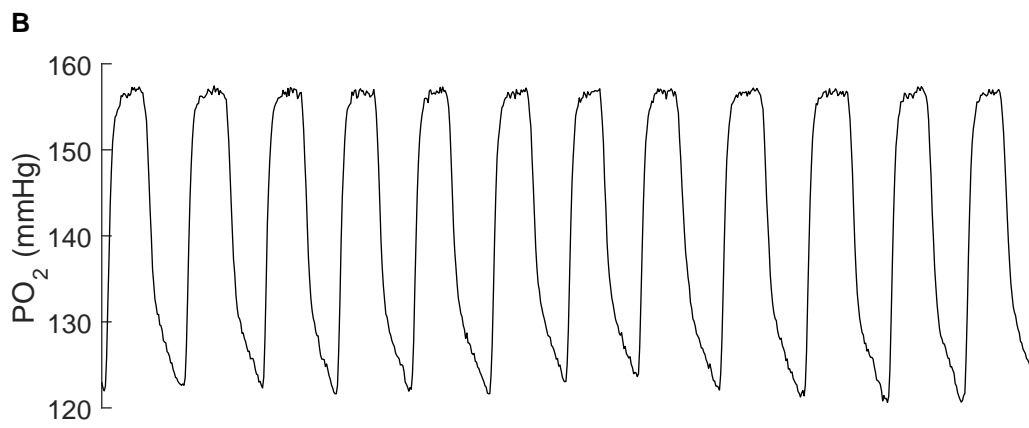
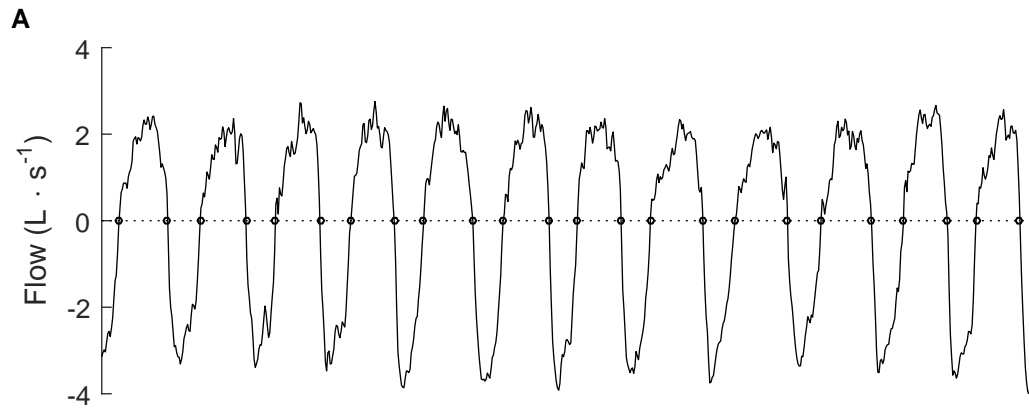
861 **Figure 5.** Comparison of Grønlund's and Cettolo & Francescato's algorithms. Upper and middle  
862 panels show the method introduced by Grønlund, which is also described in Figure 3. The bottom  
863 panel depicts the method introduced by Cettolo and Francescato (16). For the Cettolo and  
864 Francescato's method, the reference value  $t1$  is chosen accordingly to specific criteria (see text and  
865 Cettolo and Francescato, 2015 (16) for details), while  $t2$  is chosen to yield  $FO_2/FN_2$  equal to  $t1$ . The  
866 respiratory cycle is defined as the period time elapsing between  $t1$  and  $t2$ . (Used by permission;  
867 Cettolo V, Francescato MP. Assessment of breath-by-breath alveolar gas exchange: an alternative  
868 view of the respiratory cycle. *Eur J Appl Physiol.* 2015;115(9):1897–904.)

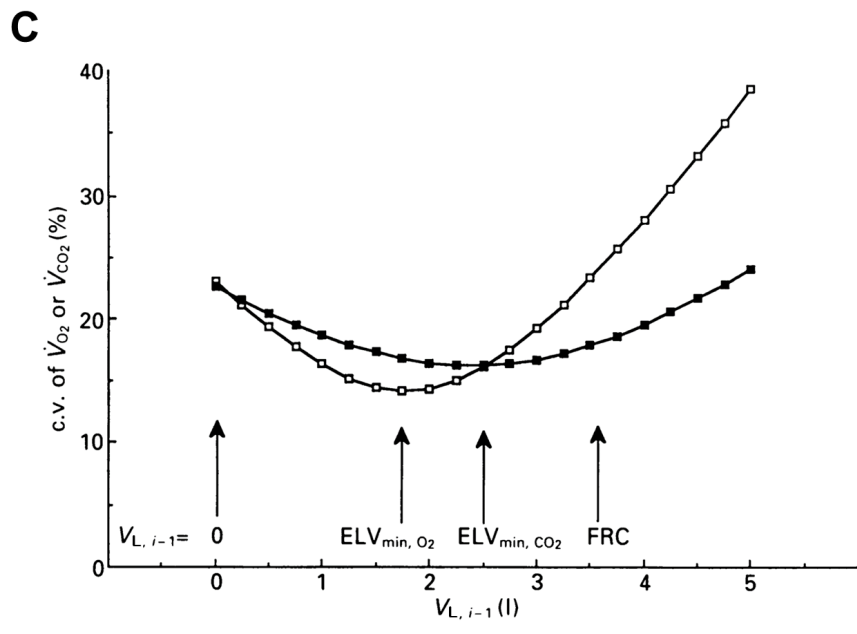
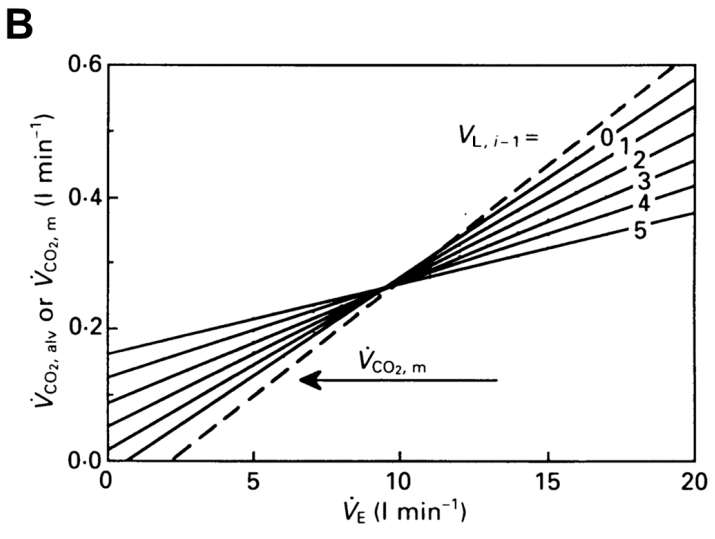
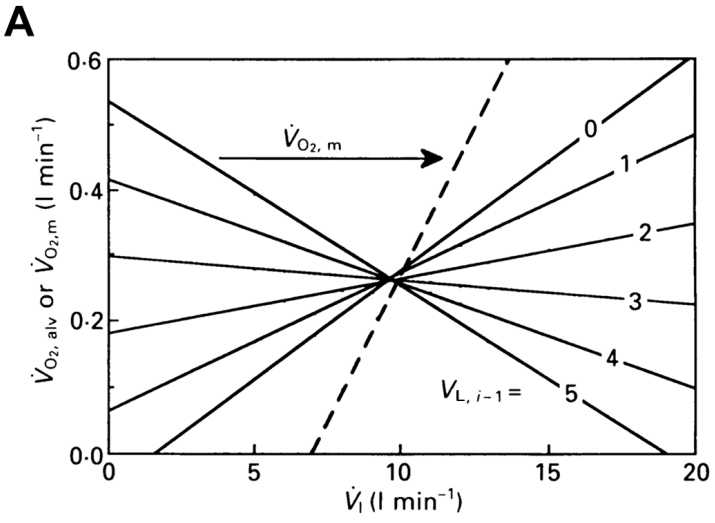
869 **Figure 6.** A single respiratory cycle identified using the Grønlund's algorithm, where  $t1$  and  $t2$   
870 represent the beginning and the end of one breath. The upper panel shows the gas flow at the mouth.  
871 The expiration occurs during positive deflections of the flow signal, while the inspiration occurs  
872 during negative deflections of the flow signal. The lower panel shows the fractional  $O_2$   
873 concentration. The soft dotted area represents the inspired gas volume, while the heavy dotted area  
874 corresponds to the expired gas volume. The thick line represents the gas flow occurring between  $t3$   
875 and  $t2$  (i.e., the volume correction for Equation 16). Some ventilatory-based variables estimated  
876 over  $t1$  and  $t2$  are as following:  $V_{ex}= 0.9$  L STPD ( $V_T= 1.2$  L BTPS),  $V_{in}=1.03$  L STPD,  $\dot{V}_E = 23$  L ·  
877  $\text{min}^{-1}$  STPD,  $\dot{V}_I= 24$  L ·  $\text{min}^{-1}$  STPD. The alveolar net transfer of oxygen uptake occurring over  $t1$   
878 and  $t2$  is equal to  $\dot{V}O_{2A} = 1.09$  L ·  $\text{min}^{-1}$  STPD. The time elapsing between  $t1$  and  $t2$  (i.e.,  $T_{TOT}$ ,  
879 which is the total time of the considered breath) is equal to 2.54 s. The corresponding breathing  
880 frequency is 24 breaths ·  $\text{min}^{-1}$ .

**Table 1.** General definition of breathing cycle (in the time domain) when using classic ( $V_{Li-1}$ -based algorithms), Grønland, and Cettolo and Francescato algorithms to estimate alveolar gas transfer.

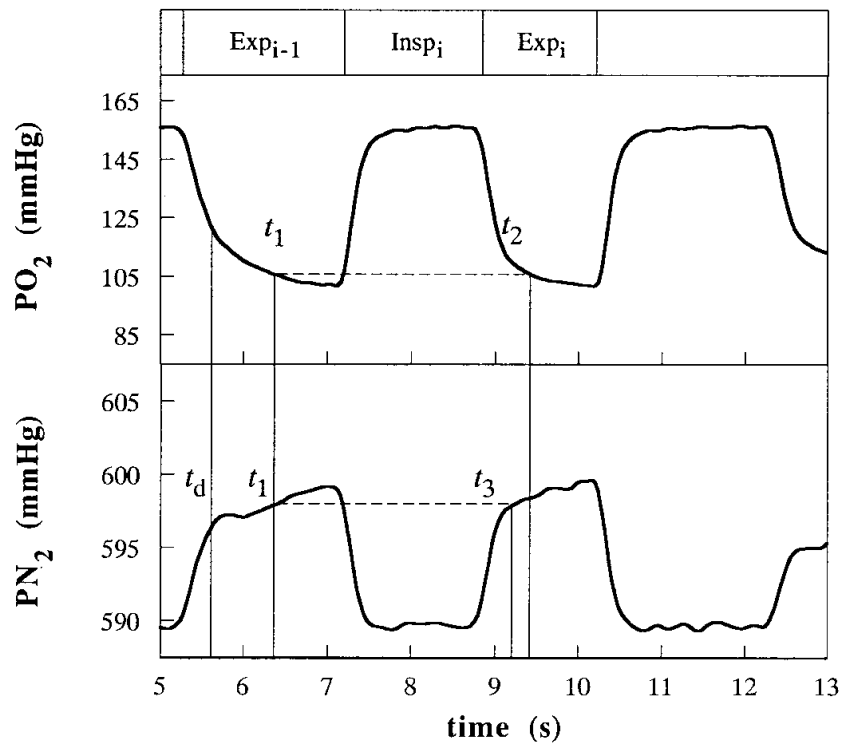
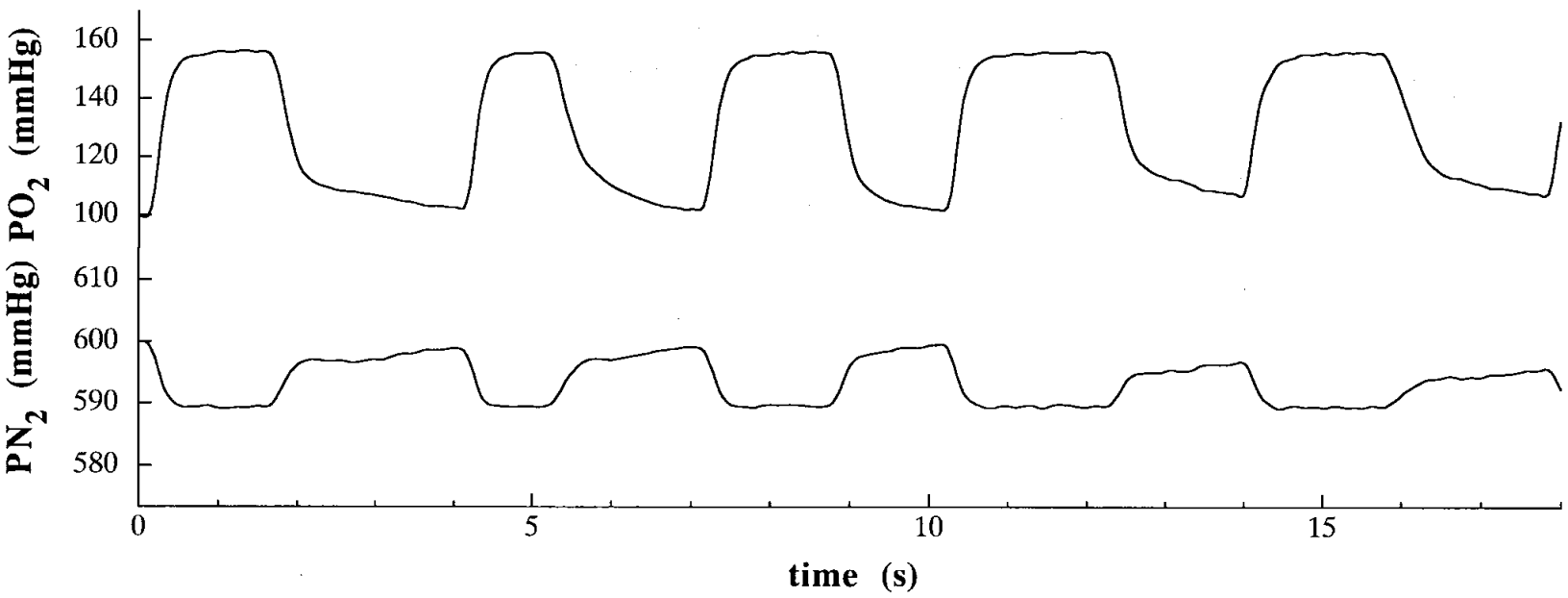
	Classic approach	G algorithm	CF algorithm
	$V_{Li-1}$ -based algorithms	$V_{Li-1}$ -independent algorithms	
Definition of breathing cycle (in time domain)	Time interval between the beginning of two consecutive inspiration phases	Time interval between two equal values of $FO_2$ (or $FCO_2$ ) on successive, but not necessarily consecutive, expiration phases, typically in the alveolar phase	Time interval between two equal values of $FO_2/FN_2$ (or $FCO_2/FN_2$ ) on successive, but not necessarily consecutive, expiration phases, typically in the alveolar phase
Signal(s) used to identify the breathing cycle	Flow signal	$FO_2$ , $FCO_2$ , and $FN_2$	$FO_2$ , $FCO_2$ , and $FN_2$
Variables required to obtain alveolar gas transfer	Flow signal, $FO_2$ , $FCO_2$ , $FN_2$ , and $V_{Li-1}$	Flow signal, $FO_2$ , $FCO_2$ , and $FN_2$	Flow signal, $FO_2$ , $FCO_2$ , and $FN_2$

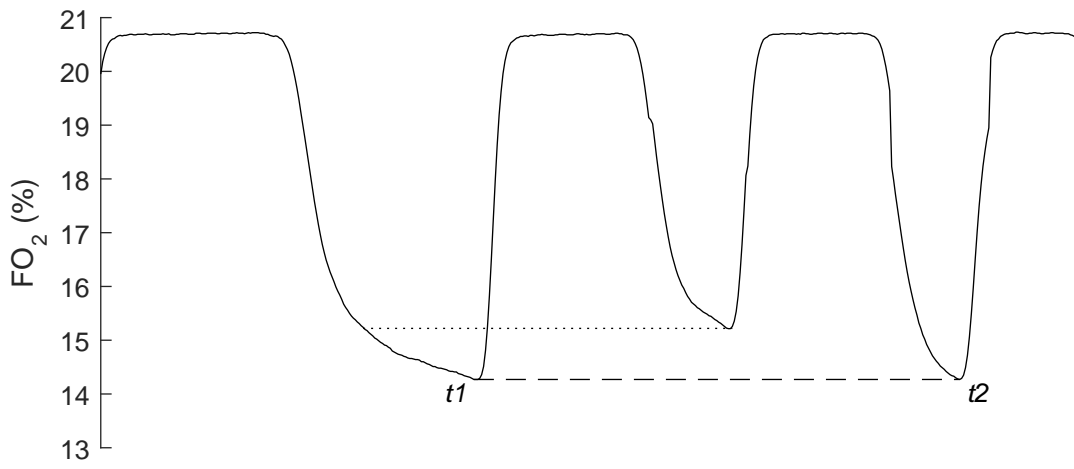
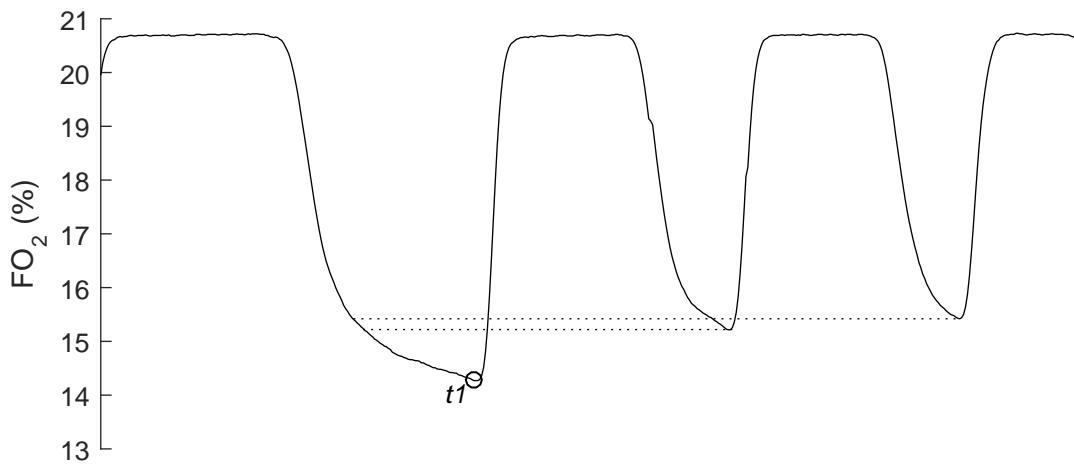
**Abbreviations:**  $V_{Li-1}$ , end-expiratory lung volume; G, Grønland algorithm; CF, Cettolo and Francescato algorithm;  $FO_2$ , oxygen fraction;  $FCO_2$ , carbon dioxide fraction;  $FN_2$ , nitrogen fraction.









**A****B****C**